Atmospheric
Measurement
Techniques

Field testing two flux footprint models

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Abstract. A field study was undertaken to investigate the accuracy of two micrometeorological flux footprint models for calculating the gas emission rate from a synthetic 10×10 m surface area source, based on the vertical flux of gas measured at fetches of 15 to 50 m downwind of the source. Calculations were made with an easy-to-use tool based on the Kormann–Meixner analytical model and with a more sophisticated Lagrangian stochastic dispersion model. A total of 59 testable 10 min observation periods were measured over 9 d. On average, both models underestimated the actual release rate by approximately 30 %, mostly due to large underestimates at the larger fetches. The accuracy of the model calculations had large period-to-period variability, and no statistical differences were observed between the two models in terms of overall accuracy.

1   Introduction

Micrometeorological techniques such as eddy covariance and flux–gradient methods measure a vertical flux of gas in the atmosphere, which can be used to deduce the flux from an underlying surface area of interest. If the underlying surface is expansive and horizontally homogenous, the measured atmospheric flux and the surface flux can be considered equivalent (Dyer, 1963). However, if the area of interest has a limited spatial extent or is located some distance from the atmospheric measurement, the relationship between the two fluxes can be complex, as the measured flux may be capturing a dynamic mixture of surface fluxes from both inside and outside the area of interest. In these cases, flux footprint modelling can be used to quantify the relationship between the measured atmospheric flux and the surface flux from the area of interest.

The analytical flux footprint model of Kormann and Meixner (2001), hereafter referred to as the KM model, is widely used to evaluate and interpret flux measurements taken over spatially limited surface sources. The KM model relies on a simplified representation of atmospheric transport (Schmid, 2002) to create an easily computable footprint. It has been used to help quantify ammonia fluxes from fertilized plots (Spirig et al., 2010), interpret methane fluxes from heterogeneous peatland areas (Budishchev et al., 2014), and to reject periods where the footprint extends outside the source of interest (Stevens et al., 2012). Other footprint models use a more realistic treatment of atmospheric transport (e.g., Kljun et al., 2002; Sogachev and Lloyd, 2004). Using a state-of-the-art Lagrangian stochastic (LS) footprint model, Wilson (2015) found a clear separation between the footprints computed with the LS and KM models, depending on atmospheric stability and the distance from the measurement location. While more rigorous footprint models are clearly more defensible, the simpler KM model has the advantage of rapid analysis and the existence of software tools that make its application more accessible to non-specialists (Neftel et al., 2008).

This field study compares the accuracy of the KM footprint model with a more rigorous LS model. The motivation for this study was the question of whether the accuracy of the LS model was sufficiently better than the KM model so as to justify a more complex LS application. In this experiment we released gas at a known rate from a small synthetic area source and measured the vertical gas flux at a downwind location using the eddy covariance technique. The KM and LS models were then used to calculate the source emission rate

from the measured atmospheric flux. The accuracy of those calculations is examined in this report. This follows the approach of Heidbach et al. (2017) and Coates et al. (2017) in their experimental evaluation of footprint models.

2 Methods

2.1 Gas release

The experiment took place on an extensive, flat agricultural field at the University of Alberta's Breton research farm, in Alberta, Canada ($53°07'$ N, $114°28'$ W). Measurements were made after autumn harvest, and the surface was rye (*Secale cereale* L.) stubble with an average height of 3 cm. No obstructions to the wind were present within 250 m of the measurement site.

A synthetic source of carbon dioxide (CO_2) gas was constructed using 10 lengths of 1/2 in. (12.7 mm) diameter PVC pipe, each 10 m long. The 10 pipes were loosely positioned to create a nominal 10×10 m square source area. Compressed CO_2 gas (99.9 % purity) passed through a mass flow controller (GFC57 configured for CO_2, Aalborg Instruments and Controls, Inc. Orangeburg, NY, USA) to a manifold (17 L) having outlets for each of the 10 pipes. Gas outlets of 1/64 in. (0.4 mm) diameter were placed every 50 cm along each pipe. We assumed equal flow rates from each outlet, which requires the gas outlets to be identical and the pressure loss across each outlet to be much greater than the pressure loss along the source piping (Flesch et al., 2004). We estimated pressure losses using simplified equations for pipe flow, assuming incompressibility and a re-entrant-type outlet shape (Fox and McDonald, 1985). For our most commonly used release rate of 90 L min^{-1}, the pressure loss across the outlets is approximately 5000 Pa, whereas the loss along a 10 m pipe section is only approximately 40 Pa.

The vertical CO_2 flux downwind of the synthetic source was measured using the eddy covariance (EC) technique. The instrumentation included a fast-response CO_2–H_2O analyzer (LI-7500DS, LI-COR Biosciences, Lincoln, NE, USA) and a sonic anemometer (CSAT3, Campbell Scientific, Logan, UT, USA) co-located at a height of 1.97 m above ground. The 10 Hz concentration and wind measurements were processed using the EddyPro® open-source software (version 6.2.1, LI-COR Biosciences, Lincoln, NE, USA) to obtain 10 min average fluxes of CO_2. The flux calculation applied a double coordinate wind rotation, Webb–Pearman–Leuning correction terms for density fluctuations (Webb et al., 1980), and spectral corrections for inadequate high- and low-frequency responses of the sensors (Moncrieff et al., 1997, 2004). Quality checks for steady-state conditions and integral turbulence characteristics were used to exclude error-prone periods (Foken and Wichura, 1996).

Gas releases took place over 9 d, with the center of the synthetic source positioned (Fig. 1) at one of three nomi-
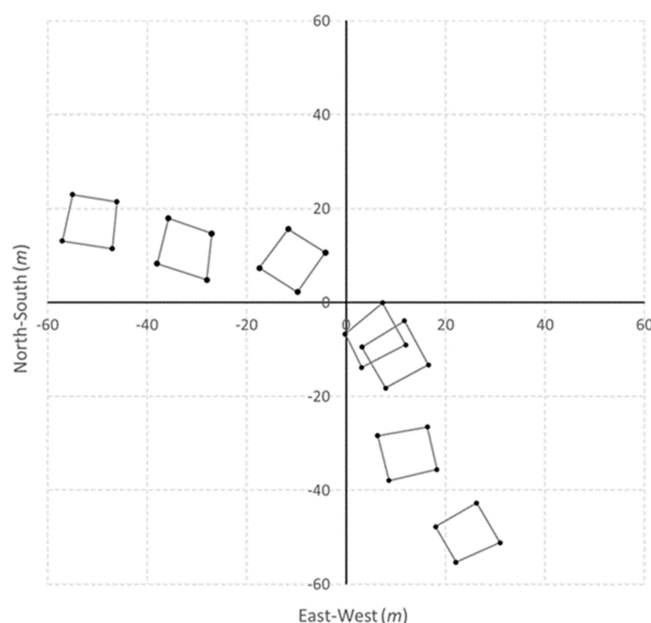

Figure 1. Map of the synthetic-source locations used in the study (polygons). The eddy covariance system was located at position (0,0).

nal distances from the EC system (fetches of 15, 30, and 50 m). Placement of the source relative to the EC system depended on the expected wind direction. Because CO_2 is naturally emitted from the landscape, it was important that the synthetic CO_2 release rate be sufficiently high so as to create a measured atmospheric flux that was many times larger than the natural landscape flux. Nicolini et al. (2017) found a CO_2 release rate of 22 L min^{-1} was sufficient to distinguish the release signal from background levels. Our situation was helped in that the experiment took place during the dormant autumn season when landscape CO_2 fluxes were small. Gas was released at rates between 30 and 90 L min^{-1}, with larger rates used for the larger fetches. Prior to any release interval and immediately after each hour of gas release, a 30 min period of background CO_2 flux was measured. These background fluxes (which were consistently small) were subtracted from the EC measured fluxes prior to undertaking the footprint analyses.

Our study consisted of more than 300 flux measurement periods of 10 min each and included periods of gas release, background flux measurements, and transitions when gas was released but a steady-state plume may not have been established over the field site (we assumed this occurred 10 min after gas was turned on). There was a total of 125 valid gas release periods. From this total we excluded 66 periods from our analysis based on two broad factors:

– 19 periods were excluded for having wind conditions associated with unreliability in the EC measurements or the dispersion model calculations, that is, light winds

with a friction velocity $u^* < 0.05\,\mathrm{m\,s^{-1}}$ or an inferred roughness length $z_0 > 0.25\,\mathrm{m}$. A low u^*-filtering criterion is often used in EC analyses (e.g., Rannik et al., 2004) and in dispersion model calculations (e.g., Flesch et al., 2014). The z_0-filtering criterion indicates an unrealistic wind profile given the bare soil conditions of our site and the likelihood of inaccurate dispersion model calculations given that wind profile.

- 47 periods were excluded when the EC measurement location was not obviously in the source plume. This included periods when the measured CO_2 flux was less than zero, when the wind direction deviated more than 30° from the line between the EC site and the source center, or when the LS footprint model (described below) indicated the plume may not have reached the EC measurement site (i.e., fewer than 1000 of 1 000 000 backward trajectories released from the EC site reached the source).

These quality control criteria eliminated over half of the gas release periods, leaving 59 periods for the footprint analysis. The final data are provided in the supplemental material accompanying this report.

2.2 Flux footprint models

2.2.1 Kormann–Meixner (KM) model

The KM model is based on an analytical solution to the steady-state advection–diffusion equation, assuming simplified power-law profiles for wind speed and eddy diffusivity and a crosswind diffusion component (Kormann and Meixner, 2001). We used the ART Footprint Tool software (Spirig et al., 2007) based on the KM model to calculate the synthetic-source emission rate (Q_{KM}, $\mathrm{g\,C\,m^{-2}\,s^{-1}}$) from the measured EC flux. The calculation uses the spatial outline of the source polygon, the EC measurement height (z_{EC}), the horizontal wind speed at height z_{EC}, the friction velocity (u_*), the standard deviation of the lateral wind velocity (σ_v), and the Obukhov length (L). The wind variables were measured with a 3-D sonic anemometer (part of the EC system). In this study, the ratio of the KM-calculated synthetic emission rate to the actual release rate (Q_{KM}/Q) is the metric for model testing. A perfectly accurate calculation gives $Q_{\mathrm{KM}}/Q = 1$.

2.2.2 Lagrangian stochastic (LS) model

A state-of-the-art LS model was also used to calculate the emission rate from the synthetic source (Q_{LS}, $\mathrm{g\,C\,m^{-2}\,s^{-1}}$) based on the measured EC flux. The relationship between the source emission rate and the EC flux was calculated from the trajectories of thousands of model "particles" travelling upwind from the EC measurement point (backward in time). We follow the calculation procedure outlined in Flesch

(1996) using the LS model detailed in Flesch et al. (2004). This model uses the wind velocity fluctuations in the three directional components (σ_u, σ_v, σ_w), the friction velocity (u_*), the Obukhov stability length (L), the average wind direction, and the surface roughness length (z_0). These properties were calculated from the 3-D sonic anemometer measurements. The LS calculations were made using 1 000 000 particles for each 10 min observation interval. A perfectly accurate LS model calculation gives $Q_{\mathrm{LS}}/Q = 1$.

2.3 Statistical analysis

The accuracies of the footprint calculations are evaluated from the ratio of the model-calculated emission rate to the actual release rate: Q_{KM}/Q and Q_{LS}/Q. These ratio data are asymmetrically distributed, and a logarithmic transform of the ratios is used when making our statistical comparisons. Thus, the geometric means of the emission ratios are our measure of central tendency. Confidence intervals for the geometric mean are calculated using the log-transformed ratio data and then converted back to ratio units (Limpert et al., 2001). The confidence intervals (CIs) are asymmetrical, and we report the upper and lower limits of the intervals.

3 Results and discussion

The synthetic emission rates calculated with both footprint models underestimate the actual emissions by roughly 30 % on average. The overall means of the footprint calculations, expressed as the ratio of the model-calculated emission rate to the actual emission rate, are $Q_{\mathrm{KM}}/Q = 0.67$ (95 % CI [0.50, 0.89]) and $Q_{\mathrm{LS}}/Q = 0.77$ (CI [0.60, 0.98]). These means are statistically less than 1.0 but not different from each other (paired t tests with $P > 0.05$). The period-to-period variability in the Q/Q ratios is large, with Q_{KM}/Q ranging between 0.04 and 2.20 and Q_{LS}/Q between 0.06 and 4.44. Some of the variability is likely due to the small size of the area source. The $10 \times 10\,\mathrm{m}$ source covers a small portion of the entire flux footprint. As opposed to larger source areas, the small area should amplify the differences between the models and increase the relative uncertainty in the footprint calculations (i.e., increasing the size of the source area means increasing the spatial integration of the footprint function in the calculations, which acts to increasingly constrain the Q/Q values closer to 1).

When examining the footprint agreements as a function of fetch (Fig. 2), we find both models are accurate at the shorter fetch of 15 m, as the means of Q_{KM}/Q and Q_{LS}/Q are not statistically different from 1. At the 15 m fetch the Q_{KM} calculation tends to slightly overestimate the actual emission rate with $Q_{\mathrm{KM}}/Q = 1.17$ (CI [1.00, 1.36]), while Q_{LS} tends to slightly underestimate it with $Q_{\mathrm{LS}}/Q = 0.84$ (CI [0.68, 1.04]). Based on the calculations of Wilson (2015) and Heidbach et al. (2017), we had hypothesized that there would be
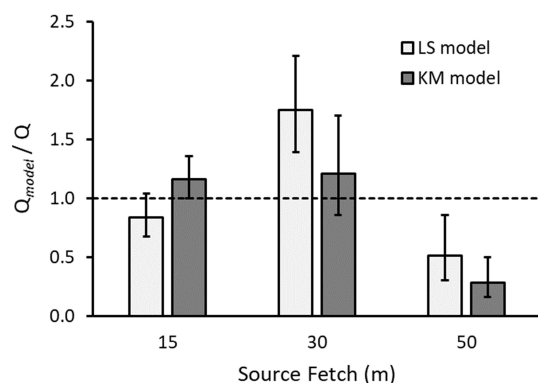
Figure 2. Agreement ratio of the footprint-model-calculated emission rate (Q_{model}) to actual release rate (Q), grouped by source fetch of $15\,m$ ($n = 26$), $30\,m$ ($n = 9$), and $50\,m$ ($n = 24$). Calculations are from the LS and KM models. The columns show the geometric mean, and the error bars show the 95 % confidence interval of the mean. The dashed horizontal line represents a Q_{model}/Q ratio of 1, or a perfect model calculation.

Figure 3. Agreement ratio of the footprint-model-calculated emission rate (Q_{model}) to actual release rate (Q), grouped by atmospheric stability: neutral ($|L| > 60\,m$), unstable ($0 > L > -60$), and stable ($60 > L > 0$). Calculations are from the LS and KM models. The columns show the geometric mean, and the error bars show the 95 % confidence interval of the mean. The dashed horizontal line represents a Q_{model}/Q ratio of 1, or a perfect model calculation.

substantial differences between the two models at the shorter fetch, with the LS model being more accurate than KM due to a better representation of horizontal turbulent transport, which is particularly important for defining the footprint at short fetches. However, this is not the case in this study. At the intermediate fetch of 30 m, the KM model slightly overestimates the emission rate with $Q_{KM}/Q = 1.21$ (CI [0.86, 1.71]), while the LS model substantially overestimates it with $Q_{LS}/Q = 1.75$ (CI [1.39, 2.21]). At the larger 50 m fetch, both models substantially underestimate the emission rate, with $Q_{KM}/Q = 0.29$ (CI [0.17, 0.51]) and $Q_{LS}/Q = 0.51$ (CI [0.30, 0.86]). The underestimate of Q_{KM}/Q at the larger fetch is similar to findings by Tallec et al. (2012) and Felber et al. (2015). At the 50 m fetch the measured EC fluxes were smaller than those measured at the shorter fetches, and in some cases the measured flux fell to a level near the background landscape flux (e.g., five periods had a measured flux that was less than 5 times the magnitude of the background flux). This was despite maximizing the gas release rate for the larger fetches. The result is that for the larger fetches there is increased measurement uncertainty (relative) in the flux signal from the gas release and increased uncertainty in Q_{KM} and Q_{LS}. Some of the relative uncertainty we see in Q/Q for the 50 m fetch is likely due to this factor.

In Fig. 3 we show the Q/Q ratios grouped according to atmospheric stability. The observations are separated into three groups having nearly equal numbers of observations: neutral ($|L| > 60\,m$), unstable ($0 > L > -60\,m$), and stable ($60 > L > 0\,m$). For the neutral and unstable groups, the mean Q/Q from both models does not statistically differ from 1, nor does it differ between groups due to the large variability in the calculations. However, in stable conditions both models are inaccurate and they substantially underestimate the actual emission rate. A more detailed look at the
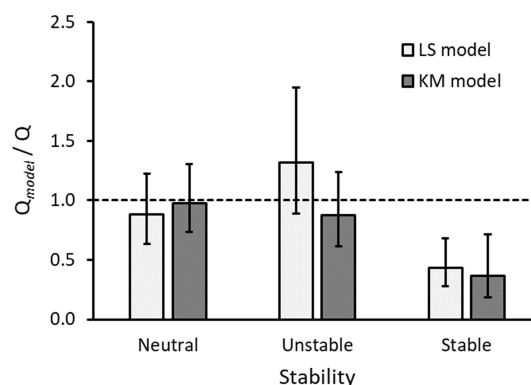
stable cases shows the Q_{KM}/Q calculations are particularly inaccurate for the 50 m fetch, with a mean of 0.14 (CI [0.03, 0.62]).

There are no clear patterns in terms of explaining the differences between the two footprint models based on environmental factors. Whether we separate the data by fetch or by stability, the results from the two models are not statistically different from each other. Wind speed, roughness length, and wind direction (deviation from a line between the EC system and the source) were also factors considered to explain the model differences, but again, no pattern was observed. The lack of model differences was unexpected given the studies of Göckede et al. (2005), Wilson (2015), and Heidbach et al. (2017) showing large differences in the calculations between analytical and LS models. This suggests that in our study, any systematic differences between the models were obscured by the substantial period-to-period variability in the Q/Q calculations and that the detection of model differences would require a much larger observational sample size than we were able to acquire.

4 Conclusions

From an end-user's perspective, our results show that both the KM and the LS model returned reasonably accurate flux footprint estimates on average, particularly for the shorter measurement fetches. Our dataset does not consistently discriminate between the performance of the two models, despite the theoretical advantages of the LS model. Based on the results of this study, we conclude that the easy-to-use KM model can provide accurate footprint calculations that are accessible to non-specialists.

It is clear that the KM and LS footprint models give systematically different results (as shown in Wilson, 2015), but we were unable to (statistically) observe these differences given the large period-to-period variability in the calculations and the relatively small number of field observations. The small area of our synthetic source likely contributed to the large variability, and a larger source may have allowed better differentiation between the models. However, period-to-period variability is the nature of footprint calculations based on simplified models of atmospheric transport like the KM and LS formulations. These model calculations, which at best approximate an ensemble average realization of the atmosphere, will not reflect the period-to-period fluctuations of actual measurement periods.

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