



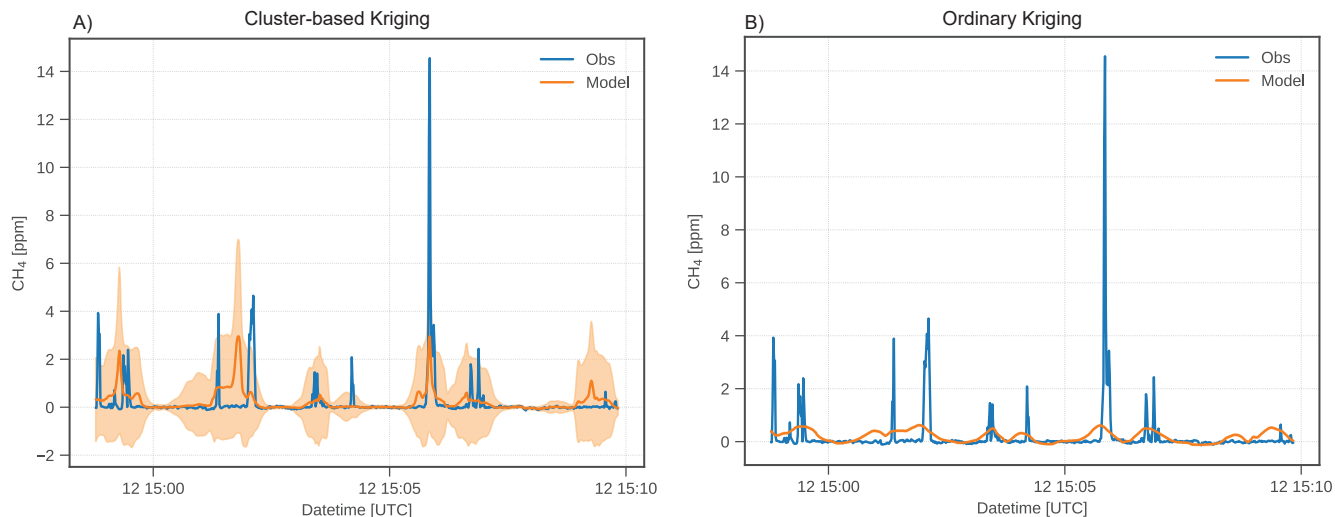
*Supplement of*

## **Controlled-release experiment to investigate uncertainties in UAV-based emission quantification for methane point sources**

**Randulph Morales et al.**

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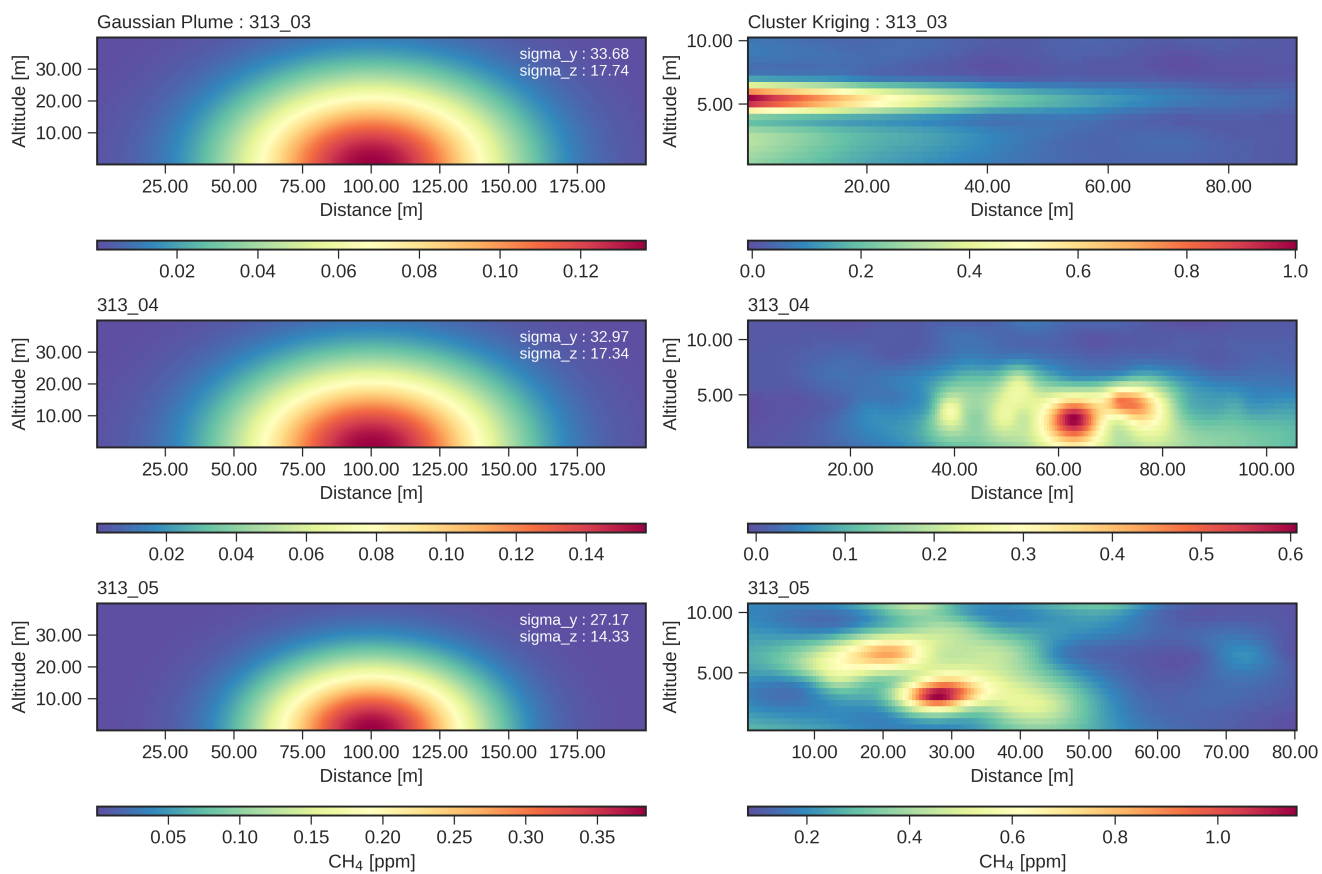


**Figure S1.** Reconstructed timeseries of flight 312\_03 extracted from the produced A) cluster-based kriging field and B) ordinary kriging field compared to the original timeseries of methane measurements. Orange shade areas indicate the uncertainty produced by kriging.

Fig. S7 illustrates the difference between the reconstructed emission plume for flight 312\_03 from QCLAS measurements using the cluster-based kriging vs. ordinary kriging. The figure on the upper left is the obtained emission plume using the cluster-based kriging. The figure on the middle left is the obtained emission plume using ordinary kriging. Figure on the upper right is the obtained background methane field and middle right is the methane field from the elevated cluster. To test whether the only difference between the cluster-based approach over ordinary kriging is the length-scale component alone, we forced our ordinary kriging approach to use length scales similar to that of the cluster-kriging approach. The resulting emission plume using ordinary kriging with length scales similar to the cluster approach are showed in the lower left plot in Fig. S7. This shows that the absence of membership probability of the background and elevated cluster in the ordinary kriging tends to produce noisier emission fields.

5 The noise in the emission field resulted to a 10 % decrease in emission estimate.

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**Figure S2.** Vertical cross-section from downwind distance of more than 100 m of methane molar fractions using a theoretical Gaussian dispersion model and cluster-kriging estimated prediction

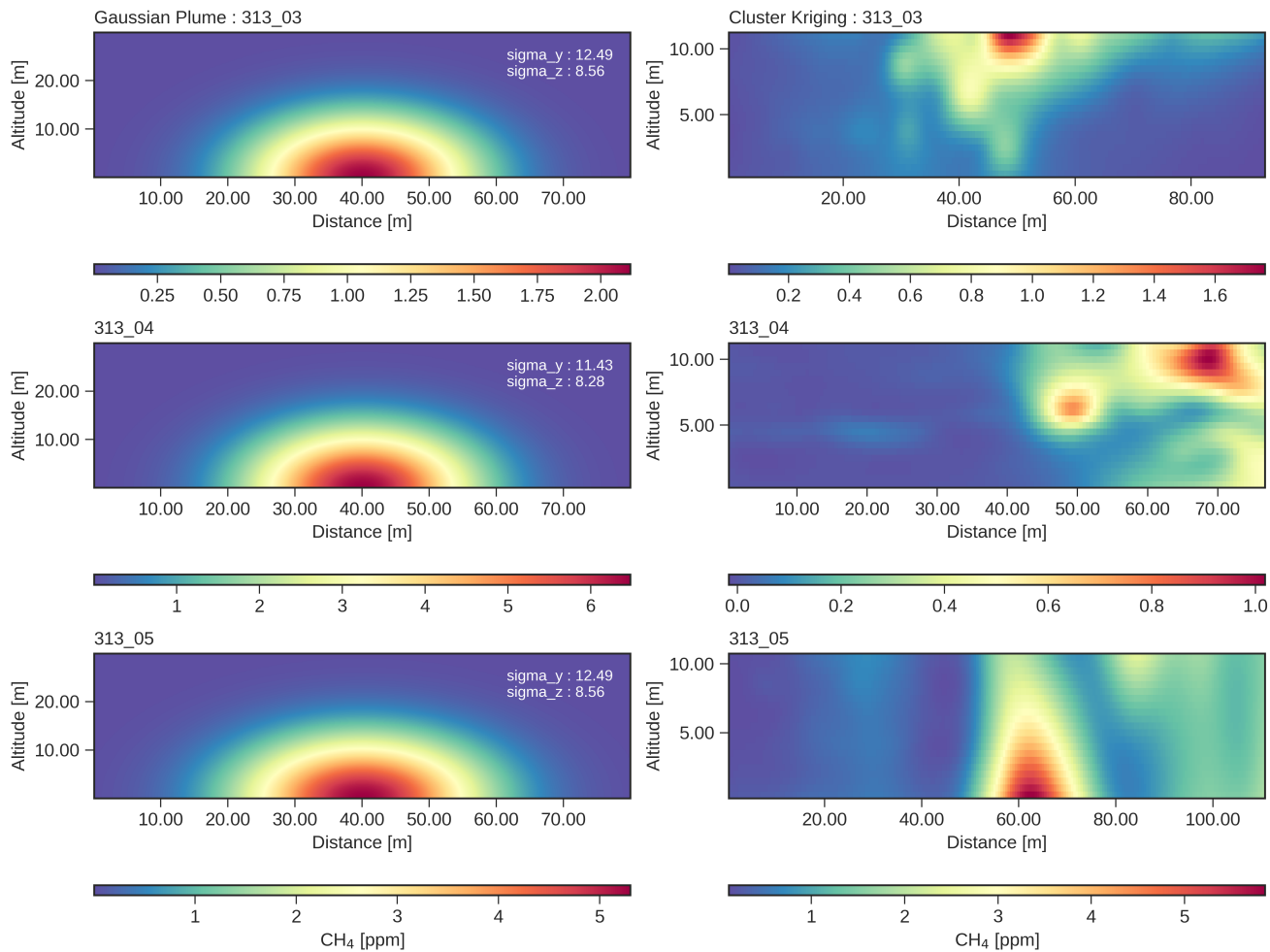
**Table S1.** Summary of emission estimates

| Date                               | Flight Code | Rel. rate [gs <sup>-1</sup> ] | Cluster Kriging |             |             | Ordinary Kriging |             |             |
|------------------------------------|-------------|-------------------------------|-----------------|-------------|-------------|------------------|-------------|-------------|
|                                    |             |                               | Proj. wind      | Sca. wind   | Log. wind   | Proj. wind       | Sca. wind   | Log. wind   |
| 23-Feb                             | 223_01*     | 0.48 ± 0.04                   | 0.64 ± 0.56     | 0.66 ± 0.41 | 0.56 ± 0.40 | 1.29 ± 0.98      | 1.26 ± 0.69 | 0.85 ± 0.70 |
| 24-Feb                             | 224_01      | 0.29 ± 0.03                   | 0.79 ± 0.66     | 0.76 ± 0.49 | 0.82 ± 0.51 | 0.60 ± 0.48      | 0.61 ± 0.30 | 0.61 ± 0.31 |
| 25-Feb                             | 225_01*     | 0.29 ± 0.03                   | 0.28 ± 0.48     | 0.31 ± 0.41 | 0.29 ± 0.42 | 0.30 ± 0.24      | 0.30 ± 0.11 | 0.29 ± 0.11 |
|                                    | 225_02*     | 0.29 ± 0.03                   | 0.41 ± 0.46     | 0.45 ± 0.34 | 0.42 ± 0.36 | 0.44 ± 0.33      | 0.45 ± 0.14 | 0.44 ± 0.15 |
|                                    | 225_03*     | 0.29 ± 0.03                   | 0.30 ± 0.50     | 0.32 ± 0.46 | 0.38 ± 0.56 | 0.48 ± 0.39      | 0.54 ± 0.18 | 0.65 ± 0.18 |
| 08-Mar                             | 308_02      | 0.26 ± 0.02                   | 0.22 ± 0.31     | 0.23 ± 0.30 | 0.27 ± 0.35 | 0.33 ± 0.27      | 0.33 ± 0.22 | 0.40 ± 0.23 |
| 09-Mar                             | 309_01      | 0.29 ± 0.03                   | 0.62 ± 0.37     | 0.77 ± 0.72 | 0.76 ± 0.74 | 0.76 ± 0.33      | 0.89 ± 0.76 | 0.97 ± 0.79 |
|                                    | 309_02      | 0.29 ± 0.03                   | 0.39 ± 0.28     | 0.44 ± 0.39 | 0.49 ± 0.42 | 0.42 ± 0.37      | 0.47 ± 0.30 | 0.51 ± 0.31 |
|                                    | 312_01*     | 0.31 ± 0.03                   | 0.32 ± 0.34     | 0.31 ± 0.28 | 0.32 ± 0.31 | 0.31 ± 0.20      | 0.30 ± 0.09 | 0.32 ± 0.10 |
| 12-Mar                             | 312_03*     | 0.39 ± 0.03                   | 0.32 ± 0.53     | 0.32 ± 0.49 | 0.33 ± 0.54 | 0.39 ± 0.26      | 0.39 ± 0.11 | 0.42 ± 0.12 |
|                                    | 313_01*     | 0.28 ± 0.02                   | 0.15 ± 0.20     | 0.13 ± 0.19 | 0.13 ± 0.18 | 0.22 ± 0.15      | 0.20 ± 0.09 | 0.20 ± 0.09 |
|                                    | 313_02*     | 0.41 ± 0.04                   | 0.74 ± 0.63     | 0.80 ± 0.60 | 0.91 ± 0.66 | 0.84 ± 0.60      | 0.83 ± 0.36 | 0.97 ± 0.37 |
| 13-Mar                             | 313_03      | 0.47 ± 0.04                   | 0.08 ± 0.16     | 0.09 ± 0.18 | 0.09 ± 0.18 | 0.06 ± 0.06      | 0.08 ± 0.08 | 0.07 ± 0.08 |
|                                    | 313_04      | 0.48 ± 0.04                   | 0.13 ± 0.12     | 0.14 ± 0.08 | 0.13 ± 0.09 | 0.14 ± 0.11      | 0.14 ± 0.08 | 0.13 ± 0.08 |
|                                    | 313_05      | 0.52 ± 0.05                   | 0.24 ± 0.34     | 0.24 ± 0.32 | 0.20 ± 0.28 | 0.28 ± 0.21      | 0.29 ± 0.15 | 0.25 ± 0.16 |
| 14-Mar                             | 314_01      | 0.26 ± 0.03                   | 0.09 ± 0.08     | 0.09 ± 0.08 | 0.18 ± 0.12 | 0.10 ± 0.07      | 0.10 ± 0.07 | 0.17 ± 0.09 |
|                                    | 314_02      | 0.45 ± 0.05                   | 0.02 ± 0.03     | 0.03 ± 0.03 | 0.04 ± 0.02 | 0.05 ± 0.02      | 0.02 ± 0.03 | 0.02 ± 0.04 |
|                                    | 314_03      | 0.68 ± 0.03                   | 0.40 ± 0.43     | 0.46 ± 0.48 | 0.26 ± 0.51 | 0.40 ± 0.35      | 0.47 ± 0.36 | 0.24 ± 0.45 |
|                                    | NMAE** [%]  |                               | 53.86           | 57.16       | 58.20       | 64.59            | 68.29       | 71.48       |
|                                    | Bias [%]    |                               | -1.06           | 3.68        | 5.63        | 17.56            | 21.69       | 23.27       |
|                                    | RMSE [%]    |                               | 68.60           | 73.07       | 75.71       | 81.14            | 86.48       | 89.35       |
| Optimal measurement condition      | NMAE [%]    |                               | 28.56           | 30.41       | 29.63       | 53.68            | 55.26       | 51.73       |
|                                    | Bias [%]    |                               | 11.44           | 12.05       | 11.90       | 48.34            | 47.53       | 44.35       |
|                                    | RMSE [%]    |                               | 38.66           | 38.40       | 37.88       | 79.55            | 77.95       | 70.48       |
| Non optimal measurement conditions | NMAE [%]    |                               | 74.11           | 78.55       | 81.05       | 73.31            | 78.70       | 87.27       |
|                                    | Bias [%]    |                               | -11.06          | -3.02       | 0.61        | -7.06            | 1.02        | 6.41        |
|                                    | RMSE [%]    |                               | 85.29           | 91.83       | 95.76       | 82.40            | 92.74       | 101.97      |

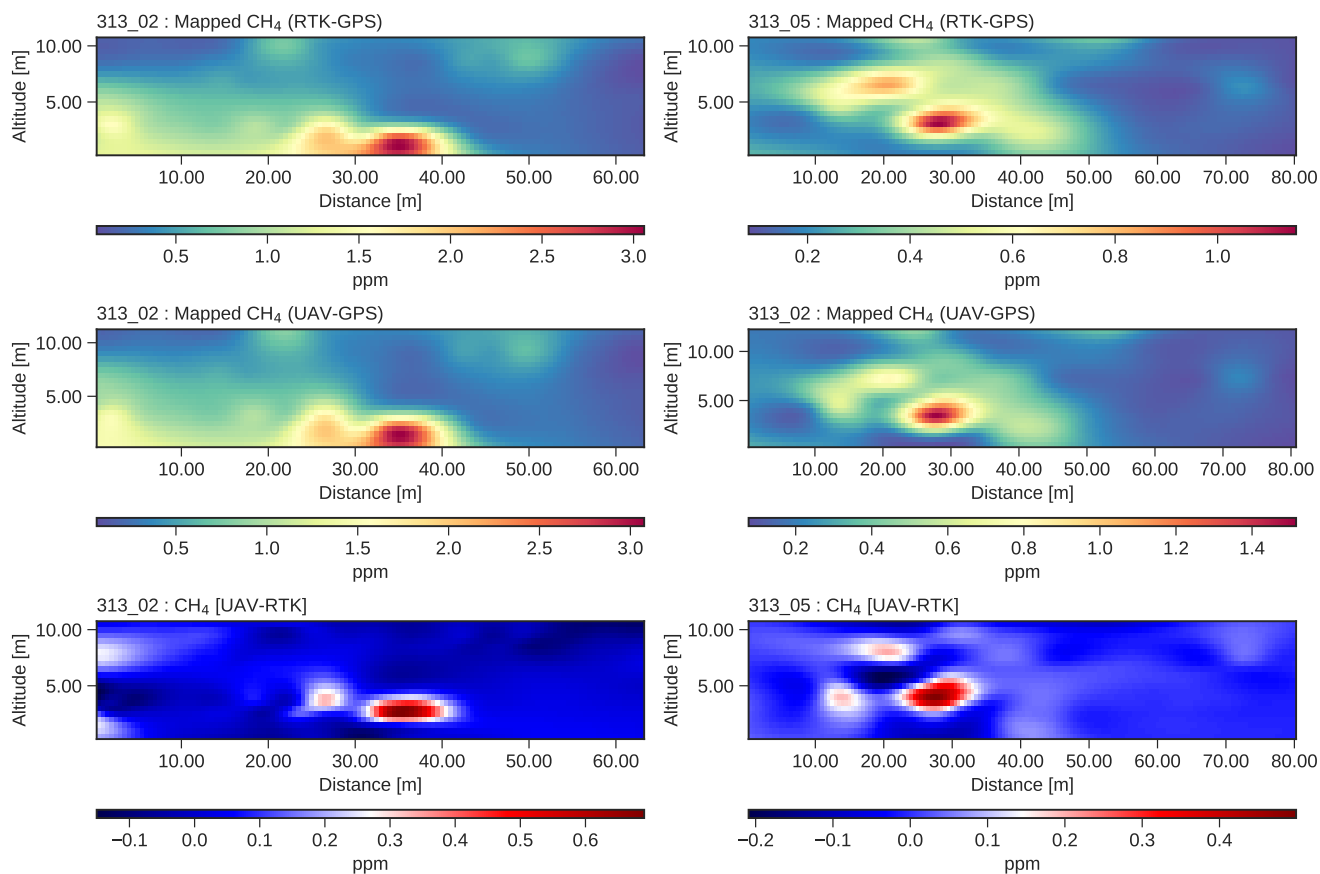
Flight codes with \* are measurement flights with optimal conditions in terms of meteorology and downwind distance described in Section 5.2.2. \*\*NMAE: Normalize mean absolute error.

**Table S2.** Altitude drift of UAV-GPS compared to RTK-GPS

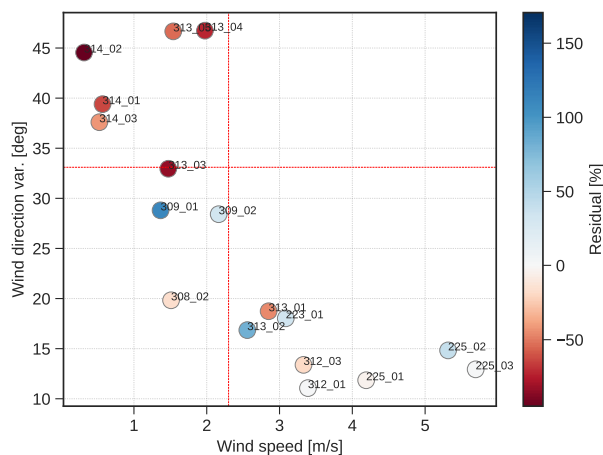
| Fl. Code | Drift<br>[cm s <sup>-1</sup> ] | Release<br>Rate | RTK-Estimate<br>[g s <sup>-1</sup> ] | UAV-Estimate<br>[g s <sup>-1</sup> ] |
|----------|--------------------------------|-----------------|--------------------------------------|--------------------------------------|
| 309_02   | 0.01 ± 0.54                    | 0.29 ± 0.03     | 0.39 ± 0.28                          | 0.38 ± 0.22                          |
| 312_01   | 0.21 ± 0.67                    | 0.31 ± 0.03     | 0.32 ± 0.34                          | 0.31 ± 0.24                          |
| 312_03   | 0.02 ± 0.82                    | 0.39 ± 0.03     | 0.32 ± 0.53                          | 0.29 ± 0.38                          |
| 313_01   | 0.12 ± 0.72                    | 0.28 ± 0.02     | 0.15 ± 0.20                          | 0.15 ± 0.17                          |
| 313_02   | 0.17 ± 0.67                    | 0.41 ± 0.04     | 0.82 ± 0.77                          | 0.82 ± 0.66                          |
| 313_03   | 0.04 ± 0.81                    | 0.47 ± 0.04     | 0.08 ± 0.16                          | 0.08 ± 0.18                          |
| 313_04   | 0.05 ± 0.80                    | 0.48 ± 0.04     | 0.13 ± 0.12                          | 0.15 ± 0.13                          |
| 313_05   | 0.17 ± 0.75                    | 0.52 ± 0.05     | 0.24 ± 0.34                          | 0.28 ± 0.29                          |
| 314_01   | 0.13 ± 0.56                    | 0.26 ± 0.03     | 0.09 ± 0.08                          | 0.09 ± 0.07                          |
| 314_02   | 0.21 ± 0.46                    | 0.45 ± 0.05     | 0.02 ± 0.03                          | 0.02 ± 0.03                          |
| 314_03   | 0.11 ± 0.40                    | 0.68 ± 0.03     | 0.40 ± 0.43                          | 0.42 ± 0.45                          |



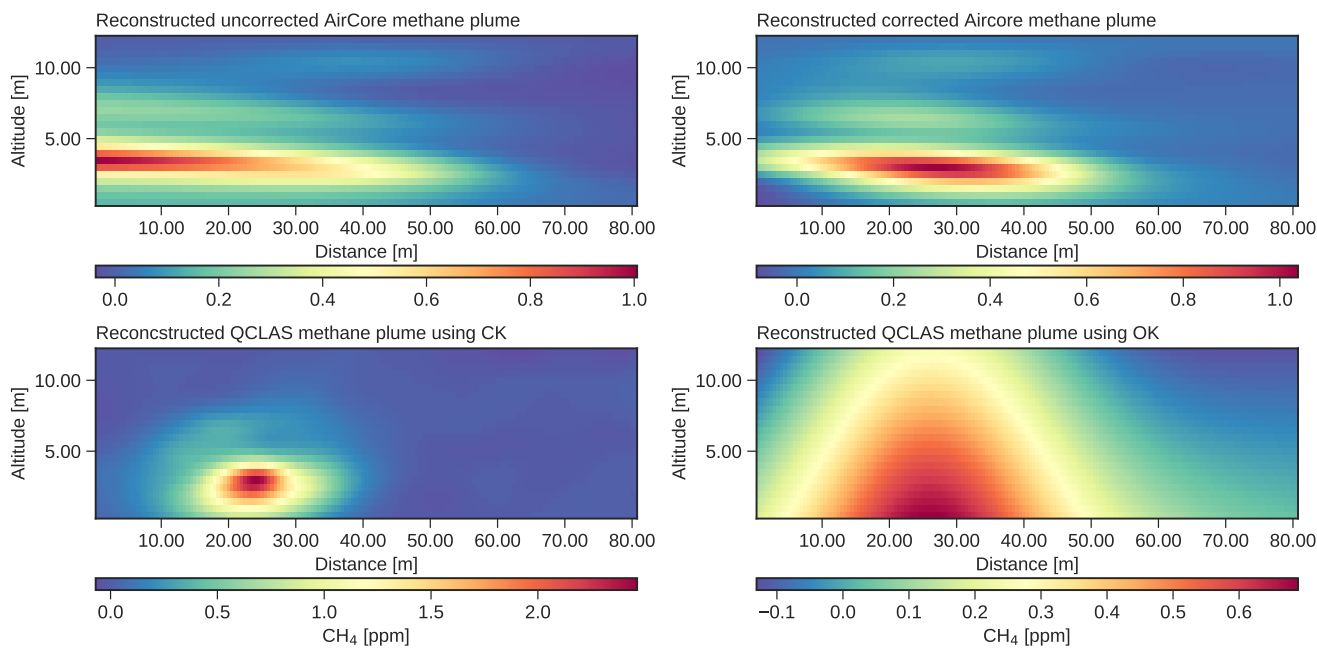
**Figure S3.** Vertical cross-section methane molar fractions generated using a theoretical Gaussian dispersion model and cluster-kriging estimated prediction at low wind speeds ( $< 1 \text{ ms}^{-1}$ )



**Figure S4.** Mapped methane plume for flights 313\_02 and 313\_05 using RTK-GPS and UAV-GPS. The difference between the methane mole fraction field is also shown.

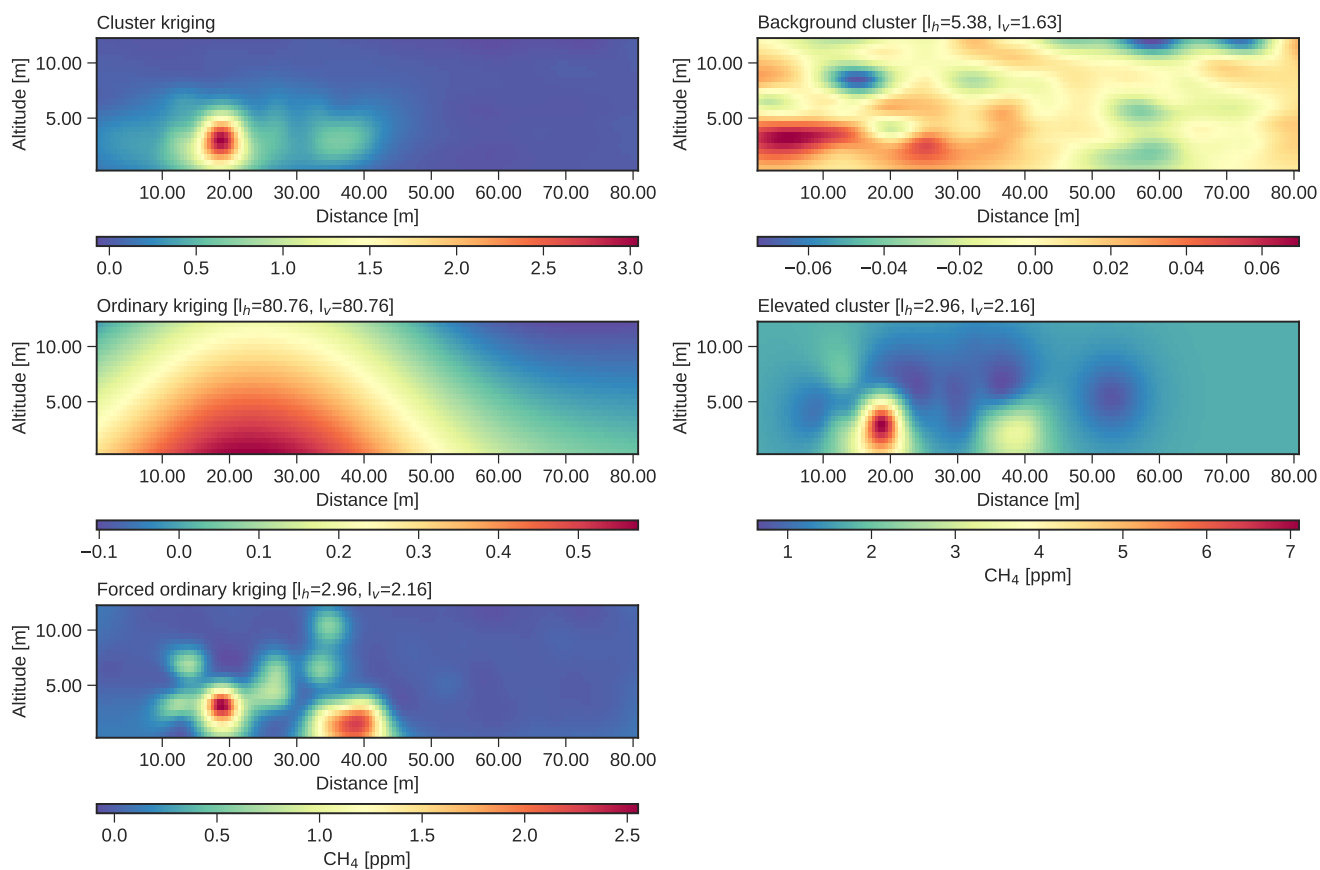


**Figure S5.** Residual plot between true and estimated release with respect to mean wind speed and directional variability. The circles in the lower right corner correspond to the eight out of 18 flights that meet the prescribed threshold. Residual errors characterized by light red and blue colors are generally lower for these flights.



**Figure S6.** Reconstructed methane plume for flight 312\_03. The figure on the upper left shows a reconstructed plume without applying a proper time correction for AirCore measurements, whereas the figure on the upper right is a reconstructed plume obtained after applying the proper time correction. The two bottom figures shows the reconstructed plume using the QCLAS measurement. After applying the proper correction, the methane plume moved spatially to the right placing it towards the center of the mapping plane. This resulted to a 23 % increase in emission estimate—closer to the true release.





**Figure S7.** Reconstructed methane plume for 312\_03 from QCLAS measurements using cluster-based vs ordinary kriging. Length scales written on top of each plot. Horizontal length scale is  $l_h$  while vertical length scale is  $l_v$ .