Laboratory characterisation of the radiation temperature error of radiosondes and its application to the GRUAN data processing for the Vaisala RS41

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Abstract. The paper presents the Simulator for Investigation of Solar Temperature Error of Radiosondes (SISTER), a setup that was developed to quantify the solar heating of the temperature sensor of radiosondes under laboratory conditions by recreating as closely as possible the atmospheric and illumination conditions that are encountered during a daytime radiosounding ascent. SISTER controls the pressure (3 to 1020 hPa) and ventilation speed of the air inside the wind-tunnel-like setup to simulate the conditions between the surface and 35 km altitude, to determine the dependence of the radiation temperature error on the irradiance and the convective cooling. The radiosonde is mounted inside a quartz tube, while the complete sensor boom is illuminated by an external light source to include the conductive heat transfer between sensor and boom. A special feature of SISTER is that the radiosonde is rotated around its axis to imitate the spinning of the radiosonde in flight. The characterisation of the radiation temperature error is performed for various pressures, ventilation speeds, and illumination angles, yielding a 2D parameterisation of the radiation error for each illumination angle, with an uncertainty smaller than 0.2 K (k = 2) for typical ascends speeds. This parameterisation is applied in the Global Climate Observing System (GCOS) Reference Upper-Air Network (GRUAN) processing for radiosonde data, which relies on the extensive characterisation of the sensor properties to produce a traceable reference data product which is free of manufacturer-dependent effects. The GRUAN radiation correction model combines the laboratory characterisation with model calculations of the actual radiation field during the sounding to estimate the correction profile. In the second part of this paper it is described how this procedure was applied in the development of the GRUAN data product for the Vaisala RS41 radiosonde (version 1, RS41-GDP.1). The magnitude of the averaged correction profile increases gradually from 0.1 K at the surface to approximately 0.8 K at 35 km altitude. Comparisons between sounding data (N = 154) that were GRUAN-processed and Vaisala-processed reveal that the daytime differences (GRUAN – Vaisala) are smaller than +0.1 K in the troposphere and increase above the tropopause steadily with altitude to +0.35 K at 35 km. These differences are just within the limits of the combined uncertainties (with coverage factor k = 2) of both data products, meaning that the GRUAN processing and the Vaisala processing are in agreement.

1 Introduction

For almost a century, radiosondes have been successfully providing essential measurements of the state of the atmosphere at unmatched vertical resolution up to an altitude of approximately 35 km. Nowadays, more than 800 radiosoundings are performed each day by the global observational network, providing essential measurement data to numerical weather prediction (NWP). These long-term global data records have great value for climate monitoring (Elliott and...
Gaffen, 1991; Gaffen, 1994; Seidel et al., 2009). However, they often contain inhomogeneities caused by changes in measurement systems (Elliott and Gaffen, 1991), and uncorrected measurement errors as well as undisclosed data processing of commercial radiosondes affect the quality of the measurement data. The need for high-quality reference data motivated the founding of the Global Climate Observing System (GCOS) Reference Upper-Air Network (GRUAN, https://www.gruan.org/, last access: 21 January 2022) in 2008 (Seidel et al., 2009; Bodeker et al., 2016).

One of the main goals of the GRUAN is to perform reference observations of profiles of Essential Climate Variables (ECVs) such as atmospheric temperature and humidity, for the purpose of monitoring climate change, and for other applications such as NWP and satellite validation. Essential criteria for establishing a reference observation include measurement traceability, correction of all known errors and biases, and the availability of measurement uncertainties. Manufacturer-processed data often do not fulfill the criteria for a reference data product, mainly because of the application of undisclosed correction algorithms in the data processing, inadequate correction of measurement errors, or missing measurement uncertainties. In contrast, it is a prerequisite for GRUAN data products (GDPs) to comply with the criteria for a reference product, for which the applied correction methods are based on extensive characterisation of the instrument and its sensors. As a consequence, the development of GRUAN data processing for a specific instrument requires considerable effort and can be a time-consuming process. Currently, GDPs are available for the Vaisala RS92 (Dirksen et al., 2014) and Meisei RS-11G (Kobayashi et al., 2019; Kizu et al., 2018) radiosonde models, as well as for Global Navigation Satellite System precipitable water vapour (GNSS-PW), while data products for additional radiosonde models, as well as for other measurement techniques such as lidar or microwave radiometer (MWR), are under development.

The main error source for daytime radiosonde temperature measurements is the warming of the temperature sensor by solar radiation, a problem that has affected temperature measurements since the beginning of balloon-borne aerological observations. A relatively easy way to estimate the radiation temperature error uses the observed day–night difference, which for previous radiosonde models was shown to amount up to 2 K in the stratosphere (McInturff et al., 1979; Luers, 1990). The temperature sensor is usually located at the far end of a sensor boom to minimise contamination by air flowing over the casing of the radiosonde. The temperature measurement by the radiosonde is a contact measurement, where the sensor assumes the temperature of the surrounding air, with heat transfer between both media acting to reduce the differences. Absorption of solar radiation by the temperature sensor heats the sensor, which is counteracted by convective cooling, conduction, and radiation, where convective cooling is considered the dominant factor (Luers, 1990). The efficiency of the convective cooling decreases with pressure at higher altitudes, leading to an increase in the temperature error with altitude, which for current radiosonde types amounts to approximately 1 K at 30 km altitude.

The exact quantification, and correction, of the radiation temperature error is a complicated and challenging effort, which is exacerbated by the fact that there is no instrument available for in situ reference measurements of the air temperature that would allow for an independent comparison of the radiosonde temperature measurements. Over time, different methods have been used to estimate the radiation temperature error. Theoretical approaches employed by for example McMillin et al. (1992), Luers and Eskridge (1995), and Luers (1997) involve solving the heat balance for the irradiated temperature sensor, which requires detailed knowledge of the thermodynamic and radiative properties of the sensor boom components, as well as thorough evaluation of the aerodynamics of the airflow around the sensor boom. The accuracy of this approach is limited by the assumptions and approximations that are necessary for material properties and for the modelling of the pressure-dependent convective heat exchange.

A widely used method is the comparison with observations from other measurement techniques, such as space-borne remote sensing instruments. Examples of this are the work by Haimberger et al. (2008) to estimate warm biases in long-term radiosonde upper-air records relative to microwave soundings (MSU) radiances, or the comparison with colocated GPS radio occultation (GPS-RO) observations by Sun et al. (2013) and Ho et al. (2017). Such comparisons provide a statistical estimate of the temperature bias between the radiosonde and the satellite instruments in question, but conclusive findings are usually not possible because satellite-based temperature profiles do not constitute a calibrated reference. Other limitations that complicate the comparison are for example that the timing of the radiosoundings needs to be adjusted to match satellite overpasses to reduce the collocation error and that accurate observations by microwave and infrared remote sensing instruments require cloud-free scenes.

A few attempts have been made to determine the radiation temperature error by direct comparison of in situ instruments (e.g. NASA, 1986). This limited number of studies is mainly due to the lack of a true, independent reference for in situ temperature observations. Philipona et al. (2013) derived a correction from an in-flight experiment, where the solar radiation temperature error was derived using the temperature difference between two identical thermocouple sensors, one exposed and the other shielded from sunlight, while simultaneously recording the shortwave and longwave fluxes. The resulting altitude-dependent correction amounts to approximately 1 K at 35 km. Using a similar approach, Lee et al. (2018c) estimate the temperature error from the bias between differently coated thermistors on the same radiosonde, which is subsequently used to correct the measured temper-
ature profile. The estimated uncertainty for this correction is 0.49 K ($k = 1$).

Following the GRUAN methodology, the characterisation of the temperature sensor is performed in a traceable laboratory environment, with a setup that can simulate the conditions that occur in flight. The result of this sensor characterisation is the basis for the correction algorithms that are employed in the GRUAN data processing that is addressed in this paper. The warming of the temperature sensor by solar radiation is determined as a function of pressure, flux, ventilation speed, and illumination angle. The actinic flux is needed to relate the laboratory characterisation of the sensor’s susceptibility to radiation to the actual temperature error. Due to the lack of information on the actual solar radiation profile in the GRUAN correction, the actinic flux is estimated with a radiative transfer model (RTM), which calculates direct and diffuse upward and downward radiance components while accounting for the changes of the location of the radiosonde and of the position of the Sun during the ascent. The correction algorithm combines both components to estimate the temperature error for each data point of the ascent. Luers and Eskridge (1995) showed that longwave heating of a sensor with a metallic coating is much smaller than the heating by shortwave (visible) radiation, so that the GRUAN correction only considers the effects from shortwave radiation.

This approach was first employed for the GRUAN data processing of the Vaisala RS92 radiosonde, where the characterisation of the radiation temperature error was performed with the radiosonde inserted in a vacuum chamber, using the Sun as a light source (Dirksen et al., 2014). This chamber generated an internal airflow that is comparable to the ventilation experienced during a radiosonde ascent, at pressures between ambient and 3 hPa. Another, similar, setup was used in the development of the data processing for the Meisei RS-11G (Kizu et al., 2018). Recently Lee et al. (2020) built a setup to investigate the radiation temperature error at temperatures that prevail in the stratosphere, but so far the latter setup has not been applied for GDP development.

Several restrictions concerning the orientation of the sensor with regard to the light source and the airflow limited the ability of the chamber used by Dirksen et al. (2014) to realistically render the in-flight conditions, and this prompted the construction of the custom-built Simulator for Investigation of Solar Temperature Error of Radiosondes (SISTER) setup at the Lindenberg Observatory, which is described in this paper. SISTER is an airtight wind tunnel that produces ventilation speeds up to 7 m s$^{-1}$ and pressures between ambient and 3 hPa. Notable features of SISTER are that the wind tunnel is wide enough to enable the axial rotation of the radiosonde with an unfolded sensor boom, which allows us to recreate the continuously changing illumination conditions resulting from the spinning of the radiosonde in flight. Furthermore, the temperature sensor and a sizeable part of the sensor boom are illuminated. This approximates the daytime situation where the sensor boom is continuously exposed to sunlight and includes the influence of the sensor boom in the determination of the radiation error. Temperature sensors are usually kept small, as the radiation error scales with sensor size (de Podesta et al., 2018), but conductive heating from the energy absorbed by the comparably large area of the sensor boom can be a relevant factor. In the characterisation of the RS92, Dirksen et al. (2014) found indications that the sensor boom contributes considerably to the overall heating of the temperature sensor. This is supported by computational fluid dynamics (CFD) model calculations by Han et al. (2018), which showed that the heating of a thin platinum-wire sensor is mainly caused by the conductive heating from the illuminated circuit board instead of the solar irradiation of the sensor wire. Finally, with SISTER the illumination geometry of the radiosonde can be adjusted to simulate solar irradiations that are representative for tropical, mid-latitude, and arctic regions.

SISTER is used for the development of the GDP for the Vaisala RS41 radiosonde. Currently, 23 GRUAN sites employ the RS41 as operational radiosonde, which effectively makes it the backbone of GRUAN in terms of upper air soundings and which illustrates the importance of developing a GDP for the RS41. Dirksen et al. (2020) discuss how the replacement of the RS92 by the RS41 poses a special challenge for GRUAN as a reference network and the strategy that is adopted to reduce inhomogeneities in the GRUAN data record.

The structure of this paper is as follows: Sect. 2 describes the SISTER setup including a characterisation of the flow pattern based on laser Doppler anemometry (LDA), Sect. 3 describes the measurements to characterise the radiation temperature error, Sect. 4 describes the analysis of these measurements and the resulting parameterisation of the susceptibility of the RS41 temperature sensor to solar radiation, Sect. 5 describes the RTM simulations to calculate the actinic flux, Sect. 6 describes the actual correction algorithm that is applied in the GRUAN data processing, Sect. 7 presents a comparison between the GRUAN-processing and the Vaisala-processing of the RS41’s temperature profiles, and Sect. 8 provides a summary and outlook.

2 Radiation test facility

2.1 Design considerations

SISTER (Simulator for Investigation of Solar Temperature Error of Radiosondes) is designed to simulate as closely as possible the conditions that are encountered during a typical radiosounding ascent. This involves controlling parameters such as pressure, ventilation speed, and the illumination geometry. The more challenging requirements for rendering realistic illumination conditions involve the illumination of the temperature sensor together with a considerable part of the
neighbouring sensor boom, as well as at the same time the continuous rotation of the sensor boom around the longitudinal axis to simulate the radiosonde’s spinning in flight. In addition, a stable airflow of approximately 5 m s\(^{-1}\) at pressures between 1000 and 3 hPa is required to mimic the ventilation by ambient air of the radiosonde during ascent. These requirements resulted in the design of an airtight wind-tunnel-like construction that is wide enough to hold a rotating radiosonde with unfolded sensor boom and that can be operated between ambient and low pressure.

The radiation test facility, shown in Figs. 1 and 2, is a rectangular-shaped wind tunnel with external dimensions of approximately 1 m \(\times\) 2 m. It is assembled of stainless steel tubes of 153 and 213 mm diameter. The actual measurement chamber, located in one leg, is formed by a 180 mm wide, 1 m long cylindrical quartz tube in which the radiosonde is mounted. The quartz tube is mounted in a metal casing that serves as mechanical support and as a safety cover. A membrane vacuum pump is used to set the pressure. The circulation of the air inside the chamber is driven by a fan that is located in the leg opposite to the measurement chamber. The fan’s diameter is comparable to that of the metal tube in which it is mounted. A rectifier behind the fan serves to reduce turbulence. A set of strainers is installed immediately before the quartz tube to further suppress turbulence. The radiosonde is mounted on a rod along the longitudinal axis of the quartz tube. To imitate the spinning of the radiosonde during ascent, the rod is rotated at constant speed by a stepper motor. The rotation period can be 1 s or longer, and fixed positions can be selected as well.

The sensor boom of the radiosonde is illuminated by a 2500 W Xe arc light source, generating a collimated beam with a divergence of a few degrees. A manual aperture limits the beam diameter to approximately 20 cm at the centre of the quartz tube. This is wide enough to illuminate the entire cross section of the quartz tube, so that for any orientation of the radiosonde, the temperature sensor and a large part of the sensor boom are illuminated. Prior to the measurements, the housing of the radiosonde electronics is removed to reduce its cross section and thus to minimise the disturbance of the airflow, leaving only the electronic board with batteries and the sensor boom. The sensor boom is bent at an angle of 45° with respect to the flow direction (see Fig. 1 and the inset in Fig. 2) and kept in place using thin threads. The illumination angle, which represents the solar-elevation angle, can be varied by turning the entire chamber around an (imaginary) vertical axis that runs through the position of the radiosonde’s temperature sensor, and the flux is varied by changing the distance between the chamber and the light source.

### 2.2 Ventilation speed

The airflow at the position of the radiosonde is characterised using 2D laser Doppler anemometry (LDA, e.g. Albrecht et al., 2003). This optical method of flow velocity measurement is non-invasive, and in a closed volume under low-pressure conditions it is the only method that does not require additional designs, such as a sealed sluice, for the insertion of a measuring probe. Along with high spatial and temporal resolution, another advantage of LDA is that no calibration is required. This is particularly important for a setup such as SISTER, where measurements are performed at different pressures.

LDA measurements rely on seeding with particles that are carried along in the airflow. The measurement principle is the detection of the Doppler shift of the laser light scattered off the moving aerosol particles. The aerosols are produced in a particle generator (atomiser aerosol generator, AMT 230) with particle sizes of about 0.2–0.5 µm, using di-ethyl-hexyl-sebacat (DEHS, Topas Co.) as the liquid for the atomiser.

During the measurement of the flow velocities, an RS41 radiosonde is installed inside the quartz tube with the same configuration as the radiation error experiments to ensure a consistent flow field around the temperature sensor. At a position along the tube axis which is close to the tip of the sensor boom, the axial and radial components of the airflow are measured at 1 to 2 cm intervals in the radial direction from the edge to about the central axis. Thus, this covers half of the tube’s diameter, but cylindrical symmetry is assumed for the flow pattern. The measurements are performed at various pressures and fan rotation speeds.

The LDA measurements show that the magnitude of the radial flow components is less than approximately 10% of the axial component, which means that the airflow over the sensor boom is predominantly laminar and in the axial direction, which resembles the situation in flight. Fig. 3 presents examples of the measured flow velocity profiles, which represent the shape that is expected for a pipe flow. The axial flow velocity is almost zero close to the tube’s wall and increases rapidly to reach a constant value at 3 to 4 cm away from the wall. The right-hand panel of Fig. 3 shows a slight decrease in the flow speed near the central axis at higher pressure levels, which is attributed to the radiosonde obstructing the flow.

Below 30 hPa, the injection of the air–particle mixture during seeding causes a noticeable rise in pressure, which presents difficulties in reaching low pressures. Furthermore, at low pressures it becomes increasingly difficult to achieve the minimal particle density required to ensure sufficient LDA counts. As a result, no measurements were performed below 20 hPa.

The LDA measurements are used to determine the flow speed around the sensor boom as a function of pressure \(p\) (in hectopascal) and fan rotation speed \(f\_\text{fan}\) (in one per second). The resulting parameterisation of the flow speed \(v\) is

\[
v(p, f\_\text{fan}) = \sum_{i,j} c_{ij} \cdot p^{i/2} \cdot f\_\text{fan}^{j/2},
\]

where the polynomial coefficients \(c_{ij}\) follow from a non-linear least squares fit to the measurements at the centre of...
The chamber with radial distances between 70 and 100 mm. These radii correspond to the area that is covered by the sensor boom of the rotating radiosonde. Table 1 lists the values of \( c_{ij} \), and the left panel of Fig. 4 shows the resulting 2D fit to the data. The blue dots at the bottom represent the data points for \( v(p, f_{fan} = 0) = 0 \) that were added to constrain the fit, with the purpose to use Eq. (1) to determine fan speed settings for flow speeds that were not covered by the LDA measurements. The plots in Fig. 4 show a close-to-linear dependence of the air speed \( v \) on fan rotation, and the left panel also shows a strong decrease in air speed for pressures below 20 hPa, which is attributed to the reduced efficiency of the fan in this pressure range.

A detailed uncertainty budget for the calculated ventilation speed cannot be derived. Instead, a combined overall uncertainty \( u(v) \) is set to a fixed value of 0.5 m s\(^{-1}\) \((k = 1)\). This value is assumed to take potential components from the LDA technique and those connected to the least-squares fitting (right panel in Fig. 4) into account. In particular it should include potential uncertainties connected to the positioning and effective flow resistance of the radiosonde’s body inside the test chamber. The latter is expected to be of systematic nature and to dominate the overall uncertainty. A thorough estimate of that uncertainty component can at best be made with very elaborate LDA measurements, for example by varying the

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**Table 1.** Polynomial coefficients used in Eq. (1) for calculation of ventilation speed as function of pressure and fan rotation.

<table>
<thead>
<tr>
<th>( i, j )</th>
<th>( c_{ij} )</th>
<th>( i, j )</th>
<th>( c_{ij} )</th>
<th>( i, j )</th>
<th>( c_{ij} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0, 0</td>
<td>(-1.03154 \times 10^{-6})</td>
<td>0, 1</td>
<td>(9.07802 \times 10^{-2})</td>
<td>0, 2</td>
<td>(4.05845 \times 10^{-3})</td>
</tr>
<tr>
<td>1, 0</td>
<td>(1.36741 \times 10^{-6})</td>
<td>1, 1</td>
<td>(-3.85667 \times 10^{-2})</td>
<td>1, 2</td>
<td>(1.52509 \times 10^{-2})</td>
</tr>
<tr>
<td>2, 0</td>
<td>(-2.84620 \times 10^{-7})</td>
<td>2, 1</td>
<td>(4.87337 \times 10^{-3})</td>
<td>2, 2</td>
<td>(-1.34985 \times 10^{-3})</td>
</tr>
<tr>
<td>3, 0</td>
<td>(1.61256 \times 10^{-8})</td>
<td>3, 1</td>
<td>(-1.67718 \times 10^{-4})</td>
<td>3, 2</td>
<td>(4.40378 \times 10^{-5})</td>
</tr>
<tr>
<td>4, 0</td>
<td>(-2.70407 \times 10^{-10})</td>
<td>4, 1</td>
<td>(1.67955 \times 10^{-6})</td>
<td>4, 2</td>
<td>(-4.77922 \times 10^{-7})</td>
</tr>
</tbody>
</table>
Figure 3. Examples of measured radial profiles of axial airflow in the test chamber at a position shortly before the sensor boom of the radiosonde. The three panels show results for different flow intensities at three different pressure levels. The flow velocities were generated by adjusting the fan voltage and thus its speed (in revolutions per second).

Figure 4. Flow speed as function of pressure and fan rotation (in revolutions per second). (a) Symbols denote measured flow speed around the central axis of the test chamber close to the sensor boom of the radiosonde. Blue symbols are manually added points for vanishing flow (fan switched off) to enable reasonable fitting. The surface shows the fit according to the empirical model (Eq. 1). (b) Equivalent plot for the residual, indicating irregular deviations of the data from the fit within about ±0.5 m s⁻¹. Note the logarithmic pressure axis for better visibility at low pressures.

2.3 Irradiation

2.3.1 Light source

The light source is a 2500 W xenon arc lamp (Osram XBO® 2500W/OFR), which has an output spectrum that is, for this application, sufficiently similar to that of the Sun. The spatial inhomogeneity of the output beam at the position of the radiosonde was verified to be less than 1.5 %, using a CMP21 pyranometer (Kipp & Zonen). The temporal stability of the lamp flux is monitored regularly in parallel to the RS41 measurements. Using the same CMP21, the irradiance at two fixed distances (r = 1.0 m and r = 1.1 m) is measured in the centre of the beam. These data show a variability (relative standard deviation, N = 29) of 1.9 %, without indication of a significant drift.

2.3.2 Flux

Measurements of the flux at various distances from the light source show that the lamp’s output decreases with distance following the inverse-square law. The data in Fig. 5 are fitted by

\[ I(r) = P_0 \cdot (r - r_0)^{-2}, \]

(2)
with \( r \) the distance measured from the lamp’s housing, and \( P_0 = 1444.6 \text{ W} \) and \( r_0 = 0.20 \text{ m} \) the fit parameters. Here \( r_0 \) accounts for the position of the virtual image of the Xe lamp that is generated by the collimating optics. Eq. (2), in combination with the transmission through the quartz wall of the measurement chamber (see Sect. 2.3.3), is used to calculate the flux on the temperature sensor during the experiments.

### 2.3.3 Transmissivity of the quartz tube

The attenuation by the wall of the quartz tube is determined by measuring the flux at the position of the sensor boom with and without the tube in place for various angles of incidence between 0 and 60°. The Fresnel equation, which describes the reflection and transmission of light incident on uncoated surfaces, is used to fit the measured transmittance \( T_c \) shown in Fig. 6.

\[
T_c(\alpha) = c_0 \cdot \frac{\tan \alpha}{\tan \beta} \left[ \frac{2 \cos \alpha}{c_1 \cos \alpha + \cos \beta} \right]^2.
\]  

(3)

Here, \( \alpha \) denotes the angle of incidence, and \( \beta = \arcsin \frac{\sin \alpha}{n_2} \) follows from Snell’s law of refraction, using \( n_2 = 1.46 \) for the refraction index of quartz. To aid and constrain the fit, the point \( T_c(\alpha = 90°) = 0 \) is added, yielding the parameters \( c_0 = 0.505 \) and \( c_1 = 0.769 \). The attenuation by the window is mainly caused by the reflection from the window’s outer surface and to a lesser extend by absorption or refraction by the quartz glass. As indicated in Fig. 1, a black-coated plate between the radiosonde and the rear wall of the chamber serves as a beam dump and prevents reflections from the rear wall, which would otherwise lead to an overestimation of the radiation error.

### 2.3.4 Linearity of \( \Delta T \) with irradiance

The current understanding of the radiative heating of the temperature sensor predicts a linear relationship between flux and the temperature error, when all other parameters are unchanged. This linearity was already proposed in the theoretical approach by Luers (1990) and was confirmed in various experiments such as Lee et al. (2018a, c). This is in agreement with our findings, presented in Fig. 7. Based on the observation that \( \Delta T \), and presumably its associated uncertainties, scales linearly with the flux, the measurements are performed for a fixed irradiance level. In practice, the experiments are performed at flux levels between 1025 and 1142 W m\(^{-2}\), which is comparable to the actinic flux at the altitudes where the radiation effect is significant.
2.3.5 Extreme solar zenith angle

As mentioned in Sect. 2.1, the angle of incidence $\alpha$ is varied to simulate the conditions for various solar-elevation angles. Due to space restrictions, the incidence angle is limited to the range $0$ to $60^\circ$. In addition, the configuration corresponding to the zenith position of the Sun (incident angle or solar elevation $\alpha = 90^\circ$) can be realised by putting the radiosonde in the fixed position shown in Fig. 8b or c. Here we exploit the cylindrical symmetry of the situation where the axis of rotation of the spinning radiosonde points towards the Sun. Due to this symmetry, a static radiosonde has the same illumination geometry as one that is spinning around its axis. Although both sides of the sensor boom are assumed to be equally sensitive to radiation, the measurements were performed while illuminating the front (Fig. 8b) and the rear side (Fig. 8c) of the sensor boom, taking the average of both afterwards.

2.3.6 Diffuse radiation

Diffuse solar radiation, resulting from light scattered by the air, clouds, or the Earth’s surface, can contribute significantly to the total actinic flux. A special configuration of SISTER is used to quantify this contribution to the radiation error, shown in Fig. 8d and e. Under the assumptions that

- the effective heating of the temperature sensor depends on the magnitude of the impinging flux only and therefore is the same for direct or diffuse light of the same intensity,
- the scattered light has a directional uniform distribution, and
- both sides of the sensor boom are equally sensitive to radiation,

the heating of the sensor due to diffuse radiation does not depend on its actual orientation. Therefore, the static, non-rotating, sensor boom is illuminated perpendicularly with a flux of $527 \text{ W m}^{-2}$, which is a good approximation of the diffuse flux encountered in flight. The measurement is performed while illuminating the front (Fig. 8d) and the rear (Fig. 8e) of the sensor boom, and the results are averaged.

2.3.7 Uncertainty budget for irradiance

The contributions to the overall uncertainty of the irradiance at the location of the radiosonde inside the test chamber were estimated as relative values and are listed in Table 2.

<table>
<thead>
<tr>
<th>Component</th>
<th>Amount</th>
</tr>
</thead>
<tbody>
<tr>
<td>Temporal stability Xe lamp</td>
<td>1.9 %</td>
</tr>
<tr>
<td>Light spot inhomogeneity</td>
<td>1.5 %</td>
</tr>
<tr>
<td>Lamp–radiosonde distance ($u(r) = 5 \text{ mm}$)</td>
<td>1.0 %</td>
</tr>
<tr>
<td>Transmission through wall of test chamber</td>
<td>2.0 %</td>
</tr>
<tr>
<td>Calibration pyranometer</td>
<td>1.0 %</td>
</tr>
<tr>
<td>Combined</td>
<td>3.4 %</td>
</tr>
</tbody>
</table>

3 Experiments

3.1 Sequence of measurements

The RS41 is illuminated typically for $30 \text{ s}$ to $3 \text{ min}$, depending on the actual pressure and ventilation speed, followed by an equivalent cooling phase after closing the shutter. This exposure time is generally long enough for the sensor temperature to approach the new thermal equilibrium before the shutter is closed. The rotation of the radiosonde introduces oscillations in the recorded temperature profile, which is caused by the periodically changing exposed surface of the illuminated sensor boom. The analysis of the measurements in Sect. 4.1 shows that the length of the rotation period does not affect the determination of the radiation error. Therefore, a rotation period of $16 \text{ s}$ is used for all measurements to represent the spinning of the radiosonde during a typical radiosounding.

The air temperature inside the test chamber is recorded by four thermistors, located at the entrance of the chamber upstream of the radiosonde, evenly distributed over the cross section (Fig. 1). These measurements are used to provide the
The parameter ranges covered with SISTER, and their associated uncertainties, are listed in Table 3. Due to the lack of a pressure gauge of suitable accuracy inside the setup, the reading of the RS41-SGP’s internal pressure sensor is used to determine the pressure in the chamber. The uncertainty budget of the pressure reading is based on the manufacturer’s specification and on comparisons that are performed with other pressure sensors. The ventilation speed is set by adjusting the voltage of the fan’s power supply and therefore the rotation speed, using the relation in Eq. (1).

The measurement program was confined to one irradiance level for each pressure–ventilation combination because of the linear relation between temperature error and irradiance (Sect. 2.3.4). It takes 1 d of measurement to cover the pressure–ventilation combinations from Table 3 for each of the eight illumination configurations that are illustrated in Fig. 8.

4 Evaluation of experimental data

Figure 10 presents a selected ∼1 h long section of data from a 1 d measurement run. Synchronised data from the various sensors are recorded continuously at 1 s intervals. The exposure periods can be recognised as peaks in the RS41 temperature raw data in the lower panel of Fig. 10. Their magnitudes are from 0.5 to 1 K in this example. The effect of the continuous rotation of the radiosonde is visible as oscillations superimposed the RS41 temperature curve.

4.1 Determination of the solar temperature effect

Fluctuations around the laboratory temperature may occur at the position of the radiosonde, since SISTER is not temperature-stabilised. Such variations are caused by adiabatic effects when setting new pressure levels, such as the temporary drop in temperature at 21,200 s in Fig. 10 and at a slower rate due to the heat exchange with the laboratory environment. The fan and the stepper motors, the radiosonde itself, and the energy from the applied radiation are potential local heat sources. These can produce small-scale temperature inhomogeneities in the airflow, which are detected by the thermistors that monitor the temperature in the test chamber. The lower panel of Fig. 10 shows that the differences between the individual thermistors due to temperature inhomogeneities can be as large as 0.5 K.

The radiation-induced \( \Delta T \) is determined from the temperature change measured by the RS41 during exposure, an example of which is shown Fig. 11 for an ∼80 s exposure at incidence angle \( \alpha = 40^\circ \). After opening the shutter, the measured temperature rises quickly at first, followed by a slower convergence to a quasi-stationary value. In the subsequent analysis, the temperature from one of the four thermistors is subtracted from the radiosonde’s readings to compensate for (slow) variations of the background. The choice of
this reference thermistor is done manually, selecting the one showing the least of the above-described fluctuations. Before correcting the radiosonde temperature, an offset is added to the thermistor readings, such that the average temperature in the 60 s before opening the shutter, represented by the blue line in Fig. 11, matches the average temperature of the radiosonde in that interval. This procedure accounts for possible calibration-related offsets between thermistor and radiosonde sensor.

Due to the radiosonde’s rotation, the exposed surface of the sensor and the sensor boom changes regularly, causing the oscillating pattern on top of the measured signal. The maxima correspond to the position of the sensor boom with the largest effective area (smallest angle between light beam and the normal to the sensor boom), whereas the minima correspond to the position where the edge of the sensor boom is turned towards the lamp. In the latter case the bar-shaped temperature sensor is still illuminated, so that \( T \) does not approach zero. These oscillations are a clear proof of the thermal coupling between the sensor and the sensor boom. Due to thermal inertia of the sensor boom, there may be a time lag between the oscillation peaks and the actual positions corresponding to minimum and maximum illumination. The lower panel of Fig. 10 shows that small oscillations are also observed in the shadow phases. These are attributed to the rotating sensor boom moving through small, persistent temperature inhomogeneities inside the measurement chamber.

During the slow convergence, the temperature sensor approaches thermal equilibrium following an exponential decay, with the rotation-induced oscillations superimposed. \( \Delta T \) follows from fitting this exponential decay with Eq. (4) below, where the length of the fit interval is chosen to contain an integer number of oscillation periods, to minimise their influence on the resulting fit, which is represented by the green trace in Fig. 11:

\[
\Delta T = c_0 + c_1 \exp(-c_2 t).
\]  

(4)

Here \( t \) is the time since opening the shutter and \( c_0, c_1, \) and \( c_2 \) are fit parameters, where \( c_0 \) represents the new equilibrium temperature, which is represented by the horizontal green line in Fig. 11. The fit windows are set manually for each exposure, because the large variety in shape, size, and temporal
behaviour of the response curves for the various experimental settings would unnecessarily complicate an automated algorithm.

After closing the shutter, the indicated temperature returns to the background level, again following an exponential decay. Eq. (4) is used again to determine the radiosonde temperature without illumination. The actual resulting $\Delta T$ is determined as the difference between the fitted equilibrium temperature rise under illumination (the green line in Fig. 11) and the average of the two background temperatures before and after the exposure period, which are indicated by the blue and orange lines in Fig. 11, respectively.

Another advantage of the fitting procedure is that it is possible to determine $\Delta T$ even when the thermal equilibrium is not reached during the exposure. This allows to keep the exposure periods reasonably short, especially in case of low pressure and ventilation speed, where it takes several minutes to reach the equilibrium.

The resulting $\Delta T$ does not depend on the accuracy of the absolute temperature measurement of the radiosonde and the reference thermistors, because the evaluation relies on differences. As a result, the uncertainty from that analysis step is small (see Fig. 11 and Sect. 4.3), because it depends mainly on the reproducibility of the indicated sonde temperature before and after exposure, and to a small extent on the formal uncertainty of the fit parameter $c_0$ or the sensor intrinsic noise and resolution. The larger final uncertainty is associated with the systematic uncertainties of the experimental pressure and ventilation values to which the actual $\Delta T$ is assigned (Sect. 4.3).

\section{Data reduction and evaluation}

Both pressure (or air density) and air speed determine the efficiency of the ventilation and thereby the exchange of sensible heat between the surface of the sensor and sensor boom and the ambient air. This heat exchange depends on the thermodynamic and fluid-dynamic properties of air, as well as on the turbulent flow around the sensor, which in turn is influenced by the sensor shape and the flow direction (see e.g. Luers, 1990). In our analysis we use a simplified parameterisation of the dependence of $\Delta T$ on the ventilation parameters $p$ and $v$, which relies on the well-known effect that the convective heat transfer is more efficient for higher values of $p$ and $v$.

For most cases the dependence of $\Delta T$ on $p$ or $v$ follows a $x^{-b}$ relation, where the value of $b$ lies between 0.30 and 0.65. The curves in Fig. 12 indicate this for pressures > 20 hPa and typical in-sounding ventilation speeds of > 3 m s$^{-1}$. For lower pressures or ventilation speeds, this relation no longer holds as is illustrated by the significantly faster rise of $\Delta T$ (see blue and black lines in the left panel). Inspired by this general behaviour, a two-dimensional polynomial function for $\Delta T$, dependent on the square root inverse of the pressure and ventilation speed, is fitted for each incidence angle to the measured $\Delta T(p,v)$ data set:

$$\Delta T(p,v) = \sum_{i,j} c_{ij} \left( \frac{1}{\sqrt{p}} \right)^i \left( \frac{1}{\sqrt{v}} \right)^j.$$

The units for $p$ and $v$ are hectopascal and metre per second, respectively. Prior to fitting, data points with $\Delta T = 0.01$ K at $v = 50$ m s$^{-1}$ are added over the entire pressure range (not shown in Fig. 13) for all data sets. This ensures that the fit is constrained so that the results comply with the expectation of a smooth and monotonic decrease in $\Delta T$ at large $v$ and allows estimating reasonable values in the high-ventilation and low-pressure range where no measurement data are available.

In the left panel of Fig. 13, the fit according to Eq. (5) is visualised as grey surface, based on the same data as in Fig. 12. The red-shaded part of the surface indicates the range of realistic ventilation speeds occurring during real soundings. The blue surfaces in the right panel represent uncertainty estimates and are discussed in Sect. 4.3. The visualisation in Fig. 13 is intended to give a first overview of the distribution and scatter of the data points. The fits were created for all of the illumination configurations, i.e. for the five incident angles 0, 20, 40, and 59°, as well as zenith, and for the diffuse setup. The two zenith and diffuse configurations were each averaged as explained in Sect. 2.3.5 and 2.3.6.

The irradiances are slightly different for the data sets of the different illumination configurations. Using the proportionality of $\Delta T$ with the amount of radiation, the results of these runs can be compared after normalisation to an irradiance reference value. Figure 14 shows example data at two ventilation and pressure levels in this pre-evaluated form, where
the ΔT values from Eq. (5) are normalised (linearly scaled) to an arbitrary value of 1361 W m$^{-2}$. The plots disclose that the ΔT values for angles between 0 and 59° are consistent. That is, the temperature error does not vary systematically with incidence in that range. The 90° curves (Sun at its zenith) show somewhat increased values at both low pressure ($<10$ hPa) and ventilation speed ($<3$ m s$^{-1}$). Thus, the measurement results show a fair overall compatibility with the simple geometry-based model presented in Fig. 9.

Figure 14 includes curves labelled “diff”, which lie – to a large extent significantly – above the groups of curves for the different incidence angles. These are the results from the particular experimental configuration where the effect of diffuse radiation is simulated. The heating of the temperature sensor is maximal when the sensor boom is irradiated perpendicularly without rotation, as expected. Translated to the in-flight conditions that means that the temperature effect by diffuse radiation corresponds to a perpendicular incidence of direct radiation with the same irradiance (radiant flux received by a surface per unit area) and therefore represents the maximum achievable effect, since the heat flux by diffuse light to the sensor is essentially independent on its orientation (no cosine effect). This is accordingly taken into account in the derivation of the operational radiation correction in the GRUAN RS41 processing.

In Fig. 14b and d the ΔT values are plotted against $p^{-1/2}$ and $v^{-1/2}$, respectively. The relatively small deviation of the curves from linearity in this representation of the results in
Figure 14. Solar temperature error for various radiation incidence angles ($\alpha_s$). $\Delta T$ from Eq. (5) is normalised, i.e. linearly scaled, for each $\alpha_s$ to an irradiance equivalent to the solar constant (1361 W m$^{-2}$) beforehand. Upper row: examples for ventilation levels of 2 and 7 m s$^{-1}$; (a) pressure as x axis; logarithmic scale for better visibility; (b) plot vs. $1/p^{1/2}$. Lower row: examples for pressure levels of 5 and 100 hPa; (c) ventilation as x axis; (d) plot vs. $1/v^{1/2}$. Shaded areas around the graphs denote 1σ-uncertainty estimates.

dicates that the measurement data can be approximated well with Eq. (5); i.e. a parameterisation with such a polynomial is justified.

4.3 Uncertainties

The uncertainty of the measured temperature error, $u(\Delta T)$, is a combination of four main components.

- Uncertainty associated with the analyses of individual radiation-induced temperature steps; see Fig. 11. This component consists of several sub-components, including the uncertainty of the parameters $c_0$ for both the up and down fits to the flanks of the temperature steps using Eq. (4), the random $T$ noise during the period before shutter opening, and the offset between the two shadow temperatures enclosing the light phase. Its magnitude is generally small and considered uncorrelated.

- Uncertainty connected to radiation (3.4 %, $k = 1$; see Sect. 2.3.7, uncorrelated). Due to the linear relationship between irradiance and $\Delta T$, this component is equivalently given as relative.

- Uncertainty of pressure (0.4–0.6 hPa), considered systematic (correlated). Pressure uncertainty is converted to temperature uncertainty via the local sensitivity $\frac{\partial(\Delta T)}{\partial p}$ from Eq. (5).

- Uncertainty of ventilation speed, set to a constant value of 0.5 m s$^{-1}$ ($k = 1$) and considered systematic (correlated). Ventilation uncertainty is converted to temperature uncertainty via the local sensitivity $\frac{\partial(\Delta T)}{\partial v}$.

Of these four components, the uncertainty of ventilation speed contributes the most to the combined uncertainty $u(\Delta T)$.

The results for the two respective realisations (front and back side of the sensor boom) of both the zenith and the diffuse settings are averaged before use in the further processing, as noted in Sect. 2.3.5 and 2.3.6. The uncertainty of these averages is estimated as the combination of the indi-
individual uncertainties and a component $u(\Delta T)_{av} = [(\Delta T)_a - (\Delta T)_b]/\sqrt{3}$, which expresses that the value lies with equal probability in the range between $(\Delta T)_a$ and $(\Delta T)_b$ (GUM, 2008).

The uncertainties associated with the measured $\Delta T$ cannot be easily represented as a function of pressure and ventilation. Instead, as a practical approach, the uncertainties for each of the eight experimental setups are 2D-interpolated onto a regular grid using a kriging procedure. The grid points are distributed linearly for ventilation (21 points between 0 and 12 m s$^{-1}$) and with logarithmic spacing for pressure (21 points between 2.72 and 1096.63 hPa). The interpolated uncertainties are then stored in $21 \times 21$ point data arrays, which are used as lookup tables for further evaluation.

Before creating these arrays, artificial $u(\Delta T)$ points are added in the $(p,v)$ plane where no measured $\Delta T$ values are available, with a spacing similar to that of the measured data. They are assigned a value of 10% of the $\Delta T$ values, which were calculated using Eq. (5). At $v = 0.1$ m s$^{-1}$ and extending over the whole pressure range, further points are added to populate the edge of the $(p,v)$ plane where ventilation approaches zero. The values are defined as 3 times the $\Delta T$ at $v = 1$ m s$^{-1}$, which mimics the expected sharp increase in $u(\Delta T)$ at vanishing flow speed. Additionally, an absolute lower boundary of 0.03 K is defined for $u(\Delta T)$. This procedure is justified as a practical approach to get meaningful results from the kriging and thus to provide useful uncertainties also for those $(p,v)$ ranges, which are not covered by the measured data.

An example for the combined uncertainties of $\Delta T$ is visualised in the right panel of Fig. 13. The black dots show the measured $\Delta T$ as deviation from the model fit, and the blue surfaces denote the $u(\Delta T)$ array as $\pm \sigma$ uncertainties. They do not exceed $\sim 0.2$ K at the lowest pressures and for ascent-realistic ventilation speeds higher than about 3 m s$^{-1}$, and the majority of the residual points are within the volume spanned by the uncertainty surfaces. The plot shows that the measurement uncertainty increases significantly at low pressures ($<10$ hPa) and especially at low ventilation speed ($<2$ m s$^{-1}$). Another example is shown in Fig. 14, with the shaded areas indicating $1\sigma$-uncertainty bands. Similarly to the $\Delta T$, the uncertainties were linearly scaled for the actual radiation correction to match the different atmospheric irradiance levels.

5 Simulation of the radiation field

The actinic flux is needed to relate the laboratory characterisation of the temperature sensor’s susceptibility to radiation to the actual temperature error. Since coincident in situ measurements of the solar radiation at the time of the radiosounding are not available, the actinic flux is estimated using the radiative transfer model (RTM) Streamer (see Key and Schweiger, 1998; Key, 2002). The Streamer model was designed to calculate broadband upwelling and downwelling fluxes in 24 shortwave and 105 longwave bands for a wide range of atmospheric conditions, using a plane-parallel atmosphere and a flat surface. The model supports surface albedo, gas absorption, and scattering from ice, water, and mixed-phase clouds, for atmospheric profiles up to 100 layers.

The Streamer model was used in the GRUAN processing for the Vaisala RS92 radiosonde data to estimate the radiation fluxes (see Section 5.2.2 in Dirksen et al., 2014). However, in the data processing of the RS41 radiosonde data, several substantial changes have been introduced. The key improvements include

- the integration of the model’s fast code in the GRUAN data processing for each radiosonde profile to enable on-demand calculations;
- the use of the actual measured position, pressure, temperature, and humidity data and the use of representative values of the surface albedo in terms of location and season;
- the consideration of variable solar angles along the balloon’s trajectory; and
- an improved handling of situations of low solar-elevation angles to improve the handling of the Earth’s curvature in Streamer.

These points are explained in more detail in the following. As mentioned before, the GRUAN radiation correction only considers the shortwave fluxes.

5.1 Model input parameters

The model’s input profiles of pressure, temperature, and relative humidity are taken from the actual radiosonde measurement. Information on the surface albedo is taken from a global data set, and a generic, representative cloud scenario is defined by cloud layers close to the surface and the tropopause, respectively.

The radiosonde profile, which has a vertical sampling of $\sim 5$ m, is mapped onto the much coarser resolution of the model by selecting the data point with the nearest altitude for each of the 100 model layers. The vertical resolution (thickness of the model layers) depends on altitude and is highest at the surface (see Table 4). The measured radiosonde profiles are extended to 52 km by inserting a standard profile above the burst point (see chap. 15 in Key, 2002). Latitude-dependent standard profiles are available for the tropics ($\phi < 23.43^\circ$), mid-latitudes (summer and winter, $23.43^\circ \leq \phi < 66.56^\circ$), and the Arctic ($\phi \geq 66.56^\circ$).

A map that incorporates the spatial and temporal variability of the surface albedo is derived from a satellite-based data set provided by Karlsson et al. (2017). Data from January 2005 to December 2015 are used to generate monthly averages of the broadband surface albedo between 0.25 and 2.5 $\mu$m, at a spatial resolution of $0.25^\circ \times 0.25^\circ$ (shown in
Figure 15. (a) Map of the monthly averaged global surface albedo between 0.25 and 2.5 µm for the month of June, used for the processing of a radiosounding performed at Lindenberg on 11 June 2020, 12:00 UTC. (b) Annual cycle of the monthly averaged albedo at GRUAN sites of various geographical latitudes.

Table 4. Vertical resolution of the Streamer model.

<table>
<thead>
<tr>
<th>Altitude range (km)</th>
<th>Resolution (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0–5</td>
<td>250</td>
</tr>
<tr>
<td>5–21</td>
<td>500</td>
</tr>
<tr>
<td>21–36</td>
<td>1000</td>
</tr>
<tr>
<td>36–52</td>
<td>2000</td>
</tr>
</tbody>
</table>

Table 5. RTM input parameters for the cloud layer scenario.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Layer 1</th>
<th>Layer 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Phase</td>
<td>liquid</td>
<td>ice solid column</td>
</tr>
<tr>
<td>Cloud optical thickness</td>
<td>15.7</td>
<td>1.1</td>
</tr>
<tr>
<td>Water content</td>
<td>0.1 g m$^{-3}$</td>
<td>0.01 g m$^{-3}$</td>
</tr>
<tr>
<td>Top of cloud</td>
<td>3.0 km</td>
<td>tropopause</td>
</tr>
<tr>
<td>Cloud thickness</td>
<td>1.0 km</td>
<td>2.0 km</td>
</tr>
</tbody>
</table>

5.1.1 Cloud scenario

Owing to their high reflectivity and light-scattering properties, clouds can considerably alter the effective albedo of a scene. The inherently large spatio-temporal variability of the cloud cover, without having accurate information on its actual configuration, constitutes a substantial source of uncertainty when estimating the actinic flux onto the radiosonde. As a compromise, a radiation profile which is the average of two extremes, a cloudy and a clear-sky situation, is constructed for each radiosounding.

The cloudy scenario consists of two separate cloud layers, whose properties are listed in Table 5: an optically thick, wet, low-level cloud at 3 km above the surface and an ice cloud underneath the tropopause. The latter requires tropopause detection by the data processing. In case of an early balloon burst below the tropopause, a tropopause altitude of 7.5 km is assumed. For the clear-sky case the same parameter settings of the model atmosphere are used, but without the cloud definitions.

5.1.2 Solar-elevation angle during ascent

The radiation field depends strongly on the solar-elevation angle $\alpha_s$, and since the solar elevation changes continuously with time, sometimes influenced by the horizontal drift of the balloon, this angle needs to be calculated for every data point of the ascent. For accurate evaluation of $\alpha_s$, the GRUAN data processing uses the Solar Position Algorithm (SPA) by Reda and Andreas (2003, 2004).

Quick changes of the solar radiation occur at sunrise or sunset, when the Sun crosses the horizon. However, at small negative values for $\alpha_s$, i.e. if the Sun is just below the horizon for an observer on the ground, the Sun can still illuminate the radiosonde. The shift of the day–night limit with altitude is illustrated in Fig. 16, which shows that sunset ($\alpha_s = 0$) occurs for the ground-based observer when the radiosonde is at 5 km altitude but that the radiosonde was illuminated until 11.5 km altitude, when the Sun was already more than $4^\circ$ below the horizon. Because Streamer assumes a plane-parallel surface and atmosphere, negative $\alpha_s$ values are associated with the nighttime situation. To resolve this, $\alpha_s$ is transformed to a small positive value, equivalent to the
Sun being just above the horizon, as experienced by the radiosonde. The transformation of $\alpha_s$ and solar zenith angle $\theta_s$ goes as follows: assuming the Earth to be a perfect sphere, the angle below the horizon at which the centre of the solar disc is still visible at altitude $h$ is given by

$$\alpha_{\text{cor}} = \arccos \frac{R}{R + h},$$

(6)

with $R$ the Earth’s radius. Using $R \approx 6.371 \times 10^6$ m, this can be approximated by

$$\alpha_{\text{cor}} \approx 0.0321 \cdot \sqrt{h},$$

(7)

with $h$ in metres. The transformed zenith angle $\theta_s'$ is given by

$$\theta_s' = \theta_{s,\text{lim}} + (\theta_s - \theta_{s,\text{lim}}) \cdot f_{hc},$$

(8)

with $\theta_{s,\text{lim}} = 85^\circ$, and

$$f_{hc} = \frac{90 - \theta_{s,\text{lim}}}{90 - \theta_{s,\text{lim}} + \alpha_{\text{cor}}},$$

(9)

This horizon correction is applied to zenith angles $\theta_s$ exceeding $\theta_{s,\text{lim}}$, which means that it is also applied when the Sun is still above the horizon. This compensates for Streamer’s overestimation of the absorption at low $\alpha_s$ due to the plane-parallel atmosphere.

### 5.2 Simulation and results

A typical radiosonde ascent takes about 90 min to reach the balloon burst point, during which horizontal drifts of more than 100 km from the launch point are not unusual (Seidel et al., 2011). Depending on location and time of the ascent, the solar-elevation angle $\alpha_s$ can vary over more than $15^\circ$ during the flight. To account for the effect of these changes on the radiation field, Streamer calculations are performed for the range of solar-elevation angles encountered in flight at steps of $0.5^\circ$. For each step, the cloudy and the cloud-free scenario are simulated. To reduce the computational effort, the simulation depth and accuracy are reduced by using the simple two-stream solver. The simulated profiles for each solar-elevation angle are stored in a lookup table (LUT). Radiation flux components are estimated for each data point of the ascent by linear interpolation from this LUT.

The Streamer model produces profiles of downward direct ($I_{\text{dir}}$) and diffuse upward ($I_{\text{dif,up}}$) and downward ($I_{\text{dif,down}}$) radiation for both the cloudy and the clear-sky scenarios. The diffuse radiation used for the final temperature correction is the sum of the upward and downward components,

$$I_{\text{dif}} = I_{\text{dif,down}} + I_{\text{dif,up}},$$

(10)

under the assumption that both sides of the sensor boom are equally sensitive to solar radiation (Sect. 2.3.6).

The radiation flux profiles $I_{\text{dir}}$ and $I_{\text{dif}}$ are constructed from the average of their respective cloudy (cl) and clear-sky (cs) cases,

$$I_{\text{dir}} = \frac{1}{2} (I_{\text{dir,cs}} + I_{\text{dir,cl}}), \quad I_{\text{dif}} = \frac{1}{2} (I_{\text{dif,cs}} + I_{\text{dif,cl}}),$$

(11)

with the associated $k=1$ uncertainties for a rectangular a priori distribution bound by both extremes:

$$u(I_{\text{dir}}) = \frac{|I_{\text{dir,cs}} - I_{\text{dir,cl}}|}{2\sqrt{3}}, \quad u(I_{\text{dif}}) = \frac{|I_{\text{dif,cs}} - I_{\text{dif,cl}}|}{2\sqrt{3}}.$$  

(12)

To account for the reduced model accuracy in favour of faster computing time, a lower limit of 5% was imposed on the uncertainty in $I_{\text{dir}}$ and $I_{\text{dif}}$:

$$u_{\min}(I_{\text{dir,dif}}) = 0.05 \cdot I_{\text{dir,dif}},$$

(13)

based on sensitivity tests of the Streamer model. Because of the above-mentioned limitations of Streamer, $u_{\min}$ is doubled for solar-elevation angles smaller than $5^\circ$.

Figure 17 shows an example of profiles of simulated direct and diffuse solar radiative fluxes for the cloudy and clear-sky scenarios, as well as the mean across both (black lines), and the uncertainty estimates (shaded areas; see Sect. 6.2). The employed cloud model, with a layer at a few kilometres above ground and another one just below the tropopause, leads to considerably different radiation fluxes compared to the clear-sky case. In particular, multiple scattering significantly amplifies the diffuse radiation in the altitude range between the cloud layers. Therefore, especially in that altitude range in the troposphere, the simulated fluxes from the two scenarios may be seen as extremes for the range of radiative fluxes that may occur for real cloud configurations.
The uncertainty of the simulated radiation fluxes is essentially derived from the difference of these boundary scenarios and therefore significantly larger in the troposphere than in the stratosphere.

6 RS41 solar radiation correction and implementation in the GRUAN data product

The correction algorithm calculates the bias $\Delta T_{rad}$ for each data point by combining the experimentally derived radiation sensitivity of the temperature sensor $\Delta T(p,v)$ from Eq. (5) and the modelled radiation profiles given by Eq. (11). The total sensor heating is then evaluated as the sum effect of the components from the diffuse and the direct radiation.

6.1 Correction

6.1.1 Direct radiation

The direct radiation $I_{dir}$ is provided by the RTM on the altitude grid of the sounding profile. The input parameters $p$, ventilation speed $v$, and the solar-elevation angle $\alpha_s$ are derived from the actual sounding data, where $\alpha_s$ follows from the time of the measurement, GPS altitude, and geographical position of the radiosonde. The pressure $p$ is calculated based on GPS altitude and the temperature and humidity profiles under the assumption of hydrostatic equilibrium. The ventilation speed is calculated by combining the ascent speed, which is derived from GPS altitude changes, and an effective horizontal speed component, which is caused by the pendulum-related oscillations around the mean horizontal trajectory. The temperature effect $\Delta T_{dir,exp}$ (Eq. 5) due to direct radiation is experimentally determined for five different solar-elevation angles $\alpha_{s,exp}$. These are used as support points for the determination of the final temperature bias $\Delta T$ at any given angle by nearest-neighbour interpolation. Thus, the part of the bias associated with direct radiation is

$$\Delta T_{dir}(p,v,\alpha_s) = \frac{I_{dir}}{I_{exp}} \cdot \Delta T_{dir,exp}(p,v,\alpha_s),$$

using the linear response for scaling the temperature effect from the fixed experimental radiation settings $I_{exp}$ to the modelled radiation $I_{dir}$.

6.1.2 Diffuse radiation

Similar to the direct radiation, $I_{dif}$ is provided by the Streamer model on the altitude grid of the sounding profile, and $p$ and $v$ are taken from the actual sounding data as described in Sect. 6.1.1. The solar-elevation angle $\alpha_s$ is not needed in the calculation of $\Delta T_{dif}$ because of the aforementioned anisotropy of the diffuse radiation. Instead $\Delta T_{dif}(p,v)$ follows from Eq. (5), using the coefficients derived for diffuse experimental setup and by linear scaling with the modelled diffuse flux:

$$\Delta T_{dif}(p,v) = \frac{I_{dif}}{I_{exp}} \cdot \Delta T_{dif,exp}(p,v).$$

6.1.3 Overall radiation correction

The calculated radiation error, which is subtracted from the raw temperature profile, for each data point is given by

$$\Delta T_{rad} = \Delta T_{dir} + \Delta T_{dif},$$

yielding the corrected temperature

$$T_{rc} = T_{raw} - \Delta T_{rad}.$$
site in summer. The total bias (red curve) is approximately 0.1 K at ground level and increases to more than 0.2 K towards the tropopause (at approximately 11 km), making it a non-negligible effect throughout the troposphere. The apparent discontinuities at 2, 3, and 11 km are caused by the two cloud layers used in the radiation model. As a result of the enhanced diffuse radiation between these cloud layers, the diffuse portion of the radiation bias (green trace) exceeds that for direct radiation (blue trace) in the troposphere. Above the tropopause, the bias increases steadily to reach approximately 0.8 K at 35 km, with the portion from direct radiation being the dominant contribution.

In Fig. 18, large-scale oscillations occur above ~25 km. Similar patterns are observed above the tropopause in numerous soundings. These are attributed to ascent speed variations caused by gravity waves. The calculated ventilation speed \( v \) that is used in the radiation correction is based on the ascent speed, which in turn is derived from the GPS measurements. In the case of gravity waves or other vertical air movements, this ascent speed can be different from the ventilating air speed at which the balloon rises through the air.

Uncertainties, which are further discussed in Sect. 6.2, are indicated in Fig. 18 as shaded areas in the left panel and as graphs for individual components in the right panel. The uncertainty due to pressure is less than 0.01 K over the entire profile, whereas above the tropopause the contributions from ventilation, radiation modelling, and laboratory experiments are of comparable magnitude. The uncertainty in the troposphere is dominated by the uncertainty in the estimated radiation profile, which is caused by the absence of information on the actual cloud configuration at the time of the sounding.

Figure 19 shows that the ensemble of estimated error profiles for a set of 154 daytime soundings is, on a first approximation, fairly similar to the individual profile shown in Fig. 18. The median (red trace in Fig. 19) exhibits the same trend in the stratosphere, with nearly the same value at 35 km (approximately 0.75 K), and the oscillations that are attributed to gravity waves are obviously absent due to the averaging. The slight spread in the data above 25 km is possibly due to seasonal variations of the solar-elevation angle, but this is the subject of further investigation. The increased variability of the data between 2 and 12 km is also attributed to the seasonal spread in the radiation profile due to the strong dependence of the diffuse radiation on the solar-elevation angle.

6.2 Uncertainty of the radiation correction

The following components contribute to the overall uncertainty estimate \( u(\Delta T_{rad}) \) for the radiation correction (note that “\( \Delta \)” denotes differences, not uncertainties):
1. Uncertainties from the laboratory experiments \( u(\Delta T_{\text{exp}}) \) (Sect. 4.3 and Table 3) and uncertainties from radiation modelling, \( u(I_{\text{RTM}}) \) (Eq. 12), combined as

\[
u(\Delta T_{\text{exp,RTM}}) = \Delta T_{\text{exp,RTM}} \cdot \sqrt{\left( \frac{u(\Delta T_{\text{exp}})}{\Delta T_{\text{exp}}} \right)^2 + \left( \frac{u(I_{\text{RTM}})}{I_{\text{RTM}}} \right)^2}.
\] (18)

2. Uncertainties of pressure and ventilation in the actual radiosonde profile, converted to temperature uncertainties:

\[
u(\Delta T_p) = \left| \frac{\partial(\Delta T)}{\partial(p)} \right| \cdot u(p),
\]

\[
u(\Delta T_v) = \left| \frac{\partial(\Delta T)}{\partial(v)} \right| \cdot u(v),
\] (19)

where the sensitivities are the partial derivatives of Eq. (5) with respect to \( p \) and \( v \), respectively.

3. Combination of the components in Eqs. (18) and (19),

\[
u(\Delta T_{\text{dir,dif}}) = \sqrt{u^2(\Delta T_p) + u^2(\Delta T_v) + u^2(\Delta T_{\text{Exp,RTM}})}.
\] (20)

where the subscript “dir,dif” in Eq. (20) indicates that the preceding steps were carried out equivalently for both the direct and diffuse radiation components \( I_{\text{dir}} \) and \( I_{\text{dif}} \).

The overall uncertainty of the radiation correction (Eq. 16) is the combination of these two:

\[
u(\Delta T_{\text{rad}}) = \sqrt{u^2(\Delta T_{\text{dir}}) + u^2(\Delta T_{\text{dif}}) + 2 \cdot \frac{\partial(\Delta T_{\text{dir}})}{\partial I_{\text{dir}}} \cdot u(I_{\text{dir}}) \cdot \frac{\partial(\Delta T_{\text{dif}})}{\partial I_{\text{dif}}} \cdot u(I_{\text{dif}})}.
\] (21)

It is assumed that the uncertainties of the direct and diffuse RTM results are strongly correlated because the occurrence of diffuse shortwave radiation is naturally linked to that of the direct light from the Sun. This is considered in Eq. (21) with a correlation term (GUM, 2008), assuming a correlation coefficient of \( r = 1 \). The sensitivities in that term are derived from Eqs. (14) and (15) as

\[
\frac{\partial(\Delta T_{\text{dir}})}{\partial I_{\text{dir}}} = \frac{\Delta T_{\text{dir}}}{I_{\text{dir}}}, \quad \frac{\partial(\Delta T_{\text{dif}})}{\partial I_{\text{dif}}} = \frac{\Delta T_{\text{dif}}}{I_{\text{dif}}}.
\] (22)

7 Comparison with manufacturer correction

To evaluate the GRUAN data processing, the GRUAN data product (GDP) for temperature is compared to the Vaisala data product (EDT) for a selection of 154 daytime and 81 nighttime soundings that were performed at Lindenberg observatory between 2014 and 2021. For each sounding, the differences between both products were gridded in 1000 m wide altitude bins, which were used to collate the statistically averaged difference profile for all soundings. In the analysis the measurement uncertainties of the data were taken into account. The GRUAN-processed data contain for each data point an estimate of the uncorrelated uncertainty together with the correlated uncertainties in the spatial and temporal domains, where the latter two include the constant contribution from the calibration uncertainty of the temperature sensor. This latter contribution is not relevant for the comparison of the radiation temperature correction of the same sensor by two different algorithms and leads to an overestimation of the resulting uncertainty. Therefore, for this analysis only the correlated uncertainties related to the radiation correction as well as the uncorrelated uncertainties were used. The uncorrelated uncertainties of the profile data averaged over a 1000 m altitude bin are added using the standard uncertainty of the mean,

\[
u_{\text{uncorr}}(T) = \frac{1}{N} \sqrt{\sum_{i=1}^{N} \nu_{i,\text{uncorr}}^2(T_i)},
\] (23)

and the correlated uncertainty for the altitude bin is given by the mean of the correlated uncertainties,

\[
u_{\text{corr}}(\Delta T_{\text{rad}}) = \frac{1}{N} \sum_{i=1}^{N} \nu_{i,\text{corr}}(\Delta T_{\text{rad},i}).
\] (24)

The total uncertainty for each altitude bin follows from the sum of the squares of the constituting components:

\[
u(T_{\text{GDP}} - T_{\text{EDT}}) = \sqrt{\nu^2_{\text{uncorr,GDP}}(T) + \nu^2_{\text{corr,GDP}}(\Delta T_{\text{rad}}) + \nu^2_{\text{uncorr,EDT}}(T) + \nu^2_{\text{corr,EDT}}(\Delta T_{\text{rad}})}.
\] (25)

where the altitude-dependent correlated uncertainties of the Vaisala product \( \nu_{\text{corr,EDT}}(\Delta T_{\text{rad}}) \) are less than 0.2 K \( (k = 1) \) at 35 km (Vaisala, 2013; Hannu Jauhiainen, personal communication, 2021). Due to the large number of data points \( N \), \( \nu_{\text{uncorr}}(T) \) vanishes, so that the resulting total uncertainty reduces to \( \nu_{\text{corr}}(\Delta T_{\text{rad}}) \).

The plot in Fig. 20a shows a good correspondence between the nighttime temperatures over the entire profile. In the troposphere the GRUAN profile is slightly warmer than Vaisala, with the median of the difference smaller than 0.05 K. Since neither GRUAN nor Vaisala processing apply a radiation correction for nighttime soundings, the observed difference is attributed to the time-lag correction that is applied in the Vaisala processing. As a consequence of the absent radiation correction for the nighttime measurements, the resulting uncertainties also reduce to zero and are therefore not visible in Fig. 20a.

The plot in Fig. 20b shows that GRUAN-processed daytime profiles are up to 0.1 K warmer in the troposphere, and
above the tropopause (approximately 10 km) the temperature difference steadily increases, with the GRUAN profile 0.35 K warmer at 35 km. The observed daytime differences between the GRUAN and Vaisala-processed data are within their combined uncertainty range for $k = 2$:

$$|T_{\text{GDP}} - T_{\text{EDT}}| < k \cdot \sqrt{u^2(\Delta T_{\text{rad,GDP}}) + u^2(\Delta T_{\text{rad,EDT}})},$$

where $k = 2$, meaning that according to the classification scheme proposed by Immler et al. (2010), both data products are, albeit barely, in agreement.

8 Summary and conclusions

The paper presents SISTER, a setup that was developed to quantify the solar heating of the temperature sensor of radiosondes under laboratory conditions by recreating atmospheric and illumination conditions that are encountered during a daytime radiosounding ascent. The resulting parameterisation of the radiation error as a function of pressure, ventilation speed, solar angle, and actinic flux is applied in the GRUAN processing for radiosonde data. It relies on the extensive characterisation of sensor properties to produce a traceable reference data product which is free of manufacturer-dependent effects. The GRUAN radiation correction model combines the laboratory characterisation with model calculations of the actual radiation field during the sounding to estimate the correction profile. The second part of the paper describes how this procedure was applied in the development of the GRUAN data product for the Vaisala RS41 radiosonde (version 1, RS41-GDP.1).

SISTER controls the pressure (3 to 1020 hPa) and the ventilation speed (0 to 7 m s$^{-1}$) of the air inside the setup to simulate the conditions between the surface and 35 km altitude, to determine the dependence of the radiation temperature error on the irradiance and the convective cooling. The radiosonde is mounted inside a quartz tube with the sensor boom unfolded in a flight-like configuration, while a 20 cm wide beam from an external 2500 W light source illuminates the complete sensor boom of the radiosonde to include the conductive heat transfer between sensor and boom. A special feature of SISTER is that the radiosonde is rotated around its axis to imitate the spinning of the radiosonde in flight. The averaging due to this rotation yields the sensor heating that depends on the effective exposed surface of the sensor boom. The irradiance geometry can be adjusted to accommodate solar-elevation angles of 0 to 60° and, in addition, 90°. A special configuration was used to quantify the heating due to diffuse radiation. LDA characterisation of the airflow inside the quartz tube showed a predominantly laminar flow in the longitudinal direction, with a velocity profile typical for a tubular flow. The LDA measurements were also used to calibrate the speed of the airflow at the position of the radiosonde between 20 and 1000 hPa. Measurements are performed for various pressures, ventilation speeds, and illumination angles, yielding a 2D parameterisation of the radiation error for each illumination angle. The uncertainty of this parameterisation is less than 0.2 K for typical ventilation speeds of 3 to 7 m s$^{-1}$.

The GRUAN data processor calculates the direct and diffuse shortwave radiation profiles using the embedded Streamer RTM, where the temperature and humidity profiles are taken from the actual sounding data. By lack of accurate cloud information, a generic cloud scenario is used, which increases the uncertainty of the radiation profile. The averaged correction profile increases gradually from 0.1 K at the surface to approximately 0.8 K at 35 km altitude. Comparison between sounding data that were GRUAN-processed
(GDP) and Vaisala-processed (EDT) reveals no differences for nighttime soundings, where the radiation correction is not applied, apart from a small offset in the troposphere that is attributed to the time-lag correction applied by Vaisala. The daytime differences are smaller than $+0.1\,\text{K}$ (GDP $-$ EDT) in the troposphere and increase above the tropopause steadily with altitude to $+0.35\,\text{K}$ (GDP $-$ EDT) at 35 km. These values are just within the limits of the combined $k=2$ uncertainties of both data products, which means that the GRUAN processing and the Vaisala processing are in agreement. It is not possible to determine which of the two data products performs better, although the GDP represents the best effort for the characterisation and correction of the radiation temperature error. This unresolved finding exemplifies the need for an independent reference instrument for in situ temperature measurements.

In its current form the correction algorithm uses a standardised cloud scenario in the estimation of the radiation profile, which as a result has a considerable uncertainty, especially in the troposphere. The accuracy of the estimated radiation profile could be greatly improved if real-time information on the actual cloud configuration during the sounding were available. A potential source for in-flight cloud information is the measured humidity profile. For air temperatures above freezing, 100% humidity indicates the presence of wet-phase clouds. However, at lower temperatures this approach has its limitations because the presence of ice-phase clouds cannot unambiguously be established from the humidity profile. Furthermore, the humidity profile provides in situ information on cloud presence, which would be sufficient for a homogeneous cloud cover but insufficient in case of scattered clouds or if the cloud scenario changes along the balloon’s trajectory. The latter could be resolved by using additional cloud information from an external source, such as satellite observations. The incorporation of space-borne cloud information would require the collection of the appropriate data covering the time of each sounding and their integration into the processing, which is a complicated effort. Still, such an extension is considered for a future version of the GRUAN processing, which despite its complexity is expected to considerably improve the accuracy of the radiation correction.

The SISTER setup is designed for measurements at room temperature, and contrary to, e.g. the upper air simulator described by Lee et al. (2020), it does not have the option to cool the radiosonde or the chamber to simulate the temperature conditions at the tropopause. Because of the $T^4$ dependence, the emitted power by longwave radiation at $-60\,\text{°C}$ is approximately 4 times smaller than at room temperature. This reduced cooling efficiency at low temperatures may modify the heat budget resulting in an increase in the radiation temperature error. However, an exact quantification of this effect is complicated and requires further investigation. According to Luers and Eskridge (1995), the heat exchange by longwave radiation of a sensor boom with metallic coating is considerably smaller than the other contributions to the sensor’s heat budget, such as the shortwave radiative heating and the convective cooling. On the other hand, Lee et al. (2018b) reported a considerable temperature increase for an irradiated aluminium-coated thermistor at low temperatures. However these experiments were performed without ventilation, and there are notable differences between the designs of the sensor booms of the RS41 and the dual thermistor used in Lee’s study. Nevertheless, recent findings by the Korea Research Institute of Standard and Science (KRISS) confirm an increase in the radiative sensor warming with decreasing temperature at low pressure, which is mainly caused by the reduction of the convective heat transfer at low temperatures (Yong-Gyoo Kim, personal communication, 2021; Lee et al., 2021). If corroborated, this effect will be accounted for in the next version of the GRUAN data processing for the RS41.

Figure 18 shows that vertical air movements such as gravity waves can cause disparities between the GPS-based ascent speed and the actual speed of the balloon rising through the surrounding air, which in turn introduces oscillations in the temperature correction profile. These oscillations can lead to a temporary under- or overcorrection of the radiation temperature error, which affects the quality of the data product. A possible way to remedy this is by adopting the method proposed by Wang et al. (2009) for quantifying vertical air movements using still-air balloon rise rates.

Changes in the exposed area due to the rotation of the illuminated radiosonde introduce oscillations in the temperature measurements. The analysis of the laboratory experiments (Sect. 4.1) shows that the determination of the resulting radiation error is not affected by this rotation but that these oscillations are well resolved due to the fast response time of the temperature sensor and sensor boom system. This finding can be exploited to improve the radiation correction: using information on the actual orientation of the radiosonde from for example an additional, position-sensitive sensor will lead to a better estimate of the instantaneous radiation temperature error.

SISTER is designed to characterise modern radiosonde types from various manufacturers. As a consequence, it is intended to use this setup to support the development of GRUAN data products for other sonde models. First measurements with other radiosonde models have already been conducted. Consistency checks by comparing the RS41 GDP temperatures with those from (future) GDP’s of other radiosondes will be an important quality test for the presented method.

Data availability. The data from the laboratory experiments that were used for Figs. 11–13, a list to data sources for Figs. 19 and 20, and two image files showing photography on how the radiosonde is installed are stored as zip file in a permanent repository at https://doi.org/10.5676/GRUAN/dpkg-2021-1 (von Rohden et al., 2021). Further data are available upon request.
Author contributions. CvR scientifically supported the development of the experimental setup, guided and executed the measurements, analysed the data, and prepared essential parts of the manuscript. MS adapted the radiation model, implemented the radiation correction procedure in the GRUAN RS41 data processor, and prepared the related sections for the manuscript. TN initiated and led the technical development and construction of the experimental setup. VM prepared and conducted the LDA measurements. RJD performed the comparison analysis and made essential contributions throughout the manuscript.

Competing interests. The contact author has declared that neither they nor their co-authors have any competing interests.

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