Estimating errors in vehicle secondary aerosol production factors due to oxidation flow reactor response time

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Abstract. Oxidation flow reactors used in secondary aerosol research do not immediately respond to changes in the inlet concentration of precursor gases because of their broad transfer functions. This is an issue when measuring the vehicular secondary aerosol formation in transient driving cycles because the secondary aerosol measured at the oxidation flow reactor outlet does not correspond to the rapid changes in the exhaust flow rate. Since the secondary aerosol production factor is determined by multiplying the secondary aerosol mass by the exhaust flow rate, the misalignment between the two leads to incorrect production factors. This study evaluates the extent of the error in production factors due to oxidation flow reactor transfer functions using synthetic and semi-synthetic exhaust emission data. It was found that the transfer-function-related error could be eliminated when only the total production factor of the full cycle was measured using constant-volume sampling. For shorter segments within a driving cycle, a narrower transfer function led to a smaller error. Even with a narrow transfer function, the oxidation flow reactor could report production factors that were more than 10 times higher than the reference production factors if the segment duration was too short.

1 Introduction

Aerosol particles affect human health, climate, and visibility (Pöschl, 2005; Seinfeld and Pandis, 2006). Organic compounds comprise approximately 20%–90% of fine aerosol mass (Kanakidou et al., 2005), and a substantial fraction of organic aerosol originates from secondary aerosol formation (Zhang et al., 2007; Hallquist et al., 2009). The secondary organic aerosol (SOA) is formed in the atmosphere via oxidation of precursor gases. Resolving the total atmospheric SOA budget and the contributions from biogenic and anthropogenic sources is challenging, but it is estimated that the majority of SOA originates from biogenic sources (Hallquist et al., 2009).

While SOA production from biogenic sources is globally higher than that of anthropogenic sources, the organic aerosol concentrations in large cities are dominated by anthropogenic SOA. High population density combined with local precursor emission sources results in significant contribution to air pollution mortality from anthropogenic SOA (Nault et al., 2021). Nault et al. (2021) studied the health effects of anthropogenic SOA and used a set of aromatic precursor gases as a proxy for total anthropogenic organic precursor emissions in selected cities. A mass fraction of 20%–62% of these emissions originated from gasoline and diesel exhaust and fuel evaporation, which implies that vehicles are an important source of SOA in urban environments.

Vehicular SOA production is not currently directly regulated. Since SOA originates from gaseous organic compounds, limitations for hydrocarbon (HC) emissions indirectly limit SOA production, but there is no universal constant to convert the measured HC emissions to potential SOA formation in the atmosphere. Thus, reduction in HC emission does not linearly translate to reduced SOA formation. Regulating the SOA production specifically would require measuring the SOA production factors (i.e., amount of potential
SOA from emissions per fuel consumed) with smog chambers or oxidation flow reactors (OFRs).

SOA production factors (PFs) from vehicles have been measured with smog chambers by initiating a driving cycle and injecting the exhaust to the smog chamber during the cycle (e.g., Gordon et al., 2014a; Platt et al., 2013). The chambers are typically operated in batch mode so that the oxidation in the chamber is actuated after the driving cycle is finished. The advantage of smog chambers compared to oxidation flow reactors is that the oxidant concentrations are close to ambient levels, and thus the photochemistry and aerosol processes resemble tropospheric conditions better. In contrast, the oxidant concentrations in OFRs are orders of magnitude higher, which can introduce non-tropospheric effects (Peng and Jimenez, 2020). The OFRs are operated in continuous flow mode, which enables the measurement of SOA production factors with a good temporal resolution. Smog chamber experiments only provide the total SOA production factor of the driving cycle, while OFR measurements can resolve how the SOA production differs between different driving conditions within the driving cycle. However, the delay caused by the residence time of the sample in the OFR complicates the calculation of SOA production factors. In this work, we address these complications.

While it is possible to measure HC and other pollutants directly from the tailpipe with only a small delay originating from the instrument response, the response time associated with a continuous SOA measurement using an OFR is significantly longer. Considering that potential SOA is always dependent on emitted HC to some extent, a natural first approach to addressing this issue can be formulated as follows: how accurately could we estimate the HC emission by measuring HC at a (non-oxidizing) flow reactor outlet instead of measuring directly from the tailpipe?

When calculating the emission rates (g s$^{-1}$) or the total emission (g) of the exhaust gases, the gas concentrations in the tailpipe need to be multiplied by the exhaust flow rate. The total emission of gas $C$ (in g) is calculated by

$$C_{\text{emitted}} = \int_{t_0}^{t_f} [C]_{\text{true}}(t) Q_{\text{exh}}(t) \, dt,$$  \hspace{1cm} (1)

where $t_0$ and $t_f$ are the start and end times of a driving cycle or event of interest, respectively; $[C]_{\text{true}}$ is the gas concentration (g m$^{-3}$) in the tailpipe; $Q_{\text{exh}}$ is the volumetric exhaust flow rate (m$^3$ s$^{-1}$); and the product of $[C]_{\text{true}}$ and $Q_{\text{exh}}$ is the emission rate (g s$^{-1}$).

If the gas concentration (e.g., [HC]) is measured at the OFR outlet instead of the tailpipe, the emission rate and subsequently the total emission will be affected as illustrated in Fig. 1 (assuming that the OFR UV lamps are off so that none of the HC is oxidized). This is because the gas concentration is modified by the OFR residence time distribution (RTD); the gas concentration at the OFR outlet is the result of convolution of the original gas concentration and the OFR transfer function, $E$. The transfer function is the RTD of a Dirac delta input impulse (Fogler, 2006). Thus, we have the following:

$$[C]_{\text{OFR}}(t) = ([C]_{\text{true}} \ast E)(t) = \int_{0}^{t} [C]_{\text{true}}(\gamma) E(t - \gamma) \, d\gamma,$$ \hspace{1cm} (2)

where $[C]_{\text{OFR}}$ is the gas concentration at the OFR outlet (assuming no dilution) and $[C]_{\text{true}}$ is the concentration in the tailpipe. As shown in Fig. 1, the multiplication of $[C]_{\text{OFR}}$ by the exhaust flow rate does not lead to the correct emission when the exhaust flow rate is not constant. Determining the correct emission would require solving for $[C]_{\text{true}}$ from the OFR measurements. Even though the transfer function, $E$, can be determined, it is usually impossible to unambiguously solve for $[C]_{\text{true}}$ in Eq. (2) because this is an ill-posed inverse problem. Thus, it is not trivial to determine the SOA production factors from driving cycles with variable driving conditions where the exhaust flow rate is not constant.

Despite the difficulties in calculating SOA PFs with OFRs, this issue is not addressed in earlier publications (Karjalainen et al., 2016; Timonen et al., 2017; Simonen et al., 2019; Pieber et al., 2018; Zhang et al., 2023). Zhao et al. (2018) recognized the problem, but there is no analysis of the mag-
itude of error caused by the OFR transfer function. It is ne-
ecessary to estimate how large an error is caused by OFRs with
different transfer functions and to determine how best to ac-
count for the transfer function when analyzing the data.

Similar issues have been studied for situations where the ex-
haust system, sampling lines, and non-ideal instrument re-
sponse cause delay and distortion to exhaust gas or particle
measurements (Ganesan and Clark, 2001; Ajtay and Weilen-
mann, 2004; Hawley et al., 2003; Weilenmann et al., 2003;
Madireddy and Clark, 2006; Geivanidis and Samaras, 2007;
Franco, 2014; Giechaskiel et al., 2021). Mahadevan et al.
(2016) studied the error in gaseous emission factors in test
cycles due to the phenomena mentioned above. They found
that the error could be as high as 51 % when using non-
corrected data and 25 % after applying a constant time shift
to correct for the delay. The effects of delay and distortion
are significantly higher for OFRs because their dynamic re-
sponse is much slower than that of gas analyzers or trans-
portation lines.

In this study, we first present the theoretical background
for calculating the SOA PF of vehicles running a transient
driving cycle. Second, we study the OFR response in two
real driving cycles and compare different measurement and
data analysis methods. Third, we use synthetic data to further
evaluate the performance of different OFRs and data analy-
sis methods. Finally, we suggest the best practices to employ
when measuring SOA PF with OFRs and provide computa-
tional tools to test the performance of any OFR for which the
transfer function is known.

2 Theoretical background

The SOA PF defines the amount of SOA that would be
formed in the atmosphere from the emitted SOA precursor
gases, normalized to, e.g., fuel consumed or distance trav-
elved. Thus, the fuel-specific SOA PF (mg (kg fuel)−1) can be
defined as

\[
\text{SOA PF} = \frac{\text{SOA}}{\text{fuel consumed}} = \frac{\text{SOA}}{C_{\text{CO}_2} + C_{\text{CO}} + C_{\text{HC}} + C_{\text{PM}}} \cdot k',
\]

(3)

where SOA is the SOA formation potential (mg) – i.e., the
SOA that could be formed in the atmosphere from the emit-
ted precursor gases. The emitted carbon is the mass of carbon
emitted (g), which is the sum of emitted carbon mass origi-
nating from different exhaust compounds (CO2; CO; HC;
and particle-phase carbon, CPM) (Platt et al., 2013). The fuel
consumed can be obtained from vehicle on-board diagnostics
(OBD) data or by dividing the emitted carbon mass with the
fuel carbon content denoted by \(k' \) (g kg\(^{-1}\)). Since the emitted
carbon is dominated by CO2, it is a good approximation to
neglect the other forms of carbon. For simplicity, the SOA

PF in this study is defined as

\[
\text{SOA PF} = \frac{\text{SOA}}{\text{CO}_2} \cdot k,
\]

(4)

where CO2 is the emitted carbon dioxide mass and \(k = k' \cdot
44/12 \); i.e., the emitted CO2 mass is multiplied by the ratio
of carbon mass to total molecular mass in a CO2 molecule.

To simplify the analysis, we assume that the SOA forma-
tion potential is single-valued and depends only on the emit-
ted precursor gases. Furthermore, we treat the momentary
SOA formation potential in the exhaust as a concentration
and call this quantity \([\text{SOA}]_{\text{ref}}\). Thus, the total SOA that is
formed from the exhaust emitted in the time interval \([t_0, t_f]\) is

\[
\text{SOA}_{\text{ref}} = \int_{t_0}^{t_f} [\text{SOA}]_{\text{ref}}(t) \cdot Q_{\text{exh}}(t) \, dt,
\]

(5)

where \([\text{SOA}]_{\text{ref}}\) is the momentary SOA formation potential
(mg m\(^{-3}\)) in the tailpipe and \(Q_{\text{exh}}\) is the exhaust gas volu-
metric flow rate (m\(^3\) s\(^{-1}\)). The time dependency of the SOA
formation potential reflects the varying precursor gas con-
centrations within the driving cycle, and this is the reference
SOA to which the SOA measured downstream of the OFR is
compared.

The SOA production factor in Eq. (4) corresponds to SOA
and CO2 emitted within a certain time interval. The moment-
ary SOA PF is determined similarly, combining Eqs. (4) and
(1):

\[
\text{SOA PF}(t) = \frac{[\text{SOA}]_{\text{ref}}(t) \cdot Q_{\text{exh}}(t)}{[\text{CO}_2](t) \cdot Q_{\text{exh}}(t)} \cdot k
\]

\[
= \frac{[\text{SOA}]_{\text{ref}}(t)}{[\text{CO}_2](t)} \cdot k.
\]

(6)

Thus, while the SOA PF for a certain time interval depends
on the exhaust flow rate, the momentary SOA PF does not.
Because of this, it is not universally possible to calculate the
SOA PF for a time interval based on Eq. (6) alone.

2.1 Determining SOA PF with an OFR

As shown in Fig. 1, the HC emission determined from the HC
concentration measurement at the OFR outlet differs from the
true HC emission. The same would be true for the part
of the total HC that constitutes the SOA precursors. As the
potential SOA formation is dependent on the precursor emis-
sion, a similar error is present when measuring the SOA
emission with an OFR.

Assuming that the OFR perfectly replicates the atmos-
pheric processes that lead to SOA formation, the SOA con-
centration measured downstream of the OFR \([\text{SOA}]_{\text{OFR}}\)
otherwise equals the SOA formation potential in the tailpipe
\([\text{SOA}]_{\text{ref}}\) but is affected by the OFR transfer function as in
Eq. (2):

\[
[\text{SOA}]_{\text{OFR}}(t) = ([\text{SOA}]_{\text{ref}} \ast E)(t).
\]

(7)
The SOA concentration measured at the OFR outlet is not only delayed because of the residence time in the OFR, but also distorted because of the residence time distribution, as shown in Eq. (7). Ideally, the reference SOA emission could be resolved from OFR measurements by deconvolution, but the noise present in the measurement prevents a perfect deconvolution of Eq. (7). Even without the noise, it is possible that no unique solution to the inversion problem exists. Thus, it is necessary to evaluate alternative methods to estimate the SOA production factor based on the distorted OFR signal.

First, to align the measured SOA concentration with the exhaust flow rate, we address the average delay caused by the OFR by shifting the OFR signal by a characteristic time constant of the OFR:

\[
[C]_{OFR}'(t) = [C]_{OFR}(t + \tau_r),
\]

where \([C]_{OFR}\) is the concentration measured downstream of the OFR. \([C]_{OFR}'\) is the delay-corrected concentration, and the constant \(\tau_r\) is a characteristic delay of the OFR. We chose to use the peak residence time of the OFR (\(\tau_{\text{peak}}\)) – i.e., the residence time at which the transfer function reaches its maximum (see Sect. A1 and Fig. S10) – as \(\tau_r\). An example of this correction is shown in Fig. 1, where the HC concentration at the OFR outlet is delay-corrected so that the peak concentration at the OFR outlet is approximately aligned with the tailpipe peak concentration. Note that this delay correction requires that the OFRs start sampling zero air immediately after the cycle ends and that the measurement downstream of OFR be continued for at least the duration of \(\tau_r\) for the delay-corrected OFR measurement to cover the full driving cycle.

After the measured SOA concentration is synchronized with the exhaust flow rate by Eq. (8), it is possible to multiply the measured SOA concentration by the exhaust flow rate in an attempt to obtain the SOA emission:

\[
\text{SOA}_{\text{OFR}} = \int_{t_0}^{t_f} ([\text{SOA}]_{\text{OFR}}'(t) \cdot Q_{\text{exh}}(t)) \, dt
\]

where \([\text{SOA}]_{\text{OFR}}'\) is the delay-corrected SOA concentration measured at the OFR outlet that is affected by the OFR transfer function as shown in Eq. (7). Note that the exhaust sample is normally diluted before introducing it to the OFR, but, at this point, we assume no dilution. Applying a constant dilution factor does not change the results of the analysis.

Comparison of Eqs. (10) and (5) shows that \(\text{SOA}_{\text{OFR}}\) is unequal to the reference SOA emission because the delay correction does not correct for the distortion inside the OFR (Eq. 2), which leads to mismatch between the exhaust flow rate and \([\text{SOA}]_{\text{OFR}}\). The only case where \(\text{SOA}_{\text{OFR}}\) universally equals the reference emitted SOA is when the OFR transfer function is a Dirac delta function – i.e., when the OFR is an ideal plug flow reactor.

### 2.2 Using the constant volume sampler

The underlying issue when determining the SOA production factor is the need to multiply the SOA concentration by the exhaust flow rate. This issue is also present when determining gaseous emissions from internal combustion vehicles; because of different instrument responses and delays, there is misalignment between gas concentration values and the exhaust flow rate, causing an error in the calculated emission factors (Nakamura and Adachi, 2013). The solution to this issue in regulated measurements is a constant volume sampler (CVS). Instead of trying to synchronize all gas analyzers with the exhaust flow rate data, the exhaust is diluted in a CVS with a dilution ratio (DR) that is inversely proportional to the exhaust flow rate:

\[
\text{DR}_{\text{CVS}}(t) = \frac{Q_{\text{CVS}}(t)}{Q_{\text{exh}}(t)},
\]

where \(Q_{\text{CVS}}\) is the constant total volumetric flow rate of the CVS, which is always greater than the exhaust flow rate. The proportional dilution ratio is achieved by an arrangement where the total CVS flow is kept constant, all the exhaust is led to the CVS, and the rest of the flow required by the CVS is sampled from filtered ambient air inlet (Nakamura and Adachi, 2013; Giechaskiel et al., 2014).

When the gas analyzers are sampling from the CVS, there is no need to multiply their concentration values by the exhaust flow rate because the dependency of emission on exhaust flow rate is already incorporated in the dilution of the CVS. Instead, the emission of a certain gas is obtained by multiplying the measured concentration by the CVS total flow.

The CVS can be utilized for OFR measurements as well to avoid the mismatch between \(Q_{\text{exh}}\) and the SOA measured with an OFR like, e.g., Zha et al. (2018), Kuittinen et al. (2021a, b), and Park et al. (2021) did. CVS should also be used in smog chamber experiments (e.g., Gordon et al., 2014a, b; Roth et al., 2020); otherwise, the injection of the exhaust into the smog chamber will not be proportional to the exhaust flow rate – i.e., the actual emission to the atmosphere.

Although the response of the OFR is much slower than that of a typical gas analyzer, it is still possible to obtain the total reference SOA emission with an OFR sampling from a CVS by multiplying the measured SOA concentration by the CVS flow rate and integrating over the full cycle:
\[
\int_{t_0}^{t_f} [\text{SOA}_{\text{OFR}}(t) \cdot q_{\text{CVS}}(t)] \, dt
\]

\[
= q_{\text{CVS}} \int_{t_0}^{t_f} \frac{[\text{SOA}_{\text{ref}} \cdot \text{SOA}_{\text{exh}}(t)] \cdot E(t)}{Q_{\text{CVS}}(t)} \, dt
\]

\[
= q_{\text{CVS}} \int_{t_0}^{t_f} \frac{[\text{SOA}_{\text{ref}} \cdot \text{SOA}_{\text{exh}}(t)] \cdot E(t)}{Q_{\text{CVS}}(t)} \, dt
\]

\[
= \int_{t_0}^{t_f} (\text{SOA}_{\text{ref}} \cdot \text{SOA}_{\text{exh}}(t)) \cdot E(t) \, dt
\]

\[
= \int_{t_0}^{t_f} \text{SOA}_{\text{ref}}(t) \cdot Q_{\text{exh}}(t) \, dt \cdot \int_{t_0}^{t_f} E(t) \, dt,
\]

\[
t_0 = 0, \ t_f \to \infty
\]

\[
= \int_{t_0}^{t_f} \text{SOA}_{\text{ref}}(t) \cdot Q_{\text{exh}}(t) \, dt = \text{SOA}_{\text{ref}},
\]

\[
t_0 = 0, \ t_f \to \infty.
\]

The integral in Eq. (15) equals the integral in Eq. (5). Thus, the first integral, in Eq. (12), equals the reference SOA emission. However, the separation of the convolution in Eq. (14) requires that the limits of integration be for the full defined range (i.e., \( t_0 = 0 \) and \( t_f \to \infty \)) as this is the full range of \( E \) (Weisstein, 2023). In this case, the integral of \( E \) is also canceled since it is a unity by definition (and when dividing by emitted \( \text{CO}_2 \) to obtain the SOA PF, \( Q_{\text{CVS}} \) in Eq. 12 is also canceled). Thus, using CVS, it is possible to obtain the reference SOA PF for the full cycle but not for parts of it. This issue was also noticed by Zhao et al. (2018) when determining the PFs for different phases of a driving cycle. In practice, \( t_f \) does not need to be infinite, but it should extend beyond the end of the driving cycle to account for the residence time in the reactor; for this reason, the measurement of \( [\text{SOA}]_{\text{OFR}} \) should also be continued after the end of the driving cycle and zero air should be injected to the reactor during that time. For the driving cycles and OFRs studied here, the error in full-cycle PF is lower than 5% when using CVS sampling where the post-sampling duration is equal to the OFR mean residence time and the error approaches zero with a longer post-sampling time (Fig. S13).

The advantage of OFRs is the continuous measurement to study the effect of different driving conditions on SOA formation. Thus, even though the CVS is a good solution for measuring the full-cycle SOA PF, the applicability of OFRs for time-resolved vehicular SOA studies remains unclear. The extent of the error in measured SOA emissions caused by the distortion is studied for different scenarios in the following sections by simulating direct sampling from the tailpipe (using Eq. 9) and by simulating CVS sampling (using Eq. 12), where the integration range is significantly shorter than the full-cycle length.

### 3 Methods

The analysis of the error in SOA PF arising from the OFR transfer function is based on a computational study, where we first define a SOA reference with temporal variability and then simulate the time series of SOA concentration at the OFR outlet affected by the transfer function. The SOA PF calculated based on the reference SOA is then compared to the SOA PF determined from the simulated OFR measurement. In addition to computational methods, experiments were conducted to obtain a realistic SOA reference, to characterize the OFR transfer function, and to evaluate the validity of the assumptions applied in the computations.

It is currently not possible to determine a true reference for the SOA formation potential in vehicle exhaust. For the purposes of this study, it would be possible to define a totally arbitrary SOA reference. However, to link the study to real exhaust emissions, we measured the time series of gaseous hydrocarbon concentration in vehicle exhaust and assumed that it represented similar temporal behavior to the real SOA formation potential in the tailpipe. Thus, we use a simple model for the reference SOA ([SOA]_{\text{ref}}), in which we assume that the potential SOA is directly proportional to the measured hydrocarbon mass concentration ([HC]) in the tailpipe:

\[
[\text{SOA}_{\text{ref}}(t)] = [\text{HC}](t) \cdot Y,
\]

where \( Y \) is the proportionality factor that includes both SOA yield and the fact that not all hydrocarbons produce SOA. Even though the proportionality factor in reality was not constant, it would mainly affect the absolute variability but not the temporal variability.

We measured HC and \( \text{CO}_2 \) concentrations in the exhaust of a Euro 6 gasoline vehicle running two driving cycles to obtain reference data. The HC concentration was measured with a flame ionization detector. The \( \text{CO}_2 \) concentration required in a SOA PF calculation (Eqs. 4 and 1) was measured with a non-dispersive infrared analyzer, and the volumetric exhaust flow rate was calculated based on the intake airflow rate and fuel consumption obtained from the on-board diagnostics data. The driving cycles were the cold-start (CS) New European Driving Cycle (NEDC), which was preceded by soaking time of 15 h and started with an engine start, and the hot-start (HS) NEDC, which was preceded by driving at 80 \( \text{km} \cdot \text{h}^{-1} \) speed for 5 min and started with an idling engine. A proportionality factor \( (Y) \) of 0.15 was used in Eq. (16), resulting in realistic SOA PFs of approximately 100 and 20 mg (kg fuel)\(^{-1}\) for cold-start and hot-start cycles, respectively.
The OFR transfer function needed to be well defined to simulate its effect on the SOA production factor calculation. For this, we used a prototype of the Dekati oxidation flow reactor (DOFR; Dekati Ltd.), which is a commercial oxidation flow reactor with a similar geometry to that of the Tampere secondary aerosol reactor (TSAR; Simonen et al., 2017). The DOFR transfer function was determined for CO₂ and toluene by measuring the DOFR outlet concentrations of 10 s input square pulses. To compare OFRs with different transfer functions, we also determined the transfer function of a potential aerosol mass (PAM) reactor by utilizing the CO₂ pulse data presented by Lambe et al. (2011). Additional details on vehicle exhaust and OFR characterization measurements are provided in Appendix A.

Two different sampling options are considered in the analysis: direct sampling from the tailpipe and sampling from a CVS. The SOA concentration at the OFR outlet was simulated by convolving the SOA reference with the OFR transfer function (Eq. 7) for cases with direct sampling. For CVS sampling, the SOA concentration at the OFR outlet was simulated by similar convolution, but the varying degree of dilution of the sample entering the OFR was accounted for.

\[
[\text{SOA}]_{\text{OFR,CVS}}(t) = \left( \frac{[\text{SOA}]_{\text{ref}}}{\text{DR}_{\text{CVS}}} \right) \ast E(t)
\]  

Both Eq. (17) and Eq. (7) assume that the OFR otherwise perfectly reproduces the SOA reference but only with a slower response. The transfer function used in these equations is the transfer function of CO₂. In reality, because of the following effects, these assumptions do not necessarily hold:

1. Non-tropospheric gas-phase chemistry and other non-tropospheric losses (e.g., wall losses of precursor oxidation products) (Peng and Jimenez, 2020, 2017; Peng et al., 2019; Palm et al., 2016) can vary within the driving cycle because, e.g., the wall losses depend on the particle surface area concentration inside the OFR. They can also affect the OFR response in general because the sample at the OFR outlet has a distribution of residence times, and some of the losses are time-dependent. Thus, the square pulse injection of a SOA precursor would not produce a SOA mass concentration profile at the OFR outlet that is similar to a CO₂ profile produced by a square pulse injection of CO₂. In other words, the use of a CO₂ transfer function would be incorrect.

2. Even though the proportionality factor in Eq. (16) was constant, the SOA yield inside the OFR can change depending on the organic aerosol mass concentration inside the OFR and on the OH exposure. As in the previous entry in this list, this may vary not only within the driving cycle but also in the OFR residence time dimension.

3. The amount of SOA formed depends on the amount of consumed precursor gases. Depending on the OH exposure in the OFR (assuming OH reactive precursor gas), all precursor gases do not necessarily fully oxidize. Since the OH exposure depends on the average OH concentration in the OFR and on the residence time, there is a distribution of OH exposures at the OFR outlet because of the residence time distribution of the OFR.

Thus, the shape of the SOA pulse originating from an input pulse of precursor gas depends on the combination of the OFR transfer function and the reaction rate constant of the precursor gas.

4. There are potential adsorption, absorption, or desorption phenomena in the OFR or preceding sampling lines. Several studies have shown that gaseous organic compounds may exhibit significant delays in sampling lines or instruments when they are first adsorbed or absorbed onto the sampling line or instrument wall and later desorbed (Pagonis et al., 2017; Deming et al., 2019; Liu et al., 2019; Morris et al., 2024). Similar effects may be present in an OFR as well for the precursor gases or their oxidation products, worsening the misalignment between the produced SOA and the exhaust flow rate. Morris et al. (2024) showed the effect of adsorption and absorption on the PAM reactor response time for ketones but not for typical SOA precursors.

To keep the analysis simple, all the effects listed above are neglected, but the estimation of their relevance is discussed here. We measured a rapid SOA formation pulse in DOFR by injecting a square pulse of toluene at the reactor inlet. The SOA concentration that was measured at the DOFR outlet following this pulse is shown in Fig. S1a. As a comparison, a computational result, the square pulse of toluene convolved with the CO₂ transfer function, is shown in the same figure. While the computational result does not perfectly replicate the measured SOA concentration, the agreement is good, and we can deduce that the effects listed above are minor for toluene SOA formation.

The average OH exposure in the toluene pulse experiment was 7.9 × 10⁻¹ⁱ cm⁻³ s⁻¹ (equivalent to approximately 6 d of OH oxidation in the atmosphere with an OH concentration of 1.5 × 10⁶ cm⁻³). At this high of an OH exposure, essentially all the toluene was consumed. For slower-reacting precursor gases, such as benzene, this would not be the case, as shown in Fig. S1b and d. However, the reaction rate constants between OH radicals and most anthropogenic SOA precursors are higher than the rate constant of toluene, indicating that the assumption that all precursor gas is consumed in the OFR is sufficient, as long as the OH exposure is approximately 7.9 × 10¹¹ cm⁻³ s⁻¹ or higher. A more detailed discussion is presented in Sect. S2 in the Supplement.

To our knowledge, the delay effects caused by adsorption, absorption, and desorption have not been characterized for typical SOA precursors. Even though we did not observe such delays for the toluene SOA formation in DOFR, the effect has a potentially high impact on other SOA precursors,
especially the less volatile ones (intermediate-volatility compounds), and needs further research.

4 Results and discussion

To study the effect of OFR RTD on the accuracy of SOA production factor, we simulate the SOA concentration at the OFR outlet for two OFRs that have distinct residence time characteristics. The PAM reactor (Lambe et al., 2011) represents an OFR with a broad transfer function, with a mean residence time of 142 s and transfer function standard deviation of 21 s. The standard deviation of the transfer function reflects the transfer function broadness, and its calculation is presented in Sect. S1. All OFR data shown hereafter are delay-corrected according to Eq. (8) by the peak residence time of the OFR (see Sect. A1).

4.1 Real driving cycles

As described in Sect. 3, in the absence of a true reference for the SOA formation potential, we generated semi-synthetic data based on the HC concentration measured from a gasoline vehicle tailpipe, assuming that SOA formation potential is directly proportional to the HC concentration (Eq. 16). The CO$_2$ and SOA concentrations at OFR outlets were simulated by convolving the tailpipe concentrations with the OFR transfer functions (Eq. 2). We assumed that the reactors were sampling zero air until the cycle started; otherwise, the exhaust from preceding driving would have been present in the OFRs and affected the cycle-specific SOA PF.

Figure 2 shows the CO$_2$ concentrations, SOA concentrations, and their cumulative emissions in the hot-start NEDC. Similar graphs for the cold-start NEDC are shown in Fig. S3. The SOA concentration at the DOFR outlet follows the reference SOA concentration better than PAM, which results in better agreement of the total emitted SOA at the end of the driving cycle (Fig. 2d). However, the DOFR-based total SOA emission is still 7% lower than the true SOA emission, mainly because the response is not fast enough to follow the reference SOA concentration during accelerations, where the exhaust flow rate is highest. PAM has the same effect, but, in addition, the PAM-derived SOA emission starts to deviate from the reference SOA emission already at the beginning of the cycle because the response is too slow to catch the SOA peak in the cycle start. These two effects result in the total SOA emission that is 18% lower than the reference SOA emission.

Because the SOA PF is directly proportional to the ratio of emitted SOA and emitted CO$_2$, the relative error in PF equals the relative error in the SOA emission. However, for the OFRs, both SOA emission and CO$_2$ emission (calculated from the delay-corrected CO$_2$ measured at the OFR outlet) are underestimated in the driving cycles studied here, so the error in PF could be decreased by normalizing the SOA emission to the CO$_2$ emission measured at the OFR outlet instead of the true CO$_2$ emission. Even though this calculation method leads to a better estimation of SOA PF in the two cases studied here, it is not guaranteed that the error in CO$_2$ measurement will always compensate for the error in SOA measurement. It is possible that in some cases, the SOA emission determined from OFR measurements is higher than the reference emission, and in such a case, normalizing to OFR CO$_2$ would amplify the error. Therefore, when presenting the integrated SOA PFs (e.g., Fig. 3a), the SOA emission is normalized to the true CO$_2$ emission.

The error in full-cycle SOA PFs is relatively small for both cold- and hot-start driving cycles despite the distorting effect of OFR transfer functions. In hot-start NEDC, the error in total SOA PF is 7% for DOFR and 18% for PAM (Fig. 3), and in cold-start NEDC the corresponding errors are 4% and 7% (Fig. S4). To study the accuracy of SOA PF in smaller subcycles, we divided the NEDC into three parts according to Karjalainen et al. (2016): the cold-start urban driving cycle (CSUDC; 0–391 s), hot urban driving cycle (HUDC; 392–787 s), and extra-urban driving cycle (EUDC; 788–1180 s). The division is used here also for the hot-start cycle although the term CSUDC does not represent a cold start in that case. The maximum error in the subcycles was 10% for DOFR (hot-start HUDC) and 23% for PAM (hot-start CSUDC). Note that the SOA PFs for the subcycles (Fig. 3a) are not the average values of momentary PFs shown in Fig. 3b. Instead, the subcycle SOA PF is calculated by normalizing the SOA emitted during the subcycle to the emitted CO$_2$.

The continuous operation of the OFRs allows for studying SOA production factors at a higher time resolution than that of the ~ 400 s subcycles. Zhang et al. (2023) investigated SOA PF as a function of the driving condition using a fast-response OFR (Veh-OFR). Such an analysis requires a time resolution on the order of seconds, and the effect of the OFR transfer function on the accuracy of momentary SOA PF at such a time resolution needs to be determined.

The time-resolved reference and OFR SOA PFs are shown in Fig. 3b for the hot-start driving cycle and in Fig. S4b for the cold-start driving cycle. The time-resolved OFR SOA PFs were calculated by normalizing the SOA concentration to CO$_2$ measured at the OFR outlet to compensate for the slow response in SOA measurement. This is important especially in the beginning of the cycle, where the CO$_2$ levels in the OFRs deviate significantly from the tailpipe concentration.

Figure 3b shows that although the DOFR PF time series resembles the reference PF time series better than PAM, neither of the OFRs can follow the rapid changes in the reference SOA PF. For example, the maximum OFR PFs during the acceleration starting at 313 s are approximately 40% of the reference maximum PF. However, when integrating the SOA and CO$_2$ emissions for a longer time interval, the agreement between the reference PF and OFR PFs improves. For
Figure 2. Time series of the exhaust flow rate ($Q_{\text{exh}}$), tailpipe, and OFR outlet concentrations of CO$_2$ (a) and SOA (b) in hot-start NEDC and the cumulative emissions of CO$_2$ (c) and SOA (d). The OFR data are simulated based on tailpipe concentrations and OFR transfer functions, and the SOA concentration refers to HC concentration multiplied by $Y$. All OFR data are delay-corrected.

Figure 3. Total SOA PFs of subcycles and the full driving cycle (a) and time series of reference SOA PF and SOA PFs determined from OFR outlet concentrations (b) in hot-start NEDC. The integrated SOA PF in panel (a) is calculated by normalizing the SOA emission to the true CO$_2$ emission, whereas for the momentary SOA PF in panel (b), the SOA concentration is normalized to the OFR CO$_2$ concentration. The PFs in both panels are calculated from semi-synthetic SOA data that are linearly proportional to the measured HC concentration in the tailpipe or the simulated HC at the OFR outlet. CSUDC, HUDC, and EUDC represent approximately 400 s subcycles within the full cycle.

To study the accuracy of different OFRs, we divide the driving cycle in short events according to different driving conditions: accelerations, constant speed driving, idling, and decelerations. The time periods are shown in Fig. S14, and the deviations from the reference SOA PF for each driving condition are shown in Fig. 4. The corresponding correlation graphs are shown in Fig. S15.

Figure 4 shows that a DOFR with narrower RTD is generally more suitable for studying SOA PFs of short events than PAM. In the cold-start cycle, PAM typically overestimates the PF because the HC originating from the engine start remains in PAM for a long time. In both cycles, the acceleration PFs are usually underestimated by both OFRs because there is typically a simultaneous increase in exhaust flow rate and HC concentration, but the OFR SOA does not reach the level of reference SOA, as illustrated in Fig. 1 for HC. In constant-speed driving, both OFRs overestimate SOA PF because this driving condition is usually preceded by accelerations, and HC originating from the acceleration is still present in the OFRs. For the same reason, the OFRs also overestimate the deceleration PFs.
As discussed earlier, normalizing the emitted SOA to the CO$_2$ emission determined from CO$_2$ concentration measured at the OFR outlet may reduce the error in SOA PF. The applicability of this method and other methods to reconcile the distortion in SOA concentration caused by the OFR transfer functions is studied in the next section.

4.1.1 Alternative data analysis and measurement methods

Figure 5 shows the SOA PF deviations for both reactors when using different data analysis and measurement methods. Overall, the different methods (except for the averaging method) result in a relatively small error of a maximum 37%. In all methods, the OFR data are delay-corrected.

The standard method. This method is the one used in previous sections; i.e., the SOA emission is normalized to true CO$_2$ emission. This method underestimates the SOA PF in most cases (Fig. 5). Note that normalization to true CO$_2$ emission is equivalent to normalizing to true fuel consumed or true distance traveled. When using the other data analysis methods described below and calculating the distance-based production factors, one first needs to determine the fuel-specific production factor and only then convert it to distance-based by multiplying by the ratio of fuel consumed per distance traveled that is available in the on-board diagnostics data.

The OFR CO$_2$ method. In this method, the CO$_2$ concentration is measured from the OFR outlet and the CO$_2$ emission is determined by multiplying the delay-corrected CO$_2$ concentration by the exhaust flow rate. In most cases, the OFR CO$_2$ method results in better agreement with the reference SOA PF compared to standard method (Fig. 5), which is in agreement with the observation that both SOA and CO$_2$ emissions are underestimated with the OFR in Fig. 2.

The convolution method. This method applies the same OFR response to the exhaust flow rate that affects the SOA and CO$_2$ concentrations that are measured at the OFR outlet. The SOA and CO$_2$ emission rates are calculated by multiplying the concentrations at the OFR outlet by exhaust flow rate that is convolved with OFR transfer function. This method was used by Simonen et al. (2019) for determining SOA emission rate, but it was not normalized to CO$_2$ emission measured at the OFR outlet but to the true fuel consumption or distance traveled, which is equal to normalizing to true CO$_2$ emission. The deviation in convolution method is of similar magnitude to the standard method and the OFR CO$_2$ method (Fig. 5).

The CVS method. In this method, the OFRs are sampling exhaust that is diluted with CVS; i.e., the dilution ratio is inversely proportional to the exhaust flow rate. The emitted SOA is calculated with Eq. (12). The emitted CO$_2$ is calculated with a similar equation, where the CO$_2$ is measured at the OFR outlet. The CVS method always leads to correct SOA PF for the full cycle as discussed in Sect. 2.2. For DOFR, the CVS method results in the least deviation in subcycles as well compared to the methods presented above. For PAM, the deviation in subcycles with this method is on average larger than the previous methods in cold-start cycle but performs better in the hot-start cycle.
Figure 5. OFR SOA PF deviation from the reference PF for full driving cycles and \(~ 400\) s subcycles when using different data analysis and measurement methods. The PFs are calculated from semi-synthetic SOA data that are linearly proportional to the measured HC concentration in the tailpipe or the simulated HC at the OFR outlet.

Although the CVS sampling is favorable especially for DOFR, it has some disadvantages. CVS requires a high flow rate of dilution air compared to partial flow diluters, and purifying such amounts of dilution air is challenging. This may lead to high background SOA formation from dilution air impurities (Zhao et al., 2018). In addition, the heat from vehicle exhaust may cause desorption of HC that was previously adsorbed onto CVS walls (Gordon et al., 2014a). However, the SOA PFs have been measured with CVS sampling with acceptable background SOA formation (Zhao et al., 2018; Kuittinen et al., 2021a; Gordon et al., 2014a).

An inherent feature of the CVS is that the dilution ratio is inversely proportional to exhaust flow rate. As shown in Fig. 2, the HC peaks usually occur during accelerations, where the exhaust flow rate is also elevated. The same is observed for NO\textsubscript{x}, so the use of CVS dilution amplifies the variations in HC and NO\textsubscript{x} concentrations compared to direct sampling from the tailpipe with a constant dilution ratio. Since the OH exposure and photochemistry in OFRs are sensitive to concentrations of NO\textsubscript{x}- and OH-reactive gases (Peng and Jimenez, 2017), using CVS may cause gas concentrations that are too high during, e.g., accelerations, where the exhaust flow rate and gas concentrations are high, and too low a signal during, e.g., idling, where concentrations and exhaust flow rate are low.

The averaging method. This method does not consider the exhaust flow rate, since it is calculated using Eq. (6). In the study by Zhang et al. (2023), the full-cycle SOA PFs were apparently determined by calculating the average of the momentary PFs instead of calculating the ratio of emitted SOA to emitted CO\textsubscript{2} although their description of the PF calculation for a full cycle is not unambiguous. Figure 5 shows that in the cold-start cycle, this averaging method leads to an overestimation by a factor of \(~ 2\) for DOFR and \(~ 2.5\) for PAM. Note that the PFs calculated with the averaging method are not compared to the average values of reference momentary PFs but instead to the reference PF, which is the emitted SOA normalized to emitted CO\textsubscript{2}.

The deconvolution method. In this method, the SOA signal simulated at the OFR outlet is first deconvolved (as described by Conesa, 2020; see Sect. S3) to obtain the reference SOA concentration in the tailpipe and then multiplied by the true exhaust flow rate to obtain the SOA emission rate. The emitted SOA is normalized to true emitted CO\textsubscript{2}. For PAM, the deconvolution method leads to the smallest errors, whereas for DOFR, the CVS method is as good as the deconvolution method. The time series of deconvolved SOA concentrations are shown in Fig. S16.

The deconvolution here represents the best possible outcome because there is no noise present in the simulated SOA.
concentration at the OFR outlet. In real-life scenarios, there is noise originating from the instrument measuring the SOA concentration and also some variability in the OFR transfer functions due to small fluctuations in flow rate and temperature. The performance of the deconvolution method in such cases is beyond the scope of this study, but our tests for 10 s square pulses of the SOA precursor showed that the deconvolution was able to reproduce the square pulses, based on the measured SOA concentration at the DOFR outlet, but not perfectly (Fig. S9).

While all calculation methods except the averaging method are able to report the SOA PF for full cycles and ~400 s subcycles with relatively good accuracy, Fig. 4 shows that, in some cases, the deviation in short driving events can be very high when using the standard method. Some of the deviations in Fig. 4 could be avoided by normalizing the SOA emission to the CO\(_2\) measured at the OFR outlet instead of the tailpipe. For example, the most severe underestimations in PAM and DOFR are observed in the beginning of the driving cycles where the OFR response to [SOA]\(_{ref}\) is much slower than the change in the tailpipe CO\(_2\) concentration and in other occasions where there is drastic change in the tailpipe CO\(_2\) concentration. Likewise, the changes in the tailpipe CO\(_2\) concentration during decelerations are much faster than the characteristic residence times of the OFRs. For this reason, we investigate whether the normalization to OFR CO\(_2\) or any of the other methods perform better for short events in the driving cycles. For this analysis, we divide the cycle into 14 s bins and calculate the deviation from reference PF for each bin using different methods. The 14 s bin duration was chosen because it is the median duration of different events in Fig. 4.

Figure 6 shows that different calculation methods, including the averaging method (but excluding the deconvolution method), report similar distributions for the deviations in short driving events. However, the standard method usually has a higher deviation at low values due to the CO\(_2\) issue mentioned before. The deconvolution method is superior for both OFRs: 98% of all OFR data are within factors of 0.81 and 1.39 of reference PF. Because of this high accuracy, the applicability of the deconvolution method in real-world scenarios should be studied in a future publication.

Both reactors tend to overestimate the SOA PFs of short events. For example, in the OFR CO\(_2\) method, the median ratios between OFR PFs and reference PFs are 1.08 and 1.13 for DOFR in hot- and cold-start cycles, respectively. For PAM, the median ratios are 1.24 and 1.87 in hot- and cold-start cycles, respectively, and in cold-start NEDC, 75% of PAM PFs exceed the reference PFs.

4.2 Special cases

Although DOFR usually reports PFs closer to reference values than PAM, this is not always the case. Figure 7 shows two synthetic examples: one where the reference SOA concentration increases simultaneously with the exhaust flow rate (typical acceleration observed in the driving cycles presented) and another where the peak in the exhaust flow rate is not aligned with the reference SOA peak (e.g., a SOA peak originating from engine start followed by an elevated exhaust flow rate due to acceleration after the engine start).

In the case where exhaust flow rate and reference SOA concentration peaks are well aligned (Fig. 7a–b), both OFRs report too low a SOA emission, which was also the case in Fig. 1, but the DOFR result is closer to the reference. However, when the two reference signals are not aligned (Fig. 7c–d), DOFR results in a higher overestimation of the emitted SOA because the SOA concentration at the DOFR outlet is still elevated when the exhaust flow rate starts to increase. This is the case with PAM as well, but, since the SOA peak at PAM outlet is distributed over a longer time period, the concentration is not as high as in DOFR, and the resulting SOA emission agrees better with the reference emission.
In Sect. 4.1, the performance of the OFRs was investigated only for one real gasoline vehicle running two cycles, and DOFR typically resulted in a better agreement with reference SOA PF than PAM. However, as illustrated in Fig. 7, DOFR does not result in better agreement in all arbitrary cases. Different vehicle types and more aggressive driving cycles may exhibit different behaviors in tailpipe gas concentrations and exhaust flow rate compared to the gasoline vehicle driving the NEDC; the alignment between the concentration peaks and the changes in exhaust flow rate may also be different. For example, in diesel vehicles, the CO\textsubscript{2} concentration is load-dependent, whereas in the gasoline vehicle studied here, the tailpipe CO\textsubscript{2} concentration was almost constant. Hybrid vehicles may repeatedly switch the combustion engine off and on during the driving cycle.

Thus, to investigate the performance of the OFRs and data analysis methods in a broader range of instances, we performed a Monte Carlo analysis on synthetic driving cycles that include various different combinations of the exhaust flow rate, CO\textsubscript{2} concentrations, and HC concentrations.

### 4.3 Synthetic driving cycles

The driving cycles have three variables that affect the SOA PF: CO\textsubscript{2} concentration, HC concentration, and exhaust flow rate. The synthetic driving cycles were generated by dividing the cycle into periods of random duration for each variable, where the value of the variable was random (but constant for the period duration). The periods for each variable were generated independently of one another so that the changes in the values of each variable did not necessarily coincide with changes in the other two variables. The generation algorithm is described in more detail in Sect. S4, and an example of a generated cycle is shown in Fig. 8. More examples are shown in Fig. S17. In total, 10 000 synthetic driving cycles were generated.

Figure 9a–b show that the distribution of full-cycle SOA PFs was skewed towards underestimation for both reactors but more severely for PAM when using the standard method for the synthetic driving cycles. The two other methods shown, the OFR CO\textsubscript{2} and convolution methods, agreed well with the reference PF. Only three methods are shown here because it was already observed in Sect. 4.1 that the averaging method was not suitable for calculating the full-cycle PFs and that the CVS method always led to a correct full-cycle PF. The deconvolution method was too time-consuming to apply for all 10 000 driving cycles.

Similar to full cycle PFs, the standard method typically underestimated the PF for PAM when calculating the PFs for 400 s subcycles (Fig. 9c). Among the other calculation methods, the averaging method led to broadest distribution of deviations and the CVS method performed best for both OFRs.

Because of the other disadvantages of the CVS sampling discussed in Sect. 4.1, the OFR CO\textsubscript{2} and convolution methods seem most feasible for exhaust measurements based on the distributions in Fig. 9c. Using the OFR CO\textsubscript{2} method for 400 s subcycles in the synthetic cycles, the median OFR-to-reference ratio was 1.00 for DOFR and 1.01 for PAM. Of all the DOFR PF ratios, 50 % ranged between 0.96 and 1.05, and PAM ratios ranged between 0.89 and 1.16. Also, 98 % of DOFR PF ratios ranged between 0.81 and 1.40, and PAM ratios ranged between 0.54 and 2.50.
Figure 8. An example of a synthetically generated driving cycle.

Figure 9. The probability distributions for full-cycle SOA PFs for 10,000 synthetic driving cycles using DOFR (a) and PAM (b) and the deviation in OFR PFs for 400 s (c) and 14 s bins (d) in the synthetic driving cycles. Boxes represent the 25th and 75th percentiles, and the line inside the box represents the median value. The points are considered outliers if they are greater than the 99th percentile or lower than the 1st percentile. The whiskers extend to most extreme data points that are not outliers.

Figure 9d shows that the different calculation methods resulted in very similar distributions when calculating the SOA PFs for short events. The CVS method led to the smallest lower outliers for both OFRs, and the lower outliers in the standard method are the closest to 1. The PAM median was the closest to the reference value when using the standard method, but, on the other hand, the 25th percentile was smaller than with the other methods. In the OFR CO₂ method, 50% of DOFR PF ratios ranged between 0.82 and 2.09, and PAM ratios ranged between 0.71 and 4.38. Of all the DOFR PF ratios, 98% ranged between 0.41 and 31.00, and PAM ratios ranged between 0.19 and 77.26. A summary of the deviations of OFR-derived PFs from the reference values in both real cycles and synthetic cycles is shown in Table 1.

Since a significant fraction of OFR-derived PFs were more than 10-fold the reference PFs for short (14 s) segments and the agreement was better for longer (400 s) segments, it is of interest to determine what the minimum segment durations are for which the OFR results are accurate enough. If we choose that the OFR result is acceptable when 99% of the PFs are less than 3 times the reference PF, the minimum duration is 110 s for DOFR and 350 s for PAM. The deviations as a function of bin duration are shown in Fig. S12.

5 Conclusions

In this study, the effect of the OFR transfer function on the accuracy of SOA PFs in transient driving cycles was investigated using semi-synthetic and synthetic exhaust gas data. The analysis was done for two OFRs: a PAM reactor, with a
Table 1. Ratios of reactor PFs to reference PFs when using the OFR CO$_2$ method. For each case, the median ratio and the 25th, 75th, 1st, and 99th percentiles of ratios are shown (notation of $P_{25}$ for the 25th percentile, etc. is used).

<table>
<thead>
<tr>
<th>Subcycles (400 s)</th>
<th>Short events (14 s)</th>
</tr>
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<tbody>
<tr>
<td></td>
<td>Median $P_{25}$ $P_{75}$ $P_{01}$ $P_{99}$</td>
</tr>
<tr>
<td>Real cycles</td>
<td>PAM 1.04 0.88 1.20 0.87 1.22</td>
</tr>
<tr>
<td></td>
<td>1.47 1.03 2.61 0.36 4.99</td>
</tr>
<tr>
<td>Synthetic cycles</td>
<td>PAM 1.01 0.89 1.16 0.54 2.50</td>
</tr>
<tr>
<td></td>
<td>1.11 0.82 2.09 0.41 31.00</td>
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</tbody>
</table>

Even though the wide residence time distributions of OFRs resulted in momentary PFs that differed from the reference PFs, it was possible to determine the integrated PFs relatively accurately for longer periods within the driving cycles. However, a wrong data analysis method could lead to PFs that are more than double that of reference PF.

When determining SOA PFs of short-duration events in a driving cycle, such as accelerations, the errors were larger for both OFRs compared to PFs of longer periods. The narrower transfer function of DOFR was advantageous, since the 1st and 99th percentiles of OFR-to-reference PF ratios in the short-duration events (14 s periods) in real driving cycles were 0.55 and 2.41, respectively, for DOFR and 0.36 and 4.99 for PAM (using the OFR CO$_2$ method).

When extending the study to synthetic driving cycles, the OFRs still reported the full-cycle PFs with a relatively small error. For 14 s bins in the synthetic driving cycles, it was observed that the OFRs may overestimate the SOA PFs by more than factor of 10. It is questionable whether any of the studied OFRs can be used to determine SOA PFs for that short driving events since the potential error is so high. The uncertainty should at least be addressed when reporting the PFs. On the other hand, the synthetic driving cycles are random and do not necessarily represent typical driving cycles, so the results represent the maximum possible error rather than the typical error observed in real driving cycles. More real cycles should be studied in order to evaluate the potential error.

By lengthening the bin duration to 110 s, the 99th percentile of DOFR PF ratios was below 3 in the synthetic driving cycles. The 99th percentile of PAM PF ratios was below 3, when the bin duration was longer than 350 s.

Deconvolution of SOA concentration measured at the OFR outlet seemed to be a promising method because it enhanced the accuracy of SOA PFs significantly. However, the result was obtained by assuming noise-free measurement of mass concentration, and thus its applicability to real-world scenarios should be further studied.

There are also other reasons than the transfer function alone for OFRs to report incorrect SOA production factors, such as non-tropospheric gas chemistry or non-tropospheric losses. In this paper, we only studied the error that was caused by the OFR transfer function. Other sources of error were isolated by assuming that the oxidation in OFRs perfectly reproduces atmospheric oxidation, that there are no non-atmospheric losses in the OFRs, and that there are no absorption- or adsorption-related delays in the OFR. The analysis is limited to conditions where the SOA formation potential is directly proportional to HC concentration and where the proportionality is constant throughout the driving cycle; i.e., the OH exposure in the OFR is sufficient to oxidize all precursor gases completely.

Even though the assumption of the SOA concentration being directly proportional to HC concentration does not generally hold, the HC measurement from the tailpipe, accompanied by the methods presented in this study, is a good sensitivity test for transfer-function-related uncertainties when determining the SOA PFs with an oxidation flow reactor. A similar analysis applies when using any other slow-response instrument to determine emission factors.

Arising from our analysis, we present the following best-practice recommendations for OFR emission measurements:

- Before the start of the cycle, the reactor must be sampling zero air to avoid previous driving affecting the cycle SOA PF. The exhaust sampling must start at the same time as the driving cycle. This concerns the engine-off periods of hybrid vehicles as well: zero air sampling should be started immediately when the combustion engine is switched off, and the tailpipe sampling started when the engine turns back on. When sampling from CVS, this is done automatically.

- When the cycle ends, the reactor must immediately start sampling zero air. The measurement must be continued at least for the duration of the OFR peak residence time to make the delay correction in data aftertreatment possible. When sampling from CVS (or when using the convolution method), the sampling of zero air must be continued at least for the duration of OFR mean residence time, but longer sampling time results in a more accurate PF (Fig. S13).

- In order to use the OFR CO$_2$ method or the convolution method, CO$_2$ should be measured downstream of the
OFR, or the OFR outlet CO$_2$ concentration should be simulated by convolving the tailpipe concentration with the OFR transfer function and dividing with the dilution ratio.

- When using a method other than the standard or deconvolution method, the distance-based production factors should be calculated by first calculating the fuel-based production factor with one of the presented methods and then using OBD data to convert the fuel-based PF to distance-based.

The MATLAB code used in this study is available as a supplement to reproduce the analysis for any OFR with a known transfer function and for any driving cycle for which the CO$_2$ and HC concentrations and exhaust flow rate are available.

Appendix A: Experimental details

A1 OFR characterization

The Dekati oxidation flow reactor (DOFR) is a commercial oxidation flow reactor, the dimensions of which are very close to those of the Tampere secondary aerosol reactor (TSAR; Simonen et al., 2017). The main geometrical additions compared to TSAR are a conical outlet and a laminating grid element in the inlet, and, unlike TSAR, all sample is evacuated through a single outlet. The oxidation reactor is surrounded by 12 UV lamps of which two can be switched on individually and the rest of the lamps in pairs, whereas TSAR has two intensity-controlled UV lamps (Kuitinen et al., 2021a). The housing of the oxidation reactor is cooled with air. The air cooling in the commercial version is enhanced compared to the prototype version used here. Similar to TSAR, DOFR is an OFR254 type reactor, which means that OH radicals inside the reactor are generated by 254 nm UV light from externally mixed ozone and water vapor.

The transfer function of DOFR was determined for CO$_2$ and toluene by injecting 10 s square pulses of gases into the reactor and measuring them downstream of the reactor. The CO$_2$ was measured with a LI-840 analyzer (LI-COR Inc.) and toluene with a Vocus proton transfer reaction mass spectrometer (Aerodyne Research Inc.). The gases were injected at the enclosure inlet, and CO$_2$ was measured directly downstream of the reactor, while the toluene was measured downstream of ejector diluter, which is an integral part of DOFR. Thus, the toluene RTD describes the response of the full unit, although we assume that this is the case for CO$_2$ RTD as well because the residence time in the diluter and its sampling lines is minor. The mean flow rate through DOFR was 6.8 L min$^{-1}$ during the CO$_2$ experiments and 6.0 L min$^{-1}$ during the toluene experiments.

The square pulses were generated by continuously injecting a constant mass flow rate of CO$_2$ or N$_2$ mixed with toluene into a fast pneumatic three-way valve (MS-151-DA actuator with a SS-42GXS6MM-51D 3-way valve; Swagelok Company), one outlet connected to the DOFR inlet and the other to the excess line. The toluene vapor was generated with a permeation oven (V-OVG; Owlstone Inc.). The measurement setup is shown in Fig. S2.

The DOFR RTDs of 10 s pulses were measured for three different UV lamp configurations: off, low (two central UV lamps on), and high (all UV lamps on). The O$_3$ generation was switched off to prevent toluene reacting with OH radicals when measuring the toluene RTD. The measured RTDs correspond to 10 s input pulses, so they do not represent the actual transfer function which is the response to a Dirac delta input. Thus, the OFR transfer functions were determined by finding the transfer function that resulted in the best agreement with the measured concentration when convolving with 10 s square pulse. The candidate function was a linear combination of Taylor distributions (Lambe et al., 2011; Huang and Seinfeld, 2019), and the best fit was found with a MATLAB function, fit. The gas analyzer response was not determined separately, so it is included in the reported transfer functions. In this study, the transfer function corresponding to low UV lamp configuration was used to simulate the DOFR output. This lamp configuration resulted in OH exposure of $7.9 \times 10^{11}$ cm$^{-3}$ s$^{-1}$ according to toluene measurements. The DOFR transfer functions for CO$_2$ and toluene are shown in Fig. S5, and the comparisons between the convolved square pulses and the measured DOFR output concentrations are shown in Figs. S6 and S7.

By switching the O$_3$ reactor on, we also measured the mass concentration that was produced from a 10 s toluene pulse for the low UV lamp configuration. The mass concentration was measured with an electrical low-pressure impactor (ELPI; Dekati Ltd.; Keskinen et al., 1992) with improved nanoparticle resolution (Yli-Ojanperä et al., 2010). It would have been possible to determine a transfer function for SOA formation based on these measurements, but since such data were not available for PAM chamber, we simulated the SOA formation in both OFRs by assuming that the SOA formation response is equal to the CO$_2$ response. Simonen et al. (2017) did measure the PAM SOA formation for a toluene pulse, but, in those measurements, the PAM ring flow was not used. Since the usage of ring flow is a standard method in PAM measurements and affects the transfer function, we used the CO$_2$ pulse data measured by Lambe et al. (2011) to determine the PAM transfer function by the same fitting procedure as for the DOFR (Fig. S8). In the measurements by Lambe et al. (2011), the PAM ring flow was used and the UV lamps were on. Using the CO$_2$ transfer function to simulate the SOA formation in DOFR resulted in a satisfactory agreement with the experimental data (Fig. S1a), so the usage of the CO$_2$ transfer function in this study was justified.

For the OFR delay correction (Eq. 8), we used the peak residence time as the correction constant. The peak residence time ($\tau_{peak}$) is the residence time for the maximum
value in the transfer function (i.e., \( E(\tau_{\text{peak}}) = \max (E(t)) \)). Figure S10 shows that the error in SOA PF was the smallest when the delay-correction constant was close to \( \tau_{\text{peak}} \).

### A2 Vehicle exhaust measurements

The vehicle in real driving cycle measurements was a Euro 6 gasoline vehicle equipped with 1.4 L turbocharged direct injection engine (110 kW). The vehicle was soaked for 15 h before the cold-start cycle and pre-conditioned by driving at 80 km h\(^{-1}\) for 5 min before the hot-start cycle. The hot-start cycle started with an idling engine. In the simulations, it was assumed that the OFRs are flushed with zero air until the cycle starts and immediately after the cycle ends. So even though the engine is running before the start of hot-start NEDC, the OFRs are filled with zero air at \( t = 0 \) s.

The total hydrocarbon concentration (methane-equivalent ppm) was measured with a flame ionization detector and the CO\(_2\) concentration with a non-dispersive infrared analyzer. Both gases were sampled directly from the tailpipe. The exhaust mass flow rate was calculated based on the intake airflow rate and fuel consumption obtained from the on-board diagnostics data. The fuel carbon content \((k')\) of 860 g kg\(^{-1}\) was used in the calculations.

**Code and data availability.** The engine exhaust data for the real driving cycles are available in the Supplement. The MATLAB code to reproduce the analysis is available in the Supplement.

**Supplement.** The supplement related to this article is available online at: https://doi.org/10.5194/amt-17-3219-2024-supplement.

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**Competing interests.** Jorma Keskinen is a member of the board of Dekati Ltd.

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