



Supplement of

Global validation of the Particulate Observing Scanning Polarimeter (POSP) Aerosol Optical Depth products over land

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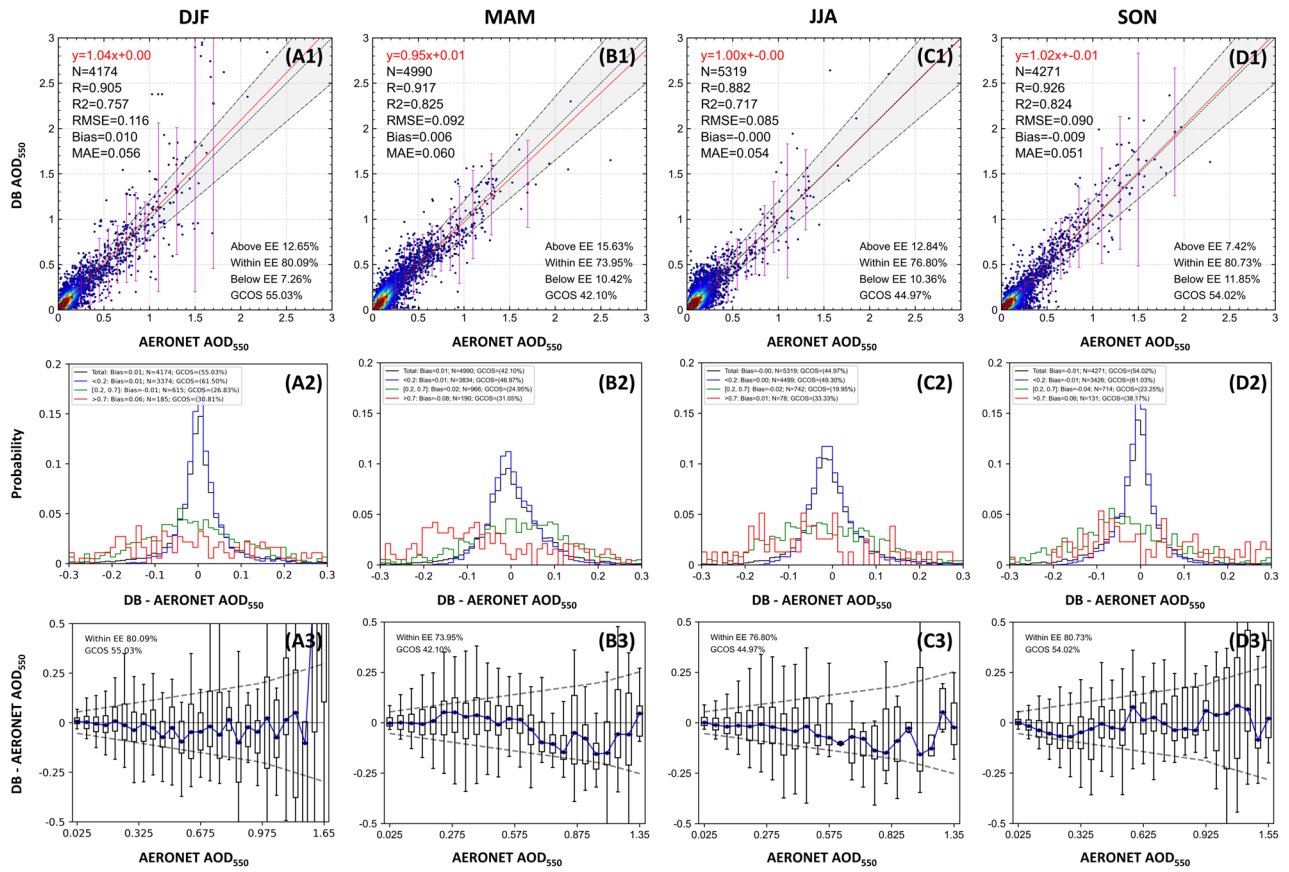


Figure S1: The same as Figure 1 but for different seasons. (1) Density scatter plots of DB AOD with AERONET AOD; (2) The probability density functions of differences (DB-AERONET); (3) Box plots of difference between DB AOD and AERONET AOD against AERONET AOD, in (A) DJF, (B) MAM, (C) JJA, and (D) SON.

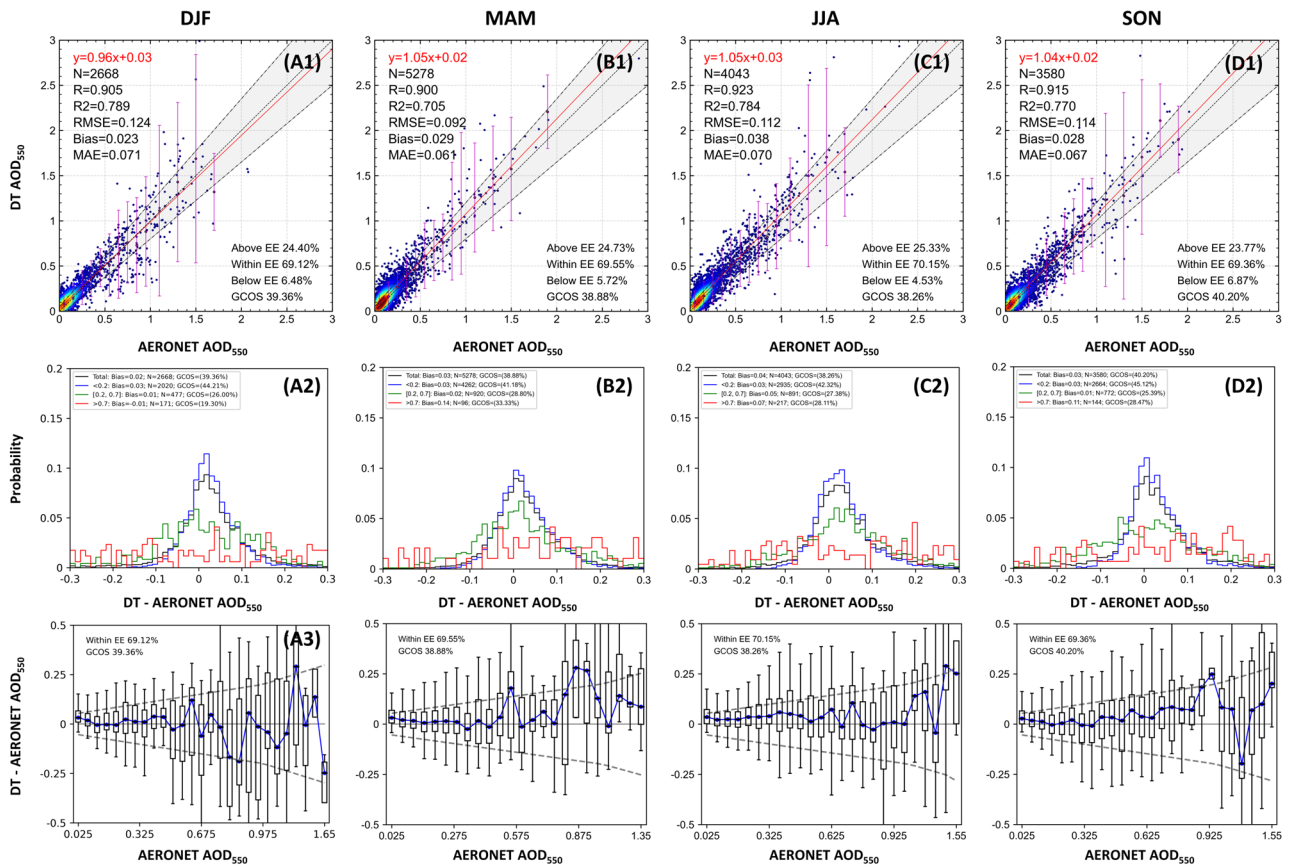


Figure S2: The same as Figure S1, but for DT.

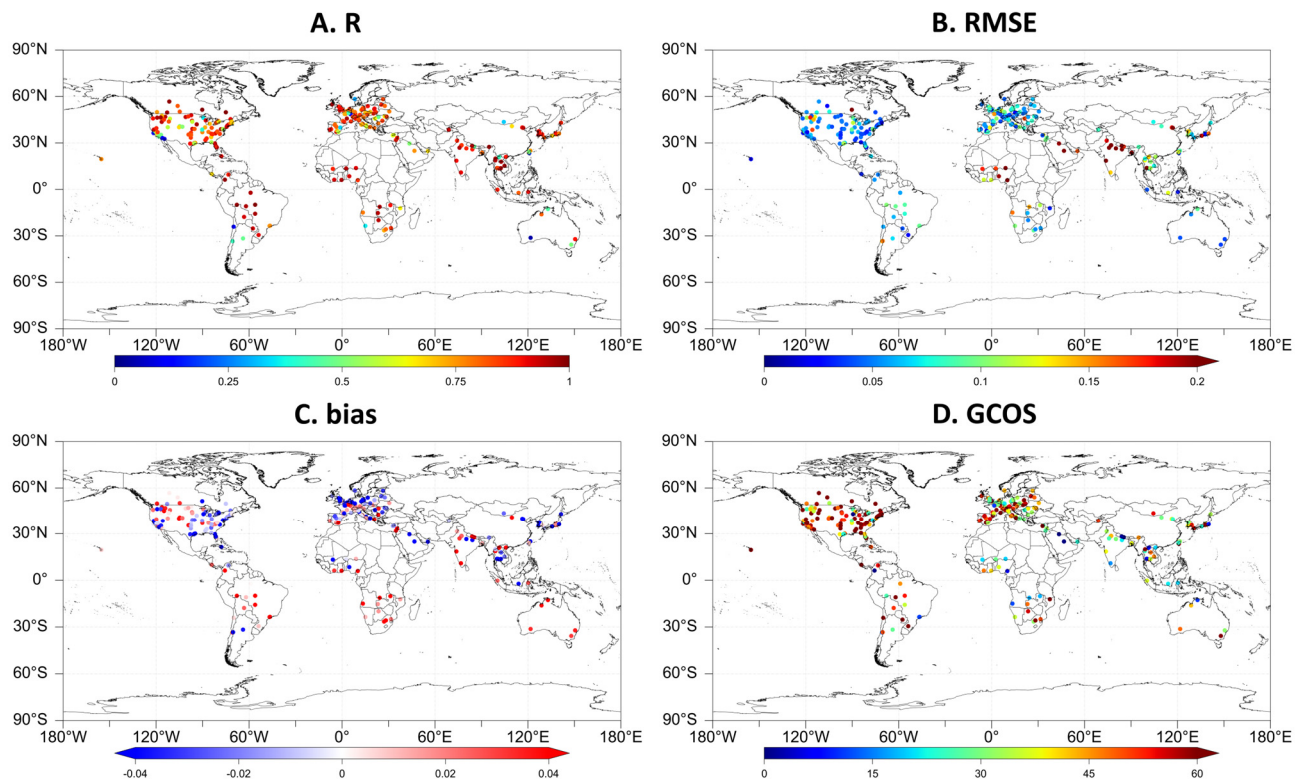
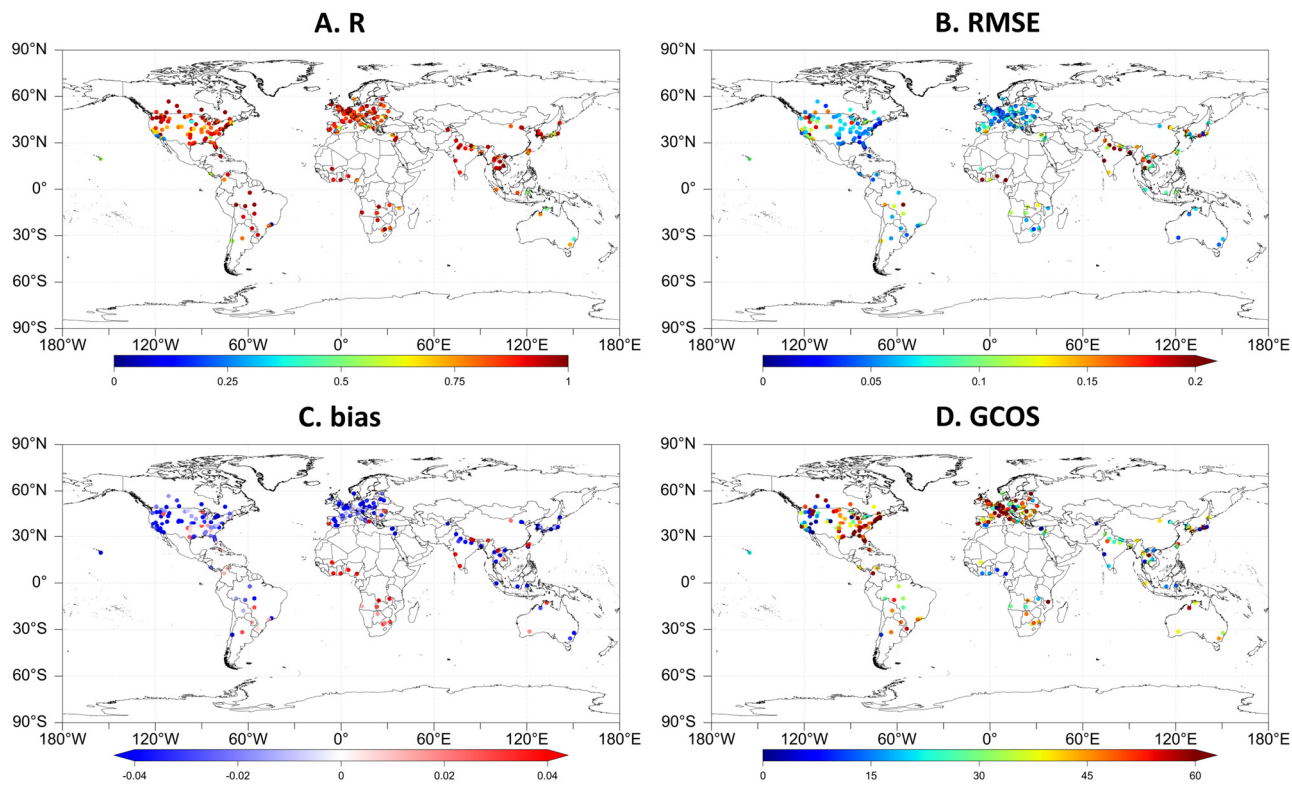


Figure S3: Site-scale statistics of the comparison of DB AOD versus AERONET AOD: (A) R, (B) RMSE, (C) Bias, and (D) GCOS.



20 **Figure S4:** The same as Fig. S4, but for DT.

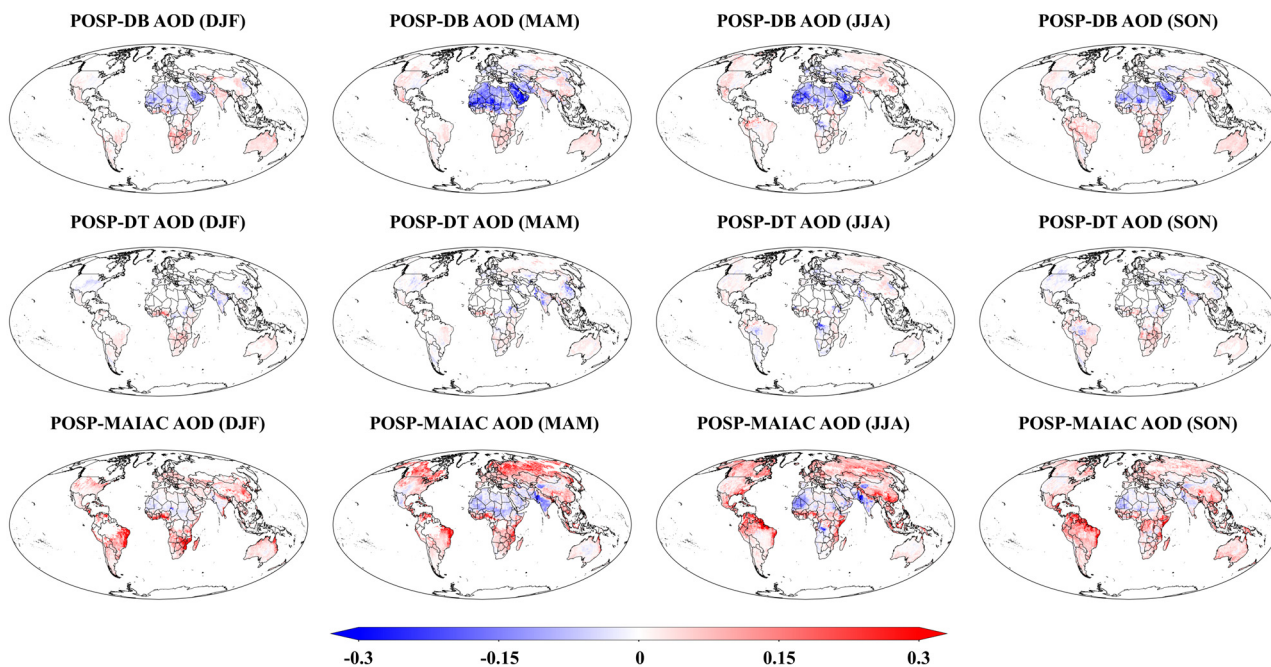


Figure S5: The differences between the seasonally averaged AOD from POSP and MODIS product for the year 2022.

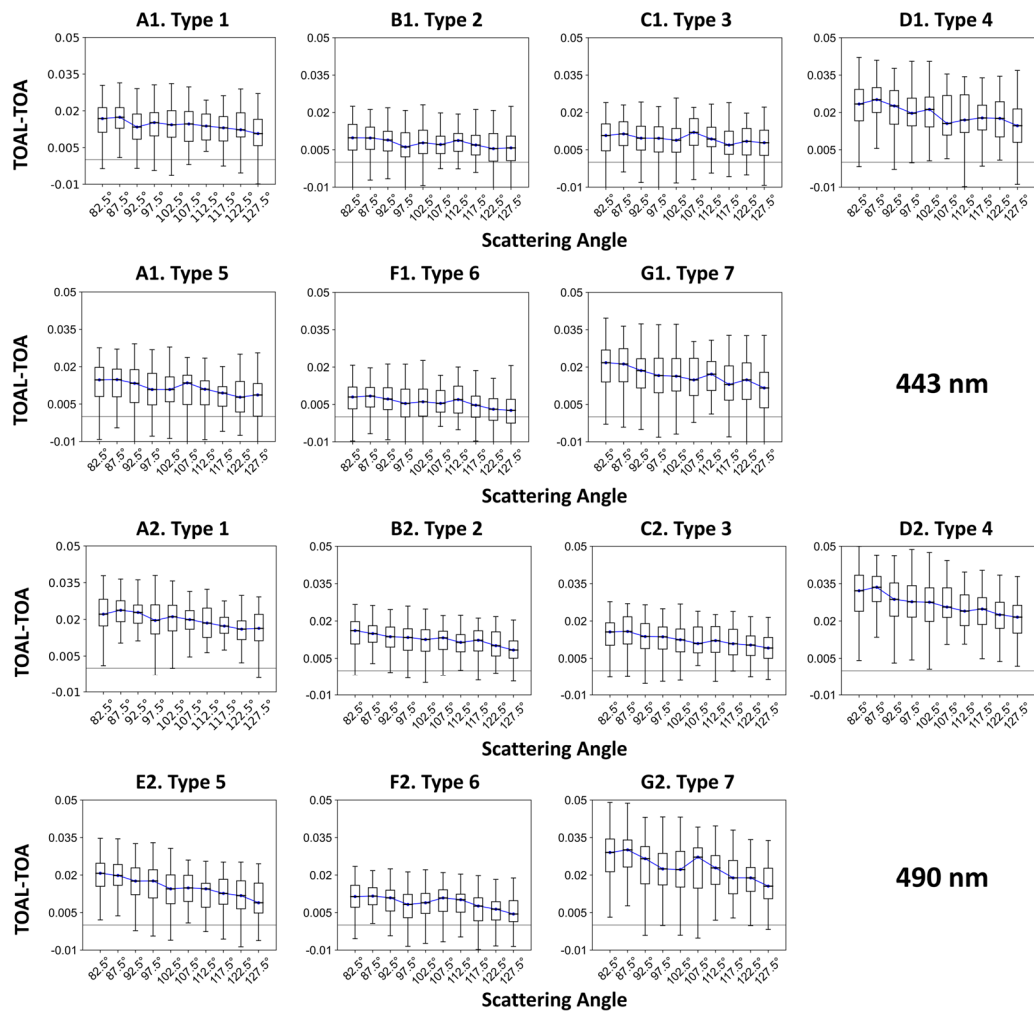


Figure S6: The boxplot of the differences for apparent reflectance between the results calculated based on the Lambertian forward radiative transfer model (TOAL) and the non-Lambertian forward radiative transfer model (TOA). The upper panel shows the differences as a function of AOD, while the lower panel presents the differences as a function of the scattering angle.

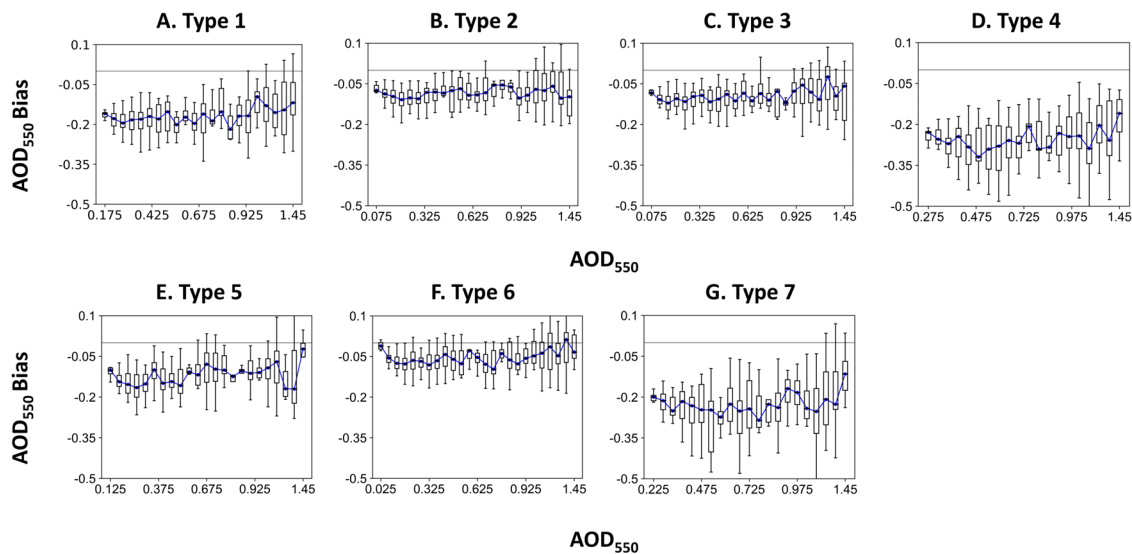


Figure S7: AOD bias as a function of aerosol loading for different urban surface types.

BRDF model

The Ross-Thick Li-Sparse (RTLS) model is a widely used semi-empirical kernel-driven model and is also the model used in the MODIS BRDF/Albedo product (MCD43) (Schaaf et al., 2002). The kernel functions are calculated as follows:

$$K_{iso}(\theta_s, \theta_v, \varphi) = 1 \quad (S1)$$

$$K_{vol}(\theta_s, \theta_v, \varphi) = \frac{\left(\frac{\pi}{2} - \xi\right) \cos \xi + \sin \xi}{\cos \theta_s + \cos \theta_v} - \frac{\pi}{4} \quad (S2)$$

where ξ is the phase angle calculated as:

$$\cos \xi = \cos \theta_s \cos \theta_v + \sin \theta_s \sin \theta_v \cos \varphi \quad (S3)$$

$$K_{geo}(\theta_s, \theta_v, \varphi) = O(\theta_s, \theta_v, \varphi) - \sec \theta'_s - \sec \theta'_v + \frac{1}{2}(1 + \cos \xi') \sec \theta'_s \sec \theta'_v \quad (S4)$$

where $O(\theta_s, \theta_v, \varphi)$ is the overlap area between the view and solar shadows, calculated as

$$O(\theta_s, \theta_v, \varphi) = \frac{1}{\pi}(t - \sin t \cos t)(\sec \theta'_s + \sec \theta'_v) \quad (S5)$$

with

$$\cos t = \frac{h \sqrt{D^2 + (\tan \theta'_s \tan \theta'_v \sin \varphi)^2}}{b \sec \theta'_s + \sec \theta'_v} \quad (S6)$$

$$D = \sqrt{\tan^2 \theta'_s + \tan^2 \theta'_v - 2 \tan \theta'_s \tan \theta'_v \cos \varphi} \quad (S7)$$

$$\cos \xi' = \cos \theta'_s \cos \theta'_v + \sin \theta'_s \sin \theta'_v \cos \varphi \quad (S8)$$

$$\theta'_s = \tan^{-1} \left[\frac{b}{r} \tan \theta_s \right] \quad \theta'_v = \tan^{-1} \left[\frac{b}{r} \tan \theta_v \right] \quad (S9)$$

In the RTLS model, h is the distance from the center of the ellipsoid to the ground, b is the length of the long half-axis radius of the ellipsoid, and r is the length of the short half-axis radius of the ellipsoid. In the MODIS BRDF product, $h/b=2, b/2=1$ is assumed (Lucht et al., 2000).

Non-Lambertian forward radiative transfer model

Qin et al. (2015) proposed a non-Lambertian forward radiative transfer model as an improvement over the original four-stream radiative transfer model:

$$\rho_{TOA} = \rho_0 + \frac{\vec{T}(\mu_s)^T \mathbf{R} \vec{T}(\mu_v) - e^{-\tau/\mu_s} |\mathbf{R}| e^{-\tau/\mu_v}}{1 - \rho_{BHR} S} \quad (S10)$$

$$\mathbf{R} = \begin{bmatrix} \rho & \rho_{DHR} \\ \rho_{HDR} & \rho_{BHR} \end{bmatrix} \quad (S11)$$

55 where, μ_s and μ_v refer the cosine of solar zenith angle and viewing zenith angle, respectively; ρ_0 refers to the path reflectance; S is the spherical albedo of the atmosphere. R denotes the reflectance matrix, ρ_{DHR} is the directional–hemispherical reflectance (DHR), ρ_{HDR} is the hemispherical–directional reflectance (HDR), ρ_{BHR} is the bihemispherical reflectance (BHR) equal to the surface albedo, and $|R|$ is the determinant of R . $\vec{T}(\mu_s) = \begin{bmatrix} e^{-\frac{\tau}{\mu_s}} & t_d(\mu_s) \end{bmatrix}^T$ and $\vec{T}(\mu_v) = \begin{bmatrix} e^{-\frac{\tau}{\mu_v}} & t_d(\mu_v) \end{bmatrix}^T$ are transmission matrices, t_d refers to the diffuse transmission. The description of the model is excerpted from (Ji et al., 2025).

60 Lambertian forward radiative transfer model

Assuming a uniform Lambertian surface, a horizontally averaged atmosphere, and atmospheric molecules primarily exist above the aerosol layer, the Top-of-Atmosphere (TOA) reflectance can be expressed as follows:

$$\rho^* = T_{\text{gas}} \left[\rho^R + T^R(\mu_s) \frac{\rho_G}{1 - S\rho_G} T^R(\mu_v) \right] \quad (\text{S12})$$

Where ρ^* is the apparent reflectance at the satellite observation, T_{gas} is the gas transmittance, $T^R(\mu_s)$ and $T^R(\mu_v)$ are the
65 upward and downward atmospheric transmittances, respectively, ρ_G is the surface-coupled reflectance, and S is the spherical albedo. The description of the model is excerpted from (Ji et al., 2024).

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