



Supplement of

MISR research-aerosol-algorithm refinements for dark water retrievals

J. A. Limbacher and R. A. Kahn

Correspondence to: R. A. Kahn (ralph.kahn@nasa.gov)

Real Refractive Index (n_r) Sensitivity Study

[Figures S1 – S5]

This section expands on the AOD retrieval sensitivity analysis for the real refractive index (n_r), illustrated in Figure 6 of the main paper. It covers a range of particle sizes, and n_r as well as AOD values are varied systematically for the particles assumed in the algorithm comparison space.

For each figure, the simulated atmosphere contains single-mode particles having n_r and effective radius (r_e) given at the top. Comparison-space particles, having varying n_r , are defined above each panel; comparisons are made for three values of AOD and a range of geometries. The geographic placement of the plots is for illustration – over-water conditions are assumed everywhere, with the surface pressure prescribed as 1013.25 mb, and the surface wind speed set to 2.5 m/s.

Parameter Space

Simulated Atmosphere **r_e values** (μm): 0.12, 0.26, 0.57, 1.28, 2.80

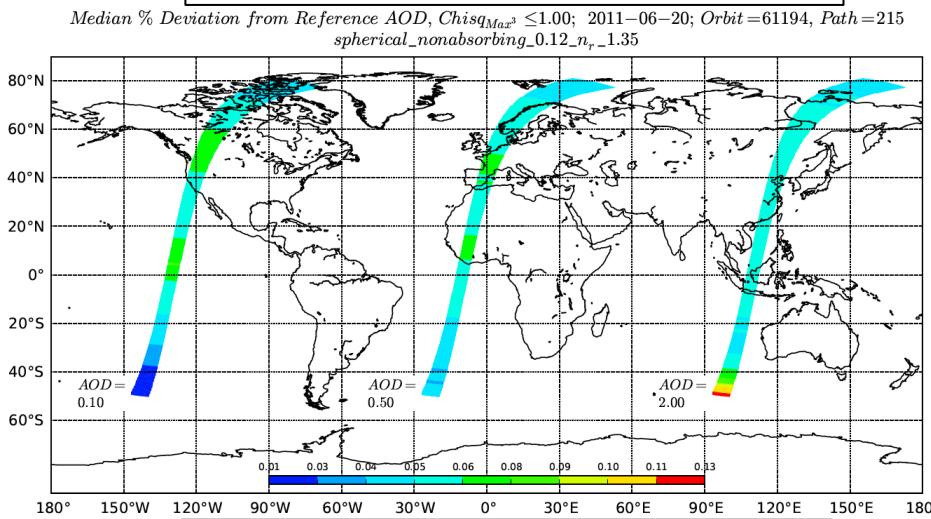
Simulated Atmosphere **AOD values:** 0.1, 0.5, 2.0

Simulated Atmosphere **n_r value:** 1.45

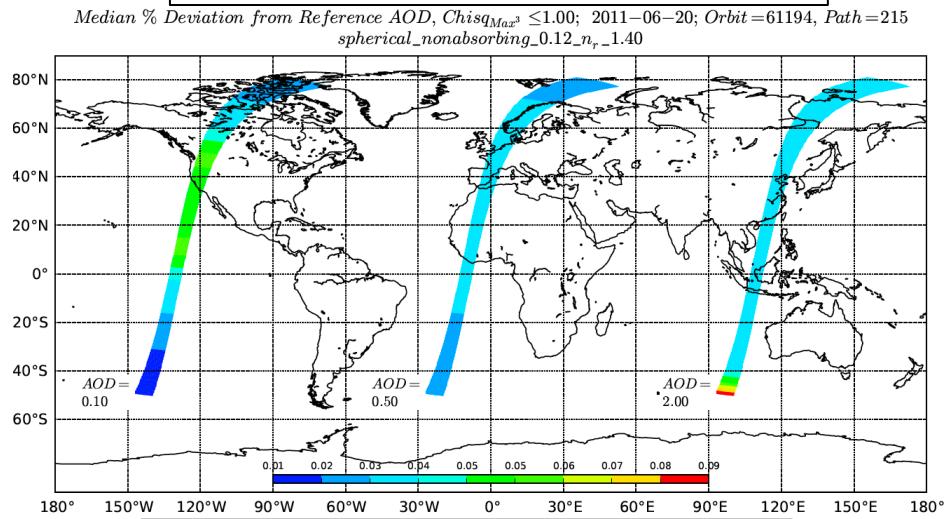
Comparison Space **n_r values:** 1.35, 1.40, 1.50, 1.55

Input Atmospheric Particles: $n_r=1.45, r_e=0.12 \mu\text{m}$

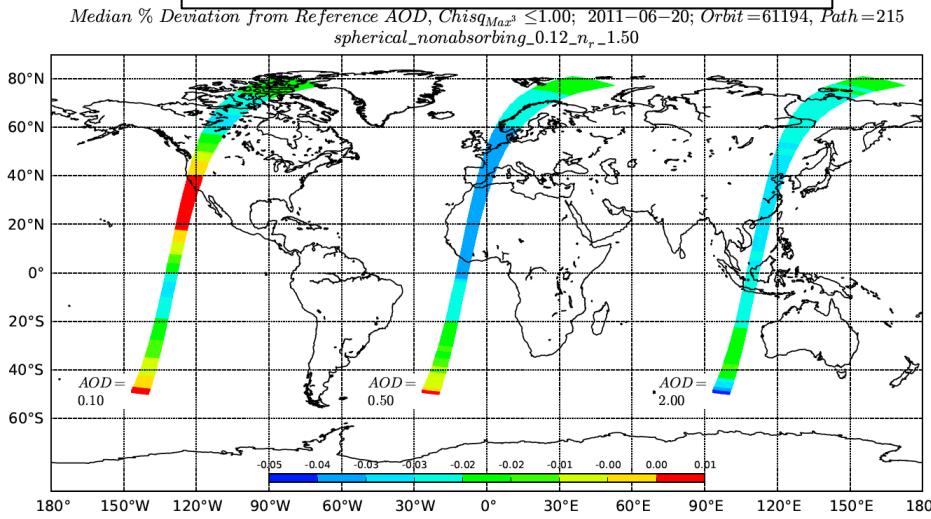
< +9% Discrepancy, Comp. space $n_r=1.35$



< +5% Discrepancy, Comp. space $n_r=1.40$



< -4% Discrepancy, Comp. space $n_r=1.50$



< -8% Discrepancy, Comp. space $n_r=1.55$

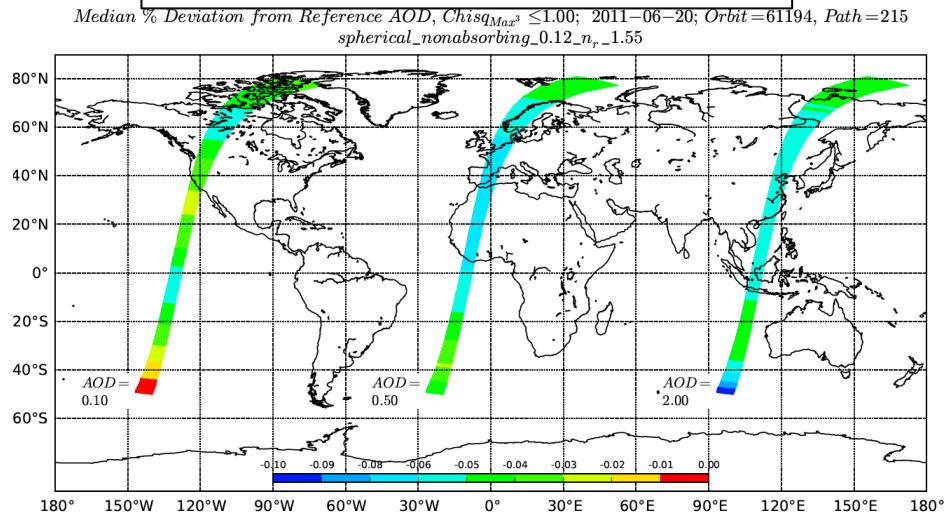
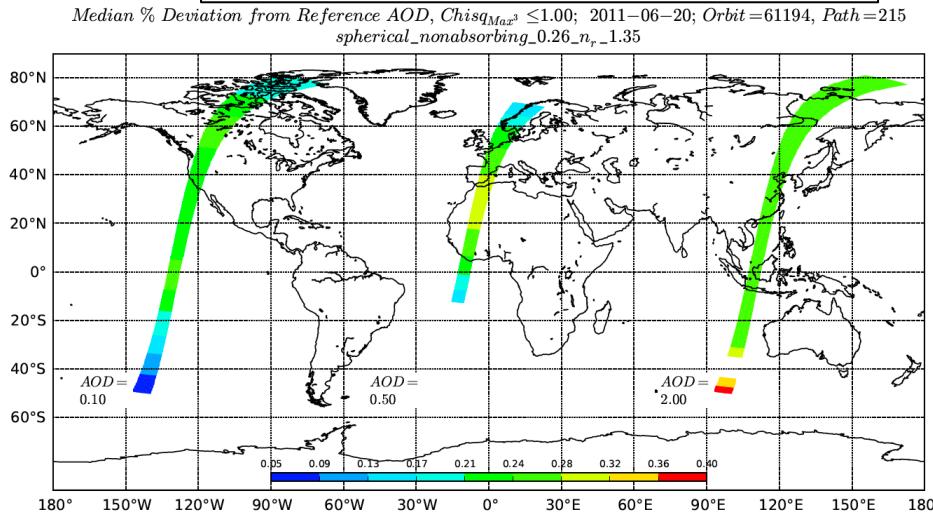


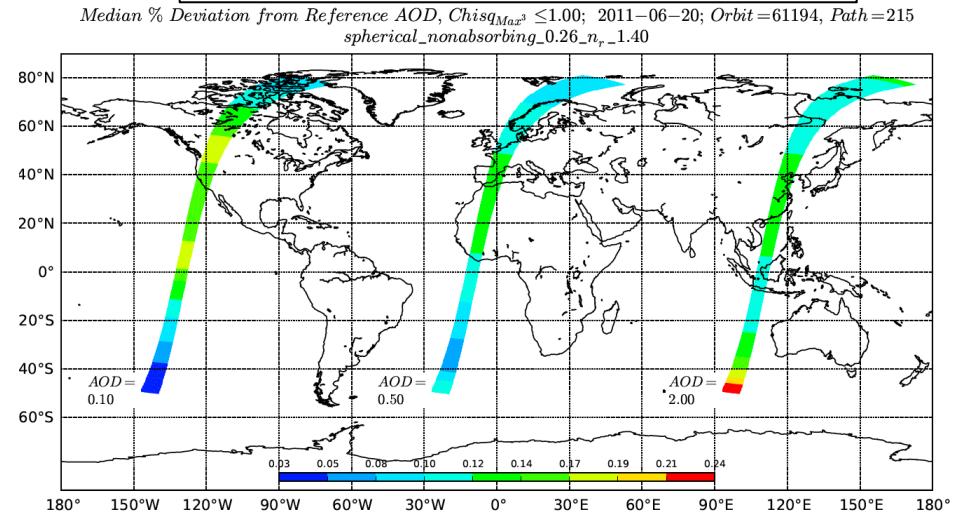
Figure S1

Input Atmospheric Particles: $n_r=1.45, r_e=0.26 \mu\text{m}$

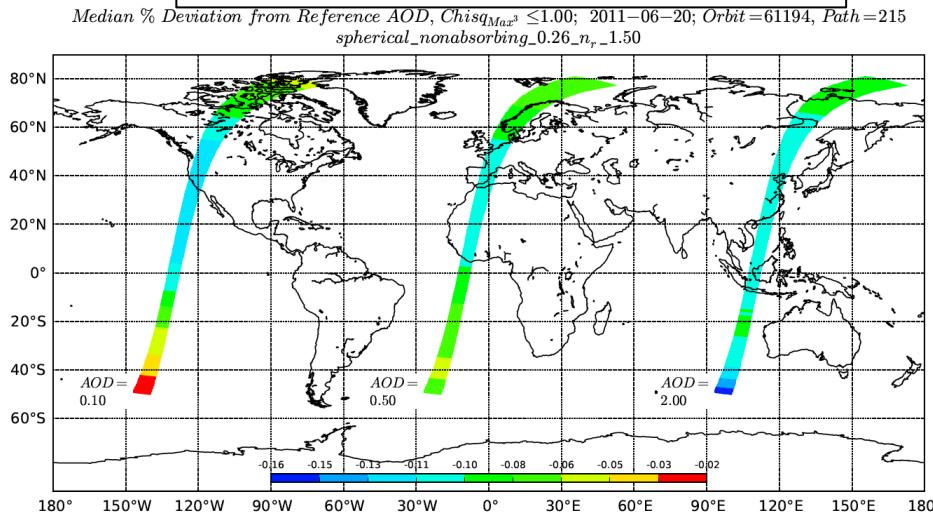
< +32% Discrepancy, Comp. space $n_r=1.35$



< +19% Discrepancy, Comp. space $n_r=1.40$



< -13% Discrepancy, Comp. space $n_r=1.50$



< -27% Discrepancy, Comp. space $n_r=1.55$

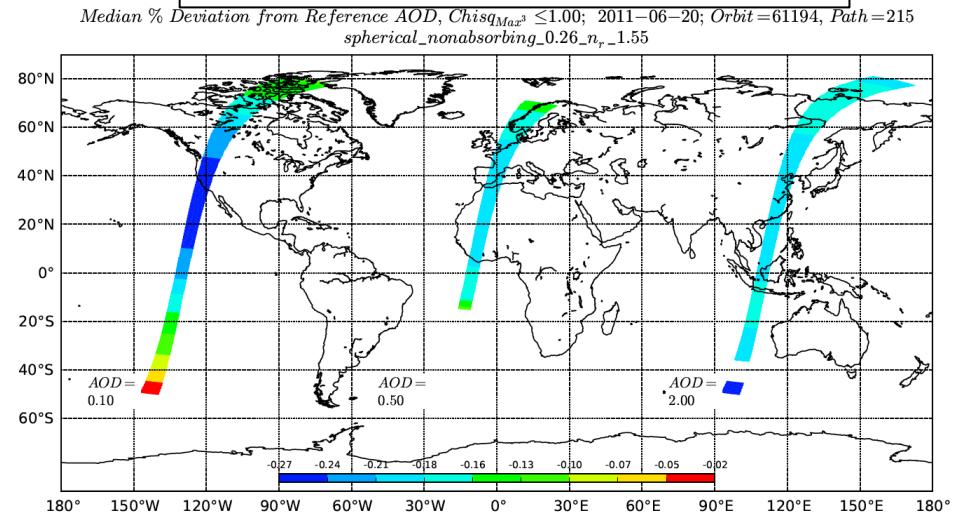
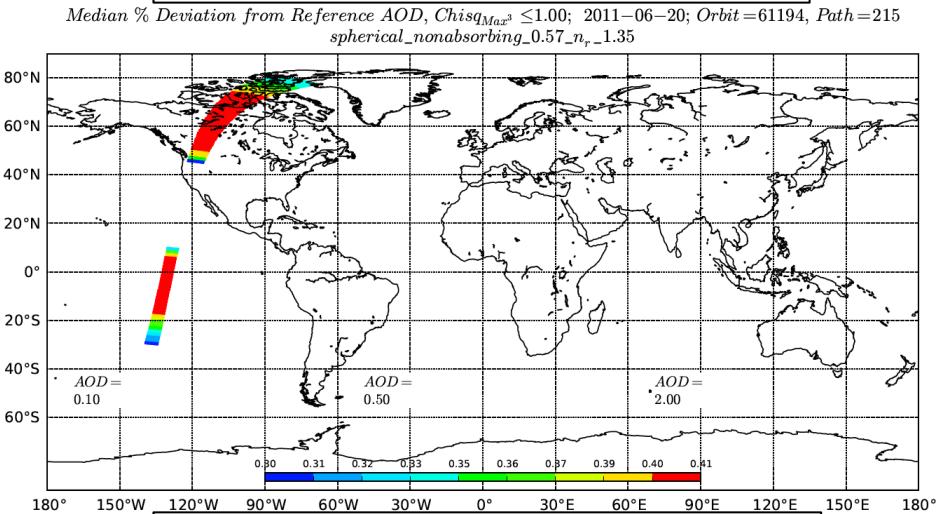


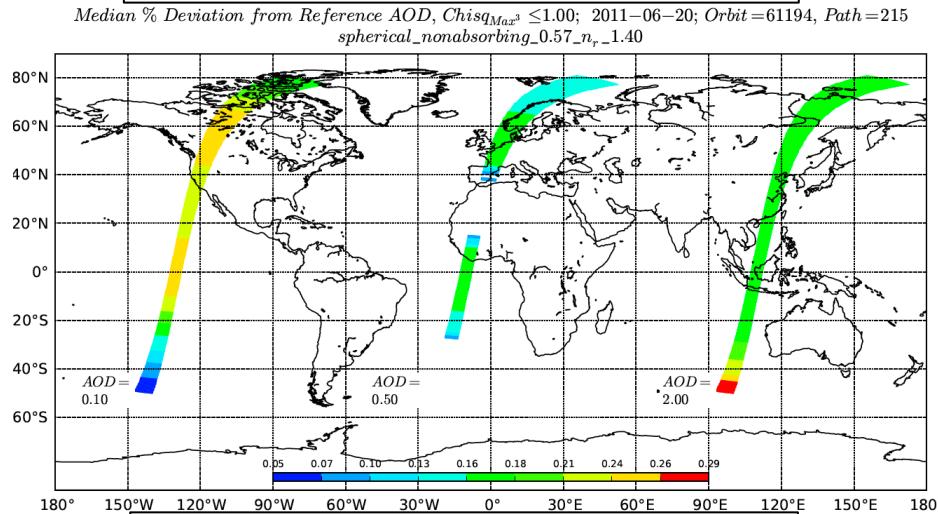
Figure S2

Input Atmospheric Particles: $n_r=1.45, r_e=0.57 \mu\text{m}$

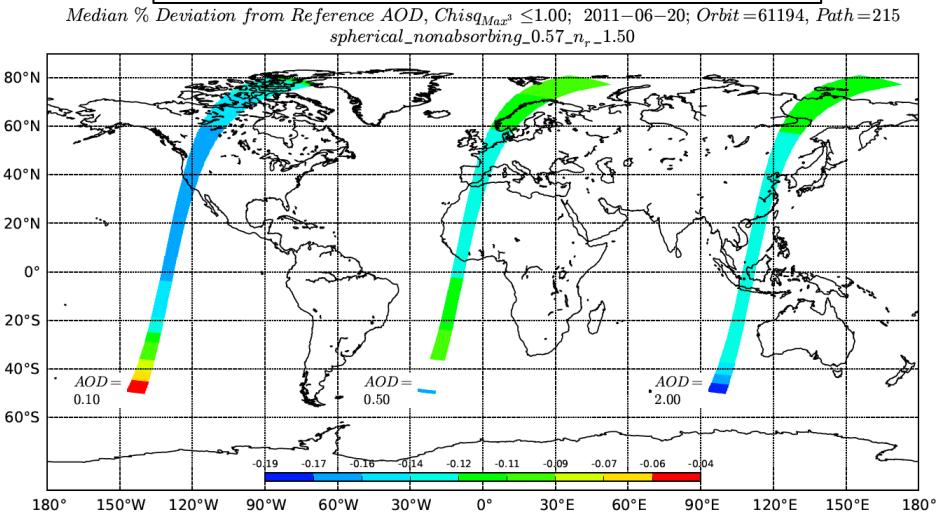
< 41% Discrepancy, Comp. space $n_r=1.35$



< +26% Discrepancy, Comp. space $n_r=1.40$



< -17% Discrepancy, Comp. space $n_r=1.50$



< -31% Discrepancy, Comp. space $n_r=1.55$

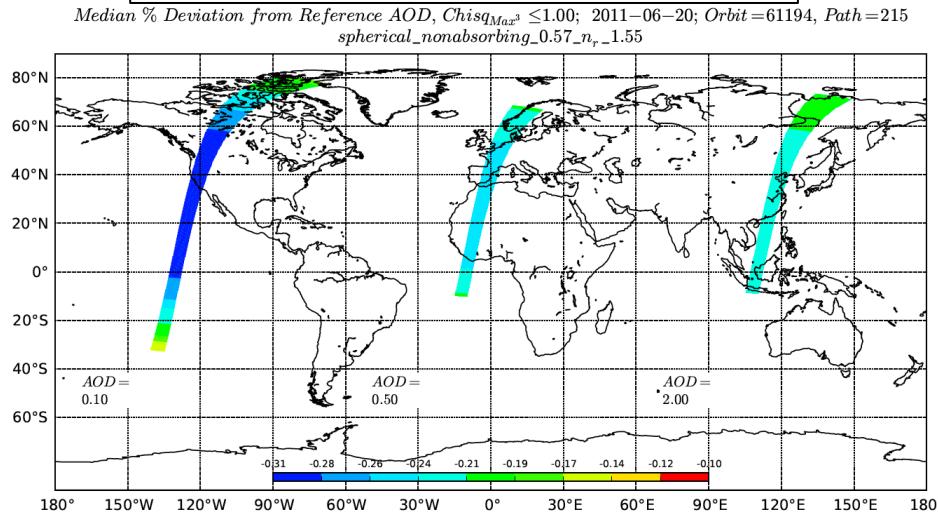
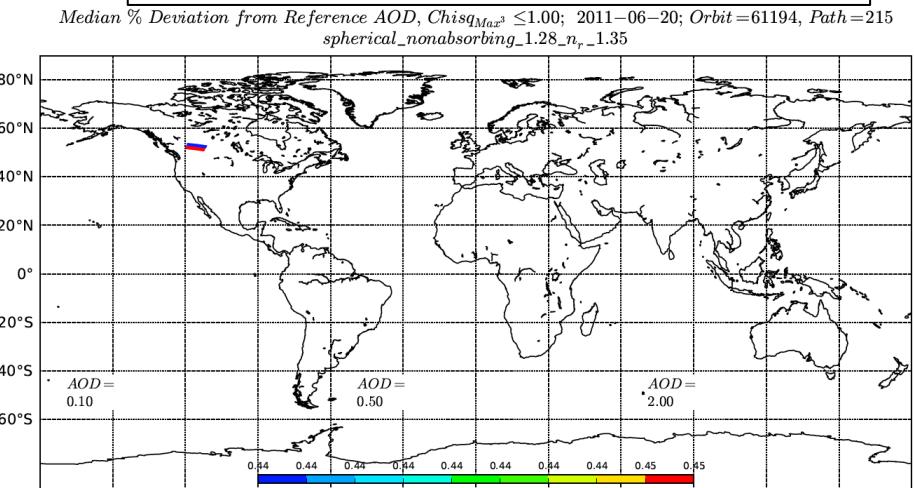


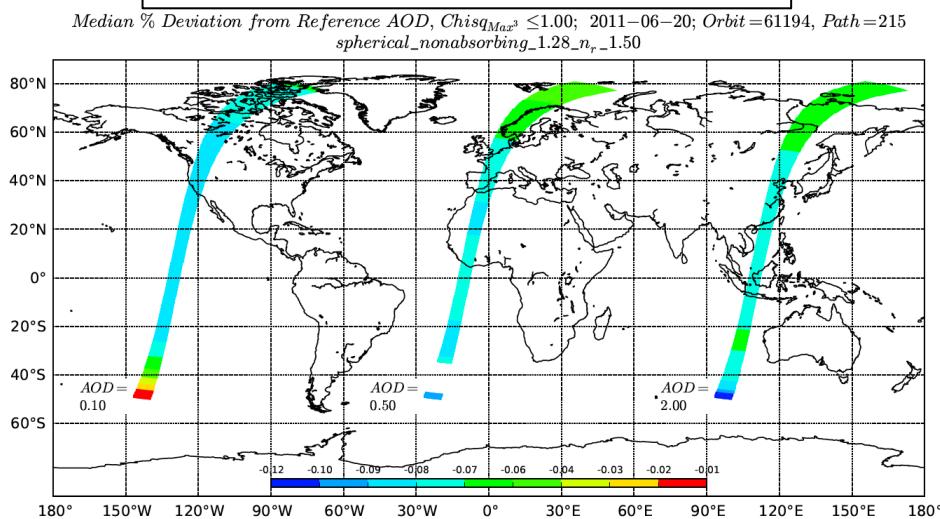
Figure S3

Input Atmospheric Particles: $n_r=1.45, r_e=1.28 \mu\text{m}$

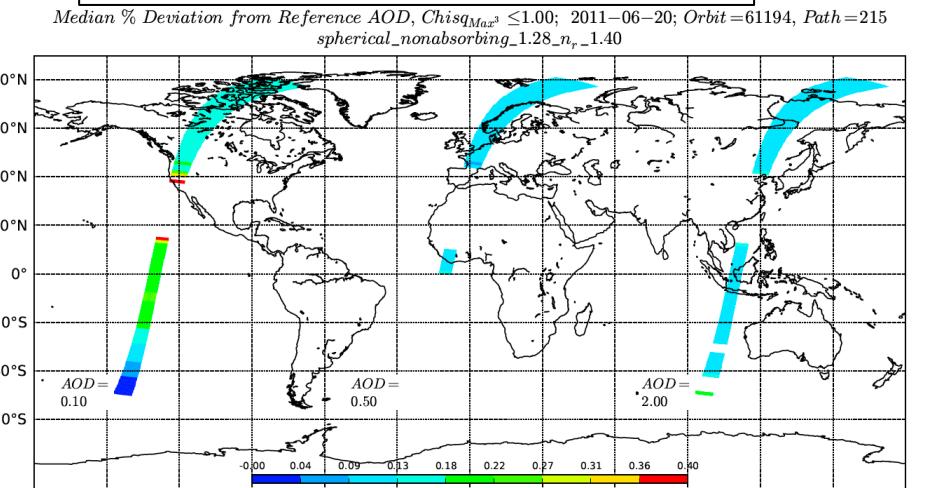
No successful retrievals, Comp. space $n_r=1.35$



< -9% Discrepancy, Comp. space $n_r=1.50$



< +27% Discrepancy, Comp. space $n_r=1.40$



< -16% Discrepancy, Comp. space $n_r=1.55$

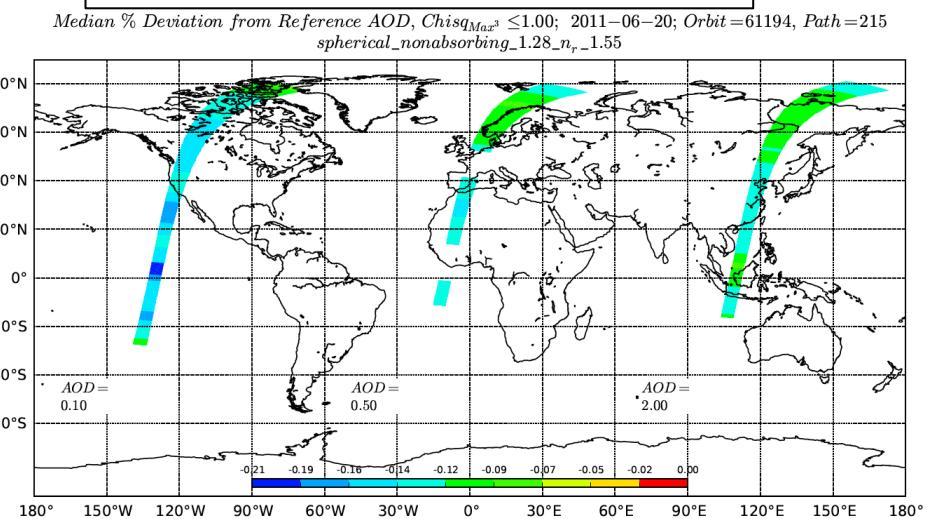


Figure S4

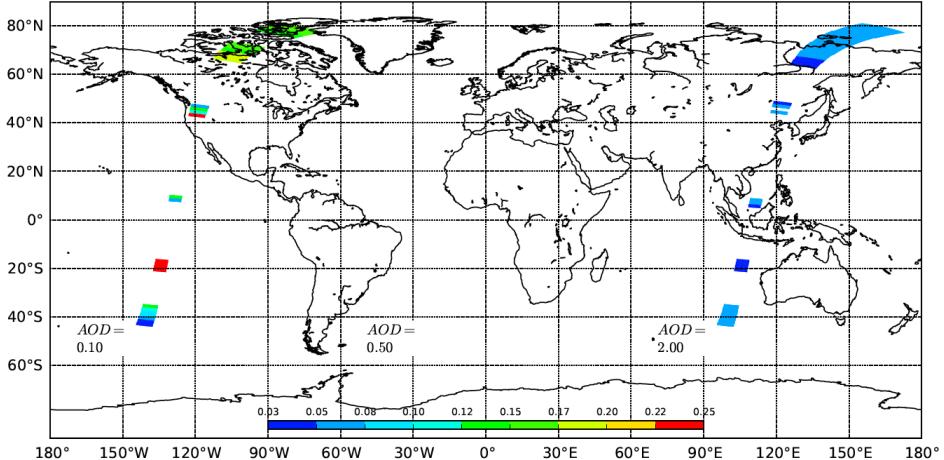
Input Atmospheric Particles: $n_r=1.45, r_e=2.80 \mu\text{m}$

No successful retrievals, Comp. space $n_r=1.35$

**For very large particles,
If n_r deviates by 0.05 or more
no successful retrievals are obtained
(i.e., some retrieval sensitivity to n_r)**

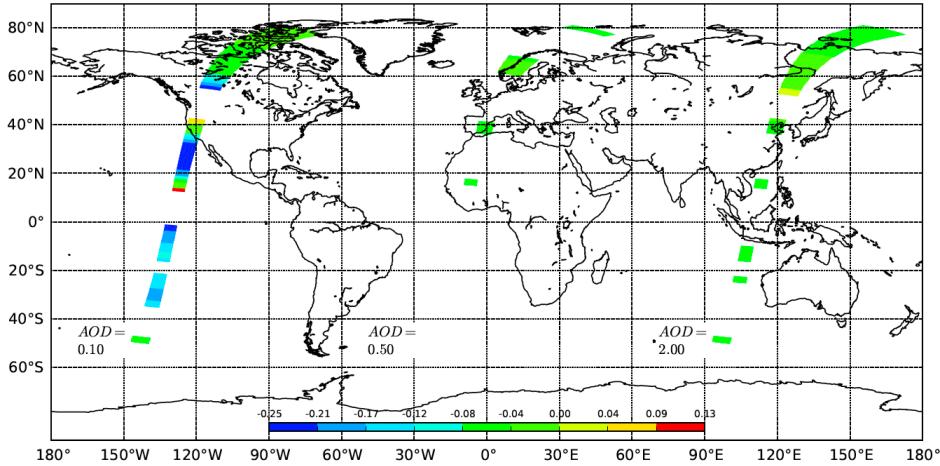
Few successful retrievals, Comp. space $n_r=1.40$

Median % Deviation from Reference AOD, $\text{Chisq}_{\text{Max}}^3 \leq 1.00$; 2011–06–20; Orbit = 61194, Path = 215
spherical_nonabsorbing_2.80_n_r_1.40



Few successful retrievals, Comp. space $n_r=1.50$

Median % Deviation from Reference AOD, $\text{Chisq}_{\text{Max}}^3 \leq 1.00$; 2011–06–20; Orbit = 61194, Path = 215
spherical_nonabsorbing_2.80_n_r_1.50



No successful retrievals, Comp. space $n_r=1.55$

Median % Deviation from Reference AOD, $\text{Chisq}_{\text{Max}}^3 \leq 1.00$; 2011–06–20; Orbit = 61194, Path = 215
spherical_nonabsorbing_2.80_n_r_1.55

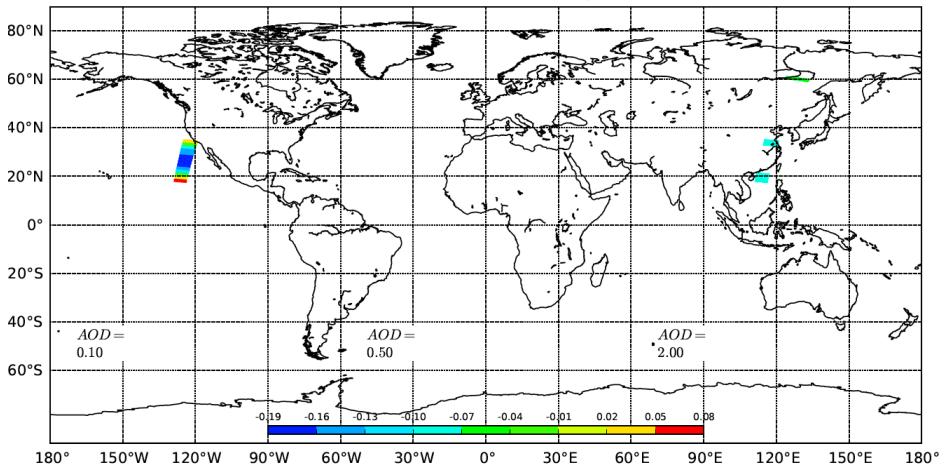


Figure S5

Real Refractive Index Sensitivity Study **Conclusions**

[Figures S1 – S5]

- When n_r is **overestimated**, AOD is systematically **underestimated**, and conversely
- Generally, retrieved AOD values **still fall within 0.05 or 20% AOD**, except in extreme cases
- **Smaller particles** are affected less by errors in n_r ,
- **Very large particles** are so sensitive to changes in n_r that mixtures **might not pass** the algorithm acceptance criteria if n_r deviates too far (~ 0.05) from the correct value
- **Medium particles** (0.26-0.57 μm) produce the largest AOD deviations for $\sim 0.1 n_r$ error, but are not sensitive enough to n_r to retrieve the correct value. Summary:
 - $r_e = 0.12 \mu\text{m}$: 5%-7.5% max. deviation for every 0.1 deviation from the correct n_r [Figure S1]
 - $r_e = 0.26 \mu\text{m}$: 20%-30% max. deviation for every 0.1 deviation from correct n_r [Figure S2]
 - $r_e = 0.57 \mu\text{m}$: 20%-40% max. deviation for every 0.1 deviation from correct n_r [Figure S3]
 - $r_e = 1.28 \mu\text{m}$: 15%-40% max. deviation for every 0.1 deviation from correct n_r [Figure S4]
 - $r_e = 2.80 \mu\text{m}$: variable max. deviation for every 0.1 deviation from correct n_r [Figure S5]
- Distributions having larger effective radii tend to have biases that vary considerably **depending on viewing/solar geometry**
- Overall, the **0.57 μm particle tends to perform the worst** if n_r is incorrect; the 0.26 μm particle is a close second. (Mixtures might still pass, but the retrieved AOD discrepancy can be $> 0.05/20\%$.)

Linear Mixing (LM) & Modified-Linear Mixing (MLM)

Sensitivity Study

This section expands on the AOD retrieval sensitivity analysis for ***Linear Mixing*** and ***Modified Linear Mixing***, as illustrated in Figure 7 of the main paper. MLM is used to approximate the radiative effects of mixtures containing two or more optically distinct aerosol components, based on pre-run radiative transfer calculations for the components individually [Abdou *et al.*, 1997]. This supplement considers bi-modal particle distributions covering a range of particle sizes and SSA values, comparing retrieved AOD results from LM and MLM with those derived from runs of the radiative transfer code using layer-effective phase function (Equs. 3 of the main text).

For each figure in this section, the simulated atmosphere and retrieval climatology contain the same bi-modal mixture of particles, specified in the figure annotation, and taken from the SA climatology [Kahn *et al.*, 2010]. Comparisons are made between radiative transfer runs using layer-effective phase function and LM or MLM approximations, for five values of AOD and a range of geometries. (The geographic placement of the plots is for illustration – all retrievals are performed over simulated black surfaces.) Mixture numbers in the figures correspond to the climatology in the MISR V22 SA climatology.

[Note that *MLM* reduces to *LM* when all particles in the mixture are non-absorbing or have the same SSA.]

Impact of *Linear Mixing*; Globally, Non-Absorbing Aerosol

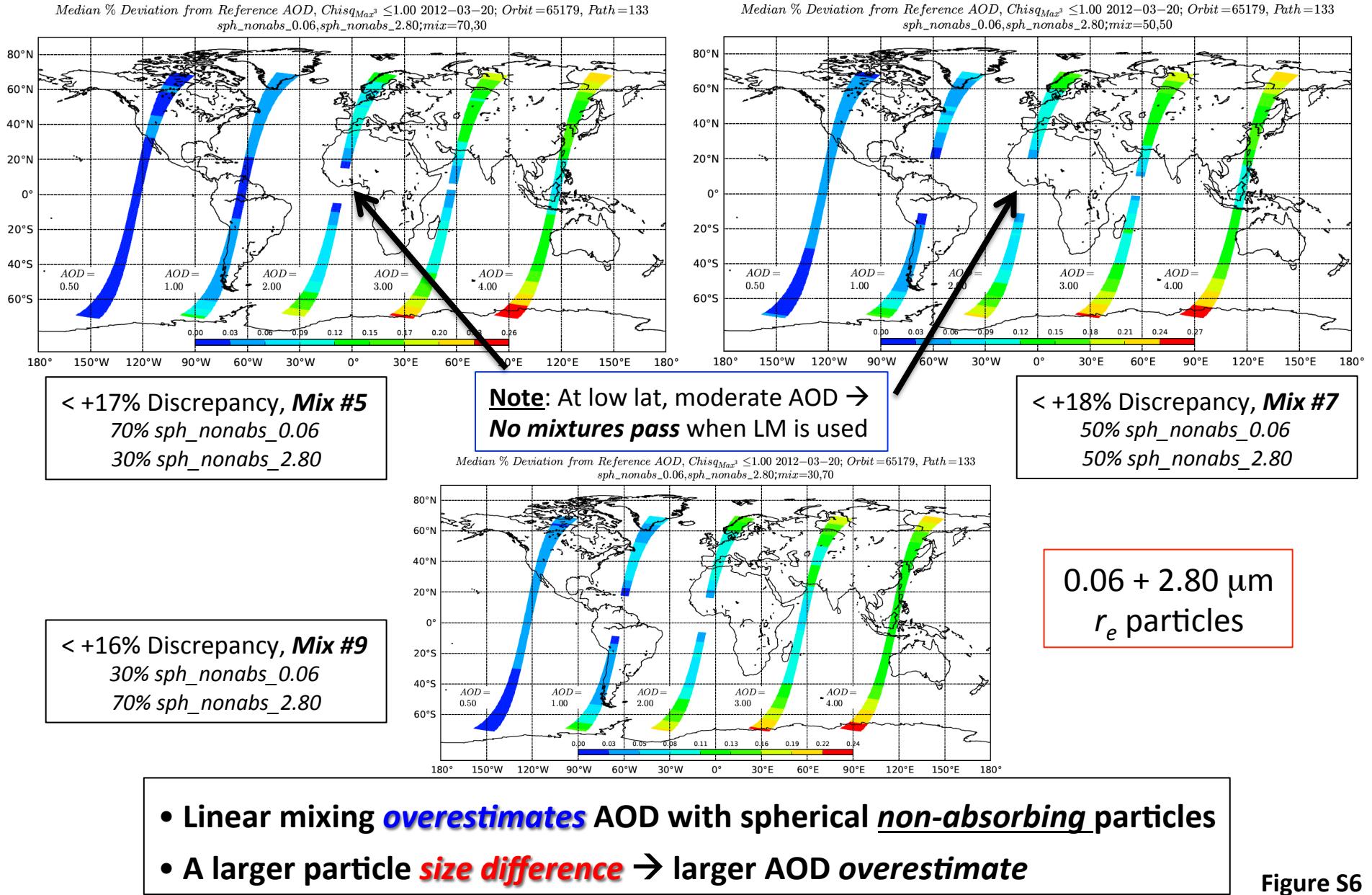


Figure S6

Impact of *Linear Mixing*; Globally, Non-Absorbing Aerosol

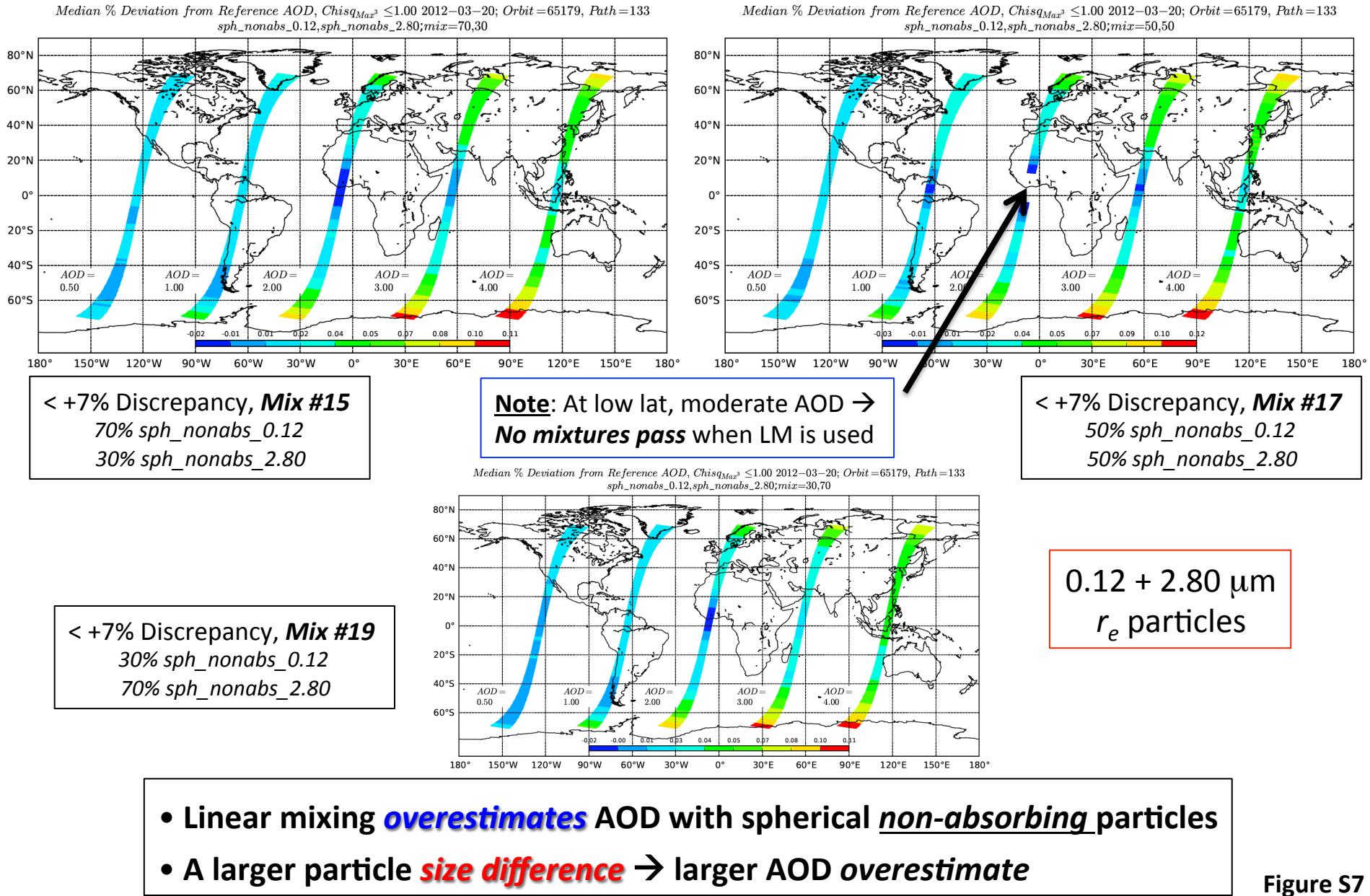
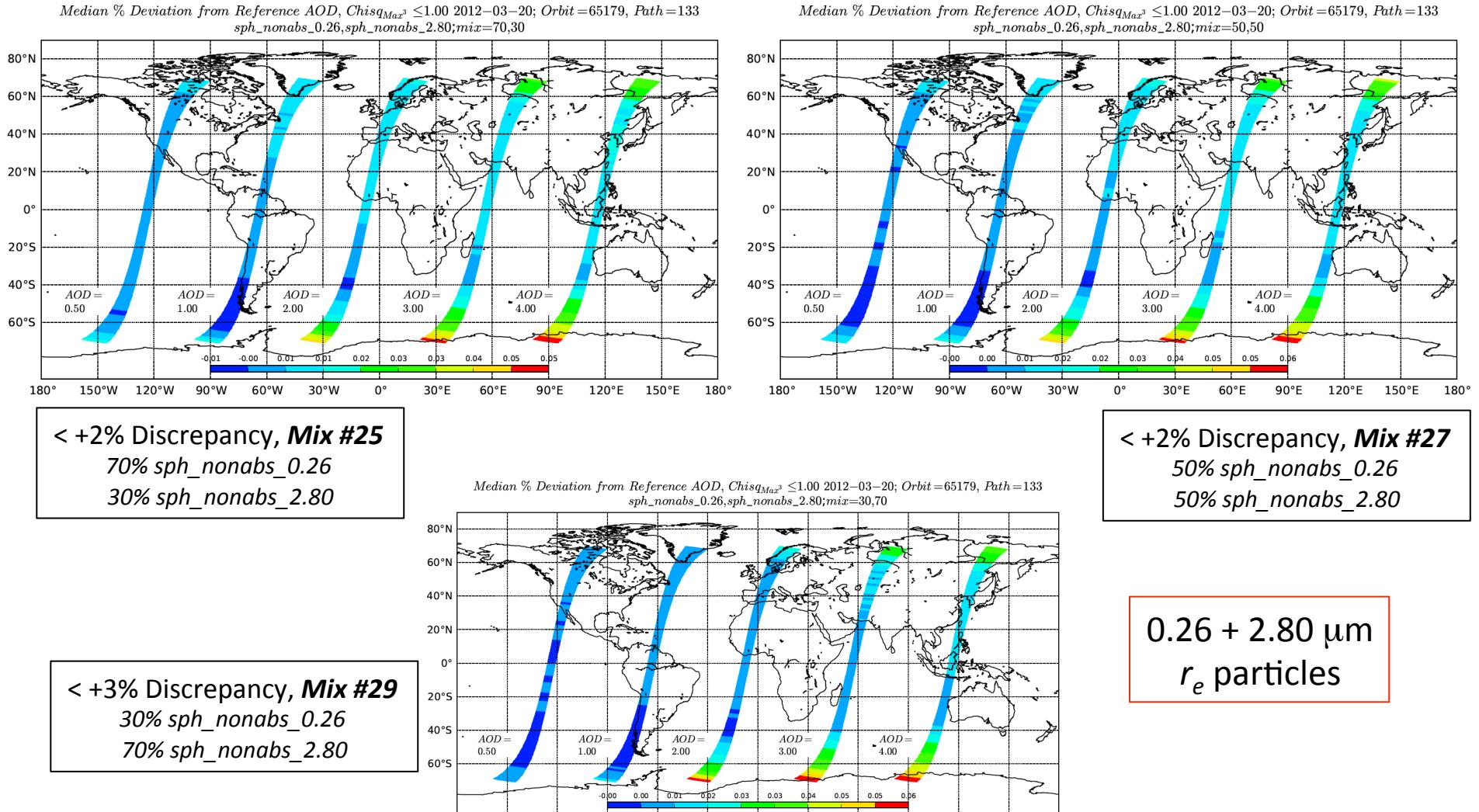


Figure S7

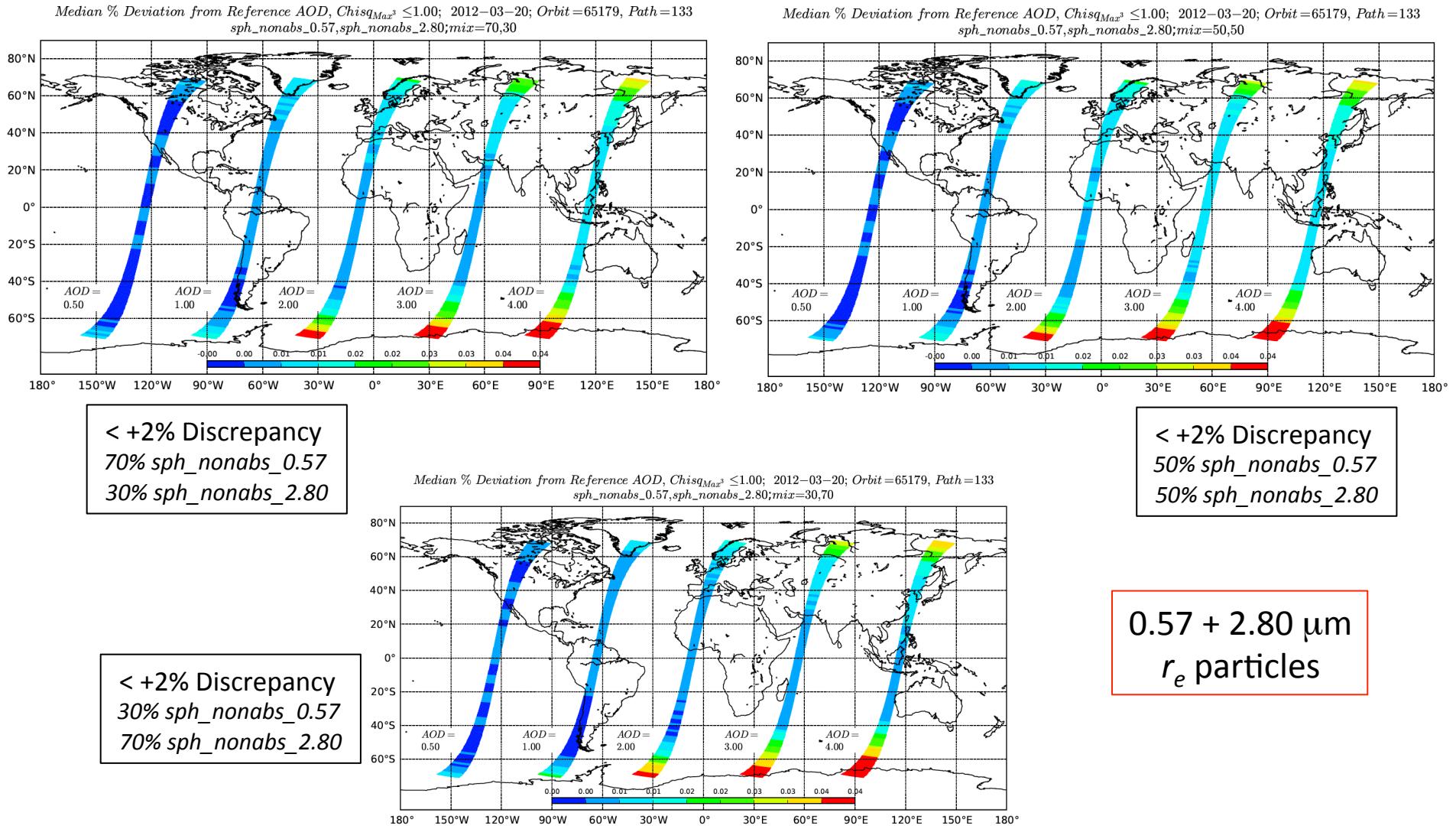
Impact of *Linear Mixing*; Globally, Non-Absorbing Aerosol



- Linear mixing **overestimates** AOD with spherical non-absorbing particles
- A larger particle **size difference** → larger AOD **overestimate**

Figure S8

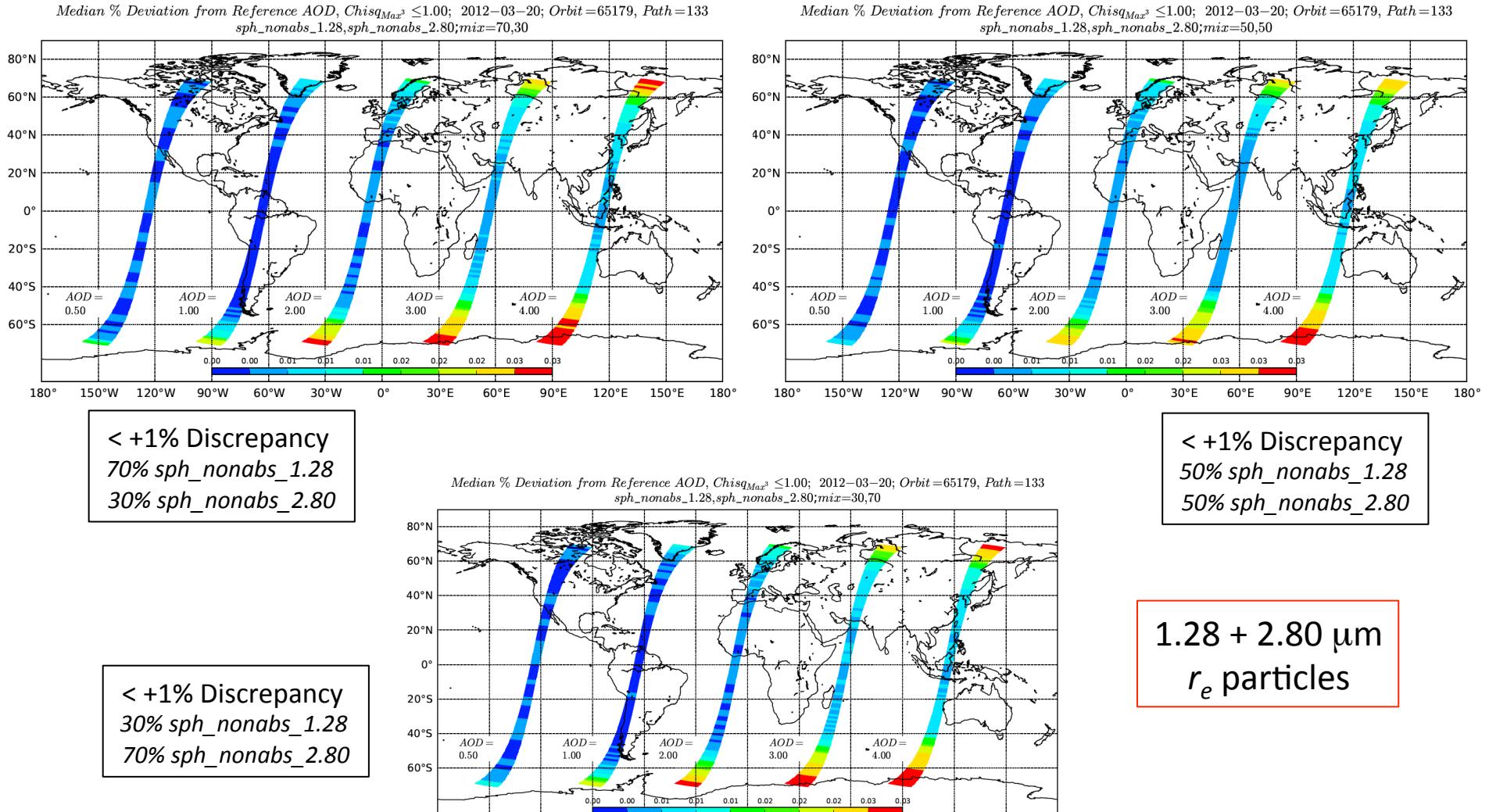
Impact of *Linear Mixing*; Globally, Non-Absorbing Aerosol



- Linear mixing **overestimates** AOD with spherical non-absorbing particles
- A larger particle **size difference** → larger AOD overestimate

Figure S9

Impact of *Linear Mixing*; Globally, Non-Absorbing Aerosol



1.28 + 2.80 μm
 r_e particles

- Linear mixing **overestimates** AOD with spherical non-absorbing particles
- A larger particle **size difference** → larger AOD overestimate

Figure S10

Impact of **MLM**; Globally, Absorbing Mixtures

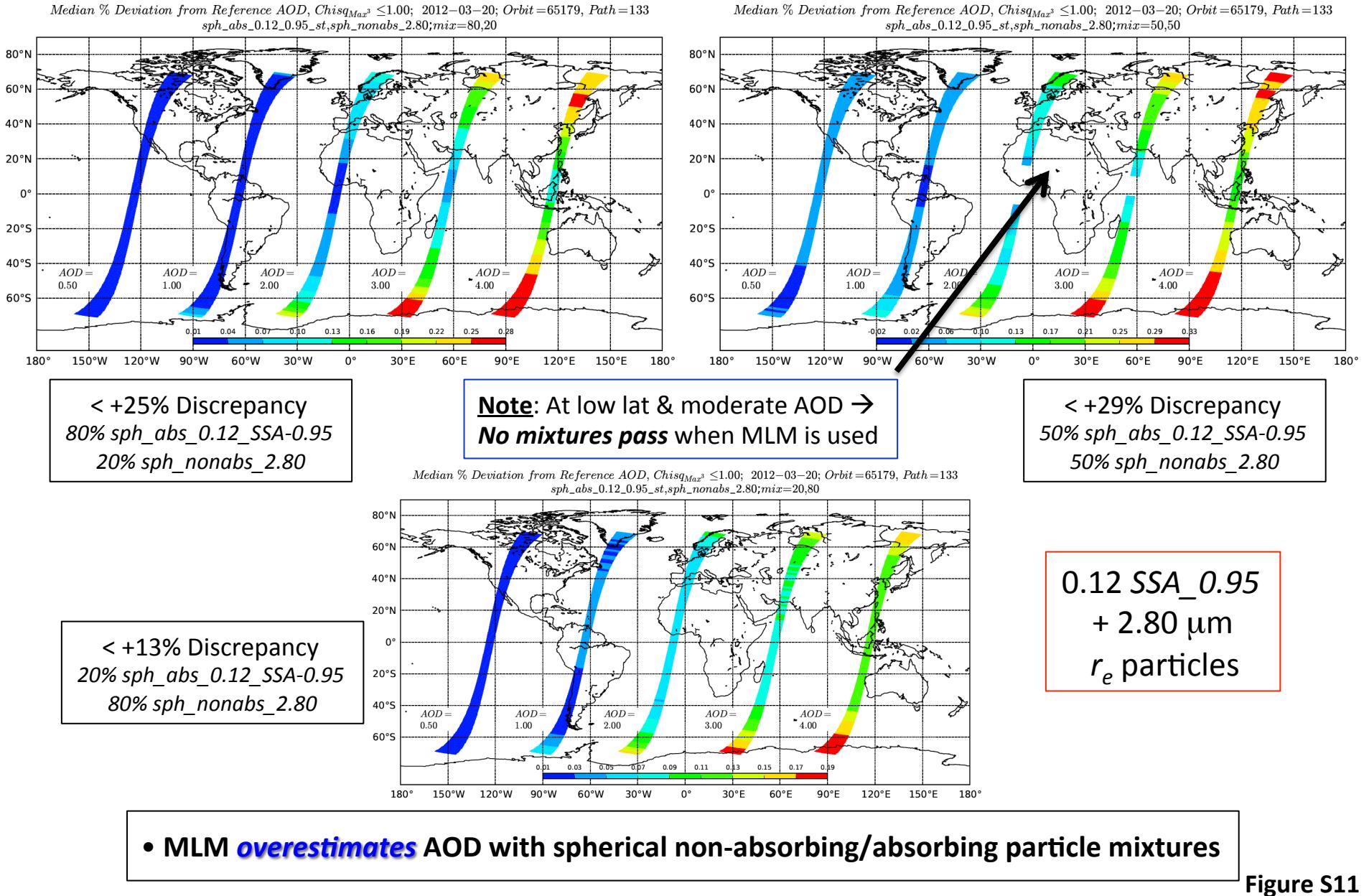
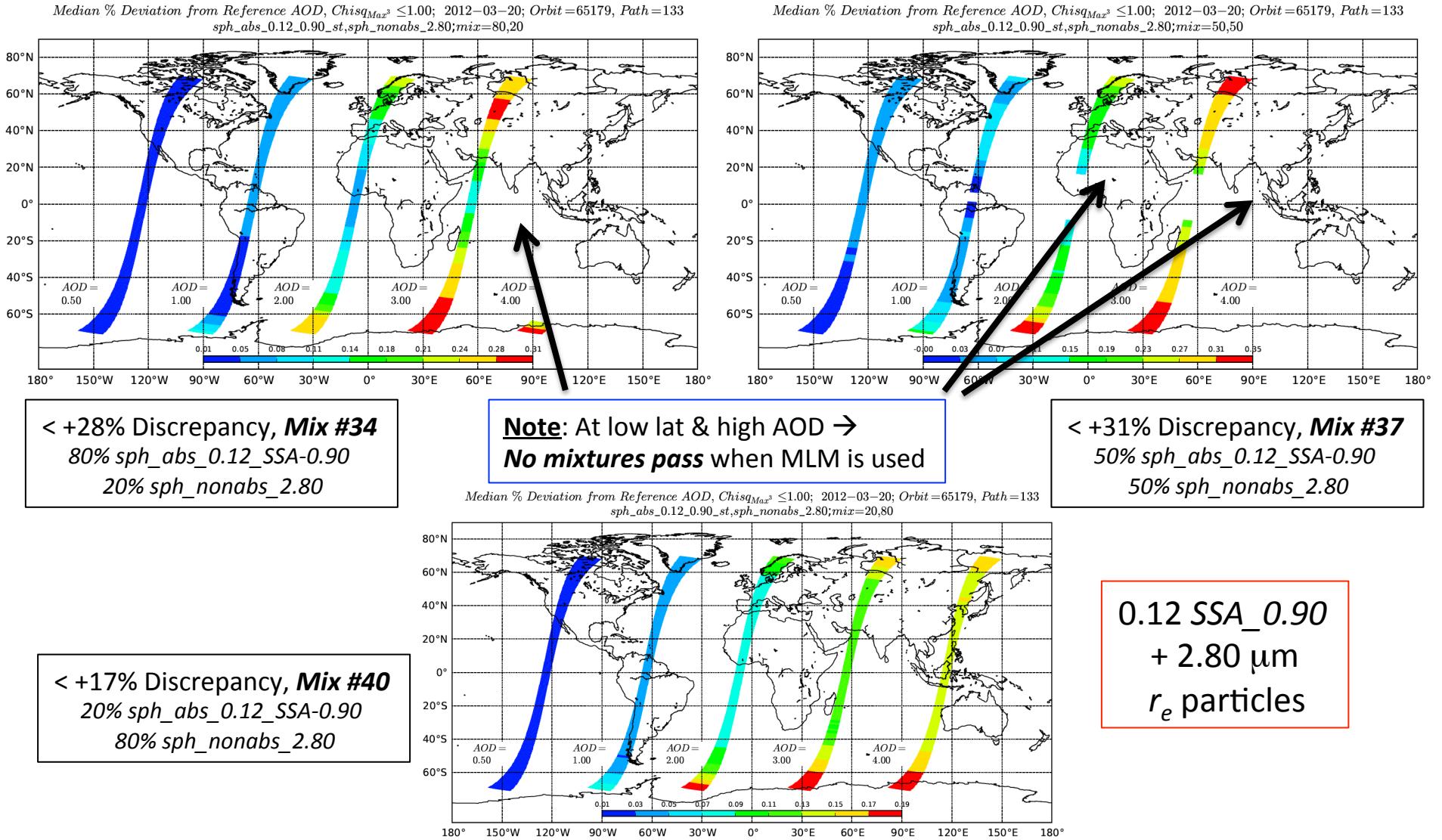


Figure S11

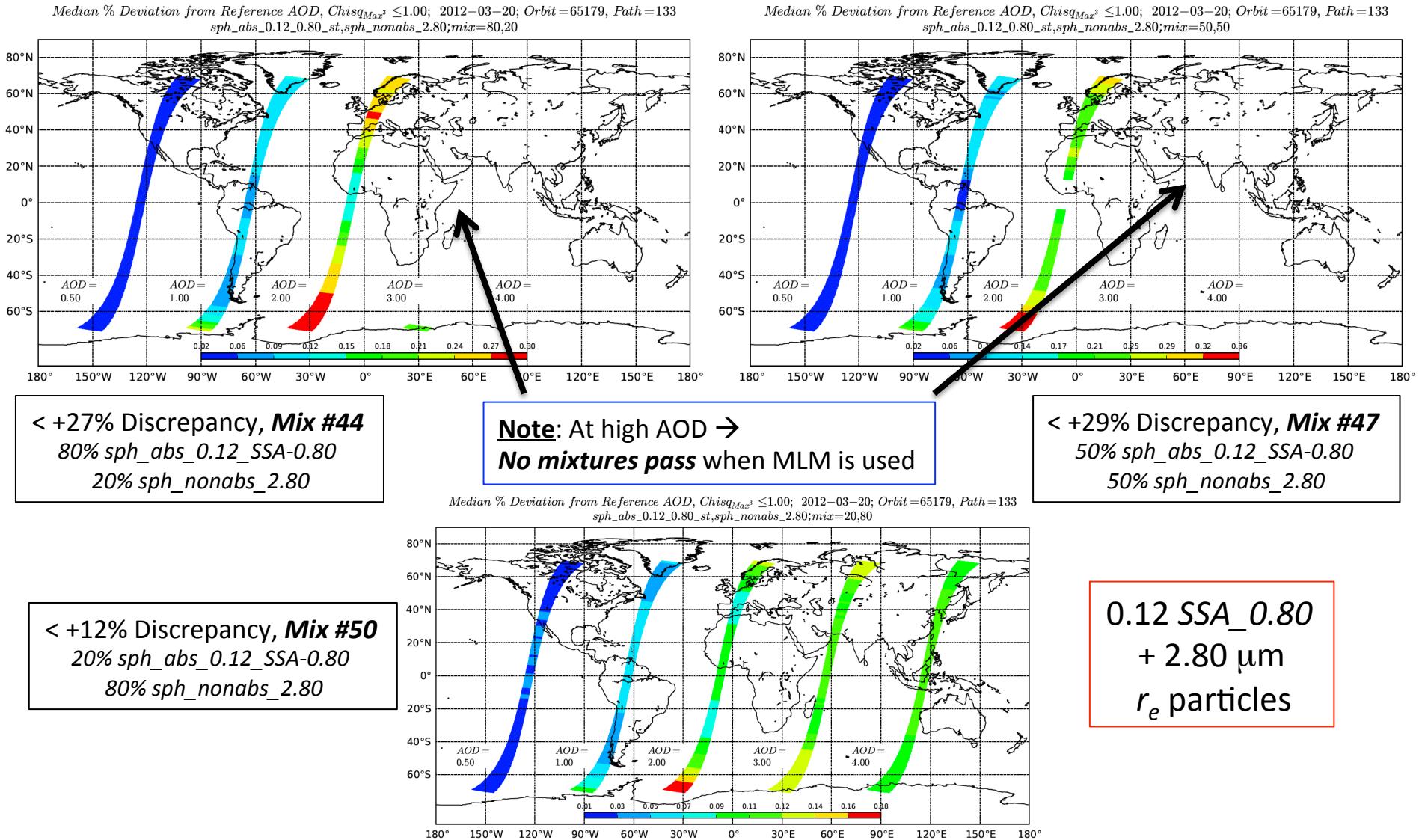
Impact of **MLM**; Globally, Absorbing Mixtures



- MLM **overestimates** AOD with spherical non-absorbing/absorbing particle mixtures

Figure S12

Impact of **MLM**; Globally, Absorbing Mixtures



- MLM **overestimates** AOD with spherical non-absorbing/absorbing particle mixtures

Figure S13

Impact of **MLM**; Globally, Absorbing Mixtures

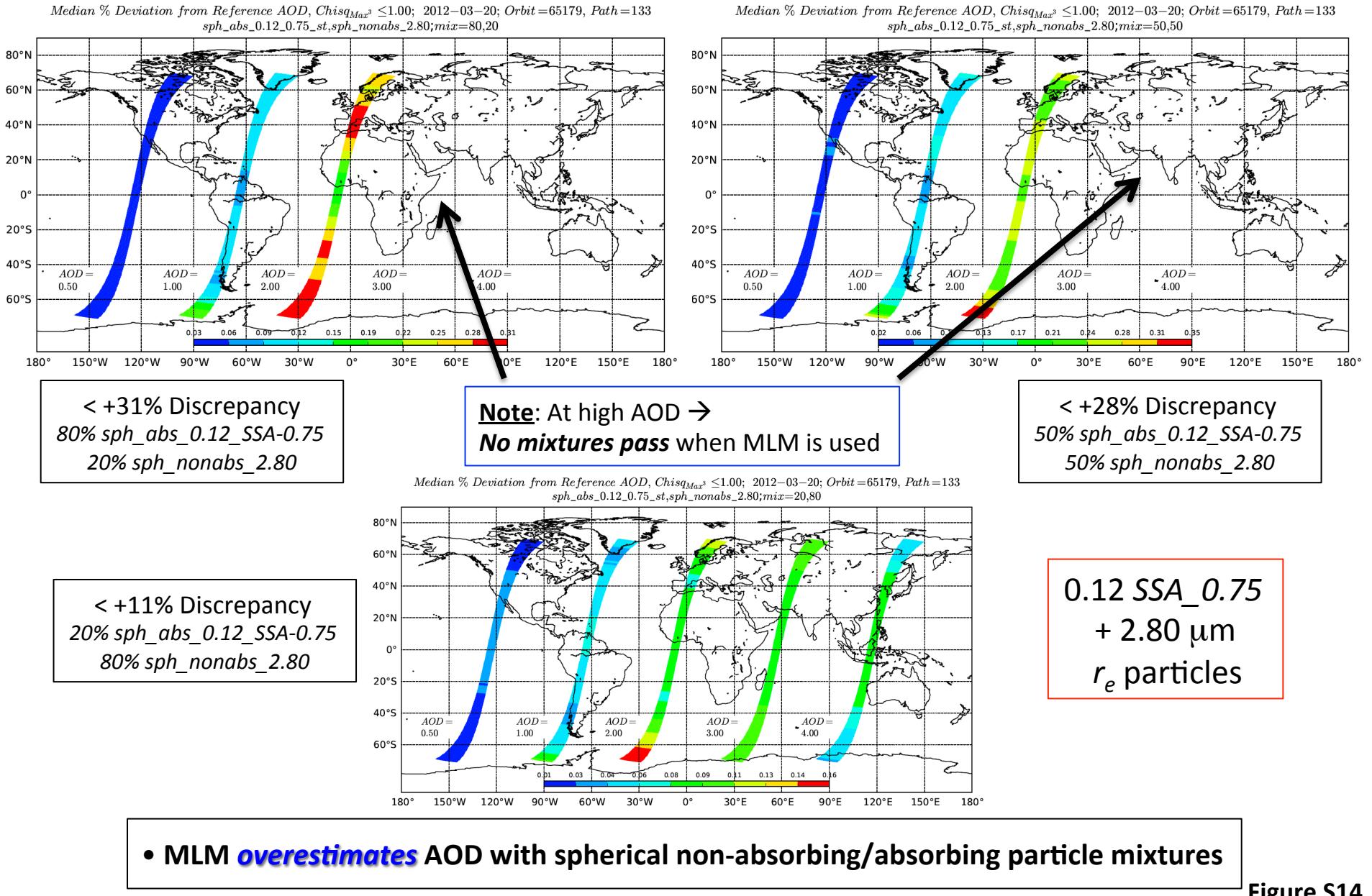
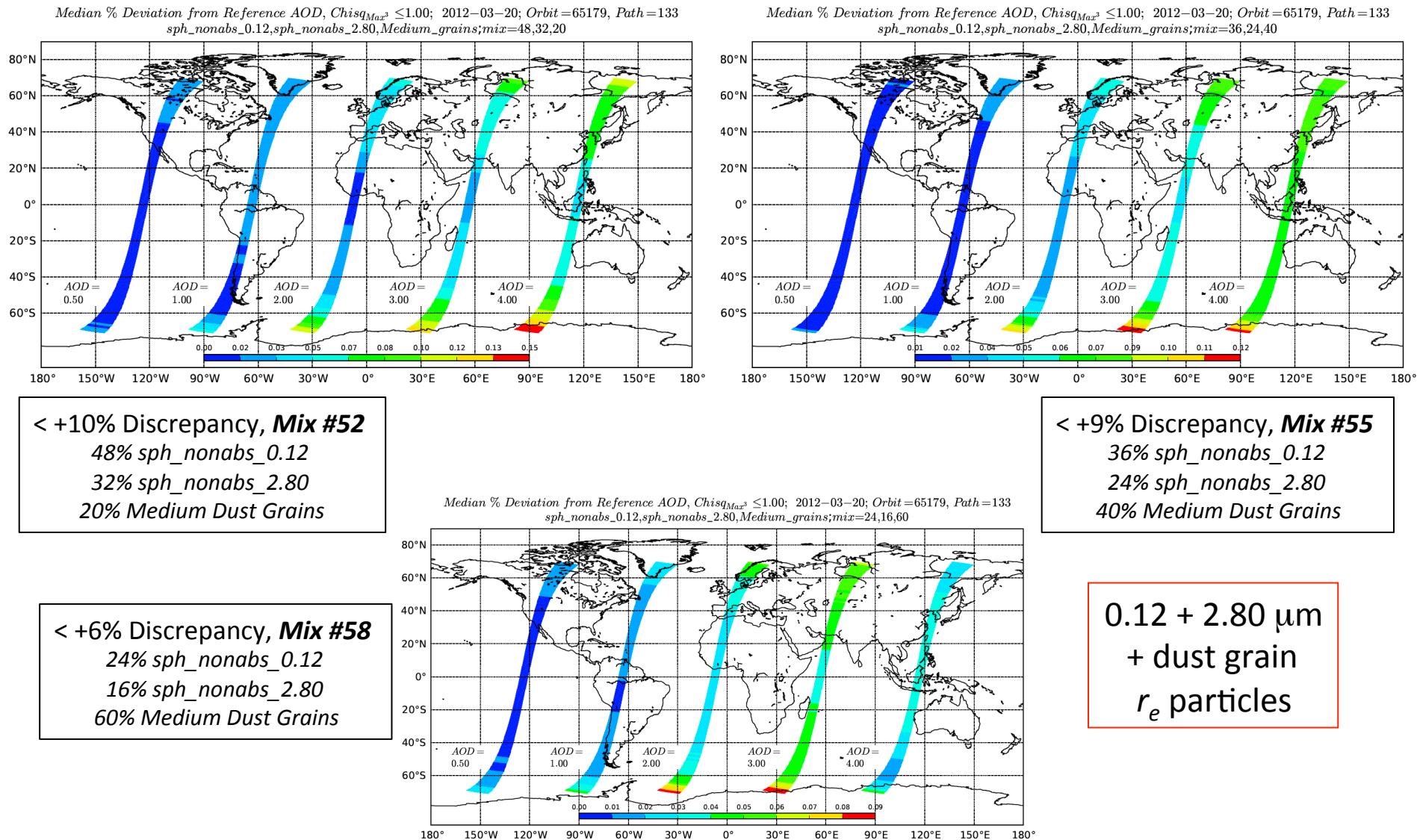


Figure S14

Impact of *MLM*; Globally, Non-Spherical Mixtures

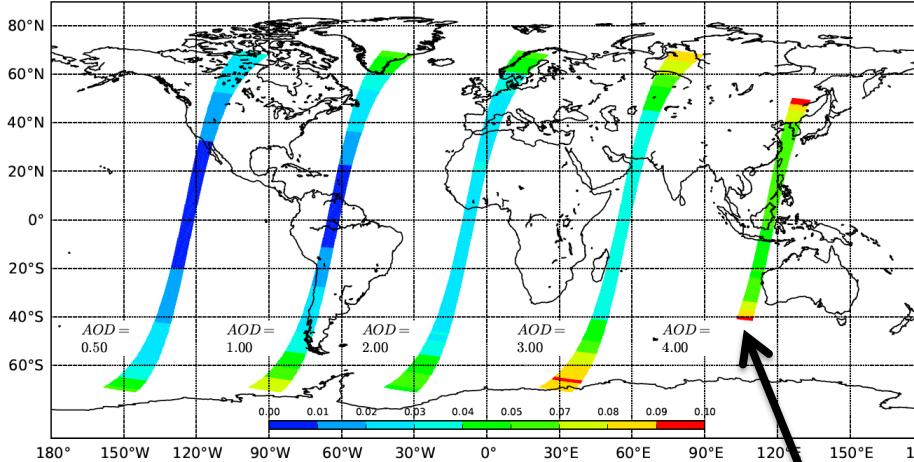


- Modified linear mixing **overestimates** AOD with non-spherical particle mixtures

Figure S15

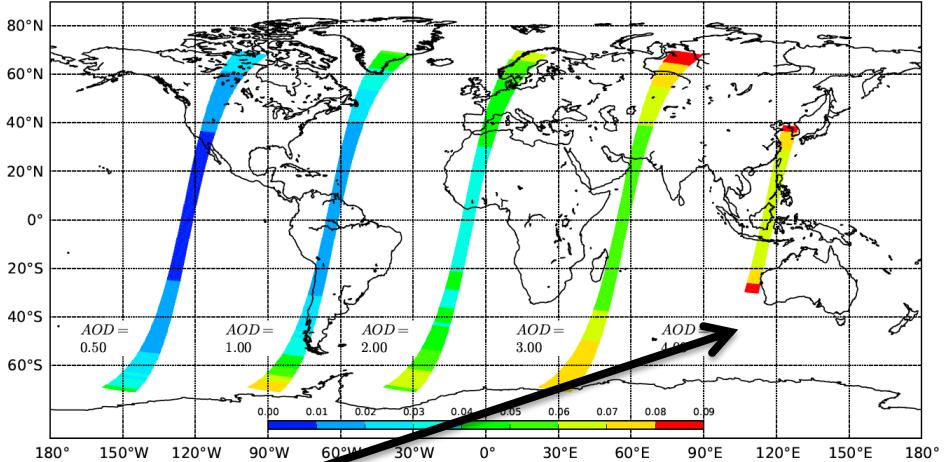
Impact of **MLM**; Globally, Non-Spherical Mixtures

Median % Deviation from Reference AOD, $\text{Chisq}_{\text{Max}}^2 \leq 1.00$; 2012–03–20; Orbit = 65179, Path = 133
 $\text{sph_nonabs_0.12, Medium_grains, Coarse_spheroids; mix=40,24,36}$



< +10% Discrepancy, **Mix #65**
 40% *sph_nonabs_0.12*
 24% Medium Dust Grains
 36% Coarse Dust Spheroids

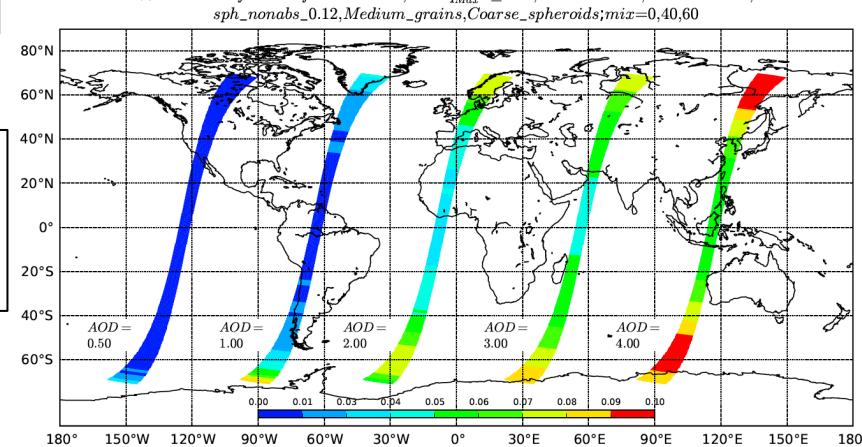
Median % Deviation from Reference AOD, $\text{Chisq}_{\text{Max}}^2 \leq 1.00$; 2012–03–20; Orbit = 65179, Path = 133
 $\text{sph_nonabs_0.12, Medium_grains, Coarse_spheroids; mix=20,32,48}$



Note: At high lat & high AOD →
 No mixtures pass when MLM is used

< +9% Discrepancy, **Mix #69**
 20% *sph_nonabs_0.12*
 32% Medium Dust Grains
 48% Coarse Dust Spheroids

< +9% Discrepancy, **Mix #73**
 0% *sph_nonabs_0.12*
 40% Medium Dust Grains
 60% Coarse Dust Spheroids



0.12 μm
 + dust grain
 + dust spheroid
 r_e particles

- Modified linear mixing **overestimates** AOD with non-spherical particle mixtures

Figure S16

Linear Mixing (LM) & Modified-Linear Mixing (MLM) Sensitivity Study **Conclusions**

- For spherical **non-absorbing** mixtures (Mixtures #1-30) [LM, Figures S6-S10]
 - Retrieved AOD values **still fall within 0.05 or 20% AOD**
 - **<5% bias** for **AOD≤1.0** in all cases
 - **Larger particle size difference** → larger AOD **overestimate**
So the **largest bias** is for **[0.06 + 2.80 μm]** mixtures
 - The effect becomes more pronounced at **high AODs** (**up to 18%** for $AOD > 2$)
- For spherical **absorbing** mixtures, AOD is also **overestimated** [MLM, Figures S11-S14]
 - The mixtures considered here (#31-50) perform reasonably well at low AODs
[sph_abs_0.12_SSA-0.80 or 90 & + 2.80 μm non-abs.]
<10% bias for **AOD≤1.0**
 - Mixtures having **larger fractions 2.80 μm non-abs. particles** (#34-40 & 44-49)
can fall outside of 0.05 or 20% AOD for $AOD \geq 2.0$ for some geometries
 - **Biases of 10-30%** for $AOD > 2.0$, **even when SSA 0.12 μm = 0.95**
- For **non-spherical** mixtures, AOD is also **overestimated** [MLM, Figures S15-S16]
 - But **<10% bias** for all non-spherical mixtures in the MISR V22 SA climatology