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Remote sensing of tropospheric turbulence using GPS radio occultation

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Abstract. Radio occultation (RO) measurements are sensitive to the small-scale irregularities in the atmosphere. In this study, we present a new technique to estimate tropospheric turbulence strength (namely, scintillation index) by analyzing RO amplitude fluctuations in impact parameter domain. GPS RO observations from the COSMIC (Constellation Observing System for Meteorology, Ionosphere, and Climate) satellites enabled us to calculate global maps of scintillation measures, revealing the seasonal, latitudinal, and longitudinal characteristics of the turbulent troposphere. Such information are both difficult and expensive to obtain especially over the oceans. To verify our approach, simulation experiments using the multiple phase screen (MPS) method were conducted. The results show that scintillation indices inferred from the MPS simulations are in good agreement with scintillation measures estimated from COSMIC observations.

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1 Introduction

Atmospheric turbulence associated with fluctuation of temperature, humidity, and water vapor are prevalent in the tropospheric region. Irregularities in the turbulence cause the index of refraction of the tropospheric medium to fluctuate. Electromagnetic signals transmitted from Global Navigation Satellite System (GNSS) satellites (for example), carrying communication and navigation information, propagate through the turbulent troposphere. The spatial changes of the index of refraction introduce irregular fluctuations in the intensity and phase of the traversing electromagnetic signals by causing scintillation (Wheelon, 2004). Signal scintillation can affect the performance of satellite communication and navigation systems such as Global Positioning System (GPS). Scintillation characteristics inferred from global GPS signal observations (employed here) are valuable resources to study atmospheric turbulence properties.

In this paper, we have employed data analysis and model simulation to investigate and quantify the effects of tropospheric turbulence on L-band signals propagating from a GPS satellite to a low-Earth orbit (LEO) satellite such as COSMIC (Constellation Observing System for Meteorology, Ionosphere, and Climate) (Anthes et al., 2008). We estimated global distribution of the turbulence strength using a scintillation parameter (scintillation index) from COSMIC radio occultation (RO) measurements. To understand and quantify the observed scintillation, we have simulated the effect of tropospheric turbulence on L-band signals propagating through multiple phase screens (MPSs). In the MPS model runs, the phase screens are assumed to be various realizations of random perturbations of index of refraction profiles through which electromagnetic waves are propagating (Knepp, 1983).

2 Global scintillation maps inferred from COSMIC RO measurements

This section presents investigation of the effect of tropospheric turbulence on L-band propagation utilizing RO observations from a GPS to a COSMIC satellites radio links. We estimated the impact of turbulence strength on L-band signals in terms of scintillation index. During the time frame relevant to this study, the COSMIC satellites provide a significant number of RO profiles (up to about 2000 profiles per day) observed by the six micro-satellites covering the entire globe. Utilizing the RO profiles, we were able to estimate the global distribution of the effect of scintillation on GPS signals. The technique provides valuable scintillation data especially over the oceans where ground-based measurements are both difficult and expensive to perform. RO data were first used to determine the intensity and location of turbulent regions (Cornman et al., 2012). Our study differs in that we aim to study the global climatology of tropospheric turbulence. In addition, we suggest that amplitude and phase in the impact parameter domain, rather than raw signal amplitude and phase, provide a more effective observable for measuring scintillation of interest.

2.1 COSMIC signal amplitude measurements

The basic observations of RO soundings on COSMIC are time series of amplitude (the 1s voltage signal-to-noise ratio) and phase of L-band signals transmitted by a GPS satellite (e.g., Hajj et al., 2002). As the radio signal propagates through the troposphere, the amplitude of the signal (raw amplitude) suffers from the effects of defocusing, multi-path propagation, and diffraction effects. Therefore, the raw amplitude fluctuation does not truly represent the effect of turbulence. To suppress amplitude fluctuations due to these effects, the canonical transform (CT) has been applied on the received complex signal to transform it from the time domain to the impact parameter domain (Gorbunov, 2002). In RO retrieval processing, the CT phase is considered the important quantity since it is used to retrieve the bending angle profile and subsequently the refractivity profile, which are the primary retrieval variables. In our study, however, the focus is on the CT amplitude. We assume that CT amplitude fluctuations are dominated by small-scale irregularities caused by turbulent processes. We note that other radio-holographic inversion methods can be used such as the full spectrum inversion (Jensen et al., 2003) and phase matching method (Jensen et al., 2004). While these methods might be easier to implement for certain orbital geometry, studies have shown that all methods yield very similar results in phase and amplitude (Gorbunov et al., 2004).

We note that CT operates under the assumption of a spherically symmetric atmosphere where each ray is uniquely identified by its impact parameter. Thus the presence of mesoscale or large-scale horizontal inhomogeneity can result in fluctuations in the CT amplitudes; however, these tend to occur at a larger spatial scales than the turbulent effects being considered so that their contribution to the scintillation estimates is expected to be small.

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2.2 Scintillation effects on COSMIC RO signals

The scintillation index σ_I can be viewed as a measure of the effect of tropospheric turbulence on L-band propagation having signal intensity *I*. σ_I can be described as a normalized standard deviation of intensity *I* fluctuation:

$$\sigma_I = \left(\frac{\langle I^2 \rangle - \langle I \rangle^2}{\langle I \rangle^2}\right)^{\frac{1}{2}},\tag{1}$$

where $\langle ... \rangle$ stands for expected value and *I* is the CT intensity, which is the square of the CT amplitude. The expected value is computed using data in 120 m intervals.

2.2.1 Scintillation index estimates

Figures 1 and 2 show global maps of σ_I estimated by applying Eq. (1) on the CT intensity computed from the COSMIC RO measurements.

In the global map of scintillation estimates presented in Fig. 1, the scintillation index is an altitudinal average of σ_I between altitudes 1 to 4 km. Figure 2 shows an average of σ_I between 4 and 8 km. In this study, we restrict our results to above 1 km due to possible data quality issues affecting the near-surface retrievals (Ao et al., 2012). The global scintillation maps presented in Figs. 1 and 2 are for the months of January, April, July, and October of the year 2008. To construct these global scintillation maps, about 60 000 RO profiles were employed. The results can be easily extended to other periods.

The scintillation maps (Figs. 1 and 2) contain a wealth of valuable information. Figures 1 and 2 show similar geographic and seasonal patterns; however, the values of σ_I are significantly higher at the lower altitudes shown in Fig. 1. This is due to the sensitivity of the radio signals to the water vapor irregularities in the lower troposphere and as a result signal scintillations are more frequently observed between the top of the boundary layer and 4 km (cf. Fig. 3 of Sokolovskiy, 2001, and Fig. 2 of Beyerle et al., 2008, for example). From the scintillation maps, the followings can be noted.

1. The effects of the tropospheric turbulence on L-band propagation have a very strong seasonal dependence. Summer hemispheres show significant turbulent activities (measured by σ_I) compared to winter hemispheres (Figs. 1a, c and 2a, c). The magnitude of the global L-band scintillation is relatively large in the summer hemisphere compared to the winter hemisphere. Increased turbulence activities due to surface heating could be a reason for higher scintillation in the summer hemisphere. This property is also consistent with the global distribution of precipitation content, which has relatively significant magnitude during summer (Adler et al., 2003; Xie and Arkin, 1997).



Figure 1. Global map of altitudinal average (1–4 km altitudes) scintillation index derived from the COSMIC RO data for January, April, July, and October 2008.

- 2. Figures 1 and 2 show that irrespective of seasons, the tropical regions are characterized by a relatively large σ_I possibly due to the concentration of significant amount of water vapor in the lower tropical troposphere.
- 3. Using σ_I as a proxy for turbulence strength, we infer that the northern hemispheric summer (July 2008, Figs. 1c and 2c) shows relatively large turbulent activities compared to the southern hemispheric summer (January 2008, Figs. 1a and 2a). During the respective summer months, the Antarctic region is characterized by less turbulence strength compared to the Arctic region. This is most pronounced in the temperate and polar regions. The effect of the Arctic sea and the high altitude of the Antarctic, make the Arctic polar region relatively warmer than the Antarctic region. The warm air in the Arctic holds more moisture than the cold air in the Antarctic. Temperature fluctuations could also cause the observed differences.
- 4. The scintillation estimates for the equinox seasons (April 2008, Figs. 1b and 2b; October 2008, Figs. 1d and 2d) are symmetrical about the equator. Scintillation estimates in the tropics are fairly symmetrical for all seasons.
- 5. The troposphere over the Sahara region is characterized by low scintillation effects on L-band propagation com-

pared to the neighboring regions to its east and west. The water vapor content is consistently low and the air is dry over the Sahara (Schrijver et al., 2009). A close comparison of the maps (Figs. 1a–d and 2a–d) shows that the strength of scintillation is relatively enhanced during July (summer) over the Sahara due to relatively hotter air.

- 6. Figures 1a–d and 2a–d clearly demonstrate an oceancontinent contrast of the scintillation estimates in the Southeast Pacific, South America, and South Atlantic regions. Over these regions, the average σ_I is low over the ocean compared to the continent. These σ_I oscillations are highly correlated with (i) the convective available potential energy (CAPE), the values of which are maximum over the continent (Riemann-Campe et al., 2009), and (ii) atmospheric relative humidity from satellite data (Du et al., 2012).
- 7. The turbulence strength difference between summer and winter seasons over the Antarctica is small compared to the turbulence strength difference between summer and winter seasons over the Arctic. Similar results based on radiosonde, satellite, and atmospheric reanalyses observation were reported (Serreze et al., 2012; Bromwich et al., 2007). Compared to other regions, the Arctic and Antarctic have the least observations available. The RO



Figure 2. Global map of altitudinal average (4–8 km altitudes) scintillation index derived from the COSMIC RO data for January, April, July, and October 2008.



Figure 3. Histogram of σ_I^2 COSMIC RO averaged over 1–8 km: (a) tropics, (b) midlatitude, and (c) high latitude.

inferred map presented in Figs. 1 and 2, therefore, helps to build and enrich the polar region database.

8. For all seasons, σ_I changes significantly with season in the Northeast Pacific compared to Southeast Pacific.

2.2.2 The index of refraction structure parameter

The index of refraction structure parameter C_n^2 is valuable for investigating propagation of electromagnetic waves in the atmosphere. Amplitude and phase of the waves propagating through the atmosphere get degraded as C_n^2 is intensified (Andreas, 1989). Unfortunately, measuring C_n^2 is expensive and difficult to perform, especially over the oceans. Due Index of refraction structure parameter C_n^2 (mean) COSMIC RO



Figure 4. The index of refraction structure parameter C_n^2 inferred from CT signal amplitude of COSMIC RO data.

to this, C_n^2 profiles are available from only a few locations over the globe (Andreas, 1989; Wheelon, 2004 and the references). RO offers the possibility of filling these gaps. Here, we present C_n^2 profiles inverted from CT amplitude scintillation incurred on COSMIC RO observations and the Rytov variance (Eq. 2).

Assuming that the wavelength of propagation is small compared to the scale of index of refraction fluctuations, σ_I can be expressed in terms of turbulence properties (C_n^2) of the medium by the Rytov variance. The Rytov variance assumes wave propagation in weak fluctuation regimes ($\sigma_I^2 <$ 1) caused by turbulence processes having characteristics of Kolmogorov spectra. Since the amplitude of fluctuations of the RO signals considered are characterized by $\sigma_I^2 <$ 1, the Rytov variance is valid for the present analysis. Note that the Rytov variance was used to describe characteristics of weak scintillation of radio and microwave propagation in the atmosphere (Clifford and Strohbehn, 1970; Woo and Ishimaru, 1973; Ishimaru, 1978; Martini et al., 2006; Blaunstein and Christodoulou, 2007). For plane waves, σ_I^2 is proportional to C_n^2 (Andrews et al., 1999):

$$\sigma_I^2 = 1.23 C_n^2 \kappa_o^{\frac{7}{6}} L^{\frac{11}{6}}, \qquad (2)$$
$$C_n^2 = 0.813 \sigma_I^2 \kappa_o^{-\frac{7}{6}} L^{-\frac{11}{6}}, \quad \kappa_o = \frac{2\pi}{\lambda}.$$

 κ_{\circ} is a wavenumber of the electromagnetic wave, λ is wavelength, and *L* is the propagation path length between a transmitter and a receiver through the turbulent medium.

The C_n^2 profile can be calculated from σ_I^2 profile for each occultation by making use of Eq. (2) with $\lambda = 0.2$ m and $\kappa_o =$

31.4 m⁻¹. Figure 3a, b, and c show the distribution of σ_r^2 averaged over 1-8 km in the tropics, midlatitude, and highlatitude troposphere, respectively. The histograms reveal that about 95 % of the σ_I^2 values are less than 1 in Fig. 3a. The distribution of σ_I^2 shows values less than 1 for more than 95 % of the cases. Since measured $\sigma_I^2 < 1$ in Figs. 1 and 2 predominantly, the application of the Rytov variance is justified for estimating C_n^2 profile. To compute C_n^2 profiles from σ_L^2 profiles, we still have to know the value of an effective signal propagation length L in the lower troposphere corresponding to RO geometry. For that purpose, L has been estimated using an MPS model simulation technique described in Sect. 3. We use the MPS model to calculate the scintillation index $\sigma_I^{2_{\text{model}}}$ by varying the value of C_n^2 (the MPS model runs use index of refraction as input derived from Kolmogorov spectra, Eqs. 3 and 4). We used the following procedures in the MPS model to estimate L. The relationship between the scintillation index $\sigma_I^{2_{\text{model}}}$ and C_n^2 is linear (Eq. 2). Using linear regression, we determine the slope in the $\sigma_I^{2\text{model}}$ and C_n^2 relationship. The propagation path length L is estimated from the slope and has an average value of L = 650 km in the lower troposphere. We recognize that L is not exactly a constant and would vary with altitudes and differ from sounding to sounding; however, we expect using a single average L to estimate C_n^2 for all occultations to be a good approximation to first order.

Figure 4 depicts representative C_n^2 profiles calculated utilizing COSMIC RO signal amplitudes received over the Central Pacific, New Mexico, Southeast Pacific, and Arctic (north of Alaska) in January and July 2008. The C_n^2 profiles



Figure 5. (a, b) Example refractivity profile employed as an input for the multi phase screen (MPS) simulation runs; (c) scintillation index σ_I^2 profiles inferred from MPS model runs; (d) σ_I^2 inferred from COSMIC RO observations (averages over Central Pacific, New Mexico, and Arctic, north of Alaska); and (e) C_n^2 derived from σ_I^2 MPS model.

are averaged over 5° latitude and 5° longitude. The C_n^2 profiles shown in Fig. 4, estimated from COSMIC RO, decrease with altitude in the lower troposphere in agreement with measured C_n^2 profiles (Andreas, 1989; Wheelon, 2004, for example). Specifically, in Fig. 4a, b, and d (Central Pacific, New Mexico, and Arctic (north of Alaska)), the C_n^2 profiles show clear seasonal behavior (summer–winter contrast). C_n^2 is larger in the July compared to January (New Mexico and Arctic (north of Alaska), Fig. 4b and d). It is larger in January compared to July (Southeast Pacific, Fig. 4c). In contrast, C_n^2 is only a little larger in July compared to January (Central Pacific, Fig. 4a). The mean C_n^2 value ($0.25 \times 10^{-14} \text{ m}^{-2/3}$), reported in (Wheelon, 2004, and the references therein), agrees with an approximate mean summer values of C_n^2 displayed in Fig. 4b and d.

3 Wave propagation simulations

3.1 MPS model

The merit of the phase screen technique to find solution of electromagnetic wave propagation through turbulent medium has been described in the literature (e.g., Knepp, 1983; Knepp and Nickisch, 2009). In the context of this paper, the MPS model is applied to simulate and quantify the effect of tropospheric turbulence (and the resulting index of refraction variations) on L-band propagation. The MPS technique employed uses the geometry of L-band propagation in a radio link from a GPS satellite (incident wave) to a LEO satellite (receiver, observation screen) (Sokolovskiy, 2001). The MPS technique involves finding the solution of the parabolic wave equation (Knepp, 1983; Knepp and Nickisch, 2009). The solution comprises application of numerical and Fourier transform techniques repeatedly for waves propagating through MPSs (Knepp, 1983; Knepp and Nickisch, 2009) idealized by parallel planes (phase changing screens). The medium of signal propagation is divided into a number of thin layers, each modeled as phase changing screens encompassed by a free space. Accordingly, we seek solution of the parabolic equation by performing successive iteration of the propagation calculations from one screen to the next and ultimately to the observation screen.

3.2 Model results and discussion

3.2.1 Index of refraction profiles: model input

The main input for the MPS model run is an index of refraction profile of the lower troposphere. The phase screens are constructed as random perturbations of an exponential background refractivity profile (first term in Eq. 3):

$$N(y) = N_{\rm o} \exp\left(-\frac{y}{H_{\rm s}}\right) + \tilde{N}(y), \qquad (3)$$

where the index of refraction profile n(y) is calculated from the refractivity profile using $N(y) = 10^6[n(y) - 1]$, $N(0) = N_\circ = 320$, and the scale height $H_s = 7$ km. The resulting background refractivity is shown in Fig. 5a. In the refractivity perturbation models ($\tilde{N}(y)$), tropospheric turbulence is taken to be nonzero only up to 8 km. $\tilde{N}(y)$ is an inverse Fourier transform of the Kolmogorov spectra (Eq. 4) modulated by

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a Gaussian random number with zero mean and standard deviation one (Knepp, 1983). In order to make the refractivity perturbations realistic, the refractivity profiles on the phase changing screens are specified by the characteristics of Kolmogorov spectra:

$$\hat{\Phi}(\kappa) = 0.033 C_n^2 \kappa^{-\frac{11}{3}}, \qquad \kappa = \frac{2\pi}{y}.$$
 (4)

Figure 5b shows example refractivity profiles calculated using Eq. (4) (an input for the MPS model runs).

3.2.2 Input parameters for MPS model runs

The input parameters for MPS model runs were as follows: the number of phase screens was equal to 4000; vertical spacing was 1 m; spacing between phase screens was 1 km; a Gaussian random number initializes each phase screen differently; on each phase screen, each altitude is initialized differently.

3.2.3 Scintillation index profiles: MPS model

The MPS model runs were performed for two cases where (a) $C_n^2 = 1.0 \times 10^{-13} \text{ m}^{-2/3}$ and (b) $C_n^2 = 5.0 \times 10^{-14} \text{ m}^{-2/3}$. For each case, 50 random realizations of the MPS runs were used to calculate CT amplitude profiles. The average CT intensity profiles (average of the 50 CT intensity profiles) were then used to calculate σ_I profiles every 50 m in the lower troposphere (shown in Fig. 5c).

For comparison and validation purposes, Fig. 5d plots σ_I profiles estimated from COSMIC RO data over Central Pacific, New Mexico, Arctic (north of Alaska), and Southeast Pacific. The MPS inferred σ_I profiles are in a reasonable agreement with the COSMIC RO inferred σ_I . Figure 5c and d show a very good agreement between the MPS model σ_I and COSMIC RO σ_I over the Central Pacific (January and July 2008) and New Mexico (July 2008). Figure 5e presents C_n^2 estimates derived from σ_I^2 profiles (MPS model, Fig. 5c). The Rytov variance has been used to invert for the C_n^2 profiles. Figure 5e reproduces the input C_n^2 values fairly well. The C_n^2 profiles shown in Fig. 5e have similarities with the C_n^2 profiles shown in Fig. 5e, the blue vertical line shows $C_n^2 = 5.0 \times 10^{-14} \text{ m}^{-2/3}$. The decrease of C_n^2 starting ~ 6 km is believed to be due to the finite vertical extent of the turbulence model in the MPS simulation.

4 Conclusions

We have used (i) radio occultation observations on board the COSMIC satellites and (ii) multiple phase screen model calculations to investigate and quantify the effect of tropospheric turbulence on L-band propagation. Instead of regular amplitude and phase data, we have used the CT amplitudes in estimating the scintillation indices from each occultation. This has the advantage of removing signal fluctuations due to atmospheric multi-path and diffraction from sharp vertical layers.

Global maps of scintillation measures across different seasons were obtained from 1 year of COSMIC RO data. The resulting global scintillation maps reveal very strong seasonal dependence, with the northern hemispheric summer exhibiting relatively large turbulent activities compared to the southern hemispheric summer. Irrespective of seasons, the tropical regions are generally characterized by a relatively large scintillation index. The maps also show clear ocean-continent contrast of the scintillation estimates in the Southeast Pacific, South America, and South Atlantic regions. The scintillation estimates appear to be positively correlated with water vapor, precipitation, and convection. We have also presented C_n^2 profiles estimated from COSMIC RO data using the Rytov variance method for weak scintillation. This represents the first ever observational estimates of global tropospheric turbulence strength. While certain simplifications have been used in this initial study, the results are encouraging, and future work can be done to refine the results and cross-validate with other observations.

We have also performed numerical simulations of radio propagation through a random phase changing screen (in which refractivity profiles were specified by the Kolmogorov spectra). Scintillation index profiles inferred from the MPS technique are in a reasonable agreement with scintillation index profiles inferred from COSMIC RO data and provide confidence to our estimates of C_n^2 profiles.

5 Data availability

The COSMIC radio occultation data used in this study were processed at the Jet Propulsion Laboratory (JPL) and are available from http://genesis.jpl.nasa.gov.

Author contributions. Esayas Shume and Chi Ao contributed to COSMIC RO data analysis, multiple phase screen simulation, and writing this paper.

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References

- Adler, R. F., Huffman, G. J., Chang, A., Ferraro, R., Xie, P.-P., Janowiak, J., Rudolf, B., Schneider, U., Curtis, S., Bolvin, D., Gruber, A., Susskind, J., Arkin, P., and Nelkin, E.: The Version-2 Global Precipitation Climatology Project (GPCP) Monthly Precipitation Analysis (1979–Present), J. Hydrometeor, 4, 1147– 1167, 2003.
- Andreas, E. L.: The refractive index structure parameter, C_n^2 , for a year over the frozen Beaufort Sea, Radio Sci., 24, 667–679, doi:10.1029/RS024i005p00667, 1989.
- Andrews, L. C., Phillips, R. L., Hopen, C. Y., and Al-Hahash, M. A.: Theory of optical scintillation, J. Opt. Soc. Am. A, 16, 1417– 1429, 1999.
- Anthes, R. A., Ector, D., Hunt, D. C., Kuo, Y.-H., Rocken, C., Schreiner, W. S., Sokolovskiy, S. V., Syndergaard, S., Wee, T.-K., Zeng, Z., Bernhardt, P. A., Dymond, K. F., Chen, Y., Liu, H., Manning, K., Randel, W. J., Trenberth, K. E., Cucurull, L., Healy, S. B., Ho, S.-P., McCormick, C., Meehan, T. K., Thompson, D. C., and Yen, N. L.: The COSMIC/FORMOSAT-3 Mission: Early Results, B. Am. Meteor. Soc., 89, 313–333, doi:10.1175/BAMS-89-3-313, 2008.
- Ao, C. O., Waliser, D. E., Chan, S. K., Li, J.-L., Tian, B., Xie, F., and Mannucci, A. J.: Planetary boundary layer heights from GPS radio occultation refractivity and humidity profiles, J. Geophys. Res., 117, D16117, doi:10.1029/2012JD017598, 2012.
- Beyerle, G., Gorbunov, M. E., and Ao, C. O.: Simulation studies of GPS radio occultation measurements, Radio Sci., 38, 1084, doi:10.1029/2002RS002800, 2003.
- Blaunstein, N. and Christodoulou C.: Radio Propagation and Adaptive Antennas for Wireless Communication Links Terrestrial, Atmospheric and Ionospheric Wiley Interscience, John Wiley And Sons, Inc., 2007.
- Bromwich, D. H., Fogt, R. L., Hodges, K. I., and Walsh J. E.: A tropospheric assessment of the ERA-40, NCEP, and JRA-25 global reanalyses in the polar regions, J. Geophys. Res., 112, D10111, doi:10.1029/2006JD007859, 2007.
- Clifford, S. F. and Strohbehn, J. W.: The theory of microwave line-of-sight propagation through a turbulent atmosphere, IEEE Trans. Antenn. Prop., AP-18, 264–274, 1970.
- Cornman, L. B., Goodrich, R. K., Axelrad, P., and Barlow, E.: Progress in turbulence detection via GNSS occultation data, Atmos. Meas. Tech., 5, 789–808, doi:10.5194/amt-5-789-2012, 2012.
- Du, J., Cooper, F., and Fueglistaler, S.: Statistical analysis of global variations of atmospheric relative humidity as observed by AIRS, J. Geophys. Res.-Atmos., 117, D12315, doi:10.1029/2012JD017550, 2012.
- Gifford, F. A.: A Similarity Theory of the Tropospheric Turbulence Energy Spectrum, J. Atmos. Sci., 45, 1370–1379. doi:10.1175/1520-0469(1988)045<1370:ASTOTT>2.0.CO;2, 1988.
- Gorbunov, M. E.: Canonical transform method for processing radio occultation data in the lower troposphere, Radio Sci., 37, 1076, doi:10.1029/2000RS002592, 2002.
- Gorbunov, M. E., Benzon, H.-H., Jensen, A. S., Lohmann, M. S., and Nielsen, A. S.: Comparative analysis of radio occultation processing approaches based on Fourier integral operators, Radio Sci., 39, RS6004, doi:10.1029/2003RS002916, 2004.

- Hajj, G. A., Kursinski, E. R., Romans, L. J., Bertiger, W. I., and Leroy S. S.: A technical description of atmospheric sounding by GPS occultation, J. Atmos. Sol.-Terr. Phy., 64, 451–469, doi:10.1016/S1364-6826(01)00114-6, 2002.
- Ishimaru, A.: Wave Propagation and Scattering in Random Media, Multiple Scattering, Turbulence, Rough Surfaces, and Remote Sensing, Academic Press, New York San Francisco London, Vol. 2, 1978.
- Jensen, A. S., Lohmann, M. S., Benzon, H., and Nielsen, A. S.: Full spectrum inversion of radio occultation signals, Radio Sci., 38, 1040, doi:10.1029/2002RS002763, 2003.
- Jensen, A. S., Lohmann, M. S., Nielsen, A. S., and Benzon, H.: Geometric optics phase matching of radio occultation signals, Radio Sci., 39, RS3009, doi:10.1029/2003RS002899, 2004.
- Knepp, D. L.: Multiple phase-screen calculation of the temporal behavior of stochastic waves, P. IEEE, 71, 722–737, doi:10.1109/PROC.1983.12660, 1983.
- Knepp, D. L. and Nickisch L. J.: Multiple phase screen calculation of wide bandwidth propagation, Radio Sci., 44, RS0A09, doi:10.1029/2008RS004054, 2009.
- Martini, E., Freni, A., and Cuccoli, F.: Impact of Tropospheric Scintillation in the Ku/K Bands on the Communications Between Two LEO Satellites in a Radio Occultation Geometry, IEEE T. Geosci. Remote, 44, 2062–2071, 2006.
- Riemann-Campe, K., Fraedrich, K., and Lunkeit, F.: Global climatology of convective available potential energy (CAPE) and convective inhibition (CIN) in ERA-40 reanalysis, Atmos. Res., 93, 534–545, doi:10.1016/j.atmosres.2008.09.037, 2009.
- Schrijver, H., Gloudemans, A. M. S., Frankenberg, C., and Aben, I.: Water vapour total columns from SCIAMACHY spectra in the 2.36 μm window, Atmos. Meas. Tech., 2, 561–571, doi:10.5194/amt-2-561-2009, 2009.
- Serreze, M. C., Barrett, A. P., and Stroeve, J.:, Recent changes in tropospheric water vapor over the Arctic as assessed from radiosondes and atmospheric reanalyses, J. Geophys. Res., 117, D10104, doi:10.1029/2011JD017421, 2012.
- Sokolovskiy, S. V.: Modeling and inverting radio occultation signals in the moist troposphere, Radio Sci., 36, 441–458, doi:10.1029/1999RS002273, 2001.
- Sokolovskiy, S. V., Rocken, C., Lenschow, D. H., Kuo, Y.-H., Anthes, R. A., Schreiner, W. S., and Hunt, D. C.: Observing the moist troposphere with radio occultation signals from COSMIC, Geophys. Res. Lett., 34, L18802, doi:10.1029/2007GL030458, 2007.
- Wheelon, A.: Electromagnetic Scintillation I. Geometric Optics, Cambridge University Press, Cambridge, UK, 2004.
- Woo, R. and Ishimaru, A.: Remote sensing of the turbulence characteristics of a planetary atmosphere by radio occultation of a space probe, Radio Sci., 8, 103–108, doi:10.1029/RS008i002p00103, 1973.
- Xie, P. and Arkin, P. A.: Global Precipitation: A 17-Year Monthly Analysis Based on Gauge Observations, Satellite Estimates, and Numerical Model Outputs, B. Am. Meteor. Soc., 78, 2539–2558, 1997.