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# **Retrieval of Macrophysical Cloud Parameters from MIPAS: Algorithm Description and Preliminary Validation**

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## Abstract

abstr The Michelson Interferometer for Passive Atmospheric Sounding (MIPAS) onboard EN-  
VISAT has the potential to be particularly useful for studying high, thin clouds, which have been  
difficult to observe in the past. This paper details the development, implementation and test-  
5 ing of an optimal-estimation-type retrieval for three macrophysical cloud parameters (cloud top  
height, cloud top temperature and cloud extinction coefficient) from infrared spectra measured  
by MIPAS, employing additional information derived to improve the choice of a priori. The  
retrieval is applied and initially validated on MIPAS data. From application to MIPAS data, the  
retrieved cloud top heights are assessed to be accurate to within 50 m, the cloud top temperatures  
10 to within 0.5 K and extinction coefficients (along the limb path attributable (mostly) to clouds)  
to within a factor of 15%, for clouds having extinction between  $10^{-4} \text{ km}^{-1}$  and  $10^{-1} \text{ km}^{-1}$ .  
This algorithm has been adopted by the European Space Agency's 'MIPclouds' project, which  
itself recognises the potential of MIPAS beyond monitoring atmospheric chemistry and seeks  
to study clouds themselves rigorously using MIPAS.

## 1 Introduction

intro

Although much of atmospheric infrared remote sensing is based upon analysis of data to es-  
timate constituent concentrations — where the presence of cloud particles in the measurements  
is treated as a source of error — it is possible to isolate measurements of cloud in order to  
20 determine the properties of clouds themselves. Clouds (especially high cloud such as cirrus)  
represent one of the largest uncertainties in climate studies (Intergovernmental Panel on Cli-  
mate Change, 2008) — and in order to have reliable estimates of radiative forcing and climatic  
impact, accurate distributions of cloud frequencies and properties must be available. Satellite  
instruments provide an opportunity to study the properties of clouds on a global scale.

## 1.1 Overview of MIPAS-ENVISAT

The Michelson Interferometer for Passive Atmospheric Sounding (MIPAS) is an infrared limb-viewing instrument and was launched in March 2002 on the European Space Agency's Environmental Satellite (ENVISAT) which, with large inclination on a polar orbit, enables global coverage pole-to-pole over a period of days, with an orbital repeat period of 35 days. (European Space Agency, 2005)

MIPAS was designed to measure limb-emission spectra (primarily for trace gases such as CO<sub>2</sub> (used to retrieve pressure and temperature), O<sub>3</sub>, H<sub>2</sub>O, HNO<sub>3</sub>, CH<sub>4</sub>, N<sub>2</sub>O and NO<sub>2</sub>) at a high spectral resolution in the near- to mid-infrared from 685 cm<sup>-1</sup> to 2410 cm<sup>-1</sup>. In its initial phase, MIPAS operated at a spectral sampling of 0.025 cm<sup>-1</sup>, measuring spectra nominally every 3 km vertically in the troposphere down to approximately 6 km — however, following persistent malfunctions in the smooth and consistent operation of the interferometer slide mechanism in early 2004, the sampling was decreased to 0.0625 cm<sup>-1</sup> but the measurement frequency increased to nominally every 1.5 km upward from approximately 4.5 km in the troposphere through the lower stratosphere (Mantovani, 2005). The MIPAS field-of-view is trapezoidal in the vertical, with a vertical extent varying between 3 – 4 km, depending upon definition. It has a characteristically wide horizontal field-of-view, extending approximately 200 km.

## 1.2 Overview of Clouds from Satellites

Cloud properties fall loosely into two categories: macrophysical and microphysical. Macrophysical properties are the large-scale properties (ie. bulk or extent), such as the altitude of a cloud, the physical depth and extent of a cloud, or are basic thermodynamic quantities, such as the temperature at the cloud top or the temperature structure within the cloud body. Microphysical parameters are, by opposition, those which relate to the small-scale (ie. constituent particle) of the cloud — such as the size and shape of cloud particles, and their distribution (which is often described in terms of water content), thus including properties such as number density, and influencing cloud optical depth, albedo, emissivity and transmissivity. Cloud extinction is

strictly a combination of macrophysical and microphysical parameters as it is derived from both the physical extent of the cloud, as well as its absorption and scattering characteristics. However, from the perspective of an assumed model whereby there is no scattering, and a single homogeneous extinction characterising the bulk of the cloud mass, in this study is designated as a macrophysical parameter.

Whilst most of our knowledge of the microphysical properties of clouds come from in-situ measurements, predominantly by aircraft-mounted instruments (campaigns include Weickmann (1947) over Germany, FIRE I and II over Wisconsin and Kansas (1992), SUCCESS over Oklahoma and Kansas (1996), CEPEX (1997), EUCREX over the Atlantic Ocean and mid-latitudes in Europe (2000), and CRYSTAL-FACE over Florida (2002)), satellite instruments are particularly well-suited to observing bulk cloud properties such as average cloud top height and temperature, not least because of the large-scale geographical regions they survey. As a general rule, limb-viewing instruments are competent at retrieving vertically-dependent parameters (such as cloud top height/pressure or cloud depth/extent) with great accuracy, although have poorer horizontal-resolving potential — but are able to detect even clouds having thin opacities of less than 0.01 due to the inherently long limb pathlength. On the contrary, nadir-viewing instruments suffer from poor vertical resolution when retrieving atmospheric temperature and composition from which cloud top temperatures (and hence cloud top heights/pressures) are derived, are limited to thicker clouds, but have very good horizontal resolution. Different spectral ranges are sensitive to different cloud properties: for instance, microwave instruments often are not sensitive to small ice cloud particles found in thin cirrus (since such short wavelengths do not cause much scattering from typical ice particles, and are high-energy enough to pass through optically thin ice clouds unobstructed), whereas visible and infrared instruments are often limited to the first layer of cloud encountered and unable to measure below (as typical clouds will be opaque to radiation at these wavelengths) (e.g. ESA's Living Planet website, 2010). As different instruments are sensitive to only certain cloud properties, due to inherent differences in sensitivities in spectral ranges, viewing geometries and so forth, it is thus important to choose to retrieve cloud properties appropriate to the satellite instrument's capabilities.

There have been many studies on clouds over the years producing climatologies: by Barton

(1983), Warren et al. (1985), Woodbury and McCormick (1983), Prabhakara et al. (1988), Wylie and Menzel (1989), Wylie et al. (1994), and King et al, 2010 — but these were all limited by a lack of global coverage. Currently, the Stratospheric Aerosol and Gas Experiment (SAGE) (e.g. SAGE-III-ATBD-Team, 2002), CloudSat (e.g., Stephens et al., 2002), the ODIN-submillimetre radiometer (SMR; e.g., Murtagh et al., 2002), the High Resolution Infrared Radiation Sounder (HIRS) instrument (e.g. Wylie et al., 2005), the Microwave Limb Sounder (MLS) (e.g., Wu et al., 2008), the International Satellite Cloud Climatology Project (ISCCP) (e.g. ISCCP, 2008), Polarization and Anisotropy of Reflectances for Atmospheric Sciences coupled with Observations from a Lidar (PARASOL; e.g., Fougnie et al., 2007), Cloud-Aerosol Lidar and Infrared Pathfinder Satellite Observations (CALIPSO) (e.g., Winker et al., 2009), the GRAPE project (e.g., Thomas et al., 2010), and the GEWEX project (e.g., Stubenrauch et al, 2009) are actively compiling cloud climatologies. However, past and current cloud detection algorithms often miss much thin cloud in satellite measurements — and hence conventional cloud climatologies and inventories are in no way complete with respect to high thin cloud such as cirrus (Wylie et al., 2005). In fact, limb-viewing has not been widely used for cloud measurements (although the new generation of instruments now are beginning to include cloud as a product on limb-viewing platforms) since such instruments tend to target atmospheric composition for which cloud detection is the only requirement, and limb-viewing cloud campaigns tend to be experimental rather than operational, hence yielding only short-time-series over a limited geographical region. Given that MIPAS should be quite sensitive to high, thin cloud if an appropriate detection method is employed, it is a natural candidate to contribute climatological information about these clouds.

Retrieval of cloud parameters from instruments such as MIPAS, although highly instrument-specific, are often dependent upon cloud-detection algorithms as estimators of cloud location (cloud top height/pressure/depth), and as selectors of data upon which retrieval schemes are run (although sometimes retrieval algorithms operationally process all data without filtering or detecting, even though retrievals are computationally expensive, and cloud detection methods provide a useful sub-filtering for efficient processing). Generally, cloud detection methods for limb-viewing and solar occultation IR instruments (such as MIPAS) are based upon a

– *threshold on:*

1. radiance (such as the Cryogenic Limb Array Etalon Spectrometer CLAES experiment (CLAES, 2007) and High Resolution Dynamics Limb Sounder HIRDLS (Lambert et al., 1999)),
2. transmission (Atmospheric Trace Molecule Spectroscopy ATMOS experiment (Kahn et al., 2002)),
3. extinction (Improved Stratospheric and Mesospheric Sounder ISAMS (Global Change Master Directory, 2007), the Halogen Occultation Experiment HALOE (Hervig and Deshler, 2002), and the Atmospheric Chemistry Experiment ACE (Bernath, 2002)), or
4. volume mixing ratio (the Limb Infrared Monitor of the Stratosphere LIMS (NASA, 2007)),

which exploit the fact that clouds introduce increased radiance and extinction, but decreased transmission and a decrease in certain specific constituent volume mixing ratios, such as ozone (e.g. NASA, 2007);

- *discontinuity in:* vertical gradients of extinction (the HALOE, or of trace gas concentrations such as ozone (the LIMS), which are introduced by large gradients at the cloud top; and
- *contrast in spectral structure:* the Cryogenic Infrared Spectrometers and Telescopes for the Atmosphere CRISTA (Spang et al., 2004) or MIPAS (operational method as in Spang et al. (2004), and alternate method presented in Hurley et al. (2009)), which rely upon spectral differences introduced by cloud as opposed to those present in cloud-free spectra.

The act of detection yields cursory information on cloud frequency of occurrence and a preliminary measure of cloud top height. In terms of other retrieved cloud parameters, it should be noted that of the instruments discussed ACE, ATMOS, CLAES, HALOE, HIRDLS, and ISAMS operationally retrieve(d) extinction.

### 1.3 Cloud Information from MIPAS

There have been several attempts to retrieve cloud parameters from MIPAS spectra, including

- *The Monte Carlo Cloud Scattering Forward Model (McCloudsFM)*: a multi-scattering model developed by Ewen (2005) to accurately model IR limb emission measurements of cirrus clouds, parameterised by effective radius, number density, cloud top height and cloud depth; however, the computational time associated with the retrieval was prohibitively large, and could not be justified given assumptions made in scattering properties and a priori biases.
- *Cloud Top Heights from Cloud Detection Method*: the Earth Observation Science Group at the University of Leicester produces near-real-time cloud top heights from MIPAS spectra from May 2008 onwards (Moore, 2008). The cloud top heights are retrieved using the operational cloud detection method called the Colour Index (CI) Method (Spang, 2004) such that the amount of cloud occurring in a given FOV is roughly anti-correlated with the value of CI. Leicester simply reports the tangent altitude at which cloud is first encountered in the MIPAS scan pattern as the cloud top height.
- *The Karlsruhe Optimised and Precise Radiative transfer Algorithm (KOPRA)*: provides accurate simulations of single-scattering clouds in a horizontally symmetric atmosphere, specific to MIPAS. KOPRA has been used to simulate different cloud types, such as cirrus, liquid water clouds, and various types of PSCs — and thus can be used to retrieve the modelled microphysical properties (IMK, 2008) given appropriate a priori atmospheric information.

To this end a more comprehensive and operational cloud parameter retrieval algorithm specific to MIPAS has been developed — and has been adopted as the macrophysical cloud parameter retrieval of the ‘MIPclouds’ project (e.g. Spang et al., 2008). In this work, a non-scattering forward model of the radiation emitted by a cloud in the MIPAS FOV is described, in terms of three macrophysical parameters: cloud top height, top temperature and extinction coefficient corresponding to the limb path, which is dominated by the extinction of the cloud itself.

The inverse problem is addressed using an adaptation of standard retrieval theory: a sequential retrieval in which the first guess and a priori are chosen using an estimate of cloud amount.

## 2 Algorithm Description

The retrieval of macrophysical parameters from a set of MIPAS spectra constituting a single limb-scan is a three-stage process applied independently in different spectral intervals ('microwindows'). These stages are:

1. Isolating the continuum radiance from each spectrum;
2. Retrieving the Cloud Effective Fraction to locate the spectrum containing the cloud-top; and
3. Retrieving the macrophysical parameters from this and vertically adjacent spectra within the limb scan pattern.

The results from each microwindow are combined to produce a best estimate of the parameters, and an associated error covariance.

### 2.1 Microwindows

Microwindows (MWs) are small subsets of the MIPAS spectrum of a few wavenumbers in width. A set of ten MWs have been selected from the MIPAS spectral range — and span the spectral region of 930–960  $\text{cm}^{-1}$  (Table 1) using a modification of the MIPAS MW selection algorithm (Dudhia et al., 2002) optimised for a joint retrieval of continuum and temperature, whereby the MWs are ranked in order of decreasing Shannon information content for clouds.

Fig. 1 shows the positions of these microwindows relative to molecular emission features. Note that each microwindow contains  $\text{CO}_2$  lines (for the temperature retrieval, discussed further in Sec. 2.3) whilst avoiding significant contributions from more variable gases such as  $\text{H}_2\text{O}$ .



**Table 1.** Microwindows for cloud macrophysical parameter retrievals from MIPAS spectra, ordered in terms of priority of selection. Note that the boundaries are multiples of  $0.125 \text{ cm}^{-1}$  so are consistent with both the ‘full-resolution’ ( $0.025 \text{ cm}^{-1}$  grid) and ‘optimised-resolution’ ( $0.0625 \text{ cm}^{-1}$  grid) spectra. table

<i>MW#</i>	<i>Wavenumber Range [<math>\text{cm}^{-1}</math>]</i>
1	937.625 – 940.625
2	941.125 – 944.125
3	944.500 – 947.500
4	955.750 – 958.750
5	948.625 – 951.125
6	936.000 – 937.625
7	934.500 – 935.875
8	953.500 – 955.000
9	951.875 – 953.250
10	958.750 – 960.875

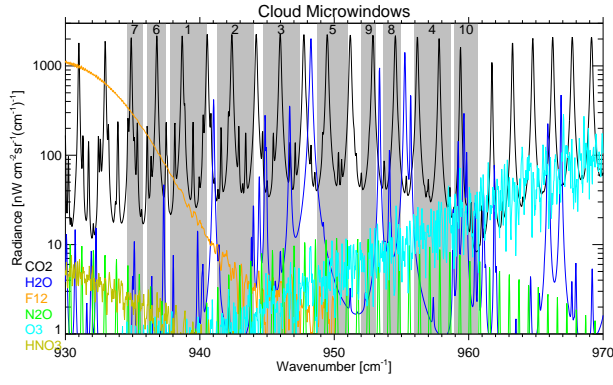
## 2.2 Continuum Radiance

Using pre-computed molecular transmittance spectra for each MW,  $\tau_\nu$ , for each tangent height altitude (based on climatological concentrations, and calculated using the radiative transfer model, the Reference Forward Model (RFM) (Dudhia, 2005)) it is possible to identify  $n_{MW}$  spectral points where molecular contributions are expected to be negligible (e.g. where  $\tau_\nu > 0.95$ ). It should be noted that at these wavenumbers molecular scattering is also negligible.

The continuum radiance,  $R$ , and associated error  $\sigma$ , can then be established by a simple mean and standard error for each radiance spectrum measured at each tangent height in a MIPAS scan pattern below about 25 km, such that

$$R = \frac{1}{n_{MW}} \sum_i L(\nu_i, z_t) \quad (1)$$

where  $L(\nu_i, z_t)$  is the measured radiance at the  $i$ th masked wavenumber  $\nu_i$  (in the particular



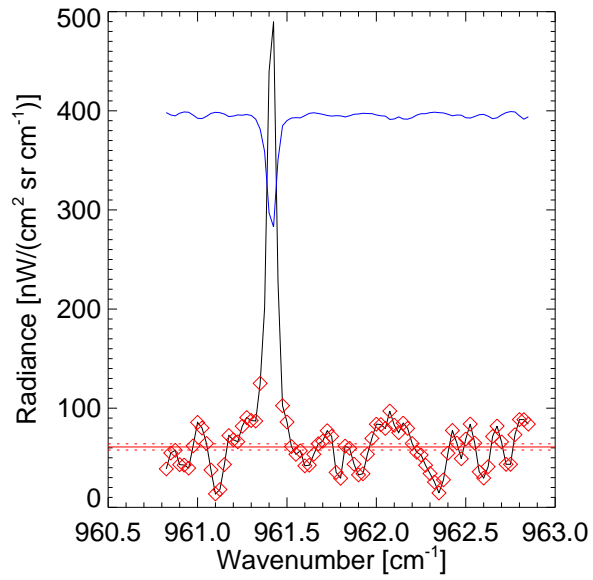
**Fig. 1.** Modelled full-resolution MIPAS spectrum for a tangent height of 9 km separated by constituent major emitters, in the spectral region of selected MWs listed in Table 1— with MW spectral regions shaded.

figure

MW) and tangent height  $z_t$ , and

$$\sigma = \frac{1}{n_{MW}} \sqrt{\sum_i (L(\nu_i, z_t) - R)^2} \quad (2)$$

using standard deviation  $D$  such that the standard error is defined as  $D/\sqrt{(n-1)}$ , where  $n_{MW}$  is the number of points averaged. By assigning an error value based on the actual  $D$  rather than the instrument noise, some allowance is made for any residual molecular contributions. Fig. 2 illustrates the continuum radiance calculation process.



**Fig. 2.** Illustration of the continuum radiance, showing the RFM-simulated MIPAS radiance at 18 km (black), the corresponding transmittance spectrum (blue, multiplied by a factor of 400 for visibility), the spectral points utilised to calculate the continuum radiance (red diamonds) along with the calculated continuum radiance (red solid line) for the spectral window considered, with the estimated uncertainty (red dashed lines).

### 2.3 Cloud Effective Fraction

The next step is to identify the spectrum containing the cloud-top. One approach could be to use a simple threshold value on the continuum radiance, but since the continuum radiance is

a strong function of atmospheric temperature **and atmospheric water vapour content** as well as cloudiness, finding a suitable threshold value is difficult. The standard MIPAS Cloud Index (CI) method (Spang et al., 2004) attempts to overcome this temperature dependence by taking the ratio of radiance in two spectral regions ( $792 - 796 \text{ cm}^{-1}$  and  $832 - 834 \text{ cm}^{-1}$ ) which react differently to cloud presence. The physical basis of the CI method is that as the field-of-view (FOV) reaches the limit of being geometrically-fully-filled with opaque cloud, the  $\text{CI} \rightarrow 1$  (as the cloud continuum radiance overwhelms the gaseous contribution to the spectral signature) whereas in the cloud-free limit, CI is large. Here, instead, it is preferable to have a scheme dependent upon the continuum radiance within each MW independently, as well as one having a more physical basis **(since it parametrises the physical (geometrical and optical) fraction of the FOV filled with cloud)**. This is done via retrieval of a ‘Cloud Effective Fraction’ (CEF) — a parameter first introduced by Hurley et al. (2009).

The CEF is defined as the fraction of the FOV covered by an optically thick, isothermal cloud with a horizontal cloud-top that would give the same continuum radiance as the observed cloud, assuming both have the same Cloud Top Temperature (CTT). Thus a single parameter  $\alpha$  (the CEF), can be used to describe the infinite range possible of cloud extinctions and spatial distributions within the actual FOV (although the concept of a single well-defined CTT in all such cases is questionable). Thus  $\alpha$  varies from 0 (cloud-free) to 1 (thick cloud completely filling the FOV) with intermediate values which may correspond either to thick cloud filling a small part of the FOV or thin cloud filling a larger fraction.

**Mathematically, the CEF,  $\alpha$ , for a FOV having central tangent height  $z_t$  is defined as**

$$\alpha = \frac{\int_{-d}^{z_t - z_c} (1 - e^{-k_c s(z)}) \phi(z) dz}{\int_{-d}^d \phi(z) dz} \quad (3)$$

whereby the FOV can be described as extending a distance  $2d$  in the vertical,  $z_c$  is the cloud top height measured upward from the Earth’s surface,  $k_c$  is the cloud extinction coefficient along the limb path  $s$ , and  $\phi(z)$  is the FOV vertical response function. From this, it is trivial to see

that, to a good approximation,

$$\alpha = \frac{R}{B_c} \quad (4)$$

where  $R$  is the continuum radiance and  $B_c$  is the (spectrally averaged) Planck function corresponding to the CTT — and this is the definition of CEF used throughout this work. Scattering from cloud particles can increase  $R$ , and thus increase the CEF — however the threshold for the CEF detection method has been selected to identify clouds optically thick enough so that scattering is not the dominant process.

This  $\alpha$  is then used as the a priori value in the retrieval of the CEF, which is done prior to the full macrophysical retrieval. To retrieve the CEF from a single microwindow spectrum, it is assumed that the observed radiance can be represented as originating from a homogeneous path with the vertically lower fraction of the FOV  $\alpha$  corresponding to an optically thick cloud whilst the upper fraction of the FOV  $(1 - \alpha)$  originates from molecular emission features above the cloud but at the same local temperature as the cloud-top. Thus, the forward model for the measured spectrally varying radiance  $R_\nu$  in order to better estimate the CEF via retrieval, is approximated as

$$R_\nu = \alpha B_c + (1 - \alpha) B_c (1 - \tau_\nu) \quad (5)$$

where  $\tau_\nu$  is the same pre-computed (climatological) molecular transmittance used in Section 2.2. Due to the narrowness of the weighting functions characteristic of limb-viewing instruments, the radiance registered within a FOV can be assumed to originate from the FOV tangent height - and not from higher (and potentially warmer) regions of the atmosphere. It is further assumed that the same expression will hold for other cloud types and distributions with the FOV parametrised by the same CEF value  $\alpha$ .

Although clearly a gross simplification, it can be made more realistic by

- (a) using microwindows containing only CO<sub>2</sub> lines rather than more variable absorbers, in which case the climatological  $\tau_\nu$  is likely to be reasonably accurate;

(b) limiting the fit to spectral points with relatively high transmittance (e.g.  $\tau_\nu > 0.75$ ), in which case the assumption of molecular emission originating near the cloud top is more likely to be valid.

In practice, this works better if  $B_c$  is constrained by a priori information — for instance, by using a temperature climatology.

The CEF is retrieved using an iterative optimal estimation scheme (Rodgers, 2000):

$$\mathbf{x}_{i+1} = \mathbf{x}_i + (\mathbf{K}_i^T \mathbf{S}_y^{-1} \mathbf{K}_i + \mathbf{S}_a^{-1})^{-1} (\mathbf{K}_i^T \mathbf{S}_y^{-1} (\mathbf{y} - \mathbf{f}_i) - \mathbf{S}_a^{-1} (\mathbf{x}_i - \mathbf{a})) \quad (6)$$

where subscript  $i$  denotes the iteration number,  $\mathbf{x}$  contains the parameters to be retrieved,  $\mathbf{y}$  contains the measurements,  $\mathbf{f}$  is the forward model (Sect. 2.5) applied to the current iteration of  $\mathbf{x}$ ,  $\mathbf{K}$  is the Jacobian matrix containing elements  $\partial \mathbf{f} / \partial \mathbf{x}$ ,  $\mathbf{S}_y$  is the error covariance matrix of  $\mathbf{y}$ ,  $\mathbf{a}$  is the a priori estimate of  $\mathbf{x}$  and  $\mathbf{S}_a$  is the error covariance of  $\mathbf{a}$ .

In the case of the CEF retrieval, the state vector contains the CEF and a retrieved value of the Planck function, and the a priori vector contains the estimated CEF  $\alpha$ , as calculated from the continuum radiance, and the Planck function evaluated at the climatological for that tangent height. The measurement vector contains the spectrally varying radiance  $L_\nu$ , which the forward model  $R_\nu$  seeks to reproduce given the appropriate  $\alpha$  and  $B_c$ .

Error on the measured spectrum is accounted for in the error covariance matrix

$$\mathbf{S}_y = \sigma_n^2 \mathbf{I}_n \quad (7)$$

for  $\sigma_n = \text{NESR}$  and the  $n \times n$  identity matrix  $\mathbf{I}_n$ . The uncertainty in the a priori is accounted for in the a priori covariance matrix  $\mathbf{S}_a$ , such that

$$\mathbf{S}_a = \begin{pmatrix} \sigma_\alpha^2 & 0 \\ 0 & \sigma_{B_c}^2 \end{pmatrix} \quad (8)$$

taking the uncertainty in the estimated CEF to be  $\sigma_\alpha^2 = (1.0)^2$ , and that in the blackbody

radiance evaluated at the tangent height can be obtained from the expression

$$\sigma_{B_c}^2 = \left( \frac{\partial B}{\partial T} \Big|_{\nu, T_t} \right)^2 \sigma_{T_t}^2 \quad (9)$$

where  $\sigma_{T_t}^2$  is the variance in the climatological temperature at  $z_t$ , typically taken around 20 K.

Once this retrieval for CEF has converged, the cloud-top is identified as lying in the highest altitude spectrum where the retrieved  $\alpha > 0.1$ . Finally, the retrieved value of  $\alpha$  is also used as a ‘measurement’ in the macrophysical parameter retrieval itself (Sect. 2.4). In principle, Eqn. 5 also yields an ‘improved’ estimate of  $B_c$  but, given the crudeness of this approximation, it is preferred to re-use the original climatological temperature profile.

## 2.4 Macrophysical Parameter Retrieval

The macrophysical parameters are retrieved using the optimal estimation formulation given in Eqn 6.

### 2.4.1 State Vector

The state vector  $\mathbf{x}$  contains the parameters to be retrieved, and in this case is defined as

$$\mathbf{x} \equiv \begin{pmatrix} z_c \\ B_c \\ \mu_c \end{pmatrix} \quad (10)$$

where  $z_c$  is the cloud-top height (CTH),  $B_c$  is the Planck function evaluated at the cloud-top temperature  $T_c$  (CTT) at the mid-point of the microwindow, and  $\mu_c = \log_{10} k_c$ , where  $k_c$  is the extinction coefficient (in  $\text{km}^{-1}$ ), which is a measure of the cloud extinction (CEX).  $k_c$  varies spectrally, and so the  $\mu_c$  retrieved in each MW corresponds to the average extinction in that MW — and any subsequent combination of MW results should keep this spectral variance in mind, even though it will be small in such a small spectral range.

In practice,  $k_c$  is the extinction coefficient corresponding to the total extinction along the MIPAS limb path, including contributions from both atmospheric and cloud components of measured signal. However, as discussed in Section 2.1, the MWs in which the cloud properties are derived have been pre-selected such that the atmospheric contributions will be negligible in comparison with the cloud signal, having transmittance greater than 95%. Thus, to good approximation, the retrieved value of  $k_c$  will correspond to the extinction of the cloud along the MIPAS limb path.

#### 2.4.2 Measurement Vector

The vector  $\mathbf{y}$ , containing the measurements used for the retrieval, is defined as

$$\mathbf{y} \equiv \begin{pmatrix} R_u \\ R_c \\ R_l \\ \alpha \end{pmatrix} \quad (11)$$

where  $R_c$  is the continuum radiance (Sect. 2.2) from the FOV containing the cloud-top, having the retrieved cloud effective fraction  $\alpha$ , while  $R_u$  and  $R_l$  are the continuum radiances from the FOVs immediately above and below, **calculated in the same manner**. The measurement covariance matrix  $\mathbf{S}_y$  is diagonal, with variances given by the errors from the continuum radiance and CEF retrieval. Although  $R_c$  and  $\alpha$  are derived from the same spectrum, the argument is that  $\alpha$  depends on the spectral structure whereas  $R_c$  is derived from the spectrally flat regions — and hence the two may be regarded as independent.

The radiance  $R_u$  from the FOV above the cloud-top is expected to have a value  $\sim 0$  (since the CEF for this FOV will have been retrieved with a value  $< 0.1$ , Sect. 2.3) and serves simply to constrain the retrieval from placing the cloud-top too high. The inclusion of the CEF in the measurement vector is discussed in the next section.



### 2.4.3 A Priori Information

This scheme essentially attempts to retrieve three macrophysical parameters from two non-zero continuum measurements,  $R_c$  and  $R_l$ . The usual method for dealing with such under-determined problems is to supply independent a priori information. Due to the spatial inhomogeneity of cloud structures, obtaining useful direct a priori information on any of the three retrieved parameters is impractical — however, there are indirect a priori constraints on the *relationships* between the retrieved parameters.

The first a priori constraint is represented by the CEF and is more conveniently introduced into the measurement vector itself ( $\alpha$  in Eqn. 11) rather than in the conventional a priori state vector  $\mathbf{a}$ . This acts as a constraint on the CTH and CEX values, as described in Sect. 2.3.

A second source of a priori information is the background temperature profile (obtained, for example, from climatology or meteorological analysis fields). Assuming this is not significantly perturbed in the presence of clouds, this acts as a constraint on the CTH and CTT, since the cloud-top temperature would be expected to correspond to a point on this profile.

Having identified the spectrum containing the cloud-top, the a priori estimate for the cloud-top height is set as the nominal tangent height for that measurement  $z_t$ , and its corresponding uncertainty  $\sigma_{z_a}$  set to  $\pm 1$  km (*cf. effective FOV width  $\sim \pm 1.5$  km, and it is reasonable that this should envelope the uncertainty in cloud top height, if the cloud detection method is trustworthy*).

For this altitude, the background temperature profile provides an equivalent radiance  $B_t$ , and uncertainty  $\sigma_{B_t}$  which is typically equivalent to a temperature uncertainty of  $\pm 10$  K. However, uncertainty with which  $z_t$  represents the actual cloud-top height, and the variation of radiance with altitude  $b = dB/dz$  (see Eqn. 14) also have to be taken into account when calculating the a priori covariance matrix elements.

There is no reasonable a priori estimate for optical thickness so it is just set at a typical mid-range value (e.g.  $\mu_a = -2.5$ ) with a large uncertainty  $\sigma_{\mu_a} = \pm 0.5$ , to capture the range of extinction for which the cloud forward model (Sect. 2.5) is applicable.

Thus the a priori vector is given by

$$\mathbf{a} = \begin{pmatrix} z_t \\ B_t \\ \mu_a \end{pmatrix} \quad (12)$$

Assuming that the Planck function varies linearly with altitude (Eqn. 14), the covariance is given by

$$\mathbf{S}_a = \begin{pmatrix} \sigma_{z_a}^2 & b^2 \sigma_{z_a}^2 & 0 \\ b^2 \sigma_{z_a}^2 & (\sigma_{B_t}^2 + b^2 \sigma_{z_a}^2) & 0 \\ 0 & 0 & \sigma_{\mu_a}^2 \end{pmatrix} \quad (13)$$

## 2.5 Cloud Forward Model

The essential assumption within the macrophysical retrieval scheme is that a cloud can be represented as a homogeneous ‘grey’ absorber characterised by just three retrieved parameters (the cloud top height  $z_c$ , the cloud-top temperature  $T_c$  and the cloud extinction  $k_c$ ).

In addition, it is assumed that the Planck function (evaluated at the spectral mid-point of the microwindow in question) varies linearly with altitude within the cloud with a known gradient, such that

$$B(z) = B_c + b(z - z_c) \quad (14)$$

where  $B_c \equiv B(T_c)$  is the Planck function for the cloud top temperature, and  $b = dB/dz$  is the vertical gradient ( $b < 0$  in the troposphere,  $b > 0$  in the stratosphere), derived from an external (e.g. climatological) estimate of the background atmospheric temperature profile.

The cloud forward model (CFM)  $\mathbf{f}$  calculates the continuum radiance originating from a cloud described by  $z_c$ ,  $T_c$  and  $k_c$ , and assumes that there is no spectral variation in absorption or in the Planck function over the limited spectral width of each microwindow.

### 2.5.1 Pencil-Beams

The continuum radiance  $L_t$  of a pencil-beam (i.e. infinitesimal solid-angle) viewing at tangent height  $z_t$  within the cloud (i.e.  $z_t < z_c$ ) is given by the standard radiative transfer equation for local thermodynamic equilibrium, assuming no molecular contributions from the atmosphere itself, and no scattering:

$$L_t = \int_s B(s) \frac{d\tau}{ds} ds \quad (15)$$

where  $B(s)$  is the Planck function (evaluated at the spectral mid-point of the microwindow) along the path  $s$ , and  $\tau(s)$  is the transmittance along the path  $s$ , given by

$$\tau = \exp(-k_c s). \quad (16)$$

Using simple circular geometry (ignoring refraction and assuming the Earth's radius,  $r_e \gg z$ ), the path distance and altitude relative to the tangent point values are related by

$$(s - s_t)^2 \simeq 2r_e(z - z_t). \quad (17)$$

Eqn. (15) can then be solved to give

$$L_t = \left( B_c + \frac{b}{r_e k_c^2} \right) (1 - \tau) - \left( \frac{b s}{2r_e k_c} \right) (1 + \tau). \quad (18)$$

The appearance of the retrieved parameter  $k_c$  in the denominator makes this potentially numerically unstable in the optically-thin limit, so a more computationally robust approximation is preferred, such that

$$L_t \simeq \left( B_c + \frac{2}{3} b (z_t - z_c) \tau \right) (1 - \tau), \quad (19)$$

which agrees with the exact solution in the asymptotic limits of transmittance. In the optically thick limit ( $\tau = 0$ ) cloud effectively just emits from its upper surface and  $L_t \rightarrow B_c$ , as expected, while in the optically thin limit ( $\tau \rightarrow 1$ ) the emission effectively comes from the point one third of the vertical distance from the tangent point to the cloud-top,  $L_t \rightarrow (\frac{1}{3} B_c + \frac{2}{3} B_t)(1 - \tau)$ , where  $B_t \equiv B(z_t)$  from Eqn. (14).

### 2.5.2 FOV Convolution

The MIPAS FOV response function is represented by a vertical trapezium with a 4 km base and a 2.8 km top when projected onto the atmospheric limb. With tangent heights spaced at 3 km intervals for the original full-resolution measurements, this gives a small overlap between adjacent measurements, but a much larger overlap for the 1.5 km spacing used in the ‘optimised-resolution’ measurements employed since 2005.

This FOV function  $\phi$  is sampled at  $N$  points (in practice,  $N = 9$ ), which determine the altitudes  $z_j$  for which the pencil-beam calculations are performed. The measured continuum radiance is then represented by a numerical convolution of the pencil-beam radiances at these altitudes ( $L_{t_j}$ ), such that

$$R = \sum_{j=1}^N a_j L_{t_j} \quad (20)$$

where  $a_j$  are coefficients of the normalised FOV convolution function at each pencil-beam altitude  $z_j$  multiplied by the ‘infinitesimal’ integration step. Below the cloud-top, as the integration occurs at finite points, the radiance is assumed to vary linearly between any two integration points – but at the cloud-top, there is a step function in radiance between that emitted by the cloud, and that emitted by the clear atmosphere.

### 2.5.3 Cloud Effective Fraction

As mentioned in Sect. 2.4.2, the CEF defined in Eqn. 4 is included in the measurement vector, therefore has to be evaluated by the forward model. Using Eqn. 20

$$\alpha = \frac{\sum_{j=1}^N a_j L_{t_j}}{B_c}. \quad (21)$$

Noting that, for optically thick cloud,  $L_t \sim B_c$  (Eqn. 19) for pencil-beams which intersect the cloud, and  $L_t = 0$  for pencil-beams above the cloud top, this expression for  $\alpha$  effectively just depends on the weights  $a_j$ , which depend only on  $z_t$ .

## 2.5.4 Definition of Cloud Forward Model

Thus, the CFM  $\mathbf{f}$  is simply Eqn. 20 applied to each of the FOVs available in the measurement vector  $\mathbf{y}$ , along with the definition of the CEF,  $\alpha$ , given in Eqn. 21. Furthermore, since these are analytic expressions, analytic derivatives are used to calculate elements of the Jacobian matrix  $\mathbf{K}$ .

## 2.5.5 Limitations of Cloud Forward Model

As a basic assumption of the forward model (CFM), the modelled cloud is assumed to fully-fill the horizontal domain of the FOV (which is a realistic assumption for cirrus fields, although potentially not for individual clouds or lower cloud layers) and to extend downwards to the surface of the Earth from the modelled cloud top height. Obviously no cloud will actually extend vertically in such a manner — this assumption is simply taken so that the cloud fills the modelled FOV to the bottom of the FOV below which that in which the cloud top is identified, and since the FOV integration does not consider any pencil-beam radiance contributions beyond this, the effective cloud base is that of the lowest extent of that FOV. These assumptions have implications upon the retrieved parameters:

1. Optically-thin clouds contains good information on all three macrophysical cloud parameters discussed here — but particularly on CEX. However, in this case there is some sensitivity to the FOV-filling assumptions.
  - Horizontal Filling Assumption: If, in reality, the cloud does not fully fill the horizontal extent of the FOV (as assumed), the retrieved CEX will be less than the real cloud extinction value. Without further information (for example, imaging to show the horizontal extent of the cloud with respect to the measurement FOV), this remains an untractable problem.
  - Vertical Filling Assumption: Similarly, if the cloud does not extend vertically to the bottom of the lowest FOV considered in the CFM (ie. that immediately below the FOV in which the cloud top is identified), a similar effect will be noticed. However,

this effect should be minimised because at these wavelengths most clouds should be opaque to radiation higher than the cloud base.

2. Optically-thick clouds will have good information on cloud top height and temperature, but will not be sensitive to extinction. Assumptions on the relative filling of the FOV will not affect the retrieved values of CTH and CTT, and the value of CEX will be fairly arbitrary, having a value reflecting a opaque or near-opaque cloud.

Furthermore, it is worth considering the optical thickness range over which the forward model is applicable. Consider first an optically thin cloud which completely fills the FOV. From the CFM, it follows that the total radiance in the FOV is

$$R_c = B_c (1 - e^{-k_c s}) \simeq B_c k_c s \quad (22)$$

The CEF of this thin cloud is

$$\alpha = \frac{R_c}{B_c} \simeq k_c s. \quad (23)$$

Assuming a pathlength of approximately 300 km, and that clouds are detected only for  $\alpha > 0.1$ , this implies that the thinnest cloud which can be registered using this detection method has an extinction coefficient of  $0.0003 \text{ km}^{-1}$ . Furthermore, for clouds having extinction of the order of  $10^{-5} \text{ km}^{-1}$ , scattering becomes a non-negligible process, and the CFM is not sufficient to describe the emitted radiance.

Turning to the optically thick limit, assume that the extinction is indistinguishable from infinity for path transmittances less than 1%:

$$\tau = e^{-k_c s} = 0.01 \quad (24)$$

Given an estimated pathlength of 300 km, this yields that clouds with  $k_c > 0.015 \text{ km}^{-1}$  are indistinguishable from one another.

Therefore, it is reasonable to expect that extinction can be retrieved in the approximate range of  $-4 \leq \mu_c \leq -1$ .

The process of scattering tends to increase the radiance emitted by a cloud — however in the range of extinction coefficients between  $10^{-4} - 10^{-1}$ , this is less than by a factor of up to two or three (see Section 3.3), which can be accounted in terms of forward modelling error in the retrieval process, but which should be realised as a limitation of the model. The inclusion of scattering into this algorithm would imply that it could not be used operationally, as addition of scattering into any calculation increases the computational cost of the problem dramatically.

As in any model, there are limits to the applicability of this algorithm, as discussed. However, as long as the limits of applicability of this model, and the errors implicit because of the basic assumptions, are well known, it can be used within the discussed range of confidence.

## 2.6 Combining Microwindow Results

### 2.6.1 Statistical Combination

Retrievals,  $\mathbf{x}_k$ , and associated covariances,  $\mathbf{S}_{xk}$ , are obtained from each of the  $M = 10$  microwindows. These results can then be combined using the standard statistical procedure for independent estimates, such that

$$\hat{\mathbf{S}}_x^{-1} = \sum_{k=1}^M (\mathbf{S}_{xk})^{-1} \quad (25)$$

$$\hat{\mathbf{x}} = \hat{\mathbf{S}}_x \sum_{k=1}^M (\mathbf{S}_{xk})^{-1} \mathbf{x}_k \quad (26)$$

where  $\hat{\mathbf{x}}$  and  $\hat{\mathbf{S}}_x$  represent the combined estimate and its covariance. There is an assumption here that the retrieved parameters do not vary spectrally — at least across the tens of wavenumbers represented by the selected microwindows (cloud-top radiances are converted to cloud-top temperatures prior to the combination). Extinction, of course, does vary spectrally — however over the small spectral range sampled by the MWs, this variation is also small. It also ignores the fact that the same a priori temperature climatology is used for each estimate, so the separate microwindow results are not strictly independent.

## 2.6.2 Spike Tests

This combination step also allows a spike-test to be applied — that is, a removal of results from any microwindows which deviate significantly from the mean. The  $\chi^2$  statistic is computed for each microwindow individually

$$\chi_k^2 = (\mathbf{x}_k - \hat{\mathbf{x}})^T \hat{\mathbf{S}}_x^{-1} (\mathbf{x}_k - \hat{\mathbf{x}}), \quad (27)$$

and if the microwindow with the highest  $\chi^2$  value exceeds the average  $\chi^2$  by some factor (e.g. 2) its results are removed from the combination and the test repeated for the remaining microwindows.

## 2.6.3 Error Inflation

In theory, the covariance  $\hat{\mathbf{S}}_x$  should contain the random error information on the retrieved values. However, it is recognised that this is an optimistic assumption since it makes no allowance for the forward model errors or approximations. If the different microwindows produce a large scatter of results, then the standard deviation  $D$  of this distribution is likely to be a better estimate of the actual uncertainty, although this does not necessarily allow for forward model errors either since all microwindows make the same assumptions. A three-element vector of scale-factors  $\mathbf{e}$  is constructed to take the maximum of these **(in order to conservatively estimate the largest error likely to propagate through from the individual retrievals, rather than the mean of all the individual retrieved errors)**, such that

$$e_m = \max \left( 1, \frac{D_m}{\sigma_m} \right) \quad (28)$$

where  $\sigma_m$  is the square root of diagonal element  $mm$  in the matrix  $\hat{\mathbf{S}}_x$  (i.e. the uncertainty in parameter  $x_m$  according to the covariance matrix) and  $D_m$  is the actual standard deviation of the parameter  $x_m$  from the different microwindow results.

The retrieval covariance is then ‘inflated’ to produce the final covariance, such that

$$\hat{\mathbf{S}}'_{x\,mm} = \mathbf{e}_m^2 \hat{\mathbf{S}}_{x\,mm}. \quad (29)$$



## 2.7 Operational Considerations

The retrieval scheme described attempts to extract the maximum cloud information (i.e. three parameters) from the spectra, and assumes that continuum radiances from the FOV containing the cloud-top, as well as the FOV immediately below, are available ( $R_c$  and  $R_l$ ).

In an operational processor, it is desirable to have alternative schemes available to perhaps retrieve fewer parameters in situations where the full retrieval fails (due to an insufficient number of microwindows providing retrievals which converge or pass the spike test), or if insufficient measurements are available (most commonly when the cloud-top is detected in the lowest spectrum in the limb scan).

Assuming that a cloud-top has been detected somewhere in the scan, the operational algorithm attempts the following retrieval schemes in sequence until one returns valid results for at least three microwindows.

1. If available, using the measurement from the tangent height below the cloud-top  $R_l$  (i.e. the cloud-top not located in the lowest tangent height in the scan), with a priori extinction information given by  $\mu_a = -2.5$  (i.e. mid-range value). This is the full three parameter retrieval ( $z_c, T_c, \mu_c$ ) from three measurements ( $R_c, R_l, \alpha$ ) (plus the nominally zero radiance measurement  $R_u$  from the tangent height above the cloud-top).
2. As (1) but setting  $\mu_a = -1.0$ , giving a ‘thick cloud’ assumption ( $k_c = 0.1 \text{ km}^{-1}$ ). Such a large initial guess value of extinction reduces the Jacobians with respect to this parameter to nearly zero, effectively leaving just two parameters ( $z_c, T_c$ ) to be retrieved from three measurements ( $R_c, R_l, \alpha$ ).
3. As (2) but without  $R_l$  — that is, the ‘thick cloud’ assumption allowing for retrieval of two parameters ( $z_c, T_c$ ) from only one tangent height using two measurements ( $R_c, \alpha$ ). This relies on the CEF retrieval in order to separate the two parameters.

### 3 Application of Algorithm

This section shows the application of the described retrieval algorithm to a small set of MIPAS data (Section 3.1), in order to highlight the quantities and errors available from the retrieval process itself, without discussion or validation of these results. Section 3.2 discusses the values retrieved by application of the algorithm to a larger MIPAS dataset, comparing to the International Satellite Cloud Climatology Project (ISCCP) high cloud climatology (ISCCP, 2008).

#### 3.1 Example Results: 1 April 2003

In this section, all measurements registered by MIPAS on 1 April 2003 have been processed using the described algorithm to highlight the products calculated and available for further analysis. Fig 3 shows the retrieved values of CTH, CTT and CEX, along with the errors stemming from the retrieval process itself (from the retrieval error covariance matrix). Furthermore, the types of retrieval, as discussed in Section 2.7, are identified by different symbols — and profiles in which there is deemed to be no cloud present are identified by a cross, giving an indication of the proportion of vertical scans taken through the atmosphere having cloud present somewhere in the scan.

#### 3.2 Application and Preliminary Validation of Algorithm to a Test Month: April 2003

Having introduced the products available from application of the retrieval algorithm to MIPAS data, the algorithm is used to process a larger dataset in order to assess whether it provides sensible estimates of cloud properties, and to compare with current climatologies.

A full month's data taken in April 2003 is used as a test ensemble. Typically around 25% of sampled MIPAS scan profiles are cloud free throughout the atmosphere, about 40% of vertical scans are retrieved with the full Type 1 retrieval, whilst about 25% are retrieved with the Type 2 retrieval and about 10% with the Type 3 retrieval. The proportion of unsuccessful retrievals is less than 1%.

Preliminary validation is carried out qualitatively, by comparing results with the ISCCP high-

cloud climatology from the D1 cloud product (ISCCP, 2008) because ISCCP is arguably the most frequently referenced cloud climatology. The high-cloud product calculated by ISCCP is used because only the highest cloud deck at each geographical location sampled by MIPAS is processed, as MIPAS is unable to see below this first-encountered-cloud. ISCCP cloud products are available every three hours — and so average cloud properties over the month are estimated by considering only those data for which there is said to be cloud (ie. no-cloud, clear-atmosphere cases do not enter into the presented averaged products), and averaging in  $2.5^\circ \times 2.5^\circ$  latitude/longitude gridboxes. The same process is used to estimate the average cloud properties retrieved from MIPAS, although there are fewer measurements in most latitude/longitude gridboxes due to lower spatial coverage provided by MIPAS).

It should be noted that ISCCP infrared cloud products are determined from nadir-measurements — as opposed to the limb-measurements registered by MIPAS — which introduces inherent geometrical differences between the two analyses. Due to the differences in geometry, it is expected that the ISCCP cloud products will show lower cloud top heights (and correspondingly, higher cloud top temperatures) because nadir measurements will penetrate further vertically into clouds, given the same opacity of cloud along the measured vertical-nadir path, than will the limb slant-paths). As well, ISCCP has a much better horizontal resolution when compared with MIPAS (a result of its nadir geometry) so it is possible that ISCCP may be able to detect low clouds near to high clouds which MIPAS would miss, thus potentially biasing the averaging statistics further.

In addition to geometrical differences between the two, the detection methods used by the two algorithms to identify those measurements in which cloud is said to occur will introduce discrepancies in the cloud products derived, since the sample of clouds selected by both is likely to be different (see ISCCP (2006) for details on ISCCP algorithms). In particular, the ISCCP cloud climatology is known to miss much high, thin cloud (Wylie, 2005), whereas MIPAS is asserted to be more sensitive to thin cloud (as a limb-viewing instrument, e.g. (Hurley et al., 2009)). Fig. 4 shows the cloud frequency of occurrence for both datasets considered.

Finally, ISCCP does not report extinction values, but rather optical depths corresponding to its nadir path, and these are obtained from measurements at approximately  $0.6 \mu\text{m}$ , so these can

really only be utilised to judge qualitatively what opacity clouds occur where.

Fig 5 shows the results of application of this retrieval algorithm to MIPAS data, along with ISCCP data, from April 2003. It is immediately obvious that (and most likely as a result of the chosen cloud detection method) the macrophysical cloud parameter retrieval presented here provides information on higher clouds (such as cirrus) which ISCCP appears to miss. MIPAS shows cloud top heights increasing toward the equator, which is expected due to increasing tropopause height toward the tropics, as does ISCCP although not showing such a strong trend. It seems to detect cloud approximately 5-10 km lower than MIPAS, and it is likely that ISCCP predominately misses the high cloud, as either a result of its cloud detection method, or its nadir-geometry, or reassigns the same high cloud a lower cloud top height due to deeper penetration into the cloud itself. Furthermore, ISCCP reports unreasonably high cloud tops at the south pole, as it is improbable that polar stratospheric cloud activity has commenced by such an early date (April) in the calendar year.

Cloud top temperatures are largely anti-correlated with cloud top heights in both the MIPAS and ISCCP results, as expected. Both the ISCCP climatology and the sample of MIPAS retrieved values exhibit the same basic shape with respect to latitude, although those estimated from MIPAS measurements are far colder, corresponding to the far higher cloud top heights insinuated by MIPAS.

Comparison of cloud opacities is only possible for those MIPAS retrievals for which a full three-parameter retrieval (type 1) is possible. It is worth noting that the CFM is applicable only for clouds having extinction coefficients ranging between  $10^{-4} \text{ km}^{-1}$  and  $10^{-1} \text{ km}^{-1}$ , as optically thinner clouds are not detected by the CEF detection method and in any case are dominated by scattering from cloud particles, and thicker clouds have no sensitivity to extinction, as all appear black beyond  $10^{-1} \text{ km}^{-1}$ . MIPAS seems to see — and appears to retrieve — more thin cloud than do its contemporaries, and particularly in regions such as the tropics where optically-thin cirrus is ubiquitous. Typical values of extinction for cirrus are reported as about  $0.05 - 250 \text{ km}^{-1}$ , putting the values of extinction retrieved from MIPAS at the lower limit of those currently catalogued. ISCCP products, as representative nadir instrument products, are limited in sensitivity to cloud opacities larger than 0.01, which may indicate that the current

climatologies, as derived from predominately nadir instruments, simply bias toward thick cloud as they are unable to capture thin cloud. If this is the case, these extinction results highlight again the suitability of limb-sounding instruments such as MIPAS for cloud analysis and study of thin clouds such as cirrus.

5 It must be mentioned, however, that the assumptions of horizontally fully-filled FOVs, as well as of cloud bases extending below the bottom of the FOV immediately below that in which the cloud top is located, could also result in low retrieved extinction values for measurements not satisfying these assumptions. There is no way, barring use of some form of added geometrical information (such as coupling imaging of each cloud-field of interest), to avoid this, as there  
10 are infinite non-homogeneous arrangements of clouds of varying opacity and clear atmosphere within each FOV. Perhaps in compiling a rigorous cloud climatology, it stands to carefully combine with such extra information in order to ensure that the clear-atmosphere component is kept to a minimum, although this is attempted in this work by choice of suitable MWs of high transmittance.

15 As well, analysis of the retrieved errors stemming from the retrieval process, as available through the retrieval's inflated MW-averaged covariance matrix  $\hat{\mathbf{S}}'_x$ , gives a quantitative estimate of the quality of the retrieved results. Fig. 6 shows the distribution of the retrieval errors for the month's worth of MIPAS data. Generally, the errors due to the retrieval indicate that the forward model/inversion are able to estimate the cloud top height within 50 m, cloud top temperature within 0.5 K, and extinction along the limb path (and largely attributable to the cloud) to within  
20 15% within the range of applicability of  $10^{-4} - 10^{-1} \text{ km}^{-1}$ .

### 3.3 Validation of Errors using KOPRA Simulations

In practice, however, the real errors are a result of the assumptions made in the forward model — horizontal and vertical (below the cloud top) homogeneity — stemming from insufficiencies  
25 in the forward model in describing reality, which cannot truly be evaluated with real MIPAS data. Furthermore, pointing errors will make MIPAS tangent altitudes uncertain by several hundred metres — and will affect the retrieved cloud top heights by the same amount — which is of the order of retrieved errors in CTH.

Whilst the forward model (CFM) discussed in the past few sections well describes an optically grey cloud, it is not necessarily a good representation of real clouds, which scatter radiation in and out of the line-of-sight. It is a useful exercise to compare the CFM with a more realistic model, which allows for scattering — and then to see how well the current retrieval is able to accurately retrieve the macroscopic parameters of a more realistic cloud.

To this end, the Karlsruhe Optimised and Precise Radiative transfer Algorithm (KOPRA) is introduced to provide more accurate simulations of scattering clouds, using a layer-by-layer approach of homogeneous layers in which the radiative transfer proceeds through a succession of extinctions, emissions and scatterings, as described in Höpfner and Emde (2005). KOPRA has been used in the European Space Agency ‘Cloud Information Retrieval from MIPAS Measurements’ MIPclouds study (Spang et al., 2008) to create a cloud spectral database for Polar Stratospheric Clouds, cirrus and liquid water clouds for a wide range of macro- and micro-physical cloud parameters, including atmospheric contributions as well as those resulting from the cloud presence itself.

For the purposes of this exercise, mid-latitude cirrus cases from the database will be considered, as they form the majority of high clouds detected by MIPAS. Mid-litudinal cirrus has been modelled here as having a cloud top height between 6.5 km and 12.5 km, a cloud depth between 0.5 km and 4 km, an effective radius between 4.0  $\mu\text{m}$  and 90.0  $\mu\text{m}$ , volume density between 1.1  $\text{m}^{-3}$  and  $1.1 \times 10^7 \text{ m}^{-3}$ , ice water content between  $10.0^{-6} \text{ g m}^{-3}$  and  $1.0 \text{ g m}^{-3}$ , with microphysical parameters defined by Baran (2001). This results in clouds modelled with extinction coefficients between approximately  $10^{-5} \text{ km}^{-1}$  and  $10^2 \text{ km}^{-1}$ .

For the sake of argument, only KOPRA simulations with cloud top heights of 10.5 km and 11.5 km and cloud depths of 4.0 km are considered (even though for the 11.5 km case the lower FOV will not have the bottom 500 m cloud-filled, but this represents a negligible radiance discrepancy). Fig. 7 compares the radiances coming from KOPRA-simulated clouds and those calculated by the CFM presented here, for the considered cases, with extinction coefficients used to colour-code the different cases.

Given that the CFM seems to accurately represent single-scattering clouds as modelled by KOPRA, it is interesting to see how well the macroscopic retrieval can estimate the retrieved

parameters, applying the full three-parameter type retrieval. Since KOPRA is a physically more rigorous model, this should give a metric of the skill with which the retrieval can determine cloud parameters for real clouds of various optical thicknesses. Again, considering the mid-latitude cirrus spectra used in the MIPclouds study, the macroscopic retrieval has been run to this end, the results of which are shown in Fig. 8.

It appears that the retrieval does a fairly consistent job of determining extinction, especially at lower extinction values ( $< 10^{-2} \text{ km}^{-1}$ ). The retrieval recognises cases of higher extinction as such — but does not necessarily get the extinction coefficient quite right for high cloud extinction, since there are negligible radiance differences once the cloud approaches the opaque limit, from values of  $10^{-2}$ – $10^{-1} \text{ km}^{-1}$ .

In terms of the retrieved cloud top heights and cloud top temperatures, the retrieval tends to consistently retrieve within 50 m and 0.5 K — however for cases of high cloud effective fraction (extinctions greater than about  $0.1 \text{ km}^{-1}$ ) it tends to overestimate cloud top height and temperature by up to 250 m and 5 K, and underestimate the extinction, in an attempt to best match the higher CFM-predicted radiance for these cases.

In conclusion, retrievals of KOPRA simulations (which are expected to better represent true clouds as they scatter radiance) using the simple CFM are reliable to within 50 m, 0.5 K and a factor of 15% of the extinction coefficient, for the extinction range for which this CFM is asserted to be representative. Thus, the CFM and retrieval based upon it work reliably within the design bounds and estimated retrieval errors provided by the error covariance matrix  $\mathbf{S}_x$ , well representing clouds for which scattering is not dominant.

### 3.4 Water Vapour Continuum

At altitudes sampled by the lower tangent heights in the vertical MIPAS scan pattern (e.g. those less than about 6 km), the water vapour continuum is difficult to distinguish from the continuum radiance introduced by emitting clouds. Due to this difficulty, the water vapour continuum becomes a potential issue for reliable cloud detection, and for retrieval of accurate cloud properties. It is possible that the water vapour spectral lines contained within some of the the selected MWs could be used to characterise the concentration of water vapour locally in the atmosphere

(at tangent heights immediately above that identified as containing the cloud top), which could then be used to disentangle the effects of the water vapour continuum from the cloud signal. In the current algorithm, the absorption from the water vapour continuum is taken into account to some extent in the utilised molecular transmittance spectra, whereby the expected water vapour continuum is effectively ‘subtracted’ from the measured continuum to establish the cloud contribution.

This has not been studied in this work, although it warrants further study, and as such may introduce errors in application of the algorithm as currently described, as regions of large water vapour concentration could be erroneously selected as cloudy measurements.

### 3.5 Comparison of CEF and CI Detection Mechanisms

Section 2.3 describes the method used to select measurements as containing cloud and as the CI Method is the traditionally used method, this section seeks to assert that the CEF is reasonable as a cloud detection method, and in fact, may capture more optically-or-geometrically thin cloud. In this section, both CEF and CI cloud detection methods are applied to the same set of spectra. This set of spectra is selected as all those spectra measured below 30 km and above the tangent height which the CEF method first detects a cloud top, which will give a realistic selection of clear and cloudy examples. Comparison between the two detection mechanisms is made using real MIPAS data for all measurements registered on 1 April 2003.

Fig. 9 shows the results of this comparison, highlighting that the CEF scheme detects more cloud than does the CI method with the application of the operational CI threshold of 1.8 (e.g., Spang, 2004) — which, arguably is set to detect clouds sufficiently opaque to cause problems for trace gas retrievals — and CEF threshold of 0.1. It is plausible that the scatter of points at higher CI are indeed cloudy cases, as there appears to be larger scatter than attributable to normal variations of temperature and trace-species concentrations. Furthermore, if the thresholds are applied and cloud detection is carried out, the CEF scheme detects more cloud particularly in regions where thin cloud such as polar stratospheric clouds or cirrus are expected. In general, the CEF method selects far more measurements as cloud-contaminated — which should yield a more complete selection of cloud data upon which to create climatological analysis.



It is worth noting that the percentage of spectra identified as containing cloud is dependent upon the choice of threshold applied to each detection method. For instance, at the operation threshold of 1.8, the CI method detects cloud in 9.8% of the studied set of spectra. The CEF method will select 9.8% of the spectra as containing cloud if its threshold is modified to 0.32 (instead of the suggested 0.1), although it is worth noting that both methods do not choose all the same individual cases as cloud-contaminated. If the CI threshold for cloud is loosened to 4.0, it selects 17.6% of the spectra in the set as cloudy — a percentage which can be matched by setting the CEF threshold to 0.08.

Application of CEF and CI cloud detection methods with the current thresholds, to MIPAS data highlights that the CEF method detects more possible cloud, including thin cloud which is frequently missed from current cloud climatologies such as ISCCP (ISCCP, 2008).

## 4 Conclusions

This study confirms that cloud top height, cloud top temperature and extinction coefficient can be successfully retrieved by modelling clouds quite simply and by using an optimal estimation-type retrieval whereby an estimate for CEF initiates the retrieval close to the correct cost minimum. **The retrieval algorithm has been tested and found reliable on simulated data, and compared with the ISCCP high-cloud climatology when the applied to real MIPAS data — although future work includes comparison with perhaps better-suited datasets such as the Cloud-Aerosol Lidar and Infrared Pathfinder Satellite Observations (CALIPSO; Winker et al., 2009).** The retrieval errors associated with application of this algorithm to **both real and simulated data** can be used to determine a measure of confidence for how well the forward model represents realistic scattering clouds. From this, CTH is retrieved to within 50 m, CTT to within 0.5 K and  $k_c$  within a factor of 15% **for clouds having extinction between  $10^{-4} \text{ km}^{-1}$  and  $10^{-1} \text{ km}^{-1}$ ,** although there do exist cases in which higher error exists. **The CTH and CTT retrievals are quite robust, however the CEX retrieval (especially for thin cloud) is sensitive to the assumptions of homogeneity within the FOV, and it is possible that the CEX can be underestimated due to atmospheric contributions along the limb path over which the extinction is calculated, although this**

effect is hopefully minimised inasmuch as possible by using atmospheric windows of negligible gaseous absorption.

It should be noted that the greatest error is expected to result from the error in the initial forward model assumption of horizontal homogeneity — that is, that a cloud can be represented by a single flat cloud top height, a single extinction coefficient and a consistent temperature structure throughout the body of the cloud. Horizontal homogeneity is a simplification of the geometry and optics of real clouds — but there are infinite possible cloud fields and it is impossible to retrieve inhomogeneous fillings of the MIPAS FOV without prior knowledge of the geometry of the inhomogeneity. Thus, whilst the assumption of horizontal homogeneity is insufficient to fully represent reality, it is the closest representation that can be accomplished without some other a priori knowledge such as a limb imager coinciding with the FTS view.

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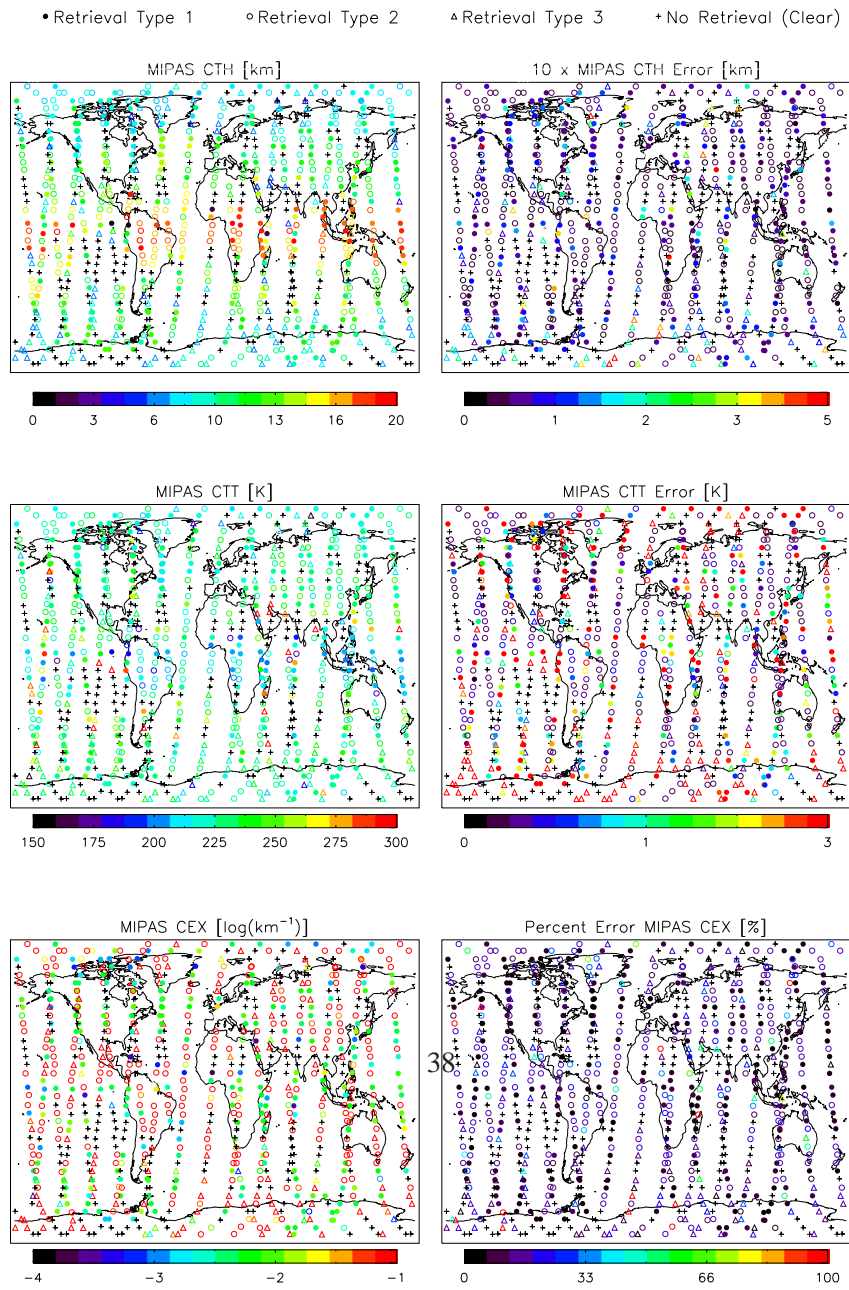
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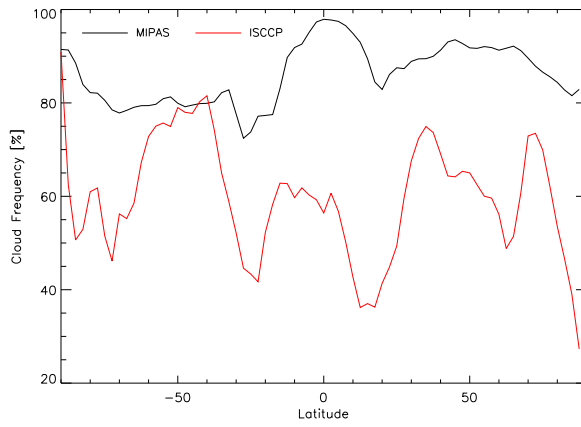
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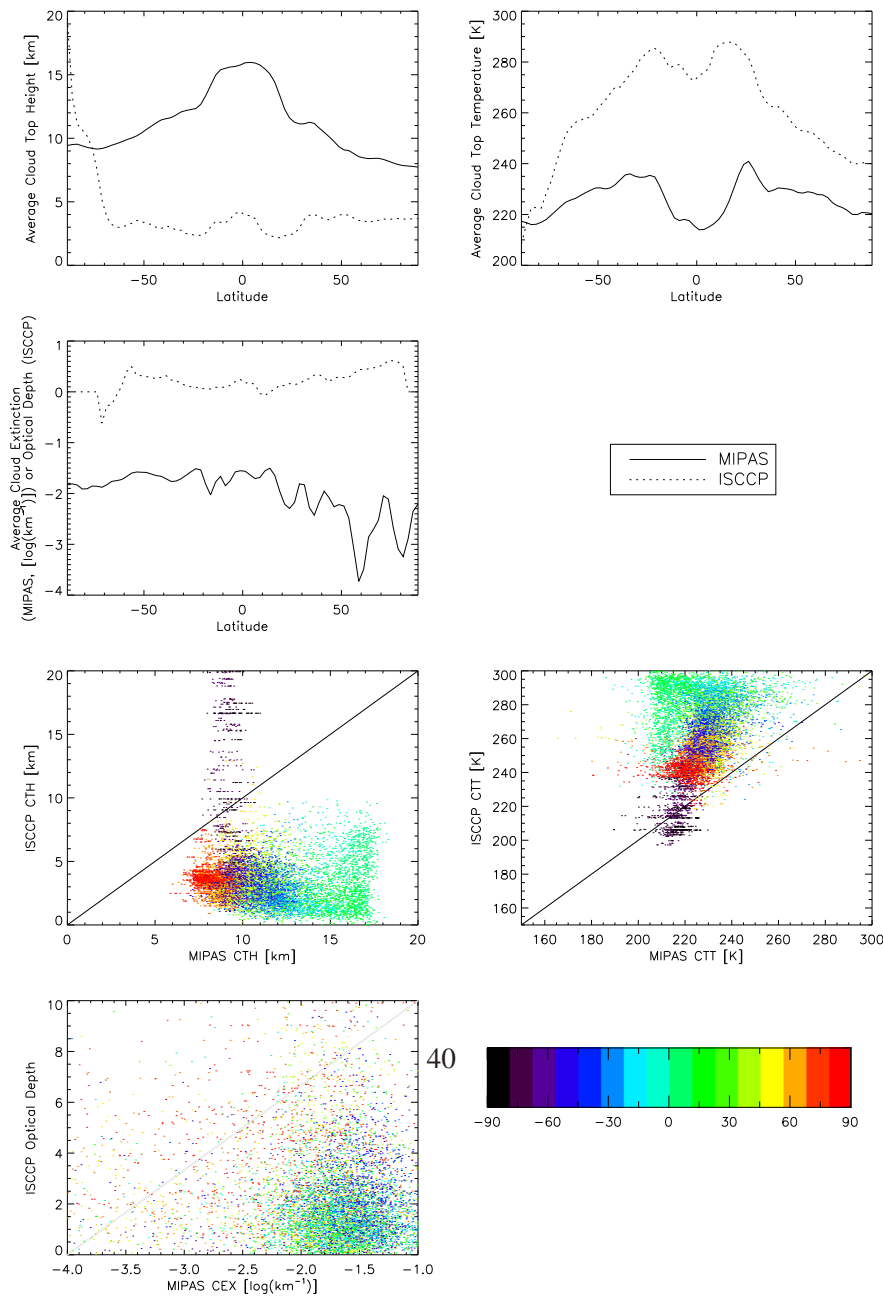
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**Fig. 3.** Application of algorithm to all MIPAS measurements taken on 1 April 2003. Retrieved parameters (left column) of CTH (top panels), CTT (middle panels) and  $k_c$  (bottom panels) and errors thereof (right panels) are given, noting the type of retrieval, corresponding to the available measurement FOVs.

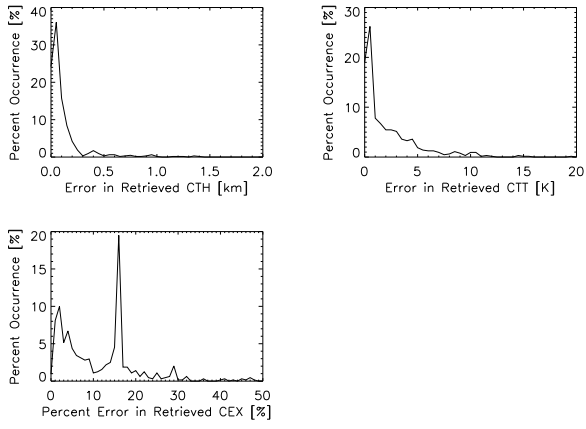


**Fig. 4.** Average cloud frequency as a function of latitude, for MIPAS (black line) and ISCCP high cloud (red line) for April 2003.

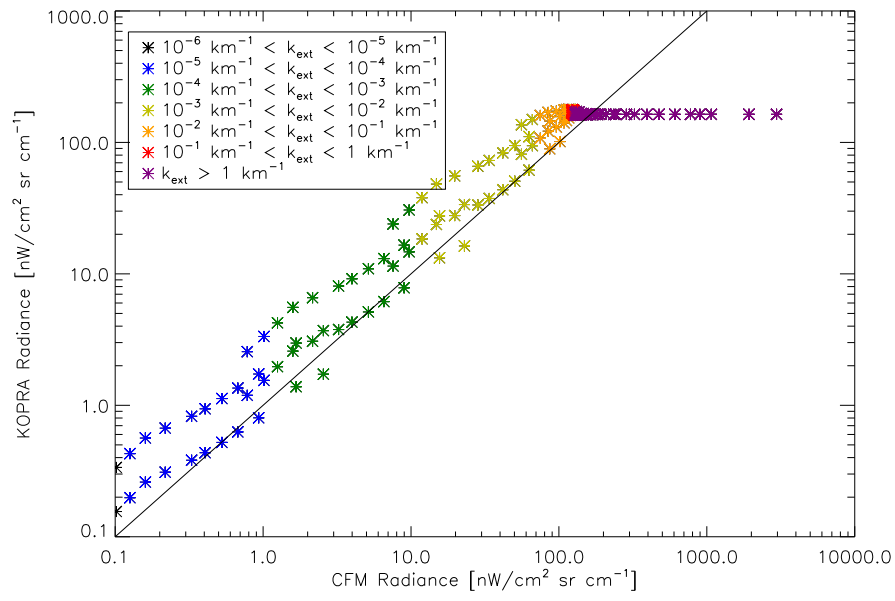


**Fig. 5.** Top panels: Zonally-averaged retrieved cloud top height (top left), cloud top temperature (top right) and logarithm of extinction coefficient (bottom left) when algorithm is applied to a month's worth of MIPAS data (solid lines), along with corresponding ISCCP quantities (dotted lines). Bottom panels: Scatterplot showing average cloud top height (top left), cloud top temperature (top right) and cloud extinction (bottom left) in a  $2.5^\circ$  by  $2.5^\circ$  latitude/longitude grid for MIPAS and ISCCP. Solid line shows one-to-one limit. Points colour-coded by latitude.

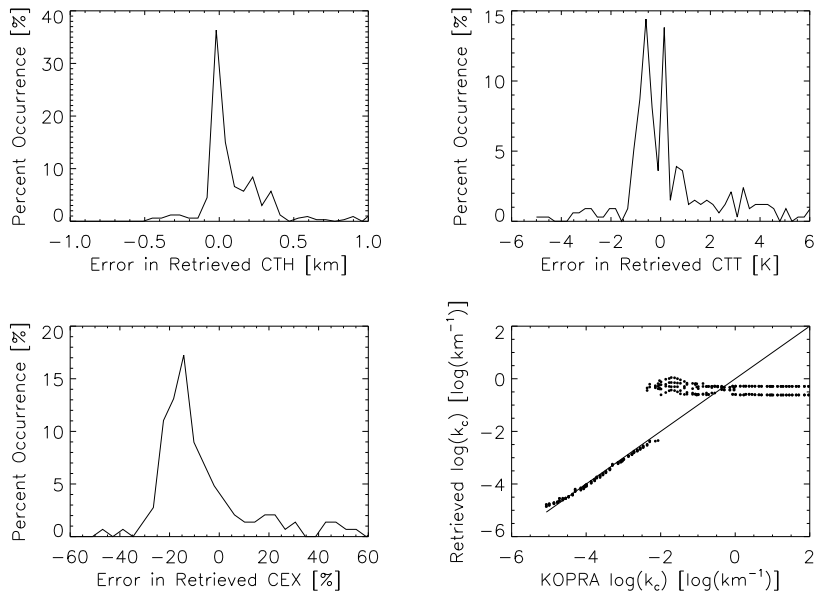




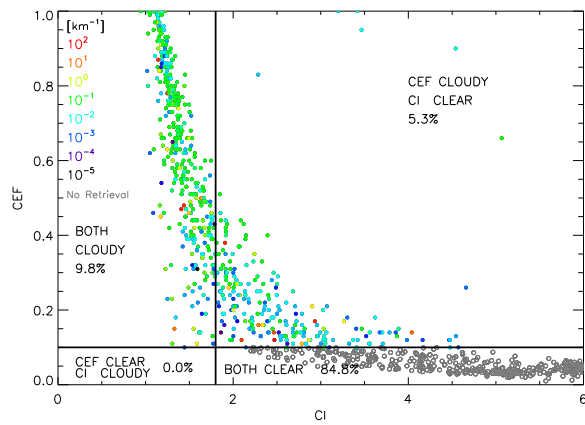
**Fig. 6.** Retrieval errors for cloud top height (top left), cloud top temperature (top right) and extinction coefficient (bottom) from application of algorithm to all MIPAS measurements taken in April 2003.



**Fig. 7.** Comparison of KOPRA (scattering and thus more realistic) and CFM (non-scattering) radiances, as a function of extinction coefficient, as indicated by colour-scale.



**Fig. 8.** Top panels: Probability distribution functions of difference between retrieved and simulated CTH (left) and CTT (right) for KOPRA-simulated clouds. Lower left panel: Probability distribution function of the percent relative difference between KOPRA-simulated  $k_c$  and retrieved  $k_c$ . Lower right panel: Scatterplot of retrieved  $\log(k_c)$  (right panel) for KOPRA-simulated clouds. Black line shows one-to-one division.



**Fig. 9.** Correlation between CI and CEF (evaluated in MW1) colour-coded by extinction coefficient (for those cases for which the retrieval has been evaluated) and by open circles for clear scans, for all spectra above the cloud top (if any) measured MIPAS on 1 April 2003. CI is anti-correlated and CEF is correlated with cloud amount. Horizontal line shows the CEF threshold (above which cloud occurs) and vertical line shows the CI threshold (to the left of which cloud occurs).