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Validation of routine continuous airborne CO₂ observations near the Bialystok Tall Tower

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Abstract

Since 2002 in situ airborne measurements of atmospheric CO₂ mixing ratios have been performed regularly aboard a rental aircraft near Bialystok (53°08′ N, 23°09′ E), a city in northeastern Poland. Since August 2008, the in situ CO₂ measurements have been made by a modified commercially available and fully automated non-dispersive infrared (NDIR) analyzer system. The response of the analyzer has been characterized and the CO₂ mixing ratio stability of the associated calibration system has been fully tested, which results in an optimal calibration strategy and allows for an accuracy of the CO₂ measurements within 0.2 ppm. Besides the in situ measurements, air samples have been collected in glass flasks and analyzed in the laboratory for mixing ratios of CO₂, CO, CH₄, N₂O, H₂, SF₆ and for isotopic ratios of δ¹³C and δ¹⁸O in CO₂. To validate the in situ CO₂ measurements that mimic the temporal averaging of the flask sampling

- process. Comparisons between in situ and flask CO_2 measurements demonstrate that these weighting functions can compensate for atmospheric variability, and provide an effective method for validating airborne in situ CO_2 measurements. In addition, we show the nine-year records of flask CO_2 measurements, from which the CO_2 increase rates are computed for the 300 m level $(1.59 \pm 0.21 \text{ ppm yr}^{-1})$ and for the 2500 m level $(1.77 \pm 0.08 \text{ ppm yr}^{-1})$. The new system, automated since August 2008, has eliminated the need for measurements and thus enables on additional vertical profile
- the need for manual in-flight calibrations, and thus enables an additional vertical profile, 20 km away, to be sampled at no additional cost in terms of flight hours. This sampling strategy provides an opportunity to investigate both temporal and spatial variability on a regular basis.

1 Introduction

²⁵ The increase of CO₂ mixing ratios in the atmosphere since pre-industrial times is the most important cause of climate change (IPCC, 2007), and this rise is due to human



activities, mainly those involving fossil fuel burning and land use change (Le Quere et al., 2009). Since atmospheric CO_2 contains a signature of surface carbon sources and sinks, a global observational network has been established to monitor CO_2 mixing ratios in the atmosphere. A quantitative determination of the distribution of carbon

sources and sinks is paramount if climate studies are to be able to analyze the response of terrestrial ecosystems to climate change and monitor fossil fuel emissions reductions in the near future. To achieve these objectives, long term accurate monitoring of atmospheric CO₂ is indispensable (Heimann, 2009).

Atmospheric transport models have been employed in inverse studies to infer the distribution of carbon sources and sinks from regular long-term CO₂ observations (Rayner et al., 1999; Roedenbeck et al., 2003; Peters et al., 2007); however, these estimates are uncertain due to the sparseness of observational constraints as well as to transport and representation errors (Engelen et al., 2002; Gurney et al., 2002; Gerbig et al., 2008). Atmospheric transport models in particular do not accurately represent verti-

- ¹⁵ cal CO₂ gradients of aircraft profiles, which could potentially be responsible for biases in the flux estimations (Stephens et al., 2007). Therefore, regular aircraft profiles are desirable in order to increase the coverage of atmospheric CO₂ observations and to improve how the vertical mixing is represented in transport models. Moreover, measuring vertical profiles of CO₂ is the only way to validate observations based on remote
- ²⁰ sensing techniques, such as Fourier Transform Spectrometers (FTS) (Washenfelder et al., 2006; Deutscher et al., 2010; Geibel et al., 2010; Wunch et al., 2010, 2011; Messerschmidt et al., 2011) from the Total Carbon Column Observing Network (TC-CON) and satellite observations, which are expected to become an important source of information in the future (Miller et al., 2005).
- Regional scale CO₂ fluxes have been investigated by aircraft campaigns throughout North America (Gerbig et al., 2003a, b) and south-western France (Sarrat et al., 2007). These campaign-based aircraft measurements are meant to provide intensive regional CO₂ information about a specific region during short periods; they are not, however, able to represent long-term variations of CO₂ fluxes. Instead, existing regular CO₂



profiles obtained from flask measurements allow the quantification of carbon fluxes over a longer period (Yang et al., 2007; Crevoisier et al., 2010; Ramonet et al., 2010). Therefore, efforts have been made to develop new methods for regular aircraft profiling; for example, both in situ and flask CO_2 measurements have been carried out aboard commercial airliners (Machida et al., 2008; Schuck et al., 2009), and aircraft profiles can now be obtained by an innovative sample system AirCore (Karion et al., 2010).

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Although flask sampling is a reliable way to obtain atmospheric measurements of CO_2 and other trace gases, and can be used to calculate column means of CO_2 from flask profiles without statistically significant bias given a sufficient number of flasks (Bakwin et al. 2003) in situ measurements are advantageous when studying high-

- (Bakwin et al., 2003), in situ measurements are advantageous when studying high-frequency variability and quantifying boundary layer mixing processes (Tans et al., 1996; Lloyd et al., 2002). Nevertheless, flask measurements are still important for validating in situ observations that may suffer from severe changes of ambient temper-ature, pressure, and humidity, as well as vibrations aboard an aircraft.
- In situ CO₂ mixing ratios have been measured regularly by a modified LI-COR 6251 system on board a rental aircraft (PZL-104 Wilga) near Bialystok, Poland since 2002. A detailed description of the analyzer system is given in Lloyd et al. (2002). Manual calibrations are performed at predefined altitude levels during a flight in order to remove potential biases due to changes of ambient pressure and temperature; however,
- significant disagreements between in situ and flask measurements are often found in routine operations. In order to improve the measurement accuracy and to obtain more scientifically useful observations within the same amount of available flight hours, a new airborne CO₂ analyzer system has been deployed and tested aboard the aircraft in April 2008, and has replaced the above-mentioned LI-COR system for routine measurements since August 2008.

The paper is organized as follows: Sect. 2 introduces the sampling site and the methods of CO_2 observations. Section 3 presents the methods for validating airborne in situ CO_2 measurements against flask measurements. The measurement data are shown in Sect. 4. Conclusions and discussion appear in Sect. 5.



2 Sampling site and methods

2.1 Site description and flight protocol

In situ measurements of CO₂ mixing ratios have been made regularly since 2002 in the vicinity of Bialystok, a city in northeastern Poland. Specifically, from 2002 to 2005, in situ ascending CO₂ profiles were made over Biebrza National Park (53°31' N, 22°40' E, \sim 60 km to the northwest of Bialystok); since 2006, the profiles have been sampled over a tall tower (53°18' N, 23°05' E, ~20 km to the north of Bialystok), where quasicontinuous in situ measurements of CO_2 , CH_4 , CO, N_2O , H_2 , and SF_6 have been made since August 2005 (Popa et al., 2010); since August 2008, two profiles of CO₂ have been collected using a new airborne CO_2 analyzer system during each flight: an 10 ascending profile over the tall tower and an additional descending profile (53°3' N, 23°02' E, ~10 km to the southwest of Bialystok). During the ascending profiling for all periods, paired flasks were manually taken by an operator using a flask sampler. In most cases, flasks were taken at seven constant altitudes, i.e. 100 m, 300 m, 500 m, 1000 m, 1500 m, 2000 m and 2500 m above ground level (the terrain in the flight area 15 is rather flat, ~150 m above sea level); exceptions are parts of the flights in 2007 and 2008, when flasks were taken only at three different altitudes (100 m, 1500 m, and 2500 m) due to limitations of funded flight hours. The sample air collected in the flask was analyzed by the GasLab at the Max Planck Institute for Biogeochemistry (MPI-BGC) in Jena, Germany, for mixing ratios of CO₂, CH₄, CO, N₂O, H₂, SF₆, and for 20 isotopic ratios of δ^{13} C and δ^{18} O in CO₂. In addition, atmospheric temperature and humidity were measured by a humidity and temperature probe (Vaisala, HMP35D). The aircraft climbed at a speed of $\sim 1.5 \,\mathrm{m \, s^{-1}}$ and descended at a speed of $\sim 5.5 \,\mathrm{m \, s^{-1}}$, corresponding to vertical resolutions of ~14 m and ~50 m, respectively (the 90 % response

time of the CO₂ analyzer system was ~9 s, see Sect. 2.2).



2.2 Characterization of the analyzer system

The new airborne CO₂ analyzer system is a modified version of a commercially available product (AOS Inc., Boulder, CO, USA). It consists of a non-dispersive infrared (NDIR) analyzer, a gas handling and a calibration system. Figure 1 shows the schematic diagram of the analyzer system.

The analyzer employs two infrared light sources, two gas cells, and two solid-state detectors to perform differential absorption measurements. The pressure in a 21 buffer downstream of the gas cells is stabilized at ~1100 mbar, a pressure that is higher than the maximum atmospheric pressure. Three CO₂ standards are employed in the ana-¹⁰ lyzer system as calibration gases, which are designated as REF, LOW, and HIGH. The reference gas has a CO₂ mixing ratio of ~380 ppm, a level that is close to the atmospheric mean CO₂ mixing ratio. The low-span and high-span gases have CO₂ mixing ratios of ~360 ppm and ~400 ppm, respectively. There are three operation modes: zero calibration, span calibration, and measurement. During zero calibration, the reference

- gas flows through the sample cell while no gas flows through the reference cell; thus both cells contain the reference gas, providing a background (zero) signal. Zero calibration is short enough to prevent diffusion of air from the pressure buffer back to the reference cell. During span calibration, low-span or high-span standard gas flows through the sample cell, while the reference gas flows through the reference cell, re-
- ²⁰ sulting in a sensitivity measurement of the analyzer. During measurement mode, the sampling air flows through the sample cell, while the reference gas flows through the reference cell, providing a measurement signal based on the absorption differences in the two cells. The mixing ratio of CO_2 of the sampling air can then be derived using the zero and span measurements.
- The flows through the sample and reference cells are ~180 sccm (standard cubic centimeters per minute, i.e., equivalent to the volume flow rate at 273.15 K and 1013.25 mbar) and ~10 sccm, respectively. The sample flow is bypassed at the same flow rate of ~180 sccm when a zero or span calibration takes place, so that the sample



inlet is constantly flushed. Water vapor in the sample air is removed by a chemical dryer tube filled with anhydrous magnesium perchlorate ($Mg(CIO_4)_2$) in order to measure the dry mole fraction of CO_2 in air.

- The cell volumes are approximately 5 cc at a pressure of ~1100 mbar. With a flow ⁵ rate of 180 sccm, the 90 % response time (assuming perfect air mixing in the sample cell) is ~4 s, which agrees well with the value derived from a laboratory test that switched between calibration and sample gases (see Fig. 2a). The response can be fitted into one exponential curve. However, the 90 % response time required to switch from one sample gas to another sample gas with different CO₂ mixing ratios is ~9 s; the increase of the response time is due to the mixing of sample air in the chemical dryer
- tube and is dependent on the size of the dryer tube. The response can then be fitted into a sum of two exponential curves (see Fig. 2b). The inlet is made of a \sim 5 m long 1/4" O.D. Synflex tube (type 1300, formerly named as Dekabon or Dekoron), and causes a time delay (from when air enters the inlet until it reaches the sample cell) of
- ¹⁵ 47 s on the ground level and 34 s on the top sampling height (~2500 m above ground) due to changes of ambient pressure. The total time lag applied to the 1 Hz in situ CO_2 data is the sum of the response time (90%) and the time delay due to the inlet tube, i.e. from 56 s to 43 s.

Temperature variation around the housing of the detectors and the light sources affects the measurements despite the fact that the two detectors of the analyzer are thermally controlled at constant temperature. When each individual internal component of the analyzer (e.g. light sources, detectors) is locally heated, CO₂ mixing ratios change ~8.3 ppm for every degree change of the housing of the light sources and ~1.8 ppm for every degree change of the housing of the detectors. This result implies that frequent calibrations are required for this analyzer to remove the thermal impacts. During flight, zero calibration is made every two minutes while low or high span calibration is carried out after every other zero calibration.

A total calibration period of 12 s is used, based on two facts: (1) the time response of the analyzer is fast, \sim 4 s for a 90% exchange, and (2) the heat flow around the



light sources and detectors due to valve switching affects the measurements. Taking a short calibration period is to minimize (1) the length of missing data due to calibrations, and (2) the influence of thermal impact. Nevertheless, laboratory tests show that CO_2 measurements of a tank air taken immediately after a 12-s calibration have a bias of

5 0.7–0.1 ppm for the period of 13–30 s after calibration. Corrections are applied to all measurements during these periods based on an empirical correction curve.

2.3 Characterization of the calibration system

The three CO₂ standards used for in-flight calibrations are contained in one 3.51 fiberwrapped aluminum cylinder (for the reference gas) and two 1.21 aluminum cylinders (for the low-span and high-span gases). The accuracy of CO₂ measurements is de-10 pendent on the stability of CO₂ mixing ratios of calibration gases delivered into the sample and reference cells, especially in the case of a long-term deployment in the field, e.g. one year or even every couple of years at the Bialystok site. To investigate the long-term CO₂ stability of the calibration system, a series of laboratory tests was carried out. A detailed description of the experimental setup is given in Winderlich (2007). This experiment involved tests of the stability of CO_2 mixing ratios for eight gas cylinders (volumes 0.75–3.5 l) associated with 3 different pressure regulators (Premier Industries, Belle Chasse, LA; Scott Specialty Gases, Plumsteadville, PA, 51– 14D; TESCOM, Tescom Europe, Selmsdorf, Germany). During these tests, the cylinders are attached with pressure regulators, followed by high-pressure stop valves that 20 block the gas flow when no experimental measurement is being performed; the valves

- of these cylinders, in contrast, are open all the time. One CO_2 standard (392.49 ppm) in a 50 I aluminum tank was used to fill all eight gas cylinders for further tests. The gases from the cylinders were measured at variable intervals depending on the availability of a high provision I offe CO, evolution (Do, Costa and Staple, 1000). The evolution
- of a high-precision Loflo CO_2 system (Da Costa and Steele, 1999). The experiment lasted ~100 days. These tests characterized the influences of pressure regulators and storage in small cylinder on CO_2 mixing ratios using two factors: a surface effect and a permeation effect (Fig. 3). These two effects are explained below in detail.



The surface effect can be explained by the tendency of CO_2 molecules to adhere to the walls of aluminum cylinders, which is a pressure-dependent process (Langenfelds et al., 2005). The CO_2 mixing ratios of the gases in the small cylinders immediately after filling are lower than that of the gas in the filled tank due to the adsorption of CO_2 molecules on the walls of these small cylinders, whereas the CO_2 mixing ratios of the gases in the small cylinders increase when the pressure drops below a relatively low level of ~30 bar due to the desorption of CO_2 molecules from the walls. The tests revealed that this effect scales with the surface area of cylinders. For example, the Al_2O_3 covered aluminum surface can explain the adsorption of 8.3×10^{16} molecules 10 at the 420 cm² inner surface of the 0.7 I cylinder (sum of reversible and irreversible

- adsorption on AL_2O_3 from Mao et al., 1994). Relying on 9.4×10^{20} molecules within the cylinder, 0.04 ppm depletion can be explained. This represents only 36% of the observed difference and could indicate a 2.75 times bigger surface roughness value of the cylinders compared to the ideally prepared Al_2O_3 surfaces from Mao et al. (1994).
- ¹⁵ The increase of CO₂ mixing ratios when the cylinder pressure is below 30 bar is consistent with the experience of other groups that use high-pressure calibration standard gases until the pressure drops to 5 to 35 bar (Daube et al., 2002; Langenfelds et al., 2005; Keeling et al., 2007). The approach of mass conservation leads to an enrichment of +0.44 ppm below ~30 bar (equivaltent to -0.11 ppm at 120 bar), which has the same magnitude as the observations.

Because some air constituents preferentially permeate the polymer material used in pressure regulators, the CO_2 mixing ratio of the gases on the high-pressure side of the pressure regulator – and eventually the gases in the cylinders – can be modified. For example, the first stage of the Scott regulator is equipped with a Viton sealed piston.

²⁵ CO₂ molecules preferentially diffuse through this polymer (Sturm et al., 2004), causing the air on the high-pressure side to become depleted in CO₂; on the low-pressure side CO₂ molecules accumulate and then diffuse when the mixing ratio of CO₂ is higher than the ambient. Therefore, for a long-term operation, the CO₂ mixing ratios of gases in the cylinders tend to decrease with time. In contrast, during each analysis of the



tank air after more than 4 h storage, the CO_2 mixing ratio increases until the CO_2 depleted air on the high-pressure side of the pressure regulator is flushed. This effect has been reported repeatedly (Da Costa and Steele, 1999; Daube et al., 2002; Keeling et al., 2007). Tests show that a TESCOM regulator has a smaller permeation effect;

⁵ however, the size of this regulator is too large to be employed in our airborne analyzer. The observed drift for 0.75 l cylinders is -0.18 ± 0.06 ppm during these tests when the cylinder valves are open and regulators are constantly attached.

Apart from the cylinder size, the variations of various parameters in different testing setups (temperature: laboratory conditions vs. 40 °C; fitting material: stainless steel vs. brass; pressure regulator type: Scott or Premier Industries) were investigated, and no influence on the trend of the CO₂ mixing ratios was observed.

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These laboratory tests led to a strategy for the use of the calibration system of the NDIR analyzer during flight: (1) calibrating the CO_2 mixing ratio of air in the small cylinder after being filled instead of using the value of the filling tank; (2) using the

- cylinders only when the pressure is above 30 bar, a conservative level below which CO₂ mixing ratios may significantly increase due to desorption of CO₂ molecules from the walls of the cylinders; (3) flushing the dead volume in the pressure regulators before measurements are started during a flight; (4) calibrating the small cylinders before and after deployment in the field to characterize a potential long-term drift in CO₂ mixing
- $_{\rm 20}$ ratios due to the diffusion effect. When these rules are followed, such a calibration system can be said to supply the measurement system with a stable CO₂ mixing ratio within 0.2 ppm.

In addition, the CO_2 mixing ratio of a sample gas is computed using the CO_2 values of the internal standards that are inferred from external standard gases, which may

differ from the actual values of CO₂ in the cylinders due to the influence of heat flow on the responses of the NDIR analyzer. However, this effect affects both sample measurement and internal calibration gases, and thus is cancelled out when the mixing ratio of sample air is computed.



Our flight interval is normally about one to three weeks; according to the CO_2 stability test, the depletion of CO_2 in the regulator could be as large as $0.5 \sim 1.0$ ppm. To overcome this, at least 1 l gas in the regulators should be flushed before flight, which ensures the mixing ratios of calibration gases running through the analyzer during flight

- are within 0.1 ppm of the real stable values. The cylinders should be used until the pressure for one of the cylinders drops below 30 bar. Calibrations of gases in the three in-flight cylinders using five external working cylinders before and after deployment in Bialystok for eight months showed drifts of CO₂ mixing ratios are smaller than 0.2 ppm. Our working cylinders are calibrated relative to the standards provided by NOAA-ESRL
- ¹⁰ (Zhao and Tans, 2006). The traceability of these laboratory standards to NOAA-ESRL at a level of 0.03 ppm for CO_2 has been confirmed by comparison programs.

3 Validation of in situ measurements with analysis results of discrete flasks

The flasks collected during flight were analyzed by an automated gas chromatographic system in the GasLab at MPI-BGC. This analytical system is regularly checked by a flask comparison program ("sausage flask program") and its consistency has been verified. Therefore, comparison of in situ CO_2 measurements with the analysis results of flasks offers one way to assess the accuracy of the in situ measurements.

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Given that air does not flow into the flasks instantaneously, flask sample data cannot be compared directly with in situ measurements. Actually, the CO₂ mixing ratio of the air in the flask is a weighted average of the mixing ratios of the air during flask flushing and filling time. During flight, flask samples are collected in two steps: first, air is pumped through the flasks at an ambient pressure for about 5 min to flush and remove the conditioning air in the flasks, and then the flasks are pressurized until the pressure reaches ~1 bar above the ambient pressure. Based on the flask sampling procedure, weighting functions for in situ measurements have been developed for comparison with flask analysis results.



3.1 Method for comparison of in situ measurements with single flask measurements

Briefly, the weighting function is derived from the assumption that the air entering a flask mixes instantaneously with the existing air in the flask. This perfect mixing has

- ⁵ been shown in laboratory tests, when a step change in the CO₂ mixing ratio in the air flowing to the flask was made and CO₂ in the air leaving the flask was analyzed with an analyzer based on the cavity ring-down spectroscopy technique. Exponential responses of this step change have been observed at flow rates from 0.5 to 3.5 l min⁻¹, indicating that the assumption of perfect mixing gives a good approximation of air mix-
- ¹⁰ ing in the flask during the flask sampling process aboard aircraft. For one single flask, the flask sampling process consists of two steps: flushing and pressurizing (see Fig. 4). During the flushing process, air flows into the flask, is instantaneously mixed, and then flows out of the flask at the same flow rate, f_0 ; at the time when the pressurizing period starts, the fraction of the air (entering the flask at time *t*) remaining in the flask, is *c*(*t*). During the pressurizing process, air flows into the flask at a decreasing flow rate of
 - f(t), and the flask is pressurized until the flask sampling is completed.

The weighting function for integrating in situ measurements so that they can be compared with the analysis result of one single flask can be described as (see Appendix A1)

$$W(t) = \begin{cases} W_{1}(t) = \frac{P_{s}}{P_{e}} \frac{1}{\tau} e^{-\frac{(t_{s}-t)}{\tau}} \left(1 - e^{-\frac{t_{s}}{\tau}}\right), \tau = \frac{P_{s}}{\frac{d\rho(t_{s})}{dt}} , 0 < t < t_{s} \\ W_{2}(t) = \frac{1}{P_{e}} \frac{d\rho(t)}{dt} , t_{s} \le t < t_{e} \end{cases}$$
(1)

²⁰ Here p_s and p_e are the flask pressures when the flask pressurizing process starts $(t = t_s)$ and ends $(t = t_e)$; p(t) is the flask pressure at time t. The weighting function for integrating in situ measurements to compare them with the analysis result of one single flask is shown in Fig. 5. The weighting function is normalized to 1 and has its maximum value at the time when the pressurizing starts $t = t_s$.



3.2 Method for comparison of in situ measurements with paired flask measurements

For the case of paired flasks, the flask sampling process consists of the same two processes: flushing and pressurizing (see Fig. 6). During flushing, air flows into and

- ⁵ out of the upstream flask and then the downstream flask at a flow rate of f_0 ; when the pressurizing period starts, the fraction of the air (entering the upstream flask at the time t) remaining in the upstream flask is $c_1(t)$, while the fraction of the air remaining in the downstream flask is $c_2(t)$. During the pressurizing period, air flows into the upstream flask at a decreasing flow rate of f(t), but out of the flask at the flow rate of f(t)/2; at the
- time when the pressurizing period ends, the fraction of the pressurizing air (entering the upstream flask at the time *t*) remaining in the upstream flask is $c'_1(t)$, while the fraction of the air coming into the downstream flask is $c'_2(t)$. It is important to note that a fraction of flushing air flows from the upstream flask into the downstream flask during the pressurizing period.

¹⁵ The weighting function for integrating in situ measurements in order to compare them with the analysis result of the upstream flask of a pair can be described as follows (see Appendix A2):

$$W_{1}(t) = \begin{cases} W_{1f}(t) = \frac{1}{\tau} \left(\frac{P_{s}}{P_{e}}\right)^{2} e^{-\frac{(t_{s}-t)}{\tau}} / \left(1 - e^{-\frac{t_{s}}{\tau}}\right), \tau = \frac{P_{s}}{2\frac{d\rho(t_{s})}{dt}}, 0 < t < t_{s} \\ W_{1\rho}(t) = \frac{2\rho(t)}{P_{e}^{2}} \frac{d\rho(t)}{dt}, t_{s} \leq t < t_{e} \end{cases}$$
(2)

The weighting function for integrating in situ measurements to compare them with the analysis result of the downstream flask of a pair can be described as follows (see Appendix A2):

$$W_{2}(t) = \begin{cases} W_{2f}(t) = \left(2\frac{P_{s}}{P_{e}} - \left(\frac{P_{s}}{P_{e}}\right)^{2}\right) \frac{\left(\frac{t_{s}-t}{\tau} e^{-\frac{t_{s}-t}{\tau}} + \left(1 - \frac{P_{s}}{P_{e}}\right)e^{-\frac{t_{s}-t}{\tau}}\right)}{\tau\left(2 - \frac{P_{s}}{P_{e}}\right)\left(1 - e^{-\frac{t_{s}}{\tau}}\right) - t_{s}e^{-\frac{t_{s}}{\tau}}}, \tau = \frac{\rho_{s}}{2\frac{d\rho(t_{s})}{dt}} \ 0 < t < t_{s} \\ W_{2f}(t) = \frac{2}{P_{e}}\frac{d\rho(t)}{dt}\left(1 - \frac{\rho(t)}{\rho_{s}}\right) \qquad t_{s} \le t < t_{e} \end{cases}$$

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(3)

where p_s and p_e are the flask pressures (both flasks have the same pressure) when the flask pressurizing process starts and ends; p(t) is the flask pressure at time t. The weighting functions for integrating in situ measurements to compare with pair-flask analysis results are shown in Fig. 7.

Here an example of using the weighting functions for integrating in situ measurements of CO₂ mixing ratios and then comparing these with flask measurement data is given. The measurement results of CO₂ mixing ratios made by the NDIR analyzer and from analyses of flask samples from a flight on 20 August 2008, in Bialystok, Poland, are shown in Fig. 8. The flask CO₂ data are shown as blue (upstream) and green
 (downstream) dots. At about 45 700 s, CO₂ flask values from the paired flasks varied by a few ppm, even though they were taken simultaneously.

The differences of integrated in situ and flask CO_2 mixing ratios using constants (1/120 over a 120 s window) and the above-described weighting coefficients are shown in Fig. 8. The improved agreements between averaged in situ and flask CO_2 mixing ratios when using the weighting functions show that the atmospheric CO_2 variability can be accounted for when using the proper weighting functions for integrating in situ CO_2 values.

3.3 Validation of in situ measurements with flask CO₂ measurements

A direct comparison of integrated in situ CO_2 values with 216 flasks from 22 flights is shown in Fig. 9a. The mean difference of in situ and flask CO_2 values is -0.45 ppm with a standard deviation of 0.88 ppm; however, obvious biases can be observed during two periods: flask No. 60 ~ 90, and >180, corresponding to 6 flights from 30 August 2008, to 30 September 2008, and 4 flights from 29 May 2009, to 7 July 2009. The discrepancies for these flights are caused by a decrease in drying efficiency of the chemical dryer and could be compensated when the in situ measurements CO_2 mixing ratios are properly

corrected using the flask values and water vapor measurements.

The biases in the differences between in situ and flask CO_2 during two periods in Fig. 9a are caused by residual water vapor in the air after the chemical dryer. This effect



can be clearly seen when the differences are plotted per flight as a function of ambient water vapor mixing ratios (see Fig. 10). The hypothesis is that the water vapor mixing ratios after the chemical dryer are proportional to the ambient values, and the drying efficiency of the chemical dryer decreases with time (inter-flight). Linear regression

- ⁵ models are fitted per flight using the least squares approach for the differences between in situ and flask CO₂ as a function of water vapor mixing ratios. One slope value is obtained from each linear regression, which is used to correct the in situ measurements of CO₂ mixing ratios based on the measured ambient water vapor mixing ratios. The comparison of integrated in situ and flask CO₂ measurements after correcting the water vapor effects for the 10 flights is shown in Fig. 9b, with the corrected values shown in
- ¹⁰ vapor effects for the 10 flights is shown in Fig. 9b, with the corrected values shown in blue. The mean difference of in situ and flask CO_2 values reduces to 0.06 ppm with a standard deviation of 0.45 ppm.

4 Measurement data

4.1 Flask CO₂

- ¹⁵ The time series of CO₂ mixing ratios at 300 m and 2500 m from 2002 to 2010 are shown in Fig. 11, excluding flasks that have been flagged as contaminated. The flasks are flagged as contaminated when abnormally low values of δ^{13} C measurements (δ^{13} C < -10 per mil on the VPDB scale) and abnormally high values of CO, and H₂ are observed. From 2002 to 2004, compressed air from Messer Griesheim Ltd was used to condition the flasks. This air contains ambient-level mixing ratios of CO₂, CH₄, N₂O, and SF₆, but during some periods, it was heavily polluted with CO and H₂. The pollution affected the analysis of air samples for CO and H₂ mixing ratios when the conditioning air was not completely flushed before air samples were collected. Starting in 2005, compressed dried ambient air filled with a compressor system from the roof
- ²⁵ of the Max Planck Institute for Biogeochemistry into high-pressure cylinders has been used as conditioning air to eliminate this problem.



A linear trend and a third order harmonic function have been fitted to the CO₂ data at 300 m and at 2500 m, respectively (see Fig. 11). For comparison, the reference marine boundary layer CO₂ (Masarie and Tans, 1995; GLOBALVIEW-CO₂, 2011) is interpolated to the latitude of the flask sampling site, and shown in Fig. 11. The increasing trend of the marine boundary layer CO_2 for the whole period $(2.00 \pm 0.02 \text{ ppm yr}^{-1})$ 5 is statistically larger than the trends of CO₂ data at 300 m (1.59 \pm 0.21 ppm yr⁻¹) or 2500 m (1.77 \pm 0.08 ppm yr⁻¹). Given the large scatter for the CO₂ at 300 m, the difference between the trend of the marine boundary layer CO₂ and that of the CO₂ data at 300 m may not be significant. However, the difference between the trend of the marine boundary layer CO_2 and that of the CO_2 data at 2500 m is more likely significant. This 10 difference is caused by larger winter signals in recent years, and could be explained by a transport pattern change or a change in the fluxes that contribute to the CO₂ data at 2500 m relative to those contributing to the Marine boundary layer CO₂ (Ramonet et al., 2010). Using the same measurement period – between July 2005 and December 2008

- ¹⁵ as in Popa et al. (2010), the CO₂ growth rates estimated from CO₂ data at 300 m and 2500 m are 2.11 ± 0.64 ppm yr⁻¹ and 2.28 ± 0.18 ppm yr⁻¹, respectively. These values are consistent with the estimated value of 2.02 ± 0.46 ppm yr⁻¹ using 300 m CO₂ data from the Bialystok tall tower (Popa et al., 2010). In summer, the level of CO₂ both at 300 m and the marine boundary CO₂ is significantly lower than the level of CO₂ at
- ²⁰ 2500 m due to the uptake of CO_2 by plant, whereas in winter, regional fossil fuel emissions increases the level of CO_2 at 300 m. To calculate the seasonal amplitude, CO_2 data at 300 m and 2500 m for the period between July 2005 and December 2008 are de-trended using the linear trends derived from the above-described fits, and then fitted to third order harmonic functions. The results show that the seasonal amplitude of CO_2
- at 2500 m (10.5 ppm) is significantly smaller than that of CO_2 at 300 m (20.4 ppm). The planetary boundary layer heights that are determined from the vertical profiles of temperature and water vapor are between 300 m and 2500 m. Both seasonal cycles have minimum values around August; however, the CO_2 mixing ratio at 300 m decreases abruptly in spring, while the CO_2 at 2500 m decreases smoothly from April to August.



This reflects the larger influence CO_2 uptake by plants has on the 300 m level than on the 2500 m level in the free troposphere.

Furthermore, the seasonal cycle of CO₂ gradients (differences of CO₂ values at altitudes of 300 m and 2500 m) is calculated, and shown in Fig. 12. These CO₂ gradients
contain useful information for estimating carbon fluxes between the surface and the free troposphere, and for improving vertical mixing of transport models (Lai et al., 2006; Stephens et al., 2007). Similarly, a smoothed curve has been fitted into these data using a third order harmonic function, which demonstrates that from April to September, the CO₂ gradients are negative, with the minimum value in July, mainly due to uptake
of CO₂ by plants through photosynthesis; however, the gradients are positive for the rest of the year, indicating CO₂ surface sources dominate sinks.

4.2 In situ CO₂

As an example, in situ continuous CO₂ mixing ratio profiles from a flight on 20 August 2008 are shown in Fig. 13. The collection of two profiles from each flight provides ¹⁵ an opportunity to assess the spatial variability of mixed-layer CO₂ averages based on observations. Flights were made every one to three weeks, around mid-day under fair weather conditions. Ascending profiles were usually made over a national park, while descending profiles were taken over a mixture of forest and cultivated land that is about 20 km away and is on the other side of the city of Bialystok. Descending profiles were always made after ascending profiles, roughly 50 min later (the average time difference

²⁰ always made after ascending profiles, roughly 50 min later (the average time difference between the time when the ascending and the descending profiles are carried out).

The planetary boundary layer (PBL) heights are determined from the potential temperature profiles using the parcel method (Seibert et al., 2000). The mixed-layer average CO₂ mixing ratio for each profile, \overline{CO}_2 , is calculated as the mass weighted average,

excluding the bottom 10% and the top 20% of the mixed layer to avoid the influence of both the surface layer at the bottom and the entrainment zone at the top. The differences of mixed-layer CO_2 averages between the ascending and the descending profiles are shown in Fig. 14, separated as the part of the growing season with peak



carbon uptake (June, July, and August) and the rest of the growing season (April, May, and September), hereafter referred to as the peak growing season and the non-peak growing season, respectively. The uncertainty of the mixed-layer averages for each profile is estimated based on the method employed in Gerbig et al. (2003a). The uncertainty ranges from 0.04 to 0.41 ppm for individual profiles. The uncertainty of the differences is the square root of the sum of variances of the ascending and the descending profiles.

The differences of mixed-layer CO_2 averages between the ascending and the descending profiles during the peak growing season are significantly larger than 0 ppm

- ¹⁰ (*t*-test *p*-value 0.006), whereas for the non-peak growing season they are not significantly different from 0 ppm (*t*-test *p*-value 0.115). The differences of mixed-layer CO_2 averages could have resulted from two main factors: the spatial gradients or changes in time associated with CO_2 sources or sinks at the surface. During the peak growing season, CO_2 is depleted in the mixed layer due to the uptake by vegetation, and as a
- ¹⁵ result, the mixed-layer CO₂ average during ascending is higher than the mixed-layer CO₂ average during descending made roughly 50 min later. The average change in CO₂ during the growing season (June–September) between local time 10:00 and 15:00 is estimated to be 0.24 ppm 50 min⁻¹ based on tower observations (Popa et al., 2010), which is much smaller than the mean difference found from the in-situ aircraft profiles
- ²⁰ of 1.1 ppm. Therefore, the differences must be due to spatial variations. The variability of the differences of the mixed-layer average CO₂ is 1.2 ppm during the peak growing season, which is larger than that during the non-peak growing season, 0.6 ppm.

5 Discussion and conclusion

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Accurate in situ measurements of CO₂ mixing ratios have been achieved using a modified commercially available NDIR analyzer system. An optimized calibration strategy has been derived based on characterization of the analyzer and test results of stability of CO₂ mixing ratios in small cylinders. An in-flight calibration system is necessary for



in situ analyzer systems to account for potential drift due to instability under severe conditions of vibrations, changing temperature and pressure aboard aircraft (Anderson et al., 1996; Daube et al., 2002; Machida et al., 2008). Although the recently available cavity ring-down spectroscopy technique (Chen et al., 2010) has been proven to be

- 5 sufficiently stable aboard a research aircraft within a field campaign period, an in-flight calibration system is still highly recommended when no other independent measurements are available or if the analyzer needs to be deployed over the long term. The automation of the new system after August 2008 eliminates the requirement of manual in-flight calibrations on certain constant height levels, and thus, by saving flight time,
- allows for more extensive spatial sampling of the atmosphere. Observed spatial gra-10 dients between two vertical profiles sampled at 20 km distance near the Bialystok tall tower indicate spatial differences in upstream source-sink distributions. In combination with high-resolution transport modeling these observations provide important information on representation errors when utilizing tall tower data in inverse models to infer surface-atmosphere fluxes. 15

A method for comparing in situ with flask CO₂ measurements using weighting functions has been developed applicable to both single and paired flask samples. Comparisons between in situ and flask CO₂ measurements demonstrate that atmospheric variability can be well accounted for by using weighting functions. Therefore, these weighting functions can be applied to compare various in situ continuous measurements with discrete measurements of other trace gases. In addition, when flask measurements from a mobile platform are used in a modeling frame work, the effective location (latitude, longitude, and altitude) of the flask measurements can be derived from integrating corresponding in situ continuous measurements using these weighting functions. 25

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In addition, we show the nine-year records of flask CO₂ from which the CO₂ increase rates are computed for the 300 m level $(1.59 \pm 0.21 \text{ ppm yr}^{-1})$ and for the 2500 m level $(1.77 \pm 0.08 \text{ ppm yr}^{-1})$. The difference between a reference trend of marine boundary layer CO_2 and that of our CO_2 data at 2500 m is likely significant, and could be



explained by a transport pattern change or a change in the fluxes that contribute to the CO_2 data at 2500 m relative to those contributing to the marine boundary layer CO_2 . The regular sampling of two profiles that are 20 km apart provides an opportunity to investigate temporal and spatial variability.

5 Appendix A

The following presents a detailed description of how the weighting functions for integrating in situ measurements are derived, i.e. how single and paired flask measurements
are compared based on two assumptions during the flask sampling process: (1) incoming air mixes instantaneously with existing air in the flasks; (2) the change of temperature in the flasks is negligible.

A1 Single flask model

The weighting function for integrating in situ measurements to compare them with a ¹⁵ single flask measurement is divided into two parts based on the processes during flask sampling: flushing and pressurizing (see Fig. 5). When the flask sampling is completed, the influence of remaining conditioning air on the CO_2 mixing ratio in the flask is negligible. The mixing ratio of CO_2 in the flask is determined by the CO_2 mixing ratios of sampling air starting at flushing until pressurizing is complete, weighted by a ²⁰ function. The CO_2 mixing ratio within the flask can be written as:

$$< \operatorname{CO}_{2} > = \int_{0}^{t_{e}} \operatorname{CO}_{2}(t) W(t) dt$$
$$= \int_{0}^{t_{s}} \operatorname{CO}_{2}(t) W_{f}(t) dt + \int_{t_{s}}^{t_{e}} \operatorname{CO}_{2}(t) W_{\rho}(t) dt$$



(A1)

where $\langle CO_2 \rangle$ is the CO₂ mixing ratio of the air in the flask; t_s and t_e are the time when the pressurizing process starts and ends; W(t) is the weighting function that consists of $W_f(t)$ and $W_p(t)$, for the flushing and the pressurizing periods, respectively. The weighting function is proportional to the amount of the air (entering the flask at time t) remaining in the flask when the flask compliance is completed in the weighting the flask at

time t) remaining in the flask when the flask sampling is completed, i.e., the volume of sampling air flowing into the flask at time t multiplied by the fraction of the air that is preserved in the flask, given the volume is reported at the same pressure. The sum of the overall weighting function is normalized to 1.

During the flushing period $(0 < t < t_s)$, the incoming air mixes with the air in the flask and flows through the flask. When the pressurizing starts $(t = t_s)$, the air already in the flask is preserved. Because the flushing period is short (around 2 min), the ambient air pressure and the volume flow rate can be regarded as constants, i.e., $f(t) = f_{0,p}(t) = P_s$. The mass balance for air in the flask at any time *t* can be written as:

$$V\frac{\mathrm{d}c\left(t'\right)}{\mathrm{d}t'}=-f_{0}c\left(t'\right)$$

where c(t') is, at any given time $t'(t < t' < t_s)$, the fraction of the air (in the flask at time t) remaining in the flask, given the boundary condition c(t' = t) = 1; V is the volume of the flask, and f_0 is the volume flow rate at the ambient pressure P_s .

The solution of the equation is

$$c(t',t) = e^{-(t'-t)/\tau}, \tau = \frac{V}{f_0}$$
(A3)

At the end of the flushing period, i.e., $t' = t_s$, the fraction of the air (in the flask at time *t*) remaining in the flask is

$$C(t_{\rm s},t) = e^{-(t_{\rm s}-t)/\tau}$$
 (A4)

According to Eq. (A.4), for the air entering the flask at any given time *t* (with the volume $f_0 \cdot dt$), the remaining volume in the flask at time t_s is $f_0 \cdot dt \cdot e^{-(t_s - t)/\tau}$. The weighting 7007



(A2)

function $W_f(t)$ is then proportional to $f_0 \cdot dt \cdot e^{-(t_s - t)/\tau}$:

 $W_f(t) \sim e^{-(t_s - t)/\tau}$

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During the pressurizing process, all incoming air is kept in the flask until the whole flask sampling process is completed (see Fig. 5). The weighting function $W_p(t)$ is thus proportional to the volume flow rate, for which mass balance can be depicted as follows:

$$W_{p}(t) \sim f(t) = \frac{V}{P_{s}} \frac{\mathrm{d}p(t)}{\mathrm{d}t}$$

where P_s is the ambient pressure before the pressurizing period starts, f(t) is the volume flow rate at the pressure of P_s , and p(t) is the air pressure in the flask.

When the flask sampling is completed, the flask pressure is $P_{\rm e}$, and the fraction of all flushing air in the flask is

$$F_1 = \frac{P_{\rm s}}{P_{\rm e}} \tag{A7}$$

and the fraction of all pressurizing air in the flask is

$$F_2 = 1 - \frac{P_{\rm s}}{P_{\rm e}} \tag{A8}$$

Based on Eqs. (A.5-8), the weighting coefficients for integrating in situ measurements



$$= \begin{cases} W_1(t) = \frac{P_s}{P_e} \frac{1}{\tau} e^{-\frac{(t_s - t)}{\tau}} / \left(1 - e^{-\frac{t_s}{\tau}}\right), \tau = \frac{P_s}{\frac{dp(t_s)}{dt}} \quad 0 < t < t_s \\ W_2(t) = \frac{1}{P_e} \frac{dp(t)}{dt} \quad t_s \le t < t_e \end{cases}$$
(A9)

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(A5)

(A6)

A2 Paired flask model

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The weighting coefficients for integrating in situ measurements to compare them with paired flask measurements are also divided into two parts during the flask sampling: flushing and pressurizing; however, the situations for the upstream and the downstream flasks are different and need to be considered separately.

The CO_2 mixing ratio within the flask can be written as:

$$< CO_{2} >_{1,2} = \int_{0}^{t_{e}} CO_{2}(t) W_{1,2}(t) dt$$
$$= \int_{0}^{t_{s}} CO_{2}(t) w_{1,2f}(t) dt + \int_{t_{s}}^{t_{e}} CO_{2}(t) W_{1,2p}(t) dt$$
(A10)

where the subscripts1 or 2 denotes the upstream and the downstream flasks respec-10 tively.

A2.1 Upstream flask

During the flushing period, the situation for the upstream flask is the same as in the single flask model and the weighting function W_{1f} is proportional to

 $C_1(t) = e^{-(t_s - t)/\tau}$

¹⁵ During the pressurizing period, the process for the upstream flask is a combination of a flushing process and a pressurizing process due to the fact that part of the air from the upstream flask flows into the downstream flask at half of the flow rate (see Fig. 7).

For air in the flask at any given time $t_{,}(t_{s} < t < t_{e})$, the mass balance equation can be depicted as follows:

$$\frac{d\left(V\frac{\rho(t)}{P_{s}}c_{1}'(t')\right)}{dt'} = -\frac{f(t')}{2}\frac{\rho(t)}{\rho(t')}c_{1}'(t')$$

(A11)

(A12)

 $c'_1(t')$ is the fraction of the air (in the flask at time *t*) remaining in the flask at any given time $t'(t < t' < t_e)$ and f(t') is the volume flow rate (at pressure P_s) of sampling air. Besides, f(t') and p(t') are constrained by the equation

$$\frac{1}{2}f(t') = \frac{V}{P_{\rm s}}\frac{{\rm d}\rho(t')}{{\rm d}t'}$$
(A13)

5 Combining Eqs. (A.12) and (A.13) produces

$$\frac{d\rho(t')}{dt'}c'_{1}(t') + \rho(t')\frac{dc'_{1}(t')}{dt'} = 0$$
(A1)

The solution of Eq. (A.14) is:

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$$C'_{1}(t',t) = \frac{\rho(t)}{\rho(t')}$$

When the flask sampling is completed, i.e., $t' = t_e$, the pressure reaches its final value, P_e , the fraction of the air (in the flask at time *t*) remaining in the flask is

$$c'_{1}(t_{e},t) = \frac{p(t)}{P_{e}}$$
 (A16)

According to Eq. (A.16), for the air entering the flask at any given time *t* (with the volume $f_0 \cdot dt$), the remaining volume in the flask at time t_e is $f_0 \cdot dt \cdot \frac{p(t)}{P_e}$. The weighting function $W_{1p}(t)$ is then proportional to $\frac{p(t)}{P_e}$. The fractions of the flushing air remaining in the upstream flask at the time t_s and the fractions of pressurizing air in the downstream flask at the time t_e are shown in Fig. A1.

When $t = t_e$, the fraction of the air (entering the upstream flask at time t, with the volume of $f(t) \cdot dt$) remaining in the upstream flask is $\frac{\rho(t)}{P_e}$, and the fraction flowing into the downstream flask is $1 - \frac{\rho(t)}{P_e}$.



4)

(A15)

When the flask sampling is completed, the flask pressure is $P_{\rm e}$, the fraction of all air that flows into the flask during flushing is

$$F_{1f} = \frac{P_{\rm s}}{P_{\rm e}} / \frac{P_{\rm e}}{P_{\rm s}} = \left(\frac{P_{\rm s}}{P_{\rm e}}\right)^2$$

and the fraction of all pressurizing air in the flask is

$$F_{1\rho} = 1 - \left(\frac{P_{\rm s}}{P_{\rm e}}\right)^2$$
 (A18)

Based on Eqs. (A.11), (A.16–18), and the normalization, the weighting function for integrating in situ measurements to compare with the upstream flask is described as

$$W_{1}(t) = \begin{cases} W_{1f}(t) = (\frac{P_{\rm s}}{P_{\rm e}})^{2} e^{-(t_{\rm s}-t)/\tau} / \int_{0}^{t_{\rm s}} e^{-(t_{\rm s}-t')/\tau} dt', & 0 < t < t_{\rm s} \\ W_{1\rho}(t) = (1 - (\frac{P_{\rm s}}{P_{\rm e}})^{2}) \frac{d\rho(t)}{dt} \frac{\rho(t)}{P_{\rm e}} / \int_{t_{\rm s}}^{t_{\rm e}} \frac{d\rho(t')}{dt'} \frac{\rho(t')}{P_{\rm e}} dt', t_{\rm s} \le t < t_{\rm e} \end{cases}$$

$$= \begin{cases} W_{1f}(t) = \frac{1}{\tau} (\frac{P_{\rm s}}{P_{\rm e}})^2 e^{-\frac{(t_{\rm s}-t)}{\tau}} / \left(1 - e^{-\frac{t_{\rm s}}{\tau}}\right), \tau = \frac{P_{\rm s}}{2\frac{d\rho(t_{\rm s})}{dt}}, 0 < t < t_{\rm s} \\ W_{1\rho}(t) = \frac{2\rho(t)}{\rho_{\rm e}^2} \frac{d\rho(t)}{dt}, t_{\rm s} \le t < t_{\rm e} \end{cases}$$
(A19)

A2.2 Downstream flask

During the flushing period ($0 < t < t_s$), the incoming air mixes with the air in the upstream flask and flows through the downstream flask. When the pressurizing starts ($t = t_s$), the air already in the downstream flask is preserved. The mass balance for the air in the upstream flask at any time *t* can be written as:

$$V\frac{dc_2(t')}{dt'} = f_0 c_1(t') - f_0 c_2(t')$$
(A20)



(A17)

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where $c_1(t')$, $c_2(t')$ are, at any given time $t'(t < t' < t_s)$, the fractions of the air (in the upstream flask at time t) remaining in the upstream and downstream flasks, respectively, given the boundary condition $c_1(t) = 1$, $c_2(t) = 0$; V is the volume of the flask, and f_0 is the volume flow rate at the ambient pressure p_s .

The solution of the equation is

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$$C_2(t',t) = \frac{t'-t}{\tau} e^{-(t'-t)/\tau}, \tau = \frac{V}{f_0}$$
(A21)

At the end of the flushing period, i.e., $t' = t_s$, the fraction of the air (in the upstream flask at time t) remaining in the downstream flask is

$$C(t_{\rm s},t) = \frac{t_{\rm s} - t}{\tau} e^{(t_{\rm s} - t)/\tau}, \tau = \frac{V}{f_0}$$
(A22)

According to Eq. (A.20), for the air entering the upstream flask at any given time t 10 (with the volume $f_0 \cdot dt$), the remaining volume in the downstream flask at time t_s is $f_0 \cdot dt \cdot \frac{t_s - t}{\tau} \cdot e^{-(t_s - t)/\tau}$. In addition, a fraction of the air that has flown into the upstream flask during flushing flows into the downstream flask during the pressurizing period, and according to Eq. (A.14), at time t_e the fraction of the air (in the upstream flask at time t_s) flowing into the downstream flask is $1 - \frac{P_s}{P}$. As a result, at time t_e , for the air 15 entering the upstream flask at any given time t (with the volume $f_0 \cdot dt$), the remaining

volume in the downstream flask is $f_0 \cdot dt \cdot \left(\frac{t_s}{\tau} \cdot e^{-(t_s-t)/\tau} + \left(1 - \frac{P_s}{P_s}\right) \cdot e^{-(t_s-t)/\tau}\right)$, which is proportional to the weighting function $W_{2f}(t)$:

$$W_{2f}(t) \sim \left(\frac{t_{\rm s} - t}{\tau} e^{-(t_{\rm s} - t)/\tau} + \left(1 - \frac{P_{\rm s}}{P_{\rm e}}\right) e^{-(t_{\rm s} - t)/\tau}\right)$$
(A23)

During the pressurizing period, the fraction of the air (in the upstream flask at time t) 20 coming into the downstream flask can be derived from Eq. (A.14):

$$c'_{2}(t_{e},t) = 1 - \frac{p(t)}{P_{e}}$$
 (A24)



According to Eq. (A.21), for the air entering the flask at any given time *t* (with the volume f(t)dt), the weighting function $W_{2p}(t)$ is then proportional to $f(t)dt\left(1-\frac{p(t)}{P_{e}}\right)$:

$$W_{2\rho}(t) \sim f(t) \left(1 - \frac{\rho(t)}{P_{\rm e}} \sim \frac{\mathrm{d}\rho(t)}{\mathrm{d}t} \left(1 - \frac{\rho(t)}{P_{\rm e}} \right) \right) \tag{A25}$$

When the flask sampling is completed, the flask pressure is p_s , and the fraction of flushing air in the downstream flask is

$$F_{2f} = \frac{V + V\left(1 - \frac{P_{\rm s}}{P_{\rm s}}\right)}{V\frac{P_{\rm e}}{P_{\rm s}}} = 2\frac{P_{\rm s}}{P_{\rm e}} - \left(\frac{P_{\rm s}}{P_{\rm e}}\right)^2 \tag{A26}$$

and the fraction of pressurizing air in the downstream flask is

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$$F_{2\rho} = 1 - F_{2f} = \left(\frac{P_{\rm s}}{P_{\rm e}}\right)^2 \tag{A27}$$

Based on Eqs. (A.23) and (A.25–27), the weighting function for the downstream flask is described as:

$$W_{2}(t) = \begin{cases} W_{2f}(t) = \left(2\frac{P_{\rm s}}{P_{\rm e}} - \left(\frac{P_{\rm s}}{P_{\rm e}}\right)^{2}\right) \frac{\left(\frac{t_{\rm s}-t}{\tau}e^{-(t_{\rm s}-t)}/\tau + \left(1-\frac{P_{\rm s}}{P_{\rm e}}\right)e^{-(t_{\rm s}-t)/\tau}\right)}{\int_{0}^{t_{\rm s}} \left(\frac{t_{\rm s}-t}{\tau}e^{-(t_{\rm s}-t')/\tau} + \left(1-\frac{P_{\rm s}}{P_{\rm e}}\right)e^{-(t_{\rm s}-t')/\tau}\right)dt'} \right) , 0 < t < t_{\rm s} \\ W_{2p}(t) = \left(1-\frac{P_{\rm s}}{P_{\rm e}}\right)^{2} \frac{\frac{d\rho(t)}{dt}\left(1-\frac{\rho t}{P_{\rm e}}\right)}{\int_{t_{\rm s}}^{t_{\rm e}} \frac{d\rho(t)}{dt}\left(1-\frac{\rho(t)}{P_{\rm e}}\right)dt} , t_{\rm s} \le t < t_{\rm e} \end{cases}$$

$$= \begin{cases} W_{2f}(t) = \left(2\frac{P_{s}}{P_{e}} - \left(\frac{P_{s}}{P_{e}}\right)^{2}\right) \frac{\left(\frac{t_{s}-t}{\tau}e^{-\frac{t_{s}-t}{\tau}} + \left(1 - \frac{P_{s}}{P_{e}}\right)e^{-\frac{t_{s}-t}{\tau}}\right)}{\tau\left(2 - \frac{P_{s}}{P_{e}}\right)\left(1 - e^{-\frac{t_{s}}{\tau}}\right) - t_{s}e^{-\frac{t_{s}}{\tau}}}, \tau = \frac{P_{s}}{2\frac{d\rho(t_{s})}{dt}}, 0 < t < t_{s} \\ W_{2p}(t) = \frac{2}{P_{e}}\frac{d\rho(t)}{dt}\left(1 - \frac{\rho(t)}{P_{e}}\right), \qquad t_{s} \leq t < t_{e} \end{cases}$$
(A28)

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Fig. 1. Flow diagram of the CO_2 analyzer system. The system consists of three standard gases, labeled REF, HIGH, and LOW. The flow rates for different paths are controlled by actuating corresponding proportional valves.

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Fig. 2. (a) One exponential curve fit for the response time from calibration to sample gas, and the 90% response time \sim 4s, **(b)** sum of two exponential curve fit for the response time from one sample to another sample gas, and the 90% response time is \sim 9s. The dashed lines indicate the 90% responses.





Fig. 3. Long-term stability of CO_2 mixing ratios of one 0.71 cylinder associated with a pressure regulator from Scott Specialty Gases. The dashed line indicates the mixing ratio of the gas in the filling tank; the solid line shows a long-term trend.





Fig. 4. The schematic of the flask sampling for a single flask, which consists of two processes: flushing, air flowing into the flask is instantaneously mixed and then flows out of the flask at the same flow rate; pressurizing, air flows into the flask with decreasing flow rate until the flask sampling is completed.





Fig. 5. The weighting function for integrating in situ measurements to compare them with the analysis result of one single flask, plotted as a function of time. The time scale is relative to a chosen time (100 s for one single flask) prior to the start of pressurizing. The weights are given in percentages. The dashed line denotes the time when the pressurizing period starts. The weighting function is calculated based on the recorded and smoothed flask pressure during flight.





Fig. 6. The schematic of the flask sampling process for the case of pair flasks, which consists of two steps: flushing and pressurizing. During the flushing, air flows into and out of the first flask at a flow rate f_0 (the air is fully mixed inside the first flask) and then flows into and out of the second flask at the same flow rate, f_0 . During the pressurizing process, air flows into the first flask at a varying flow rate f(t), but out of the first flask at the flow rate f(t)/2; air at the flow rate f(t)/2 pressurizes the second flask.











Fig. 8. An example of the performance of these weighting functions for the flight on 20 August 2008: (a) in situ measurements of CO_2 mixing ratios with flask CO_2 mixing ratios shown in blue (upstream) and green (downstream); comparison of flask data with the integrated signal of in situ continuous CO_2 measurements (b) using a constant 120-s window; (c) using the weighting functions, Eqs. (3.2) and (3.3).





Fig. 9. Comparison of in situ measurements with flask CO_2 mixing ratio measurements over Bialystok Tall Tower for 216 flasks from 22 flights between April 2008 and July 2009. Note the differences between **(a)** averaged in situ and flask CO_2 mixing ratios for blind comparison and **(b)** after correcting the insufficient drying effect for 104 flasks from 10 flights. The averaged values and standard deviations of the differences in **(a)** and **(b)** are shown in the plot in red.











Fig. 11. Time series of CO_2 mixing ratios at 300 m, 2500 m, and reference marine boundary layer (see text). A linear trend and a third-order harmonic function have been fitted to each group of these data (smoothed curves), and the dashed lines show the linear trend from the fits.





Fig. 12. Seasonal cycle of CO_2 gradients (300 m minus 2500 m); a thirdorder harmonic function is fitted to these data (the blue spline).





Fig. 13. A flight on 20 August 2008 is shown with the flight track colored by CO_2 mixing ratios: the gray lines show the projected flight tracks on the ground level and the blue bar indicates the location of the tower.





Fig. 14. Differences of mixed-layer CO_2 averages between the ascending and the descending profiles near Bialystok: (a) for the profiles made during the peak growing season; (b) for the profiles made during the non-peak growing season. The data were collected during 2008 and 2009.





Fig. A1. The fraction of the air (entering the upstream flask at time *t*) remaining in the flasks: at the time when the pressurizing period starts, t_s , the fraction of the flushing air remaining (a) in the upstream flask, $c_1(t)$ and (c) in the downstream flask; at the time when the pressurizing is complete, t_e , the fraction of the pressurizing air remaining (b) in the upstream $c'_1(t)$ and (d) in the downstream $c'_2(t)$. Note that at the time when the pressurizing period ends, the fraction of the flushing air in the upstream and the downstream flasks will be different as a result of flushing air that is moving from the upstream flask into the downstream flask.

