We thank the reviewers for taking time to provide helpful comments, recommendations and insightful questions that helped the author to improve the paper.

In the following, the issues and remarks of the reviewers are individually addressed unless they were simple typographical or technical corrections, which we simply applied. Comments of the reviewers are repeated for convenience as indented blocks. Within the provided replies, excerpts from the revised paper are marked by cursive face.

7 1 Reply to Referee 1

8 1.1 Major Remarks

Detailed presentation of mathematical methodology -duplication with pre vious work

There is quite some redundancy / repetition in the presentation of the re-11 trieval approach - Gauss-Newton iteration, setup of regularization matrix, 12 averaging kernel and gain matrix diagnostics, etc. . . - when comparing 13 this manuscript with the previous papers mentioned above, nb. the two 14 GLORIA papers. For the reader of this manuscript (including the review-15 ers) it is therefore cumbersome to identify the advances presented in the 16 current manuscript. A detailed presentation of the methodology has been 17 clearly useful in former times, when papers were difficult (or sometimes 18 almost impossible) to obtain. However, nowadays literature is mostly ac-19 cessible by just a few mouse clicks". In particular, all previous Ungermann 20 et al. papers have been published in an Open Access journal (AMT(D)) 21 and therefore are readily available. 22

As a consequence I suggest to rewrite the methodology section 2 in a significantly more compact manner, clearly indicating the differences to the previous presentation.

I agree that there is some redundancy with past papers. It is however felt that most of this repetition is necessary for two reasons: first, the interested reader should not be forced to look into the other papers to understand the current one (while she is certainly invited to); second, presentation of technical details for deriving a full set of diagnostics is helped by introducing and explaining the preceding formulae.

Still there is indeed information that is unnecessary for the purpose of this paper that 31 may be removed. The paragraph referring to Tikhony/optimal estimation was re-32 moved (6582 1.10-18) and the pragraph describing the employed regularisation (6583 33 1.17-6584 1.10) was shortened to "As compromise, the Tikhonov regularisation used 34 in this paper is chosen to approximate the precision matrix of an optimal estimation 35 covariance matrix employing the auto-regressive model to fill the covariances (e.g. 36 Steck and von Clarmann, 2001). The parametrisation used here follows closely the 37 one described by Ungermann et al. (2012) with the notable exception of the added 38

matrix for horizontal regularisation. To summarise the setup briefly, $\mathbf{L}_0 \in \mathbb{R}^{n \times n}$ 1 is a diagonal matrix, with climatological standard deviations on the diagonal. The 2 \mathbf{L}_1 matrices pose constraints on the first-order derivative in vertical and horizontal 3 direction, scaled with two quantity specific scaling factors c_q^h and c_q^v for \mathbf{L}_1^h and \mathbf{L}_1^v , 4 respectively." Some cites were also added to help the reader identify repetitions of pre-5 viously published material; e.g. the "Linearised diagnostics" section is introduced by 6 the more verbose "The diagnostics used in this work follow the linearised diagnostics 7 described by Rodgers (2000). The key point of this section is how these well-known 8 diagnostics may be derived in a memory conserving and numerically stable way re-9 quired for large-scale retrievals. It thereby expands the previous work only detailing 10 the calculation of the noise error (Ungermann et al., 2010) to the more complicated 11 estimation of systematic errors induced by background gases and uncertainties in 12 spectral line data." 13

14 2. Noise in retrieved state vector

The term noise used frequently in this manuscript to describe some properties of the retrieved profile(s) is not appropriate. Clearly the measurement (vector) is contaminated by noise, however, the retrieved profile(s) (or their discretized representation, the state vector) can have instabilities, oscillations, . . . in case of insufficient regularization.

The author does not fully agree with the reviewer comment. Clearly, an ill-posed 20 problem such as discussed here can introduce strong oscillations and other artefacts 21 by magnifying noise during the retrieval. But due to proper regularisation, the dis-22 cussed case study should be free from such artefacts. Still, even if the problem were 23 well-posed, instrument noise will reflect on the retrieved VMRs. Gaussian noise or 24 spikes in the measurements cause in a first order approximation similar structures 25 in the retrieved profiles. Plotting cross-sections of measured radiances and compar-26 ing them with retrieved trace gasses shows the striking resemblance of structures 27 including obvious artefacts. To some extent, the effect of instrument noise (Gaus-28 sian and spikes) is reduced by the smoothing properties of first-order regularisation. 29 Also, as the cross-section retrieval produces images, terminology common to describe 30 artefacts in (photographic) images seems appropriate here. 31

To distinguish this notion, the paper now uses the term "image noise" when referring to visible noise and delivers the following definition of the term: "Image noise refers here to the artefacts induced by measurement noise and similar stochastic errors in the radiances.". The image noise is already quantified in the noise error and referred by that when discussed quantitatively. Further, where appropriate the terms "measurement noise" and "noise error" are used instead of the ambiguous "noise".

1 1.2 Minor Remarks

 1. 6580.14 "This is typically accomplished by adding constraints . . . " Are there other ways of regularization?

Other regularisation methods are the (also employed) discretisation of the underlying continuous problem, the early stopping of iterative algorithms used for solving involved (linear) equation systems, or using a singular value decomposition to identify and discard small eigenvalues of the linear equation system matrix. These methods deliver robust results but are not able to fully exploit the a priori knowledge available for atmospheric retrieval problems. But they are popular in other fields.

2. 6581.04 The second sentence is incorrect, not only limb sounding inversion is illposed, nadir sounding is even worse (as correctly stated in the final section).

The given sentence does not try to make any statement with respect to the ill- or well-posedness of retrieving from nadir sounder measurements. It talks only about limb-sounders. The noted sentence is further redundant with the introduction and was removed in the revised version. The introduction is accordingly modified to: *"The retrieval of trace gases or other quantities from infrared nadir- or limb-sounder measurements is inherently an ill-posed problem, ..."*.

193.6581.06 ". . . representation of the atmospheric state x is modified . .20. until the fit . . . is deemed good enough . . . " This sounds like an21iterative procedure, which is clearly required for nonlinear problems. How-22ever, linear (small-scale) problems can be solved in just one step without23iteration.

This is indeed the case. The author sees linear problems as a sub-case of non-linear ones, as they can be treated with the same methods as the non-linear ones. In case of linearity, the iterative solver will terminate after the first iteration if proper stopping rules are in place. The following sentence should help the dissenting reader: "If the forward model is linear, a solution can be directly calculated while non-linear forward models require an iterative procedure."

- 4. 6583.19 "... insert the minimum of the cost function xf..." Rephrase!
 xf is not the minimum of the cost function, rather it is the x minimizing
 the cost function.
- This and other misuses of minimum were addressed.
- 5. 6590.18 ". . . get reduced in lockstep . . . " Please explain
- If the standard deviation of the error estimate is reduced, so is the frequency of large rel. errors in the estimate. The sentence seems to be confusing as the content should be self-evident. It was removed from the paper.

- 6. 6591.11 "This data set is rather unique . . . " — Does this refer to 1 the entire campaign data set or just the second flight on 2. March??? If 2 necessary move this sentence down or the very last sentence up. 3 It is clarified as "One of the instruments aboard was CRISTA-NF, an airborne infrared 4 limb-sounder. The data taken by CRISTA-NF in this campaign is rather unique in 5 having at the same time a high frequency of taken profiles (one profile every ≈ 15 km) 6 and a high vertical sampling ($\approx 250 \text{ m}$)." 7 6591.23 ". . . from the flight altitude down to 15 km below . . . " — This 7.8 is quite confusing. According to Ungermann et al. [2012] the scan goes 9 down to 5 km. 10 The sentence fails at communicating that the vertical coverage of the instrument 11 is 15 km. It is remedied by a simpler "Spectra are scanned from the flight altitude 12 down to ≈ 5 km in vertical steps of ≈ 250 m using a Herschel telescope with a tiltable 13 mirror." 14 8. 6592.24 Retrieval setup: it would be helpful to indicate the (total) length 15 of the measurement vector and of the state vector. 16 The sentence "In total, this gives a state vector \vec{x} with 93 870 entries and a measure-17 ment vector \vec{y} with 73 660 entries." was added. 18 6593.04 "All targets are derived between 0 km and 25 km . . . " Probably 9. 19 the lower limit is essentially the lowest tangent height!?! 20 The lower limit for "useful" values is mostly defined by the lowest tangent height. 21 Though sometimes, the signal to noise ratio further restricts the usefulness of derived 22 values as it happens for $ClONO_2$. Still, trace gas VMRs are being retrieved for all al-23 titude levels down to 0 km, whereas the lowest ones are obviously fully determined by 24 a priori information. For 1-D retrievals the difference in computational effort between 25 a lowest limit of 0 km or, e.g. 5 km is completely negligible. Having a large safety 26 margin prevents problems stemming from limb-rays passing unexpectedly below the 27 lowest retrieval limit. For cross-section retrievals, the wasted computational effort is 28 noticeable but still not worrisome. Adding or removing the lowest altitudes does not 29 meaningfully affect the time required to calculate the Jacobian matrices. The time 30 to solve the linear equation system is affected by the superfluous entries, but this 31 time is dominated by a factor of three to ten by the time to compute the Jacobians. 32 However, it is planned to use a more sophisticated choice for the lower bound de-33 pending on the lowest measurement for cross-section and tomographic retrievals in 34 the future. 35 10. According to Ungermann et al. [2012] the retrieval grid above 30km has a 36 spacing of 2 km? 37
- The text was corrected to "*The retrieval grid sampling distance is 250* m *below 20* km, *1* km *between 20* km *and 30* km, *and 2* km *above.*"

6596.18 HITRAN11: the HITRAN 2008 database [Rothman et al., 2009] 11. 1 including recent updates? 2 The reviewer assumed correctly. A reference to Rothman et al. (2009) was added 3 and the "11" was removed. 4 6600.25 ". . . being the retrieval being nonlinear)." — Isn't the retrieval 12.5 nonlinear anyway??? 6 The following should express the intended meaning clearer: "This corresponds to 7 a maximum likelihood estimator and is mathematically similar to a linear cross-8 section retrieval linearised at the state given by the assembly of the 1-D solutions." 9

¹⁰ 1.3 Technical Remarks (typos etc.)

11 1. 6584.13 Move opening parenthesis to front of citation

I do not see how to apply this comment. The given style of cite "by Rodgers (2000)."
is consistent with the AMT style guides with respect to citing.

¹⁴ 2. Figs. 2, 3, 4, 5, 11 Title of the plots "retrieval results" ???

The rather redundant titles of "retrieval result" and "horizontal resolution" were replaced with titles describing the regularisation strength of the depicted retrieval.

¹⁷ 2 Reply to Referee 2

¹⁸ 2.1 Specific Comments

191.Page 2 line 25: Points out that filaments of a lesser extent than the mea-20sured vertical resolution are not resolvable, but in the context implies that21this algorithm could do so. Surely if the measurement density is lower than22the atmospheric feature then that information is lost?

The paper notes that the vertical resolution shall be improved compared to conventional techniques. In either case the lower limit for the vertical resolution is given by the vertical sampling or the measurement density. Due to regularisation, the vertical resolution is often noticeably worse than the vertical sampling or the measurement noise makes it difficult to identify faint structures. To clarify this, the sentence "*Obviously, the lower limit for the improvement is given by the vertical sampling, which needs to be fine enough to sample structures of interest.*" was added.

 Page 9 line 16: Here a part of the elaboration of the algorithm is omitted due to the complexity of the notation. In the other parts of the manuscript the author is very explicit in describing the mathematics of the algorithm.
 A choice should be made if a full formalism is desired to allow third parties to recreate every single step of the work, or if only novel steps need to be

1 2		described. In the first case the missing steps should be included; in the second case the author could simplify the whole of section 2 and refer to the
3		literature for well established aspects of the optimal estimation algorithm.
4		A mixed approach was followed to address this comment. Material repeated from
5		previous publications was reduced to the necessary and text was added that helps
6		the reader to identify novel material (see Major Remark 1 of Reviewer $#1$ above).
7		In addition, the missing details of the algorithms were supplanted in an appendix for
8		completeness' sake.
9 10	3.	Page 13 line 9: Would this study have worked for another flight date as well? Is some date better suited than others? If yes which ones, and why.
11		The figure is representative for any kind of study. I added the sentence "The qual-
12		ity of the estimates follows the expected theoretical forecast, which makes a separate
13		calculation superfluous." to highlight the connection between the generally valid
14		theoretical forecast and the practical example.
15	4.	Page 14 line 6: A tangent point uncertainty of 100m is calculated from
16		a given pointing angle uncertainty, but due to the limb-viewing geometry
17		this number will vary as a function of the current scan angle. What is the
18		absolute tangent altitude at which a 0.02 deg pointing error results in a
19		100m tangent point error?
20		The value was given as a rough estimate. This estimate was restated more precisely
21		as "which corresponds to an uncertainty in the tangent point altitude of ≈ 125 m
22		vertically 10 km below flight level.".
23	5.	Page 15 line 20 (also, page 20 line 23): "The choice of CFC-11 is disadvan-
24		tageous for cross-section retrievals." Why chose this gas then in the first
25		place?
26		To demonstrate a positive effect even under adverse circumstances. Any new tech-
27		nique is beneficial for carefully controlled and selected use cases. We make a point by
28		using our most recently published data set and select from that the least and most
29		benefiting trace gases.
30		Further, having two data points (one gas with a strong signature and one gas with
31		a weak signature) allows thereby (to a certain extent) to extrapolate the expected
32		gains when applying the presented technique to other instruments.
33		We added "Thus, the two trace gases represent a worst case and a best case scenario
34		for the proposed algorithm and thereby allow a better quantification of expected benefits
35		for other scenarios."
36	6.	Page 16 line 3: Is there any evidence to back this up?
37		Typical error diagnostics as presented in this paper allow for a quantification of

³⁷ Typical error diagnostics as presented in this paper allow for a quantification of ³⁸ (expected) systematic errors. Obviously, many assumptions have to enter into these calculations. An example for such an error diagnostic is given in Fig. 6. Comparing
 the magnitude of the combined systematic errors (that is all error terms except the
 noise one) with the retrieved volume mixing ratios shows that for the primary targets,
 the systematic error is mostly dominated by spectral line uncertainty, whereas the
 secondary targets are also strongly affected by uncertainty in background gases or
 have a total error (much) larger than the retrieved volume mixing ration.

⁷ If such calculations count as hard evidence lies beyond the scope of this paper.

⁸ However, during the RECONCILE campaign, comparison against other instruments ⁹ for the primary retrieval targets was feasible, which asserted the validity of the re-¹⁰ trieved volume mixing ratios and the associated error bars (actually, the errors seem ¹¹ to have been overestimated generally). The secondary targets could not be validated ¹² in this way, which is certainly part of the reason why they are seen as only secondary.

7. Page 16 line 19: Based on what data sets is 200 the typical scale difference
between horizontal and vertical structures in the atmosphere?

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This value was derived from informal communication and should not be taken too seriously as it serves only as a starting point. We restate as "A natural starting point for the horizontal regularisation would be an approximate scale difference between vertical and horizontal length for large meso- or synoptic-scale structures in the atmosphere, i.e. ≈ 200 .". However, according to the current limited experience with the method, perceived best values tend to lie between 100 and 400.

8. Page 16 line 24 (also, page 20 line 11): "not very pleasing to the eye..."
This is not a very scientific statement. Could this be further quantified/classified?

Sect. 3.5 gives a quantitative discussion. While several "optimal" criteria exist to derive the "right" regularisation strength, these often just try to replicate the "trained eye" of experts. As such, the author holds the visual impression of line and crosssections plots in great esteem. The human eye is a great instrument to part order and chaos. However, to help the doubting reader, a reference to the quantitative noise level discussion was added: "... but it is visually already much more pleasing than the baseline setup (see Sect. 3.5 for a quantitative discussion)."

- 9. Page 17 line 6: The author mention that they have left out a plot of
 the stronger HNO3 distribution, which they claim confirms the structures
 they managed to extract from the weaker gases thanks to the improved
 algorithm. This plot would be a strong evidence of their conclusions.
- We do not believe that an HNO₃ plot needs to be included into the paper, as it has been published in Ungermann et al. (2012). As the published plot uses contours, we repeat it here in the same style used for the plots in the paper under discussion:



1



We modify the original paper to "Several features even look better, for example, the inclined outflow of increased ClONO₂ at 11:50 UTC at 12 km is now consistent over all neighbouring profiles." to allow a better identification of the structure related to $(11:45 \mapsto 11:50$ and addition of "inclined").

Please note further the good correspondence of the horizontal filaments at 11:00 UTC
 between the baseline HNO₃ and the reduced vert. reg. strength ClONO₂ plot.

17 10. The scenario with factor-20 000 regularisation strength seems a bit extreme.
18 Its results in this case study indicate that this would not be a viable choice
19 for a real application. Is it worthwhile including it in the case study?

This particular regularisation strength is extreme by choice as it serves as a counterpoint to the baseline setup with no horizontal regularisation and thereby as an example of what might be too much. However, a main point here is that the retrieved VMRs are far from horizontally homogeneous (especially for CFC-11) despite the chosen strength, so Fig. 5 deserves its place.

- Page 26 line 15: If this technique can indeed improve the retrieval of instrument parameters this would be a major strengths in its books, but this
 is only given as a side note here. It seems worthwhile to expand on this
 claim.
- For the CRISTA-NF limb-sounder, only the single instrument parameter "offset" is being retrieved. When retrieving individual profiles, the retrieved offset varies quite a bit between the profiles, which is compensated for by the retrieved extinction.

Regularising the extinction gives already a rather smooth and stable offset parameter.
In this case the 1-D retrieval seems to have difficulties in determining both extinction
and offset from the measurements. In practise however, the retrieved trace gas volume
mixing ratios are very similar in either case so that the "better" offset and extinction
do not really benefit the primary targets.

However, we plan to investigate the capabilities of this technique for the newer GLO RIA instrument with its more complicated 2-D detector.

12. It's somewhat unclear how much this analysis is specifically suited to the 8 instrument under test (i.e. CRISTA-NF), and how much it would ben-9 efit other techniques. The original premise of the study is that due to 10 the high sampling rate of CRISTA the individual scans are horizontally 11 correlated, a fact which is exploited with this retrieval technique. How-12 ever, other limb-sounding instruments have lower sampling rates. I.e. just 13 looking at instruments on the same air-borne platform, the other infra-red 14 limb-sounder MIPAS-Str takes a slightly longer time to complete a full at-15 mospheric scan, and the microwave instrument MARSCHALS even takes a 16 significantly longer time to do so. We guess at one point the benefit of this 17 approach becomes marginal, but it's not quite clear what this threshold 18 is. On a similar note, the application of this techniques to future air-borne 19 or satellite missions is not completely clear. The GLORIA-AB infra-red 20 limb-imager is using a truly tomographic scanning mode, so 'neighboring' 21 profiles are directly correlated, not just indirectly. The satellite missions 22 will mostly be forward or rearward looking (i.e. PREMIER), so a directly 23 tomographic retrieval approach might be more applicable in these cases. 24 The author mentions that for pushbroom imagers the retrieval would be 25 split up in swaths and each, in which case we presume that each swath 26 would be subject to a tomographic retrieval, and that horizontal correla-27 tion could then be used to improve the 3D fields. We believe to understand 28 that the technique described here could be used in a single step to retrieve 29 3D datasets, but this is only mentioned in a side note and it's not quite 30 clear that this indeed the case, nor what additional steps would be neces-31 sary to implement such an algorithm to a full 3D scenario, as compared 32 to simpler example case of this study. Overall we perceive a certain am-33 biguity as to whether this is a paper documenting the next stage in the 34 analysis of CRISTA-NF data, on which it clearly delivers, or if it's meant 35 to be a general paper on a new data processing algorithm, in which case 36 more evidence to underline the relevance to other measurement techniques 37 would be welcome. We also missed a statement whether the analysis of 38 additional campaign data of CRISTA-NF is planned in the near future. 39

Obviously, the algorithm is currently being used for our retrievals for CRISTA-NF
 and GLORIA. One paper regarding CRISTA-NF data acquired during the AMMA

- campaign in 2006 is in preparation and should shortly appear in ACPD. This does not preclude it from being applied to other instruments, even though the author cannot focus his attention on those use cases. The intent of the paper is however to provide a general description of the algorithm applicable to all kind of instruments. The paper includes one specific use case to demonstrate that it is working and to analyse its benefits and drawbacks.
- Existing instruments such as MARSHALS measures probably indeed too slowly to
 benefit from the technique, whereas MIPAS-STR might have a sufficient amount
 of measurements. However, newly built instruments in either frequency range will
 almost certainly acquire profiles faster and will therefore be able to benefit from this
 technique.
- With respect to nadir satellite instruments, current sounders such as AIRS or IASI should be able to benefit from this technique, as the amount of taken profiles is comparable. The discussed principle is directly applicable with either a 2-D or even 3-D retrieval. A dedicated case study for nadir sounders would justify its own paper. Due to the more ill-posed nadir problem, one cannot simply transfer the results of the presented case study.
- ¹⁸ With respect to PREMIER, the reviewer grasped the concept correctly.
- Obviously, there should not be doubt with respect to these topics in the conclusion. The discussion on applicability to other instruments was therefore expanded to:
- Using cross-section retrievals, it is possible to produce a better representation of 21 the true atmospheric state by exploiting the high measurement density of modern 22 instruments and the self-similarity of the atmosphere. The better reproduction of 23 thin vertical layers is important for the analysis of mixing processes in the upper 24 troposphere/lower stratosphere. Especially for trace gases with weak signature, the 25 technique reduces the image noise significantly without noticeable degradation of the 26 horizontal resolution. The algorithm is therefore currently used to process further 27 CRISTA-NF data (Ungermann et al., 2012b) and initial (non-tomographic) mea-28 surements by GLORIA (Gimballed Limb Observer for Radiance Imaging of the At-29 mosphere; see Ungermann et al., 2010). This technique might also be used to more 30 reliably derive constant and slowly varying instrument parameters, which cannot be 31 determined from pre- or post flight calibration. But the technique should also be ap-32 plicable to older airborne sounders with a more sparse sampling such as MIPAS-STR 33 (e.g. Woiwode et al., 2012), albeit with less resulting image enhancements. 34
- In contrast to the title of this paper, which was chosen mostly due to the discussed use-case, it is straightforward to extend the presented technique to retrievals for current satellite-borne nadir-sounders, as these instruments also measure closely spaced profiles (e.g. both the Atmospheric InfraRed Sounder (Aumann et al., 2003) and the Infrared Atmospheric Sounding Interferometer (Clerbaux et al., 2009) have a (sub)pixel size of 12 to 13.5 km; the operational retrievals for both instruments combine sub-pixels to reduce measurement noise, which could be achieved with less cost

of horizontal resolution with the proposed algorithm). As the viewing geometry is 1 different, the technique needs to be slightly adapted. Instead of cross-sections, 3-D 2 cubes would be retrieved with added horizontal regularisation in both along-flightpath 3 and across-flightpath direction. This only changes the state vector representation and 4 the setup of the regularisation matrix. While the resulting problem size would be 5 noticeably larger than in the presented cross-section retrieval. it is not larger than to-6 mographic problems already treated by Ungermann et al. (2011). The technique might 7 be even more beneficial when applied to nadir-sounders due to the greater ill-posedness 8 of the retrieval compared to limb-sounder retrievals. Examining and quantifying this 9 in detail deserves further study. 10

It is straightforward to extend the presented technique also to proposed near-future 11 satellite limb-imagers (Riese et al., 2005; ESA, 2012). Such a rearward-looking in-12 strument uses a 2-D detector to acquire multiple profiles simultaneously. Due to the 13 high measurement speed, consecutive images overlap in the sense that they measure 14 largely the same airmass. Assembling the measured profiles into several 2-D swaths 15 parallel to the flight-path allows the use of 2-D tomographic retrieval techniques (Car-16 lotti et al., 2001; Ungermann et al., 2010a, e.g.) to achieve an excellent resolution in 17 all three dimensions. The proposed technique is capable of evaluating all 2-D swaths 18 together in a single 3-D tomographic retrieval. By exploiting the similarity between 19 neighbouring swaths, the described technique would stabilise the inherently more ill-20 posed tomographic retrieval problem and reduce the image noise level while possibly 21 also improving the resolution. This might enhance the scientific capabilities of the 22 limb-imager, for example with respect to gravity wave detection (see Preusse et al., 23 2009). 24

²⁵ 2.2 Technical Corrections

1. Page 24 lines 4-6: Whole sentence is unclear, please rephrase.

The section was rephrased as *However*, a closer analysed reveals that the matrices 27 being multiplied and inverted in Eq. (15) are not too well conditioned to begin with 28 (about $\approx 10^5$ for the summed matrices after symmetrically scaling the diagonal to 1) 29 and both matrix-matrix multiplication and matrix-inversion are rather sensitive to 30 high condition numbers: for the given matrices, the combination of the squaring 31 and inversion in Eq. (15) introduces sufficient error to effectively remove ≈ 33 bit 32 of information, which is more than is usually employed for storing the covariance 33 matrices. 34

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