

This discussion paper is/has been under review for the journal Atmospheric Measurement Techniques (AMT). Please refer to the corresponding final paper in AMT if available.

Stack emission monitoring using non-dispersive infrared with optimized nonlinear absorption cross-interference correction algorithm

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Received: 27 November 2012 – Accepted: 29 January 2013 – Published: 21 February 2013

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Published by Copernicus Publications on behalf of the European Geosciences Union.

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Abstract

In this paper, we present an optimized analysis algorithm for non-dispersive infrared (NDIR) to monitor stack emissions. The newly developed analysis algorithm simultaneously compensates for nonlinear absorption and cross-interference between different gases. We present a mathematical derivation for the measurement error caused by variations in interference coefficients when nonlinear absorption occurs. The optimized algorithm is derived from a classical one and uses interference functions to quantify cross-interference. The interference functions vary proportionally with the nonlinear absorption. Thus, interference coefficients among different gases can be modeled by the interference functions whether gases are characterized by linear or nonlinear absorption. In this study, the simultaneous analysis of two components (CO₂ and CO) serves as an example for the validation of the optimized algorithm. The interference functions in this case can be obtained by least-squares fitting with three-order polynomials. Experiments show that the results of cross-interference correction are improved significantly by utilizing fitted interference functions when nonlinear absorptions occur. The dynamic measurement ranges of CO₂ and CO are improved by about a factor of 1.8 and 3.5, respectively. A commercial NDIR multi-gas analyzer with high accuracy was used to validate the CO and CO₂ measurements derived from the NDIR analyzer prototype in which the new cross-interference correction algorithm was embedded. Both measurements well agreed.

1 Introduction

In the infrared wavelength band between 2 and 10 μm, many gases exhibit strong absorption and interference with each other (Liu et al., 2011; Gary, 2002; Hikmat et al., 2009; Mauri et al., 2001). The accuracy and sensitivity of non-dispersive infrared (NDIR) measurement techniques are strongly influenced by cross-influences among different gases. Thus, cross-interference correction is necessary (Sayed et al., 2010;

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Bingham and Burton, 1984; Tyson et al., 1984; Lopez and Frutos, 1993). Most NDIR multi-gas analyzers use the look-up table, a matrix consisting of channel-to-channel interference constants, to correct cross-interference (Herget et al., 1976; Jong et al., 2010; Dirk et al., 2009; Harold et al., 1993). However, the way of acquiring interference constants is different. Dirk et al. (2009) assumed that the total absorption signal measured at one filter channel is the sum of the absorption of each individual gas. Thus, the interference constants of different filter channels can be measured by filling the sample cell with different nominal gases (Dirk et al., 2009). On the contrary, Harold et al. (1993) previously calculated the absorption coefficients of all gases at different filter channels by the line-by-line (LBL) calculation algorithm (Harold et al., 1993). The channel-to-channel interference constants can then be obtained through the absorption coefficients of all channels being divided by the intended one (Harold et al., 1993; Martin and Michael, 1999; Sparks, 1997). The models MIR 9000, manufactured by Environnement SA, and 60i, manufactured by Thermo Fisher Scientific, can simultaneously measure 11 and 5 gases, respectively, and both use Dirk's technique to acquire interference constants (Environnement SA; Thermo Fisher Scientific). However, NDIR analyzers, such as model L-7500 and L-7200 (both analyzers are manufactured by LiCor and are capable of simultaneous carbon dioxide and water vapor flux analysis in ambient air), use Harold's method to acquire the interference constant of water vapor to carbon dioxide (LiCor).

Within a certain concentration range, an NDIR analyzer has good linearity, and the Lambert–Beer law can be simplified as a linear equation. The cross-interference can be corrected very effectively by just using the interference constants (Dirk et al., 2009; Heusinkveld et al., 2008). In this case, each gas can be measured with high accuracy. For instance, the accuracy of model 60i and MIR 9000 for different gases is $< 2\%$, and that of L-7200 and L-7500 for H_2O and CO_2 are $< 1\%$ and $< 2\%$, respectively (accuracy estimation provided by the manufacturers). However, a specified NDIR analyzer, which has a constant optical path length, exhibits nonlinear absorption (i.e., measurement is no longer linear to the absorption) if gas concentrations are too high (Andre

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et al., 1985). In this case, the channel-to-channel interference coefficient is no longer a constant. If cross-interference is corrected by using a constant factor, correction error increases and measurement accuracy declines. Furthermore, such kind of measurement errors cannot be corrected through zero or span calibrations (Mark et al., 1983).

In fact, no matter which technique of interference constant acquisition is used, using only a constant factor to quantify gas-to-gas interference is less than optimal, feasible only if the analyzer has excellent linearity for all gases. However, the linear region restricts the dynamic range of a system. By using two or more filter channels to analyze one gas, the conflict between linearity and dynamic range can be solved to some extent. However, this approach significantly increases the cost of analyzer production and difficulty for data processing.

In this paper, the cross-interference coefficients are replaced by polynomial functions when nonlinear absorption exists. Thus, the dynamic measurement range of an NDIR analyzer can be expanded by correcting the cross-interference and nonlinear absorption. In this study, we present a detailed description of the optimized algorithm. Laboratory and field experiments were performed to test the algorithm. The measurement results were compared to the results measured by a commercial instrument with high accuracy.

2 Classical algorithm and error analysis

For a classical NDIR analyzer, within a restricted concentration range, measurement is nearly linear to the absorption. Cross-interference can be corrected by setting up a series of simultaneous equations as follows (Bingham and Burton, 1984; Dirk et al.,

2009; Harold et al., 1993).

$$\begin{aligned}
 A_{\text{total}}^1 &= \ln \left(\frac{I_0^1 / I_0^{\text{ref}}}{I_s^1 / I_s^{\text{ref}}} \right) = k_{11}A_1 + k_{12}A_2 + k_{13}A_3 + \dots + k_{1n}A_n, \\
 A_{\text{total}}^2 &= \ln \left(\frac{I_0^2 / I_0^{\text{ref}}}{I_s^2 / I_s^{\text{ref}}} \right) = k_{21}A_1 + k_{22}A_2 + k_{23}A_3 + \dots + k_{2n}A_n, \\
 &\dots\dots\dots, \\
 A_{\text{total}}^n &= \ln \left(\frac{I_0^n / I_0^{\text{ref}}}{I_s^n / I_s^{\text{ref}}} \right) = k_{n1}A_1 + k_{n2}A_2 + k_{n3}A_3 + \dots + k_{nn}A_n.
 \end{aligned} \tag{1}$$

where A_{total}^i represents the total absorbance of channel # i , I_0^i and I_s^i represent incident and emergent intensity, respectively at channel # i , I_0^{ref} and I_s^{ref} represent incident and emergent intensity, respectively, at the reference filter channel, all of which are measured by a detector. The reference channel is used to adjust any additional cause of attenuation: scattering by dust, the effect of impurities deposited on instrument windows, or any uncontrolled variation of source spectral luminance because of ageing or voltage fluctuations. The interference constant of gas j to gas i is denoted as k_{ij} . A_j represents the pure absorbance of gas i . By solving Eq. (1), the pure absorbance of each gas can be obtained. The pure absorbance can then be used for concentration retrieval with calibration curves. Here, $i, j = 1 \sim n$ and $k_{i=j} = 1$; that is, gas has zero interference to itself.

By way of a non-limiting example, assume that two gases are used for measurement and that they interfere with each other. The two gases are denoted as i and j . Assume that filter channels # i and # j , with bandwidths of Δ_i and Δ_j , respectively, are designed to measure gas i and gas j , respectively. The absorption coefficients of gas i within Δ_i and Δ_j are α_i and β_i , respectively, and those of gas j within Δ_i and Δ_j are α_j and β_j , respectively. α_i , β_i , α_j , and β_j are calculated by LBL integration of the line

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strengths provided by the HITRAN database over the relevant wavelength range (see Sect. 1) (Sparks, 1997; Rothman et al., 2005, 2009). If the absorption is linear to the concentration, the calibration curves of gas i and j and the interference coefficient of gas i to jk_{ji} and gas j to ik_{ij} can be written as.

$$C_i = \frac{1}{\alpha_i L} \times A_i; \quad C_j = \frac{1}{\beta_j L} \times A_j \quad (2)$$

$$k_{ji} = \frac{\beta_i}{\alpha_i}; \quad k_{ij} = \frac{\alpha_j}{\beta_j}$$

Here, C_i and C_j represent the concentrations of gas i and j , respectively. L is the optical-path length. α_i , β_i , α_j , β_j , k_{ji} , k_{ij} , and L are known constants for a specified NDIR multi-gas analyzer. Thus, regardless of the proportions of the gas mixture of gas i and j , the total absorbance of channels # i and # j can always be expressed as a linear superposition of the pure absorbance of gas i and j , respectively:

$$A_{\text{total}}^i = \ln \left(\frac{I_0^i / I_0^{\text{ref}}}{I_s^i / I_s^{\text{ref}}} \right) = A_i + \frac{\alpha_j}{\beta_j} A_j \quad (3)$$

$$A_{\text{total}}^j = \ln \left(\frac{I_0^j / I_0^{\text{ref}}}{I_s^j / I_s^{\text{ref}}} \right) = \frac{\beta_i}{\alpha_i} A_i + A_j$$

By solving Eq. (3), the absorbance of A_i and A_j can be obtained. The concentrations of gas i and j can be retrieved by the calibration curves in Eq. (2) with high accuracy. Thus, in theory, the cross-interference is completely corrected. However, if gas i and/or j concentration lies beyond a restricted range, nonlinear absorption occurs, and measurement accuracy declines because correction error increases. We assume that the calibration curves of gas i and j are transformed from linear curves to nonlinear functions, represented as $C_i = F(A_i)$ and $C_j = G(A_j)$, respectively. The interference coefficients k_{ji} and k_{ij} are transformed into K_{ji}' and K_{ij}' , respectively. In this case, the total

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absorbance of channels #*i* and #*j* is expressed as:

$$A_{\text{total}}^i = \ln \left(\frac{I_0^i / I_0^{\text{ref}}}{I_s^i / I_s^{\text{ref}}} \right) = F^{-1}(C_i) + k'_{ij} G^{-1}(C_j) \quad (4)$$

$$A_{\text{total}}^j = \ln \left(\frac{I_0^j / I_0^{\text{ref}}}{I_s^j / I_s^{\text{ref}}} \right) = k'_{ji} F^{-1}(C_i) + G^{-1}(C_j)$$

Here, $F^{-1}(C_i)$ and $G^{-1}(C_j)$ are the inverse functions of $F(A_i)$ and $G(A_j)$, respectively. By solving Eqs. (3) and (4), A_i , A_j , $F^{-1}(C_i)$, and $G^{-1}(C_j)$ are expressed as:

$$A_i = \frac{\alpha_i \alpha_j \ln \left(\frac{I_0^j / I_0^{\text{ref}}}{I_s^j / I_s^{\text{ref}}} \right) - \beta_j \alpha_i \ln \left(\frac{I_0^i / I_0^{\text{ref}}}{I_s^i / I_s^{\text{ref}}} \right)}{\alpha_j \beta_i - \alpha_i \beta_j} \quad A_j = \frac{\beta_i \beta_j \ln \left(\frac{I_0^i / I_0^{\text{ref}}}{I_s^i / I_s^{\text{ref}}} \right) - \beta_j \alpha_i \ln \left(\frac{I_0^j / I_0^{\text{ref}}}{I_s^j / I_s^{\text{ref}}} \right)}{\alpha_j \beta_i - \alpha_i \beta_j} \quad (5)$$

$$F^{-1}(C_i) = \frac{\ln \left(\frac{I_0^i / I_0^{\text{ref}}}{I_s^i / I_s^{\text{ref}}} \right) - k'_{ij} \ln \left(\frac{I_0^j / I_0^{\text{ref}}}{I_s^j / I_s^{\text{ref}}} \right)}{1 - k'_{ij} k'_{ji}} \quad G^{-1}(C_j) = \frac{\ln \left(\frac{I_0^j / I_0^{\text{ref}}}{I_s^j / I_s^{\text{ref}}} \right) - k'_{ji} \ln \left(\frac{I_0^i / I_0^{\text{ref}}}{I_s^i / I_s^{\text{ref}}} \right)}{1 - k'_{ij} k'_{ji}} \quad (6)$$

If the interference equations are set up by using the previous interference constants, then:

$$F^{-1}(C_i) + k'_{ij} G^{-1}(C_j) = A_i + \frac{\alpha_j}{\beta_j} A_j \quad (7)$$

$$k'_{ji} F^{-1}(C_i) + G^{-1}(C_j) = \frac{\beta_i}{\alpha_i} A_i + A_j$$

The relative measurement error is defined as (Jacob and Roy, 2012; Rao et al., 1999; Derek, 1968; Marcel et al., 1990):

$$\gamma = \frac{C_{\text{measured}} - C_{\text{true}}}{C_{\text{true}}} \times 100\%, \quad (8)$$

where C_{measured} is the concentration retrieved by using the interference constants, and C_{true} is the concentration retrieved by using the actual interference coefficients. Consequently, the measurement error of gas i γ_i and j γ_j can be mathematically calculated as:

$$5 \quad \gamma_i = \frac{F \left(\frac{\alpha_i \alpha_j \ln \left(\frac{i_0^i / i_0^{\text{ref}}}{i_s^i / i_s^{\text{ref}}} \right) - \beta_j \alpha_i \ln \left(\frac{i_0^i / i_0^{\text{ref}}}{i_s^i / i_s^{\text{ref}}} \right)}{\alpha_j \beta_i - \alpha_i \beta_j} \right) - F \left(\frac{\ln \left(\frac{i_0^i / i_0^{\text{ref}}}{i_s^i / i_s^{\text{ref}}} \right) - k'_{ij} \ln \left(\frac{i_0^i / i_0^{\text{ref}}}{i_s^i / i_s^{\text{ref}}} \right)}{1 - k'_{ij} k'_{ji}} \right)}{F \left(\frac{\ln \left(\frac{i_0^i / i_0^{\text{ref}}}{i_s^i / i_s^{\text{ref}}} \right) - k'_{ij} \ln \left(\frac{i_0^i / i_0^{\text{ref}}}{i_s^i / i_s^{\text{ref}}} \right)}{1 - k'_{ij} k'_{ji}} \right)} \quad (9)$$

$$10 \quad \gamma_j = \frac{G \left(\frac{\beta_j \beta_i \ln \left(\frac{i_0^j / i_0^{\text{ref}}}{i_s^j / i_s^{\text{ref}}} \right) - \beta_j \alpha_i \ln \left(\frac{i_0^j / i_0^{\text{ref}}}{i_s^j / i_s^{\text{ref}}} \right)}{\alpha_j \beta_i - \alpha_i \beta_j} \right) - G \left(\frac{\ln \left(\frac{i_0^j / i_0^{\text{ref}}}{i_s^j / i_s^{\text{ref}}} \right) - k'_{ji} \ln \left(\frac{i_0^j / i_0^{\text{ref}}}{i_s^j / i_s^{\text{ref}}} \right)}{1 - k'_{ij} k'_{ji}} \right)}{G \left(\frac{\ln \left(\frac{i_0^j / i_0^{\text{ref}}}{i_s^j / i_s^{\text{ref}}} \right) - k'_{ji} \ln \left(\frac{i_0^j / i_0^{\text{ref}}}{i_s^j / i_s^{\text{ref}}} \right)}{1 - k'_{ij} k'_{ji}} \right)} \quad (10)$$

All parameters in Eqs. (9) and (10) are known, and the nonlinear functions $F(x)$ and $G(x)$ can be obtained by least-squares fitting using low-order polynomials (Yan et al., 2009; Komhyr et al., 1983, 1989; Bjorck, 1996; Rao et al., 1999; Derek, 1968; Marcel et al., 1990). Therefore, gases i and j have measurement errors of γ_i and γ_j because of the variations of calibration curves and interference coefficients. These variations are caused by nonlinear absorption. Both γ_i and γ_j are related to k'_{ji} and k'_{ij} . To find whether k'_{ji} and k'_{ij} are influenced by the concentrations of gas i and j , experiments are conducted several times. The results are listed in Table 1, in which four different cases can be identified. γ_i and γ_j are zero only if the absorption is linear for both gases

(i.e., case 1). However, neither γ_i nor γ_j equals zero for all other cases (i.e., cases 2, 3, and 4). This result means that the classical algorithm can correct cross-interference completely if an analyzer does not exhibit nonlinear absorption. However, once gas i and/or j have/has nonlinear absorption, the classical algorithm for cross-interference fails, producing a measurement error because of its imperfection.

3 An optimized algorithm

A modification of interference Eq. (1) can effectively correct the measurement error produced by the imperfection of the classical algorithm when the analyzer exhibits nonlinear absorption. Taking the abovementioned gases i and j as an example, an interference function rather than an interference constant is used to qualify the gas-to-gas interference, in total contrast to the classical algorithm, even though the optimized algorithm also requires zero and span calibrations.

Assume that the interference functions of gas i to j and j to i are represented as $k_{ji}(x)$ and $k_{ij}(x)$, respectively. A modification of interference Eq. (1) can be written as:

$$\begin{aligned} A_{\text{total}}^i &= \ln \left(\frac{I_0^i / I_0^{\text{ref}}}{I_s^i / I_s^{\text{ref}}} \right) = A_i + k_{ij}(A_j) \\ A_{\text{total}}^j &= \ln \left(\frac{I_0^j / I_0^{\text{ref}}}{I_s^j / I_s^{\text{ref}}} \right) = k_{ji}(A_i) + A_j \end{aligned} \quad (11)$$

The optimized interference Eq. (11) applies not only to linear absorption but also to nonlinear absorption, resulting in great improvements in the dynamic measurement range of an NDIR analyzer, because $k_{ji}(x)$ and $k_{ij}(x)$ vary with the concentrations of gas i and j , respectively. In fact, classical interference equations can also be derived from optimized ones; that is, they can be derived from each other (see Sect. 4.3 for details). Both $k_{ji}(x)$ and $k_{ij}(x)$ can also be obtained by least-squares fitting (Yan et al.,

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2009; Komhyr et al., 1983, 1989; Bjorck, 1996; Rao et al., 1999; Derek, 1968; Marcel et al., 1990), which is similar to acquisition method for calibration curves. Details of the procedure are as follows.

3.1 Interference function of gas i to j $k_{ji}(x)$

5 Gas i with various concentrations, from low to high, is pumped into a sample cell. The concentration should preferably be prepared as more than 10 different levels and evenly distributed within the entire range. The voltages measured at the $\#i$ and $\#j$ channels are in ratio against the voltages measured at the reference channel to correct for hardware instability, and are then converted to absorbance. Least-squares fitting with an
10 ideal model is adopted to treat the data array $(A_{\text{total}(h)}^i, A_{\text{total}(h)}^j)$. Thus, the interference function of gas i to j is obtained. Here, $A_{\text{total}(h)}^i$ and $A_{\text{total}(h)}^j$ are the total absorbance of channels $\#i$ and $\#j$ when gas i is pumped into the sample cell for the h -th time ($h = 1 \sim n$).

3.2 Interference function of gas j to i $k_{ij}(x)$

15 Similar to $k_{ji}(x)$, $k_{ij}(x)$ is obtained by pumping gas j into the sample cell. The result data array is $(A_{\text{total}(h)}^j, A_{\text{total}(h)}^i)$.

In fact, the interference function is related to the characteristics of the filters designed for gas analysis, such as bandwidth, center wavelength, and transmission. For a specified NDIR multi-gas analyzer, the gas-to-gas interference can be estimated by using the literature absorption cross-sections. In this study, literature absorption cross-sections
20 from the HITRAN database were used (Rothman et al., 2005, 2009). If the interference constant obtained by line-by-line calculation is negligible (Harold et al., 1993; Martin and Michael, 1999; Sparks, 1997), the interference function can be set to zero. If the absorption is pronounced, a reasonable model should be selected for least-squares fitting. In principle, any kind of model, such as a polynomial, exponential, or logarithm
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function, is feasible as long as the fitting correlation coefficient R^2 is sufficiently close to 1. However, a model must not be too complex, because the more complex the interference function is, the more complicated the interference equations are to be solved. The most interesting thing is that any derivative functions can be Taylor-expanded into a power series. Thus, power series is an ideal model, which not only effectively models the nonlinear variation of interference coefficients but also facilitates the interference equations to be solved (Andre et al., 1985). In our case, a model of third-order polynomials is selected.

4 Experimental sections

4.1 Apparatuses

Figure 1 shows the structure of the NDIR multi-gas analyzer prototype used for experiments. The instrument includes an infrared (IR) light source, an optical filter wheel, a sample cell, a detector, and a data processor. The filter wheel has eight filters for the optical signal at certain wavelength bands. By using different filter combinations, the instrument can be used to measure different gases, such as SO_2 , NO_2 , CH_4 , N_2O , HC , H_2O , CO_2 , CO , NO , NO_2 , and H_2S . Detailed descriptions of this prototype can be found in Sun et al. (2011). For clarity, we take simultaneous CO_2 and CO analyses as an example in the following discussion. CO_2 and CO correspond to gases i and j mentioned in Sect. 2, respectively. Expansion to more than two gases is straightforward.

A gas distribution system used for laboratory experiments is shown in Fig. 2. Gas concentrations from 10 % to 90 % of nominal value can be obtained with a precision of $\pm 0.5\%$ by varying the voltages of the two mass flow meters. For the analysis presented here, measurement error caused by the gas distribution system was neglected.

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4.2 Laboratory experiments and discussions

Figures 3 and 4 show calibration curves and measurement linearity fitting results for CO₂ and CO, respectively. A three-order polynomial was used to fit the relation between gas concentration and absorbance. The parameters of the fitted polynomial and corresponding estimated errors are shown in the figures. The correlation coefficient of polynomial fit for CO₂ and CO measurements are 0.99991 and 0.99998, respectively. The polynomials of the calibration curves of CO₂ and CO are expressed as Eqs. (12) and (13), respectively (only fitting correlation coefficients are shown for linear fittings, because the actual calibration curves used in this paper are three-order polynomials; fitting parameters for linear fittings are not absolutely necessary).

$$C(\text{CO}_2) = (0.040622 \pm 0.007012) + (111.70135 \pm 6.04867) \times (A_i) + (477.13268 \pm 123.79041) \times (A_i)^2 + (215.01234 \pm 63.20941) \times (A_i)^3 \quad (12)$$

$$C(\text{CO}) = (2.29864 \pm 0.446215) + (268.19825 \pm 15.03105) \times (A_i) + (11936.11652 \pm 848.8231) \times (A_i)^2 + (-8850.98731 \pm 1364.9827) \times (A_i)^3 \quad (13)$$

According to Figs. 3 and 4, nonlinear absorptions exist for CO₂ and CO (fitting correlation coefficients for three-order polynomial models are significantly higher than those of the linear models). For effective modeling of nonlinear absorption when the NDIR technique is used for simultaneous multi-gas analyses, a typical power series model is used. Generally, the higher the order, the more complex the calibration curve and the higher the modeling precision (i.e., the more R^2 is sufficiently close to 1). Tan et al. (2008) used two three-order polynomials to calibrate both CO₂ and CH₄ channels in their mini NDIR analyzer (Tan et al., 2008). However, the NDIR analyzer L-7500 manufactured by Li-Cor uses a five-order polynomial to calibrate CO₂ but a three-order polynomial to calibrate H₂O (LiCor). In this study, both CO₂ and CO are calibrated by using a three-order polynomial, a reasonable choice because of sufficiently high fitting correlation coefficients.

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Figures 5 and 6 show the fitted interference functions (details about fitting procedures are shown in Sect. 3). Fitting values, estimated errors, and fitting correlation coefficients are clearly visible in both figures. More precisely, Fig. 5 shows the fitting results for the interference function of CO₂ to CO, and Fig. 6 shows those of CO to CO₂. The fitted interference functions of CO₂ to CO and CO to CO₂ are expressed as Eqs. (14) and (15), respectively.

$$k_{ji}(A_j) = (7.89297 \times 10^{-4} \pm 2.80151 \times 10^{-5}) + (0.23715 \pm 0.00168) \times (A_j) + (-0.02213 \pm 0.002665) \times (A_j)^2 + (1.63133 \pm 0.12229) \times (A_j)^3 \quad (14)$$

$$k_{ji}(A_j) = (-0.00491 \pm 3.86852 \times 10^{-4}) + (0.53734 \pm 0.00818) \times (A_j) + (-0.02726 \pm 0.004046) \times (A_j)^2 + (0.91542 \pm 0.04961) \times (A_j)^3 \quad (15)$$

Figures 5 and 6 show a linear relation between the absorbance of CO and CO₂ for concentrations below a critical threshold, where the interference coefficients only have invisible variations. Thus, the interference coefficient within this measurement range can be accurately approximated as a constant. However, if the concentration exceeds this range, the actual interference coefficient is no longer linear. The difference between the actual interference coefficient and the linearly approximated interference coefficient increases with the concentration, which is in good agreement with Table 1. The actual interference coefficients in Figs. 5 and 6 are calculated by A_h^j/A_h^i and A_h^i/A_h^j , respectively.

In fact, the deviation point is around 0.1 (~ 17% CO₂ volume mixture ratio (VMR)) for Fig. 5 and around 0.3 (~ 850 ppmv CO VMR) for Fig. 6. Figure 5 shows that, if CO₂ concentration is within 17%, the interference to CO can be effectively modeled by both the fitted interference function and $y = 0.2535x$. However, if CO₂ concentration exceeds 17%, a polynomial model works much better than a linear model and results in lower error. Similarly, as shown in Fig. 6, if CO concentration is within 850 ppmv, the interference to CO₂ can be effectively modeled by a linear or polynomial model.

Once CO concentration exceeds 850 ppmv, only the fitted interference function can effectively model such interference, and $y = 0.5525x$ results in great error.

Similar to those of calibration curve fittings, models used for interference function fittings are also three-order polynomials. Models are feasible because the fitting correlation coefficient R^2 is sufficiently close to 1 (0.99969 for Fig. 5 and 0.99986 for Fig. 6).

In this section, the measurement errors of different cross-interference correction algorithms are compared. Figures 7 and 8 are comparisons of the interference corrections of CO₂ to CO and CO to CO₂, respectively. Figure 7a shows the CO concentrations calculated by using the CO calibration curve after CO₂ interferences are corrected. We take 100 ppmv CO as an example. The influence of different concentrations of CO₂ on CO measurement errors calculated after interference correction is clearly visible in Fig. 7b. According to Fig. 7, CO₂ interference can be effectively corrected by both algorithms if CO₂ concentration is lower than 17%. Measurement errors calculated after interference correction by both algorithms are less than 1%. However, interference correction results with the fitted interference function are obviously better than those with the interference constant if CO₂ concentration exceeds 17%. In this case, the CO measurement errors for interference correction using the fitted interference function change by less than 1%, whereas those for interference correction using a constant factor increase with increasing CO₂ concentration. Similar to Fig. 7, Fig. 8 shows the CO₂ concentration deviations between measurement results and the true values (in this case, different concentrations of CO are sequentially pumped into the sample cell for analysis, and the actual CO₂ concentration should be zero because no CO₂ is present). Figure 8a shows CO₂ concentrations calculated by using the CO₂ calibration curve after CO interference is corrected. Figure 8b shows the influence of different concentrations of CO on CO₂ measurement errors, for which 25% CO₂ is taken as an example. According to Fig. 8, CO interference can be corrected by both algorithms if CO concentration is within 850 ppmv. Measurement errors calculated after interference is corrected by both algorithms are less than 1.5%. However, interference correction results with a polynomial interference function are obviously better

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than those with a constant factor when CO concentration exceeds 850 ppmv. The CO₂ measurement errors for interference correction using the fitted interference function stay almost the same (still less than 1.5%), whereas those for interference correction using a constant factor increase with a CO concentration increase. In fact, the upper measurement range of this analyzer prototype for CO₂ and CO is only 17% and 850 ppmv, respectively, if cross-interference is corrected by a constant factor. However, if the optimized correction algorithm is used, upper measurement ranges are extended to 31% and 3000 ppmv for CO₂ and CO measurement, respectively. Dynamic ranges for CO₂ and CO are improved by a factor of 1.8 and 3.5, respectively.

According to Figs. 7 and 8, the influence of CO to CO₂ measurement is larger than the influence of CO₂ to CO measurement. Figure 8 shows that the measurement error of CO₂ can exceed 100% if cross-interference is corrected by using a constant factor when CO concentration exceeds 1000 ppmv. For example, CO₂ measurement error is up to about 600% when CO concentration is ~2700 ppmv. In this case, the measurement results are totally unreliable, possibly because the NDIR multi-gas analyzer prototype used in this experiment is designed for continuous emissions monitoring systems installed at emission sources, such as power plants and incinerators. CO₂ concentrations emitted by these facilities are extremely high. Thus, a relatively weaker absorption waveband of 4.84 μm (rather than 4.30 μm) is selected. This wavelength band has a stronger response to CO than to CO₂. Thus, the measurement accuracy of CO₂ would be severely affected if CO interference was not completely corrected.

The exact similarity between the absorbance arrays used for the two different algorithms should be noted for comparison. Figures 7 and 8 show that the measurement errors calculated after the correction of the interferences by the two algorithms have approximately the same rapid variations. These variations are currently attributed to instrument noise. Furthermore, the measurement error cannot be up to zero (as mentioned in theoretical discussion in Sect. 2) even when a better correction algorithm, i.e., interference function, is used.

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There are several possible reasons for this issue. First, the optimized algorithm can only minimize the measurement error caused by nonlinear absorption, but it cannot correct the instrumentation error caused by a detector, an electronics device noise, or any incomplete adjustments for system drift. Second, CO and CO₂ not only interfere with each other but are also interfered by other gases. The impurities in the nominal gas and N₂, such as NO, NO₂, H₂O, and others, result in errors. The CO₂ channel is especially interfered by water vapor. The high concentrations of water vapor in the atmosphere that leak into the sample cell during the cylinders conversion period also affects the experimental result. However, the effect can be corrected easily by kicking the experiment data collected in cylinders conversion period and averaging the data sevenfold. Although error sources are unavoidable, the experimental results can still fully prove the superiority of the optimized cross interference correction algorithm, which can correct cross interference well despite linear absorption or nonlinear absorption.

4.3 Comparison of the two algorithms

A conceptual comparison of the classical and optimized cross interference correction algorithm is presented in Table 2. The processing speed is also compared in addition to the characteristics deduced from the above mathematical descriptions and discussions. The classical algorithm offers a faster processing speed than the optimized algorithm because of the relatively simpler equations to be solved.

The choice of cross interference correction algorithm has to be matched ideally to the specific requirements by balancing the assets and drawbacks of the different approaches in the selection process. Three cases can be identified based on different applications.

1. Case 1: all gases (including the target gases and the interference gases) exhibit linear absorption. Both the classical and the optimized cross interference correction algorithms work well. However, the classical algorithm is used in most cases because of a relatively faster processing speed is obtained.

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2. Case 2: all gases exhibit nonlinear absorption. The optimized algorithm is generally used if all gases exhibit nonlinear absorption.
3. Case 3: a case between Case 1 and Case 2. In this case, the classical algorithm fails while the optimized one is still applied. However, the interference equations should be set up in a compromising way. More precisely, the interference of the linear absorption gas to the nonlinear absorption gas is corrected by a constant factor. However, the interference of the nonlinear absorption gas to the linear absorption gas is corrected by utilizing a fitted interference function. This method not only compensates the nonlinear absorption problem well, but also improves the processing speed. The interference equations can actually be set up as this form based on the fact that the optimized algorithm is a generalization of the classical algorithm. The classical algorithm can be derived from the optimized one if (1) all gases (including the target gases and the interference gases) exhibit linear absorption, and if (2) a linear model “ $y = kx$ ” is used to model the gas-to-gas interference during least squares fitting.

The selection of the cross interferences correction algorithm for simultaneous two gases (e.g., gas i and j mentioned in the former sections) analysis is presented in Table 3. The expansion to more than two gases is straightforward.

5 Field applications

Instruments with a high accuracy can be used to validate the optimized algorithm. In the present study, a commercial NDIR multi-gas analyzer Model 60i manufactured by Thermo Fisher Scientific, Inc. was used to validate the CO and CO₂ results measured by the NDIR analyzer prototype, in which an optimized cross interference correction algorithm was embedded. The field experiment was operated from 18 to 27 March 2012 in the Shangfeng cement plant (30.56° N, 117.48° E) located northeast of Tongling city

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(south of Hefei, Anhui province) in central China. The prototype CO and CO₂ measurements were synchronously compared with the Model 60i measurements. Both analyzers, placed in a mini house built at above 15 m height, measured the stack emission from the cement plant. The field set-up and gas pipe connection diagram are shown in Fig. 9. Both analyzers were zero and span calibrated with the same nominal gases before the experiment. The prototype had a similar structure compared with Model 60i but arranged more compactly. Both analyzers had pressure and temperature drift compensation for the measurement results to improve accuracy. The differences between the two analyzers were the optical path-length (path-length for prototype and Model 60i are ~ 12 m and ~ 8 m, respectively) and the parameters for each designed filter. Furthermore, the prototype had a relative narrow linear dynamic range but had higher sensitivity and accuracy (within the linear dynamic range) compared with Model 60i. The performance specifications comparison of the two analyzers for CO₂ and CO is listed in Table 4. Model 60i used the classical algorithm to correct the cross-interferences among the different gases, i.e., the interferences between any two gases were quantified by utilizing a constant factor. Model 60i can correct cross-interferences well because all the gases concentrations (during the whole field experiment) were within the analyzer's linear dynamic range. Thus, the five target gases (i.e., CO₂, CO, NO, NO₂, and SO₂) were retrieved with a high accuracy ($< \pm 2\%$) (Thermo Fisher Scientific, Inc.). Using Model 60i for NDIR analyzer prototype measurements validation was a reasonable choice.

Figure 9a is a photo of the stack taken from a nearby building roof, and Fig. 9b shows the diagram of the experimental set-up used in the field. The arrangements inside the mini house are visible in Fig. 9c. The gas emission samples collected from the stack were pumped into a pretreatment system with a heat-tracing pipe. Then, the samples were imported into the two analyzers with a four-port distribution chamber after being pretreated. The heat tracing pipe was heated to a temperature of 180° C, which prevented the water vapor with high concentrations from cooling into liquid water. The acidic gases, such as NO and SO₂, were prevented from dissolving into liquid water,

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resulting in the equal measurements of the gases with the stack. The pretreatment system was used to remove dust and water vapor in the emission samples. Port A of the four-port distribution chamber was a gas inlet, and all other ports (i.e., port B, C and D) were gas outlets during the operation. Port C was connected with the prototype, Port D was connected with Model 60i, and Port B was connected directly with the ambient atmosphere with a flow meter. We adjusted the sampling rate slightly until the flow meter readings outside port B was greater than zero to ensure that the flow of gas inlet port A was greater than the sum of gas outlets port C and D. The sample system blows back once an hour to prevent the dust filter from being jammed. During blow-back period, Port B became the gas inlet because port A was blocked. The samples pumped into two analyzers during this period were a mixture of emission residuals in the chamber and ambient air, which protected the pumps inside the two analyzers well. Both the prototype and Model 60i were set to save minute averaged measurements, which facilitated the outliers (measurements acquired during blowback period) removal in post data process.

There were still residual mounts of SO_2 (< 300 ppmv) and NO_x (< 200 ppmv) in the gas emission samples despite the performance of the desulfurization and denitrification before the smoke was emitted to the atmosphere (Chan et al., 2008; Terje, 1996; Zu, 2002; Ackerman and Sundquist, 2008; Bovensmann, 2010; EPER, 2004; European Commission, 2007; Evans et al., 2009; Dong et al., 2011). Furthermore, the water vapor (5000 ppmv $\sim 1.5\%$) should not be neglected despite the pretreatment of the emission samples before being pumped into the two analyzers (Sun et al., 2011). All these gases may have noticeable absorption interferences to the CO and CO_2 measurements. If not corrected, the measurement error would increase. However, all gases (CO and interfering gases H_2O , NO, NO_2 , and SO_2) lay within the linear dynamic range of the prototype apart from CO_2 (beyond 17%), which was similar to Case 3 listed in Sect. 4.3. The classical algorithm in this case was not suitable. Therefore, the optimized algorithm had to be applied. More precisely, the correction for the interference of CO_2 to other gases (mainly CO and NO) utilized the fitted interference functions.

However, the correction for the interference of other gases (mainly CO, H₂O, SO₂, and NO) to CO₂ utilized the interference constants. This method facilitated the interference equations solution without a decline in the correction effects.

In the present study, six equations were set up based on signal detected from the six filter channels by using all the interference constants or interference functions. However, only the CO and CO₂ concentrations were retrieved and compared with Model 60i measurements.

A large amount of individual measurements were obtained from 00:59 of 18 to 10:49 of 27 March 2012, wherein both prototype and Model 60i saved measurements once a minute, resulting in at least 10000 reliable measurements. Figures 10a and 11a were hour-averaged series for the CO and CO₂ mixing ratio measured by both analyzers during the whole field experiment. In both figures, the measurements acquired during blowback period were removed. Figures 10b and 11b present the difference between the CO and CO₂ concentrations measured by Model 60i and the prototype respectively. Both figures show that the Model 60i measurements were a little higher than that of the prototype (CO and CO₂ were ~5 ppmv and ~1% higher respectively). These differences were mainly attributed to calibration error, and had little to do with the cross-interferences correction result. These differences can be minimized through repeated calibration. Although there were some deviations, the two analyzers measurements exhibited approximately the same concentration trend. The CO concentration was less than 400 ppmv and was mainly concentrated in ~30 ppmv to 200 ppmv, whereas the CO₂ concentration was mainly between 12% to 18%.

Figures 12 and 13, presenting the CO and CO₂ measurement correlation coefficient R^2 respectively, show the measurement correlation between the two analyzers after the outliers (i.e., measurements acquired during blowback period) were removed. Both figures show that a regression analysis for the CO and CO₂ measurements of the two analyzers presented a great correlation coefficient, wherein the measurement correlation coefficient for CO was $R^2 = 0.98813$ and for CO₂ was $R^2 = 0.91833$. The measurement correlation of the two analyzers for CO was better than that for CO₂ because

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of the higher absorption intensity of CO compared with CO₂ ($\sim 10^{-18}$ molec cm^{-2} vs. $\sim 10^{-21}$ molec cm^{-2}). Therefore, the CO filter channel was more sensitive to optical signal attenuation than that of CO₂. The system noise with the same level had less influence on CO than on CO₂. CO₂ was also more heavily interfered by H₂O, NO, NO₂, and SO₂ than that of CO based on the spectra parameters in HITRAN database (Rothman et al., 2005, 2009). The interferences of NO, NO₂, and SO₂ to CO was negligible compared with the interference of H₂O. However, H₂O, NO, NO₂, and SO₂ had pronounced interferences to CO₂, which indicates that the interferences to CO were more easily corrected than that of CO₂. The dense “point” regions within the blue box (in both figures) represent the concentration ranges where the gases appeared with the highest frequency. The CO concentrations were mainly concentrated in between 30 ppmv to 200 ppmv, and the CO₂ concentrations were mainly concentrated in between 12 % to 18 %, which agreed with Figs. 10 and 11.

Finally, the concentration correlation analysis between CO₂ and CO measured by both analyzers was performed to study the characteristics of pollutant gases emissions in this cement plant. Figures 14 and 15 show the correlation between the CO₂ and CO measured respectively by the prototype and Model 60i. The analysis in both figures revealed that there was a certain negative correlation between the concentrations, i.e., the CO₂ concentration reduced as CO concentration increased. This dependence exhibited in the prototype and Model 60i are expressed as Eqs. (16) and (17) with the correlation coefficient of $R^2 = 0.37709$ and 0.36624 for CO₂ to CO, respectively.

$$C(\text{CO}_2) = (-0.00951 \pm 0.0015) \times C(\text{CO}) + (16.57226 \pm 0.26934) \quad (16)$$

$$C(\text{CO}_2) = (-0.0089 \pm 0.00151) \times C(\text{CO}) + (16.6115 \pm 0.27455) \quad (17)$$

The units for CO₂ and CO in both equations were % and ppmv respectively. A detailed discussion of the characteristics of the pollutant gases emissions of this cement plant or the relationship between the gases emissions and the specific production process exceeds the scope of this article, and will be published elsewhere separately.

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Accuracy and sensitivity depend largely on the results of cross-interferences correction if the gases are measured simultaneously through the NDIR technique. An analyzer with a constant path length exhibits nonlinear absorption if the gas concentrations go beyond a restricted range, resulting in the variation of the interference coefficients with the interfering gas concentration. The classical algorithm for cross interference fails in this case. In the present paper, an optimized cross-interference correction algorithm modified from the classical interference equations is presented. An interference function rather than a interference constant is used to qualify the gas-to-gas interference. When an analyzer exhibits nonlinear absorption, the interference coefficient determined by interference function varies correspondingly. The cross-interferences can be corrected well by both algorithms if the analyzer has good linearity. However, the interference correction results from using the interference function are obviously better than that corrected using the interference constant if nonlinear absorption appears. The optimized algorithm can correct cross-interference well despite linear absorption or nonlinear absorption. The dynamic measurement ranges of the analyzer for CO₂ and CO are expanded by a factor of about 1.8 and 3.5 respectively. In the last part, a commercial NDIR multi-gas analyzer Model 60i manufactured by Thermo Fisher Scientific, Inc. is used to validate the CO and CO₂ measurements derived from a NDIR prototype, in which an optimized cross-interference correction algorithm is embedded. The two analyzers measurements exhibit approximately the same concentration trend, and a negative correlation between CO₂ and CO is derived from the measurements of both analyzers.

Acknowledgements. This work is jointly supported by the Special Scientific Research Fund of Meteorological Public Welfare Profession of China (Grant NO.GYHY201106045-1 and NO. 201109007) and the National Natural Science Foundation of China (Grant NO.41275037 and NO. 41105011). We thank X. Zhou, manager of the Shangfeng cement plant, for our access to the field site, and Liu for his valuable comments on the manuscript.

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**Table 1.** Interference coefficient behavior.

Case	Nonlinear Absorption Behavior	k'_{ji}	k'_{ij}	Measurement Error
1	Neither gas i nor j has nonlinear absorption.	$k'_{ji} = k_{ji}$	$k'_{ij} = k_{ij}$	$\gamma_i = 0;$ $\gamma_j = 0$
2	Gas i has nonlinear absorption, but gas j does not.	$k'_{ji} > k_{ji}$ and varies obviously with gas i concentration, increasing as its concentration increases.	$k'_{ij} = k_{ij}$	$\gamma_i \neq 0;$ $\gamma_j = 0$
3	Gas j has nonlinear absorption, but gas i does not.	$k'_{ji} = k_{ji}$	$k'_{ij} > k_{ij}$ and varies obviously with gas j concentration, increasing as its concentration increases.	$\gamma_i = 0;$ $\gamma_j \neq 0$
4	Both gas i and j have nonlinear absorption.	$k'_{ji} > k_{ji}$ and $k'_{ij} > k_{ij}$. Both of them vary obviously with gas their concentrations i and j concentration, respectively, increasing as increase.		$\gamma_i \neq 0;$ $\gamma_j \neq 0$

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Table 2. Comparison of the classical and optimized cross interference correction algorithm.

Algorithm	Linear absorption	Nonlinear absorption	Measurement range	Processing speed
Classical	Yes	No	Narrow	Fast
Optimized	Yes	Yes	Wide	Slow

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Table 3. Selection of the cross interference correction algorithm for simultaneous two gases analysis, gas i and j mentioned in former sections are taken as an example.

Case	Nonlinear absorption behaviors	Selection of the cross-interference correction algorithm	Implementation of the interference equations
1	Neither gas i nor j has nonlinear absorption.	Classical	Both the interference of gas i to j and gas j to i are corrected using a constant factor.
2	Gas i has nonlinear absorption, but gas j does not.	Optimized	The interference of gas j to i is corrected using a constant factor. However, the interference of gas i to j is corrected using a fitted interference function.
3	Gas j has nonlinear absorption, but gas i does not.	Optimized	The interference of gas i to j is corrected using a constant factor. However, the interference of gas j to i is corrected using a fitted interference function.
4	Both gas i and j have nonlinear absorption.	Optimized	Both the interference of gas i to j and gas j to i are corrected using a fitted interference function.

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Table 4. Performance specifications comparison of the prototype and Model 60i for CO₂ and CO, where only parts of the performance specifications used for discussion in the text are compared.

Instrument	NDIR Model 60i		NDIR Prototype	
	CO	CO ₂	CO	CO ₂
Lower detection	1 ppmv	500 ppmv	0.4 ppmv	300 ppmv
Dynamic range with linearity error $\leq \pm 2\%$	0 ~ 2500 ppmv	0 ~ 25 %	0 ~ 850 ppmv	0 ~ 17 %
Measurement error	$\pm 2\%$	$\pm 2\%$	$\pm 1\%$	$\pm 1.5\%$

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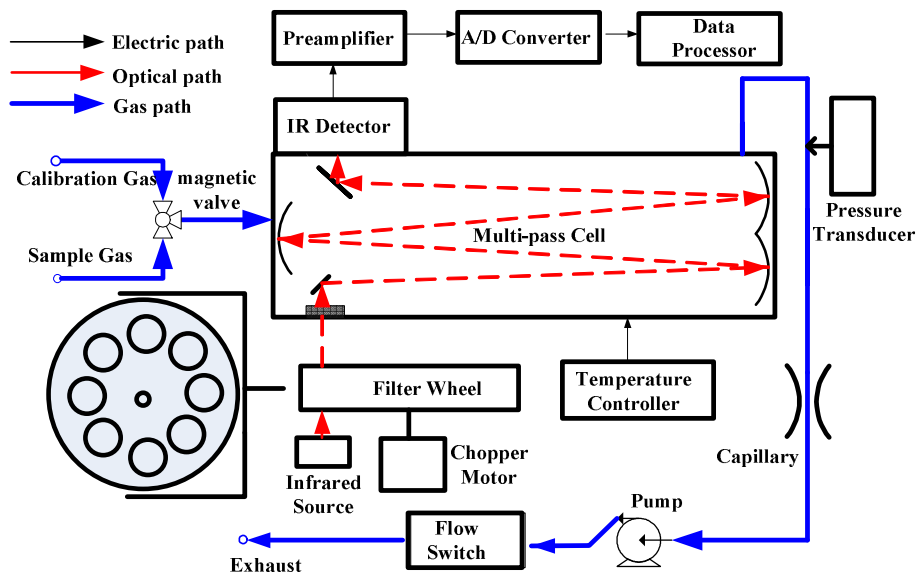


Fig. 1. Functional structure of NDIR multi-gas analyzer prototype.

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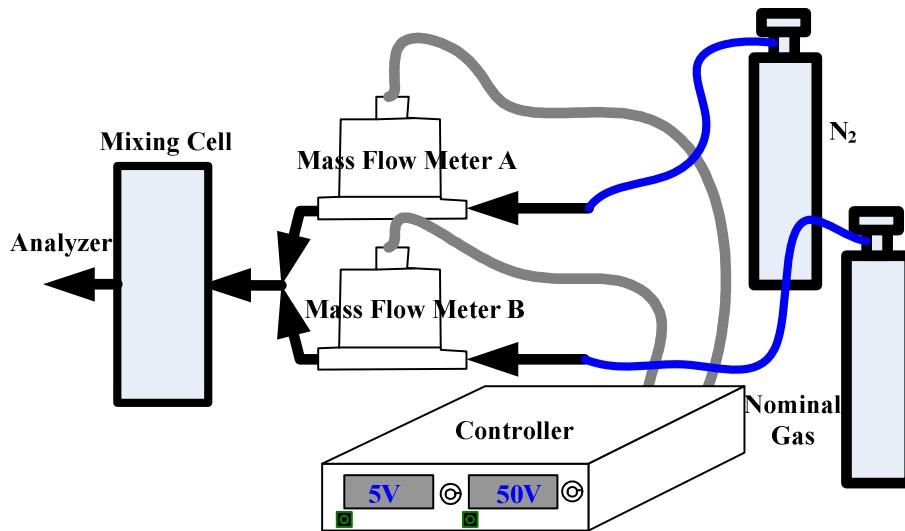


Fig. 2. Apparatus for gas distribution.

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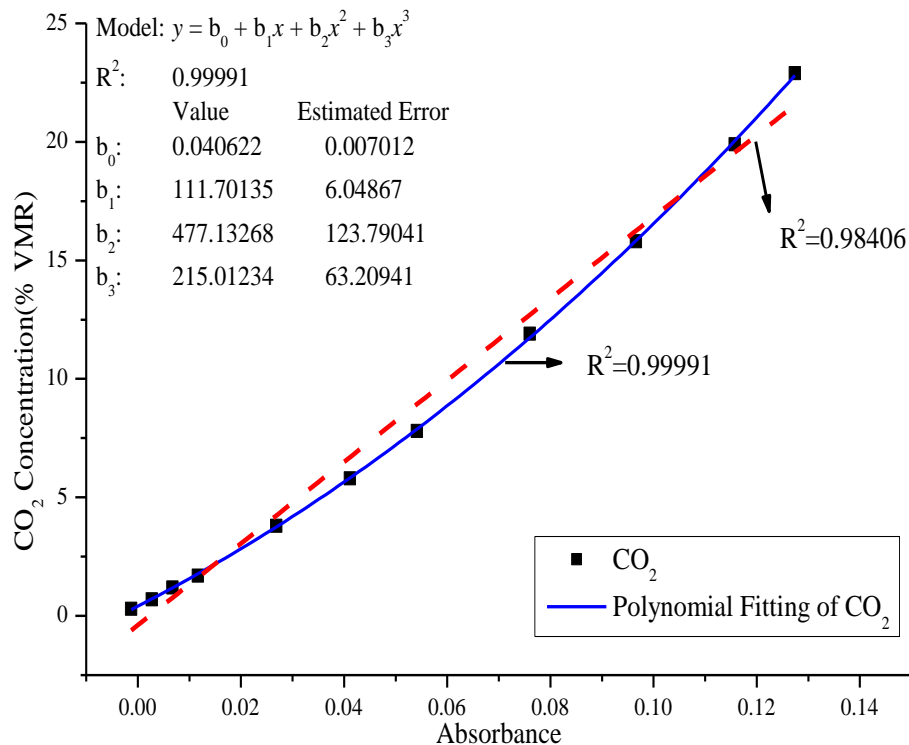


Fig. 3. Calibration curve and measurement linearity fitting results for CO₂. The red dotted line is the linear plot fitted by linear least-squares fitting, and the blue solid curve represents the calibration curve obtained by least-squares fitting using the three-order polynomial model. Fitting values, estimated errors, and fitting correlation coefficients are also included.

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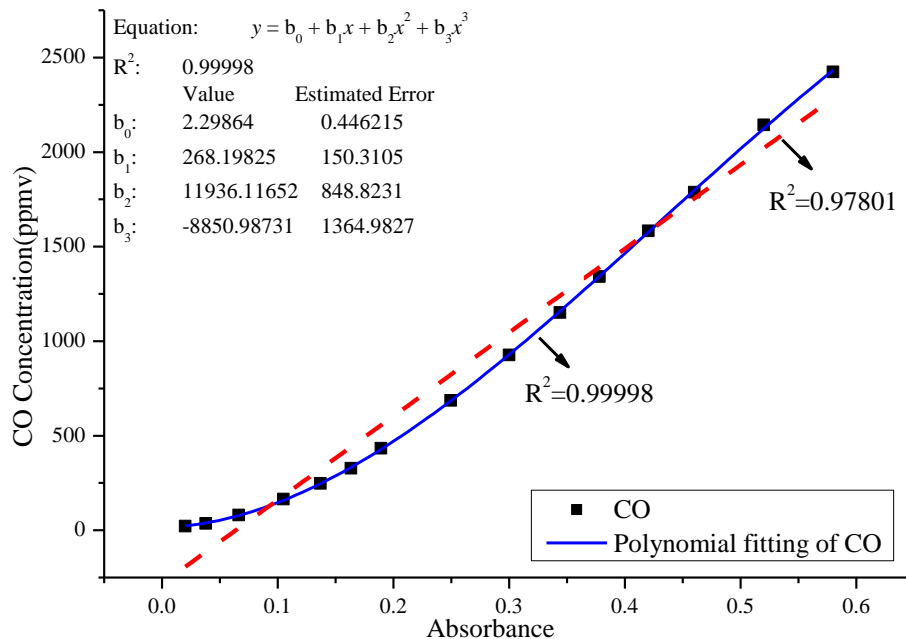


Fig. 4. Calibration curve and measurement linearity fitting results for CO. The red dotted line is the linear plot fitted by linear least-squares fitting, and the blue solid curve represents the calibration curve obtained by least-squares fitting using the three-order polynomial model. Fitting values, estimated errors, and fitting correlation coefficients are also included.

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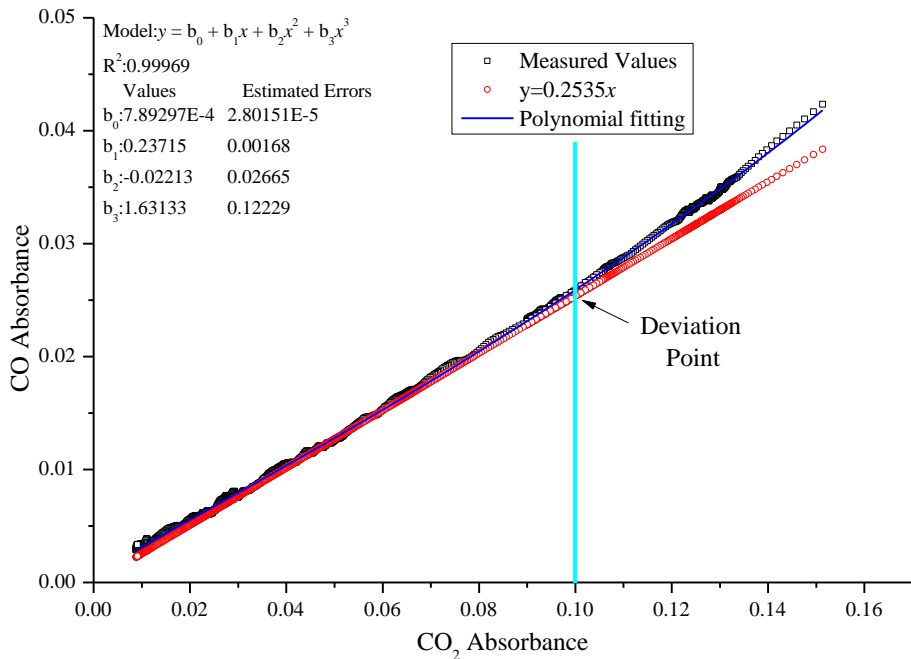


Fig. 5. Fitting results for the interference function of CO₂ to CO. The black squares “□” are absorbance arrays converted from detection voltages, the solid blue line “—” is the interference function obtained by least-squares fitting using a three-order polynomial, and the slope of the straight line marked by red circles “o” is the interference constant of CO₂ to CO. Specifically, a data array marked by black squares in Fig. 5 corresponds to the array ($A_{\text{total}(n)}^i, A_{\text{total}(n)}^j$) mentioned in Sect. 3, the solid blue line is $k_{ji}(x)$, and the slope 0.2535 of $y = 0.2535x$ is k_{ji} , which is measured through the method mentioned in Dirk et al. (2009).

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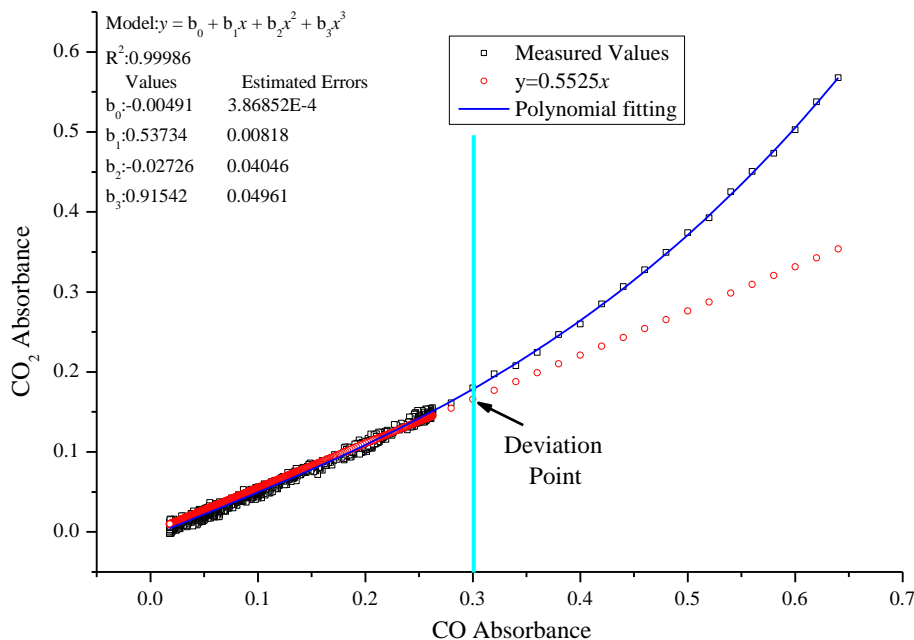


Fig. 6. Fitting results for the interference function of CO to CO₂. The black squares “□” are absorbance arrays converted from detection voltages, the solid blue line “—” is the interference function obtained by least-squares fitting using a three-order polynomial, and the slope of the straight line marked by red circles “○” is the interference constant of CO to CO₂. Specifically, the data array marked by black squares in Fig. 6 corresponds to array $(A_{\text{total}(n)}^i, A_{\text{total}(n)}^j)$, the solid blue line is $k_{ij}(x)$, and the slope 0.5525 of $y = 0.5525x$ is k_{ij} , which is measured through the method mentioned in Dirk et al. (2009).

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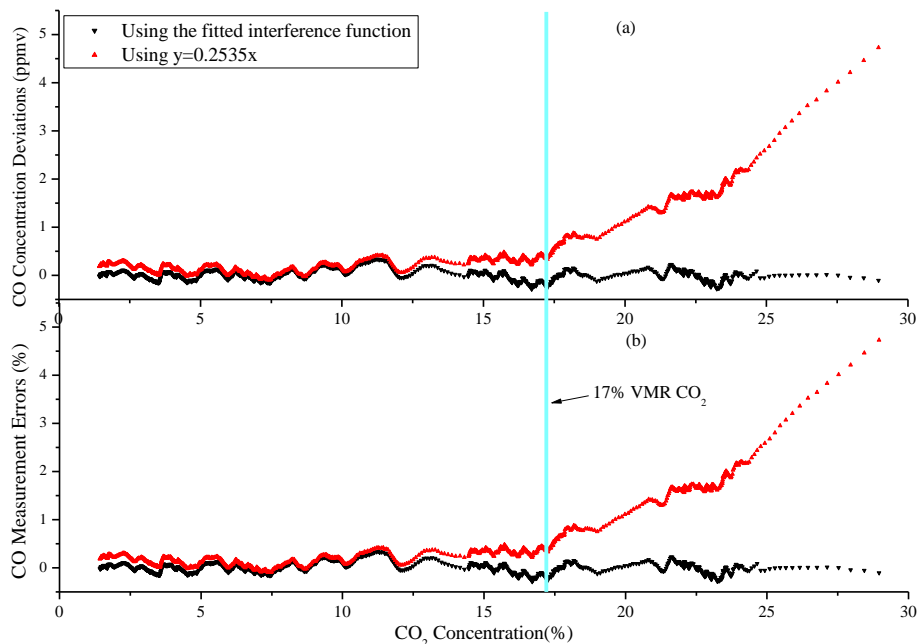


Fig. 7. Measurement errors comparison for the different cross interference correction algorithms (with respect to the interference of CO₂ to CO). **(a)** Different concentrations of CO₂ are pumped into a sample cell in sequence for the analysis but only the absorbance of the CO channel are retrieved to the concentrations; the black inverted triangle curves “∇” and the red upright triangle curves “Δ” are the CO concentration variations for the cross interferences being corrected using the fitted interference function and a constant factor respectively. **(b)** Measurement error variations calculated from **(a)** when 100 ppmv CO is taken as an example.

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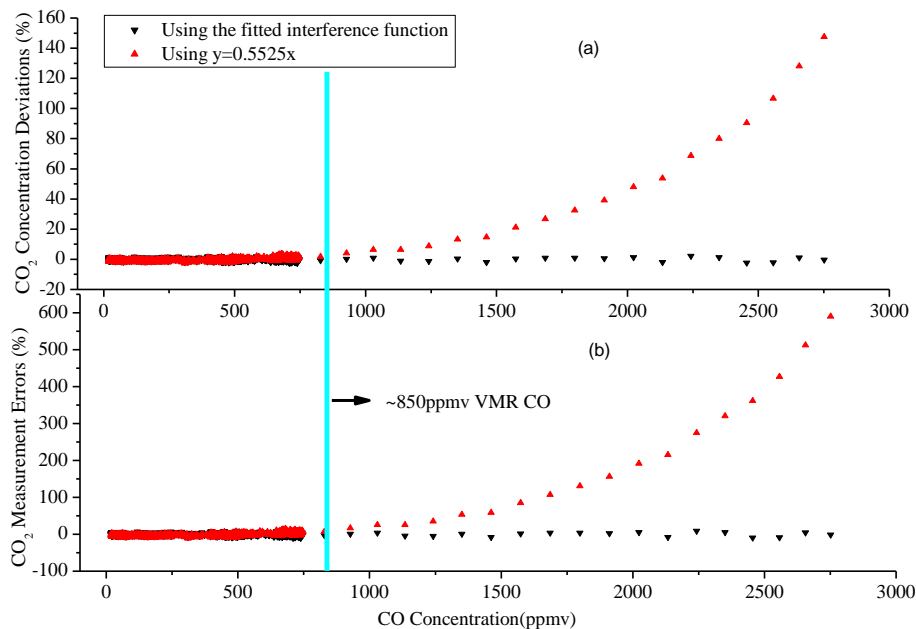



Fig. 8. Measurement errors comparison for the different cross interference correction algorithms (with respect to the interference of CO to CO₂). **(a)** Different concentrations of CO are pumped into a sample cell in sequence for the analysis but only the absorbance of the CO₂ channel are retrieved to the concentrations; the black inverted triangle curves “▽” and the red upright triangle curves “△” are the CO₂ concentration variations for the cross interferences being corrected using the fitted interference function and a constant factor respectively. **(b)** Measurement error variations calculated from **(a)** when 25 % CO₂ is taken as an example.

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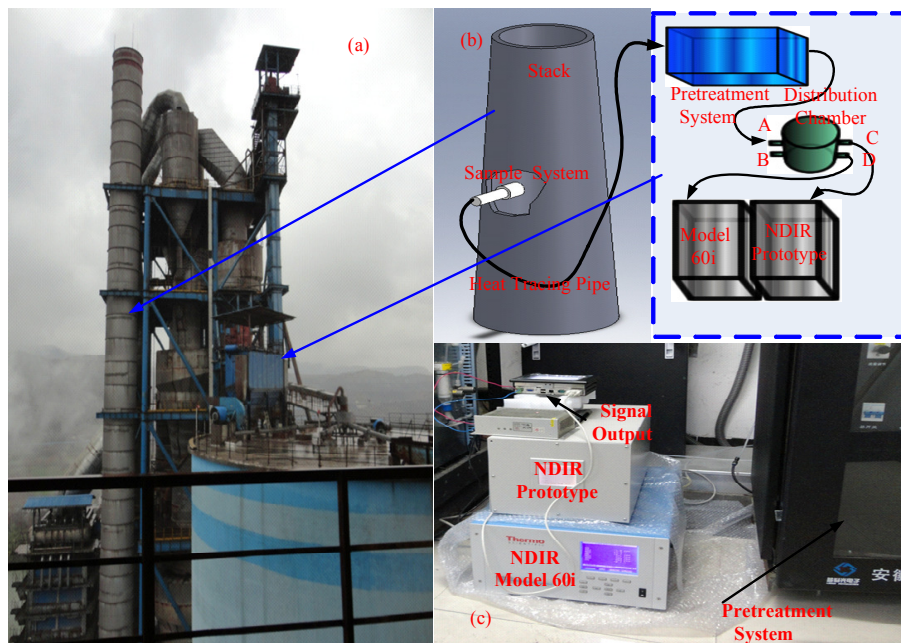


Fig. 9. Diagram of the experimental set-up used in the field. Two analyzers are placed in a mini house built about 15 m height above the ground. **(a)** A photo of the stack taken from a nearby building roof, **(b)** shows diagram of experimental set-up used in the field and arrangement inside the mini house is visible in **(c)**. See text for details.

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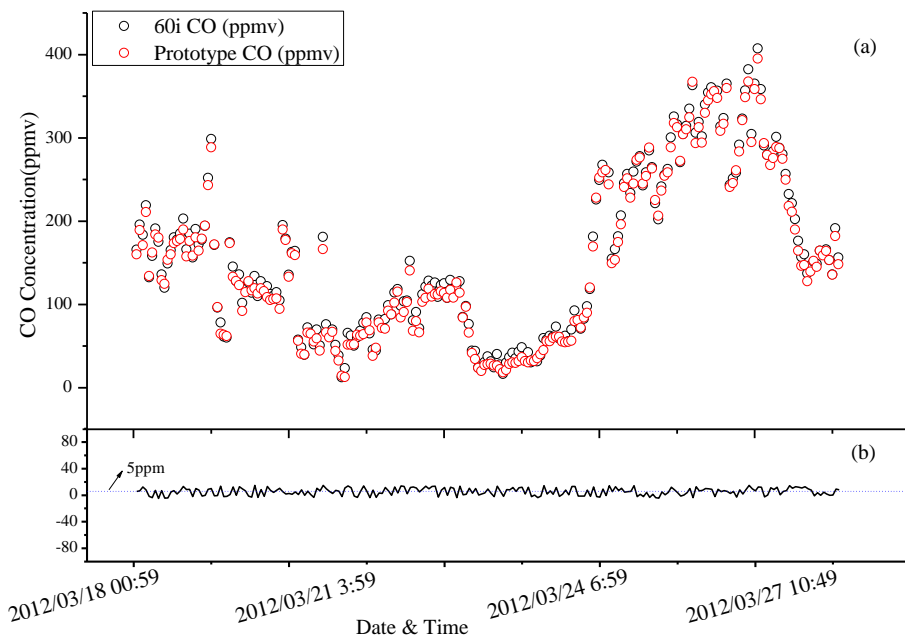


Fig. 10. (a) Time series of the monoxide dioxide volume-mixing ratio measured by the NDIR Model 60i and the NDIR multi-gas analyzer prototype. The difference between the CO concentrations measured by Model 60i and prototype are shown in **(b)**. Outliers are removed and hour averaged.

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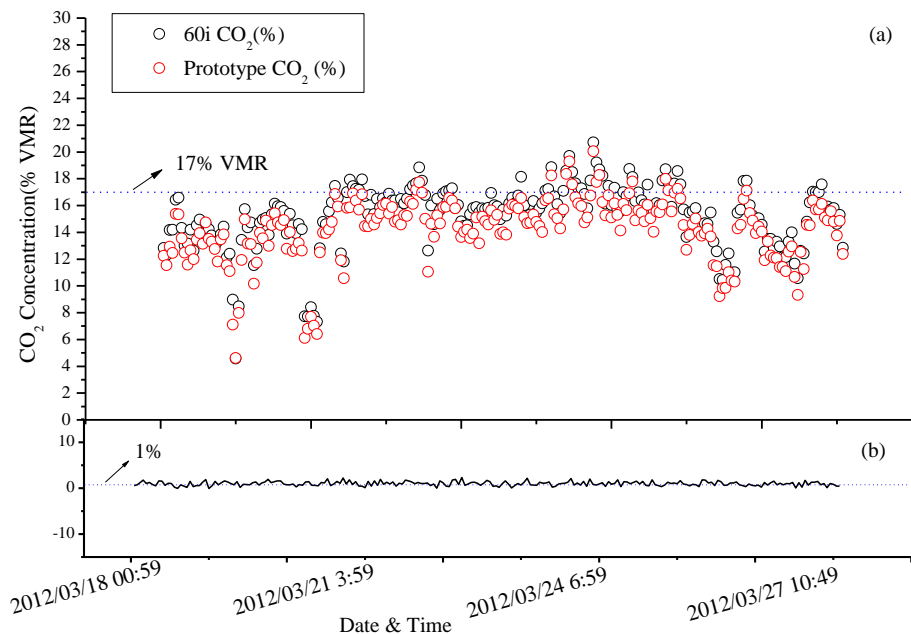


Fig. 11. (a) Time series of the carbon dioxide volume-mixing ratio measured by the NDIR Model 60i and the NDIR analyzer prototype. The difference between the CO₂ concentrations measured by Model 60i and prototype are shown in (b). Outliers are removed and hour averaged.

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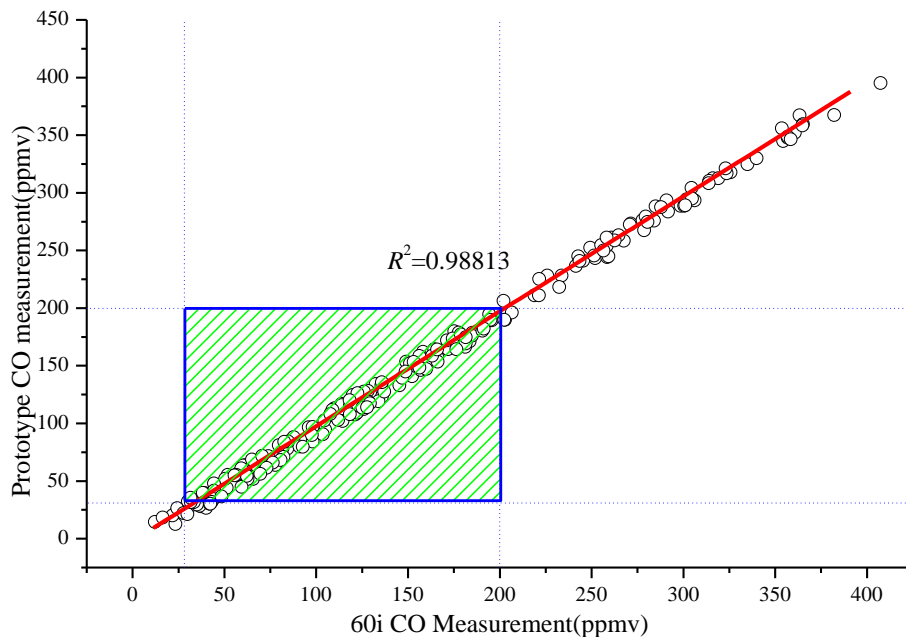


Fig. 12. CO measurement correlation between Model 60i and the NDIR multi-gas analyzer prototype after the outliers are removed. The measurement correlation coefficient R^2 is visible in the figure.

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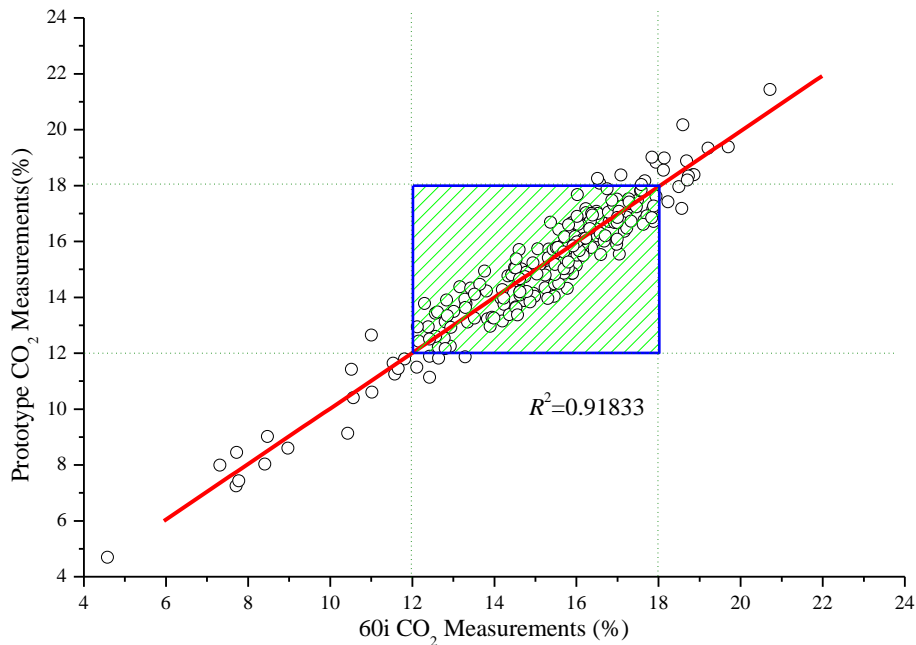


Fig. 13. CO₂ measurement correlation between Model 60i and the NDIR multi-gas analyzer prototype after the outliers are removed. The measurement correlation coefficient R^2 is visible in the figure.

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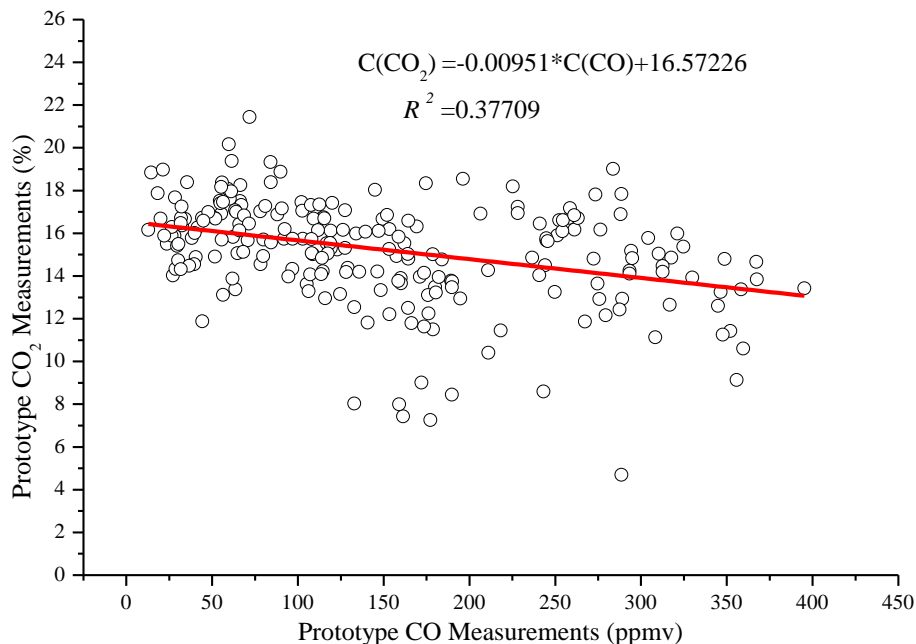


Fig. 14. Correlation between CO_2 and CO measured by the NDIR multi-gas analyzer prototype. Both the measurement correlation coefficient R^2 and the fitted correlation equation are visible in the figure.

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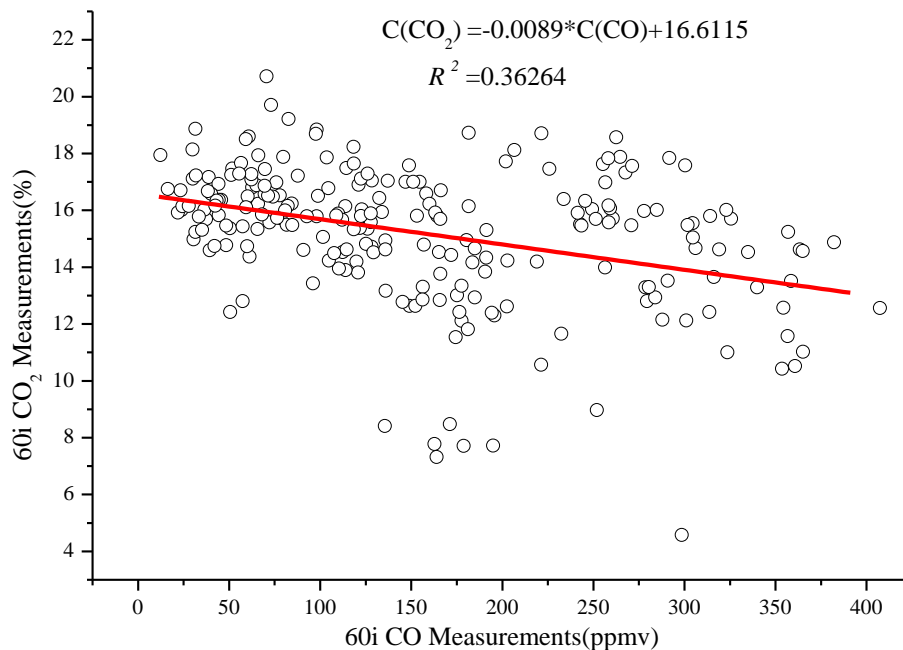


Fig. 15. Correlation between CO₂ and CO measured by Model 60i. Both the measurement correlation coefficient R^2 and the fitted correlation equation are visible in the figure.