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Effects of systematic and random errors on the retrieval of particle microphysical properties from multiwavelength lidar measurements using inversion with regularization

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Abstract

In this work we study the effects of systematic and random errors on the inversion of multi-wavelength (MW) lidar data, using the well-known regularization technique, to obtain vertically-resolved aerosol microphysical properties. The software implementation used here was developed at the Physics Instrumentation Center (PIC) in Troitsk (Russia) in conjunction with NASA/Goddard Space Flight Center. Its applicability to Raman lidar systems based on backscattering measurements at three wavelengths (355, 532 and 1064 nm) and extinction measurements at two wavelengths (355 and 532 nm) has been demonstrated widely. The systematic error sensitivity is quantified by first determining the retrieved parameters for a given set of optical input data consistent with two different sets of aerosol physical parameters. Then each optical input is perturbed by varying amounts and the inversion is repeated. We find a generally linear dependence

- of the retrieved errors in the microphysical properties on the induced systematic errors in the optical data. For the retrievals of effective radius, number/surface/volume concentrations and fine mode radius and volume, we found that these results are not
- significantly affected by the range of the constraints used in inversions. But significant sensitivity was found to the allowed range of the imaginary part of the particle refractive index to reach. Our results also indicate that exist an additive property for the deviations induced by the biases induced in the individual optical data. This permits the results
- ²⁰ here to be used to predict deviations in retrieved parameters when multiple input optical data are biased as well as to study the influence of random errors on the retrievals. The above results can be applied to questions regarding lidar design, as for example the space-borne multi-wavelength lidar to be deployed in the upcoming ACE mission anticipated to provide optical data with 15 % accuracy in each of the lidar channels.



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1 Introduction

The importance of atmospheric aerosol particles on Earth's climate and on environmental problems is widely recognized. Particularly, the Intergovernmental Panel on Climate Change 2007 (IPCC, 2007) (Forster et al., 2007) stated that atmospheric aerosol

- particles can produce a negative radiative forcing that is comparable in magnitude, but opposite in sign, to the forcing induced by the increase in greenhouse gas concentration. However, radiative forcing by atmospheric aerosol particles has greater uncertainties (twice the estimated value of the forcing) due to the large spatial and temporal heterogeneities of atmospheric aerosols (e.g. Haywood and Boucher, 2000), the wide
 variety of aerosol sources (e.g. Dubovik et al., 2002), the spatial non-uniformity and intermittency of these sources (e.g. Kaufman et al., 1997), the short atmospheric lifetime
 - of aerosols (e.g. Seinfield and Pandis, 1998), processes occurring in the atmosphere (Eck et al., 2010) and aerosol dynamics (e.g. Pérez-Ramírez et al., 2012).

Because of these challenges, the characterization of atmospheric aerosols is be-

- ¹⁵ ing made through intense observational programs using remote sensing techniques. For example, NASA has led several space-borne missions to study aerosol properties worldwide (e.g. the MODIS instrument on the TERRA and AQUA platforms). However, satellite measurements possess lower temporal resolution than ground-based systems. For example, the AERONET global network (Holben et al., 1998) is provid-
- ing large datasets of high temporal resolution ground-based aerosol measurements at more than 400 locations worldwide. But the aerosol retrievals by AERONET and by many satellite platforms only provide column-integrated properties. By contrast, the lidar technique offers vertical profiling of aerosols, from the first lidars in the early 1960s to the more sophisticated Raman lidars (Whiteman et al., 1992; Ansmann et al., 1992)
- or High Spectral Resolution Lidars (HSRL) (Shipley et al., 1983; Grund and Eloranta, 1991; She et al., 1992, 2001). Moreover, the Nd:YAG laser has been used as the transmitter for multi-wavelength Raman lidar systems (MW) which have permitted the retrieval of the profile of aerosol microphysical properties (e.g. Wandinger et al., 2002;

Bockman et al., 2005; Noh et al., 2009; Balis et al., 2010; Alados-Arboledas et al., 2011; Tesche et al., 2011; Veselovskii et al., 2012; Papayannis et al., 2012; Wanger et al., 2013; Navas-Guzmán et al., 2013).

- The first attempts to obtain aerosol microphysical properties from MW Raman lidar ⁵ measurements were done at the Institute for Tropospheric Research (IFT) in Leipzig (Germany) using the regularization technique (Müller et al., 1999a, b, 2000). The first retrievals done at the IFT were based on measurements from a complex lidar system providing six backscattering (355, 400, 532, 710, 800 and 1064 nm) and two extinction (355 and 532 nm) coefficients. Following these first efforts, a software capability based on the regularization technique was developed at the Physics Instrumentation Center
- (PIC) in Troitsk (Moscow, Russia). The retrieval code development has been further advanced and has incorporated a model of randomly-oriented spheroids for retrieving dust particle properties (Veselovskii et al., 2010). From an instrumental point of view, Veselovskii et al. (2004) and Müller et al. (2004, 2005) and demonstrated the capability
- ¹⁵ of the regularization technique to retrieve aerosol microphysical properties from a lidar system that provides just 5 optical signals using a tripled Nd:YAG laser. The optical data provided by this system were backscatter coefficients (β) at 355, 532 and 1064 nm and extinction coefficients (α) at 355 and 532 nm (hereafter this configuration is referred as $3\beta + 2\alpha$). The inversion procedure makes use of averaging of the solutions in the vicinity of the minimum of the penalty functions (Veselovskii et al., 2002). This averaging
- procedure increases the reliability of the inversions even when the input optical data are affected by small random errors.

However, lidar systems are very complex and generally possess both random and systematic errors. Random errors arise naturally from the measurement process and ²⁵ some preliminary random error sensitivity studies were done by Müller et al. (1999a, b) and Veselovskii et al. (2002, 2004). But to date, there is a lack of studies of the effects

of systematic errors on the microphysical inversions. Systematic errors in lidar systems come from many different sources and need to be considered. From the hardware point of view, systematic errors can be due to, for example, non-linearity of a photodetector or

errors in calibration of the optical data. From the methodological point of view, systematic errors can be caused by, for example, errors in the assumed atmospheric molecule density profile, the selection of the reference level (an "aerosol-free" region that may actually contain a small amount of particles), the effect of depolarization due to optical imperfections in channels that are sensitive to polarized light or the use of an incorrect

- Imperfections in channels that are sensitive to polarized light or the use of an incorrect extinction-to-backscatter ratio to convert backscatter lidar measurements to extinction. In general, we expect that systematic errors such as these can affect the retrieval. The aim of this work, therefore, is to study the sensitivity of microphysical retrievals by the regularization technique to systematic variations in the input optical data provided
- ¹⁰ by the $3\beta + 2\alpha$ lidar configuration. We will show that the results obtained can be also used to assess the sensitivity of the retrievals to random errors in a new way. The study involves simulations based on two bi-modal aerosol size distributions, one with a large predominance of fine mode and the other with slight predominance of coarse mode. First the optical data consistent with these distributions are generated using Mie the-
- ory. Then the optical inputs are systematically altered to provide a known amount of systematic error in the input data. The inversion code is run using both the biased and unbiased optical data and the deviations in the retrieved aerosol parameters are quantified. The methodology and the simulation approach are presented in Sect. 2. Section 3 is devoted to the results. Finally, in Sect. 4 we present a summary and conclusions.

20 2 Methodology and simulation approach

2.1 Inversion technique

The optical characteristics of an ensemble of polydisperse aerosol particles are related to the particle volume distribution via Fredholm integral equations of the first kind as follows (Müller et al., 1999a; Veselovskii et al., 2002):

$$g_j(\lambda_i) = \int_{r_{\min}}^{r_{\max}} K_{j,N}(m,r,\lambda_i) n(r) dr$$

Where *j* corresponds either to backscatter (β) or extinction (α) coefficients, $g_j(\lambda_i)$ are the corresponding optical data at wavelength λ_i , n(r) is the aerosol size distribution expressed as the number of particles per unit volume between *r* and *r* + d*r*, and $K_{j,N}(m,r,\lambda_i)$ are the number kernel functions (backscatter or extinction) which are here calculated from Mie theory assuming spherical particles and depend on particle refractive index *m*, particle radius *r* and wavelength λ . Finally, r_{\min} and r_{\max} correspond to the minimum and maximum radius used in the inversion. The size distribution in Eq. (1) can be written in terms of surface ($s(r) = 4\pi r^2 n(r)$) or volume ($v(r) = (4/3)\pi r^3 n(r)$) size distribution. The corresponding kernels are obtained by dividing $K_{j,N}(m,r,\lambda_j)$ by $4\pi r^2$

and $(4/3)\pi r^3$ respectively, and are thus given by:

$$K_{j,\mathsf{S}}(m,r,\lambda) = \frac{K_{j,\mathsf{N}}(m,r,\lambda)}{4\pi r^2}$$

$$\mathcal{K}_{j,V}(m,r,\lambda) = \frac{3\mathcal{K}_{j,N}(m,r,\lambda)}{4\pi r^3}$$

- ¹⁵ Where $K_{j,S}(m,r,\lambda)$ and $K_{j,V}(m,r,\lambda)$ are the surface and volume kernel functions respectively. Generally, the volume kernel functions are used in the retrieval procedure of aerosol microphysical properties (Heintzenberg et al., 1981; Qing et al., 1989). Thus, we perform the retrieval of volume size distribution using the volume kernel functions of Eq. (3). More details about the computation of these volume kernel functions from
- ²⁰ Mie extinction coefficients for spherical particles can be found in the references (e.g. Bohren and Huffman, 1983).

(1)

(2)

(3)

The regularization technique used here to solve Eq. (1) has been discussed extensively elsewhere (e.g. Veselovskii et al., 2002, 2004, 2005) and thus we provide here only a brief overview. The key point is identifying a group of solutions which, after averaging, can provide a realistic estimation of particle parameters. Such identification

- ⁵ can be done by considering the discrepancy (ρ) defined as the difference between input data $g(\lambda)$ and data calculated from the solution obtained. The retrieval uses an averaging procedure that consists of selecting a class of solutions in the vicinity of the minimum of discrepancy (Veselovskii et al., 2002, 2004). Such an averaging procedure stabilizes the inversion, as the final solution for size distribution and aerosol parameters
- is an average of a large number of individual solutions near the minimum of discrepancy (Veselovskii et al., 2002). In general, we average approximately 1 % of the total number of solutions.

The inverse problem considered here is under-determined, so constraints on the inversion are needed. We consider a set of possible values of the particle refractive ¹⁵ index as well as a set of possible radii within a certain size interval. In general, the retrieval result will depend on the range of parameters considered: the larger the range, the higher the uncertainty of the retrieval as determined by the spread in the solutions obtained. So the range of parameters should be chosen reasonably. In our research, the real part of the aerosol refractive index (m_r) is allowed to vary from 1.33 to 1.65 with

²⁰ a stepsize of 0.025, while the imaginary part (m_i) varies over the range of 0–0.01 with a stepsize of 0.001. The size interval for the inversions was limited to 0.075–5 µm with a stepsize of 0.025. Tests revealed that reducing the stepsize of the different parameters in the inversion does not decrease the spread in the solution. Therefore we take the stepsizes used as adequate for the purposes of the present sensitivity study.

2.2 Size distribution for the simulations

For the simulations we used bimodal aerosol size distributions given as (Veselovskii et al., 2004):

$$\frac{dn(r)}{d\ln(r)} = \sum_{i=f,c} \frac{N_{t,i}}{(2\pi)^{1/2} \ln \sigma_i} \exp\left[\frac{\left(\ln r - \ln r_i^n\right)^2}{2\left(\ln \sigma_i\right)^2}\right]$$
(4)

- ⁵ Where $N_{t,i}$ is the total particle number of the *i*th mode, $\ln(\sigma_i)$ is the mode width of the *i*th mode and r_i^n is the mode radius for the number concentration distribution. The index i = f, c corresponds to the fine mode and the coarse mode, respectively. In the retrieval procedure, the fine mode is taken to include all particles with radius between 0.075 µm and 0.5 µm while the coarse mode includes all particles with radius between $0.5 \,\mu\text{m}$ and $5 \,\mu\text{m}$. On the other hand, the same distribution can be written for volume 10
- concentration v(r), which is usually preferred because both fine and coarse mode can be easily distinguished. Moreover, the standard deviations of n(r) and v(r) are the same when using the relationships between radius and concentrations for each mode given by (Horvath et al., 1990):

15
$$r_i^{v} = r_i^{n} \exp\left[\frac{\left(\ln r - \ln r_i^{n}\right)^2}{2\left(\ln \sigma\right)^2}\right]$$

$$V_{\rm ti} = N_{\rm ti} \frac{4}{3} \pi \left(r_i^n \right)^3 \exp \left[\frac{9}{2} \left(\ln \sigma \right)^2 \right]$$

We consider two types of aerosol size distributions for the simulations which we call type I and type II. These size distributions are used to approximate real aerosol types found in the atmosphere. Both types use $r_t^{V} = 0.14 \,\mu\text{m}$, $\ln \sigma_t = 0.4$, $r_c^{V} = 1.5 \,\mu\text{m}$

(5)

(6)

20

and $\ln \sigma_c = 0.6$. The difference between type I and type II is the ratio of fine and coarse mode (V_{tf}/V_{tc}). Type I yields $V_{tf}/V_{tc} = 2$ and represents a distribution with a predominance of fine mode. This type can be considered to represent industrial and biomass burning aerosols (e.g. Eck et al., 2003; Muller et al., 2004; Schafer et al., 2008). Type I yields $V_{tf}/V_{tc} = 0.2$ and corresponds to a slight predominance of the coarse mode over the fine mode (e.g. Smirnov et al., 2002, 2003; Eck et al., 2005, 2010). This type

- is consistent with a mixture of dust/marine aerosol and those of pollution or biomass burning. Figure 1 illustrates the two size distributions used. For convenience, we have normalized the volume of the fine mode such that $V_{tf} = 1$. Therefore, for we have mode
- ¹⁰ $V_{tc} = 0.5$ for aerosol type I and mode $V_{tc} = 5$ for aerosol type II. For the case of a strong predominance of coarse mode (e.g. marine or dust aerosol) in $3\beta + 2\alpha$ lidar measurements, the effects of polarization and non-sphericity should be taken into account and previous work indicates that the use of kernel functions for non-spherical particles can improve the retrievals (Veselovskii et al., 2010) Here, however, our purpose is to cal-15 culate sensitivities due to random and systematic uncertainties so we consider only spherical (Mie) kernels.

The simulation consists of generating the three backscattering and two extinction coefficients for the $3\beta + 2\alpha$ lidar configuration using Mie theory for the two aerosol size distributions: type I and type II. These optical data are generated for six different configuration used for a produce of a produce of 1.25 and 1.55 and m values of 1.25 and 1.55 and m values of 1.25 and 1.55 and m values of 1.25 and 1.55 an

- ²⁰ urations of aerosol refractive indices (m_r values of 1.35, 1.45 and 1.55 and m_i values of 0.005 and 0.01). The regularization inversion is then performed on these data and we obtain the retrieved microphysical parameters. The next step is to apply a systematic bias, denoted as $\Delta \varepsilon$, to one optical datum at a time. The bias varies from -20% to +20% in 8 intervals. For each of these induced biases, the inversion is performed
- ²⁵ and a new size distribution and set of microphysical properties is obtained. For a microphysical parameter denoted as M, the comparisons we performed are expressed as the percentage difference $100 \cdot (M_{\text{bias}} - M_{\text{ret}})/M_{\text{ret}}$. This procedure is applied to each of the 5 optical data used in the $3\beta + 2\alpha$ lidar configuration.

3 Results

3.1 Uncertainties in the retrieval of particle refractive index

The $3\beta + 2\alpha$ lidar configuration permits the retrieval of particle refractive index, both real (m_r) and imaginary (m_i) parts (e.g. Veselovskii et al., 2002), by use of the regularization scheme. But the inverse problem of Eq. (1) is under-determined and as already stated, 5 we must use constraints to permit solutions to be obtained. Particularly, the selection of the range of refractive indices permitted in the retrieval is important. As commented, we limited the range of m_r between 1.33 and 1.65 and m_i from 0.0 up to 0.01. These ranges cover most types of aerosol particles present in the atmosphere, except for strongly absorption particles such as black carbon. Moreover, given that the longest 10 wavelength measurement is 1064 nm, the technique has reduced sensitivity to coarse mode of the aerosol distribution. Thus, to stabilize the retrievals, the maximum radius allowed was set to 5 µm. Additionally, the Kernel functions for radius below 0.075 are very near to zero, and thus the minimum radius allowed was set to 0.075 µm. These behaviors of Kernel functions with wavelength can be consulted for example in Chapter 11 of Bohren and Huffman (1983).

In the analysis that follows, we do not present results on the refractive index sensitivity analysis. The reason for this is that we found that the retrieval of refractive index is very sensitive to the range of permitted values for the imaginary part of the refractive

- ²⁰ index. Changing the range of permitted values of the imaginary part can change the retrieved refractive index significantly while not significantly affecting the values of the other retrieved quantities. Therefore, recalling that the retrieval is under-determined, we conclude that we can provide reasonable estimates of the refractive index only with reasonable constraints for m_i . All these results just magnify the point that refractive in-
- dex retrievals are difficult with the MW lidar technique and that some a priori knowledge of the aerosol absorption is helpful to constrain the inversion. A more in depth discussion about the limitations of the averaging procedure used here to retrieve accurate values of particle refractive index is in Veselovskii et al. (2013).

3.2 Effects on the retrievals of systematic errors in the optical data

For the scheme described previously, Fig. 2 presents the sensitivity analysis for the retrieval of effective radius (r_{eff}). Every point corresponds to the mean value of the six different combinations of aerosol refractive indices used in generating the set of optical data. The error bars shown are the standard deviations of these mean values. Generally linear patterns are observed for the deviation in retrieved value of r_{eff} for differing biases in the input optical data for both types I and II aerosols. As the linear patterns pass through the origin, least-squares fits of the form Y = aX were done to the points shown in the plot. Given the definition of $\Delta r_{eff} = r_{eff, bias} - r_{eff, ret}$, positive slopes indicate higher values of r_{eff} when the optical data are affected by biases than when they are not affected by biases, while for negative slopes just the opposite occurs. Moreover, Fig. 2 reveals the same general patterns between types I and II for each optical channel, with only small changes in the absolute values of the slopes of the

linear fits. The retrievals are more sensitive to biases in the extinction coefficients. The lowest constituition are to biases in β (255 pm) and β (522 pm) while for biases in β

¹⁵ lowest sensitivities are to biases in β (355 nm) and β (532 nm) while for biases in β (1064 nm) the sensitivity of the retrievals is in between those obtained for extinction and backscattering coefficients at 355 and 532 nm. Figure 2 also reveals that the linear patterns for different optical channels have different signs of the slopes. Considering the parameters to which the retrievals are most sensitive, the linear fit of α (355 nm) gives negative values of slope ($a = -1.68 \pm 0.12$ for type I and $a = -1.74 \pm 0.03$ for type II), while for α (532 nm) the slopes are positive ($a = 1.51 \pm 0.04$ for type I and $a = 1.82 \pm 0.09$ for type II).

The Ångström law, either for the extinction or for the backscattering can be used to help understand the sign of the slopes of Fig. 2. For the wavelengths used here, the

²⁵ Ångström exponents η_{α} and η_{β} characterize the spectral features of aerosol particles and are related to the size of the particles: large values of η_{α} and η_{β} are mainly associated with predominance of fine mode particles while low values are associated with a predominance of coarse mode (e.g. Dubovik et al., 2002). Moreover, many works

(e.g. Alados-Arboledas et al., 2003; O'Neill et al., 2005; Veselovskii et al., 2009) found an inverse relationship between the Ångström exponent for extinction and the effective radius: large values of Ångström exponent are associated with low values of $r_{\rm eff}$ while just the opposite occurs for low values of Ångström exponent. Considering this, a positive bias in α (355 nm) increases the spectral difference with α (532 nm) and would increase the value of the Ångström and thus would result in a decrease in the retrieved

- particle radius. This agrees with the negative slopes of α (355 nm) observed in Fig. 2. On the other hand, a positive bias in α (532 nm) reduces the spectral difference with α (355 nm) and thus serves to decrease η_{α} . Thus, we would expect an increase in the
- ¹⁰ retrieved particle radius which agrees with the positive slopes observed for α (532 nm) in Fig. 2. The slopes of β (355 nm) and β (532 nm) possess mostly the same sign as the corresponding extinction coefficient at each wavelength, and similar logic concerning the relationship of the Ångström exponent and the particle size given for α (355 nm) and α (532 nm) can be used to explain this behavior as well. Finally, for β (1064 nm)
- we observe positive slopes ($a = 0.791 \pm 0.008$ for type I and $a = 0.54 \pm 0.07$ for type II). Positive biases of β (1064 nm) decrease the spectral difference between β (355 nm) and β (532 nm) indicating a decrease of the Ångström exponent, and thus we would expect an increase in the retrieved particle size which agrees with the presence of positive slopes in the plot.

Figure 3 presents the sensitivity analysis for the retrieval of number concentration (*N*). From Fig. 3 we again generally observe linear patterns of the deviation in retrieved value of *N* for differing biases in the input optical data. Linear fits through the origin in the forms Y = aX were also performed. Moreover, the slopes of the linear fits of the extinction coefficients present opposite signs to those determined for the retrieval of r_{eff} ,

with positive values for α (355 nm) ($a = 3.09 \pm 0.12$ for type I and $a = 4.83 \pm 0.22$ for type II) and negative values for α (532 m) ($a = -2.78 \pm 0.17$ for type I and $a = -4.09 \pm 0.23$ for type II). Therefore, to compensate for the radius enhancement the programs tends to decrease number density.

For the sensitivities of $r_{\rm eff}$ and N shown in Figs. 2 and 3, the absolute values of the slopes at α (355 nm) and α (532 nm) are larger than 1 which indicates that the deviations in the retrieved $r_{\rm eff}$ and N using biased data are larger than the bias imposed on the input optical data. Thus, the accuracy of $r_{\rm eff}$ retrievals using $3\beta + 2\alpha$ lidar is strongly dependent on the accuracy associated with the extinction coefficients. Other slopes with absolute value less than 1, as for example those obtained for $r_{\rm eff}$ as a function of biases in β (1064 nm) (0.791 ± 0.008 for aerosol type I and 0.54 ± 0.07 for aerosol type II) indicate that the retrieval is still quite sensitive to biases in β (1064 nm).

But the slopes of r_{eff} as a function of biases in the input data for β (355 nm) and β (532 nm) are quite small indicating that biases in these optical parameters have little effect on the retrieval of r_{eff} . However, for the retrieval of number concentration the effects of biases in the backscattering optical data are not negligible with absolute values of the slopes of the linear fits between 1.3 and 0.3.

As with the effective radius and number concentration, we have performed the sen-¹⁵ sitivity analysis for the other microphysical parameters obtained from the inversion of $3\beta + 2\alpha$ lidar data. For these studies, we have also observed generally linear patterns when considering the differences in the retrieved microphysical parameters as a function of the bias in the input optical data. Again, the linear patterns pass through the origin and we therefore assumed least-squares fits of the form Y = aX. The results ²⁰ of the linear fits for all the parameters are summarized in Table 1, including also the

slopes obtained for $r_{\rm eff}$ and N in Figs. 2 and 3, respectively.

We note that for some parameters the linear fit posseses different slopes for positive and negative biases $\Delta \varepsilon$. For example, in the case of r_{eff} for type II, β (532 nm) has a slope of -0.48 ± 0.02 for positive biases and 0.02 ± 0.02 for negative biases. This is

taken into account in Table 1, where, if there is a difference in slope between positive and negative biases in the input data, the slopes relating to the positive biases are indicated by (p) while those associated with negative biases are indicated by (n). We take this difference in slope to be a reflection of the reduced sensitivity to the coarse mode of the distribution. From Table 1 we observe that the number concentration is by

far the most sensitive parameter to bias in the optical data, particularly to those biases in α (355 nm) and α (532 nm). Moreover, the sensitivities to biases at β (355 nm) are generally larger for type I than for type II (absolute values of slopes are larger), which can be explained by the fact that, for the same total volume, small particles (which predominate in type I) generally provide larger backscattering of light at the shorter wavelengths (phase function at 180 is larger) (e.g. Mischenko et al., 2000; Liou, 2002; Kokhanovsky 2004).

5

Table 1 shows that the retrievals of mean radius (r_{mean}) are more sensitive to biases in α (355 nm) and α (532 nm) than to the backscattering parameters. In general for these retrievals, different slopes are observed between positive and negative biases in the input optical data, for both type I and II distributions. The largest sensitivities of r_{mean} are found for negative biases at α (355 nm) (slopes of -1.27 ± 0.07 for type I and of -3.90 ± 0.40 for type II) and for positive biases at α (532 nm) (slopes of 1.37 ± 0.03 for type I and of 3.40 ± 0.30 for type II). As before for the effective radius, the signs of the slopes obtained for α (355 nm) and α (532 nm) can be explained in terms of the relationship of particle size and Ångström exponent. However, the difference in the sensitivity of the retrieval of r_{mean} to positive and negative biases is generally explained by the lower sensitivity of the MW technique to the coarse mode of the aerosol size distribution, as previously remarked (e.g. Veselovskii et al., 2010).

From Table 1 the slopes calculated from the linear fits of surface concentration (*S*) as function of biases in the optical data present the same patterns (sign of slopes) between types I and II. The difference in the absolute values of slopes between both types are then associated with the differences in the size distribution and with the changes in the kernel functions. The largest sensitivities of *S* are found for biases at α (355 nm) (absolute values of slopes ~ 2.0). Sensitivities to biases at α (532 nm)

(absolute values of slopes between 1.07 and 0.69) are also important both for type I and II, while the sensitivity associated with β (355 nm) is only remarkable for type I (slope of -0.73 ± 0.04). Sensitivities to biases at β (532 nm) and β (1064 nm) are quite low (absolute values of slopes below 0.5).

Referring back to Table 1, we observe that the volume concentration (*V*) is the retrieved integrated parameter least affected by bias in the input optical data as indicated by the fact that most of the slopes have absolute values below 1.0. However, there are some differences between aerosol types I and II. For type I aerosols, the retrieval of volume concentration is most sensitive to biases in β (355 nm) (slope of –1.39), while for type II aerosols retrievals are most sensitive to deviations in α (532 nm) (slope of 1.18).

5

As the regularization scheme used here computes the size distribution using the range of permitted radii of 0.075–5 μ m, the fine mode part of the distribution (but not the coarse mode) is completely covered by this inversion window, and thus we study fine mode volume radius and fine mode volume concentration. Table 1 also shows the sensitivities of these two parameters to biases in the input optical data. From the slopes of the linear fits reported for $r_{\rm fine}$ only biases in α (355 nm) and α (532 nm) produce significant deviations in the retrieval, with absolute values of the slopes between 1.0 and

- ¹⁵ 1.3, while the deviations in the retrievals created by biases in other optical parameters are almost negligible. This result would imply that accurate retrievals of $r_{\rm fine}$ can tolerate rather large errors in the backscatter data but not in the extinction data. The sign of the slopes of $r_{\rm fine}$ as function of α (355 nm) and α (532 nm) can be explained by the same reasoning given before for the effective radius: as extinction at 355 nm
- ²⁰ increases, it makes the retrieved particle radius decrease. But as α (532 nm) increases the retrieved particle radius increase. On the other hand, for the fine mode volume concentration (V_{fine}), the largest sensitivities in the retrieval are found to systematic biases at α (355 nm), with slopes of 1.59 ± 0.05 and 1.66 ± 0.17 for types I and II, respectively. For the other optical parameters, absolute values of the slopes are below 0.5 (except β
- ²⁵ (1064 nm) for type I with slope of 0.62 ± 0.03). These dependencies of the sensitivities of r_{fine} and V_{fine} are associated with the different dependencies of kernel functions with wavelength and particle radius (e.g. Chapter 11 of Bohren and Huffman, 1983).

3.2.1 Effects of the constraints of the retrievals on the sensitivity test results

The sensitivity tests applied to the different sets of data have shown linear dependencies. The data presented in Table 1 of the linear fits allows the computation of the deviations induced in retrieved quantities due to biases in the input data in an easy and straightforward way. But the generality of the results needs to be examined. For example, the results presented in Table 1 have been based on a maximum radius in the inversion (r_{max}) of 5 µm. Although for the aerosol size distributions studied here this r_{max} makes the computation more efficient, the selection of r_{max} depends on the user and becomes a constraint in the inversion procedure. Thus, we performed more simulations with r_{max} increased to a value of 10 µm to study the influence of this change in constraint on the retrieved results. Another constraint in the inversion that must be checked is the maximum value allowed for m_i . We repeated the simulations allowing m_i to range up to 0.1 (consistent with a very absorbing aerosol like black carbon). The values used as the baseline in the coming comparisons were those obtained with

- $r_{max} = 5 \,\mu m$ and with maximum value of m_i of 0.01 with no induced systematic errors. The new simulations performed after changing the constraints for r_{max} and maximum m_i also reveal linear patterns. However, these linear patterns do not pass through the origin implying that there are generally shifts in the retrieved values of the various parameters due to these changes in constraints. The analysis reveals, though, that the signs of the slopes of the linear fits remain the same and that very similar deviations in the retrieved quantities are computed using the linear fits performed, either with the baseline results or with those retrieved with the different constraints. Therefore, while the selection of exact value of the constraints for r_{max} and m_i can change the mean values of the slopes retrieved for different parameters, the sensitivity to induced biases in the input optical data is generally unchanged by these changes in constraints.
- ²⁵ in the input optical data is generally unchanged by these changes in constraints.

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3.2.2 Additive properties of the effects of systematic errors in the optical data

Thus far, the sensitivity tests that have been performed were based on perturbing a single optical input at a time. But in a real instrument, it is quite possible that two or more input data might be influenced by biases simultaneously. Given those biases, if known, should be and would be corrected for (GUM, 2009), we need to study the effects of the presence of multiple simultaneous biases in the input data since the existence of such biases would presumably not be known in a real application. In other words, we wish to determine if the preceding results based on perturbing a single optical input at a time can be generalized to predict the effects of multiple input data to being simultaneously biased. In particular, we will now test if, when multiple inputs are simultaneously biased, the results from Table 1 can be used to calculate deviations that can simply be added to determine the total bias, that is, we test whether the results in Table 1 can be considered additive. To do that we performed a set of simulations perturbing at least two optical channels by biases of the same magnitude, although

- different combinations of over/under estimations are allowed. The deviations noted as "baseline" were computed using the slopes of Table 1 and assuming that the deviations are additive. We also performed the regularization retrieval with the new set of data affected by two or more simultaneous biases, called "simulated deviations". Later we computed the differences in the microphysical properties based on the slopes given in
- Table 1 and those actually retrieved running the code with the new biased optical data. For the effective radius, the relative differences between the "baseline" and "simulated" deviations, considering the "baseline" values as the reference, are shown in Fig. 4. Box-Whisker plots are used for multiple simultaneous biases in the optical data of 1, 2, 5 and 10%. In these box diagrams the mean is represented by an open square. The
- ²⁵ line segment in the box is the median. The top limit represents the 75th percentile (P75) and the bottom limit the 25th percentile (P25). The box bars are related to the 1st (P1) and 99th (P99) percentiles, and the crosses represent the maximum and minimum values respectively. From Fig. 4, for biases of 1, 2, 5 and 10% mean values of the

differences in the effective radius are very small: 0.03, 0.34, 0.41 and 1.01 % for type I (Fig. 3a) and -0.62, -0.91, -0.49 and -0.18 % for type II (Fig. 3b). Values larger than the 25th percentiles (P25) and lower than the 75 % percentiles (P75) are found for the ranges from -1.8 % to 1.3 % (type I) and from -0.6 % to 4.4 % (type II). Only two

- ⁵ outliers are found with relative differences greater than 100%. This last occurs when all the optical channels except β (355 nm) are either overestimated or underestimated. But for these particular cases the baseline deviations are 0.009% or -0.009%, while the simulated ones are 0.557% and -0.557% respectively. These small errors are within the uncertainties associated with the regularization method, and thus these large
- ¹⁰ relative differences are a mathematical artifact created by dividing by small numbers. Moreover, tests have also been performed for the other microphysical parameters and we also found an additive property in the deviations predicted by the results shown in Table 1. Therefore, we conclude that the results of Table 1 can be reliably used to calculate the deviations in retrieved quantities due to multiple simultaneously biased ¹⁵ input data.

We take this result to be an indication that the solutions found by the inversion technique generally define a local minimum in the multi-dimensional solution space. The linear behavior of the deviations in the retrieval due to small changes in the input parameters is a characteristic of displacements from this minimum location. Multiple simultaneous displacements tend also to display this linear behavior. The results here indicate, therefore, that for biases in the input data of up to 20 %, whether for a single channel or multiple ones simultaneously, the solution space possesses linear properties and an additive behavior can be assumed.

3.3 Application to the sensitivity of retrievals to the presence of random errors in the optical data

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Up to this point, we have concerned ourselves only with the effects of biases in the input optical data on retrieved quantities. But in lidar systems random errors are also present as for example due to noise in the detectors. Any specific set of 3 + 2 data affected by

random errors can be considered as a set of biased measurements where the individual biases for each of the data follow a normal distribution. Given the additive property of the systematic errors that we have shown, we can assess the effects of random errors in the optical data by generating random biases in the optical data and computing their deviations in the microphysical parameters from the values given in Table 1. The sensitivities of the regularization technique to those random errors computed using the

procedure just outlined will be compared with previously published ones (e.g. Müller et al., 1999a, b; Veselovskii et al., 2002, 2004).

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To assess the sensitivity of the retrievals to random errors based on the additivity of systematic bias of different magnitudes and signs, we have generated a random set of 50 000 biased $3\beta + 2\alpha$ optical data consistent with varying amounts of Gaussian distributed noise and used the slopes of Table 1 to compute the distribution of the various retrieved parameters. As an illustration, Fig. 5 shows the frequency distribution of the errors in r_{eff} , N, S, V, r_{fine} and V_{fine} respectively, both for aerosol size distributions type I and II, where 15 % random error is assumed in all the optical data.

From Fig. 5 we observe that the frequency distributions possess the expected Gaussian shape for all the microphysical parameters. Most of the frequency distributions are centered essentially at zero, although some departures from this value are observed which means that random errors can induce systematic biases in the retrieved aerosol microphysical parameters. The mean values of the distributions are given in the leg-

- ²⁰ microphysical parameters. The mean values of the distributions are given in the legend. A shift in the mean value due to the presence of random error results for those retrieved parameters that display a different linear tendency for positive and negative biases in the input optical data. For example, such departures from zero are observed for retrievals of $r_{\rm eff}$, N and V for type II aerosols and are approximately -5, 1, and -7%,
- ²⁵ respectively. On the other hand, the FWHM or standard deviations of normal distributions of Fig. 5 are representative of the sensitivities to random errors in the optical data. Generally, there are many similarities in the standard deviations between aerosol types I and II. We observe clearly that *V*, r_{fine} and V_{fine} exhibit the smallest sensitivity to the imposed 15% random errors with a 1-sigma spread in the result of approximately

25%. The effective radius and surface concentration results show moderate sensitivity with 1-sigma values of ~ 30–40%, while number concentration has the highest sensitivity, with 1-sigma values of 67.6% for type I and 95.2% for type II. As expected, these sensitivities to random error track the results of the sensitivities to systematic errors,
 where the most sensitive parameter was also found to be number concentration and

the least were volume concentration, fine mode radius and volume concentration.

Using the same procedure as for 15% random error, Table 2 reports the FWHM –or standard deviations- of normal distributions obtained for other magnitudes of random errors in the optical data ranging from 5% to 20%. We observe, as expected from the linear functions involved, that increasing the random uncertainty increases

- ¹⁰ from the linear functions involved, that increasing the random uncertainty increases the deviations found in a linear fashion. Moreover, it is observed again that the largest sensitivities are for *N* while the lowest are for *V*, r_{fine} and V_{fine} . In the same way, Table 3 reports the means of the deviation of every microphysical property for varying amounts of random uncertainty in the input data. As mentioned above, the departures
- of these deviations from zero indicate that random uncertainties in the input optical data can induce varying amounts of systematic bias in the retrieved properties. This effect is found more with the type II aerosols that have a higher fraction of larger particles. Such a population is more likely to have different slopes in Table 1 due to positive and negative biases in the input optical data because of the reduced sensitivity of the
- ²⁰ MW technique to the larger particles. It is this reduced sensitivity to larger particles that in general explains the shifting of the mean values in the retrieved distributions due to varying amounts of random error in the input data.

Studies by Müller et al. (1999a, b) and Veselovskii et al. (2002, 2004) reported that for 10% random uncertainties in the optical data in the $3\beta + 2\alpha$ lidar configurations

²⁵ the retrieved uncertainties were on the order of 25 % for r_{eff} , *V* and *S*, 30 % for r_{mean} and 70 % for *N*. These values are quite similar to those reported in Table 2 for our computations of 10 % random errors. No evaluations for r_{fine} and V_{fine} were done in the studies of Müller et al. (1999a, b) and Veselovskii et al. (2002, 2004).

3.3.1 Application to instrument specification

The upcoming space-borne Decadal Survey ACE (Aerosol-Cloud-Ecosystems) mission of NASA (http://dsm.gsfc.nasa.gov/ace/) specifies a High Spectral Resolution Lidar as a core instrument to measure vertical-profiles of aerosol extinction and backscat-

- ⁵ tering worldwide. These profiles will be used to derive vertically-resolved aerosol microphysical properties such as effective radius, number concentration or complex refractive index. The system is anticipated to use the $3\beta + 2\alpha$ configuration reported here. The first preliminary reports call for an accuracy of ±15% for all backscattering and extinction coefficients, and thus the results presented here can be used to infer
- ¹⁰ the anticipated uncertainties in the microphysical properties retrieved using the regularization technique on these $3\beta + 2\alpha$ space borne data. The results clearly indicate, however, that for most quantities it is uncertainties in the extinction coefficients that need to be constrained more carefully than those in the backscattering data. Volume concentration is an interesting exception to this statement where β (355 nm) for type I
- ¹⁵ aerosols is the optical parameter requiring the smallest uncertainty budget to help reduce the uncertainties in retrievals. In this way, the results here can serve as a guide to hardware designers of multi-wavelength lidar instruments in the sense that if trade-offs need to be made between the performance of one optical channel versus another, the relative sensitivities shown in Table 1 can be used to assess which channels would
- ²⁰ benefit most from decreased uncertainty in the measurements. Another application of the sensitivities derived here is to algorithm development. Algorithms can introduce systematic uncertainties in the optical data such as through an incorrect assumption of an aerosol free region, an assumption of the extinction to backscatter ratio or the use of an estimated molecular profile. The tolerance for both random and systematic errors
- ²⁵ in the input optical data due both to instrumentation and to algorithms can be assessed once uncertainty requirements in the retrieved quantities are established.

4 Summary and conclusions

We have presented the results of a study of the sensitivity of the retrievals of aerosol physical parameters using the regularization technique to systematic and random uncertainties in the input optical data. We have focused our study on the set of data

- ⁵ consisting of three backscattering coefficients (β) at 355, 532 and 1064 nm and two extinction coefficients (α) at 355 and 532 nm (3 β + 2 α configuration). These data can be obtained by a lidar system that uses a Nd:YAG laser and combines backscatter with Raman or HSRL channels. Simulations have been done for two different aerosol size distributions; one with fine mode predominance (type I) and the other with a mixture
- fine and coarse modes (type II). Optical data consistent with these size distributions were generated using Mie theory. Retrievals were performed using these baseline optical data. The optical data were then perturbed by systematic biases in the range ± 20 % to study the effects of biases on the retrieved parameters. As the problem of the inversion of microphysical properties is under-determined, we had to use constraints.
- ¹⁵ Particularly, we have found that the range of radius and refractive index used in the inversion did not have a large influence on the sensitivities of the different microphysical particles. However, our results showed that the maximum value of m_i allowed in the retrieval had a significant influence on the value of refractive index retrieved, supporting earlier results indicating significant uncertainties in the retrieval of refractive index 20 using the $3\beta + 2\alpha$ MW lidar technique studied here.

The microphysical parameters studied included effective radius (r_{eff}) and volume (V), surface (S) and number (N) concentration. Additionally, as the inversion window ranged from 0.075 to 5 µm, we were able to study the fine mode of the aerosol size distribution (0.075–0.5 µm) separately, and thus we have also presented the results for both fine mode radius (r_{fine}) and volume (V_{fine}). From these sensitivity tests, the percentage deviations of the microphysical parameters as function of biases in the optical data presented linear patterns. Generally, these linear patterns presented the same sign of slopes between aerosol type I and II and the largest sensitivities were observed for

biases in α (355 nm) and α (532 nm). Moreover, the largest sensitivities were found for N, while the least affected parameters were V, r_{fine} and V_{fine} .

An important result is that we have found an additive property for the deviations induced by the biases in the optical data. This implies that if, for example, several optical data are simultaneously affected by systematic errors, the total deviation in the retrieved quantity can be well approximated by the sum of those deviations computed when each optical input was biased separately. From this additive property, we have been able to compute the effects of random errors in the optical data. The largest sensitivities to random errors were found for *N*, while the lowest were obtained for *V*, r_{fine} and V_{fine} . Moreover, we have found some systematic differences in the mean retrieved microphysical properties when the retrievals are affected by random errors

- in the input optical data. The presence of these systematic differences is associated with the different behavior (although with linear patterns) between positive and negative biases in the input optical data.
- ¹⁵ The result of the sensitivity tests obtained here can be used to establish acceptable error budgets in optical data if maximum permissible errors in the retrieved quantities can be established. For example, for the Decadal Survey ACE mission a multiwavelength lidar is planned. Among their measurement requirements is that the accuracy of the optical data should be ± 15 %. If these uncertainties are taken to be all random, we are able to use the results here to estimate that this implies an uncertainty in the retrieved microphysical properties by the regularization technique of ~40 % for $r_{\rm eff}$, ~85% for *N*, ~25% for *S*, ~20% for *V*, 16% for $r_{\rm fine}$ and $V_{\rm fine}$ respectively. The results also permit assessing the deviations in the retrievals if the biases in the opti-
- results also permit assessing the deviations in the retrievals if the biases in the optical data are systematic and exist in only one or more channels. In this way, trade-off decisions can be made between the retrieval requirements and the hardware config-
- decisions can be made between the retrieval requirements and the hardware configuration of a lidar system taking into account the different sensitivities of the retrievals to biases in the optical data of different channels. We hope these results aid the future design of multi-wavelength lidar systems intended for retrieval of aerosol microphysical properties.

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Table 1. Percentage deviations in the aerosol microphysical properties as a function of systematic errors in the optical data ε . Particularly the slopes *a* of the linear fits Y = aX are presented, where *X* is the systematic bias in the optical data and *Y* is the corresponding deviation in the microphysical properties. All these fits presented linear determination coefficient $R^2 > 0.90$. For the cases when there is a difference in slope between positive and negative biases in the input data, the slopes relating to the positive biases are indicated by (p) while those associated with negative biases are indicated by (n).

α (355 nm)		355 nm) α (532 nm)			5 nm)	β (53	2 nm)	β (1064 nm)		
Type I	Type II	Type I	Type II	Type I	Type II	Type I	Type II	Type I	Type II	
-1.68 ± 0.12	-1.74 ± 0.03	1.51 ± 0.04	1.82±0.09	-0.63 ± 0.02	-0.54(p) $-0.18(n) \pm 0.01$	0.27 ± 0.04	-0.48(p)/ $0.02(n) \pm 0.02$	0.791 ± 0.008	0.54 ± 0.07	
-0.15(p)/ -1.27(n) ± 0.07	$-0.80 \pm 0.04(p)/$ $-3.9 \pm 0.4(n)$	1.37(p)/ $0.58(n) \pm 0.03$	$3.4 \pm 0.3(p)/$ $0.97 \pm 0.07(n)$	0.45(<i>p</i>)/ 0.19(<i>n</i>) ± 0.05	0.02(p)/ -0.17(n) ± 0.03	-0.33(p)/ $-0.86(n) \pm 0.04$	0.09 ± 0.02	-0.21(p)/ $-0.09(n) \pm 0.01$	-0.21 ± 0.02	
3.09±0.12	4.83 ± 0.22	-2.78 ± 0.17	-4.09 ± 0.23	$-1.25 \pm 0.04(p)/$ $-0.85 \pm 0.15(n)$	0.19(p)/ $0.12(n) \pm 0.04$	1.3±0.09	$\begin{array}{c} 0.79 \pm 0.11(p) / \\ -0.37 \pm 0.05(n) \end{array}$	0.37 ± 0.05	0.29(<i>p</i>)/ -0.25(<i>n</i>) ± 0.05	
2.08 ± 0.05	1.77 ± 0.04	-1.07 ± 0.08	-0.69 ± 0.03	-0.73 ± 0.04	-0.22(p)/ $-0.04(n) \pm 0.02$	0.51 ± 0.03	0.05 ± 0.02	0.17 ± 0.02	0.04 ± 0.02	
0.26(<i>p</i>)/ 0.77(<i>n</i>) ± 0.07	-0.37(p)/ $0.35(n) \pm 0.05$	0.44 ± 0.12	1.18±0.17	-1.39 ± 0.04	-0.48 ± 0.10	0.77 ± 0.05	-0.38(p)/ $0.03(n) \pm 0.03$	0.92 ± 0.04	0.58 ± 0.05	
-0.99 ± 0.11	-1.27±0.17	1.17 ± 0.04	1.28±0.07	-0.01(p)/ $-0.06(n) \pm 0.01$	0.33(<i>p</i>)/ 0.06(<i>n</i>) ± 0.03	-0.05(p)/ $-0.22(n) \pm 0.03$	-0.11 ± 0.02	-0.17 ± 0.01	-0.28 ± 0.02	
1.59 ± 0.05	1.66 ± 0.17	-0.28 ± 0.05	-0.44 ± 0.04	-0.62 ± 0.03	0.26(p)/ -0.01(n) ± 0.01	0.22 ± 0.02	-0.11(p)/ -0.34(n) ± 0.01	-0.04 ± 0.01	-0.15(p)/ -0.34(n) ± 0.02	

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Table 2. Standard deviations of the frequency distributions of the deviation induced in the microphysical parameters due to random errors in the optical data.

Random	Random r _{eff}		1	V		S		V	r _f	ine	V	fine
Errors (%)	Type I	Type II	Type I	Type II	Type I	Type II	Type I	Type II	Type I	Type II	Type I	Type II
5	12.5	13.1	22.5	31.8	12.5	9.5	9.8	7.2	7.7	9.2	8.7	8.8
10	24.9	26.2	45.0	63.6	25.1	19.1	19.6	14.4	15.5	18.4	17.4	17.6
15	37.2	39.2	67.6	95.2	37.7	28.5	29.5	21.5	23.3	27.6	26.1	26.3
20	50.0	52.6	90.1	127.3	50.2	38.2	39.3	28.8	31.1	36.9	34.9	35.2
10*	25*		7	0*	2	5*	2	5*		_		_

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* From the previous work of Muller et al. (1999a,b) and Veselovskii et al. (2002, 2004).

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Table 3. Mean of the differences (in percentages) in the retrieved microphysical parameters due to varying amounts of random error in the optical data.

Random		r	eff		V		S		/	r _f	ine	V _f	ine
E	Errors (%)	Type I	Type II	Type I	Type II	Type I	Type II						
5	5	0.0	-1.7	-0.8	3.5	0.0	-0.4	-1.1	-2.3	0.4	0.5	0	1.4
1	0	0.0	-3.5	-1.4	7.1	0.1	-0.7	-1.9	-4.4	0.9	1.1	0.1	2.8
1	5	-0.1	-5.3	-1.9	11.1	0.3	-0.9	-2.8	-6.7	1.2	1.4	0.2	4.2
2	20	-0.3	-7.2	-2.3	15.2	0.6	-1.0	-3.8	-9.0	1.5	1.8	0.4	5.8

Fig. 1. Size distributions used for computing the simulated optical data. We have normalized the volume of the coarse mode such that $V_{tf} = 1$. Therefore, we have mode $V_{tc} = 0.5$ for aerosol type I and mode $V_{tc} = 5$ for aerosol type II.

Fig. 3. Percentage deviation of the number concentration as a function of systematic bias in the optical data (ε). (a) Type I. (b) Type II.

Fig. 4. For the effective radius, Box-Whisker diagrams of the differences between the theoretical deviations computed with the slopes of Table 1 and the simulated deviations. At least two optical channels have been simultaneously perturbed by biases of the same magnitude although different combinations of over/under estimations are allowed. In these box diagrams the mean is represented by an open square. The line segment in the box is the median. The top limit represents the 75th percentile (P75) and the bottom limit the 25th percentile (P25). The box bars are related to the 1st (P1) and 99th (P99) percentiles, and the crosses represent the maximum and minimum values respectively. We used biases in the optical data of 1% (black diagrams), 2% (blue diagrams), 5% (red diagrams) and 10% (green diagrams).

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Fig. 5. Frequency distributions of the different microphysical parameters for 15% random errors in the optical data using 50 000 random samplings of the systematic error sensitivities shown in Table 1. Random errors were simulated by a normal distribution centred at zero and with standard deviation of 15%. The random number generator is initialized at different values for each of the 5 optical data used in the $3\beta + 2\alpha$ lidar configuration. The mean value of the deviation between the microphysical parameter affected by random error and that unaffected by random error is included in the legend.

