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Tropospheric profiles of wet refractivity and humidity from the combination of remote sensing datasets and measurements on the ground

F. Hurter¹ and **O.** Maier²

 ¹Geodesy and Geodynamics Laboratory, Institute of Geodesy and Photogrammetry, ETH Zurich, Switzerland
 ²Federal Office of Meteorology and Climatology MeteoSwiss, Station aérologique, 1530 Payerne, Switzerland

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Correspondence to: F. Hurter (fhurter@phys.ethz.ch)

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Abstract

We reconstruct atmospheric wet refractivity profiles for the western part of Switzerland with a least-squares collocation approach from datasets of (a) zenith path delays that are a byproduct of the GPS (Global Positioning System) processing, (b) ground me-

- teorological measurements, (c) wet refractivity profiles from radiooccultations whose tangent points lie within the study area, and (d) radiosonde measurements. Wet refractivity is a parameter partly describing the propagation of electromagnetic waves and depends on the atmospheric parameters temperature and water vapour pressure. In addition, we have measurements of a lower V-band microwave radiometer at Payerne.
- It delivers temperature profiles at high temporal resolution, especially in the range from ground to 3000 m a.g.l., though vertical information content decreases with height. The temperature profiles together with the collocated wet refractivity profiles provide nearcontinous dew point temperature or relative humidity profiles at Payerne for the study period from 2009 to 2011.
- In the validation of the humidity profiles, we adopt a two-step procedure. We first investigate the reconstruction quality of the wet refractivity profiles at the location of Payerne to wet refractivity profiles computed from radiosonde profiles available for that location. We also assess the individual contributions of the datasets to the reconstruction quality and demonstrate a clear benefit from the data combination. Secondly, the
 accuracy of the conversion from wet refractivity to dew point temperature and relative humidity profiles with the radiometer temperature profiles is examined, comparing them also to radiosonde profiles.

For the least-squares collocation solution combining GPS and ground meteorological measurements, we achieve the following error figures with respect to the radiosonde reference: maximum median offset of relative refractivity error is -16% and quartiles are 5% to 40% for the lower troposphere. We further added 189 radiooccultations that met our requirements. They mostly improved the accuracy in the upper troposphere. Maximum median offsets have decreased from 120% relative error to 44% at 8km





height. Dew point temperature profiles after the conversion with radiometer temperatures compare to radiosonde profiles as to: absolute dew point temperature errors in the lower troposphere have a maximum median offset of –2K and maximum quartiles of 4.5K. For relative humidity, we get a maximum mean offset of 7.3%, with standard ⁵ deviations of 12–20%.

We demonstrate in this study that least-squares collocation is capable of combining humidity related datasets such that resulting humidity profiles gain from complementary strengths of the various measurement methods. Since the datasets are operational and in near-realtime available, we envisage collocation to be a possible tool for nowcasting of clouds and rain and to understand processes in the boundary layer and at its top.

1 Introduction

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Up to this date, several techniques have been developed to remotely monitor the atmospheric water vapour, being a key variable in numerical weather prediction models. Among these are e.g. microwave radiometer, differential absorption lidar, raman lidar, solar spectrometer and radiooccultation measurements. Furthermore, GNSS (Global Navigation Satellite System) receivers are able to deliver an integral measure of water vapour content at temporal resolution of at least 30 min (Bender et al., 2011a). This measure is defined by the delay of the electromagnetic wave that travels from the satellite through the atmosphere to the GNSS receiver. It includes the total influence of
 the atmosphere along its path, also that of the water vapour. With sophisticated soft-

- the atmosphere along its path, also that of the water vapour. With sophisticated software packages, the delay can be retrieved at each GNSS station. To obtain a profile of atmospheric water vapour from the delays, a GNSS receiver network, ground meteorological stations and profiles of atmospheric air temperature are needed. There are many studies that have used a tomographic approach to reconstruct humidity fields from CNSS delays. They either proceed a path delays from stations of permanent CNSS.
- from GNSS delays. They either process path delays from stations of permanent GNSS networks (Perler et al., 2011), or from campaign setups, as in the ESCOMPTE experiment in France (Champollion et al., 2005; Nilsson et al., 2007; Bastin et al., 2007).





Further works that exploit the tomographic approach are and Gradinarsky (2006), Bender et al. (2009, 2011b), Rohm and Bosy (2011), Bosy et al. (2012), Manning et al. (2012) and Rohm (2013).

In this paper, the GPS (Global Positioning System) zenith delays from permanent

- GNSS stations are taken as the basis to monitor the atmospheric water vapour above Payerne, Switzerland, the MeteoSwiss launch site of operational radiosondes. We motivate our choice for GPS path delays as primary dataset with its good time resolution, its all-weather capability, the stable and high data availability, low maintenance and the fact that financing can be shared with other applications (e.g. GNSS reference networks
- for positioning). The integral measures of several GPS receivers are interpolated to profiles of so-called wet refractivity (N_{wet}), which depends on both atmospheric temperature and water vapour pressure. For the interpolation, we employ an algorithm termed least-squares collocation. It incorporates a deterministic trend function and fits this function together with statistical parameters to the data that can be of many different
- types. Herein, we make use of the integral measures from GPS and of point measurements from ground meteorological stations, radiooccultations and from radiosondes. Temperature profiles from a lower V-band (51–58 GHz) microwave radiometer (Löhnert and Maier, 2012) in Payerne allow the conversion of wet refractivity profiles into vertical profiles of dew point temperature and relative humidity at the radiometer location.
- In Sect. 2, we describe the datasets used in this study. Section 3 explains the leastsquares collocation algorithm used to derive profiles of wet refractivity and explains how the datasets of integral and point measurements can be combined into a common collocation. We then demonstrate in Sect. 4 the performance of the algorithm with 3 yr of data that is validated against the radiosonde, whose launch site is in Payerne. We
- also show the beneficial effect of the dataset combination. Eventually, Sect. 5 sets the findings into the context of other humidity reconstruction and measurement techniques and of numerical weather prediction.





2 Description of datasets

This study makes use of data from January 2009 to December 2011 (Table 1) at the aérological station of Payerne and locations within \approx 100 km distance. The GPS data, being the main source of information for the spatial distribution of humidity in our study,

⁵ and further datasets such as ground meteorological data, radio-soundings, radiooccultations and vertical temperature profiles from the ground-based microwave radiometer that complete the retrieval of humidity from wet refractivity, are detailed in the following.

2.1 GPS zenith path delays

GNSS satellites transmit electromagnetic waves in the L-band, which travel from the satellite's orbit position to the receiver on the earth's ground. On its way across the atmosphere, the waves get bent and slowed down, causing a delay in the arrival at the receiver. The parameter called refractivity describes the propagation of radiowaves and can be well determined for the neutral part of the atmosphere from basic thermodynamic parameters at any point in space and time where measurements of these parameters are available (Essen and Froome, 1951):

$$N_{\text{tot}} = N_{\text{dry}} + N_{\text{wet}} = k_1 \cdot \frac{p_{\text{d}}}{T} + k_2 \cdot \frac{e}{T} + k_3 \cdot \frac{e}{T^2}$$

with the two contributions to total refractivity N_{tot} being

$$N_{\text{dry}} = k_1 \cdot \frac{p_{\text{d}}}{T}$$
$$N_{\text{wet}} = k_2 \cdot \frac{\theta}{T} + k_3 \cdot \frac{\theta}{T^2}$$

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 $k_1 = 77.6890 \,\mathrm{Kh} \,\mathrm{Pa}^{-1}$ $k_2 = 71.2952 \,\mathrm{Kh} \,\mathrm{Pa}^{-1}$

Discussion Paper AMTD 6, 4895-4940, 2013 **Tropospheric wet** refractivity and humidity profiles Discussion Pape from data fusion F. Hurter and O. Maier **Title Page** Introduction Abstract Discussion Paper Conclusions References Figures Tables (1) (2)Back Close **Discussion** Paper (3) Full Screen / Esc Printer-friendly Version Interactive Discussion

 $k_3 = 375463 \text{ K}^2 \text{ h Pa}^{-1}$ p_d : dry air pressure [h Pa]

- e : water vapour pressure [hPa]
- 5 *T* : air temperature [K]

where k_1 , k_2 , and k_3 are empirically determined constants that have been reported by many researchers. For our investigations, we use the values estimated by Rüeger (2002). Since p_d , e, and T are functions of space and time, also N_{tot} depends on position and time. For reasons of simplicity, we will always assume $N_{tot} = N_{tot}(x, y, z, t)$. Refractivities are in units of ppm or mm km⁻¹, which expresses the delay caused by the neutral atmosphere per kilometer of propagation path. The integral of the refractivity N_{tot} along the propagation path *s* from satellite *q* to receiver *r* yields the total propagation delay Δ^{PD} .

$$\Delta^{\text{PD}} = 10^{-6} \int_{q}^{r} N_{\text{tot}} \mathrm{d}s \tag{4}$$

There is such a delay for each satellite-receiver pair. If they were to be estimated individually by a GNSS processing software, the number of unknown parameters would be too large and their correlation to other parameters too strong to be properly handled. Mapping functions are introduced that project all delays for a station onto a common ²⁰ zenith direction. The mapped delays are then averaged producing one atmospheric parameter at a time, the so-called total zenith path delay (ZTD). Traditionally, the total zenith path delay is split into a slowly varying dry (ZDD) and a more variable wet (ZWD) part, corresponding to the integrals of N_{dry} and N_{wet} , respectively. The path integral of the refractivities in zenith direction then becomes the total zenith delay:



ZTD = ZDD + ZWD	
$\approx 10^{-6}$ \int	$N_{\rm dry, average} + N_{\rm wet, average} ds$
zenith directio	

where $N_{dry,average}$ and $N_{wet,average}$ represent horizontal averages in a cone around the receiving antenna and temporal averages over the epochs used in the GNSS processing. Apart from 31 April 2011 00:00:00 UTC to 4 June 2011 23:50:00 UTC where some problems in storing the data occured (E. Brockmann, personal communication,

- some problems in storing the data occured (E. Brockmann, personal communication, 2012), 3 yr of hourly ZTDs were provided by swisstopo, the Swiss Federal Office of Topography (Table 1). Figure 1 shows the considered GNSS receivers, which belong to the Automated GNSS Network for Switzerland (AGNES). They are distributed over an area of 125 km × 125 km around Payerne and have an average inter-station distance of
- 30 km. Some stations also recorded data from the Russian global navigation satellite system GLONASS, but only the American Global Positioning System (GPS) was used to derive the zenith total path delays for this study. In the following, we will thus use GPS synonymously to GNSS. The processing carried out by swisstopo is based on the same procedure as described in Perler et al. (2011), or in more detail in Perler (2011),
- and uses the Bernese GNSS Software Version 5.0 (Dach et al., 2007). Mapping functions applied are dry Niell for the apriori part of the troposphere and wet Niell for the estimated part. Together, they form the total zenith path delays that are determined by the software once per hour. In between, the temporal change of the troposphere is modeled with a piecewise linear function. The rapid orbits from the International GNSS
- ²⁰ Service (IGS) have been used in the processing allowing near real-time applications of the GPS path delays. They have been shown to have accuracies good enough for meteorological applications (Lutz, 2009).



(5)



2.2 Meteorological ground stations

From the permanent and automatic ground meteorological measurement network called SwissMetNet of the Swiss Federal Office of Meteorology and Climatology (MeteoSwiss), 14 to 19 stations within the perimeter of study were concurrently measuring
⁵ pressure, temperature and relative humdity during the 3 yr of our investigation (Table 1). Figure 2 displays the considered ground meteo stations and Fig. 3 the height distribution of these stations, together with the GPS stations. Uncertainties given in Table 2 are from general working experience with these sensors and correspond to their achievable measurement uncertainties that have been listed in CIMO Guide (2008).

10 2.3 Radiosonde profiles in Payerne

The radiosonde data comprises profiles from 3 yr of continuous operation (Table 1) at the Payerne aéorological station of MeteoSwiss. Most days contain 2 launches that reach the tropopause at 00:00:00 UTC and 12:00:00 UTC, roughly 1 h after launch. Exceptional days include a third sounding at 18:00:00 UTC. The parameters that are important for this study and are contained in the original data are shown in Table 2. Also shown in Table 2 are respective sensor uncertainties as given by Löhnert and Maier (2012). They comply with the working experience at MeteoSwiss and with the experience gained from intercomparison with other radiosonde systems (Nash et al., 2011).

20 2.4 Radiooccultations

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From the COSMIC Data Analysis and Archive Center (CDAAC, Version 4.0), postprocessed data products of radio occultations (ro in Tables 1 and 2) taking place during 2009–2011 and restricted to the investigation area (Fig. 1) were downloaded. They constist mostly of data from the COSMIC mission, but also occultations from the GRACE, the MetOp-A, the SACC and the TerraSar-X missions are included. Processing flow of





these data is outlined in Ho et al. (2009) and Kuo et al. (2004). From the data product *wetPrf*, containing water vapour pressure and temperature profile data from a variational analysis of total refractivity (described in VARS Documentation), profiles of wet refractivity (Eq. 3) were calculated up to a maximum height of 11 km. For uncertainty measures, the uncertainties from the product *atmPrf* were taken. Approximate values are given in Table 2. For the middle to upper troposphere they are consistent with the values given in Kuo et al. (2004) of roughly 0.3–0.5% or in Scherllin-Pirscher et al. (2011) of roughly 0.5% relative total refractivity uncertainty. For the lower troposphere they give tentative relative uncertainties of $\approx 5\%$, which do not match the values in *atmPrf*, being most likely too optimistic. For the region in the lower troposphere, where the formal uncertainties failed to be calculated, a default value of 1 ppm was adopted and needs further refinement in the future. However, all these uncertainties refer to total refractivity, being the sum of dry and wet refractivity according to Eq. (1) and hence, are only approximate measures of wet refractivity uncertainty. They are considered to be

¹⁵ conservative for at least the middle and the upper troposphere, where the variational analysis is successfully extracting temperature and dry pressure (Scherllin-Pirscher et al., 2011), but probably too optimistic for the lower troposphere. Positions of the occultation profiles have been taken along the longitude and latitude of the tangent points from the operational processing, being a good approximation of the true tangent point trajectories from ray-tracing (Foelsche et al., 2011).

2.5 Ground-based microwave radiometer for temperature profiling

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Profiles of temperature at Payerne from ground-based microwave radiometry (mwr in Table 1) have been provided by the CN-MET (Centrale Nucléaire et Météorologie) network of MeteoSwiss. A longer period of maintenance from 8 May 2009 07:10:00 UTC to 17 September 2009 12:50:00 UTC (Löhnert and Maier, 2012) and some smaller pe-

riods of missing data are the only datagaps in an otherwise continous 3 yr dataset. The deployed device is the microwave profiler system HATPRO (Humidity And Temperature PROfiler) whose original data output are brightness temperatures in the V-band with





seven channels ranging from 51 to 58 GHz. A detailed description of the system can be found in Löhnert and Maier (2012). All-weather data is used, including precipitation events. Unlike Löhnert and Maier (2012), bias was removed simply by retrieving a mean temperature difference to radiosonde at each height level for the years 2009–
 2011 and applying this difference to individual radiometer profiles.

3 Retrieval of wet refractivity and humidity profiles

There are a number of applications, where we need to know the atmospheric state at various locations that do not coincide with actual measurement locations. To interpolate and extrapolate such quantities to arbitrary locations from real meteorological mea¹⁰ surement stations, the software package COMEDIE was developed at the Geodesy and Geodynamics Lab at ETH Zürich, Switzerland (e.g. Eckert et al., 1992a,b; Hirter, 1998; Troller, 2004). COMEDIE is equiped with a least-squares collocation algorithm that had its main geophysical application in the estimation of gravity anomalies from various types of different measurements, such as the gravitational potential, the gravi¹⁵ tational force or the deflection of the vertical (Moritz, 1978). Several processing steps in

this study rely on COMEDIE. Above all, the reconstruction of wet refractivity profiles at Payerne from ZWDs and, in a more advanced version of the algorithm, from the combination of ZWDs with N_{wet} from point measurements, are carried out with COMEDIE. A short theoretical description of the least-squares collocation is given in this section.

20 3.1 Least-squares collocation algorithm

We have measurements *I* (Fig. 4) that are adjusted in the least-square sense to a deterministic part f(u, x, t), and to stochastic parts *s* and *n* (modified after Troller, 2004):

 $l = f(\boldsymbol{u}, \boldsymbol{x}, t) + s + n$

where:





(6)

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- f(u, x, t): function describing general field of measured values
- *u*: unknown parameters
- *x*,*t* : coordinates in space and time
- s: stochastic parameter $s \sim \mathcal{N}(0; \mathbf{C}_{ss})$
- *n*: stochastic parameter $n \sim \mathcal{N}(0; \mathbf{C}_{nn})$

The deterministic part is a function that describes the general shape of the measurements (Fig. 4). We employ the following deterministic functions for dry air pressure p, water vapour pressure e and ZWD:

⁵
$$p(x, y, z, t) = [p_0 + a(x - x_0) + b(y - y_0) + c(t - t_0)] \cdot e^{-\frac{z}{H}}$$
 (7)

$$e(x, y, z, t) = \left[e_0 + a(x - x_0) + b(y - y_0) + c(t - t_0)\right] \cdot e^{-\frac{z}{H}}$$

$$ZWD(x, y, z, t) = [ZWD_0 + a(x - x_0) + b(y - y_0) + c(t - t_0)] \cdot e^{-\frac{z}{H}}$$

- x_0, y_0, t_0 : coordinates of reference point and reference time
- x, y, z, t: cartesian coordinates and time
- p_0, e_0, ZWD_0 : pressure, water vapour pressure and ZWD at reference position and time

H, a, b, c: scale height, and gradient parameters in x, y, and z direction, respectively

The covariance matrix C_{ss} of the stochastic parameter *s* is described with an analytical covariance function showing spatial and temporal dependencies between measurements. In the literature, it is also termed the signal part of the measurements. The henceforth used covariance function is a function of the distance between the measurements, how much they differ in time and, a scaling factor that increases the correlation





lengths with height above ground (Hirter, 1998).

$$\mathbf{C}_{ss}(\mathsf{ZWD}_k,\mathsf{ZWD}_l) = \frac{\sigma_{\mathsf{signal}}^2}{q}$$

where we have for q:

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$$q = 1 + \left[\left(\frac{x_k - x_l}{\Delta x_0} \right)^2 + \left(\frac{y_k - y_l}{\Delta y_0} \right)^2 + \left(\frac{z_k - z_l}{\Delta z_0} \right)^2 + \left(\frac{t_k - t_l}{\Delta t_0} \right)^2 \right] \cdot e^{-\frac{z_k + z_l}{2z_0}}$$
(11)

 σ_{signal}^2 :a priori variance of signal x_k, y_k, z_k, t_k :cartesian coordinates and time of observation k x_l, y_l, z_l, t_l :cartesian coordinates and time of observation l z_0 :scale length modifying correlation lengths as a functionof height

 $\Delta x_0, \Delta y_0, \Delta z_0, \Delta t_0$: correlation lengths of space and time

The stochastic parameter *n* is described with the covariance matrix C_{nn} containing the noise of the individual measurements in the diagonal elements and with all offdiagonal elements being zero. This noise has been calculated with the uncertainties given in Table 2.

The collocation eventually estimates in a least-squares sense the parameters of the deterministic function (*a*, *b*, *c*, *H* and p_0 , e_0 and ZWD₀ for the respective fields) and the signal and noise part of each measurement. The collocation also allows the interpolation of these parts to the points where no measurements are available (see Fig. 4).

3.2 Combined collocation of ZWDs and wet refractivities

For the combined collocation, we need to describe the relationship between the two measurements. Since N_{wet} is the derivative of the ZWD in zenith direction (Eq. 5), the

6, 4895-4940, 2013 Paper **Tropospheric wet** refractivity and humidity profiles Discussion Pape from data fusion F. Hurter and O. Maier **Title Page** Introduction Abstract Discussion Conclusions References Figures Tables Paper Back Close **Discussion** Pape Full Screen / Esc Printer-friendly Version Interactive Discussion

AMTD

(10)



two observation equations become:

$$I_{ZWD} = f(\boldsymbol{u}, \boldsymbol{x}, t) + s + n$$
$$I_{Nwet} = Df(\boldsymbol{u}, \boldsymbol{x}, t) = Df(\boldsymbol{u}, \boldsymbol{x}, t) + s + n$$

₅ with

I _{ZWD} :	ZWD measurement
/ _{Nwet} :	N _{wet} measurement
f(u, x, t):	function describing general ZWD field
u :	unknown parameters of ZWD field
x ,t:	coordinates in space and time
<i>s</i> :	signal part with respect to ZWD
<i>n</i> :	noise part with respect to ZWD
Δ.	differential energies relating 7WD to re

D: differential operator relating ZWD to refractivity N_{wet}

and where D:

$$D = -\frac{\partial}{\partial z}$$

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As the differential operator is applied to the deterministic part of the ZWD (Eq. 9), we obtain

$$N_{\text{wet}}(x, y, z, t) = DZWD(x, y, z, t)$$

= $\frac{1}{H} [ZWD_0 + a(x - x_0) + b(y - y_0) + c(t - t_0)] \cdot e^{-\frac{z}{H}}$ (14)

Applying the differential operator to the signal of the stochastic part leads to two different covariance matrices. In the first case, the covariance between ZWD and N_{wet}



is derived. In a second case, we seek the covariance between two refractivities $N_{wet,k}$ and $N_{wet,l}$:

Case 1:

$$\mathbf{C}_{ss}(N_{\text{wet}}, \text{ZWD}) = \mathbf{C}_{ss}(\text{ZWD}, N_{\text{wet}})$$
$$= \frac{\sigma_{\text{signal}}^2}{q^2} \left[\frac{2 \cdot (-z_{\text{ZWD}} + z_{\text{Nwet}})}{(\Delta z_0)^2} \cdot e^{-\frac{z_{\text{Nwet}} + z_{\text{ZWD}}}{2z_0}} + \frac{1 - q}{2z_0} \right]$$

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Case 2:

$$\mathbf{C}_{ss}\left(N_{\text{wet},k}, N_{\text{wet},l}\right) = \mathbf{C}_{ss}\left(N_{\text{wet},k}, N_{\text{wet},l}\right) \\ = \frac{2\sigma_{\text{signal}}^2}{q^2} \left[\frac{e^{-\frac{z_k+z_l}{2z_0}}}{(\Delta z_0)^2} + \frac{(q-1)(q-2)}{8qz_0^2} - \frac{4(z_k-z_l)^2}{q(\Delta z_0)^4} \cdot e^{-\frac{z_k+z_l}{z_0}}\right]$$
(16)

The uncorrelated noise *n* of the ZWD becomes the uncorrelated noise of the N_{wet} measurements under the influence of the differential operator.

10 3.3 Processing

The flowchart in Fig. 5 gives an overview of the processing steps taken to obtain wet refractivity, dew point temperature and relative humidity profiles at Payerne. Rectangles with corresponding numbers denote processing steps explained in the following.

1. We obtain total air pressure and water vapour pressure estimates at the GPS stations from 20 ground meteorological stations with the individual collocation of the two parameters. We use the methodology and parameter setting outlined in Table 3 and Hirter (1998). Deterministic functions are given in Eq. (7) for pressure and Eq. (8) for water vapour pressure.



(15)



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2. From the collocated air pressure and water vapour pressure values, zenith dry delays (ZDD) are calculated at the locations of the GPS stations (Lutz, 2009):

 $ZDD = 0.002277 \cdot (p_1 - 0.155471 \cdot e_1)$

where p_1 is the total air pressure [hPa] and e_1 the partial water vapour pressure [hPa] at the station, yielding ZDD in units of meters. Note that the water vapour pressure, whose collocation is inherently problematic due to its strong spatial and temporal variations, has only a minor influence onto the ZDD. This is why we can model the ZDD to millimeter accuracy from collocated ground meteo stations, as was demonstrated in Perler (2011). In a comparison between ZDD calculated from ground meteo (Eq. 17) and from radiosonde integration at Payerne, Perler (2011) obtains 1.6mm standard deviation and a mean offset of 2.6mm (ground meteo minus radiosonde).

3. The zenith total delays (ZTD) from the GPS processing are reduced to the zenith wet delays (ZWD) by subtracting easy-to-model dry zenith delays (ZDD) using results from the previous processing step:

ZWD = ZTD - ZDD

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The uncertainty of the ZWD is very difficult to asses. It must be above the formal uncertainty given in Table 2 for the ZTD plus some uncertainty contribution added from the ZDD (see Eq. 18). We adopt a rather optimistic and tentative value of 2mm (Table 3).

4. Wet refractivities are determined with Eq. (3) from several sources: ground meteo, radiooccultation and radiosonde profiles. For ground meteo and radiosonde, uncertainties are calculated from error propagation of the values in Table 2, assuming no correlation between temperature and humidity readings. For radiooccultations. see Sect. 2.4.

Discussion Pape **AMTD** 6, 4895-4940, 2013 **Tropospheric wet** refractivity and humidity profiles Discussion Paper from data fusion F. Hurter and O. Maier **Title Page** Introduction Abstract Discussion Conclusions References Figures Tables Pape Back Close **Discussion** Pape Full Screen / Esc **Printer-friendly Version** Interactive Discussion

(17)

(18)

- 5. Different combinations of the ZWD and the N_{wet} datasets have been input into a collocation using the methodology of Sect. 3.2. The settings for the covariance matrix of the stochastic parameter *s* are listed in Table 3. Correlation lengths were set according to a rule of thumb that was derived from tests on synthetic data (not within the scope of this paper). Stable results were obtained, if correlation lengths were at least 4 times the average sampling in either space or time. Due to the large amount of data, collocations were carried out on batches of 8 h data with 1 h overlap to the next batch to ensure smooth continuation between the batches. Interpolated wet refractivities N_{wet} are output at the heights in Payerne, where also microwave radiometer derived air temperatures are given.
- 6. N_{wet} links the GPS data to meteorology. From the N_{wet} and the radiometer temperature profiles, both at Payerne, we obtain profiles of water vapour pressure e [hPa] rearranging Eq. (3). Dew point temperature T_{dew} [K] is then calculated following (Jacobson, 2005):

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$$T_{\rm dew} = \frac{4880.357 - 29.66\ln e}{19.48 - \ln e}$$

For reasons of simple comparability with humidity profiles from other techniques, the profiles are also calculated in units of percent relative humidity according to

$$f = \frac{\theta}{\theta_{\text{sat}}} \cdot 100[\%]$$
⁽²⁰⁾

with

$$e_{\text{sat}} = 6.112 \cdot \exp \frac{17.67 \cdot (T - 273.15)}{(T - 273.15) + 243.5}$$

where temperature T is given in Kelvin and water vapour pressure e and saturation vapour pressure e_{sat} (Bolton, 1980) are both in units of [hPa].

(19)



4 Results

The results from the least-squares collocation algorithm are compared to radiosonde profiles in Payerne at two stages of the processing (see flowchart in Fig. 5). Firstly, we only investigate the profile quality of the wet refractivity profiles, which are the result of

processing step 5 in Sect. 3.3. Secondly, profiles from processing step 6 in Sect. 3.3 are validated with radiosonde profiles of dew point temperature and relative humidity. Corresponding radiosonde profiles have been calculated using Eqs. (3), (19), and (20). Profiles that result from the COMEDIE processing will be called model. The radiosonde profiles are shortnamed rs to simplify description of the results. Since the model can output a profile at any time and we are mostly interested in the fast varying part of the lower troposphere, the comparison takes place at launch time of the radiosonde, that is, one hour before 00:00 UTC and 12:00 UTC.

4.1 Wet refractivity profiles

Figure 6 displays the timeseries of the difference between model and rs, where we combine the two datasets (GPS and ground meteo) in a common collocation. A clear seasonal trend is observed with strong positive values at heights around 2 km during the months June–October. This coincides with large negative values above and below, which are effects from the algorithm that tries to achieve smooth profiles. The subfigure to the right gives the root mean square difference (RMS) for all 3 yr and is a measure of interpolation quality. The BMS varies between 2 and 7 ppm below the maximum at

²⁰ of interpolation quality. The RMS varies between 2 and 7 ppm below the maximum at 2 km and 4–7 ppm above it.

Figure 7a and b show two characteristic October profiles, comparing the COMEDIE solutions with the radiosonde. They are plotted with formal uncertainty bands and for 3 different input datasets. Input datasets include (i) ZWDs only, (ii) ZWDs and N_{wet} from ground motor and (iii) ZWDs combined with N_{wet} from ground motor and for

from ground meteo and, (iii) ZWDs combined with N_{wet} from ground meteo and from radiosonde derived wet refractivities. Uncertainty bands for the model solutions are calculated a posteriori during the least-squares estimation. We note strong smoothing





of the model profiles and underestimation of the actual error of the interpolation algorithm. This is not a surprise since the algorithm is not aware of the variability that can occur in the atmosphere. Assumptions of these variabilities need to be made before the calculations and are input into Eq. (10). They are to a large extent a function of

- the network density, i.e. the sampling of the refractivity field. The coarser the network, the larger the correlation lengths have to be chosen to avoid artefacts from the algorithm. The smoothing is partly responsible for the limited capability to reproduce strong vertical changes in the atmosphere that are frequent during summer and early autumn months. Deviations of the model from the radiosonde around 2 km height result from
- ¹⁰ ground meteo values that are not representative for the situation in Payerne. This is visible in the comparison between the ZWD only and the ZWD plus N_{wet} solution, the latter showing a slightly degrading effect from the inclusion of ground meteo around 2 km height. Responsible are the stations DOL, MLS and CHA (see Fig. 3) that generally show too high values with respect to corresponding heights in Payerne.
- ¹⁵ On a single profile basis, Fig. 8a and b show the difference of the model solution to the radiosonde rs at the same dates as in Fig. 7a and b, respectively. Colour coding and naming has been kept consistent with previous plots. In Fig. 8a and b, one previously not mentioned solution is shown in black. It represents the solution achieved, if only the deterministic part from the ZWD solution is compared to the radiosonde (see
- Sect. 3.1). The blue line shows, how the solution benefits from the signal part. The improvement from the black to the blue line is especially obvious in Fig. 8b. The effect of the aforementioned stations DOL, MLS and CHA and of the smoothing of the applied correlation lengths are again well observed in all solutions shown.

A rough quantification of the loss in reconstruction quality in case of missing stations in a network is attempted in Fig. 9. It shows the RMS difference between the combined solution (GPS and ground meteo) and the radiosonde for the 3 yr data. The light green curve includes all measurement stations and is repeated from Fig. 6. For the dark green curve, the GPS and the meteo stations in Payerne are excluded from the reconstruction. Mostly affected are the refractivities in the lowermost 2 km with an





increase in RMS difference of 1–2 ppm. Since both, the AGNES and the SwissMetNet network are both not very dense in the region of Payerne, it is expected that the accuracy of wet refractivity reconstruction for all Switzerland is quite well represented with the dark green curve in Fig. 9.

- Now that the achievable accuracy in terms of absolute wet refractivities has been demonstrated, we continue the statistical analysis with relative differences between model and rs. The statistics of 3 yr of data for the lower troposphere are shown in Fig. 10a–c, where we compare the collocation results for different input data. Figure 10a includes only ZWDs in the collocation and demonstrates the quality of reconstruction is used ODD data. The median above a distinct parative effect of 10% at 15 km
- ¹⁰ if we use GPS data. The median shows a distinct negative offset of -16% at ≈ 1.5 km height and quartiles of 10% in the boundary layer. The negative offset has almost disappeared in Fig. 10b. Here, the collocation also includes N_{wet} from ground meteo stations and shows a clear improvement of the quartiles to 5–7.5% relative difference below 1.5 km. Furthermore, the strong asymmetry of the quartiles at heights between
- ¹⁵ 3 km and 4 km of Fig. 10a has been greatly reduced in Fig. 10b. In order to quantify the effect of the N_{wet} dataset on its own, it was separately included in the collocation (Fig. 10c). A clear linear trend of the median is observed that drifts away from the zero line. The spread has also increased with respect to Fig. 10b. Hence, a clear benefit comes from the combination of the two datasets.
- Radioocculations deliver an atmospheric product that can be used to calculate point measurements of wet refractivity. They can be included in the collocation approach much the same way as ground meteo measurements of wet refractivity. There are 189 radiooccultations available in the investigation area during the 3 yr (Table 1). Therefore, only a limited number of COMEDIE calculation batches would actually contain
- one or more occultations in their dataset. Eventually, 132 calculation batches could be compared to radiosonde profiles. Their statistics are shown in Fig. 11a without the occulations, but GPS and ground meteo data, and Fig. 11b with the occultations in addition to GPS and ground meteo. The occultation's influence is practically zero below





4914

1.6 km. In the upper troposphere however, an improvement in the median offset and reduction in spread is observed.

4.2 Humidity profiles

With the additional temperature profiles from the microwave radiometer, the wet refractivity profiles have been converted to dew point temperature. To display dew point temperature on a single profile basis, emagrams of the previously shown October cases for the GPS plus ground meteo solution have been determined in Fig. 12a and b. Beside the model quality of dew point temperature, also the quality of the radiometer temperatures can be demonstrated with the emagram. The smooth nature of the model solution is also noted here. In addition, the incapability to reconstruct the cloud layer between 3-4 km is shown in Fig. 12b. This is due to a lack of stations at that height in the vicinity of Payerne (Fig. 3).

The same statistical model to rs comparison as in Sect. 4.1 has been carried out on the basis of absolute differences of dew point temperature (Fig. 13a and b). Similarly to the relative wet refractivity differences in Fig. 10a and b, the differences in dew point 15 temperature increase almost uniformly with height. This is due to the increased sensitivity of errors in wet refractivity on dew point temperature with decreasing temperature and hence, with height. In Table 4 it is shown that the influence of temperature error on dew point temperature is one order of magnitude lower than is the influence of wet refractivity, which means that the microwave radiometer adds very little to the error figure 20 of the model solution.

We also calculate profiles of relative humidity (Eq. 20) from microwave radiometer temperature and model refractivity of the combined solution of GPS and ground meteo. Figure 14 shows the statistics with respect to the radiosonde as mean and standard deviation of the difference. Systematic deviations from zero of maximum 7.3% and 25

standard deviations of 12-20.0% are observed for the lower troposphere. Note that, contrary to error sensitivity in dew point temperature, where wet refractivity had much





4915

more influence than temperature, relative humidity is similarly affected by temperature and refractivity (Table 4).

5 Discussion

- This study uses an interpolation technique to determine wet refractivity profiles from
 mainly GPS zenith path delays. Many other investigators have used the tomographic approach using slant path delays from the GPS processing to reconstruct wet refractivity fields. The slant paths, if fully recoverd during the processing, do not have the averaging nature of zenith path delays and should hence contain information about the heterogeneity of wet refractivity in the atmosphere. The tomographic approach has been
 statistically validated in Perler (2011) for a one year period in Payerne, Switzerland. He obtains standard deviations of ≈ 10 ppm at the ground, which decrease to ≈ 5 ppm at 4500 m a.m.s.l. with respect to the radiosonde reference. With another tomographic method, Nilsson et al. (2007) arrive at 4–5 ppm absolute error to a radiosonde reference and a relative error of 10% most of the time for the refractivity in the lower 2 km
 of the troposphere. The problem of the tomographic approach lies in the fact that path
- delays from ground based GPS stations have very limited capability to recover vertical structures in the atmosphere above the top station as has been shown by Champollion et al. (2005) or Perler et al. (2011). GPS tomography software with data from ground-based stations, therefore, rely on information other than actual measurements
- to retrieve meaningful fields. These are often constraints on the mutual dependence between refractivities. In the here presented study, such constraints were also integrated using a statistical parameter of known covariance matrix. Additionally, a trend function has been included that describes the structure of the general ZWD field. GPS tomography was not employed with the given network due to the sparsity of crossing
- rays that are especially important for the quality of tomographic reconstructions (Bender et al., 2009). For the heights 0.5–4 km a.m.s.l., we obtain RMS differences of 2–7 ppm with the maximum difference at 2 km height. The results being close in accuracy





to other works using GPS tomography for the refractivity reconstruction suggests that, with the currently investigated station networks and reconstruction techniques, slant path delays add little additional information.

- The least-squares collocation is capable of including other measurement types. In a first experiment, ground meteo stations have been included. Ground meteo station data has been previously included into GPS tomography and its beneficial effect has been shown (Manning et al., 2013) or has been suggested (Bosy et al., 2010). We show that including ground meteo measurements of wet refractivity has a very positive effect on the mean offset with respect to the radiosonde reference, particularly in the region ≤ 2 km. Including N_{wet} profiles from radiooccultations has shown to improve the
- region ≤ 2 km. Including N_{wet} profiles from radiooccultations has shown to improve the accuracy in the upper troposphere. Due to the few occultations taking place in the study region during the 3 yr, radiooccultations give little support to the overall solution. We still demonstrate that their continuation to the ground with GPS path delays and ground meteo measurements is feasible. Foelsche and Kirchengast (2001) demonstrate that
- a thorough ray-tracing approach together with slant paths from ground stations allows retrieval of the complete information contained in radiooccultation delays.

The Raman Lidar is a measurement technique with vertical resolution superior to our technique. For an operational Raman Lidar at Payerne, Switzerland, Brocard et al. (2012) demonstrate a relative humidity agreement of 2% for day-time and 5% for night-

- time comparisons with radiosondes (conversion from mixing ratio to relative humidity with temperatures from radiosonde). Standard deviations of this comparison are around 5% (night) and 7% (day) for most of the lower troposphere. At night, when humidity gradients at 1.5 km above ground are often pronounced, standard deviation of the lidar minus sonde comparison reaches up to 10% at that height. This suggests that
- ²⁵ lidar profiles are also somewhat smoothed and do not fully catch strong gradients close to the boundary layer top, but far better than our profiles. Our relative humidity agreement is around 5%, with standard deviations of 12–20%. For the conversion of N_{wet} to relative humidity, we have temperature from the microwave profiler at hand, which adds further uncertainty to our retrieval, but is generally available, including times of





fog and light rain, and not restricted to heights below cloud base. Exceptions occur in case of strong rain, where quality of temperature profiles from radiometer have not been sufficiently investigated yet. The easy maintenance, good data reliability and low costs due to shared use with other applications are the strenghts of our solution, which

- is not a measurement technique as such, but an aggregation of data from a relatively large area (100 km radius). In contrast to the LIDAR that is very precise at one location, the aggregation aims at a certain representativity. Due to costs, a dense radiosonde or LIDAR network would be difficult to setup and maintain. With respect to radiosondes, the temporal resolution of our data is more suited to follow the evolution of atmospheric
- ¹⁰ humidity on time scales of hours. The smoothed profiles however, do not allow to image strong vertical humidity gradients correctly. The relative humidity uncertainty of the radiosonde is given as 5–10 % (Table 2) with approximately 10 m average vertical resolution. This makes it a suitable reference in case of sharp humidity gradients.

Relative humidity is still one of the most difficult variable to forecast by a numerical
¹⁵ weather prediction model. Forecast uncertainties in relative humidity of 10–20% are common (e.g. Wilhelm, 2012) and are thus of the same order of magnitude as our results. Since GPS, microwave radiometer and ground meteo stations together provide humidity information in near-realtime, we envisage a benefit of our profiles for applications of cloud and rain nowcasting. The profiles achieve dew point temperature
²⁰ quartiles ≤ 2K below 2km height and increase to 4.5K at 4km. A possible product could be the calculation of CAPE (convective available potential energy) for thunder-

storm detection or other indices related to the occurence of precipitation events and their severity, before they can be detected and quantified by other means (e.g. weather radar).

25 6 Conclusions

We present results from an interpolation approach of GPS zenith wet delays and several datasets of point measurments of wet refractivity to reconstruct wet refractivity





profiles. Water vapour profiles have been calculated, where temperature profiles from a microwave radiometer are available. Wet refractivity profiles from our processing are shown to have comparable accuracy to results from investigations that reconstruct refractivity with GPS tomography. Additional datasets, such as ground meteorological values or radiooccultations improved the results. With respect to dew point tempera-

- 5 ture, a maximum median offset of 2K and maximum guartiles of 4.5K were achived for the lower troposphere, combining the presently available data from a GPS and a ground meteo network in the western part of Switzerland. Collocation can incorporate a suite of data into a common least-squares framework. Possible further datasets
- to include would be Lidar profiles, refractivity gradients derived from rain radar clutter 10 maps, differential delays from InSAR interferograms (with topographic phase removed), or zenith path gradients, the latter being a result of the GPS processing. The combination of many already in near-realtime available datasets of either integral or point measures of refractivity could give a valuable contribution to the nowcasting community or for investigations of individual instrument accuracies, profitting from mutually 15
- complemental instrumental strenghts.

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4919

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Sensor name	Start of dataset [UTC]	End of dataset [UTC]	Time resolution	Number of stations	Data provider
radiosonde	1 Jan 2009 00:00:00	31 Dec 2011 00:00:00	2 profiles/day at 00:00:00 and 12:00:00 UTC	1	meteoswiss
GPS	28 Dec 2008 00:00:00	31 Dec 2011 00:00:00	1 h	18	swisstopo
ground meteo	1 Jan 2009 00:00:00	31 Dec 2011 00:00:00	10 min	20	meteoswiss
mwr ro	1 Jan 2009 00:00:00 1 Jan 2009	31 Dec 2011 23:53:20 21 Dec 2011	6 to 7 min 189 profiles	1 —	meteoswiss CDAAC



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Table 2. Parameters contained in the original datasets and associated sensor uncertainties (^aLöhnert and Maier, 2012, ^bCIMO Guide, 2008, ^cLöhnert and Maier, 2012).

Sensor name	Parameter	Uncertainty	Note
radiosonde ^a	temperature	±0.2K	copper-constantan thermocouples
	pressure humidity	±0.2% of value ≅ ±2hPa ±10 to 20%	water hypsometer carbon hygristor until April 2009
		±5 to 10%	capacitive polymer starting May 2009
gps	total zenith path delay	1.6 mm	average formal uncertainty from GPS processing of L1/L2 double-frequency geodetic GNSS receivers
ground meteo ^b	temperature	±0.2K	achievable measurement uncertainty
	pressure	±0.15hPa	achievable measurement uncertainty
	relative humidity	±3%	achievable measurement uncertainty
mwr ^c	temperature	± 0.5 K lower boundary layer ± 1.7 K at 4 km height	standard deviations from comparison with radiosondes
ro	total refractivity	$\approx \pm 1$ ppm at 1.0 km height ± 2 ppm at 4 km height ± 0.03 ppm at 8 km height	average formal uncertainties from operational level2 product



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6, 4895–4	940, 2013		
Tropospheric wet refractivity and humidity profiles from data fusion			
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Abstract	Introduction		
Conclusions	References		
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Back	Close		
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Discussion Paper

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Table 3. List of stochastic parameters applied in the least-squares collocation. For signal part s, see Eq. (10).

Observation	$\sigma_{ m signal}$	$\sigma_{ m noise}$	Δx_0	Δy_0	Δz_0	Δt_0	Z ₀
Pressure Water vapor pressure ZWD		0.5 hPa 0.5 hPa 2 mm		150 km 50 km 35 km	0.50 km 0.15 km 1 km		

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Table 4. Formal sensitivity effects of errors in wet refractivity and temperature on dew point temperature and relative humidity. Valid for atmospheric values of $N_{wet} = 10-50$ ppm and T = 273-293 K.

	10 ppm error in $N_{\rm wet}$	1 K error in temperature
Dew point temperature	2–11 K	≤ 0.1 K
Relative humidity	10–30 %	1–12%



Fig. 1. GPS stations whose zenith path delays contribute to this study. They are all stations from the AGNES deployed by the Swiss Federal Office of Topography. White star in Payerne denotes the place of the profile comparison.





Fig. 2. SwissMetNet (SMN) stations of MeteoSwiss used in this study.

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Fig. 3. Height distribution of the GPS (red) and ground meteorological stations (green) shown in Figs. 1 and 2, projected into a West-East plane. Their longitudinal positions were shifted to improve label readability.





Fig. 4. Principle of collocation (Troller, 2004). The circles are the measurements *I*, which are comprised of a deterministic part f(u, x, t), of signal *s* and noise *n*. Interpolation between measurements then is a filtered version that is made up of the deterministic part $f(u, x_i, t_i)$ at the interpolated position x_i and time t_i , plus the signal s'.



Discussion Paper

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Discussion Paper



Fig. 5. Flowchart of the steps carried out to get refractivity or dew point temperature profiles at Payerne. Rectangles stand for processing steps and parallelograms denote data and results from the processing. The numbers in the chart refer to the processing steps explained in Sect. 3.3. The solid lines show the processing that leads to the refractivity profiles. The second part of the study, where humidity profiles in Payerne are produced, is shown with dashed lines.



Discussion Paper

Discussion Paper

Discussion Paper





Fig. 6. Timeseries showing the difference between the COMEDIE derived wet refractivities from the GPS and ground meteo solution and the radiosonde (grey box: GPS data gap). The RMS difference for all 3 yr is plotted on the side of the timeseries.





Fig. 7. Single profiles of wet refractivity for **(a)** 17 October 2011, 12:00 UTC and **(b)** 28 October 2011, 12:00 UTC for different input datasets. The formal 1-sigma uncertainty of the profiles and of the corresponding radiosonde are shown as shaded patches.



Discussion Paper

Discussion Paper

Discussion Paper

Discussion Paper





Fig. 8. Comparison between interpolated refractivity profiles from COMEDIE and the radiosonde profile from the 17 October 2011, 12:00 UTC. ZWD function takes only the deterministic part into account. All other profiles contain also the signal part derived from either ZWD data from GPS, refractivity data from ground meteorological stations or the radiosonde at Payerne, or a combination of these datasets. (b) Comparison between interpolated refractivity profiles from COMEDIE and the radiosonde profile from the 28 October 2011, 12:00 UTC. Other information as for (a).





Discussion Paper AMTD 6, 4895-4940, 2013 **Tropospheric wet** refractivity and humidity profiles **Discussion** Paper from data fusion F. Hurter and O. Maier **Title Page** Introduction Abstract **Discussion** Paper Conclusions References Tables Figures Back Close **Discussion** Paper Full Screen / Esc Printer-friendly Version Interactive Discussion

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Fig. 9. RMS of model minus radiosonde difference for a collocation including the GPS station PAYE and the meteo station PAY (green) and for a collocation without those two stations (dark green). The comparison shows 3 yr of data with 2132 radiosonde profiles being evaluated. Note that the light green line corresponds to the right panel of Fig. 6, but with another x-axis scale.



Fig. 10. (a) Boxplot of the relative differences between COMEDIE derived wet refractivities with data from GPS only and the radiosonde. Boxes denote the 25th and 75th percentile and the median is marked inside the boxes. Total number of evaluated cases is 2132. (b) As for (a) but with COMEDIE derived wet refractivities using data from GPS and ground meteorological stations. (c) As for (a) but using COMEDIE derived wet refractivities from data of ground meteorological stations only. Note that the abscissa is scaled differently to (a) and (b).





Discussion Paper AMTD 6, 4895-4940, 2013 **Tropospheric wet** refractivity and humidity profiles **Discussion** Paper from data fusion F. Hurter and O. Maier **Title Page** Introduction Abstract Discussion Paper Conclusions References Figures Tables Close Back **Discussion** Paper Full Screen / Esc Printer-friendly Version Interactive Discussion



Fig. 11. (a) As for Fig. 10b but showing the boxplot for the upper troposphere from 1.6 km to 8 km and including only the 132 cases that would contain radiooccultations in their computation batches. **(b)** Shows the statistics of the 132 interpolation batches that contain the occultations. Data from GPS, ground meteorological stations and radiooccultation profiles of wet refractivity have been included and interpolated.



Fig. 12. Emagrams for **(a)** 17 October 2011 with dew point temperatures calculated from the COMEDIE solution (GPS plus ground meteo solution) and radiometer temperatures. **(b)** 28 October 2011, 12:00 UTC. Other information as for **(a)**.



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Fig. 13. (a) Boxplot showing the differences between dew point temperature derived from COMEDIE wet refractivities and radiometer temperatures and dew point temperature entirely calculated with radiosonde data. COMEDIE wet refractivities were calculated using GPS zenith path delays only. Boxes denote the 25th and 75th percentile. The median is marked inside the boxes. Lines show large offsets and extend from $q_{25\%} - 1.5 \cdot (q_{75\%} - q_{25\%})$ to $q_{75\%} + 1.5 \cdot (q_{75\%} - q_{25\%})$. They cover roughly 99% of the data spread if normal distribution is assumed. Further data is classified as outliers and not shown. **(b)** As for **(a)**, but with wet refractivities from ground meteo stations as additional input dataset in COMEDIE.







