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Relationship between optical extinction and liquid water content in fogs

C. Klein and A. Dabas

Groupe d'Étude de l'Atmosphère Météorologique (GAME) – UMR3589, Unité Mixte de Recherche 3589 de Météo-France et du CNRS, Toulouse, France

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Correspondence to: A. Dabas (alain.dabas@meteo.fr)

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Abstract

Studies carried out in the late 1970s suggest a simple linear relationship exists in practice between the optical extinction in the thermal IR and the liquid water content (LWC) in fogs. Such a relationship opens the possibility to monitor the vertical profile of the LWC in fogs with a rather simple backscatter lidar. Little is known on how the LWC varies as a function of height and during the fog life cycle, so the new measurement technique would help understand fog physics and provide valuable data for improving the quality of fog forecasts. In the present article, the validity of the linear relationship is revisited at the light of recent observations of fog droplet size distributions measured with a combination of sensors covering a large range of droplet radii. In particular, large droplets (radius above 15 µm) are detected, which was not the case in the late 1970s. The results confirm the linear relationship still holds, at least for the mostly radiative fogs observed during the campaign. The impact of the precise value of the real and imaginary parts of the refractive index on the coefficient of the linear relationship is also studied. The usual practice considers droplets are made of pure water. This assumption is probably valid for big droplets, it may be questioned for small ones since droplets are formed from condensation nuclei of highly variable chemical composition. The study suggests the relationship is mostly sensitive to the real part of the refractive index and the sensitivity grows with the size of fog droplets. However, large fog droplets are more likely to have an index close to that of water since they are mainly composed of water.

1 Introduction

Improving the quality of fog forecasts is a challenge for weather prediction centres. Fog is indeed a common weather phenomenon with a strong, adverse impact on human activities. This is particularly true for aviation. For instance, the worst crash in the aviation history happened in 1977 in Teneriffe with the collision of two Boing 747 jumbo-jets on

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the runaway and the death of more than 500 persons. The dense fog on the airport was a key factor (see ICAO Circular 135/AN156). Fortunately, the impact of fog on airports is not so severe most of the time, but safety regulations limit the capacity of the runways when the visibility is too short (e.g. runway visual range less than 600 m at Paris

5 Roissy Charles-de-Gaulle airport), leading to costly delays, missed connections, and cancellations (see Sullivan and Jordan, 2006, for a description of possible disruptions on a major airport like London Heathrow).

The cost for airports and aviation companies has led many research centres around the world to work on fog physics and fog numerical simulation. The final objective is to
10 develop operational tools for accurate predictions of the formation and the dissipation of fog several hours in advance. If such tools were existing airports and companies could warn the passengers, encourage them to cancel their flight, and mitigate the impact by an adequate organization of the time slots still available.

Weather conditions favourable to fog formation are well known and predictable, but
15 accurate predictions of the time of formation and dissipation is presently an unmet challenge. The reason is fog is a local phenomenon with a small vertical extension (several hundreds of meters at worst) and it involves several small-scale, highly non-linear processes. These processes are not always fully understood and they are anyway all difficult to represent in numerical models (a complete review of the state of the art in fog
20 physics can be found in Gultepe, 2007). Such processes include e. g. radiative transfer, turbulence, activation of aerosols into water drops ...

Several directions are currently pursued for improving our understanding of fog and ultimately its forecast. One of them deals with the observation. Current observation systems provide useful information but are operated at the ground and characterize
25 the state of the atmosphere in the lowest meters and not above. Observation systems for altitude measurements used operationally or for research are ill adapted. Research aircrafts for instance cannot fly in fogs as these are thin – they would have to fly close to the ground – while the visibility is weak. Instrumented masts are possible, but are expensive and are deployed with difficulty close to airfields. Free or tethered balloons

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are another possibility, but they are “single shot” (free balloons) or imply complex operations that limit their practical usefulness (Dabas et al., 2012). Remote sensors would offer many advantages. Deployed at ground, they can be operated unattended for long periods of time. As an instance, Paris Charles-de-Gaulle airport has been equipped
5 with a sodar since 2008. It detects the top height of fog layers and provides this information to the operational fog prediction system COBEL (Dabas et al., 2012; Bergot and Guédalia, 1994).

The work reported in the present article is part of an effort aimed at developing a lidar
able to measure vertical profiles of the liquid water content (LWC). The LWC can be
10 measured at ground (Gerber, 1991), but altitude measurements are scarce because they are difficult to achieve with current sensors. Observations are thus lacking for validating model simulations (Bergot, 2013). Besides, real time LWC observation could have a significant impact on fog predictions (Remy and Bergot, 2009). In this article, the
15 possibility to measure the LWC with a lidar is based on the existence of a relationship between the LWC and the optical extinction in fogs. Such a relationship was postulated by Chylek (1978) in the late 1970s and tested experimentally by Pinnick et al. (1979) in the same period. In principle, lidars can measure extinction coefficients. Due to the strong optical extinction in fogs their range is limited but fogs are thin (a few tens to a few hundreds of meters) so it should be possible to obtain useful measurements.

20 The experimental validation of Pinnick et al. (1979) was based on a particle counter and sizer developed by the Particle Measurement Systems Inc. in the 1970s. The sensor is described in Pinnick et al. (1978). According to the article, a major limitation was that particles with radii $> 15 \mu\text{m}$ were only partially detected due to losses in the ventilated collection tube. Thus the impact of larger droplets in fogs, if any, could not
25 be evaluated. A second limitation was that extinction coefficients were computed using the Mie theory with refraction indices of pure water. The refraction index of large droplets is probably close to pure water because they mostly contain water. However, drops are formed from condensation nuclei, that is, aerosols. Their refraction index depends on their chemical composition (Fenn et al., 1985; Guyon et al., 2003). In fogs,

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5 The purpose of the present paper is twofold. First, Pinnick et al. results are revisited on the basis of observations carried out recently with a state-of-the art instrumental setup. Described in Sect. 2, the setup can in principle detect and size fog droplets up to a diameter of 50 μm . In Sect. 3, the linear relationship between optical extinction and LWC in fogs is checked. Then (Sect. 4) the potential impact of the refractive index is 10 studied. As there are very few measurements of the refractive index of fog droplets, the study determines how far indices can deviate from pure water before the extinction to LWC relationship is significantly impacted. Conclusions are drawn in Sect. 5.

2 Experimental setup and data

15 The size distributions used in this article were measured during a field experiment called ParisFog (Haeffelin et al., 2010) in the frame of the research study PREVIBOSS (Elias et al., 2012). This study was designed to improve the understanding of processes involved in the life cycle of fog. It was held at Site Instrumental de Recherche en Télédétection Atmosphérique (SIRTA) located 25 km south of Paris (Heaffelin et al., 2005). Data were monitored during the winters 2010/2011 and 2011/2012. Aerosol and 20 fog particles size distributions were measured with two instruments: a Welas-2000, and a Fog Monitor 100 (Burnet et al., 2012).

Manufactured by PALAS, the Welas 2000 measures the concentration and size of particles by looking at the 90° scattering of a white light source. The size range depends on instrumental settings and type of particles. During PARISFOG, the system was expected to measure water particles from diameters of 0.4 μm to about 20 μm . The instrument was 3 m above the ground.

The FM100 is manufactured by *Droplet Measurement Technologies* (DMT). It is a forward scattering spectrometer probe placed in a wind tunnel with active ventilation. The FM100 detects particles in the diameter range 2 to 50 μm . The size distributions used in this article are retrieved with the manufacturer's software delivered with the FM100.

5 The actual performances of the FM100 are discussed in Spiegel et al. (2012).

The WELAS and the FM100 are complementary sensors. The WELAS measures small particles (up to a few microns), and the FM100 the large ones (up to several tens of microns). Intermediate sizes are detected by both so the consistency of their size distributions can be checked. Both instruments were calibrated before the campaigns 10 with glass or latex beads, but the estimation of detected droplets is done with a calibration curve that assumes the droplets are made of water. Note that the droplet size distributions used here do not need to be "real", but realistic, with regards in particular to the presence and relative contribution to LWC of large droplets.

15 Composite size distributions from both instruments were built and fitted with the sum of M log-normal modes

$$n(r) = \frac{1}{\sqrt{2\pi}r} \sum_{k=1}^M \frac{N_k}{\ln(\sigma_k)} \exp \left[-\frac{1}{2\ln^2(\sigma_k)} \ln \left(\frac{r}{r_k} \right)^2 \right]. \quad (1)$$

Here, r_k is the modal radius, σ_k sets the width of the mode, and N_k the concentration of the mode. In practice, we used a maximum of $M = 4$ modes.

20 The following sections are based on 20 different size distributions selected among several hundreds of size distributions observed during PARISFOG. The selection was done so as to cover a large variety of fog and pre fog conditions (type, optical thickness, development stage ...). The log-normal mode characteristics are given in Table 1. They were manually fitted to the measured size distributions. A fit example is shown 25 in Fig. 1. There the number of particles counted in the various classes of the FM100 and WELAS 2000 are displayed with blue dots. The fit with the sum of four log-normal modes is represented with a red, solid line. The individual modes are indicated with green dashes. The size distribution was observed on 19 November 2010, at 05:40 UTC

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(06:40 LST). A mode of large particles is detected. Its modal radius is 7.5 μm (diameter 15 μm). The figure confirms the ability of the FM100 to detect and count large particles. In the present example, droplets with diameters > 15 μm are indeed detected. Although their number is small, their contribution to the overall LWC is large (more than 70 % in the present case).⁵

3 LWC vs. extinction

The liquid water content is given by the third-order moment of the size distribution

$$W = \frac{4\pi\rho_{\text{H}_2\text{O}}}{3} \int_0^{+\infty} r^3 n(r) \text{d}r \quad (2)$$

where $\rho_{\text{H}_2\text{O}} = 1000 \text{ kg m}^{-3}$ is the density of water. As for the extinction coefficients, we have

$$\alpha(\lambda) = \pi \int_0^{+\infty} r^2 Q_{\text{ext}}(r, \lambda) n(r) \text{d}r \quad (3)$$

with $Q_{\text{ext}}(r, \lambda)$ the extinction efficiency of the particles of radius r at the wavelength λ .

In 1978, Chylek suggested that the extinction efficiency can be reasonably well approximated by a linear relationship

$$Q_{\text{ext}}(r, \lambda) \approx c_e(\lambda) \frac{2\pi r}{\lambda} \quad (4)$$

over the range of radii r practically found in fogs and for a well-chosen wavelength. Values for $c_e(\lambda)$ were proposed later by Pinnick et al. (1979).

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Combining Eqs. (3) and (4), it appears the liquid water content W can be related to the extinction coefficient $\alpha(\lambda)$ through a simple, linear equation independent of the actual size distribution $n(r)$ that is thus valid for any fog

$$\hat{W} \approx \frac{2\lambda\rho_{\text{H}_2\text{O}}}{3\pi c_e(\lambda)} \alpha(\lambda). \quad (5)$$

5 Using Eqs. (2) and (3), the liquid water contents and extinction coefficients of the 20 selected size distributions were derived for the wavelengths λ studied in Pinnick et al. (1979). The extinction efficiency $Q_{\text{ext}}(r, \lambda)$ was computed using an adaption to the programming language SCILAB of a MATLAB code published by Mätzler (2002) (this latter one derived from Borhen and Huffman, 1983). A refractive index equal to 10 that of pure water was considered. Its value as a function of the wavelength λ was taken from Hale and Querry (1973) ($1.351 + i0.00460$ @ $\lambda = 4 \mu\text{m}$ and $1.153 + i0.0968$ @ $\lambda = 11 \mu\text{m}$).

15 The 20 PARISFOG size distributions vary from weak to strong fogs (extinction coefficients from $7.8 \times 10^{-6} \text{ m}^{-1}$ to $1.36 \times 10^{-2} \text{ m}^{-1}$ at $11 \mu\text{m}$, and W from $6.89 \times 10^{-5} \text{ gm}^{-3}$ to $1.29 \times 10^{-1} \text{ gm}^{-3}$ – see Table 1). They encompass the values considered by Pinnick et al. (1979).

20 The extinction coefficients and liquid water contents of the 20 fog cases are shown with grey dots on Figs. 2 and 3 for the laser wavelengths of $4 \mu\text{m}$ and $11 \mu\text{m}$, respectively. The black curve and diamonds represent Eq. (5) ($c_e(4 \mu\text{m}) = 0.64$; $c_e(11 \mu\text{m}) = 0.31$). The results are similar to those of Pinnick et al. (1979). At $\lambda = 4 \mu\text{m}$, the dots are 25 off the black line and dispersed. There seems to be no particular relationship between both parameters independent of the size distribution. At $\lambda = 11 \mu\text{m}$ however, the dots are on the black curve suggesting the linear approximation holds. As several size distributions include a significant fraction of large droplets, Pinnick's linear approximation Eq. (5) appears to be still applicable in practice.

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In Figs. 4 and 5 are drawn the two functions

$$F(r) = \frac{4\pi}{3} \rho_{\text{H}_2\text{O}} r^3 \quad (6)$$

and

$$\hat{F}(r) = \frac{4\rho_{\text{H}_2\text{O}}}{3c_e(\lambda)} r^2 Q_{\text{ext}}(r, \lambda). \quad (7)$$

5 These functions characterize the “sensitivity” of W and \hat{W} to particles of radius r since

$$W = \int_0^{+\infty} F(r) n(r) dr \quad (8)$$

and

$$\hat{W} = \int_0^{+\infty} \hat{F}(r) n(r) dr. \quad (9)$$

10 They are drawn for $\lambda = 4 \mu\text{m}$ (Fig. 4) and $\lambda = 11 \mu\text{m}$ (Fig. 5), and the relative difference $|1 - \hat{F}/F|$ is displayed for both wavelengths in Figs. 6 and 7. At $4 \mu\text{m}$, \hat{W} is a poor approximation to W except for particles in the range $[2 \mu\text{m}, 4 \mu\text{m}]$. Outside this interval, the contribution of the particles to the liquid water content is grossly underestimated. At $11 \mu\text{m}$, the approximation is much better and holds for particles in a much wider range. The relative error is less than 10 % for radii between $1.7 \mu\text{m}$ and $13.2 \mu\text{m}$. This result is noticeable as observations suggest a vast majority of fogs contain particles within this range. Larger particles may be found, but are in very small numbers and therefore shall not contribute much to the total liquid water content. Fog extinction coefficients thus seem to be an accurate proxy for their liquid water content.

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4 Impact of the refractive index

As already mentioned, the results above are all based on extinction efficiencies calculated with the refractive index of water, that is, assuming fog particles mainly consist of water. This assumption is common in fog models or fog studies (Dumont, 2000; Elias et al., 2009; Rangognio et al., 2009; Khain et al., 2004; Laven, 2011). However, fog particles are formed from condensation nuclei, that is, aerosol, which refractive index depends on its chemical composition and can vary a lot. In large fog particles, the amount of water is large and the use of the refractive index of water is probably justified. But fogs contain small particles in large numbers, and the relative contribution of the nucleus in the overall matter of the particle may not be negligible. This is why we have studied the impact of the value of the refractive index on the W vs. extinction relationship. To our knowledge, there are no measurements of the refractive index of fog particles in the literature, so the interval of variation of the index, if any, is not known. Consequently, we did not try to see if real fluctuations of the refractive index of fog particles may or may not have an impact of how W relates to the extinction, but rather tried to determine the interval of variations the refractive index may have before it has a significant impact. We leave it to future studies to determine whether real refractive indices are within this interval or exceed it.

We proceeded in three steps. First, keeping the real value of the refractive index, we modified the imaginary part by default or excess until we found a significant impact on the extinction coefficients of the 20 PARISFOG size distributions. Second, we did the same keeping this time the imaginary part constant and tuning the real part. At last, we made the assumption that particles with a diameter larger than 1 μm are mainly made of water (the extinction coefficient for these particles is computed with the refractive index of water), and smaller particles of another matter. We considered several possible matters commonly found in aerosols and their corresponding refractive index (see Table 2 from Fenn et al., 1985).

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meters should be possible with commercial CO₂ lasers. This range is comparable to the typical vertical extension of fogs so a profiling of the LWC through the entire fog thickness seems to be possible.

The major limitation found in the article is due to a possible uncertainty on the refractive index of particles detected by the lidar. Small particles contain a significant fraction of aerosol matter with a refractive index that may differ significantly from water. Our study suggests that thick fogs with heavy LWC are unlikely to be affected, but thin fogs may be. For these fogs, it seems that LCW measurement is mostly sensitive to the real part of the refractive index.

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6, 9623–9653, 2013

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Table 1. Log-normal modes characteristics of the 20 fog size distributions used in this article. D_k is the modal diameter (equal to $2r_k$).

#	Date	Time	Mode	N_k (partcc ⁻¹)	σ_k	D_k (μm)	LWC (g m^{-3})	$\lambda = 11 \mu\text{m}$		$\lambda = 4 \mu\text{m}$	
								σ_{ext} (m^{-1})	σ_{abs} (m^{-1})	σ_{ext} (m^{-1})	σ_{abs} (m^{-1})
1	19 Nov 2010	03:00	1	44	1.3	0.92	6.89E-05	7.80E-06	7.40E-06	2.70E-05	1.30E-06
			2	7	1.5	1.8					
2	16 Nov 2010	21:00	1	200	1.3	0.95	1.76E-04	1.89E-05	1.86E-05	3.41E-05	2.80E-06
			2	15	1.2	1.8					
3	16 Nov 2011	00:52	1	225	1.3	0.88	1.88E-04	2.01E-05	1.99E-05	3.12E-05	3.00E-06
			2	50	1.3	1.3					
4	16 Nov 2011	00:57	1	275	1.28	0.85	3.15E-04	3.40E-05	3.34E-05	6.72E-05	5.20E-06
			2	95	1.25	1.35					
			3	7	1.2	2.2					
5	19 Nov 2010	05:00	1	250	1.33	1.08	3.66E-04	4.06E-05	3.90E-05	1.18E-04	6.40E-06
			2	20	1.5	1.8					
6	16 Nov 2011	01:02	1	320	1.28	0.88	1.17E-03	1.50E-04	1.18E-04	6.26E-04	2.47E-05
			2	95	1.25	1.3					
			3	5	1.2	2.2					
			4	5	1.35	6					
7	16 Nov 2010	22:00	1	830	1.34	1.1	2.62E-03	2.92E-04	2.81E-04	1.13E-03	4.95E-05
			2	160	1.23	1.9					
			3	70	1.4	2.5					
8	16 Nov 2011	01:07	1	280	1.28	0.85	7.63E-03	1.02E-03	6.64E-04	2.83E-03	1.68E-04
			2	250	1.3	1.28					
			3	20	1.2	2.3					
			4	18	1.6	6.5					
9	16 Nov 2010	22:00	1	875	1.35	1.1	9.72E-03	1.25E-03	9.58E-04	5.09E-03	2.09E-04
			2	200	1.3	2					
			3	100	1.55	2.4					
			4	50	1.7	4					
10	19 Nov 2010	05:40	1	295	1.39	1.3	2.64E-02	2.87E-03	1.57E-03	4.86E-03	5.01E-04
			2	85	1.4	2.2					
			3	12	1.25	5.4					
			4	5	1.6	15					

Table 1. Continued.

#	Date	Time	Mode	N_k (partcc $^{-1}$)	σ_k (μm)	D_k (μm)	LWC (g m^{-3})	$\lambda = 11\text{ }\mu\text{m}$		$\lambda = 4\text{ }\mu\text{m}$	
								$\sigma_{\text{ext}}\text{ (m}^{-1}\text{)}$	$\sigma_{\text{abs}}\text{ (m}^{-1}\text{)}$	$\sigma_{\text{ext}}\text{ (m}^{-1}\text{)}$	$\sigma_{\text{abs}}\text{ (m}^{-1}\text{)}$
11	16 Nov 2011	01:12	1	500	1.28	0.89	5.57E-02	5.57E-03	3.07E-03	9.37E-03	1.01E-03
			2	350	1.3	1.5					
			3	20	1.18	2.8					
			4	60	2.3	4.4					
12	19 Nov 2010	06:50	1	170	1.39	1.3	4.72E-02	6.14E-03	3.53E-03	1.23E-02	1.01E-03
			2	85	1.45	2.18					
			3	42	1.39	4.88					
			4	22	1.45	12.5					
13	16 Nov 2011	01:17	1	490	1.3	0.9	5.44E-02	7.06E-03	4.08E-03	1.32E-02	1.16E-03
			2	475	1.4	1.55					
			3	45	1.5	3.1					
			4	35	1.5	11					
14	16 Nov 2011	09:22	1	865	1.33	1	5.77E-02	7.87E-03	5.18E-03	2.34E-02	1.30E-03
			2	700	1.38	1.6					
			3	195	1.55	4.5					
			4	30	1.3	11.5					
15	16 Nov 2011	01:27	1	535	1.31	0.9	6.59E-02	8.73E-03	5.21E-03	1.86E-02	1.44E-03
			2	510	1.4	1.56					
			3	95	1.6	3					
			4	55	1.5	10					
16	16 Nov 2011	08:15	1	315	1.35	1	6.71E-02	9.25E-03	5.87E-03	2.48E-02	1.52E-03
			2	300	1.38	1.62					
			3	145	1.6	5					
			4	40	1.3	11.2					
17	16 Nov 2011	05:47	1	210	1.35	1.03	9.04E-02	1.24E-02	7.56E-03	2.90E-02	2.03E-03
			2	290	1.55	1.9					
			3	70	1.28	5.6					
			4	70	1.35	11.3					
18	16 Nov 2011	04:42	1	235	1.4	1.06	9.22E-02	1.26E-02	7.65E-03	2.81E-02	2.07E-03
			2	245	1.45	1.75					
			3	80	1.6	5					
			4	68	1.36	11.2					
19	16 Nov 2010	23:00	1	1150	1.34	1.07	1.29E-01	1.31E-02	7.28E-03	2.28E-02	2.37E-03
			2	350	1.32	2					
			3	80	2	3					
			4	80	2.15	6					
20	17 Nov 2010	00:10	1	330	1.34	1.07	1.25E-01	1.36E-02	7.18E-03	2.05E-02	2.39E-03
			2	230	1.44	2					
			3	25	1.3	6.3					
			4	25	1.6	15					

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Table 2. Refraction index of different aerosol types. From Fenn et al. (1985).

Sea salt	$1.48 + 1.4 \times 10^{-2}i$
Oceanic	$1.246 + 7.31 \times 10^{-2}i$
Ice	$1.093 + 0.239i$
Meteoric	$1.509 + 0.691i$
Water Soluble	$1.72 + 5.0 \times 10^{-2}i$
Dust	$1.62 + 0.105i$
Soot	$2.23 + 0.73i$
75 % H_2SO_4	$1.670 + 0.485i$
Volcanic	$2.15 + 0.270i$

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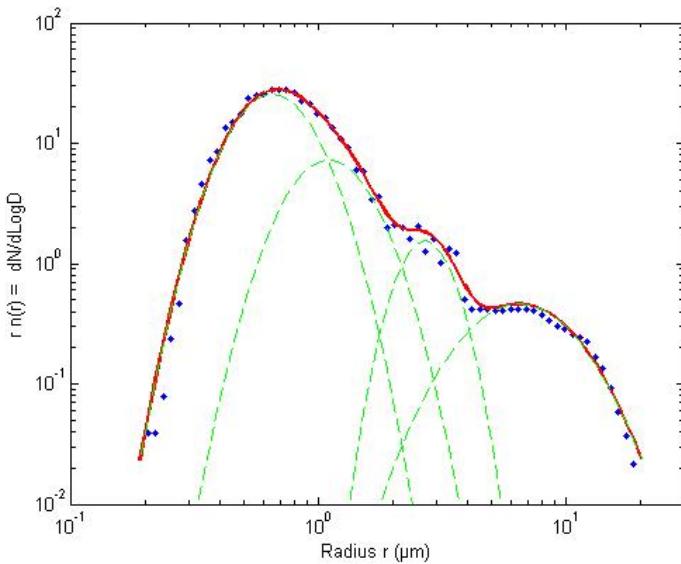


Fig. 1. Composite size distribution measured by Welas 2000 and FM100 on the 19 November 2010, at 05:40 UTC. The measurements (in parts by cubic meter and unit of natural logarithm of the diameter D) are the blue dots. A sum of $M = 4$ log-normal modes are fitted. Each mode is represented by green dashes. The sum fitted to the measurements is the red, solid, line. The parameters of the modes are given in Table 1 (fog case 10).

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Fig. 2. Extinction coefficients at $\lambda = 4 \mu\text{m}$ vs. the liquid water content for the 20 droplet size distributions studied in the paper. The liquid water contents are derived from the size distributions with Eq. (2). The grey dots are the extinction coefficients computed with Eq. (3) while the back curves and the diamonds show the extinction coefficients produced by the linear approximation proposed by Pinnick et al. (1979).

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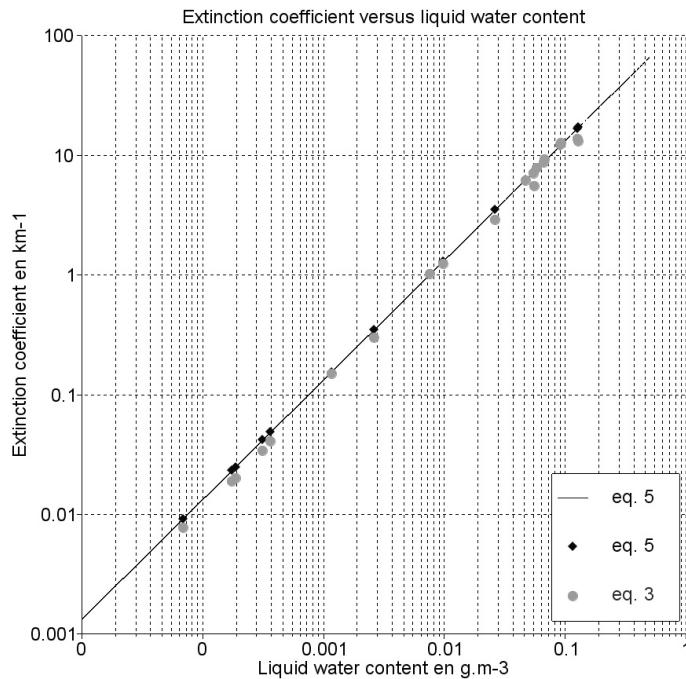


Fig. 3. Same as Fig. 2 for $\lambda = 11 \mu\text{m}$.

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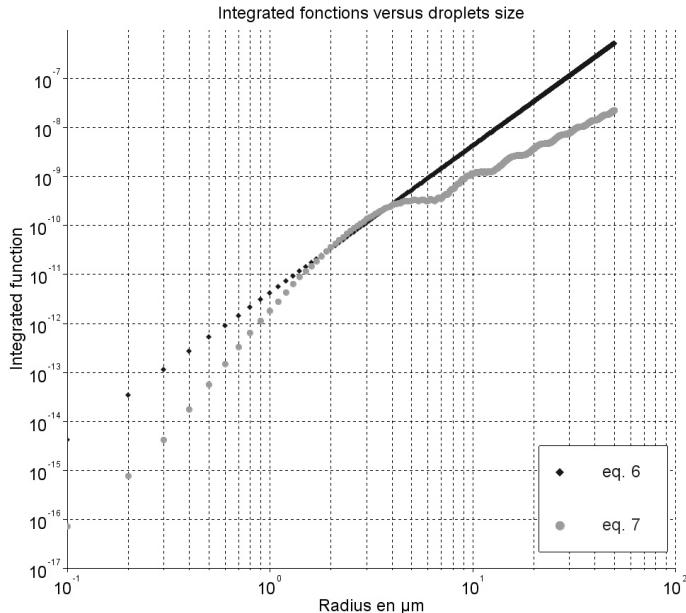


Fig. 4. Functions $F(r) = 4\pi\rho_{\text{H}_2\text{O}}r^3/3$ and $\hat{F}(r) = 4\rho_{\text{H}_2\text{O}}r^2Q_{\text{ext}}(r,\lambda)/(3c_e(\lambda))$ as a function of the droplet radius r for $\lambda = 4 \mu\text{m}$.

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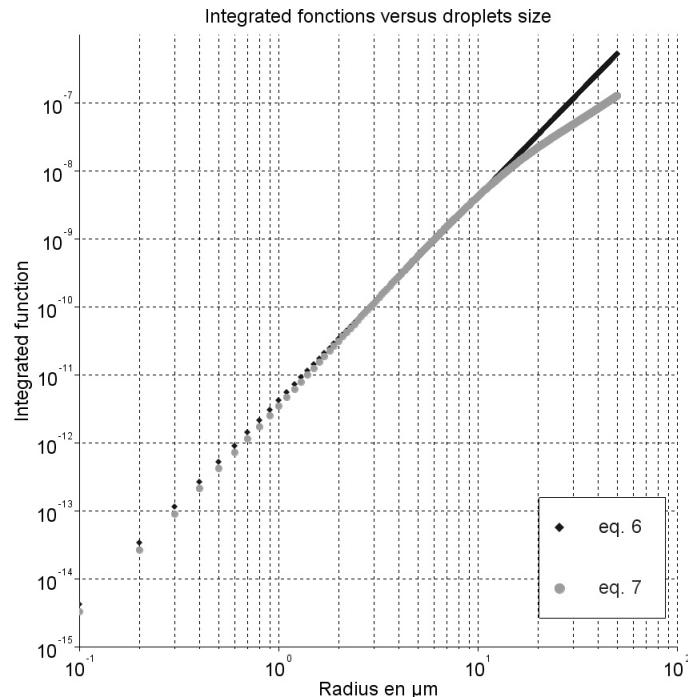
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**Fig. 5.** Same as Fig. 4 for $\lambda = 11 \mu\text{m}$.[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[|◀](#)[▶|](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

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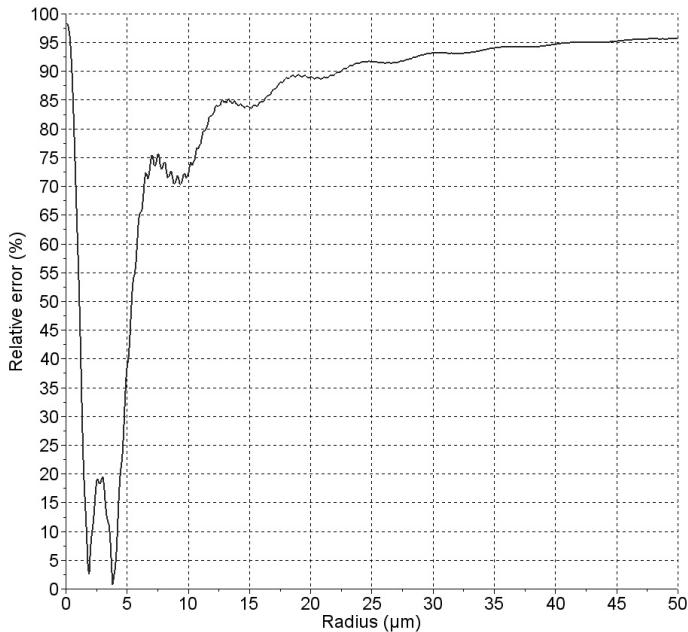


Fig. 6. Relative difference $|1 - \hat{F}/F|$ between $F(r)$ and $\hat{F}(r)$ (in %) for $\lambda = 4 \mu\text{m}$.

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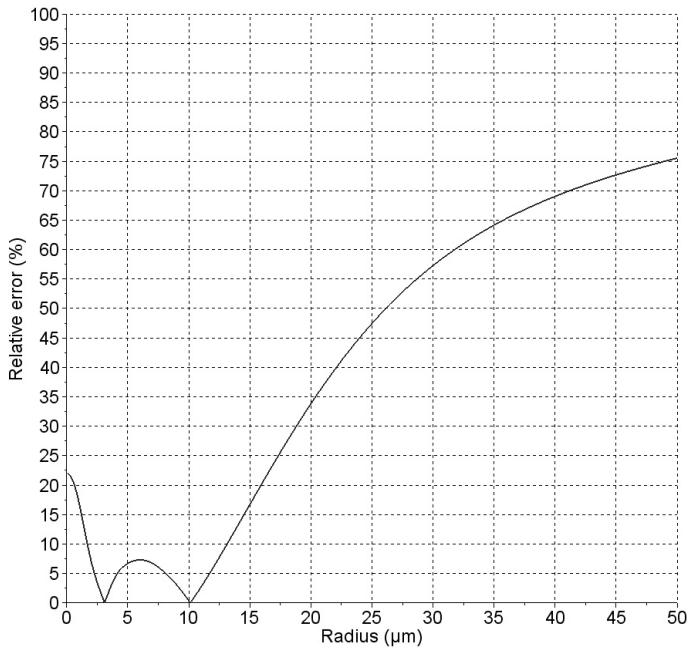


Fig. 7. Same as Fig. 6 for $\lambda = 11 \mu\text{m}$.

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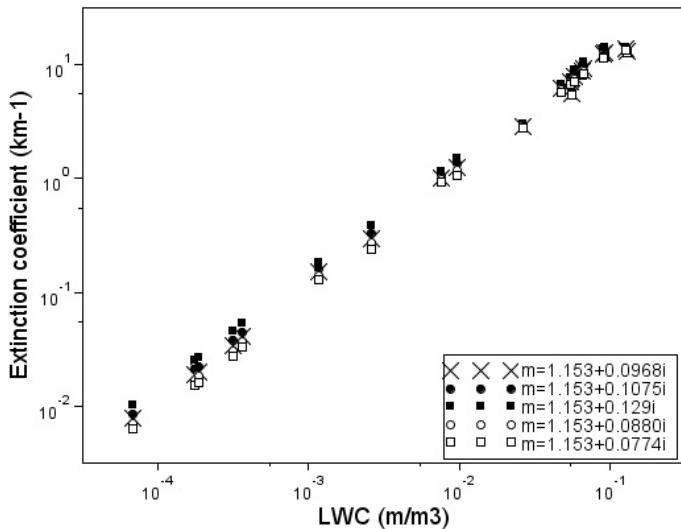


Fig. 8. Extinction coefficients (as a function of the liquid water content) for the 20 size distributions of PARISFOG for a refractive index with a variable imaginary part. The reference is the refractive index of water $m = 1.153 + 0.0968i$ (\times). The circles and squares are for the refractive indices that produce maximum extinction efficiency relative errors of 10 and 25 % respectively, in excess (filled) or default (open).

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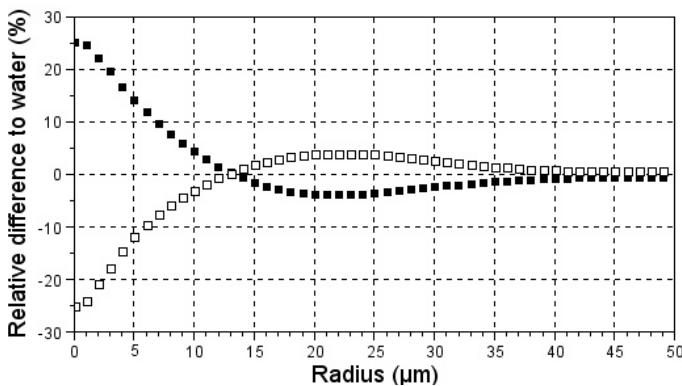
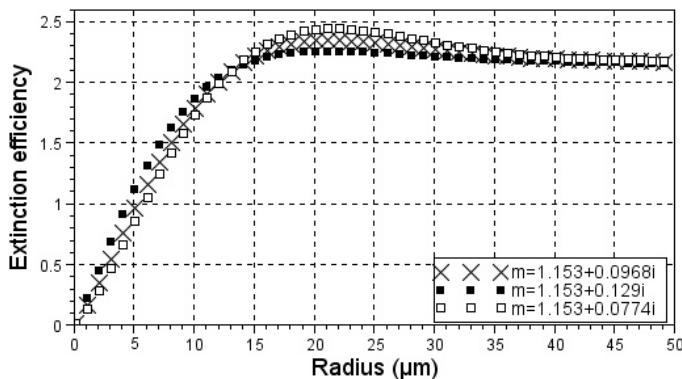


Fig. 9. Extinction efficiencies (top panel) for the refractive indices $m = 1.153 + i0.0968$ (water), $m = 1.153 + i0.129$ and $m = 1.153 + i0.0774$, and relative difference (in %) to pure water (bottom panel). The laser wavelength is 11 μm .

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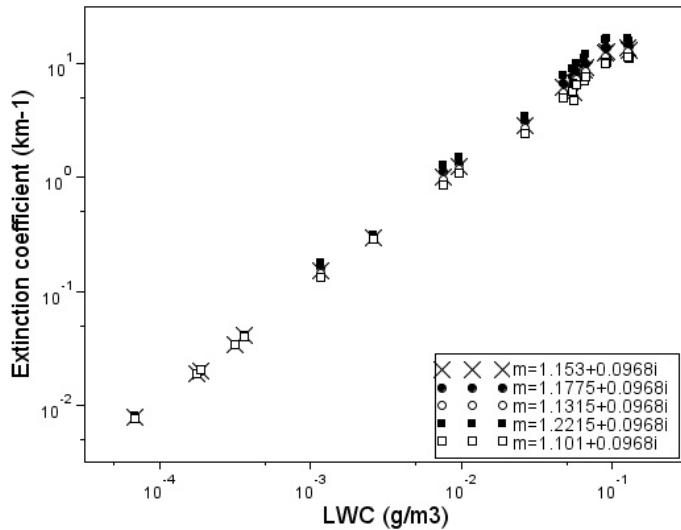


Fig. 10. Same as Fig. 8 for refractive indices with a variable real part.

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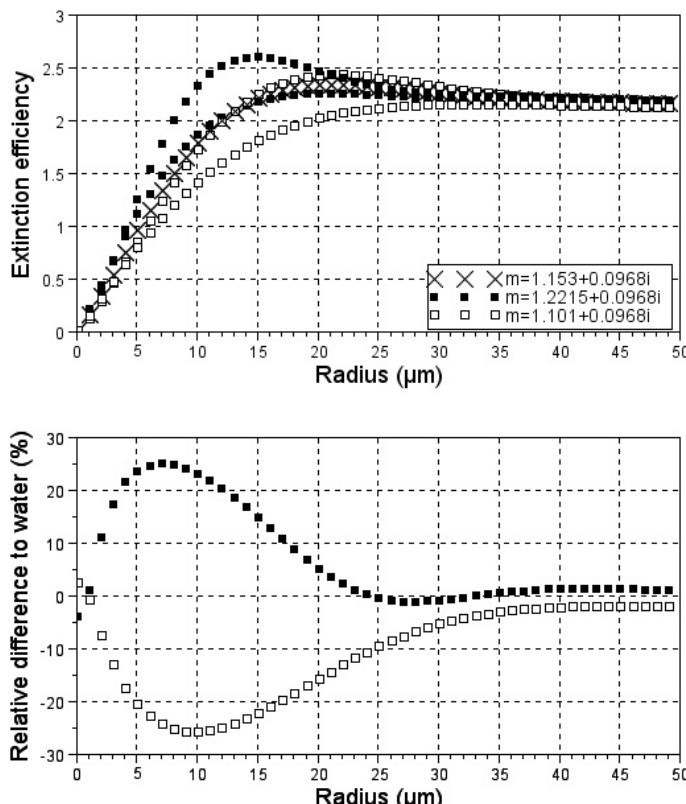


Fig. 11. Same as Fig. 9 for varying real parts of the fog droplet refractive index.

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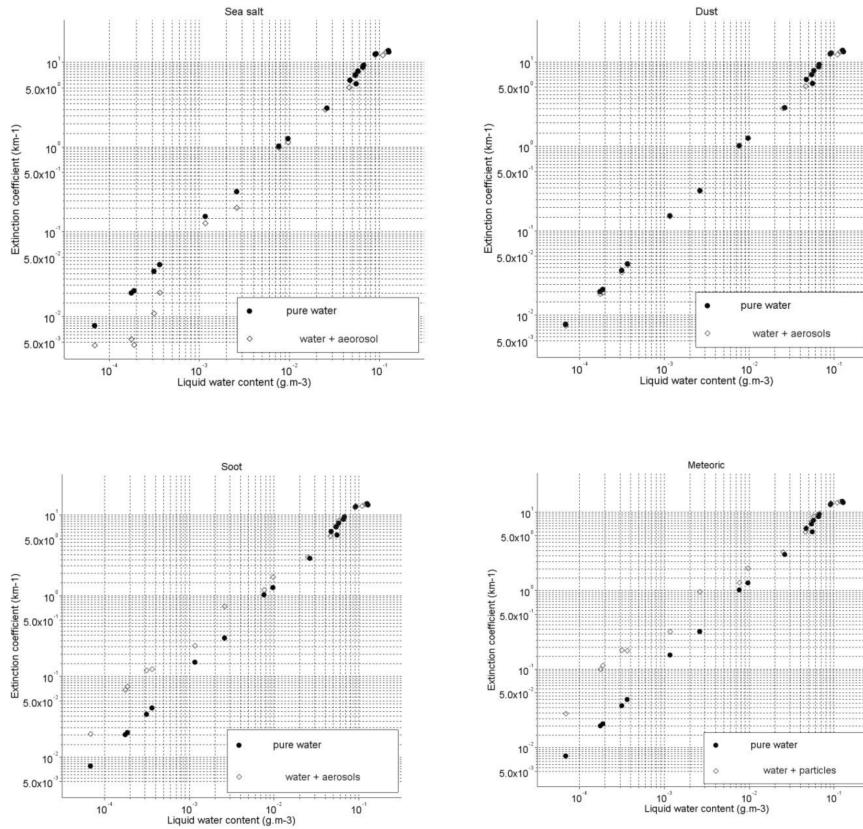


Fig. 12. Extinction coefficient vs. liquid water content for the 20 fog cases studied in the article and a refractive index for particles with radii $< 1 \mu\text{m}$ equal to the refractive index of sea salt (top left panel), dust (top right panel), soot (bottom left panel) and meteoric particles (bottom right panel) according to Fenn et al. (1985) (see Table 2). The extinction coefficients (in pink) are compared to the extinction coefficients obtained with the refractive index of pure water at $11 \mu\text{m}$.