

Interactive comment on “Investigation of ground-based microwave radiometer calibration techniques at 530 hPa” by G. Maschwitz et al.

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Investigation of Ground-Based Microwave Radiometer Calibration Techniques at 530 hPa

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Abstract

Ground-based microwave radiometers (MWR) are becoming more and more common for remotely sensing the atmospheric temperature and humidity profile, as well as path integrated cloud liquid water content. The calibration accuracy of the state-of-the-art MWR HATPRO-G2 (Humidity And Temperature Profiler - Generation 2) was investigated during the second phase of the Radiative Heating in Underexplored Bands Campaign (RHUBC-II) in Northern Chile (5320 m above mean sea level, 530 hPa) conducted by the the Atmospheric Radiation Measurement (ARM) program conducted between August and October 2009. This study assesses the quality of the two frequently used liquid nitrogen and tipping curve calibrations by performing a detailed error propagation study which exploits the unique atmospheric conditions of *RHUBC-II*. Both methods are known to have open issues concerning systematic offsets and calibration repeatability. For the tipping curve calibration an uncertainty of $\pm 0.1\text{K}$ to $\pm 0.2\text{K}$ (K-band) and $\pm 0.6\text{K}$ to $\pm 0.7\text{K}$ (V-band) is found. The uncertainty in the tipping curve calibration is mainly due the atmospheric inhomogeneities and the assumed air mass correction for the Earth curvature. For the liquid nitrogen calibration the estimated uncertainty of $\pm 0.3\text{K}$ to $\pm 1.6\text{K}$ is dominated by the uncertainty of the reflectivity of the liquid nitrogen target. A direct comparison between the two calibration techniques shows

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that for six of the nine channels which can be calibrated with both methods agree within the assessed uncertainties. For the other three channels the unexplained discrepancy is below 0.5K. Systematic offsets, which may cause the disagreement of both methods within their estimated uncertainties, are discussed.

Passive remote sensing instruments are widely used to retrieve atmospheric state variables. Measurements along the absorption lines of atmospheric gases can provide vertically resolved profiles of the gas concentration and/or temperature. Therefore, a realistic simulation of atmospheric absorption and emission is essential for the development of retrievals for atmospheric state variables. As radiative transfer models employ absorption line parameters that are obtained from laboratory measurements, field measurements are needed for independent evaluation. The aim of the Radiative Heating in Underexplored Bands Campaign (RHUBC-II) (Turner and Mlawer, 2010), which is part of the Atmospheric Radiation Measurement program (ARM) (Stokes and Schwartz, 1994), is to evaluate and improve existing absorption models. In addition to frequent radiosonde profiles of temperature, pressure and humidity, RHUBC-II data offers a unique set of accurate radiation measurements of the middle-to-upper troposphere. This paper concentrates on the microwave spectral region, which is widely used by space-borne and ground-based radiometers. For RHUBC-II this spectral range is covered by the passive microwave radiometer HATPRO-G2 (Humidity And Temperature Profiler- Generation 2). The radiometer has seven K-band channels along the rotational water vapor line at 22GHz to retrieve information about the atmospheric water vapor and liquid water content. Another seven V-band channels along the oxygen absorption complex at 60GHz are used to retrieve temperature profiles.

Ground-based temperature profiling using V-band frequencies has first been suggested by Westwater (1965) and is now performed operationally at several sites worldwide (Güldner and Spänkuch, 2001). However, compared to radiosondes profiles, temperature profiles derived from radiometric measurements can show biases up to 1K (Liljegren, 2002; Löhnert and Maier, 2011). It is still unknown whether these origi-

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nate from uncertainties in the oxygen absorption line parameters or from inaccuracies in the radiometer's absolute calibration. On the one hand, Cadeddu et al. (2007) evaluate oxygen absorption characteristics around 60GHz by radiometer measurements and test different sets of absorption coefficients. They show that different sets of oxygen absorption line parameters lead to retrieved temperature profiles that may differ by more than 2K. On the other hand, the accuracy of the commonly used liquid nitrogen (LN_2) calibration is found to be 1 – 2K (Liljegren, 2002). Similar issues are present in the K-band for the remote sensing of water vapor (Hewison, 2007). This makes clear that calibration and absorption model uncertainties are subject to the same level of uncertainty. Consequently, microwave radiometer calibration techniques need to be improved and well characterized before measurements may be used to evaluate current absorption models. Thus, the main goal of this paper is to evaluate two commonly used independent microwave radiometer calibration methods by carrying out a detailed error propagation by realistically considering multiple error sources.

The LN_2 calibration method is compared to the tipping curve method (Han and Westwater, 2000). Generally, all microwave channels can be calibrated using liquid nitrogen as a cold absolute standard. However, a successful tipping curve calibration requires a non-optically thick atmosphere at the frequency at stake. At sea level only K-band channels are transparent enough to be calibrated by this method. Fortunately, for the low pressure conditions at the RHUBC-II site, the tipping curve method can also be applied to the two most transparent V-band channels allowing a first-time independent evaluation of the LN_2 calibration in the V-band.

This paper is organized as follows: In Section 1 we briefly describe the RHUBC-II measurement campaign and the instrument which this study is based on. In the following Section 2 the theory behind calibration methods and the instrument used in this study is described, and Section 3 performs the actual calibration assessment. First, an error propagation study of the LN_2 calibration procedure is carried out in order to characterize the effects of different assumptions to the overall uncertainty. Specifically, these are

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the uncertainties attributed to the cold and hot target temperatures and emissivities, as well as to the detector non-linearity. Secondly, a similar procedure is carried out for the tipping curve calibration, where uncertainties such as pointing error, horizontal homogeneity and Earth curvature effects are discussed. Section 3.2.5 summarizes and compares the results of the two methods and Section 4 recommends steps to be taken in order to guarantee an optimal calibration result.

1 Measurement Campaign

The primary focus of RHUBC-II was to characterize and improve the accuracy of gas absorption models using high spectral resolution radiance observations in spectral regions that are normally opaque at lower altitudes due to strong water vapor absorption and high air pressure (Turner and Mlawer, 2010). The measurement site was set up at 5320m above mean sea level on the Cerro Toco next to the Chajnantor Plateau (22.96S, 67.77W). The plateau is part of the Atacama Desert in Northern Chile, which is one of the driest regions on Earth. Here, the amount of Precipitable Water Vapor (PWV) ranges from 0.1 – 5.0mm (Rutllant, 1977).

RHUBC-II was conducted within the dry season between August and October 2009. The ARM program set up a Self-Kontained Instrument Platform (SKIP) providing infrastructure and power supply for a variety of different instruments. Several radiometric instruments provide measurements almost across the entire infrared spectrum (Turner et al., 2012). The passive microwave radiometer HATPRO-G2 (Rose et al., 2005) took the data for this analysis and is described in detail below. The instrumentation was completed by an automatic weather station (AWS) and atmospheric profiles from 128 Vaisala RS92-K radiosondes launched during the campaign. During RHUBC-II PWV ranged from 0.2mm-1.5mm with an average value of 0.6 ± 0.3 mm. The synoptic station at the site recorded extraordinary constant surface conditions: a daily mean tempera-

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ture of $266.3 \pm 2.8\text{K}$, an air pressure of $532.2 \pm 2\text{hPa}$, and a relative humidity of $23 \pm 15\%$.

The HATPRO-G2 is a 14 channel total-power microwave radiometer measuring within the K- and the V-band allowing high temporal resolution *PWV*, Liquid Water Path (*LWP*), humidity and temperature profile retrievals from brightness temperature measurements. It was manufactured by Radiometer Physics GmbH and is operated by the University of Cologne. In the K-band, atmospheric radiation is measured at seven channels along the wing of the water vapor absorption line at 22.35GHz. Another seven V-band channels measure along the oxygen absorption complex centered around 60GHz (Fig. 1). The receivers of each frequency band are designed as filter-banks in order to acquire measurements at each frequency channel simultaneously. The channels have been designed with well characterized band-pass filters allowing precise frequency allocation of the signal. The eleven most transparent channels (K-band and V-band up to 54.94GHz) have a half power band-width of 230MHz. For the three remaining channels frequencies the spectral gradient is low, so wider band-widths of 600MHz, 1000MHz and 2000MHz provide higher precision at equal integration times. A parabolic mirror diameter of 250mm gives an antenna half power beam width for the channels along the water vapor line of 3.3-3.7 and 2.5-2.7 along the oxygen absorption complex. During RHUBC-II the radiometer was operated in a continuous scanning mode. It measured at symmetric elevation angles in a fixed azimuthal plane (70/250) at elevations 90.0, 45.0, 30.0, 15.0, 9.6 and 4.8. With an integration time of 1s each scan takes about 30s. In this study, these scans are used to apply the tipping curve calibration technique to the stored voltages of the nine low-opacity radiometer channels between 22.24GHz and 52.28GHz.

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2 Radiometer Calibration

Calibrating the radiometer means to determine the relation between the detected voltage (U_{det}) and the received power. The relation is derived by measuring against black body targets with a well known physical temperature T_{phys} . The spectral radiance B_ν that is emitted by the black body target is given by Planck's law:

$$B_\nu = \frac{2h\nu^3}{c^2} \frac{1}{\exp(\frac{h\nu}{k_b T_{phys}}) - 1} \quad (1)$$

in $\text{W m}^{-2} \text{sr Hz}^{-1}$, with the Boltzmann constant k_b and Planck's constant h . Calibration procedures based on Equation 1 provide measurements expressed in Planck equivalent brightness temperatures

$$T_b^{PL} = B_\nu^{-1}(I_\nu), \quad (2)$$

with the received spectral radiance I_ν . In the following, given temperature values are always Planck equivalent. The relation between detected voltages and measured brightness temperatures T_b is expressed by the following set of calibration parameters:

$$U_{det} = g T_{sys}^\alpha, \quad (3)$$

with the detector gain g , the total system noise temperature $T_{sys} = T_R + T_b$ – being the sum of the receiver noise temperature T_R and measured T_b – and the non-linearity parameter α (Radiometer Physics GmbH, 2011). At the beginning of every deployment period, the complete set of calibration parameters for HATPRO-G2 is determined by a LN_2 calibration. Additionally, during operation noise diode calibrations (every 30min) and hot load calibrations (every 5min) are performed. For details on the procedures'

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input and output parameters confer Table 1. In the following the different procedures are introduced.

2.1 Liquid Nitrogen Calibration

HATPRO-G2 uses a LN_2 target that is mounted alongside the radiometer for calibration. The calibration target is observed from above using a reflector which is tilted by 45°. The load is filled with a microwave absorber to guarantee the target's black body properties. The target temperature T_C is the actual boiling temperature of LN_2 . The hot load is an internal black body at ambient temperature T_H , where venting ensures a homogeneous temperature distribution. In order to take the system non-linearity α into account a 4-point calibration scheme is used (Fig. 2), which means that the radiometer measures at four calibration points to derive the calibration parameters g , T_R and α (Eq. 3) (Radiometer Physics GmbH, 2011). The determination of α is realized by noise injection from an internal noise diode (T_N). After integrating on the hot and cold target for 30s, respectively, the cycle is repeated with additionally injected noise. T_R , g , T_N and α are then determined by solving the following system of equations:

$$U_C = g (T_R + T_C)^\alpha \quad (4)$$

$$U_H = g (T_R + T_H)^\alpha \quad (5)$$

$$U_{CN} = g (T_R + T_C + T_N)^\alpha \quad (6)$$

$$U_{HN} = g (T_R + T_H + T_N)^\alpha, \quad (7)$$

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with U_C , U_H , U_{CN} , U_{HN} denoting radiometer voltages measured on the cold, ambient, cold plus noise and ambient plus noise references, respectively. Instead of using Planck spectral radiances $B_\nu(T)$ within these calibrations equations, Equation 1 is expanded in terms of $(h\nu/k_bT)$ and truncated after the first term. For HATPRO-G2's frequency range of $22\text{GHz} < f < 58\text{GHz}$ and temperature range of $T_C < T_{phys} < T_H$ the truncation error of this approximation is negligible. Furthermore, Equations 4 – 7 are valid within HATPRO-G2's frequency range, as long as the non-linearity α is close to one. This condition is fulfilled by the HATPRO-G2 receivers. As a consequence, the target's physical temperatures can directly be inserted into Equations 4 – 7. The derived calibration parameters and the resulting brightness temperatures agree with the black body equivalent brightness temperatures T_b^{PL} (Eq. 2).

After a successful calibration, T_N from a well burned-in noise diode is stable enough to serve as a secondary calibration standard during operation. During RHUBC-II only one single LN_2 calibration was performed after radiometer set up on August 11, 2009. Therefore, in Section 3.1.5), we give a repeatability analysis of the calibration procedure using LN_2 calibration performed with the same radiometer at the Research Center Jülich.

2.2 Tipping Curve Calibration

An alternative to the LN_2 calibration is the so-called tipping curve calibration which can be used to calibrate low-opacity radiometer channels. The general idea is to replace the LN_2 target by the cold clear sky. Han and Westwater (2000) discuss this method in detail and specify an absolute calibration accuracy of better than 0.5K for K-band channels. In principle, the method uses opacity-air mass pairs from elevation scans. T_b measurements are re-calibrated in an iterative process, where the opacity τ is calculated from the following equation:

$$\tau = \ln \left(\frac{B(T_{mr}) - B(T_{back})}{B(T_{mr}) - B(T_b)} \right), \quad (8)$$

with Planck spectral radiances B (Eq. 1). $T_{back} = 2.73\text{K}$ denotes the cosmic background radiation and T_{mr} is the mean radiative temperature of the atmosphere, which is calculated independently (Sec. 3.2.1). The tipping curve calibration encompasses a large brightness temperature range and Eq 8 is highly non-linear. Therefore, it is necessary to perform the tipping curve calibration in the power domain ($B(T_b)$) and convert the power values to black body equivalent T_b by the inverse of Equation 1 afterwards. Initial T_b values in Equation 8 are set by using a prior calibration or an educated guess. Assuming clear sky conditions and a homogeneously stratified and non-opaque atmosphere, the opacity scales linearly with the air mass for low optical depths along the slant path. The slope of this linear relation is the zenith opacity τ^{zen} . Zenith T_b^{zen} and τ^{zen} are connected by

$$B(T_b^{zen}) = B(T_{back}) e^{-\tau^{zen}} + B(T_{mr}^{zen}) (1 - e^{-\tau^{zen}}). \quad (9)$$

$B(T_b^{zen})$ provides an updated cold reference at zenith. This procedure is repeated iteratively and converges to optimal calibration parameters g and T_R (Eq. 3), assuming that α remains unchanged. For a perfect calibration the regression line would pass through the origin of the opacity-air mass diagram. However, deviations can result from horizontal atmospheric inhomogeneities within the scanned volume. Quality thresholds that guarantee the goodness of the fit are used to filter out tipping curve calibrations under inhomogeneous conditions.

Tipping curves are a standard calibration tool that is commonly used to calibrate K-band channels of ground based radiometers. During RHUBC-II the manufacturer's internal procedure performed a tipping curve calibration of the K-band channels every 6h. For this, the radiometer scanned towards an azimuth of 50.0N at the following

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elevation angles: 30.0, 33.3, 38.4, 45.6, 56.4 and 90.. Throughout the campaign 97 from 269 tipping curves passed the manufacturer's internal quality checks.

V-band channels are generally not included in tipping curve routines because at sea level, the opacity of these channels is too high. However, at 530hPa HATPRO-G2 channels at 51.26GHz and 52.28GHz are transparent enough to apply the tipping curve calibration. Zenith T_b is below 40K and 60K, respectively (Fig. 1) – well below the boiling temperature of LN_2 . For the analysis in this study the tipping curve calibration is not only applied to the K-band channels, but also the first two V-band channels (Sec. 3). Quality thresholds for the horizontal atmospheric homogeneity can be varied (cf. Sec. 3.2.5) and possible uncertainty sources can be investigated separately. The algorithm used within this analysis has been verified with K-band results from the manufacturer's internal calibration procedure.

2.3 Noise Diode Calibration

T_N is determined by every HATPRO-G2 LN_2 and tipping curve calibration (Sec. 2.1 and 2.2). T_N is stable enough to be used as a secondary calibration standard for several months (cf. Sec. 3.1.5). The stability of g for the V-band channels is guaranteed by injecting noise periodically – with a frequency of 10Hz – while the radiometer is pointing to an arbitrary scene (T_{scene}). T_{scene} can be extracted by using the fraction of the detected signal with and without noise.

Using T_R from a previous hot load calibration (cf. Sec. ??) gives a corrected detector gain g . Updating g with such high frequency is not necessary for the K-band channels, because the more stable Gallium arsenide (GaAs) technology compared to Indium Phosphide (InP) technology (V-band) is used. Therefore, in the K-band a noise calibration is performed every 30min to recalibrate T_R . The noise is injected while pointing to the ambient temperature target whereby T_R can be updated.

2.4 Hot Load Calibration

This calibration type uses the ambient hot load target as a reference. The hot load temperature T_H is known from a precision in-situ measurement within the target itself. HATPRO-G2 uses a second sensor to check for malfunction of the primary sensor. Generally, temperature gradients within the target may lead to a T_H that is not representative for the emitted radiance (McGrath and Hewison, 2001). For HATPRO-G2 such temperature gradients are sufficiently reduced ($< 0.2\text{K}$, Sec. 3.1.4), because the airflow from the internal blower covers the internal target. In order to correct for significant changes in HATPRO-G2's detector gain that occur on time scales longer than 5min, the hot load target is reviewed every 5min with an integration time of 4s. For the V-band channels, g is known from continuous noise switching (Sec. 2.3) and thus T_N is used to update T_R during every hot load target calibration.

3 Calibration Analysis

3.1 Liquid Nitrogen Calibration

Biases of 1-2 K are found when comparing simulated and measured T_b for radiometer channels along the oxygen absorption complex at 60GHz (Liljegren, 2002; Löhnert and Maier, 2011). However, it is left open whether these biases originate from uncertainties in the LN_2 calibration or in the oxygen absorption model. This bias would be too large for an absolute evaluation of absorption models because absorption model uncertainties are on the same order (Hewison and Cimini, 2006). Therefore, the absolute accuracy of HATPRO-G2 measurements is assessed by propagating uncertainties of the calibration parameters through the LN_2 calibration procedure. The contribution of each source of uncertainty is estimated by separately varying the individual input pa-

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rameters for U_{det} (Eq. 4 – 7). The total system noise temperature T_{sys} , when pointing to the LN_2 target, is modelled as:

$$T_{sys} = (1 - r) T_{tar} + r T_{cont} + T_R + T_N, \quad (10)$$

with the signal emitted by the target itself (T_{tar}), a contaminating component T_{cont} , which is reflected into the signal beam, the receiver noise T_R , and T_N , which is injected by an internal noise diode. r is the reflectivity of the calibration target:

$$r = \frac{(n - 1)^2}{(n + 1)^2}, \quad (11)$$

with n being the real part of the target's refractive index. r would be zero in case of a perfect black body target. For further information on reflectivities of radiometer calibration targets refer to Randa et al. (2005). T_N and T_R are determined by the calibration procedure (Eq. 4 – 7). The uncertainty of T_N and T_R results from error sources associated with T_{tar} , T_{cont} and r . The associated error sources are analyzed in the following.

An important error source of a calibration that uses an external LN_2 target is the formation liquid water on the radome due to condensation. This effect is not discussed here, because HATPRO-G2 uses a combined dew blower/heater system which effectively prevents condensation during measurements and LN_2 calibrations.

3.1.1 Boiling Point Correction

When calibrating against a liquid nitrogen target, the LN_2 boiling point serves as reference. At standard pressure ($p_0 = 1013.25\text{hPa}$) this is $T_0 = 77.36\text{K}$. However, the boiling point depends on the atmospheric pressure p and has to be corrected accordingly. For

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HATPRO-G2 the corrected boiling point is calculated from surface pressure supplied by the internal sensor. At 530hPa the correction is several Kelvin. Any inaccuracy in the applied correction impacts T_b – especially for scenes close to or below the cold calibration temperature. However, different instrument manufacturers use different formulas for the pressure dependent correction (Fig. 3):

$$T_C^{RPG} = T_0 - 0.00825 (1000.00 - p), \quad (12)$$

$$T_C^{RAD} = 68.23 + 0.009037 p, \quad (13)$$

with p in hPa. T_C^{RPG} and T_C^{RAD} refer to Radiometer Physics GmbH (2011) and Radiometrics (2007), respectively. The different formulations might be explained by the fact that the pressure dependency is often calculated for high technical pressures in the laboratory. At standard pressure the discrepancy between these formulations is still mostly negligible, however with decreasing pressure it increases and reaches 1.1K at 530hPa. In Figure 3 the impact of the different boiling point corrections on the calibration is shown. The effect itself is not frequency dependent, but the impact on measured T_b increases with decreasing channel opacity. It can be seen that moving away from the hot target increases the cold target's influence. At the LN_2 boiling point the discrepancy between the different corrections already exceeds 1K. The proper pressure-dependent correction for the LN_2 boiling point can be calculated from the Clausius-Clapeyron Equation:

$$\ln\left(\frac{p}{p_0}\right) = \frac{\Delta H_{vap}}{R} \left(\frac{1}{T_0} - \frac{1}{T}\right), \quad (14)$$

with the boiling point of liquid nitrogen T and the ideal gas constant R . Apart from the pressure Equation 14 only depends on the heat of vaporization ΔH_{vap} , which is constant for an ideal gas. Based on Equation 14 a consistent formulation is now used:

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$$T_C = \frac{710.5241}{9.185 - \ln\left(\frac{p}{1013.25}\right)}. \quad (15)$$

Using the atmospheric pressure during the LN_2 calibration at RHUBC-II of $p = 534.7$ hPa, Equation 15 gives a boiling point of $T_C = 72.2$ K. For RHUBC measurements this adapted boiling point decreases calibrated T_b values by up to 1.4K compared to the original LN_2 calibration (Eq. 12). Note, that the National Institute of Standards and Technology (NIST) gives a boiling point of $T_C = 72.3$ K at 534.7hPa (Span, 2000).

3.1.2 Refractive Index of Liquid Nitrogen

The refractive index of the LN_2 target n_{LN_2} determines the reflectivity r_{LN_2} of its surface (Eq. 11). n_{LN_2} is derived from laboratory measurements. Reesor et al. (1975) determine $n_{LN_2} = 1.2$ for a frequency range of 18GHz to 26GHz. The results are in agreement with several other experiments at frequencies between 0.5GHz (Hosking, 1993) and 130GHz (Vinogradov et al., 1967). Therefore, $n_{LN_2} = 1.2$, which corresponds to a reflectivity of $r_{LN_2} = 0.82\%$ (Tab. 2), is assumed for all HATPRO-G2 channels. The contaminating signal T_{cont} (Eq. 10) is estimated to originate from the receiver ($T_{rec} = 305$ K) and being reflected back at the LN_2 surface. As T_{rec} is much higher than the LN_2 target temperature even a small reflectivity results in a reflective component that has to be added to the cold target temperature. In this case, a reflective component T_{refl} is calculated to $T_{rec} = 1.9 \pm 0.6$ K when an n_{LN_2} uncertainty of ± 0.03 is assumed (Benson et al., 1983). The resulting T_b uncertainty reaches 1.4K for $T_b = 5$ K, which is the minimum measured T_b within the K-band during RHUBC-II (Fig. 4). The effect decreases linearly with higher T_b values. For the most opaque channels in the V-band the uncertainty reduces to 0.1 – 0.2K. Finally, it disappears at the hot calibration point.

Additionally, the LN_2 surface is exposed to the environment and is thus deformed by capillary waves and boiling bubbles. On the one hand, this can lead to frequency dependent interferences resulting in variations in the reflectivity r_{LN_2} of the target (Shitov et al., 2011), because the deformation length scale is on the range of the received signal wavelength. These variations are on time scales well below the integration time on the LN_2 target of 30s. Therefore, they are assumed to compensate each other over the integration period. On the other hand, air bubbles on the LN_2 surface reduce the density of the interacting surface. This effect will not be compensated by averaging and may improve the cold target's black body characteristics because r_{LN_2} is reduced. However, it is difficult to quantify this effect. Assuming that the density of the interacting LN_2 -air volume is reduced by 1% due to air bubbles would lead to a T_C reduced by 0.2K.

Resonance Effect

Continuous observations of the LN_2 evaporating from the cold load were carried out at the Research Center Jülich. The observations were conducted with the same radiometer that was previously deployed at RHUBC-II. While the level of the LN_2 declines, its distance to the receiver s increases and the resonance condition changes. The effect on T_{tar} (Eq. 10) can be interpreted as a small perturbation $r_{res}(s)$. Averaged over time $r_{res}(s)$ is zero ($\langle r_{res}(s(t)) \rangle = 0$). Via r_{res} these standing waves contribute to the reflective component:

$$T_{refl} = (r_{LN_2} + r_{res}(t)) (T_{cont} - T_C) \quad (16)$$

Note that r_{res} is unknown, because the reflectivity on the receiver end is not known. The corresponding amplitudes and phases of the observed signal are frequency dependent and affect the uncertainty of the calibration point. The maximum uncertainty

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is estimated to be twice the amplitude of the oscillation observed at each channel, because the integration time within the LN_2 calibration is small compared to the oscillation periods. K-band channels show oscillation amplitudes of 0.1K to 0.6K. In the V-band the noise level is generally higher making it more difficult to detect oscillations and may lead to a reduction of amplitudes, which are 0.1 – 0.3K. For both receiver bands, amplitudes in the band's center show higher amplitude. Most probable this is caused by the isolator which is located directly after the feed horn. The isolator is designed to cover the large band width of the whole receiver. Its performance might slightly decrease towards the band edges. Figure 4 shows the impact of the resonances on calibrated T_b for 23.04GHz. This channel has the largest uncertainty: for RHUBC-II measurements with T_b below 10K the maximum uncertainty range reaches 1.2K. The impact of the resonances can be diminished by integrating on the cold target for exactly one oscillation period. However, the periods are channel dependent. Therefore, a more practical solution is to determine the calibration parameters from repeated calibrations while the LN_2 evaporates. The remaining uncertainty is due to the fact that only a limited number of repetitions is possible before the LN_2 has evaporated. In this study, the maximum uncertainty from resonances is assumed, because for RHUBC-II only a single cold load integration was performed.

3.1.3 Non-Linearity Parameter

Concerning the non-linearity parameter α there are two aspects to be analyzed: 1.) the effect of α on the calibration characteristic ($T_b = f(U_{det})$) and 2.) its variability. The first point is addressed by simulating the LN_2 calibration with a classical 2-Point calibration scheme. This scheme is a simplification of the 4-point scheme: it assumes a linear relation between U_{det} and measured T_b ($\alpha=1$) and no additional noise is injected. The impact on the calibration characteristic is given in Figure 5. Apart from numerical effects, the impact diminishes at the two calibration points T_C and T_H . The impact on

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the calibration is slightly higher for V-band channels because α is generally smaller than for the K-band channels. Nevertheless, the effect depends on T_b : the maximum difference of 0.3K is reached at the lower end of the measured T_b range. Therefore, K-band channels are most affected. In any case, considering the detector non-linearity noticeably improves the calibration. The variability in α is investigated by 28 LN_2 calibrations that were performed with HATPRO-G2 at the Research Center Jülich, Germany between July 2010 and November 2011. α cannot be determined independently, because it characterizes the non-linearity of the whole radiometer system. Within the considered time period, no significant drift of α is found. Therefore, the standard deviation of α over all 28 calibrations reflects the random uncertainty of the α determination, which is 0.1 – 0.2% of the mean α value of each channel. It can be concluded that α is solely a frequency dependent instrument property. For the K-band channels the variability is largest at 22.24GHz and decreases with frequency. Figure 5 shows the impact on calibrated T_b , when the original α is varied within the range of uncertainty. Again, the effect is largest for small measured T_b . Combined with the higher variability of α , K-band channels are most affected. Anyway, the effect does not exceed ± 0.04 K (Tab. 5) and is therefore negligible.

3.1.4 Hot Load Temperature

All calibration types (Tab. 1) use the internal ambient target as a hot reference. The main source of uncertainty is the in-situ temperature measurement of the target. It is considered by assuming a maximum uncertainty of ± 0.2 K for the in-situ temperature measurement. This value is reasonable as it reflects the maximum deviation between the two temperature sensors within the ambient target during the campaign. For the three saturated V-band channels the resulting T_b uncertainty lies within ± 0.2 K and ± 0.3 K. For smaller T_b values the impact of the uncertainty within the in-situ measurement drops linearly. All other channels are affected by approximately ± 0.1 K.

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3.1.5 Repeatability and Validity

The repeatability is the capability of a calibration to reproduce the calibration parameters on time scales with negligible instrument drift. It is particularly important to assess the repeatability, because in this study a single LN_2 calibration is compared to a number of tipping curve calibrations. We address this issue by analysing 11 LN_2 calibrations that were performed within about two hours, using the same radiometer which was deployed at RHUBC-II. The measurements were conducted at the Juelich Research Center on November 10, 2011. It is assumed that the repeatability is characterized by the stability of the noise diode temperature T_N , which is determined with every calibration. Using T_N from the 11 calibrations allows to map the uncertainty within T_N into the range of measured brightness temperatures. For these simulations the detector voltages, the target temperatures, and the other three calibration parameters in a 4-point calibration scheme (the system noise temperature T_R , detector gain g and the detector non-linearity parameter α) are kept constant while only T_N is varied.

The impact on measured T_b is demonstrated for the HATPRO-G2 channels at 51.26GHz (Fig. 6). For this channel the standard deviation of T_N is $\sigma(T_N) = 2.0$ K. Variations in T_N affect T_b measurements below the hot calibration point T_H . The repeatability can be expressed by the standard deviation $\sigma(T_b)$. $\sigma(T_b)$ does not only depend on the variation of $\sigma(T_N)$, but also on the distance between T_N and T_H , and the T_b value itself. The lower T_b , the larger the impact of T_N variations. For typical T_b values at 51.26GHz under RHUBC-II conditions ($T_b \approx 38.4$ K) $\sigma(T_b)$ is 0.4K. The results are summarized for all channels in Figure 6. It shows that the repeatability $\sigma(T_b)$ ranges between 0.2K and 0.4K for the non-opaque channels. For the opaque channels above 54GHz, the impact of T_N on T_b is negligibly small, because the calibration is dominated by the ambient target temperature. It is assumed that the uncertainty is mainly caused by noise and small variations from calibration to calibration in the level of LN_2 in the cold calibration load, which changes the resonance condition for standing waves between the receiver

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and the LN_2 surface.

The second point we would like to address here is the validity period of the LN_2 calibration. This aspect is rather important for the V-band channels which cannot be calibrated by the tipping curve calibration. Measurements of these channels depend on the noise diode temperature derived from a liquid nitrogen calibration. Our paper includes a comparison of the liquid nitrogen calibration and the tipping curve calibration. Results of the liquid nitrogen calibration, performed on August 11, are compared to tipping curve results from August 16. This comparison is only possible when the instrument's drift in between the analyzed days is negligible.

Like the repeatability, the drift is recorded by the variation of T_N . We have analyzed 28 liquid nitrogen calibrations performed with HATPRO-G2 in at the Juelich Research Center between June 2010 and May 2012. A trend analysis of T_N for these calibrations reveals that T_N increases by $-0.012K$ to $+0.007K$ per day in the K-band and by $+0.046K$ to $+0.061K$ per day in the V-band (Tab. 3). This means that within the five days between August 11 and 16, T_N changes by less than $+0.1K$ in the K-band and $+0.3K$ in the V-band. The impact on T_b can be derived similarly to the repeatability analysis discussed above. We use the first calibration on November 10 performed in Jülich as reference. When this calibration is simulated with a T_N modified by the five day drift, T_b is affected by less than $0.05K$ for all channels and therefore we can conclude that the T_N drift is negligible for the analysis in this study (Tab. 3).

3.2 Tipping Curve Calibration

The tipping curve calibration results and the associated uncertainties are investigated by a procedure that uses the elevation scans in the $70N/250N$ azimuthal plane, which were continuously performed during RHUBC-II. The results from these elevation scans cannot be used to determine the detector non-linearity α and the noise diode temperature T_N , because no noise is injected during the scans. Nevertheless, calibrated zenith

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T_b values, which can be derived from each single scan do not depend on these parameters. Measurements at elevations 90.0 , 45.0 , 30.0 and 15.0 are considered in the calibration procedure used for this analysis. Expressed in terms of air masses these correspond to 1.0 , 1.4 , 2.0 and 3.0 . This is an advantage compared to the method used by Han and Westwater (2000), who combine zenith measurements with only one additional measurement at an air mass that varies between 1.5 and 4 . Fitting more than two opacity-air mass pairs allows the user to set quality thresholds that reduce the impact of atmospheric inhomogeneities on the calibration results (Sec. 3.2.5). From each scan passing the quality thresholds, zenith T_b is calculated from Equations 1, 8 and 9. Calibrated zenith T_b could then be used as a cold calibration point T_C to derive a T_b value for the scene. The impact of different possible sources of uncertainty are examined in the following. Furthermore, the most appropriate quality thresholds are determined.

3.2.1 Mean Radiative Temperature

The frequency dependent mean radiative temperature of the atmosphere T_{mr} is a required parameter for the calibration. If a radiosonde profile exists, it can be calculated using a radiative transfer model to compute the absorption coefficient and optical depth by:

$$T_{mr} = \frac{\int_0^\infty T(s) \beta(s) e^{-\tau(0,s)} ds}{1 - e^{-\tau(0,\infty)}}, \quad (17)$$

with the absorption coefficient $\beta(s)$, the physical temperature profile along the slant path $T(s)$ and the total opacity $\tau(0, \infty)$ along the slant path. T_{mr} must be determined prior to the calibration and cannot be determined from the radiometer itself. One possibility is to use a climatological T_{mr} derived from radiative transfer calculations with a climatology of atmospheric profiles. However, the tipping curve procedure is more accurate when the ambient surface temperature T_{surf} is used as predictor for T_{mr}

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in a linear regression scheme (Han and Westwater, 2000). Therefore, τ is calculated from RHUBC-II radiosonde profiles using the Rosenkranz'98 absorption model (Rosenkranz, 1998). Then, the predictand T_{mr} is calculated for the nine non-opaque HATPRO-G2 channels from 22.24–52.28GHz and different elevation angles from Equation 17. The surface temperature, taken from the campaign's *AWS*, is averaged over a time period of 5min before and 1h after launch of each radiosonde. Finally, linear regression coefficients are calculated from the obtained T_{mr} - T_{surf} -pairs. For 22.24GHz the *RMSE* (Root Mean Square Error) is 3.2K at three air masses. The *RMSE* decreases towards higher frequencies and reaches 1.1K/1.2K at 51.26GHz/52.28GHz at three air masses. The regression allows us to estimate T_{mr} from the continuous ambient surface temperature measurements throughout the campaign.

Figure 7 shows the sensitivity of calibrated zenith T_b to uncertainties in T_{mr} . Assuming an uncertainty of T_{mr} of one *RMSE*, affects T_b in the V-band by ≈ 0.1 K. In the K-band the effect has virtually no impact. In order to exclude the effect of biases within the radiative transfer calculations, these are compared to results from the Liebe'93 (Liebe et al., 1993) and the Liebe'87 (Liebe, 1987) model. At three air masses the different model result in a T_{mr} that agrees within 0.1K (Tab. 5). T_b results are not affected by such small differences. We can therefore conclude that T_{mr} can be derived from surface temperatures with sufficient accuracy for the tipping curve calibration.

3.2.2 Air Mass Correction

The tipping curve procedure uses scene observations to derive opacities at different air mass values. For a plane-parallel non-refracting atmosphere the air mass depends only on the elevation angle θ . In this case, the relative air mass is given by $a_0 = 1/\sin(\theta)$. However, for real observations the relative air mass differs from a_0 , when observing off zenith. On the one hand, the air mass is reduced due to the Earth's curvature. On the other hand, atmospheric refraction increases the air mass. The

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effects from refraction and curvature increase when approaching the horizon and affect the tipping curve results. Even though, the curvature effect is predominant, refraction is not negligible. Here, both effects are considered by a spherical ray-tracing algorithm that uses refractive index profiles derived from RHUBC-II radiosondes. The refractive index n is calculated at each level using a bulk formula:

$$n = 1 + \left(c_1 \frac{p-e}{T} + c_2 \frac{e}{T} + c_3 \frac{e}{T^2} \right) \cdot 10^{-6}, \quad (18)$$

with the atmospheric temperature T [K], the pressure p [hPa] and the partial pressure of water vapor e [hPa]. Here, the best available set of coefficients suggested by Rueeger (2002) is used:

$$c_1 = 77.695, \quad c_2 = 71.97, \quad c_3 = 3.75406, \quad \text{in } \text{K hPa}^{-1}. \quad (19)$$

The ray-tracing algorithm calculates the slant path lengths for each height layer. The slant path opacity $\tau(\theta)$ for the given radiosonde profile is then integrated over the full path length. Finally, the exact relative air mass value is given by:

$$a = \frac{\tau(\theta)}{\tau^{zen}}, \quad (20)$$

For each tipping curve scan, a is calculated by using the closest available radiosonde profile. The usage of a instead of a_0 does not notably affect the tipping curve results for K-band channels under RHUBC-II conditions. For the two V-band channels, the impact is higher: zenith T_b results are affected by $\Delta T_b^{zen} = +0.2$ K.

The uncertainty of the ray tracing algorithm is assessed by the variation between all four radiosondes of the analyzed day. It is found that the uncertainty does not have any effect on the tipping curve results. Using the air mass correction suggested by Han

and Westwater (2000) leads to an underestimation of T_b results by 0.1K at 51.26GHz and 52.28GHz, while the K-band is not affected.

3.2.3 Beam Width Correction

The tipping curve calibration assumes that T_b measurements are given at distinct nominal air masses. However, microwave radiometers receive the incoming radiation over an aperture that is defined by the antenna pattern (Han and Westwater, 2000). For HATPRO-G2 side lobe suppression is better than -30dB . Numerical simulations of the beam pattern reveal that 99.5% of the signal is received within an angular range of two half-power beam widths (HPBW). It is concluded that contribution from outside this range can be neglected.

Still, the finite HPBW affects the effective air mass value because T_b does not scale with the elevation angle. For transparent radiometer channels this results in an over-estimated T_b because a larger part of the signal is received from directions below the nominal air mass value. This effect on measured T_b increases with air mass. In order to derive T_b measurements for the nominal air mass values, the specified HPBW is used (Rose et al., 2005). The beam is modeled as a Gaussian shaped lobe with a doubled HPBW being 7 for the K-band and 5 for the V-band channels. It is resolved by equally distributed an weighted radiative transfer calculations around the nominal elevation angle with a resolution of 0.1 (air mass correction is included). The corrections are applied to all T_b measurements within tipping curve scans on August 16, 2009. For air masses between one and three, the correction is below 0.1K for the K-band channels due to the small opacities under the low water vapor conditions during RHUBC-II. At 51.26GHz and 52.28GHz, the correction is 0.1K and 0.2K at two air masses, and +0.5K and -0.5K at three air masses, respectively. Zenith T_b values from the tipping curve calibrations of these two channels are affected by 0.5K, when using air masses between one and three. Han and Westwater (2000) derive a theoretical T_b correction

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from a Gaussian shaped antenna pattern and an effective scale height. Compared to the numerical calculations with radiosonde profiles used here, this approach leads to a much smaller beam width correction: the impact on calibrated T_b would be less than 0.1K at three air masses for all channels.

3.2.4 Pointing Error

The tipping curve procedure is very sensitive to uncertainties in the radiometer elevation pointing. A miss-pointing of 1 can easily lead to a calibration error of several Kelvin (Han and Westwater, 2000). As mentioned before, the radiometer continuously performed elevation scans along the (70N/ 250N) azimuthal plane. The V-band channels at 51.26GHz and 52.28GHz show almost constant T_b differences between the two scanning directions that reach 2 – 3K at four air masses. Model simulations show that a large part of these differences are systematic and can be explained by a tilt of the instrument by 0.2 (Fig. 8). Note that the simulations consider the beam width and air masses in a spherical and refracting atmosphere (Sec. 3.2.2).

Han and Westwater (2000) point out that tilts can be balanced by averaging measurements of symmetric elevation angle prior to the tipping curve procedure. Nevertheless, the random effect from atmospheric inhomogeneities can not be compensated by this method. The effect of inhomogeneities on T_b increases with air mass as water vapor variations close to the surface are observed. This is reflected in the stronger variance of up to 0.7K at four air masses, when successive scan are compared (Fig. 8). This suggests that – depending on the measurement site and weather conditions – only measurements down to three air masses should be used for the tipping curve calibration. Furthermore, the considered air mass range may additionally be constrained by site dependent obstacles.

For the RHUBC-II deployment, the detected instrument tilt is not compensated by aver-

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aging, because the degree of homogeneity differs significantly towards both scanning directions. For the K-band channels, T_b measurements towards both azimuthal directions deviate from each other by up to 2K at four air masses. The difference can be explained by drier air masses over the hillside of Cerro Toco (70N) compared to the open plateau (250N). Consequently, in the K-band the number of succeeding successful scans towards both directions is reduced significantly. Therefore, scans towards both directions are separately used after correcting the elevation angles by 0.2. Finally, it is assumed that the correction results in a residual pointing uncertainty of 0.05. This uncertainty has no effect on the K-band channels results. Though, it increases with channel opacity and results in an $\pm 0.1\text{K}$ uncertainty of calibrated T_b in the V-band (Tab. 5).

3.2.5 Quality Control and Results

Five days after the original LN_2 calibration, the second operational day during RHUBC-II (August 16, 2009) offers ideal clear sky conditions for analyzing continuous tipping curve calibration. In addition to the available four radio soundings, detector voltages and T_b data from HATPRO-G2 were taken.

The quality of a tipping curve scan is estimated by two criteria which determine if the atmosphere is horizontally stratified to the required degree. Two measures are used to determine the goodness of the linear fit between measured opacities and air masses: the linear correlation coefficient $\text{corr}(\tau, a)$ and χ^2 , which is sensitive to deviations of τ from the linear relation to a . We are aware that these statistical quantities are not well-defined for the small number of used opacity-air mass-pairs. Nevertheless, they can be used to index the quality of the fit. χ^2 is defined in a relative way:

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$$\chi^2 = \sum_{i=0}^n \frac{(\tau_i^{\text{calc}} - \tau_i^{\text{fit}})^2}{\tau_i^{\text{calc}}} \quad (21)$$

This study indicates that a relative threshold of $\chi_{\text{max}}^2 = 1 \times 10^{-5}$ is most appropriate. Figure 9 illustrates the influence of different correlation thresholds on the tipping curve results. Naturally, raising the correlation threshold corr_{min} reduces the number of successful scans while increasing the calibration quality. Obviously, the quality threshold for χ^2 is a sensible supplement, because even scans with very high correlations coefficients fail. Generally, V-band channels show higher correlations than K-band channels, because the temperature field seems much more homogeneous than the atmospheric water vapor field. Different correlation thresholds have been tested and it is found that the manufacturer's default threshold ($\text{corr}_{\text{min}} = 0.9995$) is adequate for all calibrated channels. Higher values are not beneficial, because the standard deviation of all tipping curves on August 16, 2009 is not changed significantly. The number of successful tipping curves depends on the channel frequency: being small for the three K-band channels next to line center (49 – 69), there are 120 and 216 successful tipping curves in for the V-band channels at 51.26GHz and 52.28GHz, respectively (Tab. 4). Again, this indicates the high inhomogeneity of atmospheric water vapor that is most pronounced close to the line center at 22.235GHz.

Figure 10 shows time series of zenith T_b differences between successful tipping curve calibrations and the original LN_2 calibration for selected channels. In Table 4 the results are summarized for all calibrated channels. The assumed quality thresholds result in a good repeatability of the tipping curve calibration throughout the day. The standard deviation of ΔT_b over all scans is 0.1K-0.2K for the K-band channels. For the V-band channels at 51.26GHz and 52.28GHz it is 0.5K and 0.3K. It is assumed that this variability is induced by random processes as atmospheric turbulence and radiometer noise. Therefore, it can be used to estimate the random uncertainty of tipping curve calibrations. Twice the standard deviation gives the maximum uncertainty range of measured

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T_b from a single tipping curve calibration (Tab. 5). One possibility to eliminate the random variability is to take the daily mean average of the tipping curve results. A similar approach is taken by Liljegren (1999) who introduces a rolling dataset of calibration parameters to the calibration procedure of *ARM* radiometers.

[Summary and Discussion]

Two different calibration techniques for a state-of-the-art ground-based MWR have been assessed on the basis of RHUBC-II data. The most common error sources that need to be considered when specifying the accuracy of the brightness temperature measurements are discussed. Table 5 gives a summary of the different uncertainty contributions. Although the uncertainties discussed with respect to the LN_2 calibration are partially instrument specific, we note that *RPG*-HATPROs account for a major part of existing ground-based *MWRs* and thus this analysis is valid for a significant part of the world-wide available systems. The analysis of the tipping curve calibration is generally applicable to all ground-based *MWRs*.

3.3 Liquid Nitrogen Calibration

For the LN_2 calibration, a systematic error at 530hPa was identified and corrected for by applying an improved formulation of the pressure dependent boiling point of LN_2 . After this correction, the LN_2 calibration is mainly influenced by the temperature uncertainties of the cold and hot calibration targets. Here, the main contributions arise from the uncertainty of the reflective component that superposes with the signal from the LN_2 target. The reflective component depends on the refractive index of the liquid nitrogen surface n_{LN_2} and the strength of the standing wave that builds up between the LN_2 surface and the receiver. This leads to T_b uncertainties, because n_{LN_2} is not exactly known and the development of the standing wave depends on the level of evaporating LN_2 in the cold load target. Resonances primarily affect the K-band channels, because here the largest amplitudes are observed. Additionally, both effects are frequency de-

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pendent: The impact on calibrated T_b increases with decreasing T_b . Consequently, at RHUBC-II K-band channels – with measured T_b below 10K – are most affected.

Approaching the hot calibration point, uncertainties in the temperature measurement of the internal ambient target gain influence. It is shown that a non-zero reflectivity of the internal target can influence the derived T_b values. However, the effect is difficult to quantify because there is no information available on the uncertainty of the hot load reflectivity. In general, for different channels the overall uncertainty is between $\pm 0.3K$ and $\pm 1.6K$ (Tab. 5). Furthermore, the LN_2 calibrations benefit from considering the detector non-linearity parameter α within the 4-point calibration scheme. Compared to the 2-point calibration scheme neglecting α can result in a bias in the scene T_b in low opacity channels that is close to 0.2K.

3.4 Tipping Curve Calibration

Tipping curve results are very sensitive to the exact radiometer pointing. Therefore, scans on both sides of the radiometer were used to diagnose the instrument's tilt. The pointing is improved by compensating the instrument's tilt with a residual uncertainty of about 0.05. The residual effect is negligible in the K-band and even in the V-band T_b is only affected by 0.1K. Further sources of uncertainty are the derivation of the mean radiative temperature T_{mr} . The uncertainty of T_{mr} affect T_b by up to $\pm 0.3K$ in the V-band. Finally, the uncertainty of successful tipping curve calibrations is dominated by atmospheric inhomogeneities that are not completely excluded by the quality thresholds (Sec. 3.2.5). The inhomogeneities lead to uncertainties up to $\pm 0.2K$ in the K-band and up to $\pm 0.7K$ in the V-band. The contribution from atmospheric inhomogeneities can be reduced by averaging the results of several tipping curve calibrations instead of the current practice to use a single tipping curve for an extended measurement period.

Compared to Han and Westwater (2000) more realistic air mass and beam-width corrections – using observation from one to three air masses – are applied. In comparison

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to a plane parallel non-refracting atmosphere, the used air mass correction that considers the Earth curvature and refraction (Rueeger, 2002) raises calibrated zenith T_b by 0.2K at 51.26GHz and 0.1K at 52.28GHz. Neglecting the antenna beam width would increase zenith T_b measurements at RHUBC-II by up to 0.2K.

In total, all effects add up to an zenith T_b uncertainty up to $\pm 0.2\text{K}$ in the K-band and up to $\pm 0.7\text{K}$ in the V-band. It is important to mention that these estimations depend on the atmospheric conditions at RHUBC-II. The assessed uncertainties may deviate for locations with higher opacities.

3.5 Comparative Assessment

After assessing the uncertainties of the two calibration procedures, both are compared on the basis of calibrated zenith T_b on August 16, 2009. The average tipping curve results are compared to measurements based on original LN_2 calibration five days before (Fig. 11). However, in Section 3.1.5 it is shown that the comparison is still possible, because the instrument drift over this period is negligible. Zenith T_b from tipping curves are generally smaller than T_b derived from the LN_2 calibration. Table 4 shows that for the chosen quality thresholds ($corr_{min} = 0.9995$, $\chi_{max} = 1 \times 10^{-5}$) the difference $\Delta T_b = T_b(TIP) - T_b(LN_2)$ reaches the maximum of -1.3K . ΔT_b does not seem to depend on the number of averaged tipping curves, because the repeatability of tipping curve results throughout the day is very good ($< \pm 0.2\text{K}$, Tab. 4). For the two V-band channels the difference is -1.8K at 51.26GHz and -2.0K at 52.28GHz. Additionally, Figure 11 shows the results of the improved boiling point correction (Eq. 15). This correction significantly reduces the bias between the two calibration techniques to -0.4K at 51.26GHz and -0.7K at 52.28GHz (cf. Fig. 10 to 11). Apart from the channel at 27.84GHz, the tipping curve calibration in the K-band generally provides smaller T_b results than the LN_2 calibration. Still, the total uncertainty ranges of both calibration methods overlap for the two V-band channels and for most K-band channels (Fig. 11)

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when the updated boiling point correction is included. Only at 22.24GHz and 27.84GHz are slightly outside the overlap range (-0.2K and -0.4K , respectively). Nevertheless, the three lowest K-band channels show a bias, which systematically increases towards the line center. This rises the question whether an atmospheric water vapor signal has contaminated the LN_2 calibration via a reflective component (Sec. 3.1.2). Such an external atmospheric signal would reduce the reflective component and therefore calibrated T_b . An additional frequency dependent effect results from the antenna's beam width which increases with decreasing frequency. Therefore, the low frequency channels could be influenced by an external signal that originates from objects at ambient temperature or from the atmosphere.

Finally, the question which technique gives results that are closer to the truth cannot be answered. However, radiative transfer calculations for the K-band channels and the results from the tipping curve calibration agree very well: Zenith T_b measurements that are calibrated by the tipping curve calibration only deviate by 0.3K-0.8K from simulated T_b values from RHUBC-II radiosonde profiles for all K-band channels (Fig. 11). Therefore, we recommend to use the tipping curve calibration for the K-band channels whenever possible (Tab. 5). This is especially true for low opacity condition, where the uncertainty of tipping curve results are small and the results show a very good repeatability (Figure 10). In contrast, the LN_2 calibration suffers from large uncertainties at the cold calibration point: The influence of standing waves can be reduced by averaging calibration results. However, the T_b uncertainty resulting from an uncertain refractive index of LN_2 remains.

For the two V-band channels the uncertainty of the tipping curve is much larger than in the K-band, because most effects that impact the uncertainties grow with channel opacity. In the V-band, both calibration techniques are in good agreement, when the LN_2 calibration is used with the improved boiling point correction. Also simulations for 51.26GHz and 52.28GHz agree well with the tipping curve calibration results. Though, for the other non-opaque V-band channels below 56GHz, simulated T_b are systemati-

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cally smaller than T_b values from the improved LN_2 calibration. The difference reaches almost 3K at maximum. Still, T_b uncertainties for non-opaque channels are smaller than for the LN_2 calibration, which suffers from resonances and an uncertain refractive index of LN_2 in the V-band, too. Of course, the LN_2 calibration results can be tuned to the tipping curve results by adapting n_{LN_2} . However, when doing this, each channel provides a significantly different n_{LN_2} value. Furthermore, this excludes an independent comparison of both calibration techniques.

4 Outlook

Summarizing, a larger number of detailed uncertainty assessments are needed to explain the differences between the LN_2 calibration and the tipping curve calibration. Upcoming measurement deployments should be accompanied by an accuracy analysis of the two calibration methods. Particularly, it would be valuable to repeat the sensitivity study for radiometer measurements under different atmospheric conditions, because RHUBC-II covers only the extreme case of dry and relatively warm conditions at high altitudes. Parts of the estimated calibration uncertainties might scale with $T_{mr}(1 - e^{-\tau})$ of the observed atmosphere, as suggested by one of the reviewer's of this study. Other parts depend on the instrument type and the calibration procedure. At this point future deployments will help estimate how general the assessed calibration uncertainties are.

An important aspect concerning the LN_2 calibration is to verify its reproducibility by repeated calibrations. Additionally, frequent elevation scans help to improve the calibration accuracy by the tipping curve method. Using both methods simultaneously gives the opportunity to detect possible calibration problems.

Finally, when the calibration accuracy is properly assessed, the resulting T_b measurements can be used to validate gas absorption models. In contrast to the K-band where different absorption models show a good agreement, in the V-band T_b calculations from

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different models deviate by up to 2K. Any significant deviation from the measurement can then be assigned to the model spectroscopy, i.e. the absorption parameters. Here, RHUBC-II data gives the opportunity to validate gas absorption models in a very dry middle-to-upper troposphere.

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C1382



Fig. 1. Highly spectrally resolved brightness temperature (T_b , *top*) and opacity (τ , *bottom*), calculated by the Rosenkranz'98 absorption model (Rosenkranz, 1998), for the spectral range covered by HATPRO-G2. Spectral features are the water vapor absorption line 22.24GHz (*left*) the oxygen absorption complex at 60GHz (*right*). At 530hPa, pressure broadening is reduced and single transitions can be recognized in the spectral wing of the oxygen absorption complex



Fig. 2. Schematic illustration of a 4-point calibration: The detector voltage U_{det} is measured at four calibration points: U_C , U_H , $U_{CN} = U_C + U_N$, $U_{HN} = U_H + U_N$. T_R is the system noise power, U_N results from injected noise by the internal noise diode (T_N). T_C and T_H are known quantities, T_N and the non-linearity parameter α are determined by the calibration.

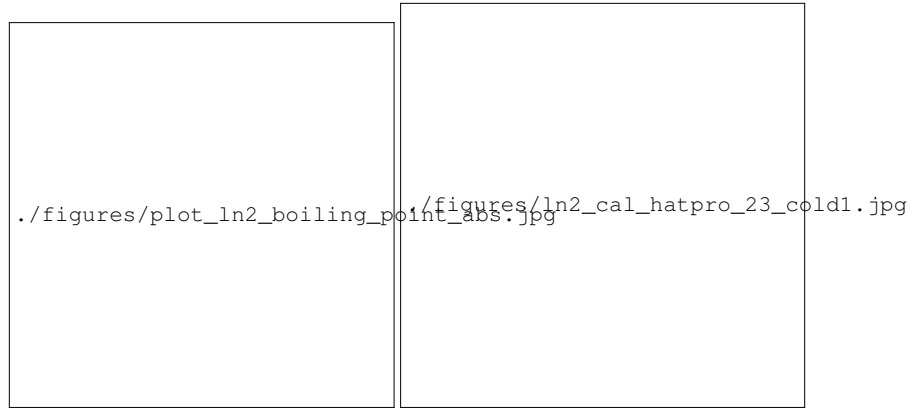


Fig. 3. Boiling point correction for LN_2 : Different radiometer manufacturers have used different formulations for the pressure dependent correction of the LN_2 boiling point: absolute boiling points (a) and their impact on derived T_b (T_b reference from Equation 15, b), *red*: Eq. 12, (Radiometer Physics GmbH, 2011), *green*: Equation 13, (Radiometrics, 2007), *blue*: new formulation (Eq. 15), *orange*: reference values (Span, 2000), *crosses*: calibration point T_C and T_H , *b*: impact on the derived T_b from differences in the assumed temperature of the cold calibration target (T_C). *Lines*: LN_2 calibration simulations using the different corrections for the 23.04GHz HATPRO-G2 channel, *X*: cold and hot calibration point.

C1385



Fig. 4. a: uncertainty in derived T_b from uncertainties at the cold calibration point: *blue*: area of uncertainty resulting from the uncertainty for the refractive index of the LN_2 surface ($n = 1.20 \pm 0.03$, (Benson et al., 1983)), *green*: area of uncertainty for a single calibration due to resonances between the LN_2 surface and the receiver, b: uncertainty in derived T_b from uncertainties at the hot calibration point: *red*: area of uncertainty from errors in the in-situ temperature measurement of the internal ambient target ($\Delta T_H = \pm 0.2K$), *X*: cold and hot calibration point, note that the y-axes of the two subplots have different limits.

C1386

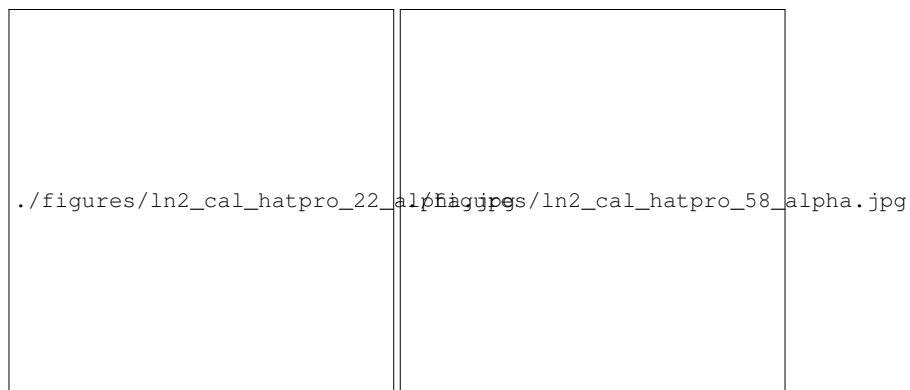


Fig. 5. The effect of the non-linearity parameter α of the radiometer system and its uncertainty on calibrated T_b for two exemplary HATPRO-G2 channels. The exact 4-point scheme solution serves as the reference (zero line), *red*: 2-point calibration ($\alpha = 1$, no noise injection), *green*: 2-point calibration using α from the original 4-point calibration performed at the beginning of RHUBC-II, *shaded area*: uncertainty resulting from random uncertainty of α .

C1387



Fig. 6. *a*): impact of variations in noise diode temperature T_N on T_b measurements for the 51.26K channel. Vertical lines mark the mean brightness temperature $T_b = 38.4\text{K}$, the ambient target temperature $T_H = 293.1\text{K}$, and the average noise diode temperature $T_N = 1501.3\text{K}$. The reference for ΔT_b is the first calibration on November 10, 2011 performed with HATPRO-G2 at the Juelich Research Center, *b*): repeatability of the LN_2 calibration. The mean difference ΔT_b from the reference calibration (first calibration on November 10) and standard deviation $\sigma(T_b)$ (error bars) of 11 LN_2 calibrations is given for all HATPRO-G2 channels. The colored numbers give the standard deviations $\sigma(T_N)$ and $\sigma(T_b)$.

C1388



Fig. 7. Sensitivity of calibrated T_b to uncertainties in the T_{mr} calculations. *Crosses*: ΔT_b resulting from a T_{mr} varied by $\pm 3 RMSE(T_{mr})$ ($RMSE$ = Root Mean Square Error), *solid*: linear fit, *dashed*: uncertainty area of one $rms(T_{mr})$ and the resulting uncertainty of T_b . The $RMSE(T_{mr})$ is 1.3K (51.26GHz) and 1.4K (52.28GHz).

C1389

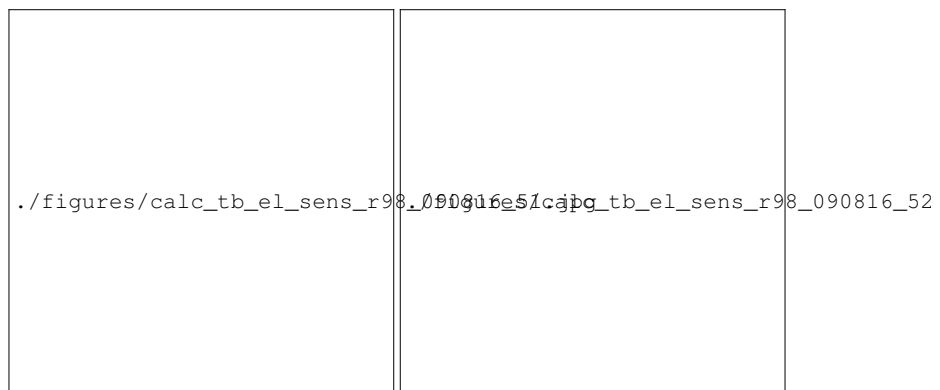


Fig. 8. *Lines*: radiative transfer calculations at different air masses for four clear sky radio sondes launched at 09:27LT, 10:39LT, 12:03LT, 13:44LT on August 16, 2009. Air masses are modified in order to simulate a tilt t of the radiometer by 0.1, 0.2 0.3: $\Delta T_b = T_b(el = el + t) - T_b(el = el - t)$, (el = elevation), *crosses*: mean HATPRO-G2 measurements during radiosonde ascents (5min before and 1h after each launch), radiative transfer calculations corrected air mass values, the antenna beam width and exact band-pass filters are considered.

C1390

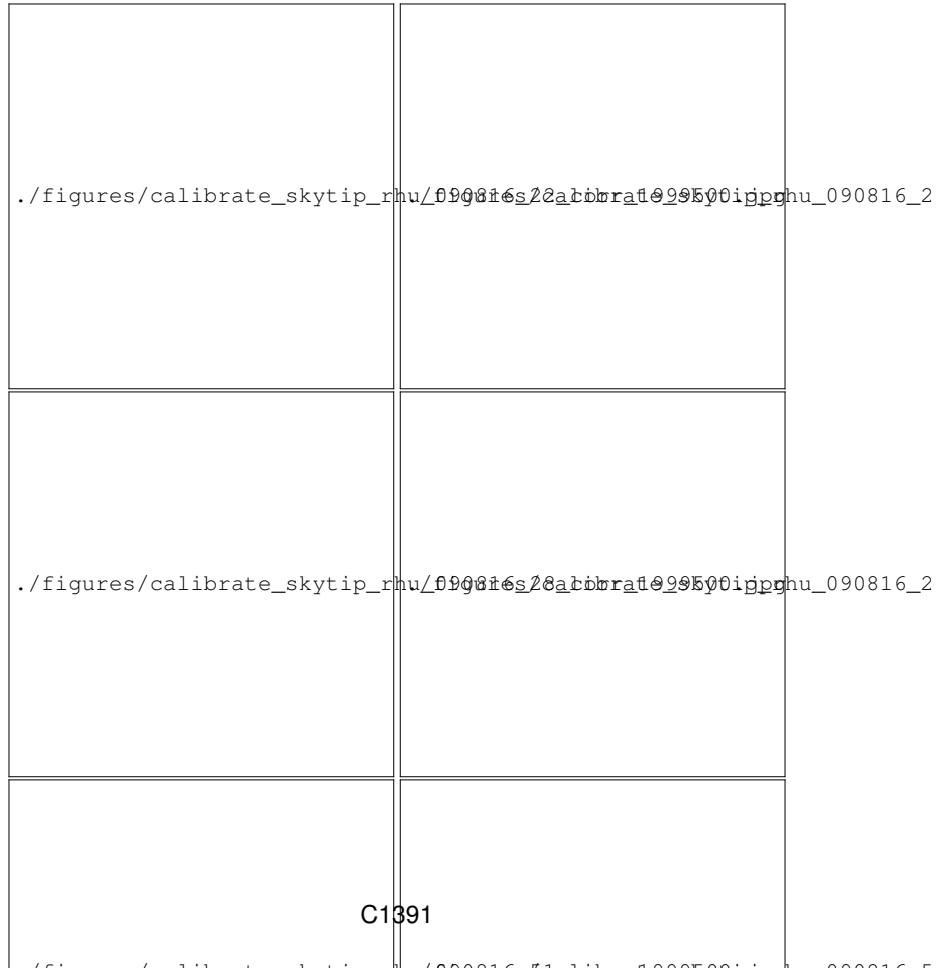


Fig. 10. Time series of tipping curve results $TB(TIP)$ (August 16) minus the original LN_2 calibration $TB(LN_2)$ on (August 11) for selected HATPRO-G2 channels. The daily mean value (standard deviation) is displayed within each subfigure. *Crosses*: one-sided elevation scans towards $70N$, *circles*: scans towards $250N$, *black line*: mean calibrated zenith T_b and standard deviation (dashed) for scans towards $250N$, quality control thresholds are set to $corr_{min} =$



Fig. 11. Calibration comparison for HATPRO channels (*left*: K-band, *right*: V-band): ΔT_b refers on the mean zenith T_b values based on the original LN_2 calibration on August 11, 2009 (boiling point correction Eq. 12). X : LN_2 calibration results with the improved boiling point correction (Eq. 15), *light blue*: estimated uncertainty range of the LN_2 calibration (Tab. 5), $+$: tipping curve results, *red*: estimated uncertainty range associated with the tipping curve calibration (Tab. 5), *green*: range of zenith T_b differences from radiative transfer calculations with three different absorption models: Liebe'87 (Liebe, 1987), Liebe'93 (Liebe et al., 1993) and Rosenkranz'98 (Rosenkranz, 1998). V-band calculations for < 56 GHz have been convolved with the real band pass filter shapes measured with a resolution of 10MHz.

C1393

Table 1. Information on the standard calibration schedule during RHUBC-II. For both frequency bands the *Type*, repetition *Period* and *Number* is given: liquid nitrogen calibration (LN_2), tipping curve calibrations (TIP), noise diode calibrations (NOI) and hot load calibrations (HOT). Pointing: 90.0=internal ambient target, 0.0= LN_2 target, i=input parameter, o=output parameter.

K-band channels				
Type	LN_2	TIP	NOI	HOT
Period	-	6h	30min	5min
Number	1	97	4067	14503
Pointing	-90/0	elev. scan	-90	-90
U_{det}	i	i	i	i
T_H	i	i	i	i
T_C	i	i	-	-
α	o	i	i	i
T_N	o	o	i	-
T_R	o	o	o	i
g	o	o	o	o
V-band channels				
Type	LN_2	TIP	NOI	HOT
Period	-	6h	cont.	5min
Number	1	-	-	14503
Pointing	-90/0	-	scene	-90
U_{det}	i	-	i	i
T_H	i	-	i	i
T_C	i	-	-	-
α	o	-	i	i
T_N	o	-	i	-
T_R	o	-	-	o
g	o	-	o	i

C1394

Table 2. Refractive indices, (n_{LN_2}) and reflectivities r_{LN_2} of the liquid nitrogen target and the resulting reflective components (T_{refl}) .

ν GHz	n_{LN_2}	r_{LN_2} [%]	T_{refl} [K]
<i>orig.</i>	1.20	0.82	1.9
<i>min</i>	1.17	0.61	1.4
<i>max</i>	1.23	1.06	2.3

C1395

Table 3. Results of 28 liquid nitrogen calibrations performed with HATPRO-G2 at the Juelich Research Center between June 2012 and May 2012. $\overline{T_N}$ is the mean value of the 28 calibration, $T(T_N)$ is the calculated trend, $D5$ represents the estimated 5 day drift over between the two days analyzed in this study, $D74$ estimates the drift over 74 days, corresponding to the duration of the measurement campaign RHUBC-II.

ν [GHz]	$\overline{T_N}$ [K]	$T(T_N)$ [K/day]	$D5(T_b)$ [K]	$D74(T_b)$ [K]
22.24	401.1	+0.007	-0.03	-0.41
23.04	399.0	+0.006	-0.02	-0.23
23.84	353.4	+0.005	-0.02	-0.30
25.44	342.5	+0.005	-0.02	-0.30
26.24	370.5	+0.005	-0.02	-0.29
27.84	363.3	+0.006	-0.02	-0.29
31.40	340.1	-0.012	+0.02	+0.23
51.26	1500.1	+0.046	-0.04	-0.52
52.28	1341.8	+0.059	-0.05	-0.69
53.86	1227.3	+0.054	-0.03	-0.49
54.94	1181.3	+0.046	-0.01	-0.19
56.66	1079.6	+0.049	-0.01	-0.12
57.30	1083.8	+0.048	-0.01	-0.11
58.00	1134.8	-0.061	-0.01	-0.12

C1396

Table 4. Difference (ΔT_b) of mean zenith T_b (standard deviation) [K] from successful tipping curve calibrations (TIP) on August 16, 2009 to T_b values based on the LN_2 calibration on August 11. $\Delta T_b = T_b(TIP) - T_b(LN_2)$. ΔT_b is calculated for different quality control thresholds within the tipping curve calibration (Sec. 3.2.5, n is the number of averaged successful tipping curve calibration on August 16, 2009. Results from calibrations including a beam-width correction and an exact air mass calculation are given in column ‘corr’. The uncorrected results are given in column ‘uncorr.’

$corr_{min} = 0.9995 / \chi_{max}^2 = 10^{-5}$					
ν [GHz]	corr.	n	uncorr.	n	
22.24	-1.3(0.2)	49	-1.2(0.2)	39	
23.04	-0.7(0.2)	50	-0.7(0.2)	49	
23.84	-0.5(0.2)	69	-0.5(0.2)	68	
25.44	-0.5(0.2)	125	-0.4(0.2)	133	
26.24	+1.0(0.2)	85	+1.0(0.2)	95	
27.84	-1.3(0.1)	67	-1.3(0.1)	71	
31.40	-0.5(0.2)	101	-0.5(0.2)	101	
51.26	-0.4(0.4)	120	-0.2(0.5)	130	
52.28	-0.7(0.3)	216	-0.4(0.3)	223	

C1397

Table 5. Assessed total calibration uncertainties for RHUBC-II in Kelvin. For the LN_2 calibration, the total uncertainty results from uncertainties of the refractive index of the LN_2 surface (n_{LN_2}), from resonances between the receiver and the LN_2 target (res), from uncertainties in the in-situ hot load measurement (hot), and from the detector non-linearity (α). The uncertainties are assessed for the mean T_b values measured at each channel on August, 16, 2009. For the tipping curve calibration the total uncertainty results from the derivation of the mean radiative temperature (T_{mr}), from the beam pointing (poi), and from atmospheric inhomogeneities (atm).

Liquid Nitrogen Calibration					
ν [GHz]	n_{LN_2}	res	hot	α	total
22.24	± 0.7	± 0.4	± 0.1	± 0.04	± 1.2
23.04	± 0.7	± 0.8	± 0.1	± 0.04	± 1.6
23.84	± 0.7	± 0.2	± 0.1	± 0.03	± 1.0
25.44	± 0.7	± 0.1	± 0.1	± 0.03	± 0.9
26.24	± 0.7	± 0.3	± 0.1	± 0.03	± 1.1
27.84	± 0.7	± 0.2	± 0.1	± 0.03	± 1.0
31.40	± 0.7	± 0.2	± 0.1	± 0.02	± 1.0
51.26	± 0.6	± 0.3	± 0.1	± 0.03	± 1.0
52.28	± 0.6	± 0.1	± 0.0	± 0.00	± 0.7
53.86	± 0.4	± 0.1	± 0.0	± 0.00	± 0.5
54.94	± 0.1	± 0.0	± 0.1	± 0.00	± 0.2
56.66	± 0.1	± 0.0	± 0.2	± 0.00	± 0.3
57.30	± 0.1	± 0.0	± 0.2	± 0.01	± 0.3
58.00	± 0.1	± 0.0	± 0.1	± 0.01	± 0.2
Tipping Curve Calibration					
ν [GHz]	T_{mr}	poi	atm		total
22.24	± 0.0	± 0.0	± 0.2		± 0.2
23.04	± 0.0	± 0.0	± 0.2		± 0.2
23.84	± 0.0	± 0.0	± 0.2		± 0.2