

# 1 Retrieval techniques for airborne imaging of methane 2 concentrations using high spatial and moderate spectral 3 resolution: Application to AVIRIS

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## 11 12 **Abstract**

13 Two quantitative retrieval techniques were evaluated to estimate methane (CH<sub>4</sub>) enhancement  
14 in concentrated plumes using high spatial and moderate spectral resolution data from the  
15 Airborne Visible/Infrared Imaging Spectrometer (AVIRIS). An Iterative Maximum a  
16 Posteriori Differential Optical Absorption Spectroscopy (IMAP-DOAS) algorithm performed  
17 well for an ocean scene containing natural CH<sub>4</sub> emissions from the Coal Oil Point (COP) seep  
18 field near Santa Barbara, California. IMAP-DOAS retrieval precision errors are expected to  
19 equal between 0.31 to 0.61 ppm CH<sub>4</sub> over the lowest atmospheric layer (height up to 1.04  
20 km), corresponding to about a 30 to 60 ppm error for a 10 m thick plume. However, IMAP-  
21 DOAS results for a terrestrial scene were adversely influenced by the underlying landcover. A  
22 hybrid approach using Singular Value Decomposition (SVD) was particularly effective for  
23 terrestrial surfaces because it could better account for spectral variability in surface  
24 reflectance. Using this approach, a CH<sub>4</sub> plume was observed extending 0.1 km immediately  
25 downwind of two hydrocarbon storage tanks at the Inglewood Oil Field in Los Angeles,  
26 California, with a maximum near surface enhancement of 8.45 ppm above background. At  
27 COP, the distinct plume had a maximum enhancement of 2.85 ppm CH<sub>4</sub> above background,  
28 ~~and was consistent with known seep locations and local wind direction~~ and extended more  
29 than 1 km downwind of known seep locations. A sensitivity analysis also indicates CH<sub>4</sub>

1 sensitivity should be more than doubled for the next generation AVIRIS sensor (AVIRISng)  
2 due to improved spectral resolution and sampling. AVIRIS-like sensors offer the potential to  
3 better constrain emissions on local and regional scales, including sources of increasing  
4 concern like industrial point source emissions and fugitive CH<sub>4</sub> from the oil and gas industry.

5

6 **Keywords:** Iterative Maximum a Posteriori Differential Optical Absorption Spectroscopy  
7 (IMAP-DOAS), Singular Value Decomposition (SVD), Retrieval, Methane, CH<sub>4</sub>,  
8 Concentration, Fugitive, Emissions, Point source, Plume, Coal Oil Point (COP) seep field,  
9 Inglewood Oil Field, Los Angeles, Airborne Visible/Infrared Imaging Spectrometer, AVIRIS

10

## 11 **1 Introduction**

12 Atmospheric methane (CH<sub>4</sub>) is a long-lived greenhouse gas with an instantaneous radiative  
13 forcing 21 times greater than carbon dioxide (CO<sub>2</sub>) on a per molecule basis (IPCC, 2007). In  
14 the late preindustrial Holocene (1000 to 1800 A.D.), mean concentrations were 695 ppb  
15 (Etheridge et al., 1998) and global concentrations have increased to around 1800 ppb in 2013  
16 (NOAA, 2013). While anthropogenic sources made up an estimated 4 to 34% of pre-industrial  
17 emissions (IPCC, 2007; Houweling et al., 2000), between 60 and 70% of emissions are  
18 presently anthropogenic (Lelieveld et al., 1998). Further, ice core records have indicated CH<sub>4</sub>  
19 concentrations are closely tied to atmospheric temperature records, while present-day  
20 concentrations have not been observed in the previous 420,000 years (Wuebbles and Hayhoe,  
21 2002).

22 While the global CH<sub>4</sub> budget is relatively well constrained (550 +/- 50 Tg CH<sub>4</sub> yr<sup>-1</sup>), there is  
23 considerable uncertainty regarding partitioning between individual natural and anthropogenic  
24 source types and locations (IPCC, 2007). Major sources of anthropogenic CH<sub>4</sub> emissions  
25 include the energy, industrial, agricultural, and waste management sectors. In the United  
26 States, 50% of anthropogenic CH<sub>4</sub> emissions are from the energy sector, including natural gas  
27 and oil systems, coal mining, and stationary/mobile combustion (EPA, 2011). Global fugitive  
28 CH<sub>4</sub> emissions from natural gas and oil systems are of increasing concern, estimated at  
29 | 1,354.42 million metric tonsMMT-CO<sub>2</sub> E yr<sup>-1</sup> (64.50 Tg CH<sub>4</sub> yr<sup>-1</sup>) and expected to increase  
30 35% by 2020 (EPA, 2006). Recent studies also suggest official inventories are  
31 underestimated, for example, top-down estimates indicate fugitive CH<sub>4</sub> emissions are between

1 2.3 and 7% of CH<sub>4</sub> produced annually for the Denver-Julesburg Basin, Colorado (Petron et  
2 al., 2012). In the Los Angeles Basin, CH<sub>4</sub> emissions appear underestimated (Wunch et al.,  
3 2009) and unaccounted sources appear to be fugitive and natural CH<sub>4</sub> emissions (Wennberg et  
4 al., 2012).

5 Significant natural CH<sub>4</sub> sources include wetlands, termites, and geological seeps (IPCC,  
6 2007). Globally, geological seeps are highly uncertain but estimated to contribute between 20  
7 to 40 Tg CH<sub>4</sub> yr<sup>-1</sup> for terrestrial environments (Etiope et al., 2009) and about 40 Tg CH<sub>4</sub> yr<sup>-1</sup>  
8 for marine seepage (Kvenvolden and Rogers, 2005). In addition, increased surface and ocean  
9 temperatures associated with global warming may increase CH<sub>4</sub> emissions from melting  
10 permafrost (Woodwell et al., 1998) and CH<sub>4</sub> hydrate destabilization (Kvenvolden, 1988).

11

## 12 **2 Airborne measurements of CH<sub>4</sub>**

13 Aircraft measurements of gas concentrations are useful because they offer the potential to  
14 measure local/regional variations in gas concentrations and complement ongoing efforts at  
15 coarser spatial resolutions, such as spaceborne sensors. These airborne measurements can  
16 improve greenhouse gas emissions inventories and offer the potential for detection and  
17 monitoring of emissions (NRC, 2010).

18 Research and commercial aircraft equipped with in situ gas measurement provides some sense  
19 of CH<sub>4</sub> variability at local and regional scales (ARCTAS, 2010; Schuck et al., 2012). The  
20 nadir-viewing Fourier Transform Spectrometer (FTS) included as part of the Carbon in Arctic  
21 Reservoirs Vulnerability Experiment (CARVE) (Miller and Dinardo, 2012) and spectrometers  
22 like MAMAP (Methane Airborne MAPper) (Gerilowski et al., 2011) also offer the potential  
23 to measure local emissions. For example, MAMAP detected elevated CH<sub>4</sub> concentrations  
24 from coal mine ventilation shafts near Ibbenbüren, Germany ~~(Krings et al., 2013)~~allowing for  
25 an inversion estimate that agreed closely with emission rates reported from mine operators  
26 (Krings et al., 2013). However, these non-imaging spectrometers have a small field of view  
27 (FOV) and are limited to flying transects across local gas plumes rather than mapping plumes  
28 in their entirety.

29 By combining large image footprints and fine spatial resolution, airborne imaging  
30 spectrometers are well suited for mapping local CH<sub>4</sub> plumes. ~~However, increased spatial~~  
31 ~~resolution requires reduced spectral resolution, thereby decreasing detection sensitivity.~~The

1 Airborne Visible/Infrared Imaging Spectrometer (AVIRIS) has a 34° FOV and measures  
2 reflected solar radiance at the nadir viewing geometry across 224 channels between 350 and  
3 2,500 nm (Green et al., 1998). Strong CH<sub>4</sub> absorption features present between 2,000 and  
4 2,500 nm can be observed at a 10 nm spectral resolution sampling and Full Width Half  
5 Maximum (FWHM). These absorptions are clearly shown in Fig. 1 by transmittance spectra  
6 calculated for CH<sub>4</sub> using Modtran 5.3 (Berk et al., 1989), parameterized for a mid-latitude  
7 summer model atmosphere and nadir-looking sensor at 8.9 km altitude. High resolution  
8 transmittance is shown in red for Fig. 1a and convolved to AVIRIS wavelengths in Fig. 1b,  
9 while water vapour (H<sub>2</sub>O) transmittance has been included in blue to indicate spectral overlap  
10 with CH<sub>4</sub>.

11 These shortwave infrared (SWIR) absorptions have permitted mapping of concentrated gas  
12 plumes in both marine and terrestrial environments using AVIRIS. For bright sun-glint scenes  
13 at the Coal Oil Point (COP) marine seep field in the Santa Barbara Channel, California,  
14 Roberts et al. (2010) developed a spectral residual approach between 2,000 and 2,500 nm and  
15 Bradley et al. (2011) a band ratio technique using the 2,298 nm CH<sub>4</sub> absorption band and  
16 2,058 nm carbon dioxide (CO<sub>2</sub>) absorption band. However, these techniques are not suited for  
17 terrestrial locations that have lower albedos and have spectral structure in the SWIR. A  
18 Cluster-Tuned Matched Filter (CTMF) technique is capable of mapping CH<sub>4</sub> plumes from  
19 marine and terrestrial sources (Thorpe et al., 2013) as well as CO<sub>2</sub> from power plants  
20 (Dennison et al., 2013), however, this method does not directly quantify gas concentrations.

21 The logical next step is to focus on quantification and uncertainty estimation using techniques  
22 originally developed for satellite sensors such as Differential Optical Absorption  
23 Spectroscopy (DOAS) (Platt, 1994). In this study, an Iterative Maximum a Posteriori  
24 Differential Optical Absorption Spectroscopy (IMAP-DOAS) (Frankenberg et al., 2005c)  
25 algorithm was adapted for gas detection in AVIRIS imagery. In addition, a hybrid approach  
26 using Singular Value Decomposition (SVD) and IMAP-DOAS was also developed as a  
27 complementary method of quantifying gas concentrations within complex AVIRIS scenes.

28

### 29 **3 Basic principles of IMAP-DOAS**

30 Retrieval algorithms for absorbing species in the SWIR require radiative transfer modelling of  
31 solar radiation along the light path to the sensor and must be capable of simulating changes in  
32 radiation due to differing abundances of absorbers. These techniques permit comparison of

1 simulated at sensor radiance with a known abundance of absorbers with measured radiance  
2 provided by the sensor. Differential Optical Absorption Spectroscopy (DOAS) (Platt, 1994) is  
3 one approach that has been used for a number of applications, including ground-based (Stutz  
4 et al., 2010), satellite (Schneising et al., 2012), and airborne measurement (Gerilowski et al.,  
5 2011). The underlying principle of DOAS is to isolate higher frequency features resulting  
6 from gas absorptions from lower frequency features that include surface reflectance as well as  
7 Rayleigh and Mie scattering (Bovensmann et al., 2011). To do so, a polynomial function  
8 accounting for low-frequency features is often used, which is described in further detail in  
9 Section 5.2.

10 Classical DOAS (Platt, 1994) is based on the Lambert-Beer law and describes the relationship  
11 between incident intensity for the vertical column ( $I_0(\nu)$ ) and measured intensity ( $I(\nu)$ ) after  
12 passing through a light path ( $ds$ ) containing ~~multiple-an~~ absorbers:

$$13 \quad I(\nu) = I_0(\nu) \cdot \exp\left(-\int \sigma(\nu, p, T)c(s)ds\right). \quad (1)$$

14 Each absorber has an associated absorption cross section ( $\sigma$ ) and number concentration of the  
15 absorber ( $c(s)$ , molecules/m<sup>3</sup>). Equation (1) is wavelength dependent and the absorption cross  
16 section varies with temperature ( $T$ ) and pressure ( $p$ ). If the atmospheric absorption features  
17 are fully resolved by the instrument and only weak absorbers are present~~For ideal instruments~~  
18 ~~(or weak absorbers),~~ Eq. (1) can be linearized with respect to slant column density  $S$ :

$$19 \quad \vec{\tau} = \ln\left(\frac{I_0(\nu)}{I(\nu)}\right) \approx \sigma(\nu, \bar{p}, \bar{T}) \cdot \int c(s)ds = \sigma(\nu, p, T) \cdot S. \quad (2)$$

20 where measured ~~differential~~ optical density ( $\vec{\tau}$ ) is proportional to the product of the absorption  
21 cross section and the retrieved  $S$ , the path integral of the concentration of the absorber along  
22 the lightpath.  $S$  is related to the vertical column density ( $V$ ), the integral of the concentration  
23 along the vertical from the surface to the top of atmosphere, by way of the airmass factor ( $A$ ),  
24 where  $A=S/V$ . In the SWIR, scattering in the atmosphere is generally low (Buchwitz and  
25 Burrows, 2003; Dufour and Breon, 2003) and for our applications, the impact of scattering is  
26 far lower than the retrieval precision error. Thus, it can be neglected and  
27  $A=1/\cos(\text{SZA})+1/\cos(\text{LZA})$ , where SZA is the solar zenith angle and LZA is the line of sight  
28 zenith angle. However, scattering could become non-negligible in some examples, including  
29 industrial plumes that contain heavy aerosol loading or dark surfaces with low SZA.

30 For a single absorber measured with a moderate spectral resolution and ignoring scattering, a  
31 theoretical slant optical density ( $\vec{\tau}_\lambda^{meas}$ ) can be calculated as follows

1  $\bar{\tau}_\lambda^{meas}(x) = -\ln(\langle \exp(-x \cdot A \cdot \bar{\tau}_\lambda^{ref}) \rangle).$  (3)

2 where the reference vertical optical density ( $\bar{\tau}_\lambda^{ref}$ ) is scaled by both the airmass factor ( $A$ ) as  
3 well as a retrieved scaling factor ( $x$ ) and  $\langle \cdot \rangle$  denotes convolution with the instrument  
4 function. In addition to scaling  $\bar{\tau}_\lambda^{meas}$ ,  $x$  can be used to estimate gas concentrations relative to  
5 those concentrations present within the reference atmosphere.

6 However, moderate spectral resolution spectrometers cannot fully resolve individual  
7 absorption lines and must convolve light using an instrument lineshape (ILS) function wider  
8 than individual absorption lines. ~~If absorptions are strong, this results in a non-linear~~  
9 ~~relationship between the measured differential-optical density ( $\bar{\tau}$ ) and the retrieved slant~~  
10 ~~column density of the absorber ( $S$ ) shown in Eq. (2) (Frankenberg et al., 2005c). Further,~~  
11 ~~optical densities can be large in the SWIR, especially in the 2,300 nm region, with its strong~~  
12 ~~H<sub>2</sub>O and CH<sub>4</sub> absorption lines are saturated within their line cores strengths.~~ These factors  
13 ~~render invalidate~~Eq. (2) ~~non-linear~~ and cause classical DOAS algorithms to fail, ~~requiring~~  
14 ~~iterative procedures to account for the induced non-linearity for moderate spectral resolution~~  
15 ~~spectrometers and strong absorbers.~~

16 To address the strong sensitivity of the shape of spectral absorption lines to temperature and  
17 pressure as well as unresolved absorption lines (Platt and Stutz, 2008), the Weighting  
18 Function Modified Differential Optical Absorption Spectroscopy (WFM-DOAS) retrieval  
19 algorithm was developed (Buchwitz et al., 2000). WFM-DOAS introduced weighting  
20 functions to linearize the problem about a linearization point in the expected slant column  
21 density using vertical profiles of all absorbers as well as pressure and temperature profiles. It  
22 has been used to estimate column amounts of CO (carbon monoxide), CO<sub>2</sub>, and CH<sub>4</sub> using  
23 Scanning Imaging Absorption Spectrometer for Atmospheric Chartography (SCIAMACHY)  
24 data, which has a spectral ~~sampling interval~~resolution between 0.2 and 1.5 nm (Buchwitz et  
25 al., 2005). A modified WFM-DOAS algorithm is used with the airborne MAMAP, which has  
26 a SWIR grating spectrometer for measuring CH<sub>4</sub> and CO<sub>2</sub> absorptions between 1,590 and  
27 1,690 nm with a 0.82 nm FWHM (Gerilowski et al., 2011)(Krings et al., 2011). In addition to  
28 detecting elevated CH<sub>4</sub> concentrations from coal mines (Krings et al., 2013), MAMAP has  
29 been used to measure both CH<sub>4</sub> and CO<sub>2</sub> emissions from power plants ~~(Gerilowski et al.,~~  
30 ~~2011)(Krings et al., 2011).~~

1 Frankenberg et al. (2005c) developed the IMAP-DOAS algorithm, which uses optimal  
2 estimation theory to adjust the slant column densities of multiple gasses until total optical  
3 density fits the observed measurement. IMAP-DOAS considers the shape of the spectral  
4 absorption lines as they vary with temperature and pressure in multiple atmospheric layers  
5 and convolves absorption lines using the instrument lineshape function. This technique is  
6 based on a simple non-scattering radiative transfer scheme, which allows very fast retrievals  
7 and is well suited for processing of AVIRIS imagery.—For the 2,300 nm range, where  
8 Rayleigh scattering can be ignored and aerosol optical depths are low, this assumption in  
9 IMAP-DOAS is valid given errors induced by neglected scattering in AVIRIS scene are  
10 typically much lower (0 to 2%) than precision errors in retrieved column estimates (>3%).  
11 Additional details of the IMAP-DOAS algorithm and retrieval method are presented in Sect.  
12 5.

13 While IMAP-DOAS has been used with SCIAMACHY data to estimate global column-  
14 averaged mixing ratios for CH<sub>4</sub> (Frankenberg et al., 2005a; Frankenberg et al., 2011) and CO  
15 (Frankenberg et al., 2005b), this study is the first to use aircraft measurements. Moderate  
16 resolution spectrometers like AVIRIS require large fitting windows and disentangling surface  
17 spectral features from atmospheric absorptions becomes more complicated using fitting  
18 routines such as WFM-DOAS and IMAP-DOAS. High resolution spectrometers can  
19 circumvent this problem since atmospheric absorption lines are narrow and surface properties,  
20 which vary on a scale greater than 5 to 10 nm, can be fitted using polynomial functions. In  
21 this case, reflectance spectra of terrestrial surfaces (not including narrow atmospheric  
22 features) can usually be represented by a low order polynomial as a function of wavelength.  
23 For the 10 nm spectral resolution sampling—and FWHM of AVIRIS, distinguishing surface  
24 features from atmospheric absorptions will be more difficult. Therefore, we developed an  
25 alternative hybrid approach using both IMAP-DOAS and SVD of surface reflectance  
26 properties at background CH<sub>4</sub> concentrations.

27

#### 28 **4 Study sites and AVIRIS data**

29 Two AVIRIS scenes were used in this study, both acquired in California in 2008. The first  
30 scene was acquired over the COP marine seep field near Santa Barbara from an 8.9 km  
31 altitude, resulting in an image swath of ~5.4 km and a ground instantaneous field of view  
32 (IFOV) of ~7.5 m. The scene was acquired on 19 June 2008 at approximately 19:55 UTC

1 | [\(12:55 PDT\)](#) with a  $11.4^\circ$  solar zenith resulting in high sun-glint. COP is one of the largest  
2 | natural seeps with total atmospheric  $\text{CH}_4$  emissions estimated at  $100,000 \text{ m}^3 \text{ day}^{-1}$  ( $0.024 \text{ Tg}$   
3 |  $\text{CH}_4 \text{ yr}^{-1}$ ) (Hornafius et al., 1999). A 308 by 191 pixel image subset was used for the IMAP-  
4 | DOAS and SVD algorithms, covering  $3.31 \text{ km}^2$  centered on the COP seep field  
5 | ( $34^\circ 23' 46.59'' \text{N}$ ,  $119^\circ 52' 4.47'' \text{W}$ ).

6 | The second scene covered the Inglewood Oil Field, located in Los Angeles in an area that has  
7 | active oil and gas extraction (DOGGR, 2010). The AVIRIS scene was acquired at  
8 | approximately ~~210~~:12 UTC [\(14:12 PDT\)](#) on 18 September 2008 at 4.0 km altitude, resulting  
9 | in a swath width of  $\sim 2.7 \text{ km}$ , ground IFOV of  $\sim 3 \text{ m}$ , and a  $38.1^\circ$  solar zenith. For this scene, a  
10 | 161 by 172 pixel image subset ( $0.25 \text{ km}^2$  centered at  $33^\circ 59' 28.68'' \text{N}$ ,  $118^\circ 21' 34.59'' \text{W}$ ) was  
11 | selected because it contains a  $\text{CH}_4$  plume detected using a CTMF technique, with hydrocarbon  
12 | storage tanks as a probable emission source (Thorpe et al., 2013).

13

## 14 | **5 IMAP-DOAS retrieval method**

15 | The IMAP-DOAS retrieval relies on layer optical properties of absorbing species calculated  
16 | for a realistic temperature/pressure and trace gas concentration profile for a given location. In  
17 | addition, instrument lineshape and flight parameters are used with geometric radiative transfer  
18 | calculations to simulate at-sensor radiances and Jacobians with respect to trace gas  
19 | abundances for each atmospheric layer. In the following, we describe input parameters and  
20 | additional details of the IMAP-DOAS retrieval.

### 21 | **5.1 IMAP-DOAS input parameters**

22 | For the two 2008 AVIRIS scenes, temperature, pressure, and  $\text{H}_2\text{O}$  volume mixing ratio  
23 | (VMR) profiles acquired from the National Centers for Environmental Prediction/National  
24 | Center for Atmospheric Research (NCEP/NCAR) Reanalysis project were extracted for the  
25 | appropriate date and time for either location (Kalnay et al., 1996). [The NCEP data are](#)  
26 | [provided on a  \$2.5^\circ\$  latitude  \$\times\$   \$2.5^\circ\$  longitude grid every 6 hours with 17 pressure levels](#)  
27 | [between 10 and 1,000 mb.](#) Prior profiles of  $\text{CH}_4$  and  $\text{N}_2\text{O}$  are based on the U.S. standard  
28 | atmosphere obtained from the radiative transfer models LOWTRAN/MODTRAN (Kneizys et  
29 | al., 1996). These profiles were scaled to reflect the VMR for  $\text{CH}_4$  and  $\text{N}_2\text{O}$  using the 2008  
30 | mean VMR provided from the NOAA Mauna Loa station, United States (NOAA, 2013). For  
31 | both gasses, the percent increase of the 2008 mean VMR compared to the U.S. standard



1 atmosphere at 0 km altitude was calculated and used to update the VMR up to 25 km altitude.  
2 Finally, we computed vertical optical depths for 10 atmospheric layers at 100 mb intervals  
3 between 0 and 1,000 mb.

4 For AVIRIS, the strongest CH<sub>4</sub> absorptions occur between 2,200 to 2,400 nm (Fig. 1).  
5 Spectral parameters for CH<sub>4</sub>, H<sub>2</sub>O, and N<sub>2</sub>O were used from the HITRAN database (Rothman  
6 et al., 2009). We used a classical Voigt spectral line-shape to calculate CH<sub>4</sub>, H<sub>2</sub>O, and N<sub>2</sub>O  
7 vertical optical densities for each of the 10 atmospheric layers.

8 Given that the two AVIRIS scenes were acquired at different flight altitudes and SZA,  
9 geometric air mass factors (AMF) had to be calculated for each of the 10 layers to account for  
10 either one (above sensor) or two (below sensor) way transmission through each layer. For  
11 example, the COP flight was at 8.9 km altitude with a solar zenith angle of 11.4°, placing the  
12 aircraft approximately at the boundary between atmospheric layer 3 and 4 (Fig. 2). In this  
13 simplified setup, the AMF for layers 1 to 3 (above the aircraft) is calculated as  
14  $1/\cos(11.4^\circ)=1.02$ , while for layers 4 to 10, an AMF of 2.02 ( $1/\cos(11.4^\circ)+1/\cos(0.0^\circ)$ )  
15 accounts for two way transmission. Similar calculations were performed for the Los Angeles  
16 scene, which was acquired with a SZA of 38.1° at 4.0 km altitude placing the aircraft  
17 approximately at the boundary between layer 5 and 6.

18 Additional input parameters for the IMAP-DOAS algorithm are shown in Fig. 3, including the  
19 AVIRIS radiance data, spectral ~~resolution sampling~~ of the sensor, signal-to-noise ratio (SNR)  
20 estimate, and the full width at half maximum of the instrument line-shape (FWHM=10.42 nm,  
21 assuming a Gaussian line-shape). An average FWHM and SNR was calculated for bands  
22 included within the fitting window, while the high resolution solar transmission spectrum was  
23 generated using a solar linelist (Geoffrey Toon, personal communication, 2013).

24 The optimal choice of a fitting window for the IMAP-DOAS CH<sub>4</sub> retrievals was determined  
25 iteratively. We began using all spectral bands between 2,100 and 2,500 nm corresponding to  
26 strong CH<sub>4</sub> absorptions, but observed strong correlations with surface features. This is likely  
27 related to spectrally smooth convolved transmissions from 2,200 to 2,300 nm and above 2,370  
28 nm (Fig. 1b). As we decreased the size of the fitting window to focus on the more high-  
29 frequency CH<sub>4</sub> features, the spectral variability associated with AVIRIS bands at either end of  
30 the fitting window was reduced and results improved. The fitting window selected for this  
31 study used 9 bands between 2,278 and 2,358 nm, including three prominent absorption  
32 features visible in CH<sub>4</sub> Jacobians shown in Fig. 4a.

## 1 5.2 Forward model and optimal estimation

2 Using 10 atmospheric layers and the gasses CH<sub>4</sub>, H<sub>2</sub>O, and N<sub>2</sub>O results in a state vector with  
3 30 rows ( $\vec{x}_n$ ). ~~In principle, N<sub>2</sub>O could be neglected at this spectral resolution but we included~~  
4 ~~it for the sake of completeness.~~ A forward radiative transfer model at high spectral resolution  
5 was used to calculate modeled radiance at each wavelength using the equation below

$$6 \quad \vec{F}^{hr}(\vec{x}_i) = \vec{I}_0^{hr} * \exp\left(-\sum_{n=1}^{30} \vec{A}_n \cdot \vec{\tau}_n^{ref} \cdot \vec{x}_{n,i}\right) * \sum_{k=0}^K a_k \lambda^k. \quad (4)$$

7 where

8  $\vec{F}^{hr}(\vec{x}_i)$  is the forward modeled radiance at the i-th iteration of the state vector,

9  $\vec{I}_0^{hr}$  is the incident intensity (solar transmission spectrum),

10  $\vec{A}_n$  is the AMF for each n ~~layer of each gas number of atmospheric state vector elements~~ (30  
11 rows, specified for each of the 10 layers and repeated for each gas),

12  $\vec{\tau}_n^{ref}$  is the reference total optical density for each n number of atmospheric state vector  
13 elements layer (the sum of including optical densities of CH<sub>4</sub>, H<sub>2</sub>O, and N<sub>2</sub>O),

14  $\vec{x}_{n,i}$  is the trace gas related state vector at the i-th iteration, which scales the prior optical  
15 densities of CH<sub>4</sub>, H<sub>2</sub>O, and N<sub>2</sub>O in each n layer (30 rows).

16  $a_k$  are polynomial coefficients to account for low-frequency spectral variations.

17 The high resolution modeled radiance is then convolved with the ILS and sampled to the  
18 center wavelengths of each AVIRIS spectral band. This results in a low resolution modeled  
19 radiance at the i-th iteration of the state vector ( $\vec{F}^{lr}(\vec{x}_i)$ ), calculated using a known  $\vec{\tau}_n^{ref}$  scaled  
20 by  $\vec{x}_{n,i}$ .

21 In addition to the priors-scaling factors for CH<sub>4</sub>, H<sub>2</sub>O, and N<sub>2</sub>O in each n layers ( $\vec{x}_n$ ), the state  
22 vector ( ~~$\vec{x}_a$~~ ) contains the spectral shift (not shown here) as well as a low order polynomial  
23 function ( $a_k$ ) to account for the broad-band variability in surface albedo (see Frankenberg et  
24 al., 2005c).

25 At each iteration i, a Jacobian Matrix is calculated where each column represents the derivate  
26 vector of the sensor radiance with respect to each element of the state vector ( $\vec{x}_i$ ).

$$27 \quad \mathbf{K}_i = \left. \frac{\partial \vec{F}^{lr}(\vec{x})}{\partial \vec{x}} \right|_{\vec{x}_i}. \quad (5)$$

1 The forward model and the Jacobian Matrix can be used to optimize the state vector at the i-th  
2 iteration as follows (Rodgers, 2000)

$$3 \quad \vec{x}_{i+1} = \vec{x}_a + (\mathbf{K}_i^T \mathbf{S}_\varepsilon^{-1} \mathbf{K}_i + \mathbf{S}_a^{-1})^{-1} \mathbf{K}_i^T \mathbf{S}_\varepsilon^{-1} \cdot [\vec{y} - \vec{F}^{lr}(\vec{x}_i) + \mathbf{K}_i(\vec{x}_i - \vec{x}_a)]. \quad (6)$$

4 where

5  $\vec{x}_a$  is the a priori state vector (30 rows),

6  $\vec{x}_i$  is the state vector at the i-th iteration (30 rows),

7  $\mathbf{S}_\varepsilon$  is the error covariance matrix,

8  $\mathbf{S}_a$  is the a priori covariance matrix,

9  $\vec{y}$  is the measured AVIRIS radiance,

10  $\vec{F}^{lr}(\vec{x}_i)$  is the forward model evaluated at  $\vec{x}_i$ ,

11  $\mathbf{K}_i$  is the Jacobian of the forward model at  $\vec{x}_i$ .

12 The a priori state vector was set to 1 for each gas at each layer, while the a priori covariance  
13 matrix was set to constrain the fit to the lowest atmospheric layer (height up to 1.04 km)  
14 where high variance is expected. To achieve this, very tight prior covariances were set for all  
15 atmospheric layers except the lowermost one, which is basically unconstrained. This  
16 assumption is reasonable given that the COP and Inglewood scenes contain CH<sub>4</sub> emission  
17 from ground sources that are not expected to extend above this atmospheric layer. CH<sub>4</sub>  
18 concentrations were calculated by multiplying the CH<sub>4</sub> state vector at the last iteration (CH<sub>4</sub>  
19 scaling factor) by the VMR for the lowest layer of the reference atmosphere (Fig. 2).

20

## 21 **6 Basic principles of SVD**

22 SVD transforms a large number of potentially correlated vectors into a smaller set of  
23 uncorrelated (orthogonal) vectors, denoted as singular vectors (Press et al., 2007; Rodgers,  
24 2000). It is closely related to Principal Component Analysis (PCA) and offers the potential for  
25 reduced computation time by efficiently summarizing high dimensional data. It has been used  
26 in a number of remote sensing applications, including cloud detection using the Michelson  
27 Interferometer for Passive Atmospheric Sounding (MIPAS) (Hurley et al., 2009), retrieving  
28 aerosol optical densities of mineral dust using the Infrared Atmospheric Sounding  
29 Interferometer (IASI), and retrieval of terrestrial chlorophyll fluorescence using the Fourier

1 Transform Spectrometer (FTS) onboard the Greenhouse gases Observing SATellite (GOSAT)  
2 platform (Guanter et al., 2012).

3 For this study, we constructed an  $m \times n$  matrix  $\mathbf{L}$ , where  $m$  is the number of spectral bands  
4 (for the  $\text{CH}_4$  fit window) and  $n$  is the number of radiance spectra in a specific AVIRIS scene.  
5 This can be expressed as

$$6 \quad \mathbf{L} = \mathbf{U}\mathbf{\Lambda}\mathbf{V}^T. \quad (7)$$

7 where the  $m \times m$  matrix  $\mathbf{U}$  contains the left singular vectors and the  $n \times n$  matrix  $\mathbf{V}$  contains  
8 the right singular vectors in their respective columns.  $\mathbf{\Lambda}$  is an  $m \times n$  rectangular diagonal  
9 matrix containing the  $m$  singular values of  $\mathbf{L}$  on its diagonal. These singular values are  
10 essentially eigenvalues that correspond to the  $m$  columns of  $\mathbf{U}$ , which are analogous to  
11 eigenvectors. Each of the  $n$  columns of  $\mathbf{V}$  is essentially a principal component of the scene,  
12 with each successive column capturing increasingly less signal variability. Therefore,  $\mathbf{L}$  can  
13 be recomposed as a linear combination of singular vectors scaled by the singular values  
14 (Murtagh and Heck, 1987).

15

## 16 **7 SVD retrieval method**

17 For each AVIRIS image subset, the radiance scene was first standardized by fitting a first  
18 order polynomial to each radiance spectrum and dividing it by the polynomial fit. Next, a  
19 mean radiance spectrum was calculated from the standardized data and the IMAP-DOAS  
20 retrieval was performed on the mean spectrum to generate the  $\text{CH}_4$  Jacobian for the lowest  
21 layer ( $\mathbf{K}_{\text{CH}_4}$ ) (Fig. 5). This standardization was performed to ensure that the computed  $\text{CH}_4$   
22 Jacobian is representative for all pixels; without it, calculations of Jacobians for each  
23 continuum level would be required. As an alternative to standardization, a SVD in log-space  
24 could be considered since optical depths are linear with respect to changing concentrations in  
25 the vicinity of the linearization point.

26 Using Eq. 7, the SVD was performed on each image subset using the standardized radiance  
27 ( $m \times n$  matrix  $\mathbf{L}$ , where  $m$  is the number of spectral bands and  $n$  is the number of radiance  
28 spectra). Due to computing limitations, the economy version of the SVD was calculated using  
29 MATLAB (Mathworks, Natick, Massachusetts). This resulted in  $\mathbf{U}_{econ}$  maintaining a  
30 dimension of  $m \times m$  (left singular vectors in  $m$  columns), but reduced matrix dimensions for  
31  $\mathbf{V}_{econ}$  and  $\mathbf{\Lambda}_{econ}$  ( $n \times m$  and  $m \times m$  respectively).

1 The first  $c$  columns of  $\mathbf{U}_{econ}$  ( $\mathbf{U}_{select}$ , an  $m \times c$  matrix where the optimal selection of  $c$  is  
2 described below) and the  $\text{CH}_4$  Jacobian ( $\mathbf{K}_{\text{CH}_4}$ , an  $m \times 1$  matrix) are concatenated to generate  
3 a matrix  $\mathbf{J}$  (dimensions of  $m \times c+1$ ). The basic principle is to reflect the general variability in  
4 spectral radiances by a linear combination of the first  $c$  eigenvectors and the  $\text{CH}_4$  Jacobian,  
5 which relates to deviations from background concentrations since the background radiance is  
6 already modeled using the linear combination of eigenvectors. A similar technique was used  
7 to retrieve terrestrial chlorophyll fluorescence using the FTS onboard GOSAT (Guanter et al.,  
8 2012). The linear combination of eigenvectors is an empirical way to compute the forward  
9 model radiance, which can include many detector and surface albedo features that the IMAP-  
10 DOAS approach cannot easily handle.

11 Using linear least squares, we can now find a vector  $\mathbf{W}$  that minimizes the cost function  
12 involving the measured radiance spectra  $\mathbf{y}$ :

$$13 \quad \|\mathbf{y} - \mathbf{J}\mathbf{W}\|^2. \quad (8)$$

14  $\mathbf{W}$  represents the contribution of each column of  $\mathbf{J}$  to the measured radiance. The modeled  
15 radiance  $\mathbf{F}$  can be calculated by multiplying  $\mathbf{J}$  by the weights  $\mathbf{W}$ :

$$16 \quad \mathbf{F} = \mathbf{J}\mathbf{W}. \quad (9)$$

17 resulting in a modeled radiance that can be compared to the measured radiance for each  
18 spectrum.

19 The previous equation can be rewritten as the sum of the background and  $\text{CH}_4$  component of  
20 the radiance as follows:

$$21 \quad \mathbf{F}(\mathbf{W}, \mathbf{J}) = \sum_{k=1}^c \mathbf{J}_k \cdot \mathbf{W}_k + \mathbf{J}_{c+1} \cdot \mathbf{W}_{c+1} \quad (10)$$

22 where the left term represents the background radiance modeled as a linear combination of the  
23 first  $c$  eigenvectors of  $\mathbf{J}$  ( $\mathbf{J}_k$ ) multiplied by the corresponding weights  $\mathbf{W}_k$ . The right term is the  
24  $\text{CH}_4$  component of the scene, the product of  $\mathbf{J}_{c+1}$  (the  $\text{CH}_4$  Jacobian,  $\mathbf{K}_{\text{CH}_4}$ ) and its  
25 corresponding weight  $\mathbf{W}_{c+1}$  (denoted as  $\text{RCH}_4$ ). In Equation (10), the fit coefficients are  $c$  and  
26  $\mathbf{W}$ .  $\text{RCH}_4$  indicates how much of the observed radiance for each spectrum can be associated  
27 with the  $\text{CH}_4$  Jacobian (i.e. changes in absorptions due to  $\text{CH}_4$ ) and can be used to both  
28 estimate  $\text{CH}_4$  concentrations as well as its uncertainties. Similar to the IMAP-DOAS  
29 approach,  $\text{RCH}_4$  for each pixel is multiplied by the VMR for the lowest layer of the reference  
30 atmosphere and results in an estimated  $\text{CH}_4$  concentration in ppm above/below the average.

1 The same 9 bands between 2,278 and 2,358 nm that made up the IMAP-DOAS retrieval  
2 window were initially used for the hybrid SVD approach. In an iterative process, additional  
3 bands between 2,218 and 2,457 nm were included to better account for high frequency  
4 variation present in the scenes. A portion of the scene was selected for a homogeneous  
5 landcover and the standard deviation of the RCH<sub>4</sub> results for different fitting windows was  
6 calculated. A 16 band fitting window (2,278 to 2,428 nm) was selected because it produced  
7 the lowest standard deviation in RCH<sub>4</sub> and thereby minimized noise in results.

8 Using these 16 bands, the hybrid SVD retrieval was performed iteratively by increasing the c  
9 columns of  $\mathbf{U}_{econ}$  used to generate  $\mathbf{U}_{select}$ . This resulted in 16 SVD retrievals, which were  
10 assessed by minimizing the standard deviation of the RCH<sub>4</sub> results for the portion of the scene  
11 selected to represent homogeneous landcover. This technique was used to determine the  
12 optimal number of columns of  $\mathbf{U}_{econ}$  to use with the SVD retrieval for the COP and Inglewood  
13 scenes.

14

## 15 **8 Results for IMAP-DOAS sensitivity study**

16 To investigate the expected IMAP-DOAS retrieval errors for the 9 band fitting window  
17 between 2,278 and 2,358 nm, the covariance  $\hat{\mathbf{S}}$  was calculated using the following equation

$$18 \quad \hat{\mathbf{S}} = (\mathbf{K}^T \mathbf{S}_\varepsilon^{-1} \mathbf{K} + \mathbf{S}_a^{-1})^{-1}. \quad (11)$$

19 where the diagonal of  $\hat{\mathbf{S}}$  corresponds to the covariance associated with CH<sub>4</sub>, H<sub>2</sub>O, and N<sub>2</sub>O at  
20 each of the 10 atmospheric layers.  $\mathbf{S}_\varepsilon$  is the error covariance matrix, a diagonal matrix  
21 representing expected errors resulting from shot-noise and dark current that is calculated  
22 using the SNR for the AVIRIS sensor.

23 The precision error of the IMAP-DOAS retrieval algorithm is calculated by multiplying the  
24 square root of the corresponding diagonal entry of  $\hat{\mathbf{S}}$  (the standard deviation of the CH<sub>4</sub> fit  
25 factor) by 1.78 ppm CH<sub>4</sub>, the 2008 mean VMR provided from the NOAA Mauna Loa station,  
26 United States (NOAA, 2013). These errors were calculated for a number of hypothetical  
27 sensors with varying spectral-~~resolutionsampling intervals (SSI)~~ and FWHM across a range  
28 of SNR (Fig. 6). As expected, the IMAP-DOAS error decreases as SNR increases and as the  
29 ~~spectral resolution sensor SSI~~ and FWHM become finer. The black line (10 nm ~~spectral~~  
30 ~~resolutionSSI~~ and FWHM) approximates the AVIRIS sensor and the SNR for bands used in  
31 the IMAP-DOAS retrieval was conservatively estimated between 100 and 200 using an

1 AVIRIS instrument model for low albedo surfaces (Rob Green, personal communication,  
2 2013). Using scene parameters similar to the COP flight (8.9 km altitude, 11.4° solar zenith),  
3 this corresponds to an error of between 0.31 to 0.61 ppm CH<sub>4</sub> over the lowest atmospheric  
4 layer (up to 1.04 km) shown in Fig. 2a. Given that about 10% of the total column is within the  
5 lowest layer, this error is considerable and roughly corresponds to an error of 30 to 60 ppb in  
6 column-averaged CH<sub>4</sub> over the total atmospheric column.

7

## 8 **9 Results for IMAP-DOAS**

### 9 **9.1 COP**

10 For the COP subset shown in Fig. 7a, measured radiance for the first band of the IMAP-  
11 DOAS retrieval window at 2,278 nm had a ~~maximum of 6.436 (sensor saturation)~~, minimum  
12 of 0.1158, maximum of 6.436 (sensor saturation), and mean of 2.0516  
13 microwatt·cm<sup>-2</sup>·sr<sup>-1</sup>·nm<sup>-1</sup> (uWcm<sup>-2</sup>sr<sup>-1</sup>nm<sup>-1</sup>). Sensor saturation occurs only for a small  
14 portion of the scene where the full well of the detector is saturated for multiple channels in the  
15 SWIR. Sonar return contours of subsurface CH<sub>4</sub> bubble plumes are overlain and correspond to  
16 known seep locations (Leifer et al., 2010). In Figure 7b, the CH<sub>4</sub> scaling factor is shown for  
17 the lowest atmospheric layer (height up to 1.04 km) and a CH<sub>4</sub> enhancement is clearly visible  
18 consistent with emission from seep locations and the 2.3 ms<sup>-1</sup> southwesterly wind measured at  
19 the nearby West Campus Station. The standard deviation of the residual (the difference  
20 between measured and modeled radiance) was also calculated to evaluate the ability of IMAP-  
21 DOAS to model radiance. This result is shown in Fig. 7c and has a similar visual appearance  
22 to Fig. 7a, indicating a strong albedo influence.

23 CH<sub>4</sub> concentrations were calculated by multiplying the retrieved CH<sub>4</sub> scaling factor by the  
24 VMR for the lowest atmospheric layer (1.78 ppm CH<sub>4</sub>). In Figure 7d, ppm CH<sub>4</sub> for the lowest  
25 layer is shown (subcolumn XCH<sub>4</sub>), excluding 740 bright pixels (greater than 5  
26 uWcm<sup>-2</sup>sr<sup>-1</sup>nm<sup>-1</sup> in the fitting window) associated with high standard deviation of the  
27 residuals. These results indicate enhancements in the lowest layer up to 2.5 times  
28 concentrations present in the reference atmosphere, equivalent to 4.46 ppm CH<sub>4</sub> averaged  
29 across the distance from the ocean surface to 1.04 km. However, there appears to be a positive  
30 bias in these results given concentrations for locations upwind of the plume appear higher

1 than the expected background concentration of 1.78 ppm. Therefore, the subcolumn  $X_{CH_4}$   
2 results appear overestimated. This observed bias will be further addressed in Sect. 11.

3 In Figure 7, location L1 and L2 correspond to the measured and modeled radiance plotted in  
4 Fig. 8. At location L1 (Fig. 8a), the measured radiance (black) is nearly horizontal for  
5 wavelengths between 2,278 and 2,328 nm, indicating sensor saturation due to high sun-glint.  
6 This causes considerable disagreement with the modeled radiance (red) as indicated by the  
7 residual radiance shown in the bottom plot; this pixel was excluded from the results shown in  
8 Fig. 7d. For Figure 8b (location L2), the radiance is considerably lower and there is better  
9 agreement between measured and modeled radiance, resulting in a retrieved concentration of  
10 2.18 ppm  $CH_4$  for this pixel. This radiance was detrended in Fig. 8c and the  $CH_4$  Jacobian for  
11 the lowest layer is overlain to indicate the location of  $CH_4$  absorptions at 2,298, 2,318, and  
12 2,348 nm.

## 13 **9.2 Inglewood**

14 The Inglewood subset (Fig. 9a) is highly heterogeneous, with a maximum measured radiance  
15 of 0.8033, minimum of 0.0192, and mean of 0.2800  $uWcm^{-2}sr^{-1}nm^{-1}$  at 2,278 nm. A road  
16 crosses the scene from north to south, separating the Inglewood Oil Field on the left from a  
17 residential neighborhood on the right. In this complex urban environment, the low order  
18 polynomial in the IMAP-DOAS algorithm is unable to account for some of the high  
19 frequency spectral variability that interferes with  $CH_4$  absorptions. Therefore, the  $CH_4$  scaling  
20 factor results for the lowest atmospheric layer are heavily influenced by the land surface type  
21 (Fig. 9b). For example, the road appears clearly visible and high  $CH_4$  scaling factors occur for  
22 individual structures within the neighborhood. Dark spectra also appear to have erroneously  
23 high  $CH_4$  scaling factors, including heavily vegetated areas in the northwest and southeast of  
24 the scene.

25 For the lowest atmospheric layer, subcolumn  $X_{CH_4}$  results are shown in Fig. 9d, excluding  
26 dark pixels less than 0.1  $uWcm^{-2}sr^{-1}nm^{-1}$  in the fitting window. While background  
27 concentrations are expected around 1.78 ppm  $CH_4$ , observed background concentrations  
28 appear biased upward, between 2 and 3 ppm. Despite the noisy results, a feature of elevated  
29  $CH_4$  is visible in the center of the image with maximum concentrations in excess of 5.5 ppm.  
30 This  $CH_4$  plume is consistent with a 2.2  $ms^{-1}$  southwesterly wind measured nearby at the time  
31 of image acquisition (weatherunderground.com, 2012). Using higher resolution Google Earth



1 imagery acquired one year after the AVIRIS flight, two hydrocarbon storage tanks were  
2 identified immediately upwind and are the probable emission source (Fig. 9e).

3

## 4 **10 Results for SVD**

### 5 **10.1 COP**

6 While the IMAP-DOAS technique permitted CH<sub>4</sub> retrievals for the more homogeneous  
7 marine location, high frequency variation present in the terrestrial example interferes with  
8 CH<sub>4</sub> absorptions and makes mapping more challenging. To permit retrievals for terrestrial  
9 locations, a hybrid approach using SVD and IMAP-DOAS was used to first account for high  
10 frequency variation present in the scene and determine what variance of the standardized  
11 radiance resulted from changes in CH<sub>4</sub>.

12 In Figure 10, all 16 columns of  $\mathbf{U}_{econ}$  are shown in addition to the CH<sub>4</sub> Jacobian ( $\mathbf{K}_{CH_4}$ ).  
13 Following the iterative method described in Sect. 7, 4 of the total 16 columns of  $\mathbf{U}_{econ}$  were  
14 used to generate  $\mathbf{U}_{select}$  and account for over 99.99% of the variance. Next,  $\mathbf{U}_{select}$  and  $\mathbf{K}_{CH_4}$   
15 were concatenated to generate the  $\mathbf{J}$  matrix, which is used for modelling radiance (see Eq. 9).

16 In Figure 11b the weights ( $R_{CH_4}$ ) associated with the column of  $\mathbf{J}$  that corresponds to the  
17 CH<sub>4</sub> Jacobian are shown (see Eq. 9). Within the scene, expected background values are 0 and  
18 the distinctive CH<sub>4</sub> plume is similar to the IMAP-DOAS results (Fig. 7b). In Figure 12d, ppm  
19 CH<sub>4</sub> relative to background is shown excluding 323 pixels (0.55% of total scene) associated  
20 with standard deviation of the residuals greater than 0.0075 (Fig. 11c; a unitless value given  
21 the SVD was performed on standardized radiance). CH<sub>4</sub> concentrations exceed 3 ppm above  
22 background within the plume, gradually decrease downwind, and approach expected  
23 background concentrations.

### 24 **10.2 Inglewood**

25 Using the iterative method described in Sect. 7, 9 columns of  $\mathbf{U}_{econ}$  were selected to generate  
26  $\mathbf{U}_{select}$  for the Inglewood scene. The  $R_{CH_4}$  results (Fig. 12b) more clearly distinguish the CH<sub>4</sub>  
27 plume compared to the IMAP-DOAS results (Fig. 9b), however, the SVD standard deviation  
28 of the residuals indicates higher errors for vegetated surfaces (Fig. 12c). Excluding pixels  
29 with greater than 0.0075 standard deviation of the residual, retrieved concentrations relative to

1 background are shown in Fig. 12d. Expected background concentrations are observed  
2 throughout much of the scene and CH<sub>4</sub> concentrations are highest for the western portion of  
3 the plume (in excess of 4 ppm above background).

4 In Figure 12, location L3 and L4 correspond to the measured and modeled radiance plotted in  
5 Fig. 13. At location L3 (Fig. 13a), there is considerable disagreement between the measured  
6 (black) and modeled radiance (red) as indicated by the residual. L3 is located in a vegetated  
7 region and because the standard deviation of the residual exceeds 0.0075, this pixel was  
8 excluded from the results shown in Fig. 12d. In contrast, there is good agreement for L4,  
9 which is made up of bare soil with an estimated concentration of 0.38 ppm CH<sub>4</sub> above  
10 background (Fig. 13b).

11 As described in Section 9.2, high standard deviation of the residuals were observed for dark  
12 pixels in IMAP-DOAS results for the Inglewood scene (Fig. 9c). In Fig. 9d, dark pixels less  
13 than 0.1 uWcm<sup>-2</sup>sr<sup>-1</sup>nm<sup>-1</sup> in the fitting window were excluded from IMAP-DOAS results,  
14 which included vegetated surfaces. For the hybrid approach using SVD and IMAP-DOAS,  
15 pixels with greater than 0.0075 standard deviation of the residual were excluded from the  
16 results shown in Fig. 12d, also corresponding to vegetation within the scene. The average  
17 radiance at 2,278 nm for those pixels with greater than 0.0075 standard deviation of the  
18 residual for the hybrid approach (Fig. 12d, black pixels) was only 0.1368 uWcm<sup>-2</sup>sr<sup>-1</sup>nm<sup>-1</sup>  
19 compared to the 0.3129 uWcm<sup>-2</sup>sr<sup>-1</sup>nm<sup>-1</sup> average for the remaining pixels in the scene. Dark  
20 pixels and their corresponding low SNR cause lower single measure precision and are thus  
21 problematic for both the IMAP-DOAS and the hybrid approach.

## 23 11 Discussion

### 24 11.1 Comparison of retrieval results

25 The IMAP-DOAS and hybrid SVD approach were capable of quantifying CH<sub>4</sub> concentrations  
26 from plumes over marine and terrestrial environments. For both techniques, agreement  
27 between measured and modeled radiance was poorest at albedo extremes, for example  
28 saturated pixels at COP and dark, vegetated surfaces at Inglewood. SVD results indicate near  
29 surface enhancements relative to background; absorptions resulting from background CH<sub>4</sub>  
30 concentrations in the scene are contained in  $\mathbf{U}_{select}$  and the retrieval used the CH<sub>4</sub> Jacobian

1 from the lowest layer of the atmospheric model. Similarly, the IMAP-DOAS retrieval also  
2 provides ppm CH<sub>4</sub> enhancements averaged over the lowest atmospheric layer (up to 1.04 km).  
3 For the IMAP-DOAS results from COP and Inglewood, an average background ppm CH<sub>4</sub>  
4 concentration was calculated for the portion of the scene selected to represent homogeneous  
5 landcover (see Sect. 7). To account for the observed positive bias in subcolumn XCH<sub>4</sub> (see  
6 Sect. 9), this average concentration was subtracted from subcolumn XCH<sub>4</sub>, resulting in ppm  
7 CH<sub>4</sub> relative to background. However, different portions of each scene were excluded from  
8 IMAP-DOAS and SVD results due to observed biases. For example, pixels were excluded  
9 from IMAP-DOAS results at Inglewood using an albedo threshold (Fig. 9d), while a standard  
10 deviation of the residual threshold was applied to SVD results (Fig. 12d). To permit  
11 comparison between results, only those pixels not excluded from either the IMAP-DOAS or  
12 SVD results are shown in Fig. 14 and Fig. 15.

13 These results were also ~~validated against~~compared with an independent technique, the  
14 Cluster-Tuned Matched Filter (CTMF) that was applied to both scenes (Fig. 14c and Fig.  
15 15c). ~~The CTMF uses a gas transmittance spectrum as a target to calculate CTMF scores for~~  
16 ~~each image pixel where scores greater than one indicate significant evidence of the gas~~  
17 ~~signature (Thorpe et al., 2013; Funk et al., 2001).~~ The CTMF is trained with a gas  
18 transmittance spectrum as a target to calculate CTMF scores for each image pixel where  
19 scores greater than one indicate significant evidence of the gas signature (Funk et al., 2001).  
20 Because the CTMF uses the inverse of the scene's covariance structure to remove large-scale  
21 noise to isolate the gas signal, it is best suited for detecting concentrated sources rather than  
22 background concentrations. A detailed description of the CTMF algorithm including results  
23 from both the COP and Inglewood image subsets is available in Thorpe et al., 2013. The  
24 CTMF does not provide an estimate of gas concentrations, rather it provides an image of gas  
25 anomalies that can be evaluated for consistency with probable emissions sources and local  
26 wind direction. In contrast, IMAP-DOAS and the hybrid SVD approach provide CH<sub>4</sub>  
27 concentrations as well as uncertainty estimates.

28 At COP, there is good spatial agreement between the observed plumes obtained with the  
29 IMAP-DOAS (Fig. 14a), hybrid SVD (Fig. 14b), and CTMF (Fig. 14c) approaches (Thorpe et  
30 al., 2013). IMAP-DOAS CH<sub>4</sub> concentrations are generally higher (mean 0.12, standard  
31 deviation 0.43 ppm relative to background) than the SVD results (mean -0.01, standard  
32 deviation 0.63 ppm relative to background). The location of an identical transect is shown for

1 the IMAP-DOAS (Fig. 14a, green line), SVD (Fig. 14b, cyan), and CTMF results (Fig. 14c,  
2 red). At each point along the transect, an average value was calculated for 21 pixels centered  
3 on the transect in the horizontal direction. The average values along the transect are plotted in  
4 Fig. 14d and indicate concentrations for IMAP-DOAS (green) are generally higher than for  
5 the SVD approach (cyan) with both transects sharing the cyan figure axes. Where the transect  
6 intersects the plume, there is good agreement in the pronounced peak in values from the three  
7 techniques, including CTMF results (red) that were offset for clarity and correspond to the red  
8 figure axes. While the CTMF technique appears better suited for detecting diffuse portions of  
9 the plume (Fig. 14c), it does not provide CH<sub>4</sub> concentrations.

10 Using the hybrid SVD approach, the maximum observed concentration within the scene was  
11 2.85 ppm CH<sub>4</sub> above background, located at a region of subsurface CH<sub>4</sub> bubble plumes as  
12 shown by the sonar return contours (Fig. 11a). Averaged over the lowest atmospheric layer (a  
13 distance of 1.04 km), this maximum concentration will increase when scaled for a smaller  
14 atmospheric column. For example, concentrations increase to 590 ppm CH<sub>4</sub> above  
15 background if all enhancements are within a 5 m atmospheric column. Near surface  
16 concentrations are likely much higher; Leifer et al. (2006) measured up to  $2 \times 10^4$  ppm CH<sub>4</sub> at  
17 5 m height using a flame ion detector.

18 For Inglewood, the CH<sub>4</sub> plume is clearly visible in IMAP-DOAS (Fig. 15a), hybrid SVD (Fig.  
19 15b), and CTMF (Fig. 15c) results (Thorpe et al., 2013). CH<sub>4</sub> concentrations for IMAP-  
20 DOAS are generally higher (mean 0.13 and standard deviation 1.03 ppm relative to  
21 background) than the hybrid SVD results (mean -0.04 and standard deviation 1.60 ppm  
22 relative to background). Overall there is good spatial agreement for the observed CH<sub>4</sub> plume  
23 obtained using these three distinct techniques.

24 Similar to the COP comparison, the location of an identical transect is shown for the IMAP-  
25 DOAS, SVD, and CTMF results. An average was calculated at each point along the transect  
26 (for 9 pixels centered on the transect in the vertical direction) and plotted in Fig. 15d,  
27 indicating two locations with enhanced CH<sub>4</sub> between the 70<sup>th</sup> and 100<sup>th</sup> pixels. For this portion  
28 of the transect, there is considerable disagreement between the IMAP-DOAS (Fig. 15d, green  
29 line) and SVD concentrations (blue). This discrepancy can be partly attributed to the influence  
30 of the choice of the number of columns of  $U_{econ}$  used to generate  $U_{select}$ . (see Section 7). For the  
31 transect shown in Fig. 15d, 9 columns of  $U_{econ}$  were used, resulting in a mean concentration  
32 along the transect of 0.4141 ppm CH<sub>4</sub> relative to background. Selecting 10 columns of  $U_{econ}$

1 decreased the mean concentration along the transect to 0.3664 ppm relative to background  
2 with a standard deviation of the difference between transects obtained using 9 and 10  
3 columns equal to 0.2959 ppm. In contrast, using 8 columns of  $U_{econ}$  results in a mean  
4 concentration of 0.4144 ppm relative to background and the standard deviation of the  
5 difference between transects obtained using 9 and 8 columns is reduced to 0.1508 ppm  
6 relative to background. This indicates that retrieved  $CH_4$  concentrations obtained using the  
7 SVD approach is influenced by the choice of  $U_{select}$  because higher-order singular vectors can  
8 start correlating with the computed  $CH_4$  Jacobian.

9 For the SVD approach at Inglewood using 9 columns of  $U_{econ}$ , the maximum within the  $CH_4$   
10 plume was 8.45 ppm above background with concentrations decreasing downwind of the  
11 hydrocarbon storage tanks (Fig. 12d). Such enhancements are feasible given tanks represent  
12 large emission sources; natural gas storage tanks can emit between 4.3 and  $42.0 \times 10^{-4}$  Gg  
13  $CH_4$  per  $(10^6)$   $m^3$  gas withdrawals per year (IPCC, 2000) and tank venting represented  
14 approximately 14.4% (212 Gg  $CH_4$ ) of the total U.S.  $CH_4$  emissions from petroleum systems  
15 in 2009 (EPA, 2011).

## 16 **11.2 Potential for AVIRISng and future sensors**

17 While  $CH_4$  retrievals are promising using AVIRIS, the next generation sensor (AVIRISng)  
18 will have a 5 nm spectral resolution~~SSI~~ and FWHM that should significantly improve  $CH_4$   
19 sensitivity. An IMAP-DOAS retrieval error between 0.31 to 0.61 ppm  $CH_4$  over the lowest  
20 atmospheric layer (height up to 1.04 km) is expected for an AVIRIS scene acquired at 8.9 km  
21 altitude, 11.4° solar zenith, and with a SNR conservatively set between 100 and 200 (Fig. 6,  
22 black line). This corresponds to about a 32 to 63 ppm retrieval error for a 10 m thick plume or  
23 322 to 634 ppm for a 1 m thick plume. For a similar AVIRISng scene, the IMAP-DOAS  
24 retrieval error would be reduced to between 0.18 to 0.35 ppm over the lowest atmospheric  
25 layer for the same range of SNR (Fig. 6, red line), however retrieval errors remain significant.  
26 In addition, SNR for AVIRISng should be considerably improved, further reducing retrieval  
27 errors.

28 To further assess this increased sensitivity,  $CH_4$  Jacobians were calculated for AVIRISng and  
29 AVIRIS for a 5%  $CH_4$  enhancement over the lowest atmospheric layer. In Figure 16a, the  
30 AVIRIS  $CH_4$  Jacobian (black line) has a  $-4.7 \times 10^{-4} \Delta u W cm^{-2} sr^{-1} nm^{-1} / \Delta VMR$  amplitude  
31 between a peak at 2,310 nm and the  $CH_4$  absorption at 2,320 nm. For AVIRISng (red line)

1 this amplitude is  $-9.8 \times 10^{-4} \Delta u W \text{cm}^{-2} \text{sr}^{-1} \text{nm}^{-1} / \Delta \text{VMR}$ , roughly representing a doubling of  
2  $\text{CH}_4$  sensitivity compared with AVIRIS. However, additional improvements should result  
3 from a greater number of detector pixels and the improved SNR of AVIRISng. Sensors with a  
4 finer spectral resolutionSSI and FWHM offer the potential for even greater sensitivity, as  
5 shown by the grey line in Fig. 16a for a spectral resolutionSSI and FWHM of 1 nm and  
6 reduced IMAP-DOAS retrieval errors indicated by the grey dashed line in Fig. 6.

7

## 8 **12 Conclusions**

9 In this study, two retrieval techniques were used to measure  $\text{CH}_4$  enhancements for  
10 concentrated plumes over marine and terrestrial locations in AVIRIS data. The IMAP-DOAS  
11 algorithm performed well for the homogenous ocean scene containing the COP seeps and  
12 retrieval errors are estimated between 0.31 to 0.61 ppm  $\text{CH}_4$  over the lowest atmospheric  
13 layer (height up to 1.04 km). For the Inglewood subset, IMAP-DOAS results became heavily  
14 influenced by the underlying landcover, while the hybrid SVD approach was particularly  
15 effective given that it could better account for spectrally variable surface reflectance. Using  
16 the hybrid SVD approach for the COP and Inglewood plumes, maximum near surface  
17 concentrations were 2.85 and 8.45 ppm  $\text{CH}_4$  above background respectively. An additional  
18 benefit of the hybrid SVD approach is that it requires less than half the computational time of  
19 the IMAP-DOAS retrieval.

20 | Given a 5 nm spectral resolutionSSI and FWHM,  $\text{CH}_4$  sensitivity should be more than  
21 doubled for AVIRISng. This might permit  $\text{CH}_4$  retrievals for weaker absorption features  
22 centered at 1,650 nm, as well as  $\text{CO}_2$  retrievals for absorptions at 1,572, 1,602, and 2,058 nm.  
23 However, both the AVIRIS and AVIRISng sensors were not designed for detecting gas  
24 plumes and sensitivity could be dramatically improved using a spectrometer designed  
25 exclusively for mapping gas plumes. For example, an imaging spectrometer with 0.05 nm  
26 | spectral resolutionSSI and 0.15 nm FWHM would have an IMAP-DOAS error around 18  
27 times smaller than AVIRIS.

28 While non-imaging spectrometers such as MAMAP have increased  $\text{CH}_4$  sensitivity compared  
29 | to AVIRIS and AVIRISng, they are currently limited to flying transects across local gas  
30 plumes due to a small field of view. In contrast, airborne imaging spectrometers combine  
31 large image footprints and fine spatial resolution necessary to map local  $\text{CH}_4$  plumes in their  
32 | entirety however have considerably higher expected errors for retrieved  $\text{CH}_4$  concentrations. -

1 In this study, the observed COP plume extended more than 1 km, however, the Inglewood  
2 plume was much smaller, extending only 0.1 km downwind. Such plumes with a small spatial  
3 extent are of increasing concern, including industrial point source emissions, leaking gas  
4 pipelines (Murdock et al., 2008), and fugitive CH<sub>4</sub> ~~from the oil and gas industry~~emissions  
5 (Howarth et al., 2011). Imaging spectrometers permit direct attribution of emissions to  
6 individual point sources which is particularly useful given the large uncertainties associated  
7 with anthropogenic emissions, including fugitive CH<sub>4</sub> emissions from the oil and gas industry  
8 (Petron et al., 2012; EPA, 2013; Allen et al., 2013), and the projected increase in these types  
9 of emissions (EPA, 2006). Therefore, AVIRIS-like sensors offer the potential to better  
10 constrain emissions on local and regional scales (NRC, 2010), improve greenhouse gas  
11 budgets and partitioning between natural and anthropogenic sources, as well as complement  
12 data provided at coarser spatial resolutions.

13

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22

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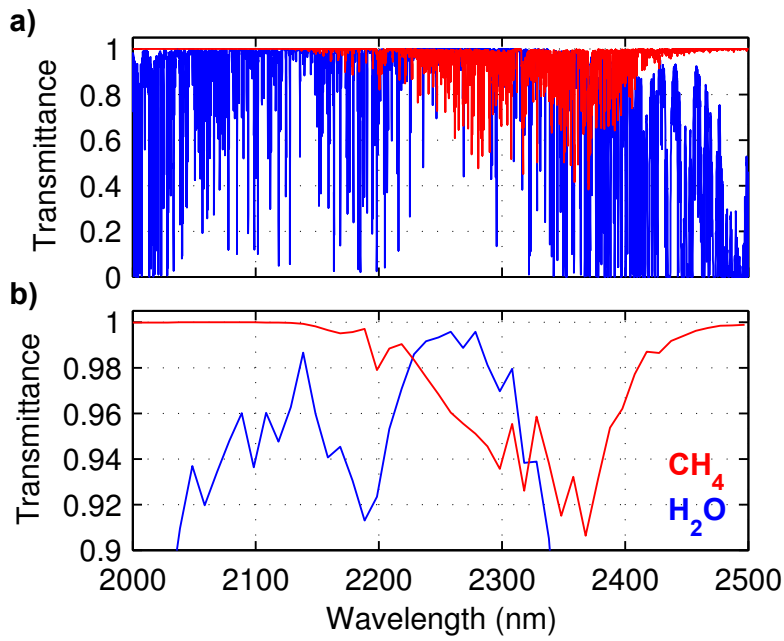
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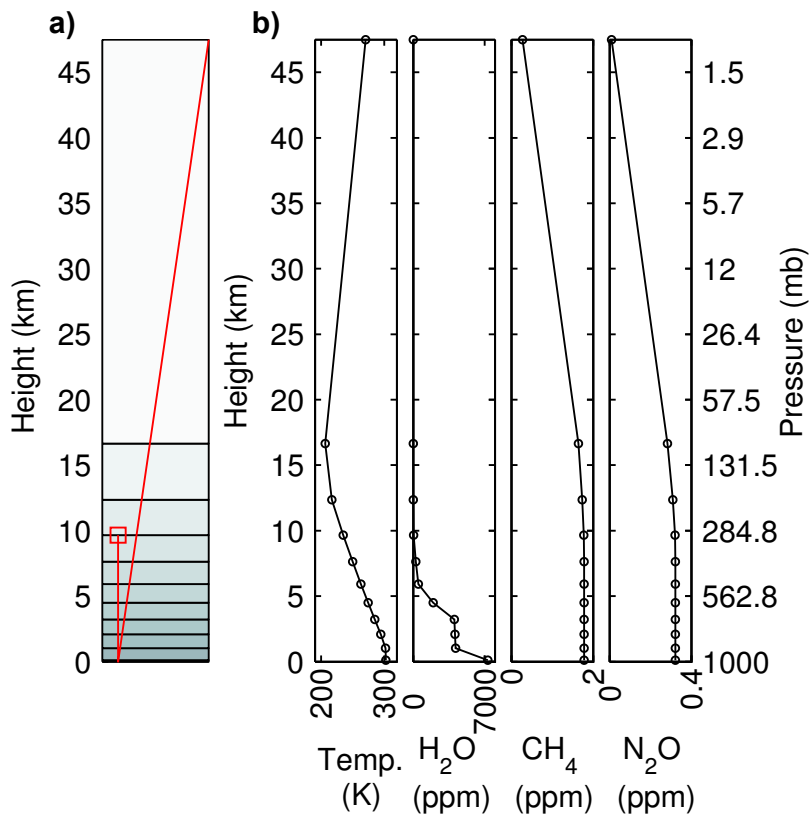
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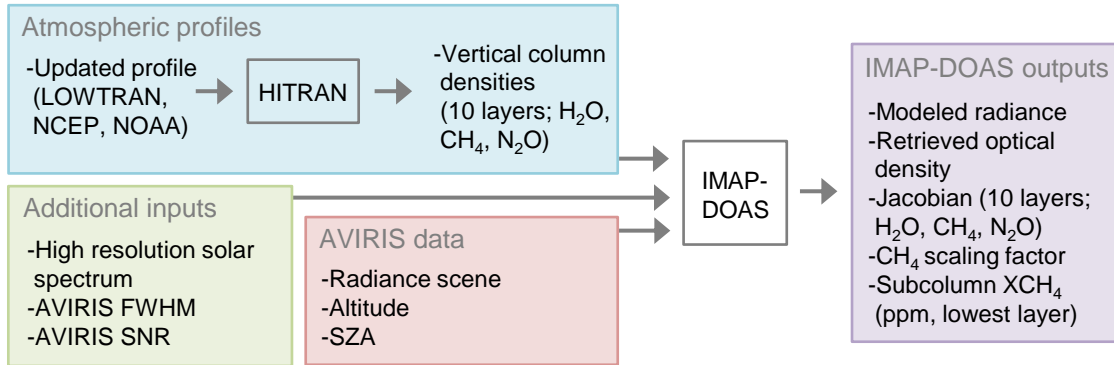
1  
 2 Figure 1. a. High resolution CH<sub>4</sub> and H<sub>2</sub>O transmittance. b. Transmittance convolved to the 10  
 3 nm AVIRIS spectral resolution~~spectral sampling interval~~.



5  
 6 Figure 2. a. 10 atmospheric layers were used for retrievals (layer 1 at the top). For the COP  
 7 scene, the aircraft was placed between layer 3 and 4 (red square). The slant and vertical light

1 paths (red lines) were used to scale optical densities appropriately. b. Profiles of temperature  
2 and VMR of H<sub>2</sub>O, CH<sub>4</sub>, and N<sub>2</sub>O for the boundaries of each layer (black circles).

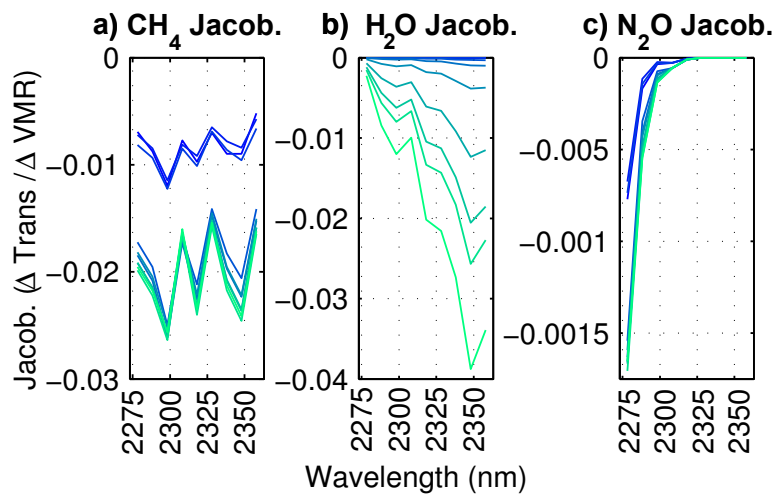
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4

5 Figure 3. Processing steps for IMAP-DOAS CH<sub>4</sub> retrieval.

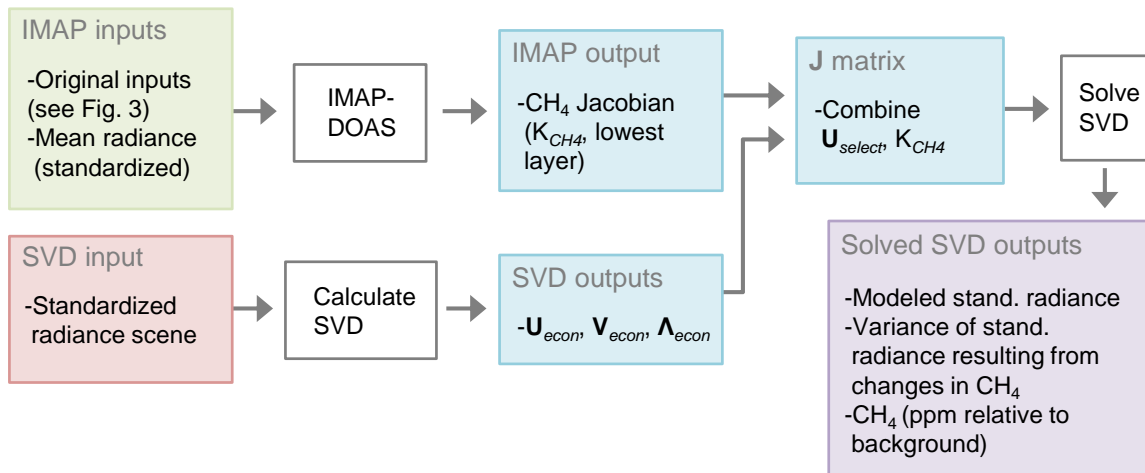
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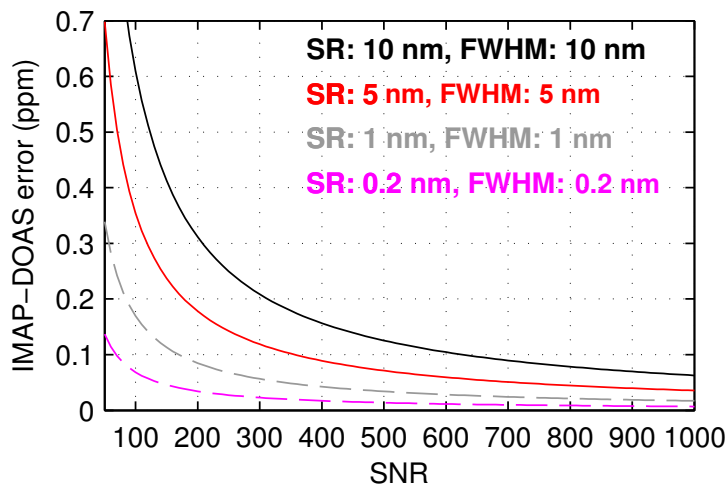
7

8 Figure 4. a. CH<sub>4</sub> Jacobian for each of the 10 atmospheric layers with colors transitioning from  
9 dark blue at the highest layer (layer 1) to light green for the lowest layer (layer 10). The CH<sub>4</sub>  
10 Jacobians with smaller magnitudes (dark blue) are for layers above the flight altitude. The  
11 same color scheme is used for the H<sub>2</sub>O Jacobians (b) and N<sub>2</sub>O Jacobians (c).

12

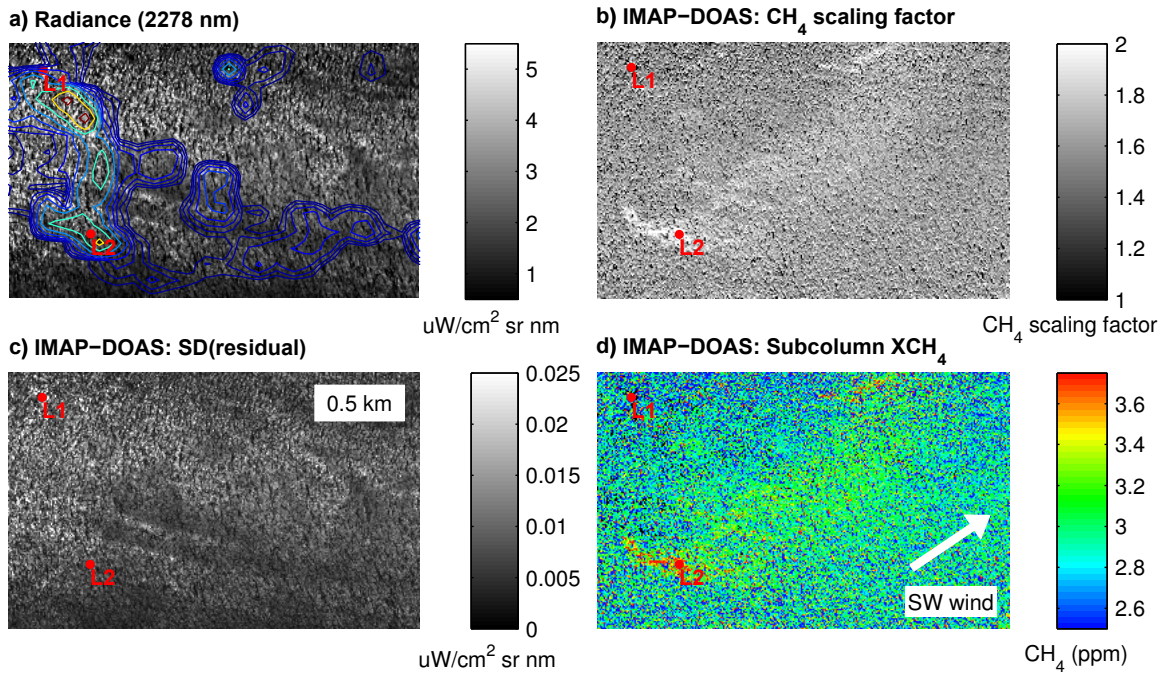


1  
2 Figure 5. Processing steps for the SVD retrieval method. The IMAP-DOAS retrieval is  
3 performed on a mean radiance for the image subset to generate the CH<sub>4</sub> Jacobian for the  
4 lowest layer. The SVD is used to calculate  $U_{econ}$ ,  $V_{econ}$ , and  $\Lambda_{econ}$  while  $U_{select}$  is combined  
5 with the CH<sub>4</sub> Jacobian to generate the  $J$  matrix.  $J$  is used to determine the portion of each  
6 radiance spectra associated with the CH<sub>4</sub> Jacobian (i.e. absorptions due to CH<sub>4</sub>) and can be  
7 used to estimate CH<sub>4</sub> concentrations.



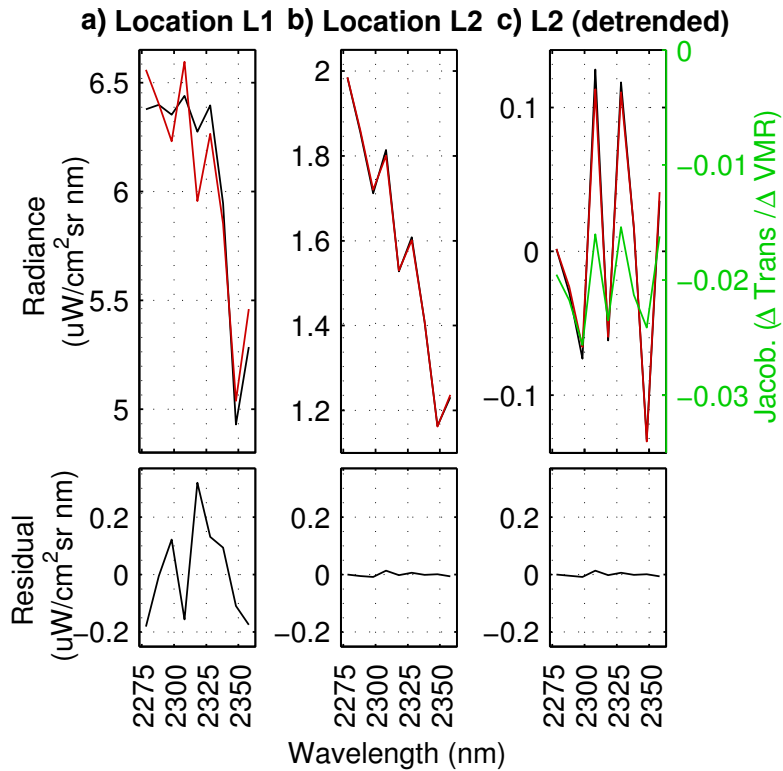
9  
10 Figure 6. Estimated IMAP-DOAS retrieval errors (ppm CH<sub>4</sub>) for four hypothetical sensors,  
11 each with the spectral resolution (SR)~~sampling interval (SSI)~~ equal to the FWHM. Errors are  
12 relative to lowest atmospheric layer (height up to 1.04 km) and decline with increased signal  
13 to noise ratio (SNR).



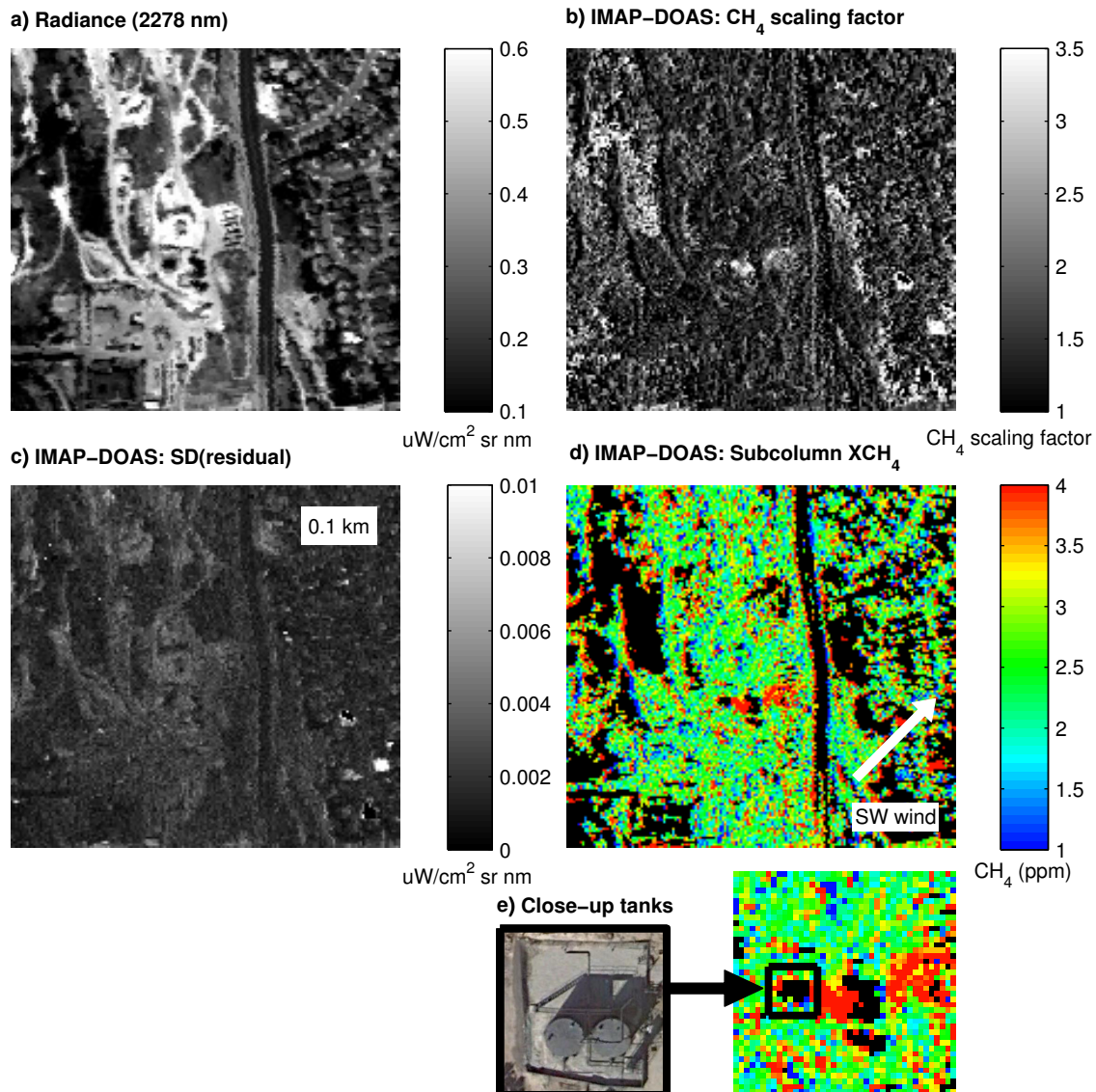


1  
 2 Figure 7. a. Measured radiance at 2,278 nm showing strong variability in brightness. Sonar  
 3 return contours (Leifer et al., 2010) are overlain and correspond to known seep locations. b.  
 4 For the same image subset, CH<sub>4</sub> scaling factor for the lowest atmospheric layer (layer 10)  
 5 indicates a CH<sub>4</sub> plume consistent with the local wind direction. c. The standard deviation of  
 6 the residuals (measured minus modeled radiance) depends strongly on brightness (a). d.  
 7 Subcolumn XCH<sub>4</sub> (ppm CH<sub>4</sub> for the lowest layer) excluding bright pixels (greater than 5  
 8  $\text{uWcm}^{-2}\text{sr}^{-1}\text{nm}^{-1}$  in the fitting window) associated with high standard deviation of the  
 9 residuals. For two spectra (indicated by location L1 and L2), measured and modeled radiance  
 10 are provided in Fig. 8.

11



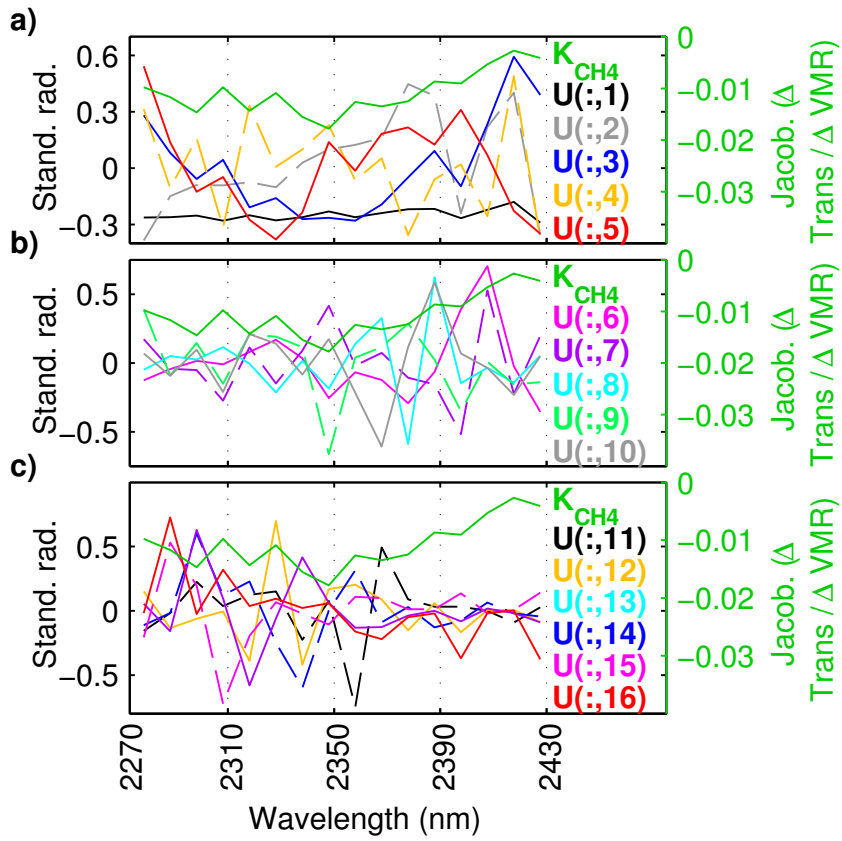
1  
 2 Figure 8. a. For location L1 (see Fig. 7), the measured radiance (black) indicates sensor  
 3 saturation due to high sun-glint between 2,278 and 2,328 nm. This causes considerable  
 4 disagreement with the modeled radiance (red), as indicated by the residual radiance shown in  
 5 the bottom plot. b. There is better agreement for location L2. c. The radiance shown in b was  
 6 detrended and the  $\text{CH}_4$  Jacobian for the lowest layer overlain (green) to indicate the location  
 7 of  $\text{CH}_4$  absorptions at 2,298, 2,318, and 2,348 nm.  
 8



1

2 Figure 9. a. Radiance at 2,278 nm showing a portion of the Inglewood Oil Field. b. For the  
 3 same image subset,  $\text{CH}_4$  scaling factor for the lowest atmospheric layer (layer 10) appears  
 4 heavily influenced by land surface type. c. Standard deviation of the residuals also appears  
 5 influenced by land cover. d. Subcolumn  $\text{XCH}_4$  (ppm  $\text{CH}_4$  for the lowest layer) excluding dark  
 6 pixels (less than  $0.1 \text{ uWcm}^{-2}\text{sr}^{-1}\text{nm}^{-1}$  in the fitting window). e. Close-up of hydrocarbon  
 7 storage tanks upwind of observed plume (Google Earth, 2013).

8



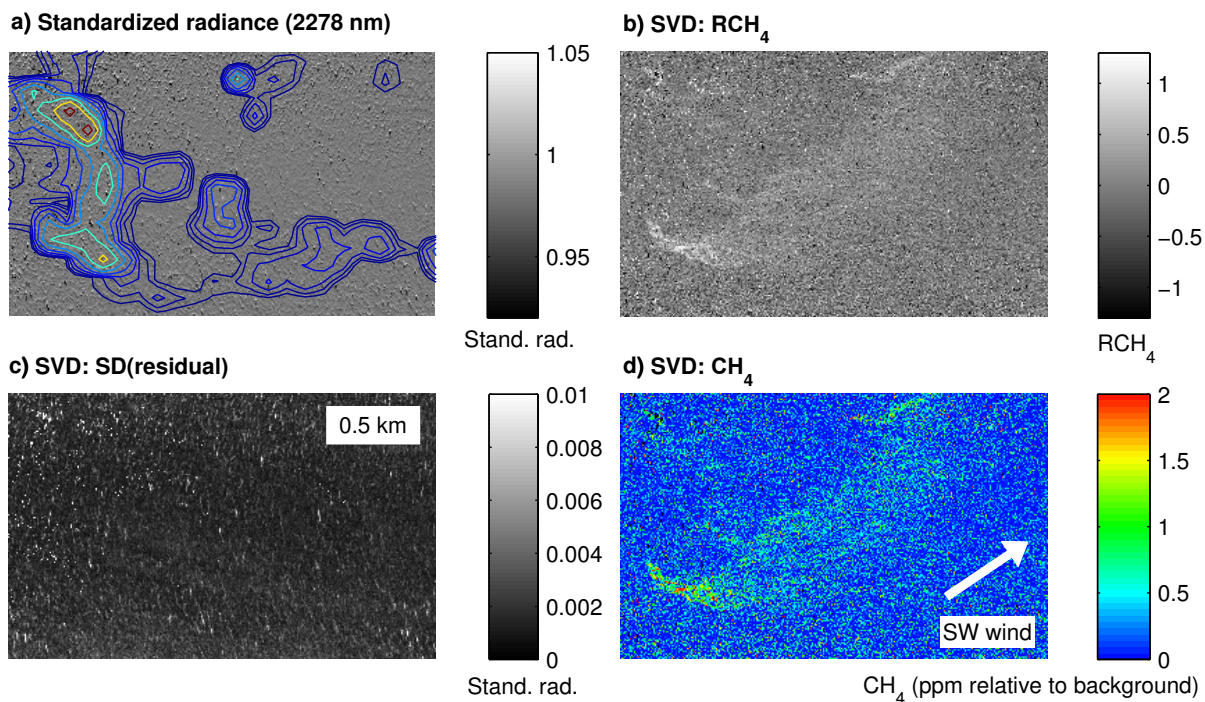
1

2 Figure 10. a. Singular vectors contained in  $U_{econ}$  for COP scene with  $CH_4$  Jacobian ( $K_{CH_4}$ )  
 3 plotted for reference.

4

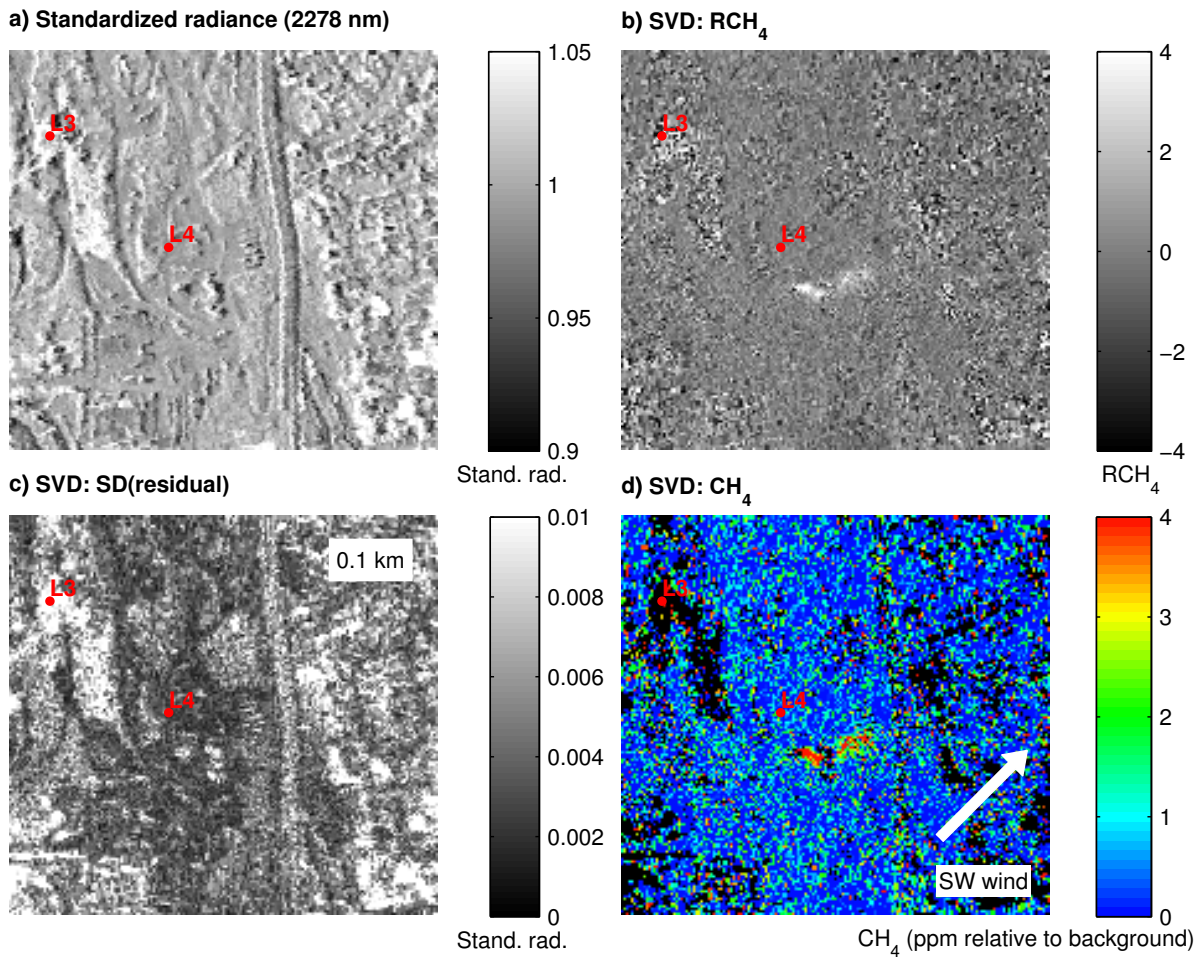
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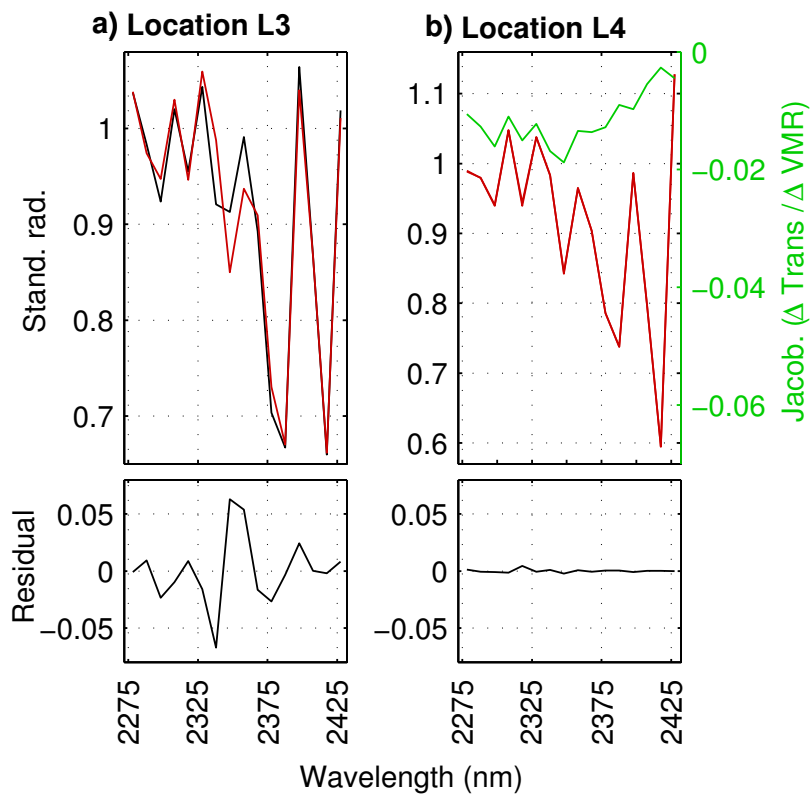
1  
 2 Figure 11. a. Standardized radiance used for calculating SVD at COP (showing only 2,278  
 3 nm). b. For the same image subset, RCH<sub>4</sub> results clearly indicate CH<sub>4</sub> plume. c. The standard  
 4 deviation of the residuals (measured minus modeled radiance). d. ppm CH<sub>4</sub> relative to  
 5 background excluding pixels with greater than 0.0075 standard deviation of the residual (a  
 6 unitless value given the SVD was performed on standardized radiance).

7

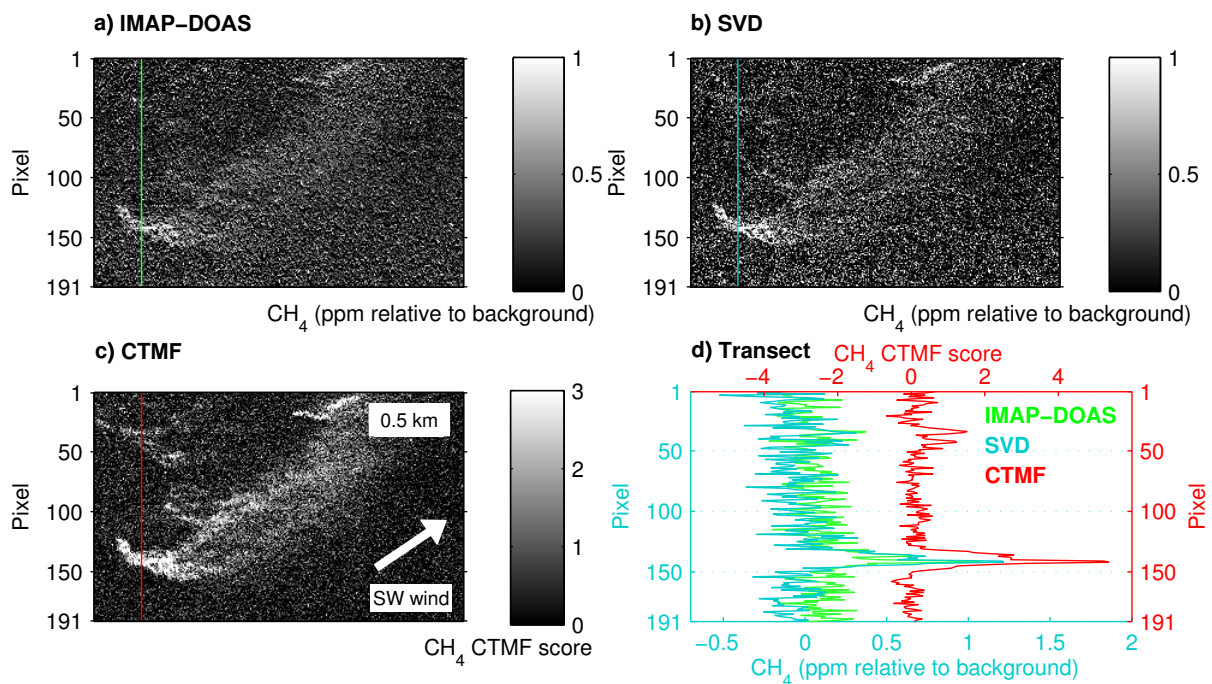


1  
 2 Figure 12. a. Standardized radiance used for calculating SVD for Inglewood subset (showing  
 3 only 2,278 nm). b. For the same image subset, RCH<sub>4</sub> results indicate CH<sub>4</sub> plume at the center  
 4 of the scene. c. The standard deviation of the residuals (measured minus modeled radiance). d.  
 5 ppm CH<sub>4</sub> relative to background excluding pixels with greater than 0.0075 standard deviation  
 6 of the residual (a unitless value given the SVD was performed on standardized radiance). For  
 7 two spectra (indicated by location L3 and L4), measured and modeled radiance are provided  
 8 in Fig. 13.

9  
 10



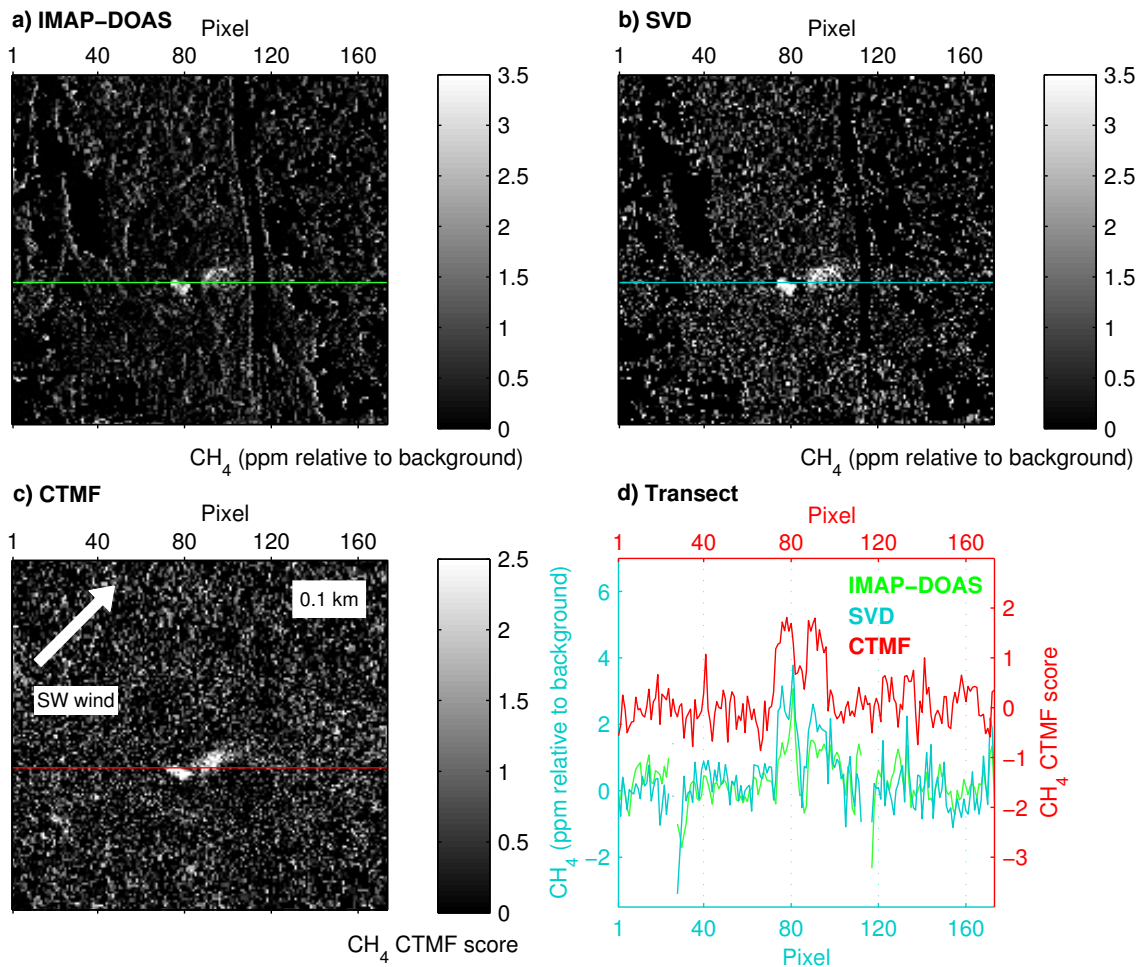
1  
 2 Figure 13. a. The modeled (red) and measured standardized radiance (black) for location L3,  
 3 which corresponds to a dark spectrum with an average radiance of  $0.0376 \text{ uWcm}^{-2}\text{sr}^{-1}\text{nm}^{-1}$ .  
 4 L3 is located in a distinct region with high values for the standard deviation of the residuals  
 5 (see Fig. 12c) and was excluded from the results shown in Fig. 12d. b. For location L4, there  
 6 is better agreement between modeled and measured radiance (average  $0.5187$   
 7  $\text{uWcm}^{-2}\text{sr}^{-1}\text{nm}^{-1}$ ). The CH<sub>4</sub> Jacobian for the lowest layer is overlain (green) to indicate the  
 8 location of CH<sub>4</sub> absorptions.  
 9



1  
 2 Figure 14. For the same COP subset, there is good agreement between results obtained using  
 3 three techniques. a. IMAP-DOAS. b. SVD. c. Cluster-Tuned Matched Filter (CTMF). The  
 4 location of a vertical transect is shown for the IMAP-DOAS (green line), SVD (cyan), and  
 5 CTMF results (red). d. Values along the transect are shown for IMAP-DOAS (green), SVD  
 6 (cyan), and CTMF (red). At each point along the transect, an average value was calculated for  
 7 21 pixels centered on the transect in the horizontal direction. IMAP-DOAS and SVD transects  
 8 share the cyan figure axes, while the CTMF transect was offset for clarity and corresponds to  
 9 the red figure axes.

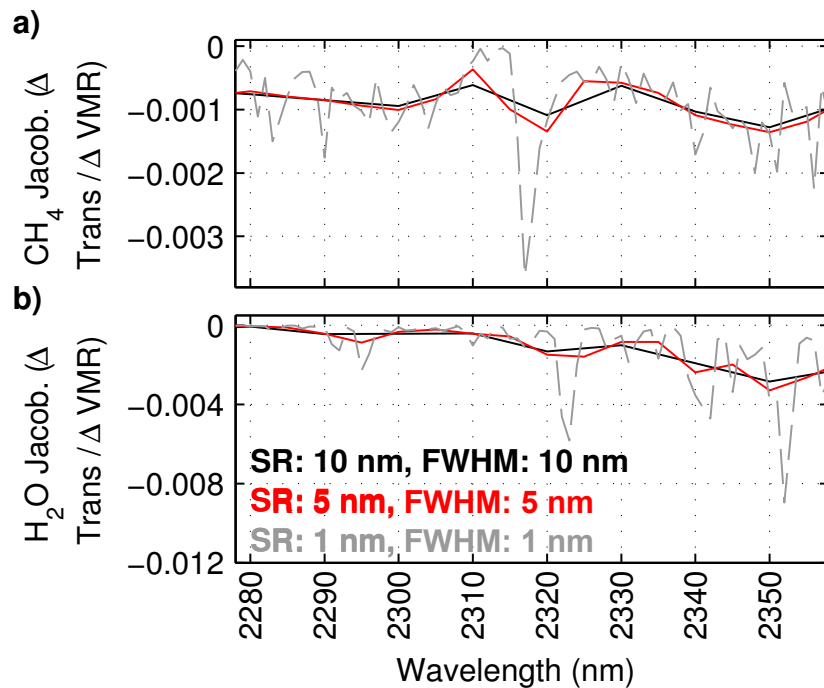
10





1  
 2 Figure 15. For the same Inglewood subset, there is good agreement between results obtained  
 3 using three techniques. a. IMAP-DOAS. b. SVD. c. Cluster-Tuned Matched Filter (CTMF).  
 4 The location of a horizontal transect is shown for the IMAP-DOAS (green line), SVD (cyan),  
 5 and CTMF results (red). d. Values along the transect are shown for IMAP-DOAS (green),  
 6 SVD (cyan), and CTMF (red) approach. At each point along the transect, an average value  
 7 was calculated for 9 pixels centered on the transect in the vertical direction. IMAP-DOAS and  
 8 SVD transects share the cyan figure axes, while the CTMF transect was offset for clarity and  
 9 corresponds to the red figure axes.

10



1  
 2 Figure 16. a. For the lowest layer of the atmospheric model (height up to 1.04 km), the CH<sub>4</sub>  
 3 Jacobian calculated for AVIRISng (red) indicates improved sensitivity compared to the CH<sub>4</sub>  
 4 Jacobian for AVIRIS (black). Even greater sensitivity can be achieved using a finer spectral  
 5 resolution (SR) and FWHM (dashed grey). b. H<sub>2</sub>O Jacobians calculated for the same three  
 6 sensors.