Atmos. Meas. Tech. Discuss., 7, 2459–2490, 2014 www.atmos-meas-tech-discuss.net/7/2459/2014/ doi:10.5194/amtd-7-2459-2014 © Author(s) 2014. CC Attribution 3.0 License.



This discussion paper is/has been under review for the journal Atmospheric Measurement Techniques (AMT). Please refer to the corresponding final paper in AMT if available.

Validation of GOMOS ozone precision estimates in the stratosphere

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Received: 19 February 2014 - Accepted: 28 February 2014 - Published: 12 March 2014

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Published by Copernicus Publications on behalf of the European Geosciences Union.





Abstract

Accurate information about uncertainties is required in nearly all data analyses (intercomparisons, data assimilation, combined use, etc.). Validation of precision estimates (viz., the random component of estimated uncertainty) is important for remote sens-

- ⁵ ing measurements, which provide the information about atmospheric parameters via solving an inverse problem. For the Global Ozone Monitoring by Occultation of Stars (GOMOS) instrument, it is of a real challenge, due to dependence of signal-to-noise ratio (and thus precision estimates) on stellar properties, small number of self-collocated measurements, and uncertainty estimates growing with time due to instrument age-
- ¹⁰ ing. Estimated uncertainties of ozone retrievals are small in the stratosphere for bright stars, which results in additional complexity of detecting them on the background of natural ozone variability.

In this paper, we discuss different methods for geophysical validation of precision estimates and their applicability to GOMOS data. We propose a simple method for val-

idation of GOMOS precision estimates for ozone in the stratosphere. This method is based on comparisons of difference in sample variance with the difference in uncertainty estimates for measurements from different stars selected in a region of small natural variability.

For GOMOS, the difference in sample variances for different stars at altitudes 25– 45 km is well explained by the difference in squared precisions, if stars are not dim. Since it is observed for several stars, and since normalized χ^2 is close to 1 in these occultations in the stratosphere, we can conclude that GOMOS precision estimates are realistic in occultations of sufficiently bright stars. For dim stars, errors are overestimated due to improper accounting for the dark charge correction uncertainty in the

²⁵ error budget. The proposed method can also be applied to stratospheric ozone data from other instruments, including multi-instrument analyses.





1 Introduction

Nearly all data analyses (for example, data comparisons, data assimilation, combined use etc.) require information about the data uncertainty. Validation of precision estimates (viz., the random component of the estimated uncertainty) is needed when the uncertainty of measurements cannot be fully characterized or is based on assumptions. This is especially important for remote-sensing measurements, which retrieve the information about atmospheric parameters via solving inverse problems. Precision of the remote sensing measurements is usually estimated via propagation of instrumental noise through the inversion algorithm. These precision estimates can be imperfect due
 to incomplete forward models or approximations used in retrievals.

This paper is dedicated to validation of precision estimates for ozone profiles in the stratosphere by the Global Ozone Monitoring by Occultation of Stars (GOMOS) instrument. GOMOS is a stellar occultation instrument on board the Envisat satellite (Bertaux et al., 2010; Kyrölä et al., 2010), which operated in 2002–2012. Vertical pro-

- files of ozone, NO₂, NO₃ and aerosol extinction are retrieved from ultraviolet and visible (UV-VIS) stellar spectra measured as a star sets behind the Earth limb, with a sampling frequency of 2 Hz. The spectra observed through the atmosphere are normalized by the reference stellar spectrum observed above the atmosphere thus giving selfcalibrated transmission spectra (transmittances), the basis for retrievals of trace gases
- from GOMOS measurements (Bertaux et al., 2010; Kyrölä et al., 2010). The GOMOS inversion of the chemical composition is performed in two steps (Kyrölä et al., 2010). First, atmospheric transmission data from every tangent height are inverted to horizon-tal column densities (along the line of sight) for gases and optical thickness for aerosols (spectral inversion). Then, for every constituent, the collection of the horizontal column
- densities at successive tangent heights is inverted to vertical density profiles (vertical inversion). Although the measurements are performed during night and day, only night-time measurements have been used in scientific studies so far, as the scattered solar light degrades significantly the quality and altitude coverage of daytime occultations. In





this paper, only night-time measurements (with the solar zenith angle larger than 107° at tangent points) are discussed. GOMOS has performed about 150–200 night-time occultations per day with global coverage. Typical examples of GOMOS data coverage and distribution over the globe are shown e.g. in (Bertaux et al., 2010; Kyrölä et al., 2010; Sofieva et al., 2013; Tamminen et al., 2010). The vertical resolution (including

the smoothing properties of the inversion) of GOMOS ozone profiles is 2 km below 30 km and 3 km above 40 km; it is the same for all occultations.

In this paper, we discuss challenges in validation of GOMOS precision estimates and propose a simple method that allows validation of ozone precision estimates in the

- stratosphere. The paper is organized as follows. Section 2 outlines the principles of GOMOS precision derivation. In Sect. 3, we overview the existing methods for validation of precision estimates and discuss their applicability to GOMOS measurements. In Sect. 4, we describe the proposed differential method for validation of precision estimate, present its application to GOMOS ozone profiles in the stratosphere and discuss its extension for other instruments. The extension estimate strates are set of the proposed differential method for validation of precision estimate.
- its extension for other instruments. The summary concludes the paper.

2 Outlines of GOMOS precision derivation. Quality of retrievals

For GOMOS, the random component is dominating in the total error budget. For nighttime occultations, instrumental noise consists of three components: photon noise, the dark charge of the CCD, and readout noise (Bertaux et al., 2010; Kyrölä et al., 2010).

- Statistics of photo-counts obeys a Poisson distribution, which can be approximated to good accuracy by a normal distribution due to large values of photo-counts. In the GO-MOS processing, the mean dark current is estimated and subtracted from the recorded signal as an offset signal, but its variance is taken into account in the noise term. The dark charge increases with time due to instrument ageing (Tamminen et al., 2010). Its relative contribution to process for dimensional data and subtracted and subtracted form the recorded signal as an offset signal, but its variance is taken into account in the noise term. The dark charge increases with time due to instrument ageing (Tamminen et al., 2010). Its relative contribution to process for dimensional data and the process dat
- relative contribution to noise budget is larger for dim stars and at lower altitudes due to attenuation of stellar flux caused by the atmosphere. Note that at the stellar spectra level, dark charge and readout noise are additive, i.e., they do not depend on the





mean stellar signal. However, at the transmission spectra level (after dividing by the reference spectrum), all noise components become non-additive: they depend strongly on the stellar signal (noise is small for bright stars and larger for dimmer stars).

- In the stratosphere, the main source of the modeling error is the incomplete scintillation correction, which is of random nature. The residual scintillation error (i.e., the uncertainty due to incomplete scintillation correction) has been characterized in depth (Sofieva et al., 2009) and has been included in the inversion algorithm (Sofieva et al., 2010). The residual scintillation error depends on the obliquity of occultation; it vanishes for vertical (in-orbital-plane) occultations. Both the instrumental noise and the residual scintillation error are then propagated through the inversion (for details, see Kyrölä et al., 2010; Sofieva et al., 2010; Tamminen et al., 2010), and the uncertainties of the retrieved profiles are given by the corresponding covariance matrices. The square roots of their diagonal elements are often referred (also in this paper) to as precision estimates.
- The normalized χ^2 statistics, χ^2_{norm} , is commonly used for validating adequacy of theoretical description of measurements (forward model) and for indication of correctness of error estimates. For GOMOS, χ^2_{norm} after the spectral inversion is:

$$\chi_{\text{norm}}^2 = \frac{1}{N - p} (T - T_{\text{mod}})^T \mathbf{C}^{-1} (T - T_{\text{mod}}), \qquad (1)$$

²⁰ where *T* is the vector of observed transmittances, *T*_{mod} is the vector of modelled (theoretical) transmittances, **C** is the covariance matrix of measurement errors, *N* is the number of measurements and *p* is the number of retrieved parameters. If the theoretical model describes well the experimental data and the measurement errors are properly defined, $\chi^2_{norm} \approx 1$. For GOMOS v.6 data, χ^2_{norm} is very close to unity in the stratosphere (Fig. 1) thus indicating realistic uncertainty characterization in this altitude range. Some increase of χ^2_{norm} at lower altitudes is quite expected and is related mainly to uncertainties in aerosol modeling. For dim and medium-brightness stars, χ^2_{norm} can be even smaller than 1 in the mesosphere. This indicates overestimated instrumental





noise, and can results in overestimated uncertainty of the retrieved profiles. Overestimation of ozone uncertainties for dim stars is confirmed also by our validation analysis of precision estimates, as presented below in the paper.

3 Methods for validation of precision estimates

⁵ In this section, we review existing validation methods and discuss their applicability to GOMOS measurements.

3.1 Approaches to validation of precision estimates for atmospheric measurements

In laboratory, the experimental precision estimates can be obtained using the repeated measurements under the same conditions: the sample variance $s^2 = var(x)$ approaches the variance of random error distribution σ^2 (i.e., squared precision) when the size of sample *N* tends to infinity. The sample variance has a χ^2 distribution with N-1 degrees of freedom. It can be approximated for large *N* by a Gaussian distribution with the variance

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$$\operatorname{var}(s^2) \approx \sigma^4 \frac{2}{N}$$
,

giving the uncertainty of the experimentally estimated precision.

Contrary to laboratory experiments, geophysical observation conditions cannot be kept exactly constant for atmospheric measurements. Therefore, the sample variance contains a contribution due to the natural variability $\sigma_{nat}^2 : s^2 = \sigma^2 + \sigma_{nat}^2$. For validation of uncertainty estimates, σ_{nat}^2 should be minimized by selecting collocated measurements or it should be known from independent sources.



(2)

Approaches to validation of error estimates usually rely on variance of difference s_{12}^2 in a set of collocated measurements x_1 and x_2 :

$$s_{12}^{2} = \left\langle (x_{1} - x_{2})^{2} \right\rangle - \left\langle x_{1} - x_{2} \right\rangle^{2} = \sigma_{0,\text{nat}}^{2} + \sigma_{1}^{2} + \sigma_{2}^{2}.$$
 (3)

⁵ In Eq. (3), $\sigma_{0,nat}^2$ stands for the natural variability within a space-time collocation window (note that $\sigma_{0,nat}^2$ is different from σ_{nat}^2), and $\langle . \rangle$ denotes the mean. Three methods for precision validation have been developed and applied.

Method 1

For perfectly collocated measurements ($\sigma_{0,nat}^2 \approx 0$) from the same instrument with the

¹⁰ same precisions $\sigma_1 = \sigma_2 = \sigma$, Eq. (3) is reduced to $s_{12}^2 \approx 2\sigma^2$, thus allowing validation of uncertainty estimate σ . This method was realized, for example, for closely collocated MIPAS and OSIRIS measurements (Bourassa et al., 2012; Piccolo and Dudhia, 2007). The uncertainty of this experimental precision estimate $\hat{\sigma}^2 = s_{12}^2/2$ is defined by the uncertainty of sample variance s_{12}^2 .

15 Method 2

Fioletov et al. (2006) have proposed estimating simultaneously measurement precision and natural variability from sample variances of two perfectly collocated datasets and the variance of their difference (see Fioletov et al., 2006, and Appendix A for details). Since the precision estimates by the Fioletov's method are linear combinations
of three sample variances, they can have large uncertainty if one of the sample variances is large and/or the number of collocated measurements is limited (Appendix A; Fioletov et al., 2006). It is nearly impossible to select measurements exactly at the same location and time (perfectly collocated). In practice, satellite measurements separated by a few hundreds of kilometers and a few hours are considered as collocated.



The natural variability within the space-time collocation window is small but not zero. This results in additional difficulties in the application of this method, as observed by Bourassa et al. (2012). The small-scale natural variability also disturbs application of the Method 1.

5 Method 3

Provided many collocated measurements from the same instrument are available (selfcollocations), the precision of the dataset can be estimated also via computing twodimensional structure function, or the rms difference as a function of increasing separation in time and in space. Then the limit at zero spatio-temporal mismatch will de-

¹⁰ fine the measurement precision. This method has been applied to validation of radiooccultation measurements by Constellation Observing System for Meteorology, Ionosphere, and Climate (COSMIC) (Staten and Reichler, 2009), which consists of identical instruments on board of six microsatellites.

For a single instrument, self-collocated data can be successive measurements from same orbit, or measurements from different (successive) orbits. An analogous method (evaluation of the 1-D structure function) has been applied for validation of precision estimates of the MIPAS (Michelson Interferometer for Passive Atmospheric Sounding) instrument on board the Envisat satellite (Laeng et al., 2014).

3.2 Specifics of GOMOS measurements – challenges for precision validation

The stellar flux recorded by GOMOS, and thus signal-to-noise ratio and precision of retrieved profiles, depend on the magnitude and spectral class of the observed star, which means that the measurement precision varies substantially over the dataset. Precision of retrieved profiles depends slightly on obliquity of occultation due to the influence of scintillations (Sofieva et al., 2009). The GOMOS error estimates also slightly depend on ozone concentration, but this dependence is much weaker than the dependence on stellar magnitude and the spectral class. In addition, GOMOS uncertainty estimates





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grow with instrument age (Tamminen et al., 2010). These features make challenges for validation of GOMOS precision.

The number of self-collocated GOMOS measurements which are separated by less than 300 km in space and by less than 3 h in time is very limited. A sufficient amount

- 5 (~ 200 per year) of collocated occultations of the same star, which would potentially allow a statistically significant validation of precision estimates by methods 1 or 3, are available only for one star, namely star number 30 in the GOMOS catalogue (S30, we will use similar notations for stars in GOMOS catalogue hereafter). However, S30 collocations occur during winter close to the North Pole where natural variability of
- ¹⁰ ozone is large. In addition, the measurements in limb-viewing geometry are not local but horizontally integrated with the effective horizontal extent ~ 300 km; therefore GO-MOS measurements with the same tangent point but at different azimuth angles are not expected to be exactly the same. We applied a variant of the method 3 to these GOMOS ozone profiles (the details of the analysis is presented in Appendix B) and,
- as expected, found that a significant excess of natural variability over the GOMOS precision estimates for S30 combined with the absence of very close collocations do not allow making definitive conclusions about the quality of GOMOS precision estimates (Appendix B). Other GOMOS self-collocations (less than 30 per year) are for different stars in successive orbits (Guirlet et al., 2006) in years 2002–2004.

The estimated retrieval uncertainty for GOMOS ozone is small in the stratosphere; for very bright stars it is ~ 0.5–2 % (Sofieva et al., 2009; Tamminen et al., 2010). For experimental estimation of precision in such occultation by the Fioletov's method, a very large number of collocations with measurements from another instrument is needed, even in the regions of low natural variability (Appendix A). For example, in equatorial regions with natural ozone variability ~ 5 %, in order to estimate/validate the GOMOS precision ~ 1 % with uncertainty of 50 %, more than 2500 collocated and accurate measurements would be needed. Such amount of collocations for each GOMOS star (or similar stars) is not available, even for satellite instruments with dense sampling like Michelson Interferometer for Passive Atmospheric Sounding (MIPAS) on board Envisat or Microwave





Limb Sounder (MLS) on board EOS-Aura. For example, at latitudes 20° S– 20° N, there are only ~ 500 collocations per year of MIPAS measurements with that of ten brightest GOMOS stars. Consequently, the method of (Fioletov et al., 2006) cannot be applied to validation of GOMOS precision estimates either.

A simple method allowing validation of GOMOS ozone precision estimates is presented below.

4 A differential method for validation of GOMOS ozone precision estimates

4.1 Description of the method

If the measurements are selected in a region of small and slowly-changing natural variability, then the sample variances corresponding to different datasets *i* (for GOMOS, corresponding to different stars) can be written as

$$s_i^2 = \sigma_{\rm nat}^2 + \sigma_i^2.$$

5

If the precision estimates are correct, then the difference in sample variance will be equal to the difference in precision estimates, $s_i^2 - s_j^2 = \sigma_i^2 - \sigma_j^2$. The term σ_{nat}^2 cancels out because it is assumed to be the same for both samples.

At the same time, s_i^2 provides the upper limit for experimental estimates of measurement precision, as $s_i^2 > \sigma_i^2$. If $\sigma_i \to 0$, then $s_i^2 \to \sigma_{nat}^2$.

Important conditions for successful application of this method (which we call "differ-20 ential method" hereafter) are:

- a. Natural variability should be the same for the samples i and j.
- b. Natural variability should not be large compared to the precision estimates, otherwise the sample variance estimates will have large uncertainty. This condition of small natural variability is satisfied for ozone in the tropical stratosphere and in the summer stratesphere at other latitudes.
- the summer stratosphere at other latitudes.



(4)



c. Measurements in each sample should be of the same precision.

4.2 Data and results

For an initial analysis, we selected tropical occultations $(20^{\circ} \text{ S}-20^{\circ} \text{ N})$ in the year 2008. The restriction to one year was made in order to avoid multi-year variability due to

quasi-biennial oscillation. Only stars for which more than 200 occultations were available are considered. The latitudes of these occultations are shown in Fig. 1 and the information about these occultations is presented in Table 1. A particular star is available only during 2–3 months; its successive occultations are at approximately the same latitude and the same local time. The GOMOS measurement scheme provides naturally homogeneous longitudinal (zonal) coverage. For other years, the sampling pattern is very similar. The outliers and suspicious data were removed by the screening procedure presented in Appendix C.

The comparison of sample variances and precision estimates are presented in Fig. 3 for very bright stars S4 and S10 (left), and star S4 and the dim star S134 (right). As seen in Fig. 3 (left), the sample variances for the two bright stars S4 and S10 are very close to each other and show specific variations with height. The sample variance in S4 occultations is slightly larger than for S10 occultations, and this difference is fully accounted for by the difference in squared precisions (although S4 is brighter than S10, uncertainty estimates are larger for S4 because these stars have different effective

- temperatures). The uncertainty (rms) of sample variance shown by error bars in Fig. 3 has been estimated according to Eq. (2). Very small error bars on squared precision curves (dashed lines) show the standard deviation of the precision distribution, which is very small for ozone in tropics. The analogous comparison for the bright star S4 and the dim star S134 show very similar features: sample variance in S134 occultations is
- ²⁵ larger than that in S4 variance by the amount approximately equal to the difference in the corresponding squared precision estimates.

Figure 4 compares difference in the sample variance $s_2^2 - s_1^2$ with the difference in squared precisions $\sigma_2^2 - \sigma_1^2$, for different pairs of stars. In this comparison, time intervals



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are restricted in such a way that the spatio-temporal coverage by the selected stars is as close as possible. In particular, the time interval from 10 September to 20 October is taken for stars 2 and 161, and the interval from 15 August to 28 October for stars 9 and 143, etc. The difference in sample variance is in perfect agreement with the difference in precision estimates for the stars of visual magnitude smaller than ~ 2 . 5 This can serve as an indicator of correctness of these GOMOS precision estimates, in combination with the upper limit of uncertainty given by the sample variances and proximity of χ^2_{norm} to 1. In the comparisons with dim stars (cases S9&S143 and S4&S134), the difference in squared precision estimates is somewhat larger than the difference in sample variances, which might indicate an overestimation of error bars for dim stars 10 (see also discussion below).

If the GOMOS ozone error estimates are correct, then the estimates of natural variability $\hat{\sigma}_{nat}^2$ computed from occultations of each star:

$$\hat{\sigma}_{nat}^2 = s_i^2 - \sigma_i^2$$

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should be approximately the same (provided the real natural variability in the corresponding samples in the equatorial stratosphere is the same). Figure 5 (top) shows estimates of natural variability in the latitude zone 20° S-20° N at altitudes 25-40 km inferred from the sample variance and precision estimates for different stars, which are plotted as a function of precisions σ_i , for the considered year 2008. For this analysis, all measurements shown in Table 1 are used. The dashed black line shows $\hat{\sigma}_{nat 0}^2$ estimated from the limit s_i^2 as $\sigma_i^2 \rightarrow 0$ and technically computed as a weighted mean of $\hat{\sigma}_{nat}$ estimates using the 7 brightest stars:

$$\hat{\sigma}_{\text{nat},0}^2 = \sum_{i=1}^7 w_i \left(s_i^2 - \sigma_i^2 \right),$$

where the weights w_i are inversely proportional to the uncertainty of the parameter $(s_i^2 - \sigma_i^2)$ estimated as described above (this section and Eq. 2). This estimated



(5)

(6)



natural variability is approximately $\hat{\sigma}_{nat,0}^2 \approx 32.5 (\%)^2$, or $\hat{\sigma}_{nat,0} \approx 5.7\%$. As seen in Fig. 5 (top), many estimates of natural variability from individual stars agree within 2σ uncertainty intervals with $\hat{\sigma}_{nat,0}^2$. This can serve as an indicator of correctness of GOMOS error estimates for these cases. However, for three stars: S113, S135 and S143, the estimates of natural variability become even negative. This indicates overestimation of error bars for these occultations. Another interesting feature is variations in natural variability, which can be related to atmospheric processes or/and to non-uniform sampling by measurements.

We have performed analogous estimations of natural variability also for years 2007 and 2003 (center and bottom panels in Fig. 5). In 2007, the features are very similar to these observed for year 2008: very close estimates of natural variability of a few percent for bright stars, and very low, even negative, estimates of natural variability variance for dim stars (stars S113, S134, S141, S143, S159 in 2007; stars S43, S134, S135 in 2003). Note that in 2003 the collection of stars is slightly different from that in 2007–

- ¹⁵ 2008, because the azimuth range for GOMOS measurements has been restricted after 2005 due to instrumental problems. Furthermore, uncertainty estimates are smaller for all stars in 2003 than in 2007 and 2008 (the ageing effect). It is interesting to note that the estimated natural variability (we consider here the estimates based on observations of 7 brightest stars) is very similar in 2003 and 2007: 4.2 and 4.3 %, respectively; but
- it is larger in 2008, 5.7%. This feature might be related to quasi-biennial oscillation (QBO): years 2003 and 2007 correspond to easterly QBO winds at 10 hPa, while the QBO winds were westerly in 2008. However, this hypothesis requires a more detailed examination.

4.3 Discussion

²⁵ The proposed differential method allows testing the precision estimates in complicated cases like GOMOS ozone measurements, when collocated measurements are not





available and estimated precision is small (good accuracy). The requirement for application of this method is that natural variability is small and slowly-varying.

Small additive errors (i.e., the errors, which do not depend on stellar properties) in precisions cannot be detected by the method. Indeed, if precision estimates have an additive component $\sigma_*^2 : \sigma_i^2 = \tilde{\sigma}_i^2 + \sigma_*^2$, $\sigma_j^2 = \tilde{\sigma}_j^2 + \sigma_*^2$, then it is cancelled out in the difference $\sigma_i^2 - \sigma_j^2$. In this case, it is impossible to say whether σ_*^2 is realistic or not, if σ_*^2 is small enough so that the natural variability estimates $s^2 - \sigma_i^2$ are positive. All dominating measurement uncertainty components (photon noise, dark charge) strongly depend on the stellar properties. The only exception is the residual scintillation error, which depends on obliquity of occultation (and does not depend on stellar properties), i.e., it is additive. However, the residual scintillation error is relatively small and it has an accurate parameterization in GOMOS retrievals (Sofieva et al., 2010), therefore it should not disturb the application of the differential method to GOMOS data (this is consistent

¹⁵ The analysis of GOMOS occultations in the tropical stratosphere has shown that the difference in sample variances for different stars at altitudes 25–45 km is well explained by the difference in precisions, if stars are not dim (visual magnitude less than 1.9). Since (i) this is observed for several stars and (ii) $\chi^2_{norm} \approx 1$ in these occultations in the stratosphere, we can conclude that GOMOS precision estimates are close to reality for such measurements.

with the results presented above).

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total error budget.

For some dim (and cool) stars, the random error has been significantly overestimated, which results in negative estimates of natural variability variance using Eq. (5). This is also confirmed by $\chi^2_{norm} < 1$ down to 30 km in occultations of dim stars. The careful inspection of the inversion algorithm has shown that, most likely, the reason for such behavior is imperfect estimation (a moderate overestimation) of dark charge variance. This overestimation of dark charge is present for all occultations, but for bright stars this is invisible in retrievals, as the dark charge has a small contribution to the





The condition of small natural variability is not satisfied in the mesosphere and lower thermosphere (MLT). In addition, GOMOS error estimates for ozone are significantly smaller than the natural variability in the mesosphere, thus estimating their difference from sample variances would become uncertain. However, there are reasons to trust

the GOMOS precision estimates also at upper altitudes. First, the error estimates are based on the same method as in the stratosphere, and we see no reasons why they should fail at upper altitudes. Second, $\chi^2_{norm} \approx 1$ holds for the whole altitude range, thus one would expect correctness of these error estimates also at upper altitudes.

The differential method for validation of precision estimates cannot be applied in the upper troposphere and the lower stratosphere either, because of large ozone variability in this region caused by variations in the tropopause height.

Provided the conditions a-c (Sect. 4.1) are satisfied, the method can be also applied to other constituents. However, these conditions are often not satisfied for other constituents retrieved by GOMOS. Let us consider NO₂ as an example. The condition c is

violated for NO₂. Precision estimates for NO₂ exhibit rather large scattering (not shown here), therefore small differences in variabilities are not detectable by precision estimates: they are within uncertainty intervals. For GOMOS, the differential method for precision validation is applicable mainly for ozone in the stratosphere, which was the primary scientific motivation for this instrument.

20 4.4 Extension for other instruments

The extension of the differential method for precision validation by including data from another instrument is quite straightforward: it can be considered as one more sample with corresponding precision estimates.

As an example, we compare natural variability in tropics, as estimated by GOMOS ²⁵ data of 7 brightest stars and by the MIPAS instrument on board the Envisat satellite. MIPAS is a Fourier transform spectrometer operating in infrared, which provides vertical profiles of ozone and other trace gases. For our illustration, we have used the data processed with KIT IMK/IAA version V5R_O3_220/221 Research Processor (von





Clarmann et al., 2003, 2009). MIPAS provides ozone profiles in the altitude range from 6 to 70 km with a vertical resolution of 2-5 km. In the tropical stratosphere, estimated precision of MIPAS ozone profiles is 1-3%. Recent validation of MIPAS precision estimates using self-collocated measurements (methods 1 and 3 explained in Sect. 3.1)

⁵ have shown that the MIPAS precision estimates are close to reality (Laeng et al., 2014). Figure 6 shows profiles of natural variability estimates $\hat{\sigma}_{nat}$ obtained with Eq. (5) for latitudes 20° S–20° N using MIPAS night-time data and GOMOS measurements of 7 brightest stars in 2008. As observed in Fig. 6, estimates of natural variability from GOMOS and from MIPAS are very close to each other, even variations with altitude are similar. The values of mean natural variability in the altitude range 25–45 km are very close to each other: 5.78% for MIPAS and 5.68% for GOMOS. Such a good agreement can be considered as an additional confirmation that both MIPAS error bars and GOMOS error bars for bright stars are realistic.

5 Summary

In this paper, we have discussed validation of precision estimates for ozone profiles retrieved by the stellar occultation instrument GOMOS/Envisat. The validation of GOMOS precision estimates is challenging, because of dependence of instrumental noise (and thus uncertainty of retrieved profiles) on stellar properties, insufficient number of GOMOS-GOMOS collocated measurements and small uncertainties of ozone retrievals in case of bright stars. We have proposed a simple differential method for validation of GOMOS ozone precision estimates, which is based on comparisons of difference in sample variance with the difference in squared precision estimates, for measurements from different stars selected in the region of low natural variability.

The application of the proposed method to GOMOS ozone profiles in the stratosphere has shown that GOMOS precision estimates are realistic for non-dim stars (magnitude less than 1.9). For dim stars, uncertainties of retrieved ozone profiles are overestimated. The reason for this overestimation is now understood: it is related to





improper accounting the uncertainty associated with dark charge correction in the GO-MOS noise error budget. This issue will be corrected in the future GOMOS data processing.

The application of the differential method to other altitude ranges and to other con stituents is hardly possible due to violation of assumptions needed for the method to work. Extension for using other instruments is quite natural, as illustrated in our paper using GOMOS and MIPAS measurements. Estimates of ozone natural variability in tropics from MIPAS and GOMOS 7 brightest stars are very close to each other; thus providing an addition confirmation of correctness of the corresponding error estimates,
 for both instruments.

Appendix A

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Uncertainty of precision estimates by the Fioletov's method

Fioletov et al. (2006) have proposed a method that allows simultaneous estimates of measurements precision and natural variability based on (perfectly) collocated data from two instruments. This method relies on sample variances s_i^2 of the collocated data:

$$s_i^2 = \sigma_{\text{nat}}^2 + \sigma_i^2, \ i = 1,2$$
 (A1)

and the variance of their difference:

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$$S_{1,2}^2 = \left\langle (x_1 - x_2)^2 \right\rangle = \sigma_1^2 + \sigma_2^2$$

In Eqs. (A1) and (A2), σ_{nat}^2 is natural variability and σ_i^2 are measurement precisions. Solving Eqs. (A1) and (A2) for these parameters, we get their experimental estimates



(A2)

based on sample variance:

$$\begin{split} \hat{\sigma}_{nat}^2 &= 0.5 \left(s_1^2 + s_2^2 - s_{12}^2 \right) \\ \hat{\sigma}_1^2 &= 0.5 \left(s_1^2 - s_2^2 + s_{12}^2 \right) \\ \hat{\sigma}_2^2 &= 0.5 \left(s_2^2 - s_1^2 + s_{12}^2 \right) \end{split}$$

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The uncertainty of the natural variability and precision estimates given by Eq. (6) depend on uncertainty of sample variances, which depend, in turn, on sample variances themselves and the number of measurements. The estimates are thus only as accurate as the least accurate of these parameters. In approximation of large samples (when χ^2 distribution for the sample variance can be approximated by a normal distribution with 10 the variance given by Eq. 2), the variance of the estimate Eq. (A3) can be expressed in terms of "true" natural variability and precision variances σ_{nat}^2 , σ_1^2 and σ_2^2 as:

$$\operatorname{var}(\hat{\sigma}_{1}^{2}) = \operatorname{var}(\hat{\sigma}_{2}^{2}) = \operatorname{var}(\hat{\sigma}_{nat}^{2}) = \frac{1}{2N} \left(\left(\sigma_{nat}^{2} + \sigma_{1}^{2} \right)^{2} + \left(\sigma_{nat}^{2} + \sigma_{2}^{2} \right)^{2} + \left(\sigma_{1}^{2} + \sigma_{2}^{2} \right)^{2} \right)$$
(A4)

with the following simple estimates for upper and lower limits 15

$$\frac{1}{N} \left(\sigma_{\text{nat}}^4 + \sigma_1^4 + \sigma_2^4 \right) < \text{var}(\hat{\sigma}_{1,2,\text{nat}}^2) < \frac{1}{N} \left(\sigma_{\text{nat}}^2 + \sigma_1^2 + \sigma_2^2 \right)^2$$
(A5)

The estimates can be very uncertain in case where the natural variability significantly exceeds the measurement precision, or in case of poor accuracy of the collocated data. For example, let $\sigma_2 \ll \sigma_1$ and $\sigma_{nat}/\sigma_1 = 5$. Then the relative uncertainty of precision

estimate
$$\frac{\operatorname{std}(\hat{\sigma}_1^2)}{\sigma_1^2} \approx \sqrt{\frac{1}{N} \left(1 + \frac{\sigma_{\text{nat}}^4}{\sigma_1^4} + \frac{\sigma_{\text{nat}}^2}{\sigma_1^2}\right)}$$
, which is ~ 255 % for $N = 100$, ~ 85 % for $N = 900$ and ~ 51 % for $N = 2500$.

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(A3)

Appendix B

Validation of GOMOS precision estimates using self-collocated data

Relatively many self-collocated GOMOS occultations exist only for one star, S30 (magnitude 1.7, effective temperature 30 000 K), close to North Pole in winter. In our analysis, we selected the ozone profiles retrieved from S30 occultations with ground separation d_0 less than 300 km and time difference Δt less than 3 h. For majority of collocated pairs, the time difference is ~ 100 min (one orbit). We have used data from years 2007–2008, in which the number of collocated profiles is maximal, ~ 200 profiles per year (a relatively short time period of 2 years has been used in order to avoid the effect of changes in error estimates with time due to instrument ageing).

Figure 7 shows profiles of the parameter $s_{12}/\sqrt{2}$, s_{12} being the sample standard deviation (Eq. 3) as a function of the distance *d*. The parameter $s_{12}/\sqrt{2}$ approximates the experimental error estimates, which should converge to predicted error estimates when $d \rightarrow 0$ (if the latter ones are correct). It is analogous to the integral of structure function, which is widely used in the theory of random functions (e.g., Yaglom, 1987).

- ¹⁵ function, which is widely used in the theory of random functions (e.g., Yaglom, 1987). The distance *d* represent the separation of air parcels corresponding to collocated measurements with the advection of air masses taken into account. It is evaluated as $d(z) = |\mathbf{d}_0(z) + \mathbf{v}(z) \cdot \Delta t|$, where $\mathbf{d}_0(z)$ is the ground distance and $\mathbf{v}(z)$ are the profiles of wind speed from ERA Interim data at locations of GOMOS occultations.
- As observed in Fig. 7, the experimental precision estimates $s_{12}/\sqrt{2}$ decrease with decreasing separation of measurements, as expected, but, because very small separations are not covered with GOMOS data, they are larger than the predicted error estimates. A similar analysis of collocated MIPAS ozone data close to North Pole in winter has shown a very similar behavior of experimental and estimated uncertaintice (not shown here). However, when analyzing collocated MIPAS data at North Pole
- ties (not shown here). However, when analyzing collocated MIPAS data at North Pole in summer, the experimental error estimates converge practically down to precision estimates, as shown in Fig. 26 of Laeng et al. (2014). This is a clear indication that



the ozone natural variability, even at small scales (a few hundreds of kilometers), is not zero in winter polar regions. The magnitude of this small-scale natural variability

 $\sqrt{s_{12}^2/2 - \sigma^2}$ is very similar in analyses of GOMOS and MIPAS data, it is ~ 3% at 20–30 km increasing up to 5–6% at 40–50 km.

Absence of collocated GOMOS data in the regions of low natural variability does not allow a full validation of precision estimates according to Method 3, whose application is illustrated here. However, we observe a reasonable behavior of GOMOS precision estimates: they are lower than the sample variances of ozone profile difference.

Appendix C

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10 Screening of outliers in GOMOS data

The following three-step procedure has been applied for removing invalid or suspicious GOMOS data.

- 1. The whole profile is ignored, if
 - values of mixing ratio > 15 ppmv or < -0.5 ppmv is reported at altitudes 25-45 km;
 - ii. number density > 5×10^9 cm⁻³ is reported at ozone minimum (77–80 km).
 - iii. value of mixing ratio > 100 ppmv is reported at any altitude.

Any of i–iii conditions result in removing the whole profile. This is the filtering of clear outlier-profiles.

- 20 2. A value at a certain altitude level is filtered, if:
 - the value is flagged (http://earth.eo.esa.int/pcs/envisat/gomos/documentation/ 04_Vol10_Gomos_3K_v7.pdf)



- ii. error estimate or absolute value of mixing ratio exceed the threshold given in Table A1.
- 3. For stars with UV flux < 900 photons, all values above 42 km are removed.

UV flux at 275 nm was pre-computed for each star using the Plank law. This operation removes the upper part of the ozone profiles from occultations of dim and cool stars, which are unreliable at high altitudes due to insufficient signal-to-noise ratio in ultraviolet (Kyrölä et al., 2006).

Finally, profiles having too few valid points (less than 10) and the valid altitude range smaller than 20 km in the stratosphere were ignored.

Note that this screening procedure differs from the more conservative one recommended in the GOMOS readme document http://earth.eo.esa.int/pcs/envisat/gomos/ documentation/RMF_0117_GOM_NL__2P_Disclaimers.pdf.

Acknowledgements. The work has been supported by the ESA Ozone Climate Change Initiative project. The work of the FMI team has been supported by the Academy of Finland (projects MIDAT, ASTREX and INQUIRE).

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Table 1. Information about the GOMOS occultations used for the analyses (years 2003, 2007, 2008). The obliquity angles are practically the same for different years. The occultations with large obliquity angles (> 60°) were performed in 2003.

Star_id	Visual magnitude	Effective temperature	Mean obliquity, deg
2	-0.7	7000 K	49
4	0	5800 K	34
9	0.5	24 000 K	42
10	0.6	28 000 K	38
12	0.8	30 000 K	31
18	1.2	9700 K	70
29	1.6	10 200 K	7
31	1.7	15 200 K	55
38	1.8	11 000 K	68
41	1.9	4100 K	39
43	1.9	4250 K	17
45	1.9	26 000 K	42
63	2.1	2800 K	55
71	2.2	7000 K	39
84	2.4	4500 K	62
113	2.7	5000 K	53
124	2.8	30 000 K	25
134	2.8	6600 K	29
135	2.8	5800 K	1
141	2.8	4600 K	40
143	2.9	7200 K	35
148	2.9	4100 K	32
157	2.9	9300 K	62
159	2.9	7200 K	30
161	2.9	4500 K	49





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Table C1. Upper limit for allowed uncertainty and mixing ratio. All values larger than these thresholds are removed.

Altitudes	maximal uncertainty	maximal mixing ratio (modulus)
< 18 km	70 %	10 ppmv
18–65 km	30 %	50 ppmv
> 65 km	150 %	50 ppmv



Fig. 1. χ^2_{norm} for stars of different magnitudes. Dots: individual values, solid lines: median profiles, dashed lines: 16th and 84th percentiles. Number of occultations is specified in the figure. The 2008 data in the Northern Hemisphere are used.



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Fig. 2. Locations of occultations selected for the analysis. Each color corresponds to a particular star, whose number in the GOMOS catalogue is written near the corresponding line.







Fig. 3. Sample variances s_i^2 and the estimated precision variances σ_i^2 of GOMOS ozone profiles (left) for stars 4 and 10 in Januray–March 2008; (right) for stars 4 and 134.







Fig. 4. Difference in sample variance $s_2^2 - s_1^2$ (solid lines) and the difference in precision variances $\sigma_2^2 - \sigma_1^2$ (dashed lines), for different collocated pairs of stars specified in the legend.







Fig. 5. Estimates of natural variability variance $\hat{\sigma}_{nat}^2 = s_i^2 - \sigma_i^2$ at altitudes 25–40 km for different stars plotted as a function of precisions σ_i . Star numbers in GOMOS catalogue are indicated. Colors indicate star magnitude: from red for bright stars (small magnitude, small star number) to blue for dim stars (large magnitude, large star number). The errorbars are 2σ uncertainty intervals. Dashed lines indicate the mean natural variability estimates obtained using 7 brightest stars. Magenta lines highlight zero.















