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assimilation of radio
occultation**

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Ionospheric assimilation of radio occultation and ground-based GPS data using non-stationary background model error covariance

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Abstract

Ionospheric data assimilation is a powerful approach to reconstruct the 3-D distribution of the ionospheric electron density from various types of observations. We present a data assimilation model for the ionosphere, based on the Gauss–Markov Kalman filter with the International Reference Ionosphere (IRI) as the background model, to assimilate two different types of total electron content (TEC) observations from ground-based GPS and space-based FORMOSAT-3/COSMIC (F3/C) radio occultation. Covariance models for the background model error and observational error play important roles in data assimilation. The objective of this study is to investigate impacts of stationary (location-independent) and non-stationary (location-dependent) classes of the background model error covariance on the quality of assimilation analyses. Location-dependent correlations are modeled using empirical orthogonal functions computed from an ensemble of the IRI outputs, while location-independent correlations are modeled using a Gaussian function. Observing System Simulation Experiments suggest that assimilation of TEC data facilitated by the location-dependent background model error covariance yields considerably higher quality assimilation analyses. Results from assimilation of real ground-based GPS and F3/C radio occultation observations over the continental United States are presented as TEC and electron density profiles. Validation with the Millstone Hill incoherent scatter radar data and comparison with the Abel inversion results are also presented. Our new ionospheric data assimilation model that employs the location-dependent background model error covariance outperforms the earlier assimilation model with the location-independent background model error covariance, and can reconstruct the 3-D ionospheric electron density distribution satisfactorily from both ground- and space-based GPS observations.

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1 Introduction

The ionosphere is becoming more relevant to human society with its reliance on modern technology, since the accuracy of navigation and quality of telecommunication is influenced by ionospheric conditions. Disruption of communications and navigation systems can have severe societal consequences. Even though the ionospheric observational techniques and the ionospheric models have gone through considerable development sustained over many decades, accurate monitoring and forecasting of the ionosphere conditions still presents obstinate challenges. Data assimilation procedures have recently come to play an important role in ionospheric research to overcome limitations of observations and models, and is an active area of research and development.

Some of the most comprehensive operational physics-based ionospheric data assimilation systems have been developed by Utah State University (e.g., Schunk et al., 2005; Scherliess et al., 2006) and University of Southern California and Jet Propulsion Laboratory (e.g., Wang et al., 2004; Pi et al., 2009; Komjathy et al., 2010). Lee et al. (2012) have recently assimilated the retrieved FORMOSAT-3/COSMIC (F3/C) electron density profiles into a general circulation model of the thermosphere and ionosphere. Extensive variational data assimilation procedures have been developed with an empirical ionospheric model (e.g., Bust et al., 2004, 2007). Nicolls et al. (2009) applied this methodology to improve the E region electron density retrieval from the F3/C data. Yue et al. (2011a, 2012) have assimilated F3/C and other Radio Occultation (RO) data into an empirical ionospheric model to obtain an improved global specification of the ionosphere.

The NOAA United States-Total Electron Content (US-TEC) model (Fuller-Rowell et al., 2006) is designed to specify TEC over the continental United States (CONUS) from ground-based GPS TEC data. The US-TEC uses the empirical ionosphere model, International Reference Ionosphere 95 (IRI95) (Bilitza, 1997), as a background model, and uses the empirical orthonormal functions (EOFs) and their coefficients (Spencer

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et al., 2004) to represent states in the Kalman filter (Kalman, 1960; Kalman and Bucy, 1961). The average root mean square error of US-TEC is 2.4 TEC units (Araujo-Pradere et al., 2007). The Kalman filter is one of the most commonly used approaches to ionospheric data assimilation. The Kalman filter update equation is given as

$$\mathbf{x}_a = \mathbf{x}_b + \mathbf{K}(\mathbf{y} - \mathbf{H}\mathbf{x}_b), \quad (1)$$

$$\mathbf{K} = \frac{\mathbf{P}\mathbf{H}^T}{\mathbf{H}\mathbf{P}\mathbf{H}^T + \mathbf{R}}, \quad (2)$$

where $\mathbf{x}_a$ is the state vector after an update, $\mathbf{x}_b$ is the state vector of the background model, $\mathbf{y}$ is a vector of observations, $\mathbf{H}$ relates the state to the observations, $\mathbf{H}^T$ is transpose matrix of $\mathbf{H}$, $\mathbf{P}$ is the background model error covariance, $\mathbf{R}$ is the observation error covariance, and $\mathbf{K}$ is the Kalman gain (e.g., Welch and Bishop, 2000). In the US-TEC, the Kalman filter state $\mathbf{x}_b$ is composed of the coefficients of EOFs that characterize the principal modes of electron density vertical profiles. If Ψ_v and $\mathbf{a}_v$ represent vertical EOFs and their coefficients, the electron density at a given altitude location v and longitude/latitude location h is expressed as $\mathbf{Ne}(v, h) = \sum_{m=1}^6 \mathbf{a}_{v_m}(h) \Psi_{v_m}(v)$ where $\mathbf{Ne}$ is the grid-point electron density itself and m is an order of EOF. $\mathbf{x}$ in Eq. (1) is given by a vector of $\mathbf{a}_v$ in the US-TEC. The 6 EOFs are computed by using singular value decomposition, EOF1 is the dominant term of EOFs to represent the mean ionospheric profile. The higher-order EOFs gradually decrease their significance for allowing the reconstructed profile to depart from the mean (Spencer et al., 2004).

MARINER IV first applied the RO observation technique to observe the Mars atmosphere and ionosphere in 1965 (Kliore et al., 1965). MicroLab-1 GPS/MET was launched in 1995 and applied to monitor the Earth's atmosphere and ionosphere by using GPS RO technique (Hajj and Romans, 1998; Kursinski et al., 1997). The integrated content of ionospheric electron density, namely total electron content (TEC), has been measured between the GPS satellites and MicroLab-1. This is a way to observe the ionosphere horizontally at different altitudes and obtain the electron density profile

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using the Abel inversion technique. The F3/C mission was launched in April 2006, and has six micro satellites in the different orbital planes. The GPS radio occultation experiment (GOX) is one of the satellite mission objectives, and observes the ionosphere and atmosphere vertical structure by using the RO observation technique. RO observations, particularly from F3/C, have significantly improved our capability of monitoring the global ionosphere (Cheng et al., 2006; Schreiner et al., 2007).

The overarching goal of our study is to assimilate not only the ground-based GPS data, but also F3/C RO data into US-TEC. However, the original scheme was designed for assimilation of TEC between ground-based stations and GPS satellites, and is not ideal for assimilation of the RO TEC data. New data assimilation approaches that can better accommodate the RO data need to be developed. To this end, our study attempts to make the scheme more flexible; thus the Kalman filter equations will now be solved with respect to the grid-point electron density values (i.e., x is given by a vector of grid-point electron density itself, $\mathbf{Ne}(v, h)$) so that more realistic characteristics of the background model error can be incorporated. A new type of the background model error covariance is derived from an ensemble of IRI model outputs by representing location-dependent vertical and horizontal correlations using EOFs. Its performance is compared with a case where a simple stationary (i.e., location-independent) correlation is used in the Kalman filter. It should be noted that this study primarily focuses on implementation of the Kalman filter update step. The Kalman filter forecast step is outside of the scope of this study.

We use Observing Simulation System Experiments (OSSEs), designed to mimic realistic observing systems of the ground-based GPS, and F3/C RO data to assess the impact of different types of the background model error covariance and the quality of assimilation analyses. Assimilation results are further validated with Millstone Hill incoherent scatter radar (ISR) electron density data, and compared with the F3/C GOX electron density profiles retrieved by the Abel inversion technique. Assimilation analyses are also presented in the form of TEC maps during both the daytime and nighttime. The use of F3/C RO data in data assimilation procedures is shown to improve both the

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vertical and horizontal structure of the ionospheric electron density distribution. The model domain extends from -140° to -60° with 2° resolution in longitude, from 10° to 60° with 2° resolution in latitude, and from 80 to 1000 km with 15 km resolution in altitude.

2 Data error and data thinning

When ground-based GPS and F3/C RO observation data are ingested into the data assimilation model, the observational errors need to be taken into account. Data from 200 ground-based GPS stations on the CONUS and F3/C RO TEC are used in examples shown later. More than 2000 GPS stations exist on the ground all over the world, and can yield the high-resolution TEC observations to determine horizontal structures of the ionosphere for monitoring various ionospheric phenomena and diurnal variations (Liu et al., 1996). However, most stations don't provide the differential code bias (DCB) of GPS receivers. Kakinami et al. (2009) used the Global Ionospheric Map (GIM) developed by Jet Propulsion Laboratory (Mannucci et al., 1998) as a reference to eliminate the instrumental biases. The differential instrumental biases of GPS receivers are estimated by the GIM minimum TEC value at 04:00 to 06:00 LT at GPS receivers, while the DCB of GPS satellite is calibrated by using the center for orbit determination in Europe (CODE) values (Schaer, 1999). The ground-based GPS TEC in this study is treated as DCB-free TEC after these DCB calibration processes. The main error sources of the absolute TEC value obtained from RO include multipath effects, DCBs from GPS and Low Earth Orbit (LEO) satellites, and errors in leveling of the phase to the pseudorange TEC (Yue et al., 2011b). This study used the F3/C podTec data produced by the COSMIC Data Analysis and Archival Center (CDAAC), and assumes that the absolute TEC values are free of DCB and multipath errors because these major errors are eliminated by CDAAC.

Every GPS satellite can transmit signals at dual-frequency carrier phases (L1: 1575.42 MHz, L2: 1227.60 MHz). Coarse/Acquisition (C/A: 1.023 MHz) and Precision

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codes (P1: 10.23 MHz) are coded on the L1 carrier phase, and another Precision code (P2: 10.23 MHz) is coded on the L2 carrier phase. The absolute and relative TEC can be calculated from the pseudorange and carrier phase respectively (Sardón et al., 1994). Since the satellite error sources influence the precision of TEC calculated from pseudorange (**TEC_P**), the precision of **TEC_P** is much lower than the TEC calculated from carrier phase (**TEC_L**). The leveled TEC is obtained by leveling the carrier phase TEC to the pseudorange TEC to benefit from the precision of **TEC_L** and the accuracy of **TEC_P**. Although the main errors of ground-based GPS and F3/C RO data are mostly eliminated, some unknown errors still remain. The leveling error formula of each GPS

observation arc is given by $\sqrt{\frac{\sum_{i=1}^n (\text{TEC}_{L_i} - \text{TEC}_{P_i})^2}{n}}$, where n is the number of observations in each GPS arc and i is the i th observation data point in each GPS arc, where the cycle slip has been resolved. The leveling TEC errors are small but hardly eliminated completely, and it should be taken into consideration when modeling the observation error covariance.

Data thinning is required because sampling space and time frequency of the GPS technique is significantly higher than the temporal and spatial resolution of data assimilation analysis. In this study, the grid point resolution is 2° for longitude and latitude, and 15 km for altitude. To thin the data, one out of 31 continuous observation data points for a given GPS arc is selected for ingestion into the assimilation model. This number for the data thinning is determined by trial and error. The standard deviation from 31 continuous samples is calculated to determine the representativeness error resulting from the fact that scales resolved by the data assimilation model are lower than what are observed.

The main sources of GPS data errors are described in the section. Errors resulting from the multipath effects and the DCB of GPS satellites, F3/C satellites, and ground-based GPS stations have been eliminated before ingestion through the various calibration processes mentioned above. The leveling TEC error and representativeness

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error are the two types of errors that are combined to model the observation error covariance.

3 Covariance models

We develop two types of the background model error covariance in this study (**P** in Eq. 2): location-independent covariance and location-dependent covariance, and compare their effects on the quality of assimilation analysis. Location-independent (i.e., stationary) covariance refers to a covariance whose correlation structure is homogeneous and isotropic (in other words, the vertical and horizontal correlations at every grid location are identical). A Gaussian function is used to describe the stationary correlation in examples shown later. The length scale of longitude and latitude is 3° and the length scale for altitude is 50 km. These length scales are determined by a number of length scale tests. The variance of the background model error covariance is calculated from 62 different IRI electron density distributions, the equivalent of two months' worth of data, obtained by using randomized values of IG index and sunspot number IRI input parameters. The IG index affects the *NmF2* and sunspot number changes the *hmF2*; the IG index and sunspot number are specified by the random values sampled from a uniform distribution bounded by the given maximum and minimum value. In reality, spatial correlation of the electron density varies with location (i.e., inhomogeneous) and direction (i.e., anisotropic) in the ionosphere. Assuming the same model error correlation is likely to result in unexpected errors when assimilating observations particularly from satellites. This study examines will examine how important this can be for determining ionospheric electron density distribution.

Here, the location-dependent correlation is designed by separating it into two parts: the vertical correlation and the horizontal correlation, and by using the EOFs to represent these correlations. First, we compute EOFs from the 62 different IRI ionospheric electron density distributions, **Ne**, by using the singular value decomposition. This is the same ensemble of IRI outputs used for calculating the variance. The electron density

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profiles are decomposed to 3 EOFs and their coefficients at each longitude and latitude location as in Eq. (3).

$$\mathbf{Ne}^{(k)}(v) = \sum_{m=1}^3 \mathbf{a}_{v_m}^{(k)} \Psi_{v_m}(v) \quad (3)$$

where $\mathbf{Ne}^{(k)}$ is k th sample of the IRI electron density profiles ($k = 1, \dots, 62$), v is the given altitude location, Ψ_v is a matrix that contains the EOFs for the vertical direction, and $\mathbf{a}_v$ is a vector of the vertical EOF coefficients. After determining the EOFs at each longitude and latitude location, the covariance of the EOF coefficients is computed from 62 sets, and then multiplied by the EOFs as in Eq. (2) to obtain the vertical covariance function $\mathbf{C}_v$.

$$\mathbf{C}_v = \Psi_v \text{cov}(\mathbf{a}_v, \mathbf{a}_v^T) \Psi_v^T \quad (4)$$

where cov means the sample covariance, $\mathbf{a}_v^T$ and Ψ_v^T are the transpose of $\mathbf{a}_v$ and Ψ_v . The vertical correlation $\mathbf{Corr}_v$ can then be obtained after normalization and localization as in Eq. (5),

$$\mathbf{Corr}_{v_{i,j}} = \left(\frac{\mathbf{C}_{v_{i,j}}}{\sqrt{\mathbf{C}_{v_{i,j}}} \sqrt{\mathbf{C}_{v_{i,j}}}} \right) \circ \xi_{i,j} \quad (5)$$

where i and j are the element indices in the covariance matrix, ξ is the localization (i.e., tapering) function and $\circ$ refers to an operation for the element by element multiplication. Localization is used to ameliorate effects of spurious correlations due to sampling errors. The Gaspari and Cohn function (Gaspari and Cohn, 1999) is used for the localization.

Figure 1a shows the vertical EOFs at a given longitude and latitude location. The location-independent vertical correlation (Fig. 1b) illustrates that the correlation is identical at every altitude, as calculated by using the same Gaussian function, while the

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location-dependent vertical correlation (Fig. 1c) shows that the vertical correlation is different at different altitudes. The vertical correlation at low altitude (below 150 km) is higher with lower altitude locations, but is lower with higher altitude locations. The vertical correlation at high altitude (above 150 km) is, on the other hand, higher with higher altitude locations, but is lower with lower altitudes. This result suggests that the vertical correlation is strongly dependent on altitude locations. Since the vertical correlation is determined from the IRI empirical model outputs, rather than real observations, the vertical correlation used here is not free of errors when assimilating the real data. The length scale of localization function for altitude changes at different altitudes to reflect the vertical correlation length scale, which varies considerably with altitude.

The idea of calculating the horizontal correlation, the second part of location-dependent correlation, is similar to the vertical correlation. The k th horizontal map of IRI electron density at a given altitude, ν , is decomposed to 3 EOFs and its coefficients as shown by Eq. (6).

$$\mathbf{Ne}^{(k)}(h) = \sum_{m=1}^3 \mathbf{a}_{h_m}^{(k)} \Psi_{h_m}(h) \quad (6)$$

where h is the given horizontal (longitude and latitude) location, Ψ_h is a matrix of the EOFs for the electron density on horizontal surface, and $\mathbf{a}_h$ is a vector of the horizontal EOF coefficients. After decomposing the total of 62 maps into 3 EOFs and their coefficient, the covariance of the EOF coefficient is computed and then multiplied by the EOFs to convert it to the covariance of electron density on a grid, as in Eq. (7). The horizontal covariance $\mathbf{C}_h$ is given by

$$\mathbf{C}_h = \Psi_h \text{cov}(\mathbf{a}_h, \mathbf{a}_h^T) \Psi_h^T \quad (7)$$

where the $\mathbf{a}_h^T$ and Ψ_h^T are the transpose matrixes of $\mathbf{a}_h$ and Ψ_h .

The horizontal correlation is obtained after normalization and localization as in Eq. (6); this step is the same as calculating the vertical correlation.

$$\text{Corr}_{h_{i,j}} = \left(\frac{C_{h_{i,j}}}{\sqrt{C_{h_{i,j}}} \sqrt{C_{h_{i,j}}}} \right) \circ \xi_{i,j} \quad (8)$$

The length scale of localization for longitude and latitude is 3° . Figure 2a and b display the location-independent and dependent horizontal correlations at longitude -122° , latitude 32° , and Fig. 2c and d displays the location-independent and dependent horizontal correlations at another location, longitude -82° , latitude 48° . As suggested by the fact that the horizontal correlation obtained from IRI empirical model outputs vary with location significantly, the location-dependent correlation information needs to be accounted for in the data assimilation scheme to successfully assimilate the real observations. As indicated by the blue circle in Fig. 2b and d, the extent of horizontal correlation is localized by the Gaspari and Cohn function to minimize the effect of spurious correlations resulting from the sampling error. The location-dependent type of the background model error covariance is modeled by multiplying the location-dependent vertical correlation, location-dependent horizontal correlation, and model variance, as shown in Eq. (9).

$$\mathbf{P} = \text{Var}_{i,j} \circ \text{Corr}_{h_{i,j}} \circ \text{Corr}_{v_{i,j}} \quad (9)$$

The advantage of modeling the background model error covariance in this manner is not only getting the variance, but also the vertical and horizontal correlation of ionospheric electron density distribution varying according to its locations and geophysical conditions (e.g., day and night). The disadvantage is that it requires more computing time and memory than utilizing location-independent (i.e., stationary) correlation in the assimilation scheme. This issue can be coped with by pre-computing the EOFs and the EOF coefficients covariance in advance and by adopting space matrix methods.

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4 Assimilation experiments with synthetic data

The OSSEs, in which synthetically generated observations sampled from the IRI model output (i.e., the simulation truth) are assimilated, provide the assessment of the data assimilation (DA) procedure under idealistic conditions. A total of six different OSSEs have been conducted to examine the effects of different types of background model error covariance on the assimilation analysis quality. The simulation results are shown for the North American continent at 00:00 UT on 5 February 2008 (Fig. 3). Note that the simulation truth and the background model states are different in the OSSEs presented here. The simulation truth is calculated from IRI with the lower IG index rather than the real IG index. This parameter setting makes synthetically generated observations of electron density lower than the climatological prediction by IRI in an effort to account for the tendency of IRI to overestimate the TEC during the extreme solar minimum conditions. Two different kinds of TEC data are considered in the OSSEs: ground-based GPS data and F3/C occultation data.

Figure 3a displays the distributions of observations used in these experiments: ground-based GPS station (black point) and F3/C occultation TEC path (red line). Six different experiment settings are as follows: (1) location-independent background model error covariance with synthetic ground-based GPS data (Fig. 3b), (2) location-independent background model error covariance with synthetic F3/C RO data (Fig. 3c), (3) location-independent background model error covariance with both ground-based and F3/C RO data (Fig. 3d), (4) location-dependent background model error covariance with synthetic ground-based GPS data (Fig. 3b), (5) location-dependent background model error covariance with synthetic F3/C RO data (Fig. 3c), and (6) location-dependent background model error covariance with both ground-based and F3/C RO data (Fig. 3d). The OSSE results are shown at longitude -100° and at latitude 44° to compare the vertical structures of assimilation analyses. Figure 3b and c compares electron density profiles from the IRI background model, the simulation truth, and data assimilation results for ground-based GPS data and F3/C RO data, respectively. The

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comparison suggests that assimilation results obtained using location-independent and location-dependent background model error covariance are both close to the simulation truth when assimilating ground-based GPS data. For assimilation of the F3/C RO data, on the other hand, a choice of the background model error covariance type makes a considerable difference. The electron density profile obtained using the location-independent covariance lies significantly away from the simulation truth and almost next to the background electron density. Figure 3d illustrates the OSSE electron density profile results for assimilation of both ground-based GPS data and F3/C RO data. The updated electron density profile using the location-dependent background model error covariance compares with the simulation truth far better than the one using location-independent model error covariance. The OSSE results suggest that the location-dependent background model error covariance effectively facilitates the assimilation of ground-based GPS and F3/C RO data independently, and of both simultaneously. In assimilation examples shown in the following sections, the location-dependent background model error covariance is used.

5 Assimilation results: TEC maps

We have conducted several data assimilation experiments over the CONUS with real ground-based GPS and F3/C RO TEC data on 21 October 2008. Assimilation results are presented as total electron content, which is the column-integrated electron density from 80 to 1000 km. Results are compared to the background model TEC to examine the impact of F3/C RO data as well as ground-based GPS data. Figures 4 and 5 show TEC maps for the daytime (14:00–21:00 UT) and nighttime (02:00–09:00 UT) on 21 October 2008. At each UT, 3 TEC maps are shown: a DA TEC map using ground-based GPS data, an IRI background TEC map, and a DA TEC map using both ground-based GPS and F3/C RO data. It is clear that both types of data can modify the climatological TEC distribution predicted by the IRI successfully. Through comparison of two DA TEC maps, the influence of F3/C RO data is evident, particularly over the ocean where

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ground-based GPS stations are absent. For instance, see the TEC maps at 02:00 UT in Fig. 5, in which TEC have been updated over the ocean thanks to F3/C RO data. Our data assimilation system can assimilate effectively both space-based and ground-based GPS observations in the daytime and nighttime.

6 Validation with ISR data

The use of the location-dependent background model error covariance in the data assimilation scheme is essential when assimilating both ground-based GPS and F3/C RO data as suggested by the OSSE experiments. The accuracy of the data assimilation model must now be validated in terms of its ability to assimilate the real observation data. Here, the Millstone Hill incoherent scatter radar data are used to validate electron density profiles obtained from the assimilation of real ground-based GPS and F3/C RO data. Figure 6 displays the profiles at each 15 min. interval between 16:00 UT and 17:45 UT on 21 October 2008. Shown are the background model IRI (black), the data assimilation result (red is the DA electron density located at Millstone Hill; red dashed line is the DA electron density assimilating only ground-based GPS data), and the Millstone Hill data and its error bar (blue). The data assimilation results are obtained every 15 min. The displayed incoherent scatter radar profile is the median value over 15 min. The altitude grids where F3/C RO paths intersect with the ISR line-of-sight are indicated by green boxes, at 16:15 UT, 16:45 UT, and 17:45 UT. The F3/C RO paths pass through at different altitude regions over Millstone Hill over this period; they pass through the E region and F region at 16:15 UT, and between 500 km to 800 km altitude at 16:45 UT and 17:45 UT. In these three time periods the data assimilation result agrees well with ISR electron density. When no F3/C RO data are assimilated in addition to ground-based GPS data, the agreement of DA and ISR electron density profiles is considerably poorer.

The F3/C electron density profile calculated from the Abel inversion (obtained from CDAAC) can also be compared to our data assimilation analysis. The comparison is

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presented for 16:15 UT on 21 October 2008 when the RO path is located closed to Millstone Hill. Figure 7a displays the 3-D observing geometry of Millstone Hill ISR (blue) and F3/C RO (red), and the TEC map from the DA result is shown on the longitude-latitude plane at the bottom. Figure 7b compares vertical electron density profiles from the ISR and data assimilation analysis at the Millstone Hill location. The ISR error bar plotted along the ISR profile, suggests high measurement uncertainty in the upper portion of the profile. The data assimilation electron density profile agrees well with ISR from altitude 200 km to 400 km, where the ISR error is relatively small, including $hmF2$ and $NmF2$ values. Figure 7c compares the Abel-inversion retrieval of electron density profile (black) with the data assimilation result (red) along the RO tangent point (i.e., red line in Fig. 7a). The $hmF2$ from data assimilation results is estimated to be slightly higher than the Abel inversion result, while the $NmF2$ is estimated to be lower.

7 Discussion

In this study, we develop a new background model error covariance model to account for spatially variable correlation patterns of the model errors. Even though the location-dependent covariance model reflects more realistic correlations, the OSSE results indicate that both location-independent and location-dependent covariance works equally well for assimilation of ground-based GPS data. See Fig. 3b where electron density profiles obtained by using both types of the covariance models are shown to produce similar results and compare well with the simulation truth. This result suggests that the vertical and horizontal error correlation might not have significant importance when assimilating the ground-based GPS TEC. Since the radio signal is transmitted from GPS satellites to ground-based receivers, the ground-based GPS TEC data tend to contain more information about the horizontal ionospheric structure and less about the vertical ionospheric structure. Vertical correlation in the background model error covariance is rather irrelevant in inverting the ground-based GPS TEC data since they are a nearly vertically integrated quantity. Moreover, the horizontal extent of ground-based GPS

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observations is mostly limited in the vicinity of ground-based stations, and therefore the long-range horizontal correlation does not play a significant role either.

RO TEC values are computed from radio signals transmitted from GPS satellites to LEO satellites that pass through the ionosphere at different altitudes over extensively large horizontal areas, and F3/C RO data can thus provide vertically resolved ionospheric information. To invert RO TEC data accurately, the vertical and horizontal correlation in the background model error covariance needs to be realistic. The OSSE results presented in Fig. 3c demonstrate this point, showing that electron density profiles obtained using a more realistic covariance model are closer to the simulation truth. When assimilating the F3/C RO data, it is therefore important that the background model error covariance reflects realistic location-dependent correlation structures.

The accuracy of the background model error covariance affects the quality of data assimilation analyses, especially when assimilating different kinds of GPS data. The OSSE results shown in Fig. 3d, obtained from assimilation of ground-based and RO synthetic data, illustrate this point clearly. Electron density profiles estimated by using the location-dependent error covariance are closer to the simulation truth in comparison to the cases with the location-independent error covariance. Even though the OSSE electron density profiles obtained by using the location-independent error covariance is reasonable for assimilating ground-based GPS data alone. The results are deteriorated when assimilating the same data in addition to the RO data. These detailed comparisons suggest that the choice of the background model error covariance needs to be suitable for all types of GPS data being assimilated; otherwise the accuracy of data assimilation analysis would not be optimal.

To validate the electron density profiles, the DA results are evaluated and compared to the Millstone Hill ISR data from 16:00 UT to 17:45 UT at every 15 min. interval on 21 October 2008. Both ground-based GPS and F3/C observations are located closed to the ISR at three intervals: 16:15 UT, 16:45 UT, and 17:45 UT. At other time intervals, only ground-based GPS data are available. DA results agree poorly with ISR data when only ground-based GPS data are assimilated. Since the ground-based GPS data

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contain little information about the vertical ionospheric structure, assimilating ground-based GPS data alone will not modify the vertical structure predicted by the background model. On the other hand, the results from assimilation of both ground-based GPS and F3/C RO TEC agree better with the ISR electron density profile in the F region at (16:15 UT) and at high altitude from 500 km to 800 km (16:45 UT and 17:45 UT). The validation with the ISR data supports our premise that our data assimilation procedure with the location-dependent background model error covariance effectively reconstructs the 3-D electron density from both ground-based GPS and F3/C RO data.

The tangent points of the F3/C are aligned with the Millstone Hill ISR line-of-sight at 16:15 UT on 21 October 2008, when the DA results compare well with the ISR electron density profile. The comparison of our DA results with the ISR electron density profile and with the profile retrieved from the F3/C using the Abel inversion is shown in Fig. 7b and c, respectively. This comparison reflects the respective observing geometry of ISR and F3/C RO techniques, since the later one is slightly veered from vertical. The DA electron density profile agrees well with the ISR data from altitude 200 km to 400 km, where the ISR error is relatively small, including $hmF2$ and $NmF2$ values. In comparison with the Abel inversion result, the $hmF2$ is estimated to be slightly higher, while the $NmF2$ is estimated to be lower. Below altitude 150 km, the Abel inversion yields unphysical negative electron density value. Liu et al. (2010) have shown that electron density profiles obtained by the Abel inversion are prone to a large amount of error below about 200 km. With the help of regularization though the background model error covariance in the Kalman filter, electron density profiles resulting from our data assimilation procedure are more robust than the Abel inversion results.

The ground-based GPS technique can provide valuable continual monitoring of the ionosphere, but its spatial coverage is regional. To achieve global monitoring of the ionosphere, including the oceans and remote regions where it is difficult to deploy ground-based stations, space-based observing techniques like the F3/C are crucial. TEC maps, shown in Figs. 4 and 5 for both daytime and nighttime, demonstrate this point. Because of its spatially limited observing geometry, the ground-based GPS

observation can modify the background ionosphere horizontal structure only in the vicinity of station locations. On the other hand, the space-based GPS technique can provide greater spatial coverage because RO paths pass through the ionosphere rather horizontally. Data assimilation approaches, such as the one presented here, can take advantage of both observing techniques to improve the global ionospheric specification. In addition, the TEC maps display the feature akin to the plasmaspheric tail (ionospheric plume) at 20:00 UT (Fig. 4) (Foster et al., 2002). The similar plasmaspheric tail signature is shown in both assimilation results but is not seen in the background model. Our data assimilation procedure has the capability to reconstruct realistic transient ionospheric features, such as plasmaspheric tails, that are absent in IRI. Resulting assimilation analyses can be used for storm time studies to identify the plasmaspheric foot points in the ionosphere.

8 Conclusions

In this study, we presented a new approach to assimilate F3/C Radio Occultation (RO) data as well as ground-based GPS data into the background model International Reference Ionosphere (IRI) and examined the impact of RO data on the reconstructed 3-D ionospheric electron density structure. Unlike the current US-TEC, which solves Kalman filter equations with respect to EOF coefficients, we developed a new data assimilation procedure in which the Kalman filter equations are solved in terms of grid-point electron density in order to accommodate a more flexible regularization strategy. Four main conclusions were drawn from our results.

The first conclusion is, as illustrated by the OSSE experiment results, that the location-dependent model error covariance facilitated inverting both ground-based GPS and F3/C RO TEC data independently, and that it is a key to successfully assimilating both data at the same time. This conclusion was drawn from demonstrating the limitation of the location-independent covariance model (based on the Gaussian function) for the assimilation of RO observational data, and developing a new covariance

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model whose correlation structures depend on longitude, latitude, and altitude location. The location-dependent covariance model was constructed by representing vertical and horizontal correlations with EOFs and their coefficients as shown in Figs. 1 and 2. OSSE experiments with the location-independent model error covariance showed that results were satisfactory for ground-based GPS data assimilation, but the OSSE result assimilating F3/C RO TEC does not agree well with the simulation truth. Therefore, the OSSE result illustrated that the location-dependent model error covariance worked well with both datasets separately, and even better assimilating both simultaneously.

Second, we validated assimilation analyses using Millstone Hill ISR data and concluded that assimilation of ground-based and RO data using our new procedure improved the agreement with ISR electron density profiles. This was true particularly when F3/C RO data are present in the vicinity of Millstone Hill, since the DA scheme is able to correct altitude structures quite well.

The third conclusion is that our scheme can produce a more robust profile than the Abel inversion thanks to regularization though the use of more realistic background model error covariance in the Kalman filter update equation. This point was demonstrated by sampling our DA results along the RO tangent points, and comparing them with F3/C RO electron density profiles calculated from the Abel inversion, as shown in Fig. 7 for the Millstone Hill location. Our DA results are generally similar to the Abel inversion results, but importantly, our scheme was able to produce more robust profiles due to an improved regularization in inversion methods.

Our final conclusion is that the F3/C RO could improve the electron density results over greater areas, including oceans and remote regions where no ground-based stations exist. Furthermore, the F3/C RO data has the potential to improve the altitude structures of DA analysis. For the F3/C mission, 1000 ~ 2500 RO events per day (3000 at maximum) have occurred, however the current RO global coverage is not complete at a given time. This should be greatly improved when the FORMOSAT-7/COSMIC-2 (F7/C2), with twelve micro satellites, will be launched in 2016 and 2018. Each micro satellite will be equipped with the appropriate satellite signal receiver to conduct the

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RO experiment with GNSS and GLONASS. This new mission is expected to yield more than 14 000 RO events per day. By assimilating F7/C2 RO data into our data assimilation model, the global ionosphere specification will be significantly improved. Our new DA procedure can also be incorporated into the NOAA/SWPC ionospheric assimilation model US-TEC to increase the assimilation analysis accuracy. With the expanded availability of RO data, the electron density distribution analysis will be improved over greater regions including areas where ground-based GPS stations are absent, and the approach presented in this paper supports such future prospects.

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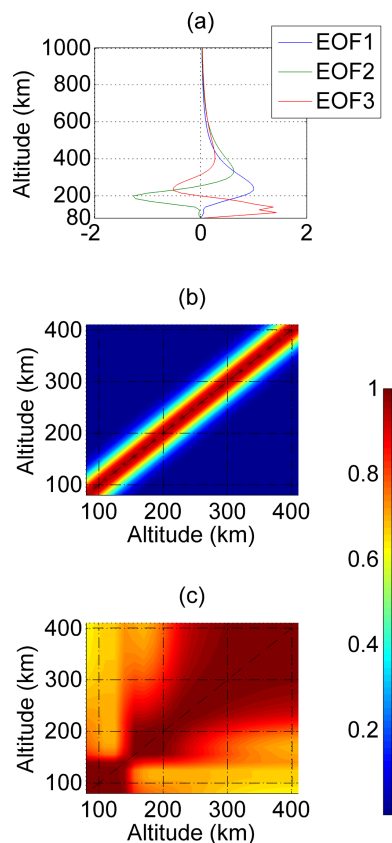


Fig. 1. The vertical correlation at Longitude -122° and Latitude 28° . **(a)** The EOFs calculated from 62 IRI Ne profiles with different sunspot numbers and IG indexes. **(b)** The location-independent vertical correlation modeled with a Gaussian function. **(c)** The location-dependent vertical correlation obtained from EOFs and its coefficients.

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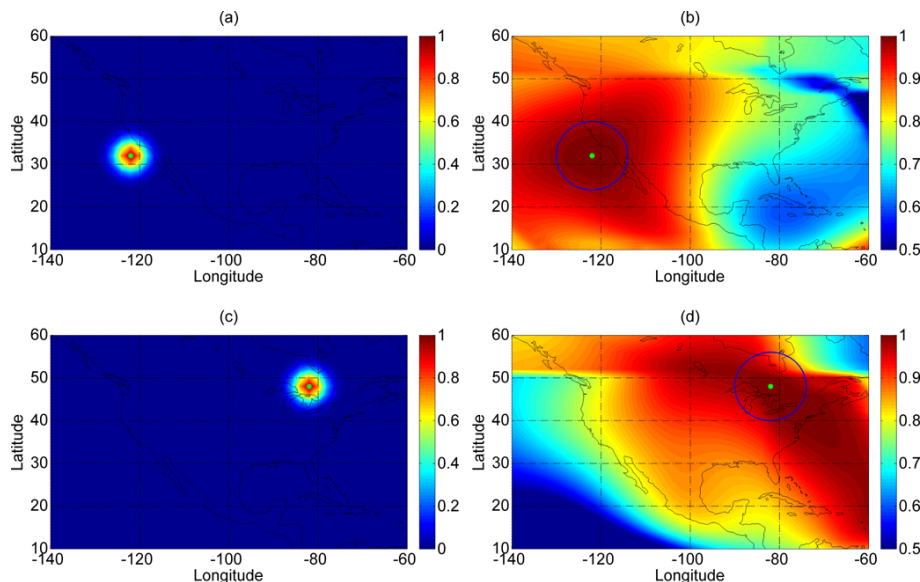


Fig. 2. The horizontal correlation at 00:00 UT. **(a)** The location-independent horizontal correlation modeled using a Gaussian function at altitude 200 km with respect to a grid point at longitude -122° and latitude 32° marked by the green dot. **(b)** The location-dependent horizontal correlation modeled with the horizontal EOF profiles and its EOF coefficients' covariance for the same reference point as **(a)**. The blue circle surrounding the dot is the full-length of the Gaspari and Cohn localization function, with which the correlation is tapered towards zero from the center (green dot) to the rim of the blue circle. **(c)** The location-independent horizontal correlation at altitude 200 km with respect to a point at longitude -82° and latitude 48° . **(d)** The location-dependent horizontal correlation for the same reference point as **(c)**.

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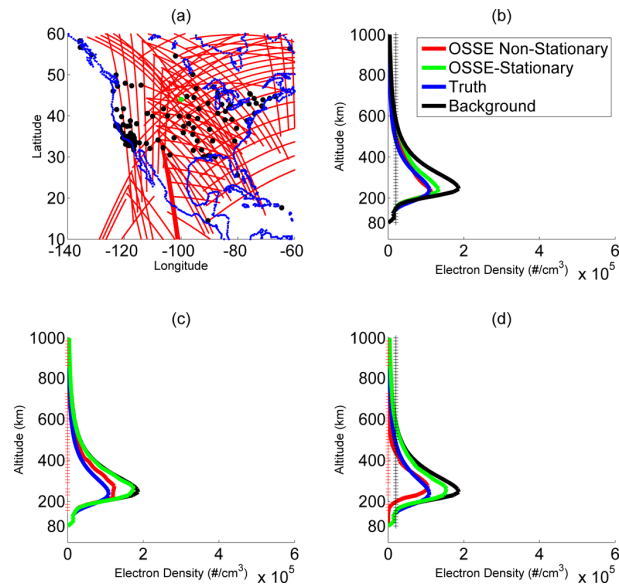


Fig. 3. The OSSE result of the data assimilation model for 00:00 UT on 5 February 2008. **(a)** The F3/C RO TEC paths of assimilated observations are shown as the red line, the black points are the ground-based GPS stations used in the OSSE. The green dot indicates a location where electron density profiles are sampled for comparison and validation. **(b)** The electron density profiles are sampled from OSSE DA results obtained by assimilating the synthetic ground-based GPS data, which is integrated from the OSSE truth with different covariance models. The red line indicates the OSSE DA result with a location-dependent model error covariance (computed from EOFs), the green line is the OSSE DA result with a location-independent model error covariance (Gaussian), the blue line is the OSSE truth, and the black line is the background model. **(c)** Is the same as **(b)**, but OSSE DA results are obtained by assimilating the synthetic F3/C data. **(d)** Is the same as **(b)**, but OSSE DA results assimilated the synthetic data obtained from ground-based GPS and F3/C data. *Note:* the plus symbols indicate altitudes where TEC paths pass through this validation location, where the red color is used for F3/C and the black color is for ground-based GPS data.

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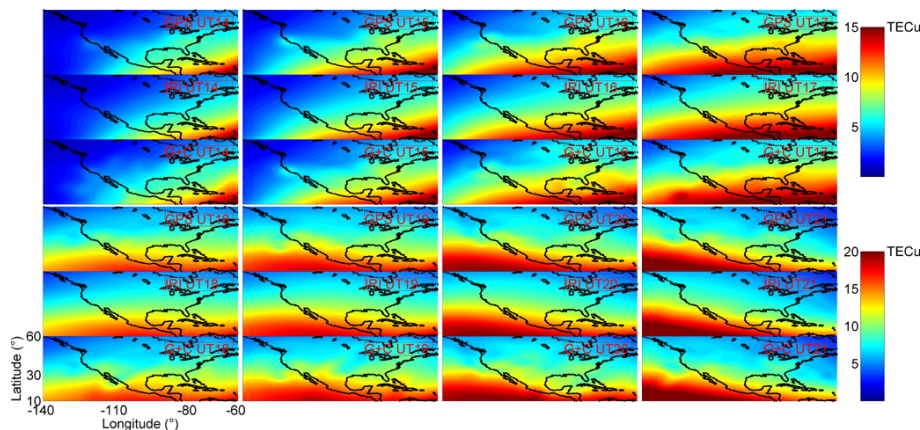


Fig. 4. The DA and background model IRI TEC map of the North American Continent at daytime 14:00–17:00 UT (top 3 rows) and 18:00–21:00 UT (bottom 3 rows). Each time period has 3 different TEC maps, including a DA TEC map using ground-based GPS data, an IRI TEC map, and a DA TEC map using ground-based GPS and F3/C RO data.

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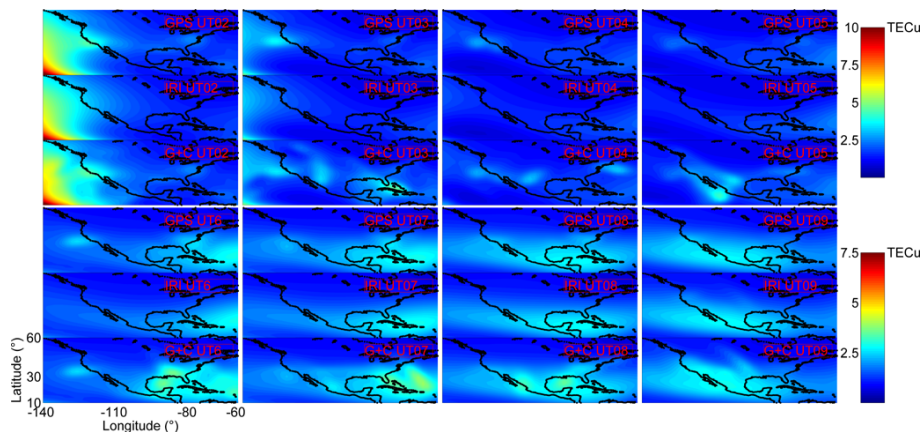


Fig. 5. The DA and background model IRI TEC map of the North American Continent at night-time 02:00–05:00 UT (top 3 rows) and 06:00–09:00 UT (bottom 3 rows). Each time period has 3 different TEC maps, including a DA TEC map using ground-based GPS data, an IRI TEC map, and a DA TEC map using ground-based GPS and F3/C RO data.

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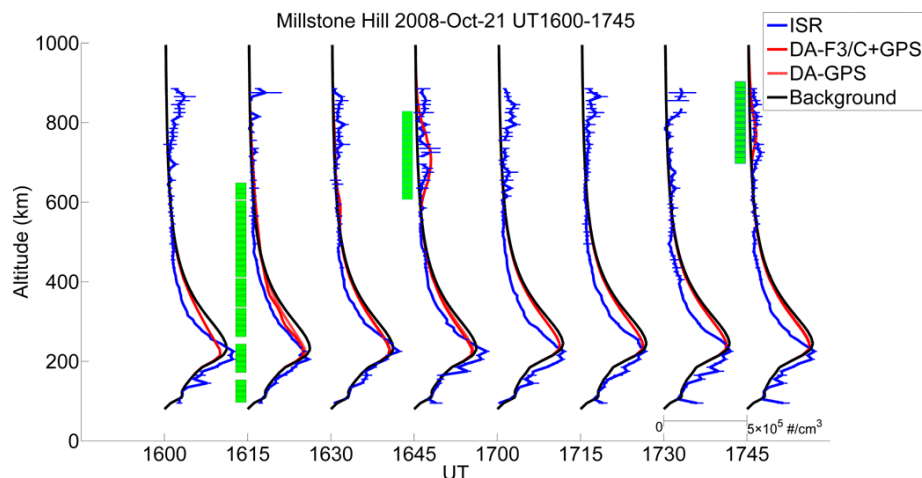


Fig. 6. Comparison of data assimilation results and Millstone Hill incoherent scatter radar observations from 16:00 UT to 17:45 UT, with a time period of 15 min. The red line is the DA electron density located at Millstone Hill and the red dashed line is the DA electron density assimilating only ground-based GPS data, while the black line is the background of the DA model. The blue line is the observation and error bars of Millstone Hill incoherent scatter radar. The green boxes indicate that the altitude had F3/C RO passing through.

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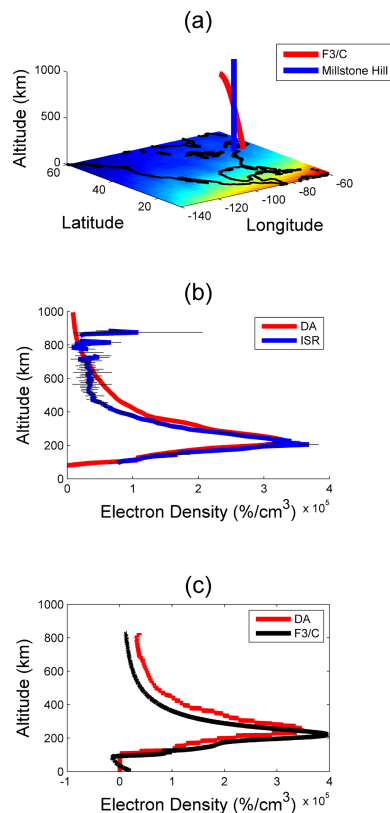


Fig. 7. The comparison of the data assimilation results, Millstone Hill incoherent scatter radar observation, and F3/C electron density profile from the Abel inversion. **(a)** The location of F3/C RO tangent point electron density profile (red) and the location of Millstone Hill observation electron density profile (blue). **(b)** The electron density profile of DA (red), ISR (blue) and ISR's error bars (black) over Millstone Hill. **(c)** The electron density profile of DA (red) and F3/C (black) along the RO tangent point.

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