



**Investigating bias in
the application of
curve fitting
programs**

P. A. Pickers and
A. C. Manning

This discussion paper is/has been under review for the journal Atmospheric Measurement Techniques (AMT). Please refer to the corresponding final paper in AMT if available.

Investigating bias in the application of curve fitting programs to atmospheric time series

P. A. Pickers and A. C. Manning

Centre for Ocean and Atmospheric Sciences, School of Environmental Sciences,
University of East Anglia, Norwich, NR4 7TJ, UK

Received: 31 May 2014 – Accepted: 19 June 2014 – Published: 16 July 2014

Correspondence to: P. A. Pickers (p.pickers@uea.ac.uk)

Published by Copernicus Publications on behalf of the European Geosciences Union.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Abstract

The decomposition of an atmospheric time series into its constituent parts is an essential tool for identifying and isolating variations of interest from a data set, and is widely used to obtain information about sources, sinks and trends in climatically important gases. Such procedures involve fitting appropriate mathematical functions to the data, however, it has been demonstrated that the application of such curve fitting procedures can introduce bias, and thus influence the scientific interpretation of the data sets. We investigate the potential for bias associated with the application of three curve fitting programs, known as HPspline, CCGCRV and STL, using CO₂, CH₄ and O₃ data from three atmospheric monitoring field stations. These three curve fitting programs are widely used within the greenhouse gas measurement community to analyse atmospheric time series, but have not previously been compared extensively.

The programs were rigorously tested for their ability to accurately represent the salient features of atmospheric time series, their ability to cope with outliers and gaps in the data, and for sensitivity to the values used for the input parameters needed for each program. We find that the programs can produce significantly different curve fits, and these curve fits can be dependent on the input parameters selected. There are notable differences between the results produced by the three programs for many of the decomposed components of the time series, such as the representation of seasonal cycle characteristics and the long-term growth rate. The programs also vary significantly in their response to gaps and outliers in the time series. Overall, we found that none of the three programs were superior, and that each program had its strengths and weaknesses. Thus, we provide a list of recommendations on the appropriate use of these three curve fitting programs for certain types of data sets, and for certain types of analyses and applications. In addition, we recommend that sensitivity tests are performed in any study using curve fitting programs, to ensure that results are not unduly influenced by the input smoothing parameters chosen.

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



isolate and extract the variation of interest from the complete data set (Martin and Diaz, 1991). For example, an examination of trends in the amplitude of the CO₂ seasonal cycle (e.g. Chan and Wong, 1990) requires the seasonal component to be separated from any long-term trend and irregular variations, a technique known as time series decomposition (Pierce, 1979; Theodosiou, 2011).

The analysis of atmospheric time series is often a complex process because the data are usually highly auto-correlated and consist of periodic and irregular variations on both long and short time-scales. Additionally, mechanical failure of the instruments or down-time for other reasons can result in gaps in the time series, so that data are not always spaced at regular time intervals (Trivett et al., 1989). For these reasons, simple curve fitting procedures, such as moving averages and cubic splines, are generally inadequate for the analysis of atmospheric time series, which has led to the development of more sophisticated fitting procedures (Trivett et al., 1989).

It has been recognised previously that the application of a particular curve fitting program in the analysis or decomposition of an atmospheric time series may introduce biases that could significantly influence the results and conclusions of an investigation (Nakazawa et al., 1997; Tans et al., 1989). Thus, scientific conclusions drawn from time series analyses may depend not only on the atmospheric measurements themselves, but also on the curve fitting program used. Consequently, it has been recommended that more than one curve fitting program is employed in any given time series study, so that possible biases can be identified (Nakazawa et al., 1997).

Despite this recommendation, the vast majority of studies and published papers involving time series analysis of atmospheric greenhouse gas data appear to rely on a single curve fitting program for extracting information from the data. For example, Bacastow (1976) found a correlation between the Southern Oscillation Index (SOI) and the residual variation (i.e. any remaining variation left in a data set, once the long-term trend and seasonal variation have been removed) from both the South Pole and Mauna Loa CO₂ data sets; the correlation found in this study has formed the foundation of numerous subsequent studies (e.g. Reichenau and Esser, 2003; Jones et al.,

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

2001), and yet is contingent on the results from a single parametric curve fitting program. Keeling and Shertz (1992) inferred the long-term rate of decline in atmospheric O_2 mole fraction based on the application of the same curve fitting program used by Bacastow (1976). Piao et al. (2008) suggested that the Northern Hemisphere terrestrial biosphere may be sequestering less carbon than previously thought, due to an increase in carbon losses during autumn, resulting from the strong dependence of respiration to rising temperatures; this conclusion was drawn from de-trended atmospheric CO_2 data derived using a single digital filtering program (Thoning et al., 1989). More recently, Minejima et al. (2012) investigated the origin of pollution events at a Japanese island site that were identified from de-trended atmospheric O_2 and CO_2 data using the Thoning et al. (1989) program only.

Our intention in this paper is not to dispute the science underpinning any of the above or other studies, but rather to highlight the absence of any assessment of the suitability of the curve fitting program used in many applications. The uncertainty associated with relying on a single curve fitting program appears not to have been investigated or quantified in any of the studies cited above; hence, it is not known if the results might have been biased by the curve fitting program employed.

The scientific import of relying on a single curve fitting program is that many studies present results showing very small trends that are barely discernable amongst the “noise” of the data. This may explain why some studies have come to contradictory conclusions; for example, Chan and Wong (1990) and Keeling et al. (1996) disagree regarding the direction of the trend in the atmospheric CO_2 seasonal cycle amplitude at Alert, Canada, and Enting (1987) and Thoning et al. (1989) reach opposite conclusions regarding correlations between the magnitude of CO_2 seasonal maxima in spring and the magnitude of seasonal minima the following autumn.

There are only a few studies that have investigated the uncertainty associated with curve fitting analyses, or compared two or more programs on the same time series. To our knowledge, the first two such investigations (Tans et al., 1989; Trivett et al., 1989) were prompted by a NOAA (National Oceanic and Atmospheric Administration, USA)

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



and UN WMO (United Nations World Meteorological Organization) funded meeting in March 1988 on the treatment and data processing techniques used for CO₂ time series (Elliott, 1989). Both of these studies, however, provided only a preliminary assessment of the differences between some curve fitting procedures rather than an in-depth analysis. For example, although Tans et al. (1989) compared six different curve fitting procedures, they were only applied to 3 year CO₂ flask sample data sets from a single station. In Trivett et al. (1989), the discussion on the differences found between two curve fitting programs is very brief, simply stating that the seasonal cycle outputs are comparable between the two curve fitting programs, and that the “forward step-wise multiple linear regression” curve fitting program used by the authors had limitations, such as sensitivity to outliers.

A more comprehensive analysis is presented by Nakazawa et al. (1997) who compared a digital filtering program, developed at Tohoku University, Japan, and a harmonic regression program. The authors emphasised the importance of using more than one curve fitting program in analyses of atmospheric time series, stating that an assessment of the global carbon cycle using one program could be quite different from that derived using the same data but a different program (Nakazawa et al., 1997).

Since the study by Nakazawa et al. (1997), there is no evidence in the published literature of subsequent work on curve fitting bias, either by Nakazawa and colleagues, or by other authors. Furthermore, the vast majority of studies and published papers involving time series analysis of atmospheric greenhouse gas data have continued to infer scientific conclusions from atmospheric greenhouse gas measurements based on analyses using a single curve fitting program.

Small trends in atmospheric greenhouse gas mole fraction time series can have significant consequences for the Earth system, and therefore may have substantial implications for climate change policy. Given the political and socioeconomic implications of climate change and public interest in high profile climate science publications, it is essential to ensure that information and conclusions inferred from atmospheric time

series are reproducible using a number of techniques, and are not exaggerated or attenuated by artefacts or biases of the curve fitting programs used.

The general lack of investigation into uncertainty and bias associated with using a single curve fitting program is surprising, considering their widespread use in atmospheric research over the past 30 years or so. In addition, it is unlikely that a single curve fitting program can adequately represent all atmospheric greenhouse gas mole fraction time series; in other words, a given curve fitting program may be better suited to examine data sets with particular characteristics, or for particular types of analyses. The objective of our paper, therefore, is to contribute to addressing the lack of consideration of curve fitting bias in analyses of atmospheric time series, by comparing the outputs from three widely used curve fitting programs, applied to atmospheric time series displaying diverse characteristics.

1.1 Aims and outline of paper

In this paper we investigate bias associated with the application of three curve fitting programs, known as HPspline, CCGCRV, and STL, that are widely used within the atmospheric greenhouse gas measurement community and have not been extensively compared previously. Specifically, we assess the performance of each program with respect to the complete curve fit, representation of the long-term trend and the growth rate in the long-term trend, representation of the seasonal cycle, vulnerability to gaps and outliers in the data, and sensitivity to the input parameter settings of the programs.

We emphasise that the purpose of employing curve fitting programs to atmospheric time series is not to produce a fit that passes through the most number of data points as possible, but to extract the salient features of interest, such as seasonality, and separate these components from anomalous “noise” or other features within the time series. Thus, our objective is not to determine which of the three curve fitting programs examined is “best”, but rather to elucidate differences in the output from each program when given the same input data sets. In addition, we assess whether any of the three programs are better suited to time series exhibiting particular “characteristics”, for

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



the late 1980s. The version of CCGCRV used in this study was written in Interactive Data Language (IDL) by Paul Krummel (Marine and Atmospheric Research Group, Commonwealth Scientific and Industrial Research Organisation (CSIRO), Australia).

Approximations of the seasonal cycle and the long-term trend variation are made by fitting a polynomial equation combined with a harmonic function:

$$C(t) = a_0 + a_1t + a_2t^2 + \dots + a_{(n-1)}t^{(n-1)} + \sum_{k=1}^h m_k [\sin(2\pi kt + \varphi_k)] \quad (4)$$

where t is time in years, n is the number of polynomial terms (typically three), $a_0, a_1, \dots, a_{(n-1)}$ are constants, h represents the number of harmonics in the function (typically four), and m_k and φ_k define the magnitude and phase of each sinusoidal component respectively. The fit to a data set is achieved with a linear least squares regression, applying the “LFIT” routine from Numerical Recipes in Fortran (Press et al., 1996).

The next step is to calculate the residuals of the input data to $C(t)$ and filter them using a Fast Fourier Transform (FFT) algorithm, so that short-term and interannual (long-term) variations can be retained in the fitted curve (Thoning et al., 1989). This is achieved by transforming the data from the time domain into the frequency domain using the FFT, multiplying by a low-pass digital filter to remove variations of a specified frequency (see below), and then transforming the filtered data back to the time domain using an inverse FFT (Thoning et al., 1989). The low-pass filter function used is a decreasing exponential represented as follows:

$$H(f) = \exp\left[-\ln(2) \cdot \left(\frac{f}{f_c}\right)^4\right] \quad (5)$$

where f_c is the cut-off frequency of the low-pass filter, typically expressed in days.

The low-pass filter is applied to the residuals twice, once with a short-term cut-off ($f_c = f_s$) value for smoothing the data, and once with a long-term cut-off ($f_c = f_l$) to remove any remaining seasonal oscillation and to represent interannual variations in the

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

- Step 2: the annual cycle-subseries are then smoothed by LOESS, using a first degree polynomial and q equal to the value of the seasonal smoothing window ($swin$; set by the user).
- Step 3: a low-pass moving average filter is applied, where the length of the moving average is set to the frequency of the input data series, $n_{(p)}$ (i.e. 12, for monthly time series). This is followed by a moving average with length = 3 and then with LOESS smoothing. These three moving averages result in the loss of $n_{(p)}$ data at each end of the time series; hence, the seasonal smoothing in step 2 is extended by $n_{(p)}$ positions at each end to account for this expected loss.
- Step 4: the smoothed, cycle-subseries is detrended to prevent low frequency variation from being included in the seasonal component of the decomposition.
- Step 5: a deseasonalised series is computed by subtracting the computed seasonal component from the entire time series.
- Step 6: this deseasonalised series is smoothed using LOESS with q equal to the value of the trend smoothing window ($twin$; set by the user). This produces a trend component which is used in step 1 of subsequent iterations of the inner loop.

The outer loop of STL down-weights any outliers in the data by assigning robustness weights, ρ_v , to the series using a bisquare weight function, B (Cleveland et al., 1990):

$$\rho_v = B(|R_v|/h) \quad (7)$$

where R_v is the residual component (i.e. the data with the trend and seasonal components removed) and $h = 6 \times \text{median}(|R_v|)$. In subsequent iterations of the inner loop, the neighbourhood weight, $v_i(x)$, used in the LOESS smoothing of steps 2 and 6 is multiplied by the robustness weight, ρ_v , of the preceding pass of the outer loop. For more details regarding the STL program we refer the reader to Cleveland et al. (1990).

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



When choosing values to use for the *swin* and *twin* parameters, Carslaw (2005) points out that the seasonal and trend components should not compete for the same variation in the data, and low-frequency fluctuations should be retained in the trend component and not in the remainder. In this study, unless otherwise stated, we used a *swin* value of 5 years and a *twin* value of 25 months, which are the values typically used by our international colleagues (S. Mikaloff-Fletcher, NIWA, personal communication, 2011).

A major limitation of STL is that it can only be applied to equally-spaced data with no gaps (Manning et al., 1990). Such data sets can be derived by pre-treating the original data set using an interpolation or smoothing technique, however, such interpolation techniques may create biases or artefacts in the time series, particularly if there are large gaps. In order to mitigate this limitation, all comparison tests we have carried out with the three curve fitting programs used time series consisting of monthly mean data that were already equally spaced in time, and had few or no missing values.

2.2 Time series

The three curve fitting programs described above were applied to semi-continuous atmospheric measurement data, provided by international colleagues and available to download from the World Data Centre for Greenhouse Gases (WDCGG) website at: <http://ds.data.jma.go.jp/gmd/wdogg/> (see Table 1). In order to investigate the ability of each curve fitting program to represent particular features of atmospheric time series, we selected a suite of input data sets that provide a diverse variety of seasonal and trend characteristics, and that are notable for their long duration (several decades). For example, we chose the atmospheric CO₂ data set from Alert Station, Canada (ALT), shown in Fig. 1a, because it has a relatively large seasonal cycle amplitude and a very regular but asymmetric seasonal pattern with prolonged and rounded maxima and contrasting sharp minima, which are characteristic of high northern latitude CO₂ data sets. Previous studies (e.g. Nakazawa et al., 1997; Tans et al., 1989; Trivett et al., 1989)

have found that curve fitting programs often struggle to represent the deep troughs of the seasonal minima of such time series.

Other atmospheric time series we have chosen to examine exhibit more complex seasonal patterns, for example, the ALT CH₄ data set, shown in Fig. 2a, is characterised by a double seasonal maximum during winter. In contrast, the Baring Head, New Zealand (BHD) CO₂ seasonal cycle exhibits a variable pattern, such that it can be difficult to determine seasonal cycle characteristics. This is partly because, in contrast to the ALT CO₂ data set, the BHD CO₂ seasonal cycle has a much smaller amplitude, owing to a considerably smaller terrestrial biosphere in the Southern Hemisphere. We also examine the BHD ozone (O₃) data set, which exhibits a seasonal cycle with relatively high interannual variability, in that the magnitude of the maxima and minima fluctuate significantly from year to year, although the shape of the seasonal cycle is relatively consistent. In addition to complex seasonal patterns, some of the time series were chosen because they exhibit different trend characteristics. For example, there is little variability in the growth rate of the ALT and BHD CO₂ long-term trends, whereas the ALT and Cape Grim Observatory, Australia (CGO) CH₄ long-term trend growth rates vary considerably.

As mentioned above, STL requires equally-spaced data, so we only used monthly mean time series and we interpolated the data to fill any gaps (see Table 1). Interpolation was carried out by applying HPspline to the original time series, and using values of the curve fit as surrogate data where there were missing values. Since our objective is to investigate bias associated with curve fitting programs, and not to infer scientific conclusions, interpolating missing data has not had any influence on our results and conclusions. In using monthly mean data, however, we were not able to assess the programs with respect to fitting higher frequency variations such as diurnal cycling or synoptic scale variability.

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



2.3 Experimental methods

The three curve fitting programs were tested for their ability to represent each time series as a whole, and for under-estimation and over-estimation of the curve fits at the seasonal maxima and minima. We also assessed the proportion of data “captured” by the curve fitting programs, defined as when the curve fit passes within the $\pm 1\sigma$ standard deviation uncertainties of the data. The decomposed components of the time series (i.e. seasonal, long-term trend, growth rate of the long-term trend and residual components) were also compared, and the programs were assessed for their ability to cope with outliers and gaps in the data, which were introduced artificially. Each of the programs was also tested for sensitivity to the input parameters of the fitting programs, such as the number of harmonics used in the fit. Table 2 lists the range of input parameter setting values that we have used, but to ensure the robustness of our conclusions on the behaviour of the three curve fit programs, we also tested many intermediary values of these input parameter settings. Analyses of the seasonal cycle amplitude of the detrended time series were performed using the ALT CO₂ and BHD CO₂ time series only, allowing for both Northern and Southern Hemisphere representation of the terrestrial biosphere seasonal cycle, whereas all the other curve fitting program tests were performed on all five time series.

The use of statistical analyses in the few existing atmospheric curve fitting comparison studies has been limited, with previous authors relying heavily on visual interpretation of graphical representations of the curve fit outputs in order to describe the differences between programs (e.g. Nakazawa et al., 1997; Tans et al., 1989; Trivett et al., 1989). We have attempted to employ some statistical techniques in our analysis, however, time series are complex and highly auto-correlated, which makes the use of many statistical tests redundant or inappropriate. For example, *t* tests can be used to determine if the means of two populations are significantly different, but this is somewhat meaningless when applied to an atmospheric time series, which consists of three components: a long-term trend, seasonal cycle, and residual variations. Therefore, we

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

have cautiously employed t tests in comparisons of the individual decomposed components only, such as the mean long-term trend, and also for the analysis of quantifiable seasonal characteristics, such as the mean seasonal cycle amplitude.

Carslaw (2005) states that it is difficult to assess the relative performance of different curve fitting programs, as there is no obvious point of reference against which different programs can be compared. Thus, in order to provide a robust, quantitative framework for comparing outputs from the three curve fitting programs, we have used 1σ standard deviations of the monthly mean data as an uncertainty estimate of the data, and to provide a quantitative point of reference, to which we have compared differences in the curve fitting program outputs. Differences between curve fitting program outputs that were larger than the uncertainty of the data were deemed to be significant within the context of the data set, as this indicates that the choice of one curve fitting program over another produces a difference in the given output that is greater than the uncertainty of the measured data.

3 Results and discussion

3.1 Curve fits

We first ran all three curve fitting programs on all five data sets listed in Table 1, using the input parameters shown in bold in Table 2. The differences between the three program curve fits are smallest for the BHD CO₂ and CGO CH₄ time series. These two time series are the least challenging for the programs, owing to the relatively small seasonal cycle amplitudes of the data. The largest differences between the program curve fits are for the ALT CO₂ and ALT CH₄ time series (with differences of up to 2 ppm and 15 ppb respectively), which both have relatively large seasonal cycle amplitudes, shown in Figs. 1a and 2a. Figures 1a and 2a also show that the programs produce much more similar curve fits to each other for the ALT CO₂ data than for the ALT CH₄ data, and this is likely because of the more complex seasonal pattern exhibited by CH₄

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



as mentioned in Sect. 2.3 above. Figures 1b and 2b show the residuals of the ALT CO₂ and ALT CH₄ curve fits, which are distributed around zero for all three programs, and are almost always largest for HPspline and smallest for CCGCRV for both time series.

Across all five time series, the differences between the curve fits are notably largest between HPspline and CCGCRV, and the smallest differences are either between HPspline and STL (for ALT CO₂ and BHD CO₂), or CCGCRV and STL (for ALT CH₄, BHD O₃, and CGO CH₄). The largest curve fit differences between the three programs most often coincide with the timing of the seasonal maxima and minima (as shown in the inset plots of Figs. 1a and 2a), where the curve fitting programs have a tendency to either under- or over-estimate the seasonal inflexion points. As shown in Fig. 3, the differences between the curve fits generated by the three programs are often significant because they exceed the uncertainty of the monthly mean measurements (as represented by the 1σ standard deviations of the monthly means).

Comparing how closely the programs fit to the data points can provide useful insight into the appropriate use of a curve fitting program, even though the purpose of fitting curves to atmospheric time series is not to fit as closely to the data points as possible, as mentioned previously. The curve fits from CCGCRV are consistently closest to the data points for all five time series (see Table 3). In the case of the CGO CH₄ time series, the CCGCRV curve fit is within ±1σ standard deviations for every single data point. The HPspline curve fits are the most distant from the data for all five time series; the closest agreement between the HPspline curve fit and the data is for the BHD CO₂ time series, where the curve fit captures 90 % of the data. This pattern is congruent with the residuals of the curve fits, which are smallest for CCGCRV, largest for HPspline, and intermediary for STL across all five time series (shown in Figs. 1b and 2b, for ALT CO₂ and CH₄).

It is important not to arrive at the erroneous conclusion that CCGCRV performs “better” than STL or HPspline because it produces a curve fit that is closest to the input data points. As stated previously, the purpose of applying curve fitting programs to atmospheric time series is to separate the time series into trend, seasonal and residual

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



components. By producing a curve fit that is closer to the data, CCGCRV retains more short-term variation in the seasonal and trend components of the fit, thus resulting in smaller residuals. In contrast, HPspline is much less “flexible”, meaning that the curve fits do not follow closely to the original data points as often, particularly for time series with large interannual variations in the seasonal cycle, such as the ALT CH₄ time series. Hence, for HPspline, a larger proportion of the variation in the data set is assigned to the residual component of the decomposition compared to the CCGCRV and STL decompositions. This lack of flexibility in the HPspline curve fits is attributed to the spline stiffness component of the program.

Carlsaw (2005) states that seasonality is a concept that cannot be explicitly defined, and there is no definitive boundary between what constitutes seasonal and residual variation, hence it is vulnerable to subjective interpretations. A curve fitting program that incorporates some interannual variability within the seasonal component of the fit cannot be said to perform either better or worse than a program that assigns the same interannual variation to the residual or long-term components of the fit. Even so, some curve fitting programs may be better or worse suited to certain types of analyses, or for decomposing certain types of data, based on how the trend, seasonal and residual variations in a time series are extracted. What is apparent from our analyses, is that CCGCRV and STL attribute more interannual variability in the data to the seasonal component of the time series, whereas HPspline attributes more of such variability to the residual component.

3.2 Long-term trends

Overall, the long-term trend curves produced by the three programs agree well when the mean slopes of the trends for the entire time series are compared (e.g., for ALT CH₄, see Fig. 4b). This is not surprising for CCGCRV and HPspline, which both use third degree polynomial functions as part of the trend calculation and therefore would be expected to produce similar long-term trends. It is reassuring that the STL trend curves also agree well, since STL separates out the trend variation using a very

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



CCGCRV trend smoothing value (f_1) of 667 days, compared to a typical STL trend smoothing value (*twin*) of 25 months (~ 760 days). Although there are large differences between the trend and growth rate curves on short-term time-scales for some of the time series, it is reassuring that there are no significant differences between the trend and growth rate means for the whole time series, since for some atmospheric greenhouse gases, such as CO_2 , even very small differences in the long-term atmospheric accumulation over the past decades could propagate into very large differences in future projections of atmospheric CO_2 mole fraction. Our findings do indicate, however, that care must be taken in studies that examine and report the most recent behaviour in the accumulation of greenhouse gases in the atmosphere, since such results are sensitive to the curve fit program used, both because of the short time-scales involved (a few years or less) and because of possible end effects.

3.3 Seasonal cycles

Comparing how effectively the curve fitting programs represent interannual variations in the seasonal cycle demonstrates that HPspline is least able to follow interannual variability in the magnitude of the seasonal minima and maxima for all five time series; e.g. the HPspline curve captures less than 50 % of the ALT CO_2 maxima and CGO CH_4 minima data points (see Fig. 6). CCGCRV is able to capture interannual seasonal variability the most effectively, and STL has intermediary effectiveness, capturing at least 70 % of the maxima and minima for all the time series. Unlike Nakazawa et al. (1997), Trivett et al. (1989) and Tans et al. (1989), we find that CCGCRV and STL are able to adequately represent the deep summer CO_2 minima at ALT (the programs fitted 91 % and 95 % of these minima respectively), a feature that is characteristic of high latitude Northern Hemisphere stations; HPspline was also able to represent 78 % of the deep summer CO_2 minima at ALT, but under-estimated some of the deepest CO_2 minima significantly.

Comparison of the magnitudes of the seasonal cycle maxima and minima show that HPspline produces higher seasonal maxima values and lower minima values, whilst

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



conversely, STL produces lower seasonal maxima values and higher seasonal minima values; CCGCRV produces intermediary values of both the seasonal maxima and minima. The differences between the mean magnitudes of the seasonal inflexion points are statistically significant to the 95 % confidence level in some cases. For example, the differences in the mean seasonal maxima calculated by HPspline and STL for the ALT CO₂ and BHD CO₂ time series are significant at 0.23 ppm and 0.10 ppm respectively. In addition, the STL seasonal minima occur on average six days earlier than those of HPspline, which is also statistically significant.

Figure 7a shows the differences in the ALT CO₂ seasonal cycle amplitude produced by the three curve fitting programs. The mean seasonal cycle amplitudes produced by HPspline, CCGCRV and STL for the ALT CO₂ data set are 15.3 ppm, 15.2 ppm and 15.1 ppm, respectively. As with the seasonal maxima and minima, overall, HPspline produces the largest seasonal cycle amplitudes, STL produces the smallest, and CCGCRV produces intermediary values, for both the ALT and BHD CO₂ time series. The mean seasonal cycle amplitudes produced by HPspline, CCGCRV and STL for the BHD CO₂ data set are 1.24 ppm, 1.16 ppm and 1.06 ppm, respectively; the difference in the HPspline and STL amplitudes of 0.18 ppm is statistically significant. For both time series, all three programs indicate that the value of the seasonal maxima is increasing and the value of the seasonal minima is decreasing; hence, the three programs also show that the seasonal cycle amplitude of CO₂ is increasing in magnitude over time at both ALT (see Fig. 7b) and BHD. These positive trends in the seasonal cycle amplitude are statistically significant for all three programs at both sites, except for the HPspline ALT CO₂ amplitude trend, which is not significant. There are no significant differences between the CO₂ seasonal cycle amplitude trends produced by the three programs, either at ALT (indicated by the error bars in Fig. 7b) or at BHD, which in part is owing to the relatively large interannual variability in the seasonal cycle amplitude.

Many of the differences in the seasonal output from the three programs are also scientifically significant in addition to being significant based on statistics alone. Previous studies that have examined changes in the seasonal cycle of greenhouse gases

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



over long time periods, such as Piao et al. (2008), typically find small trends, for example of less than a day per year in the shift in phasing of the seasonal cycle. Therefore, differences in the phasing of the program outputs on the order of several days (e.g. as found for CO₂ seasonal minima) indicate that results from such studies may be significantly biased by the choice of curve fitting program. In addition, the current WMO/GAW (Global Atmosphere Watch) compatibility goal for measurement stations is ±0.1 ppm (±0.05 ppm in the Southern Hemisphere) for CO₂ and ±2 ppb for CH₄ (Brailsford, 2012); thus, introducing uncertainties greater than these values during the data analysis process simply because of the choice of curve fitting program is scientifically significant and should be avoided if possible.

3.4 Gaps and outliers

The programs were assessed for their ability to cope with gaps in the time series by introducing artificial gaps with durations from 3 to 11 months into the time series. Figure 8 shows the effect of an 11 month gap in the ALT CO₂ time series on the HPspline and CCGCRV curve fits. STL is not shown in Fig. 8, since the program requires that the data are regularly spaced and is unable to recognise the artificial gaps. This is effectively because STL does not take into consideration the time stamps of the data, only the frequency of the input data, $n_{(p)}$, which is defined by the user (see Sect. 2.1.3) and is assumed to be constant throughout the time series. When run with exactly a year of data missing, STL processes the data as if there were no gap at all, whereas gaps that are shorter or longer than 12 months cause very large fitting anomalies in all output after the gap.

CCGCRV curve fits are significantly affected by gaps in the time series, as are the long-term trend and growth rate components of the CCGCRV decomposition. In contrast, HPspline is relatively unaffected by gaps in the time series for all components of the decomposition. This indicates that the Reinsch spline part of HPspline is more robust to gaps than the CCGCRV filtering, since if either the polynomial or harmonic functions were the vulnerable components, which are common to both programs, one

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

would expect HPspline to be affected similarly to CCGCRV. Varying the time of year of the gaps has no effect on the response of the curve fitting programs, with the exception of the ALT CO₂ time series, for which the anomalies caused by the gaps are larger when the gaps incorporate the seasonal maxima. This is most likely owing to the asymmetric shape of the ALT CO₂ seasonal cycle in which the seasonal maxima constitutes a large proportion of the year. We also note that our tests were conducted on relatively long time series of 20 or more years; for shorter time series, we would expect both HPspline and CCGCRV to be less robust to gaps.

The three programs were also tested for vulnerability to outliers by replacing one of the time series data points with a data point that was either 1 % greater or less than the original value. These tests reveal that all three programs are affected to some degree by even such relatively small outliers, and by only a single outlier in time series of 20 or more years' duration. Across all five time series, CCGCRV is generally the most sensitive of the three programs to outliers, although STL is also significantly affected, and sometimes more so than CCGCRV (see Fig. 9). In addition, anomalies in the CCGCRV curve fits only occur at the point in the time series where the outlier also occurs, whereas the STL curve fits are characterised by anomalies in the preceding and subsequent years also. The detrended output of the decomposition is more severely affected by the outliers than the trend and growth rate outputs for both CCGCRV and STL, which suggests that the f_s and *swin* smoothers are more susceptible to outliers than the f_1 and *twin* smoothers.

As with the artificial gaps, HPspline is the most robust program to outliers in the time series, although some of the outlier anomalies in the HPspline curve fit are significant (see Fig. 9). Importantly, an outlier that occurs near to the inflexion points of the seasonal cycle can influence the magnitude and/or the timing of the seasonal maximum or minimum for any of the programs (see Fig. 9), and can cause significant biases in the seasonal analysis of a time series. Although HPspline is relatively robust to outliers, the curve fit reveals small anomalies that “echo” throughout the entire data set, coincide with the timing of the outlier within the seasonal cycle, and diminish in magnitude

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[◀](#)
[▶](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)


Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



with increasing time (both forwards and backwards in time from the occurrence of the outlier). We believe that this “echo” is an artefact of the spline, since it is not present in the trend (which is independent of the spline), and disappears from the curve fit and detrended outputs when the flexibility of the spline is increased (that is, by increasing the spline stiffness parameter, $SD2$). Therefore, while less severely affected, a larger proportion of the HPspline curve fit could be biased by a single outlier in the time series which may not be obvious on first inspection, whereas the effect of an outlier will be more easily recognisable in the CCGCRV and STL outputs (and thus, it is likely to be easier to filter the outlier as a spurious point and re-compute the curve fits).

The “echo” effect resulting from outliers in the HPspline curve fits becomes more apparent when an outlier is placed at the beginning of the time series (i.e. within the first seasonal cycle). Both CCGCRV and STL are affected by such an outlier at the time that it occurs, but the curve fits for the rest of the time series remain unaffected. HPspline, however, is more severely affected by this outlier, both at the time that it occurs, and throughout the rest of the time series than when it occurs in the middle of the time series. This effect, where a curve fitting program is more susceptible to time series anomalies when they occur at the ends of the data set is known as an “end effect”. HPspline is not the only curve fitting program found to be susceptible to end effects, as STL also occasionally exhibited significant end effects in the long-term trend growth rate (Sect. 3.2 above).

3.5 Program input parameters

The ranges of input parameters tested are shown in Table 2. These ranges were chosen to test the limits of the three curve fitting programs, and are therefore not necessarily appropriate for all analyses of atmospheric time series. The input parameters tested include the “stiffness” of the spline component of the HPspline fitting program (i.e. the $SD2$ setting), the f_s and f_l smoothing parameters for CCGCRV, the $swin$ and $twin$ smoothing parameters for STL, and the number of harmonic and polynomial terms included in the HPspline and CCGCRV programs. For the five time series that we used

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

find that there is no fixed combination of smoothing parameter values that causes the programs to behave similarly to each other, since one combination of smoothing parameter values may produce very similar trends, but quite different detrended outputs, and vice versa. We also found that when CCGCRV and STL are run with smoothing parameter values of $f_s = swin$ and $f_l = twin$, the STL curve fits are more flexible than the CCGCRV curve fits, and the STL trend is less flexible than the CCGCRV trend. This result indicates that STL assigns a greater emphasis to seasonal time-scale variations than trend time-scale variations when compared to CCGCRV.

Altering the input smoothing parameters of the three programs also causes the outputs from some of the previous tests in Sects. 3.1 to 3.4 to change. For example, we find that using the input smoothing parameter values that result in the most similar curve fits, STL is the most flexible program and CCGCRV is only slightly less flexible, which is converse to the previous result, when the default smoothing parameter settings were used. STL is also more severely affected by outliers than CCGCRV, which again is in contrast to the previous outlier test results. Figure 10 summarises four examples of how the curve fitting outputs can be substantially influenced by changing the input smoothing parameters of each program, and demonstrates how it is possible to obtain entirely different results from a time series using the same curve fitting program with different input smoothing parameter values. Thus, not only might a time series analysis be biased by the choice of curve fitting program, but also by the choice of input smoothing parameters. Figure 10 also indicates that in a few circumstances, the curve fitting programs produce the same outputs, despite using very different values of the input parameter smoothing values. For example, it appears that STL has an almost identical response to a 1% outlier when the *swin* value is varied from 5 to 25 years (Fig. 10a), and CCGCRV has a very similar response to an 11 month gap in the time series when the f_s value is varied from 50 to 200 days (Fig. 10b).

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



3.6 Re-analysis of zero-crossing trends of Piao et al. (2008) using HPspline and STL

In order to demonstrate the importance of whether scientific conclusions are unduly influenced by the choice of curve fitting program, we have used HPspline and STL to replicate the zero-crossing analysis in Piao et al. (2008), who used CCGCRV. In brief, Piao et al. (2008) used CCGCRV to detrend CO₂ time series from ten Northern Hemisphere field stations from the Globalview-CO₂ database (GLOBALVIEW-CO₂, 2004), linearly interpolated the detrended data to obtain values of the spring downwards zero-crossing dates (SDZ) and the autumn upwards zero-crossing dates (AUZ), and then for each year, subtracted the SDZ from the AUZ to obtain the carbon uptake period (CUP) of the terrestrial biosphere. Trends in the CUP were determined using linear regressions, and the probability that these trends were statistically significant was calculated.

Figure 11 shows the results of Piao et al. (2008) alongside our re-analysis of the CUP trends with exactly the same input time series, but using STL and HPspline output instead of CCGCRV output. Trends that are positive indicate the CUP is getting longer, and suggests that the net terrestrial biosphere carbon sink is getting larger, while negative trends indicate the opposite. There are small differences between the CUP trends calculated using the three different curve fitting programs at all of the stations, and a statistically significant difference between the STL and HPspline trends at SCH (determined based on the standard error of the linear regressions used to calculate the CUP trends). No other station showed statistically significant differences in the output from the three different curve fitting programs, and at all ten stations, the mean CUP trends agree well for all three curve fitting programs.

Our re-analysis does, however, reveal that the number of stations exhibiting negative and statistically significant CUP trends is dependent on the curve fitting program used. The analysis of Piao et al. (2008) found that 9 out of the 10 stations have negative CUP trends (see Fig. 11), and that 3 of these 9 negative CUP trends are statistically significant. In contrast, only 8 of the STL trends are negative, although 5 of these are

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



statistically significant (as is one of the positive trends), and for HPspline, 7 of the trends are negative, only one of which is statistically significant.

Although we have found the conclusions from the curve fitting analysis in Piao et al. (2008) to be robust when using any of the three curve fitting programs presented here, the analyses of individual stations is dependent on the curve fitting program used. This one example highlights the importance of investigating the influence of curve fitting bias on the scientific conclusions of an analysis by employing more than one curve fitting program wherever possible.

4 Conclusions and recommendations

We have investigated bias in the application of three commonly used curve fitting programs to monthly mean atmospheric time series from three stations: Alert Station, Canada, Cape Grim Observatory, Australia, and Baring Head, New Zealand. Our comparisons show that there are often significant differences between the outputs of these three programs, and that the outputs are also sensitive to the choice of program input smoothing parameters. We have also found that the differences between the program outputs depend on the amount of interannual variability in the time series and the seasonal cycle amplitude. For time series with gradual year-on-year changes and/or a relatively small seasonal cycle amplitude, the programs produce much more similar outputs to each other than for time series that are characterised by relatively high interannual variability and/or a relatively large seasonal cycle amplitude. More specifically, we draw the following conclusions from our study:

1. CCGCRV was found to be the most flexible program, HPspline was the least flexible, and STL demonstrated intermediate flexibility, where flexibility describes the amount of short- and long-term variability in the time series that the three programs are able to represent. Hence, the HPspline and CCGCRV curve fits were found to be consistently the least similar across all five time series. The difference

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



in flexibility is also reflected in the residual components of the decomposition, which were consistently largest for HPspline, smallest for CCGCRV, and intermediate for STL. Even when the *SD2* spline stiffness setting of HPspline was increased to its maximum value (minimum stiffness), it was not possible to make the HPspline curve fits as flexible as the CCGCRV and STL curve fits.

2. The mean slopes of the long-term trend and associated growth rate curves agreed well between all three programs over long time periods, although there were some significant differences between the curves for individual years. HPspline tends to generate smoother trend and growth rate curves than the other two programs, as the program assigns a greater proportion of the long-term variability to the residual component of the decomposition.
3. For some time series, statistically significant differences were found between the HPspline and STL magnitudes of the seasonal maxima, minima and amplitudes, and the timing of the seasonal inflexion points. This is in part attributable to STL assigning a smaller proportion of the variation in the time series to the seasonal component of the decomposition. STL and CCGCRV over- and under-estimated the seasonal maxima and minima less frequently than HPspline, which for some time series, captured less than 50 % of the seasonal inflexion points. All three programs, however, found that the magnitude of the CO₂ seasonal cycle amplitude at both ALT and BHD has increased over time.
4. STL cannot be used when gaps exist in the time series, and requires the data to be at evenly spaced intervals. CCGCRV was significantly affected by gaps of 11 months, whereas HPspline was relatively robust to gaps in the time series.
5. All three programs were found to be vulnerable to relatively small outliers (1 % larger or smaller than the original data point) in the time series, although, in general, CCGCRV was found to be the most vulnerable, and STL was more severely affected than HPspline. All three programs were more vulnerable to outliers that

a broad range of characteristics, such as magnitude of the seasonal cycle amplitude, and interannual variability in both the seasonal and trend variation.

1. For analyses where it is appropriate or useful to assign more variation to the residual component of a time series decomposition, and less variation to the trend and seasonal components, we recommend the use of HPspline. A key example is investigating correlations between atmospheric time series and large scale climate phenomena or climate indices such as the El Niño/Southern Oscillation.
2. For analyses where it is important that year-to-year variations in the seasonal and trend components are retained, we recommend CCGCRV, for example in studies such as Piao et al. (2008) examining changes in features of the seasonal cycle. STL is also appropriate for such analyses, although the user should be aware that STL assigns less variation to the seasonal component, and more variation to the trend component compared to CCGCRV, depending on the input smoothing parameter settings used.
3. For analyses where it is important to accurately represent the magnitude or timing of the seasonal inflexion points, and/or the seasonal cycle amplitude, we recommend CCGCRV and STL, but not HPspline. This includes analyses where the time series is characterised by deep, short minima or maxima, such as high latitude Northern Hemisphere atmospheric CO₂ time series.
4. For analyses where it is important to fit the data as closely as possible, we recommend the use of CCGCRV, and discourage the use of HPspline.
5. For studies reporting the most recent growth rate in the accumulation of gases in the atmosphere, we strongly recommend the use of more than one curve fitting program, since growth rate calculations are particularly sensitive to possible end effects.
6. For calculations of mean long-term trends, results can be sensitive to trend values at the ends of the time series, which in turn can sometimes be quite different

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



across the three curve fitting programs. Therefore, for such calculations, we recommend the use of more than one curve fitting program.

7. For analyses of interannual variations of the long-term trend, particularly for time series with variable long-term trend growth rates, such as atmospheric CH₄ time series, we recommend CCGCRV and STL, but not HPspline. We also warn users that STL occasionally generates spurious variations at the ends of the long-term trend growth rate curves.
8. For analyses where the time series contains gaps, or the data are not evenly spaced through time, we recommend HPspline, but not CCGCRV or STL. In particular, users should be aware that STL is unable to fit across gaps in time series. For analyses including time series with gaps, and where the focus of the investigation is such that another recommendation in this list advises use of CCGCRV or STL, it may be appropriate to first use an interpolation technique to populate the gaps in the time series, and then carry out the analyses with CCGCRV or STL.
9. For analyses where the time series contains outliers, if the purpose is to identify the outliers and remove them from the time series, we recommend CCGCRV, because the program is sensitive to outliers, but only at the time they occur, meaning that outliers are easily recognisable and can subsequently be removed.
10. If the purpose of an analysis of a time series containing outliers is to produce curve fits, or to decompose the data without removing the outliers, we recommend STL or CCGCRV. This is because although HPspline tends to be affected to a lesser degree than STL at the time of the outlier occurrence, the program output is affected throughout a much larger proportion of the time series than the STL and CCGCRV outputs. Additionally, for time series that contain outliers near the ends, we discourage the use of HPspline because it is sensitive to end effects caused by outliers.

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



11. We recommend that users choose appropriate values of the input smoothing parameters based on the characteristics of the time series, and not based on the values that are typically used by colleagues, or that have been used historically. We also highly recommend that users conduct sensitivity tests to ensure that the scientific results of an analysis are not unduly biased by the choice of input smoothing parameter settings.
12. Advice on how to choose appropriate input smoothing parameter settings for CCGCRV and STL is given in Thoning et al. (1989) and Cleveland et al. (1990) respectively. We recommend that the $f_s/swin$ and $f_l/twin$ values are sufficiently different so that the CCGCRV and STL short- and long-term smoothing procedures do not compete for the same variation in the data.
13. Finally, we strongly recommend that users employ more than one curve fitting program, to ensure that the results of an analysis will not be unduly biased by the choice of curve fitting program. This is particularly important for analyses that are more vulnerable to curve fitting bias, such as those that examine relatively small trends or changes in time series that are very variable, and for analyses where a high degree of accuracy is required, such as a comparison of time series from two locations, for example.

Key examples of further work that would improve our understanding of possible curve fitting bias include comparing curve fitting program outputs using higher frequency time series, such as weekly, daily or hourly averages, conducting curve fitting comparisons using additional curve fitting programs to the three tested here, and conducting comparisons on shorter time series.

Our results clearly show that significant bias and uncertainty can be introduced in the application of curve fitting programs to atmospheric time series. It is thus important that investigators ensure that curve fitting programs are appropriate for the application for which they are used, use more than one program to analyse the same data so that any

biases can be identified, and test the sensitivity of the results to the input smoothing parameters.

Great care is taken by experimental scientists to ensure that atmospheric greenhouse gas measurements are very precise, reproducible, and compatible with other measurement sites. The same care and attention is essential in the analysis of these data, and in the application of curve fitting programs, to ensure the robustness and reproducibility of scientific interpretation and conclusions drawn.

Acknowledgements. We thank Paul Krummel (CMAR, CSIRO, Australia) for providing the CCGCRV IDL code and for making the Cape Grim Observatory CH₄ data available on the CSIRO website, and Sara Mikaloff-Fletcher (NIWA, New Zealand) for providing the STL R script used in this work. We also thank Steve Piper (Scripps Institution of Oceanography, USA) and Mike Salmon (UEA, UK) for assistance with HPspline. The Baring Head CO₂ data were kindly provided by Gordon Brailsford (NIWA, New Zealand) and Britt Stephens (NIWA, New Zealand and NCAR, USA). The Alert Station CO₂ and CH₄ data were made available via WDCGG by Doug Worthy (Environment Canada, Canada), and the Baring Head O₃ data were made available via WDCGG by Sylvia Nichol (NIWA, New Zealand). We also thank Britt Stephens, Gordon Brailsford, Martin Manning (Victoria University of Wellington, New Zealand), Paul Krummel and Sara Mikaloff-Fletcher for their helpful input during the initial phases of this project. Finally, we thank Shilong Piao (Peking University, China), Jonathan Barichivich (UEA, UK), and Ángel Gómez-Peláez (Izaña Atmospheric Research Center, Meteorological State Agency of Spain) for helpful discussions on the use of curve fitting programs, and Robert Jenkins (UEA, UK) for advice regarding the statistical analyses. P. A. Pickers is supported by a UK Natural Environment Research Council Ph.D. studentship (NE/K500896/1).

References

- Amritkar, R. E. and Kumar, P.: Interpolation of missing data using nonlinear and chaotic system analysis, *J. Geophys. Res.*, 100, 3149–3154, doi:10.1029/94JD01531, 1995.
- Bacastow, R. B.: Modulation of atmospheric carbon dioxide by the Southern Oscillation, *Nature*, 261, 116–118, doi:10.1038/261116a0, 1976.

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Bacastow, R. B., Keeling, C. D., and Whorf, T. P.: Seasonal amplitude increase in atmospheric CO₂ concentration at Mauna Loa, Hawaii, 1959–1982, *J. Geophys. Res.-Atmos.*, 90, 10529–10540, doi:10.1029/JD090iD06p10529, 1985.

Brailsford, G. W. (Ed.): Report of the Sixteenth WMO/IAEA Meeting on Carbon Dioxide, Other Greenhouse Gases, and Related Measurement Techniques (GGMT-2011), Wellington, New Zealand, World Meteorological Organization Global Atmosphere Watch Report Series No. 206, available at: <http://www.wmo.int/pages/prog/arep/gaw/gaw-reports.html> (last access: 2 December 2013), 2012.

Carlsaw, D. C.: On the changing seasonal cycles and trends of ozone at Mace Head, Ireland, *Atmos. Chem. Phys.*, 5, 3441–3450, doi:10.5194/acp-5-3441-2005, 2005.

Chan, Y. H. and Wong, C. S.: Long-term changes in amplitudes of atmospheric CO₂ concentrations at Ocean Station P and Alert, Canada, *Tellus B*, 42, 330–341, 1990.

Cleveland, R. B., Cleveland, W. S., McRae, J. E., and Terpenning, I.: STL: a seasonal-trend decomposition procedure based on Loess, *Journal of Official Statistics*, 6, 3–33, 1990.

Dlugokencky, E. J., Nisbet, E. G., Fisher, R., and Lowry, D.: Global atmospheric methane: budget, changes and dangers, *Philos. T. Roy. Soc. A*, 369, 2058–2072, doi:10.1098/rsta.2010.0341, 2011.

Elliott, W. P.: The Statistical Treatment of CO₂ Records, NOAA Technical Memorandum ERL ARL-173, Maryland, USA, 1989.

Enting, I. G.: The interannual variation in the seasonal cycle of carbon dioxide concentration at Mauna Loa, *J. Geophys. Res.*, 92, 5497–5504, doi:10.1029/JD092iD05p05497, 1987.

GLOBALVIEW-CO2: GLOBALVIEW-CO2: Cooperative Atmospheric Data Integration Project – Carbon Dioxide, CD-ROM, NOAA GMD, Boulder, Colorado, 2004.

Houghton, R. A.: Balancing the global carbon budget, *Annu. Rev. Earth Pl. Sc.*, 35, 313–347, doi:10.1146/annurev.earth.35.031306.140057, 2007.

Jones, C. D., Collins, M., Cox, P. M., and Spall, S. A.: The carbon cycle response to ENSO: a coupled climate-carbon cycle model study, *J. Climate*, 14, 4113–4129, doi:10.1175/1520-0442(2001)014<4113:TCCRTE>2.0.CO;2, 2001.

Keeling, C. D.: The concentration and isotopic abundances of carbon dioxide in the atmosphere, *Tellus*, 12, 200–203, 1960.

Keeling, C. D., Guenther, P. R., and Whorf, T. P.: An Analysis of the Concentration of Atmospheric Carbon Dioxide at Fixed Land Stations and over the Oceans based on Discrete

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

samples and Daily Averaged Continuous Measurements, Scripps Institution of Oceanography, 1986.

Keeling, C. D., Bacastow, R. B., Carter, A. F., Piper, S. C., Whorf, T. P., Heimann, M., Mook, W. G., and Roeloffzen, H.: A three-dimensional model of atmospheric CO₂ transport based on observed winds: 1. analysis of observational data, American Geophysical Union, Geophysical Monograph, 55, 165–236, 1989.

Keeling, C. D., Chin, J. F. S., and Whorf, T. P.: Increased activity of northern vegetation inferred from atmospheric CO₂ measurements, *Nature*, 382, 146–149, doi:10.1038/382146a0, 1996.

Keeling, C. D., Piper, S. C., Whorf, T. P., and Keeling, R. F.: Evolution of natural and anthropogenic fluxes of atmospheric CO₂ from 1957 to 2003, *Tellus B*, 63, 1–22, doi:10.1111/j.1600-0889.2010.00507.x, 2011.

Keeling, R. F. and Shertz, S. R.: Seasonal and interannual variations in atmospheric oxygen and implications for the global carbon cycle, *Nature*, 358, 723–727, doi:10.1038/358723a0, 1992.

Manning, M. R., Lowe, D. C., Melhuish, W. H., Sparks, R. J., Wallace, G., Brenninkmeijer, C. A. M., and McGill, R. C.: The use of radiocarbon measurements in atmospheric studies, 13th Radiocarbon International Conference, 32, 37–58, 1990.

Martin, F. and Diaz, A.: Different methods of modeling the variability in the monthly mean concentrations of atmospheric CO₂ at Mauna Loa, *J. Geophys. Res.*, 96, 18689–18704, doi:10.1029/91JD01710, 1991.

Minejima, C., Kubo, M., Tohjima, Y., Yamagishi, H., Koyama, Y., Maksyutov, S., Kita, K., and Mukai, H.: Analysis of $\Delta O_2 / \Delta CO_2$ ratios for the pollution events observed at Hateruma Island, Japan, *Atmos. Chem. Phys.*, 12, 2713–2723, doi:10.5194/acp-12-2713-2012, 2012.

Nakazawa, T., Ishizawa, M., Higuchi, K., and Trivett, N. B. A.: Two curve fitting methods applied to CO₂ flask data, *Environmetrics*, 8, 197–218, doi:10.1002/(SICI)1099-095X(199705)8:3<197::AID-ENV248>3.0.CO;2-C, 1997.

Piao, S., Ciais, P., Friedlingstein, P., Peylin, P., Reichstein, M., Luysaert, S., Margolis, H., Fang, J., Barr, A., Chen, A., Grelle, A., Hollinger, D. Y., Laurila, T., Lindroth, A., Richardson, A. D., and Vesala, T.: Net carbon dioxide losses of northern ecosystems in response to autumn warming, *Nature*, 451, 49–52, doi:10.1038/nature06444, 2008.

Pierce, D. A.: Signal extraction error in nonstationary time series, *Ann. Stat.*, 7, 1303–1320, doi:10.1214/aos/1176344848, 1979.

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Press, W. H., Teukolsky, S. A., Vetterling, W. T., and Flannery, B. P.: Numerical Recipes in Fortran 90, The Art of Parallel Scientific Computing, 2nd Edn., Cambridge University Press, 1996.

Reichenau, T. G. and Esser, G.: Is interannual fluctuation of atmospheric CO₂ dominated by combined effects of ENSO and volcanic aerosols?, *Global Biogeochem. Cy.*, 17, 5–1, doi:10.1029/2002GB002025, 2003.

Reinsch, C. H.: Smoothing by spline functions, *Numer. Math.*, 10, 177–183, doi:10.1007/bf02162161, 1967.

Tans, P., Thoning, K. W., Elliot, W. P., and Conway, T. J.: Background atmospheric CO₂ from weekly flask samples at Barrow, Alaska: optimal signal recovery and error estimates, NOAA Technical Memorandum, ERL ARL-173, Air Resources Laboratory, Silver Spring, Maryland, USA, 112–123, 1989.

Theodosiou, M.: Forecasting monthly and quarterly time series using STL decomposition, *Int. J. Forecasting*, 27, 1178–1195, doi:10.1016/j.ijforecast.2010.11.002, 2011.

Thoning, K. W., Tans, P. P., and Komhyr, W. D.: Atmospheric carbon dioxide at Mauna Loa Observatory 2. Analysis of the NOAA GMCC data, 1974–1985, *J. Geophys. Res.-Atmos.*, 94, 8549–8565, doi:10.1029/JD09iD06p08549, 1989.

Trivett, N. B. A., Higuchi, K., and Symington, S.: Trends and seasonal cycles of atmospheric CO₂ over Alert, Sable Island, and Cape St. James, as analyzed by forward stepwise multiple regression technique, NOAA Technical Memorandum ERL ARL-173, Air Resources Laboratory, Silver Spring, Maryland, USA, 27–42, 1989.

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Table 1. Atmospheric time series used in this study, including site location and altitude, gas species, time period and data source. Note, all data are monthly-mean baseline-only data, i.e. representative of “clean” background air.

Station Name	Location and Altitude	Gas Species	Percent of time series interpolated	Period	Data Source
Alert Station (ALT) Canada	82.45° N, 62.52° W 210 m a.s.l.	CO ₂ CH ₄	< 2 < 2	1988–2009 1988–2009	^b ^b
Baring Head (BHD) New Zealand	41.41° S, 174.87° E 85 m a.s.l.	CO ₂ O ₃	10 ^a 26 ^a	1970–2011 1991–2010	^c ^d
Cape Grim Observatory (CGO) Australia	40.68° S, 144.68° E 94 m a.s.l.	CH ₄	< 2	1984–2011	^e

^a Percentage interpolation required for BHD data is relatively high, not because the data do not exist, but because only baseline data (i.e. data that are consistent with the concept of a well-mixed atmosphere) are reported to the WDCGG database.

^b WDCGG (Doug Worthy, Environment Canada, Canada).

^c Britt Stephens, National Center for Atmospheric Research, USA; Gordon Brailsford and Antony Gomez, National Institute of Water and Atmospheric Research Ltd., New Zealand.

^d WDCGG (Sylvia Nichol, National Institute of Water and Atmospheric Research Ltd., New Zealand).

^e Paul Krummel, CSIRO Marine and Atmospheric Research, Australia, and the Australian Bureau of Meteorology (Cape Grim Baseline Air Pollution Station), website: <http://www.csiro.au/greenhouse-gases/>.

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[◀](#)
[▶](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)


Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Table 2. Range of input parameter settings that were varied to test program sensitivity. Values in bold text indicate typical settings used by colleagues and throughout this study, unless otherwise stated.

Program Name	Parameter	Values Tested
HPspline	Spline stiffness parameter, $SD2$, in ppm yr^2	1, 30 , 99 999,
	Number of harmonic terms	2, 4 ,
	Degree of polynomial function	1, 3 , 5
CCGCRV	Short-term cut-off value (f_s), in days	5, 50 , 200
	Long-term cut-off value (f_l), in days	100, 667 , 1200
	Number of harmonic terms	2, 4 , 6
	Degree of polynomial function	1, 3 , 5
STL	Seasonal smoothing window ($swin$), in years	1, 5 , 50
	Trend smoothing window ($twin$), in months	5, 25 , 500

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[◀](#)
[▶](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)


Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Table 3. Percentage of data points “captured” by HPspline, CCGCRV and STL for the five atmospheric time series. “Captured” points are those for which the fitted curve passes within the $\pm 1\sigma$ standard deviation of the monthly mean for each data point.

Station	Gas Species	CCGCRV (%)	STL (%)	HPspline (%)
ALT	CO ₂	97.7	88.6	76.9
	CH ₄	99.2	83.7	65.9
BHD	CO ₂	99.4	95.9	90.0
	O ₃	88.6	73.4	67.5
CGO	CH ₄	100	94.5	73.6

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)

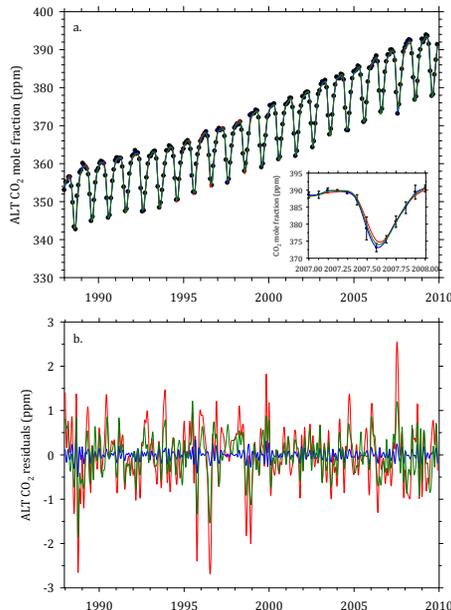


Figure 1. (a) HPspline (red line), CCGCRV (blue line) and STL (green line) curve fits to monthly means of CO₂ mole fraction (black dots) measured at ALT, Canada. The inset shows a single year of data, with the standard deviations (SD) of the observed monthly means represented by the black error bars. Error bars are not shown on the full size plot to retain clarity. In general, all three curve fits lie within the standard deviation limits. HPspline exceeds the SD limits for 23.1% of the data, STL exceeds the SD limits for 11.4% of the data, and CCGCRV exceeds the SD limits for 2.3% of the data. These exceptions generally occur at the seasonal maxima and minima, where the curve fit programs have a tendency to over- or under-fit the seasonal inflexion points. **(b)** Residuals of the HPspline (red line), CCGCRV (blue line) and STL (green line) curve fits to monthly means of CO₂ mole fraction measured at ALT, Canada. Overall, HPspline produces the largest residuals, CCGCRV produces the smallest residuals, and STL produces intermediate residuals.

Investigating bias in the application of curve fitting programs

P. A. Pickers and A. C. Manning

Title Page	
Abstract	Introduction
Conclusions	References
Tables	Figures
◀	▶
◀	▶
Back	Close
Full Screen / Esc	
Printer-friendly Version	
Interactive Discussion	



Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

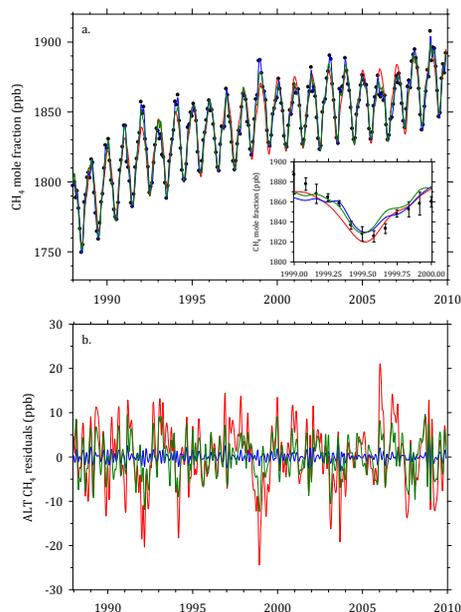


Figure 2. (a) HPspline (red line), CCGCRV (blue line) and STL (green line) curve fits to monthly means of CH_4 mole fraction (black dots) measured at ALT. The inset shows a single year of data, with the SD of the observed monthly means represented by the black error bars. Error bars are not shown on the full size plot to retain clarity. In general, all three curve fits lie within the SD limits. HPspline exceeds the SD limits for 34.1% of the data, STL exceeds the SD limits for 16.3% of the data, and CCGCRV exceeds the SD limits for 0.8% of the data. As with CO_2 , the curve fitting programs tend to exceed the SD limits at the seasonal maxima and minima, where the programs over- or under-fit the seasonal inflexion points. (b) Residuals of the HPspline (red line), CCGCRV (blue line) and STL (green line) curve fits to monthly means of CH_4 mole fraction measured at ALT, Canada. As for Fig. 1b, HPspline produces the largest residuals, CCGCRV produces the smallest residuals, and STL produces intermediate residuals.

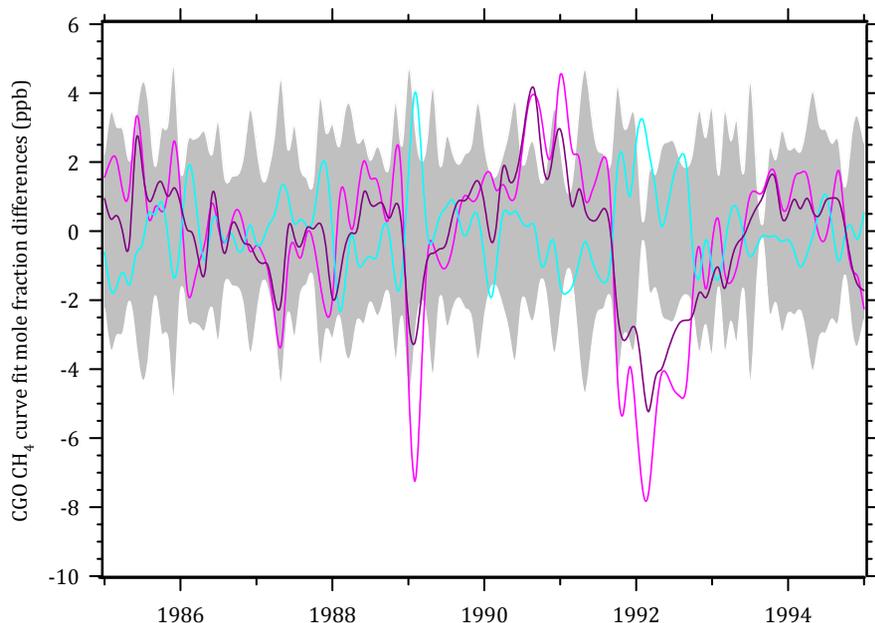


Figure 3. Comparison of the curve fit mole fraction differences between HPspline and CCGCRV (pink), CCGCRV and STL (cyan), and HPspline and STL (purple) for a subset of the CH₄ time series at CGO (between 1985 and 1995). The SD of the monthly mean measurements (grey shading) are also shown for comparison. The SD consist of discrete data points at monthly intervals, however, we have chosen to represent them as a continuous band to aid visual comparison to the curve fit differences. The largest differences are between HPspline and CCGCRV (pink), although differences between all three programs sometimes exceed the standard deviation of the observations.

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page	
Abstract	Introduction
Conclusions	References
Tables	Figures
◀	▶
◀	▶
Back	Close
Full Screen / Esc	
Printer-friendly Version	
Interactive Discussion	



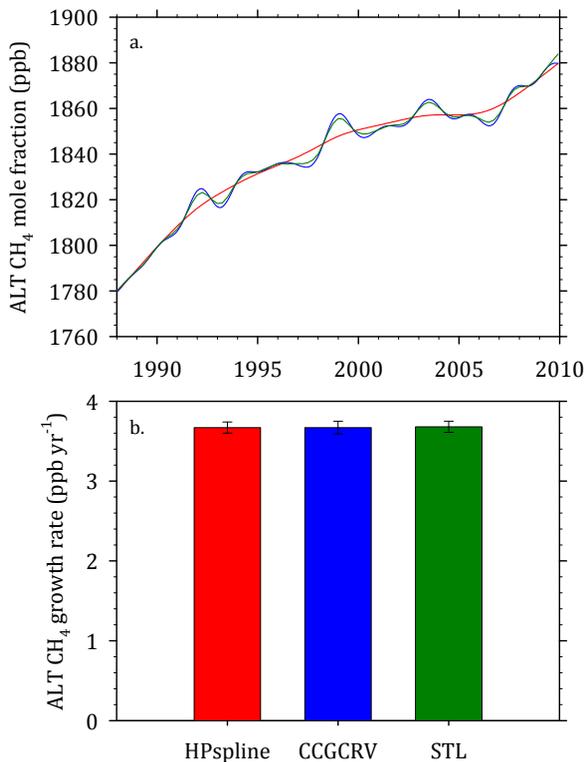


Figure 4. (a) Long-term trend of monthly mean CH₄ observations at ALT produced by HPspline (red line), CCGCRV (blue line), and STL (green line). **(b)** Although there are large differences between the long-term trends of the three curve fitting programs over short time-scales, the mean slope of the long-term trends (long-term growth rate) for the entire time series are very similar for all three programs. Error bars shown indicate the standard error of the regressions of the mean long-term trends.

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

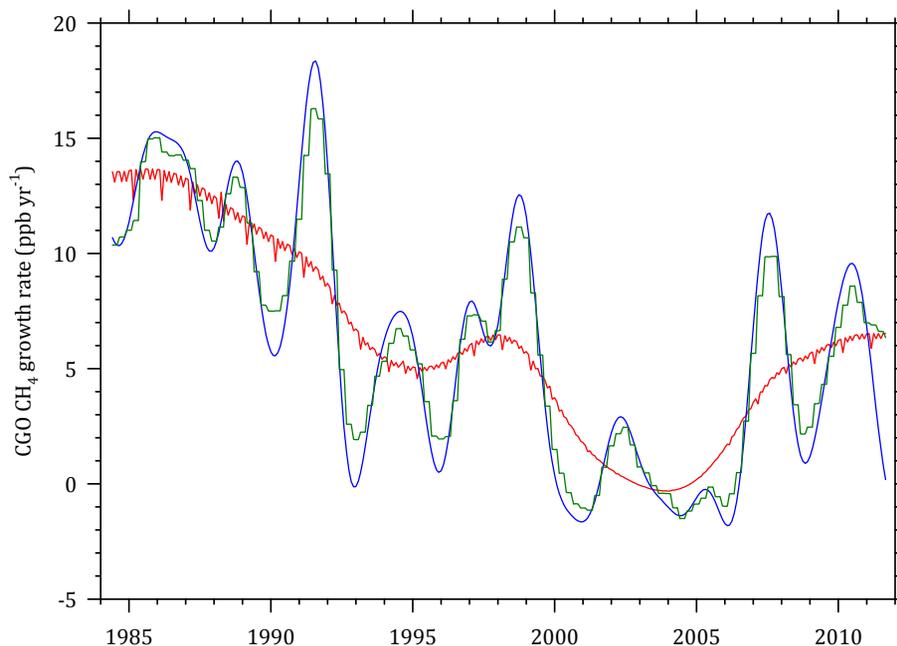


Figure 5. Growth rate of the long-term trend in monthly mean CH_4 observations at CGO produced by HPspline (red), CCGCRV (blue), and STL (green). As with the long-term trends, the mean growth rates calculated for the whole time series are similar for all three curve fitting programs, although there are large differences on short time-scales, also analogous to findings for the long-term trends. HPspline calculates a growth rate that is much smoother than those calculated by CCGCRV and STL, due to the stiffness of the spline component of the HPspline fitting procedure. The “ringing” effect superimposed on the HPspline growth rate curve is caused by the stiff spline and increases in magnitude towards the ends of the time series.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

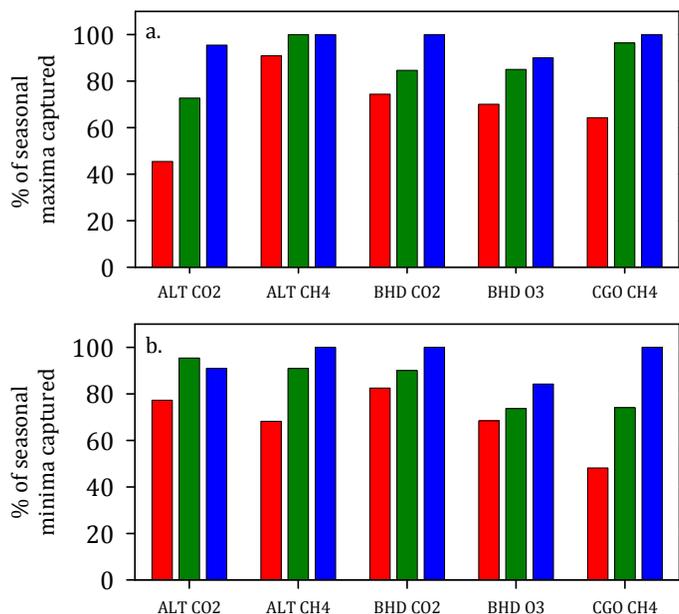


Figure 6. Percentage of seasonal maxima (plot *a*) and seasonal minima (plot *b*) “captured” by HPspline (red bars), STL (green bars) and CCGCRV (blue bars) for all five time series. The term “captured” refers to the curve fit passing within the $\pm 1\sigma$ standard deviation limits of the monthly mean data at the seasonal inflexion points. With one exception (ALT CO₂ minima), CCGCRV always captures the greatest number of seasonal maxima and minima (approximately 96% across all five time series), STL captures approximately 86% across all five time series, and HPspline captures the least: approximately only 68% across all five time series. This difference between the three programs reflects their comparative “flexibility” as defined by the input smoothing parameters of the program settings, i.e. HPspline is the least flexible program, STL displays intermediate flexibility, and CCGCRV is the most flexible program.

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[◀](#)
[▶](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)


Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

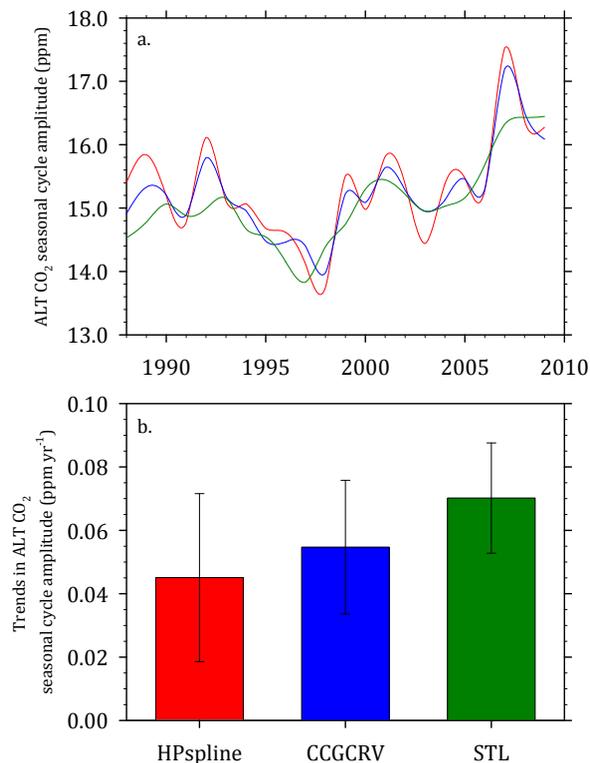


Figure 7. (a) Seasonal cycle amplitude of monthly mean CO₂ observations at ALT produced by HPspline (red) CCGCRV (blue) and STL (green). **(b)** Mean linear trends in the seasonal cycle amplitude of monthly mean CO₂ at ALT, calculated using the detrended output of the three curve fitting programs. Even though there are relatively large differences between the amplitudes of individual years, the mean trends are not significantly different from one another, as shown by the black error bars, which denote the standard error of the mean amplitude linear regressions.

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

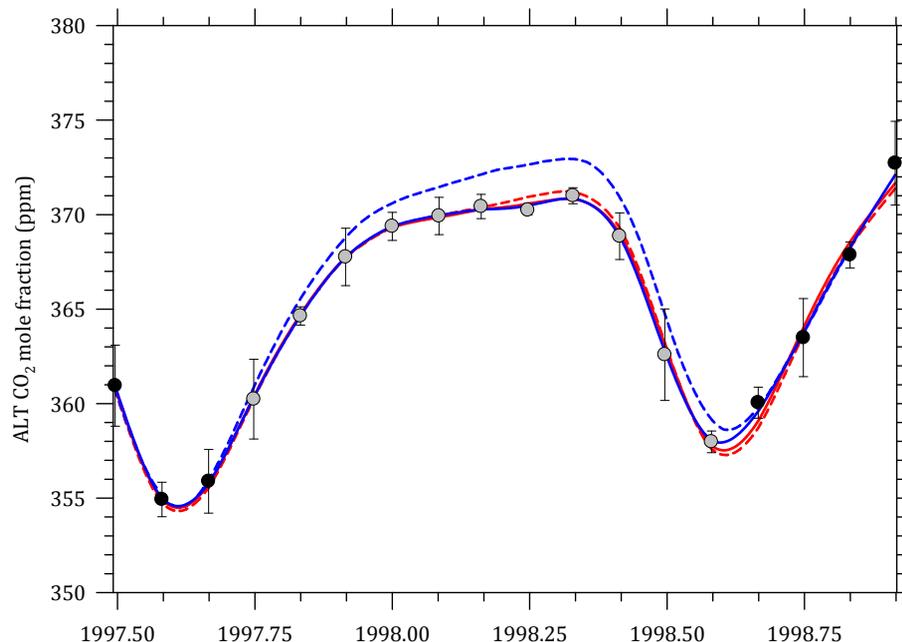


Figure 8. A subset of HPspline (red dashed line) and CCGCRV (blue dashed line) curve fits to monthly mean CO_2 observations at ALT (black dots), where data from October 1997 to August 1998 have been removed in order to create an artificial 11 month gap in the time series (solid grey dots). The curve fits for the two programs with no artificial gap are also shown by the two solid lines for comparison. Error bars indicate the SD limits of the monthly mean observations. Since STL is unable to recognise gaps in the time series, the program processes the data as if no gap exists and so it cannot be plotted against the other two program outputs. CCGCRV is severely affected by the gap as indicated by the significant increase in the seasonal maximum. HPspline is relatively robust to gaps in the time series, which only causes a small change in the curve fit.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

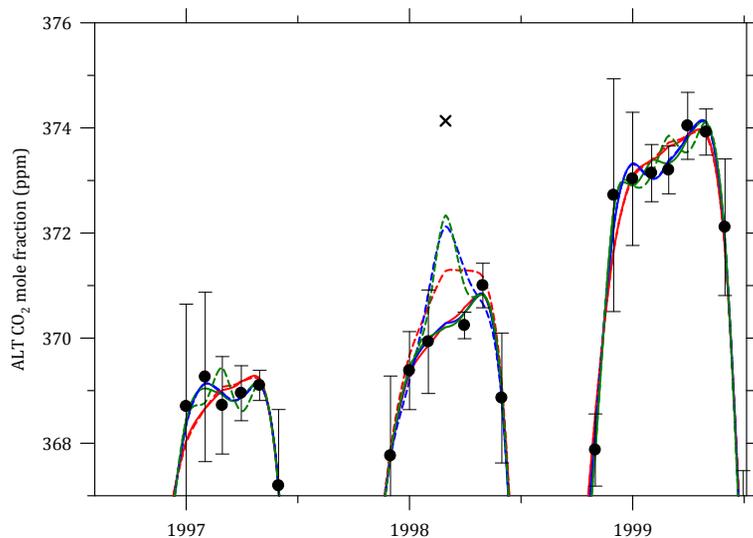


Figure 9. A subset of HPspline (red dashed line), CCGCRV (blue dashed line) and STL (green dashed line) curve fits to monthly mean CO_2 observations at ALT (black dots) from January 1996 to January 2000, where the monthly mean for March 1998 has been replaced with an artificial outlier (black cross) that has a value 1% greater (~ 4 ppm) than the original measured value. The curve fits for the three programs with no artificial outlier are also shown by the three solid lines for comparison. Error bars indicate the SD limits of the monthly mean observations, and the y axis has been scaled to aid visual comparison of the curve fit differences. As shown, both CCGCRV and STL are significantly affected by the outlier at the point of occurrence. Additionally, the timing of the seasonal maximum has shifted two months earlier for the STL and CCGCRV curves, to coincide with the occurrence of the outlier in March 1998. STL is also affected by spurious variation in the adjacent years, which shifts the timing of the seasonal maxima earlier by two months in 1997. HPspline is relatively robust to the influence of the outlier, however, the timing of the seasonal maximum is also shifted earlier in the year by two months.

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

Title Page	
Abstract	Introduction
Conclusions	References
Tables	Figures
◀	▶
◀	▶
Back	Close
Full Screen / Esc	
Printer-friendly Version	
Interactive Discussion	



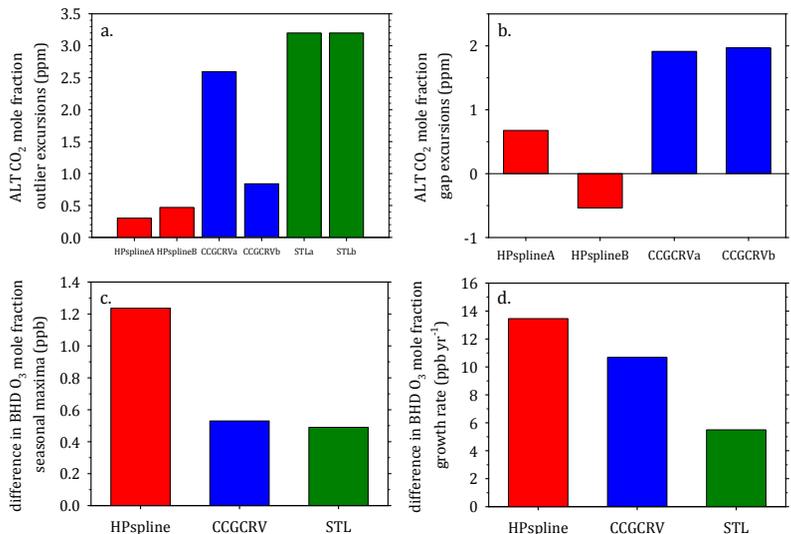


Figure 10. Four plots demonstrating the dependency of the curve fits on the program input smoothing parameters. **(a)** excursions in the ALT CO₂ curve fits caused by an outlier (1 % greater than the original data point) in March 1998, where for HPsplineA, $SD2 = 30$; for HPsplineB, $SD2 = 9999$; for CCGCRVa, $f_s : f_l = 50 : 667$; for CCGCRVb, $f_s : f_l = 200 : 667$; for STLa, $swin : twin = 5 : 25$; and for STLb, $swin : twin = 25 : 25$. **(b)** Excursion in the ALT CO₂ curve fits caused by an 11 month gap during 1998, where the program input smoothing parameters are varied as for plot a. Note that STL cannot fit across gaps and for this reason was not included in this plot. **(c)** Differences in the BHD O₃ 1998 seasonal maximum generated by varying the input smoothing parameters with the following values: HPspline: $SD2$ values of 30 and 1000; CCGCRV: $f_s : f_l$ values of 50 : 667 and 200 : 667; STL: $swin : twin$ values of 5 : 25 and 25 : 25. **(d)** Differences in the BHD O₃ 2001 long-term trend growth rate generated by varying the input smoothing parameters with the following values: HPspline: $SD2$ values of 30 and 99999; CCGCRV: $f_s : f_l$ values of 50 : 667 and 50 : 200; STL: $swin : twin$ values of 5 : 25 and 5 : 5.

Investigating bias in the application of curve fitting programs

P. A. Pickers and
A. C. Manning

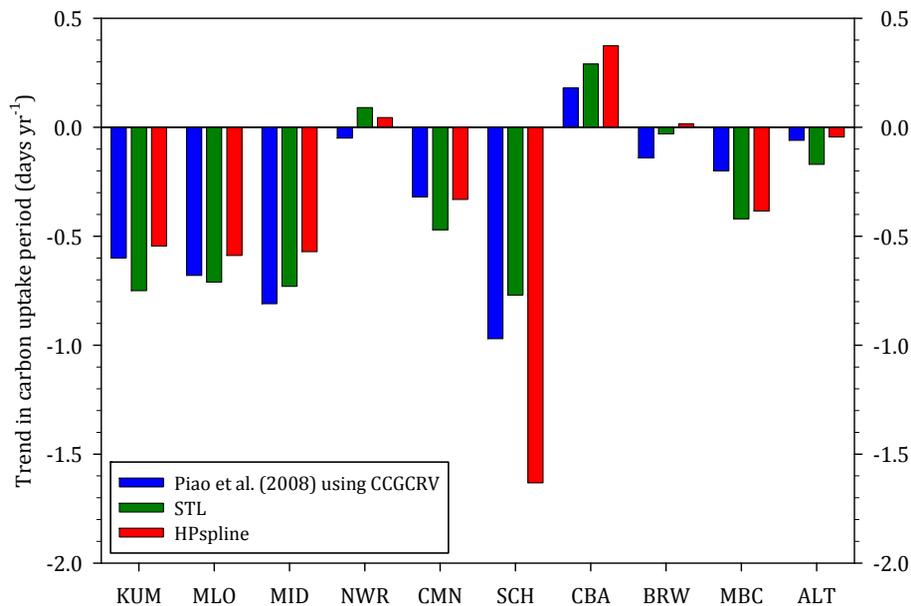


Figure 11. Carbon update period (CUP) trends calculated from 10 atmospheric CO₂ time series in the Globalview-CO₂ (GLOBALVIEW-CO₂, 2004) database. Blue bars indicate the original trends taken from Piao et al. (2008), who used CCGCRV, with green and red bars indicating the re-analysed CUP trends using STL and HPspline respectively. The atmospheric measurement stations are: Cape Kumukahi, USA (KUM), Mauna Loa, USA (MLO), Sand Island, USA (MID), Niwot Ridge, USA (NWR), Mt. Cimone, Italy (CMN), Schauinsland, Germany (SCH), Cold Bay, USA (CBA), Barrow, USA (BRW), Mould Bay, Canada (MBC), and Alert Station, Canada (ALT). Stations are all in the mid to high latitudes of the Northern Hemisphere, presented in order of increasing latitude from left to right. The mean standard error of the HPspline linear regressions is ± 0.3 days yr⁻¹, and the mean standard error of the STL linear regressions is ± 0.1 days yr⁻¹.