



Quantifying error of remote sensing observations of wind turbine wakes

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Quantifying error of remote sensing observations of wind turbine wakes using computational fluid dynamics

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Abstract

Wind-profiling lidars are now regularly used in boundary-layer meteorology and in applications such as wind energy and air quality. Lidar wind profilers exploit the Doppler shift of laser light backscattered from particulates carried by the wind to measure a line-of-sight (LOS) velocity. The Doppler Beam Swinging (DBS) technique, used by many commercial systems, considers measurements of this LOS velocity in multiple radial directions in order to estimate horizontal and vertical winds. The method relies on the assumption of homogeneous flow across the region sampled by the beams. Using such a system in inhomogeneous flow, such as wind turbine wakes or complex terrain, will result in errors.

To quantify the errors expected from such violation of the assumption of horizontal homogeneity, we simulate inhomogeneous flow in the atmospheric boundary layer, notably stably-stratified flow past a wind turbine. This slightly stable case results in 15° of wind direction change across the turbine rotor disk. The resulting flow field is sampled in the same fashion that a lidar samples the atmosphere with the DBS approach, enabling quantification of the error in the DBS observations. The observations from the instruments located upwind have small errors, which are ameliorated with time averaging. However, the downwind observations, particularly within the first two rotor diameters downwind from the wind turbine, suffer from errors due to the heterogeneity of the wind turbine wake. Errors in the stream-wise component of the flow are generally small, less than 0.5 m s^{-1} . Errors in the cross-stream and vertical velocity components are much larger: cross-stream component errors are on the order of 1.0 m s^{-1} and errors in the vertical velocity exceed the actual measurements of the vertical velocity. DBS-based assessments of wake wind speed deficits based on the stream-wise velocity can be relied on even within the near wake within 0.5 m s^{-1} , but cross-stream and vertical velocity estimates in the near wake are compromised. Measurements of inhomogeneous flow such as wind turbine wakes are susceptible to these errors, and interpretations of field observations should account for this uncertainty.

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1 Introduction

Since the emergence of a modern generation of lidar wind profilers in the mid-2000s, several commercial products have entered the market and have gained wide use for wind energy, air quality, and urban meteorology applications. Procedures have been established for ensuring traceability of the calibration of lidars and documenting uncertainty in lidar measurements (Gottschall et al., 2012). The requirement of plentiful aerosol particles for scattering the signal has been documented (Aitken et al., 2012a). Extensive interest in the complex flow in wind farms has inspired the use of both profiling and scanning lidars in wind farms to quantify turbine wakes (Käsler et al., 2010; Rajewski et al., 2013; Rhodes and Lundquist, 2013; Krishnamurthy et al., 2013; Lungo et al., 2013; Smalikho et al., 2013). Dual-Doppler (Newsom et al., 2005; Stawiarski et al., 2013; Newsom et al., 2013) and triple-Doppler (Mikkelsen et al., 2008; Mann et al., 2008; Khadiri-Yahzemi et al., 2013) approaches enable the full three-dimensional flow to be resolved. The ability of such instruments to resolve atmospheric turbulence has been explored (Sathe et al., 2011; Sathe and Mann, 2013; Fuertes et al., 2014), and lidar measurements in heterogeneous urban flow have been compared with tower measurements (Lane et al., 2013).

However, when relying on measurements from a single instrument, critical assumptions about the flow are required to estimate three components of the flow (Courtney et al., 2008). Doppler lidars sample the flow over a volume extending along the laser beam. Many lidar wind profilers exploit the Doppler shift of laser light backscattered by particulates carried by the wind. A known frequency of light is emitted from the laser, and the backscattered radiation will have a shift in frequency related to how rapidly particulates are moving toward or away from the laser source along the line of the beam or the line of sight (LOS) (Cariou, 2011). To provide profiles of wind speed and wind direction, many commercially available lidar (and sodar) systems use the Doppler Beam Swinging (DBS) technique. By shifting the beam between a series of four radial wind directions typically at approximately 60° elevation and perpendicular to each other, the

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Doppler shift (and therefore the LOS velocity) can be calculated. For pulsed lidars, all altitudes are measured based on the same pulse. Measurements at different heights are identified based on the arrival time of the backscatter compared to the initiation of the pulse.

Typically, the assumption of horizontal homogeneity over a horizontal area is invoked to interpret DBS measurements to calculate horizontal and vertical wind speeds rather than LOS velocities. However, if that assumption of horizontal homogeneity is applied to velocity retrievals in the case of inhomogeneous flow, errors in wind speed estimation will emerge.

Although DBS methods have been used with sodar (Barthelmie et al., 2003) and lidar (Nygaard, 2011; Rhodes and Lundquist, 2013; Kumer et al., 2013) to characterize wind turbine wakes, the error in DBS measurements of wind turbine wakes has not yet been quantified. Approaches to quantifying this error have been explored, but not in the context of the inhomogeneous flow near a turbine wake. The effect of complex terrain has been explored analytically (Bingöl et al., 2008) with linear flow models such as WAsP (Bingöl et al., 2009), and with Reynolds-Averaged Navier Stokes (RANS) computational fluid dynamics (CFD) models (Boquet et al., 2010; Harris et al., 2010; Meissner and Boquet, 2011; Bezault and Boquet, 2011; Gkainias et al., 2011; Butler and Quail, 2012; Bradley et al., 2012). Hasager et al. (2013) use RANS CFD to correct measurements in flow over offshore platforms. Wainright et al. (2014) use large-eddy simulation (LES) to simulate fields retrieved by sodar toward error quantification.

To date, LES CFD has not been used to simulate the wind fields as retrieved by lidar with DBS, although LES CFD can quantify the uncertainty in measurements resulting from very inhomogeneous flow such as turbine wakes. The goal of this study, therefore, is to quantify DBS error in wind turbine wake flows by employing LES of atmospheric boundary-layer flow. The full three-dimensional time-varying flow (both upwind and downwind of a wind turbine) is calculated with the model. From the full flow field, lidar “observations” are retrieved using the DBS scanning strategy, which involves sampling four beams and calculating the components of the flow from four separate LOS

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velocities. Wind profiles, or simulated towers at the lidar locations, are also extracted from the simulations. The differences between the DBS retrievals and the wind profiles quantify the DBS error in inhomogeneous flow.

To bound the error introduced by inhomogeneity in the flow, we explore a worst-case scenario of a stable atmospheric boundary layer flowing past a wind turbine. Stable layers can often exhibit considerable change of wind direction with height. Further, wind turbine wakes tend to persist longer in stable conditions with minimal background turbulence that can erode the wake, thereby introducing and maintaining significant heterogeneity in the wake. This heterogeneity is expected to challenge the DBS approach. For a lidar using the typical DBS approach with four beams, each 60° from horizontal, two opposing beams are 92 m apart at an altitude of 80 m. This horizontal distance is on the order of modern wind turbine rotor diameters. This large distance is especially problematic for measuring the cross-stream velocity, which is based on beams that span the wake – one beam may measure flow within the wake, while the opposite may be in the free stream or even on the opposite side of the wake. Furthermore, the vertical velocity measurement relies on all four beams, and different beams can measure opposite sign vertical velocity, undermining the measurement. The stream-wise velocity measurement relies on the stream-wise beams, so this measurement may be more accurate because the stream-wise velocity gradients are less extreme. However, the gradients of stream-wise velocity with respect to the stream-wise direction are strongest nearest the rotor.

To quantify the effects of these numerous sources of DBS measurement error, we perform LES of stably-stratified flow past a wind turbine. We then introduce a series of hypothetical DBS lidar observations into the upstream and the waked flow to compare the observations that would have been retrieved by a lidar using DBS in the flow to the actual characteristics of the wake as simulated. Section 2 includes a description of the simulations and the locations of the simulated DBS measurements. Section 3 presents the calculations of DBS error, including quantification of error in the stream-wise, cross-stream, and vertical velocity components. In Sect. 4, we interpret these

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results and assess their implications for future measurements of complex flows like wind turbine wakes by instruments relying on the DBS method.

2 Data and methods

Because the probe length of the lidars considered here for use with the DBS method are on the order of tens of meters long, it is critical to resolve atmospheric eddies at that scale or finer to understand the effect of such eddies on the observations. It is also necessary to capture the time variability of these eddies. Therefore, it is necessary to employ LES, which explicitly resolves the largest scales of three-dimensional atmospheric turbulence and allows them to evolve in time. These eddies are responsible for most of the turbulent transport and turbulence kinetic energy production in the atmospheric boundary layer.

It is also necessary to represent the turbine and its effects on the flow. Our simulations are based on an incompressible LES solver that includes the effects of atmospheric stratification through the Boussinesq buoyancy approximation. The solver also incorporates an actuator line model to represent the effect of a wind turbine on the flow, similar to the simulations presented in Churchfield et al. (2012a). Actuator line models (Sørensen and Shen, 2002) represent turbine blades as separate rotating lines. Simulations from this LES-actuator line tool have been compared favourably to observations at the Lillgrund offshore wind farm (Churchfield et al., 2012b).

Although we have chosen to employ an actuator line model for this investigation, a similar approach could be taken with other LES capabilities that represent wind turbines as actuator disks, where the turbine rotor is represented by a permeable circular disk with uniformly distributed thrust forces (Calaf et al., 2010; Mirocha et al., 2014; Aitken et al., 2014b). Wu and Porté-Agel (2011) compare rotating and nonrotating actuator disk models with wind tunnel measurements and find satisfactory agreement between observations and rotating actuator disk models. Martínez-Tossas et al. (2014) compare actuator line and actuator disk models, concluding that they produce similar wake

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profiles although the actuator line model can generate flow structures near the blades such as root and tip vortices that the actuator disk model cannot. Using a curvilinear immersed boundary approach, Kang et al. (2014) conclude that the actuator line model is necessary for maintaining rotation within the wake and for accurately capturing the size and turbulence levels in the far wake, as well as for capturing wake meandering. Because of the potential role of wake meandering in defining the flow inhomogeneities that may affect lidar observations, we have chosen to use an actuator line model for this investigation.

2.1 Simulations of the stably stratified atmospheric boundary layer

The LES is performed using the Simulator fOr Wind Farm Applications (SOWFA; Churchfield and Lee, 2014) developed at the National Renewable Energy Laboratory. The simulations discussed here employ the same two-stage methodology as in Churchfield et al. (2012a), briefly summarized here. Turbulent atmospheric flow is generated using the LES solver on a domain with idealized periodic lateral boundaries, without turbines, to generate a precursor simulation. A plane of turbulent data from the upwind lateral boundary is saved at every time-step once the turbulent boundary layer has reached a quasi-equilibrium state. For the simulation here, quasi-equilibrium was reached at 1.8×10^4 s. Next, a turbine is introduced into the flow that has been initialized from the quasi-equilibrium precursor flow field. Upstream boundary conditions for this inner domain are provided by the saved planes of inflow data. The outflow condition on the downstream boundary allows the turbine wake to exit without re-entering this turbine-resolving domain. More details on this procedure are presented in Churchfield et al. (2012a). For the simulations developed here, the precursor domain was 5000 m in the mean flow direction, 2500 m wide, and 750 m tall with 10 m grid resolution and a model time step of 0.025 s. The domain including the turbine was 3000 m in the mean flow direction, 2500 m wide and 750 m tall. Grid resolution in the turbine domain telescoped from 10 to 5 to 2.5 to 1.25 m near the turbine (as seen in Fig. 1).

The turbine introduced into the model is similar to the GE 1.5-MW SLE deployed at the National Wind Technology Center (Clifton et al., 2013). This upwind horizontal axis turbine has a three-bladed, 77 m rotor diameter (D) with a hub height of 80 m. Pitch and yaw angles are fixed relative to their neutral frame of reference; a variable speed torque controller is activated.

For this investigation of DBS error, we chose stable stratification because of the potential error introduced by the veering of wind with height. Additionally, because of the lower atmospheric turbulence level, turbine wakes persist farther downwind, allowing the influence of turbine wakes on lidar measurements using the DBS approach to be explored in more detail. The simulations included an imposed surface roughness of 0.1 m with a geostrophic wind that yielded an average wind speed at hub height approximately equal to 6.5 m s^{-1} . In addition, a uniform initial potential temperature profile ($\theta(z)$) was specified, with $\theta = 300 \text{ K}$ for $z < 150 \text{ m}$ and $d\theta/dz = 0.01 \text{ K m}^{-1}$ for $z > 150 \text{ m}$, creating a capping inversion. Random perturbations were imposed at the outset on the mean velocity field within the boundary layer to initiate the turbulent motion. With a surface cooling rate of $-1.4 \times 10^{-4} \text{ K s}^{-1}$ (or 0.5 K h^{-1}), a slightly stable profile developed after the 1.8×10^4 second equilibration period, with a wind shear exponent α of 0.45 across the rotor disk and a change of wind direction of 15 deg across the rotor disk, accompanied by a turbulence intensity (TI) of 4.5 % at hub height (80 m). This case is based on the stable atmospheric boundary-layer observations collected with lidars during the Crop Wind Energy Experiment (CWEX) campaign (Rhodes and Lundquist, 2013).

The numerical simulations exhibit heterogeneities in the flow that will affect DBS observations. Contours of the velocity components along the wake centerline ($y = 1250 \text{ m}$ or $y/D = 0$ in Fig. 1) show clear evidence of the turbine wake (Fig. 2). In the stream-wise component of the flow (top of Fig. 2), a wind speed deficit of 40 % is evident in both the top and bottom of the rotor disk. The wake wind speed is asymmetric, with a larger deficit in the bottom portion of the rotor disk as measured along this centerline. The deficit in the top portion of the rotor disk erodes quickly, likely because of the

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downstream (not shown), but by 3 D downwind (top of Fig. 4), this mixing has been rapidly eroded. By 7 D downwind, little evidence of the wake persists in the cross-stream component of the flow. The background shear has reestablished.

The vertical component of the flow (Fig. 5) clearly exhibits the counterclockwise motion of the wake (recall that these slices are looking upwind). At 3 D downwind, sinking motion is evident on the $y/D > 0$ side of the wake, with rising motion on the $y/D < 0$ side. This circulation is stretched but still persists through 5 D downwind, but by 7 D downstream, the magnitudes of vertical velocities in the wake are greatly reduced. Little evidence of the wake, in terms of vertical velocities, remains by 10 D downwind.

The asymmetries in the flow will affect the retrievals of wind speed estimates using the DBS method.

2.2 Lidar simulator method

To imitate the sampling approach of a lidar, probes were inserted into the flow field to measure LOS velocity components. In the DBS sampling technique, four beams, each at some angle θ from vertical (approximately 30 deg), are directed toward the north, east, south, and west, measuring the LOS velocity V_r of the flow along each beam denoted by subscripts $V_{rN}, V_{rE}, V_{rS}, V_{rW}$. The LES-calculated velocity vector (at 1.25 or 2.5 m resolution), described by components u , v , and w (stream-wise or west to east in Fig. 1, cross-stream or south to north, and vertical, respectively) is available at each grid cell in the domain. To calculate the LOS velocities $V_{rN}, V_{rE}, V_{rS}, V_{rW}$, we take the dot product of the LES-calculated velocity vector and the beam direction vector. Assuming horizontal homogeneity in the altitudes sampled, the system of wind equations becomes

$$u_L = \frac{V_{rE} - V_{rW}}{2\sin\theta}, \quad (1)$$

$$v_L = \frac{V_{rN} - V_{rS}}{2\theta}, \text{ and} \quad (2)$$

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$$w_L = \frac{V_{rN} + V_{rS} + V_{rE} + V_{rW}}{4\cos\theta}, \quad (3)$$

where u_L , v_L , and w_L describe the lidar estimates of flow in the stream-wise (west to east in Fig. 1), cross-stream (south to north), and vertical directions where w is positive for upward motion.

To simulate measurement platforms within the computational domain, the LES velocity field (u , v , and w) was sampled at 1 Hz frequency at multiple locations upwind of the turbine, downwind of the turbine, and across the wake. At each instrument location, the samples were collected along the four slanted beams (slanted at $\theta = 30^\circ$ from vertical) of a simulated vertical profiling lidar with 2.5 m vertical resolution. Two beams were aligned with the wind (V_{rE} , V_{rW}), and along the wake, and the other two beams (V_{rN} , V_{rS}), were perpendicular to the flow and across the wake. Additionally, at each location, u , v , and w were sampled along a vertical “truth beam” of the same 2.5 m resolution. The beams all sampled to a maximum height of 200 m to match typical field capabilities of commercial lidars (Courtney et al., 2008; Aitken et al., 2012). To these estimates of velocities V_{rN} , V_{rE} , V_{rS} , V_{rW} , we apply the assumption of horizontal homogeneity reflected in equations (Eq. 1–Eq. 2) to calculate the DBS estimates of u_L , v_L , and w_L . The estimated velocities u_L , v_L , and w_L can then be compared to the actual profiles of u , v , and w directly sampled from the LES field at the locations where the simulated lidar is measuring.

No model was applied for averaging along the beams. Lidars do incorporate variable range weighting functions (Banakh and Smalikho, 1997; Lindelöw, 2007; Cariou, 2011), but the emphasis here is on exploring the error introduced into measurement resulting from flow gradients that break the assumption of horizontal heterogeneity between beams at a given height, instead of any product-specific averaging along the beams.

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3 Quantification of DBS error in turbine wakes

Instruments were located upwind of the turbine to sample the inflow as well as across and on the edges of the wake, as seen in Fig. 1. We define error as the difference between the simulated measurements u_L , v_L , and w_L and the directly sampled truth measurements u , v , and w , which are based on the actual velocity profiles above the instrument locations. In such cases, the error of a component is simply given by the difference between the components:

$$E_u = u - u_L. \quad (4)$$

In other cases, it is useful to normalize these differences by the hub-height mean wind speed U_H of 6.5 m s^{-1} . As an error metric, we apply the root-mean-square (RMS) error of each velocity component, normalized by the hub-height wind speed U_H :

$$\text{RMS}_u = \frac{\sqrt{(u - u_L)^2}}{U_H}. \quad (5)$$

Normalizing by each error component locally by the corresponding wind velocity component becomes problematic for the v and w components because those components can become very small. A global RMS is a simple summation.

We also wish to explore the effect of averaging time on error. Wakes are unsteady and meander laterally and vertically. Because of this unsteadiness and the resulting gradients, a single measurement in time is more vulnerable to error than the average of many measurements, and we attempt to quantify how error changes as averaging time is increased.

3.1 Global error and the effect of averaging time

First, we explore the effect of time averaging on error, recognizing that wakes are non-stationary processes that meander. To explore this effect of time averaging in a global

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sense, we can take the hub-height free-stream mean speed normalized RMS of the error (Eq. 5) at all the simulated instruments and at all heights. This approach provides a gross single value of error for the entire set of measurements (Fig. 6). For each velocity component, this error decreases when longer averaging times are employed; the error appears to approach an asymptote for averaging times between five and ten minutes. As expected, the cross-stream (v component) error is the largest, followed by the stream-wise (u component), and then the vertical (w component). For stream-wise velocity, the global error is approximately 2 % (when normalized by hub-height inflow velocity) and decreases with larger averaging time. Because this error is averaged over all locations explored in these simulations, it is likely not an appropriate general metric. Instead, location-specific error metrics may be more appropriate for understanding specific measurement errors.

3.1.1 Error as a function of distance downstream

Perhaps the simplest case of error is that of the error along the wake centerline ($y = 1250$ m in Fig. 1, or $y/D = 0$ in Fig. 3 through Fig. 5), and we can explore that error both as a function of distance downstream (expressed in terms of x/D where D is the turbine rotor diameter of 77 m) and as a function of averaging time (Fig. 7). Notably, upstream errors are nonzero, likely because of nonstationarity in the flow, but those errors become negligible for averaging times longer than one minute in all components of the flow. Downwind of the turbine, the largest errors for all components occur in the near-wake region, between $0D$ and $2D$ downwind of the turbine. In fact, in this near-wake region, increasing the averaging time fails to decrease the error. However, upwind of the turbine and in the far-wake region, increasing the averaging time results in a reduction of error.

In the near-wake region, the DBS method is unable to accurately measure the flow regardless of averaging time because of the very large and persistent velocity gradients in this region. The v and w component error is large from $0D$ to $5D$, even compared to the free-stream hub-height wind speed (as in Fig. 6). Wake rotation, characterized

by the v - and w -velocity components, nearly vanishes beyond 5 D downstream (Figs. 4 and 5), so the reduction of error at distances past 5 D cannot be considered consequential. Therefore, measurements of wake rotation using the DBS method are questionable.

3.1.2 Error as a function of distance across the wake

Previous work (Bingöl et al., 2008, discussed further in Rhodes and Lundquist, 2013) has shown that, in homogeneous flow, DBS error in measurements of the stream-wise and cross-stream components of the flow is a function of vertical velocity. However, in a wind turbine wake, vertical velocities vary in magnitude and sign across the wake, with updrafts located on the left side looking upwind ($y/D < 0$) and downdrafts located on the right side looking upwind ($y/D > 0$). This inhomogeneity is further complicated in the stable case presented here as the wind direction changes with height such that the upper part of the wake is turned toward $y/D < 0$. As a result, larger errors in estimates of the stream-wise velocities occur on the $y/D < 0$ side of the wake (Fig. 8) even though longer averaging times clearly reduce error at most locations across the wake and at all distances downwind. The assessment of error also provides some evidence of the wake expansion as it moves downwind – the largest errors are expected to occur at the wake edges. The location of maximum error increase from $y/D = -0.6$ (at $x/D = 3$) to $y/D = -1.2$ (at $x/D = 5$) to $y/D = -1.8$ (at $x/D = 9$) for the shortest averaging time. Of note, the location of maximum error is not the same for all averaging times, especially in the far-wake regions of $x/D \geq 7$, which we attribute to wake meandering at these distances.

At all distances downwind and all locations across the wake, the maximum normalized RMS error in the stream-wise component is less than 4 % of the free-stream hub-height wind speed, considering all heights within the rotor disk. Wake velocity deficits are on the order of 40 % of the free-stream hub-height wind speed.

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3.2 Velocity error as a function of height along the wake centreline

Comparisons of the DBS-retrieved velocities to the actual velocities along the wake centreline emphasize the vulnerabilities of the DBS method even in the centre of the wake (Fig. 9). The stream-wise velocity estimates (left panels) are based on the two beams parallel to the stream-wise flow, and so even in the near-wake region, the errors are very small, particularly in comparison to the free-stream velocity. However, the rotation of the wake shown in the cross-stream component (middle panels of Fig. 9) is cancelled out by the DBS method at both 3 D and 5 D downwind of the turbine, although the overall change of wind direction with height in the domain is reasonably well-captured by the DBS method. The inhomogeneities in the wake are not captured in the method used to estimate velocity from the DBS method, but these inhomogeneities reduce as the wake propagates downstream. Therefore, by 7 D downstream (not shown), when the cross-stream components again become small, the errors between the DBS estimates and the actual cross-stream velocity become negligible. Similarly, the errors in DBS estimates of the vertical velocity are very large between the turbine and 5 D downwind (right panels of Fig. 9) because of the large vertical velocities in the near-wake region. Even by 7 D downstream, agreement between the DBS estimates of vertical velocity and the actual vertical velocity has not been attained along the wake centreline.

3.3 Velocity error profiles across the wake

Large inhomogeneities are expected at the edge of the wake because of the contrast between the wake flow and the free stream flow. We also expect inhomogeneities in the centre of the wake caused by the wake rotation. To quantify the error in wind speed estimates based on the DBS approach, we inspect the profiles of error (Eq. 4) at instruments located on the edges of the wake in comparison to the errors from locations in the centre of the wake (along $y/D = 0$).

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The largest errors are found in the row of instruments closest to the turbine, at $x/D = 1$ (Fig. 10, top row). Although the stream-wise errors (top left panel of Fig. 10) are small on the wake edges, these errors approach 0.5 m s^{-1} at the centre of the wake. The cross-stream velocity errors (top centre panel of Fig. 10) are considerable throughout the wake, approaching 1 m s^{-1} at all locations within the wake. The vertical velocities (top right panel of Fig. 10) are generally overestimated on the side of the wake with rising motion (red line, $y/D < 0$) and underestimated on the side of the wake with sinking motion (blue line, $y/D > 0$).

These errors decrease as the wake propagates downwind of the turbine. By 3 D downwind (centre row of Fig. 10), the maximum error in the stream-wise component (centre left panel) is less than 0.3 m s^{-1} , with the greatest error near the top of the rotor disk for a measurement at the edge of the wake on the rising side. The cross-stream component (centre panel) still suffers from significant error, near 0.5 m s^{-1} at all locations across the wake and exceeding 0.5 m s^{-1} in the centre of the wake. The DBS estimates of the vertical velocity component (centre right panel) exaggerate the rising motion near the top of the rotor disk on the side of the wake with rising motion (red line, $y/D < 0$). The DBS error also overestimates vertical motion in the bottom of the rotor disk on the side of the turbine with general sinking motion. Because the errors in estimates of vertical motion are on the order of the vertical velocities themselves, the DBS approach should not be considered reliable for estimates of vertical velocities in this region of the wake.

Farther downwind, errors are generally reduced. At 5 D downwind (bottom row of Fig. 10), the largest percentage error is in the vertical component (bottom left panel) from the lidar located near the centreline, although the cross-stream errors are still large in the centre of the wake and at the top of the rotor disk at the location on the rising side of the wake. By 7 D downwind (not shown), the error in the stream-wise component is negligible, but errors in the cross-stream component are on the order of 0.2 m s^{-1} .

4 Discussion and conclusions

Numerous commercial lidar and sodar systems use a DBS technique to estimate winds for wind energy, air quality, and urban meteorology applications. Using LES of stable atmospheric boundary-layer flow past a wind turbine, we have quantified the error expected from observations collected using the DBS measurement approach in the vicinity of a wind turbine wake. The three-component velocity vectors calculated by the LES are converted into LOS velocities representative of lidar technology using four beams and the DBS method. These LOS velocities are then used to calculate the wind field estimates that would have been observed by instruments located within this flow. The difference between these DBS estimates of winds and the actual wind profiles at the instrument locations are used to quantify the error that can be expected from the application of the DBS approach in heterogeneous flow.

These stable atmospheric boundary-layer simulations represent a worst-case scenario of single-instrument measurement error, given the heterogeneous flow across the measurement volume resulting from the wind turbine wake, as well as the significant (15°) change of wind direction across the altitudes of the turbine rotor disk with rotor diameter D. These results provide reasonable error bounds for remote sensing observations of wind turbine wakes using the DBS approach. For the case simulated here, time averaging of the observations of at least five minutes can eliminate some of the error in the observations, notably for the upwind measurements and the far downwind measurements ($x > 5D$) aligned with the flow along the wake centreline.

The largest DBS-related errors are found in the near-wake region, between the turbine and 2D downwind of the turbine, and at locations where the wake rotation induces significant cross-stream and vertical velocities (both the wake edges and along the wake centreline). Although stream-wise velocity errors in this near-wake region are less than 0.5 m s^{-1} at 1D and 2D downwind in the regions of the rotor disk altitudes, the cross-stream velocity errors are on the order of 1.0 m s^{-1} and the vertical velocity errors are on the order of 0.2 m s^{-1} (in excess of actual vertical velocities). Therefore,

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DBS-based assessments of wake wind speed deficits based on the stream-wise velocity can be relied on even within the near wake within 0.5 m s^{-1} , but cross-stream and vertical velocity estimates in the near wake are compromised. These errors are larger for shorter time-averaging periods for these equilibrated and stationary simulations. Of course, part of the near-wake error is due to the fact that the DBS beams may be sampling outside of the wake, especially in the upper portion of the rotor disk. This error can be accounted for in the analysis of results (Rhodes and Lundquist, 2013).

The DBS approach has been used to characterize wind turbine wakes with sodar (Barthelmie et al., 2003) and with lidar (Nygaard, 2011; Rhodes and Lundquist, 2013; Kumer et al., 2013), and has also been applied to complex urban flows (Lane et al., 2013). As shown here, measurements of inhomogeneous flow such as wind turbine wakes are vulnerable to errors, and interpretations of field observations should account for this uncertainty, beyond the uncertainty in the radial velocity measurements provided by the manufacturers of the instruments. The limitations presented here do not undermine the benefits of DBS-based systems, which include the ability to rapidly profile winds at multiple altitudes simultaneously. In fact, we suggest that combining DBS-style instruments with more flexible instruments that can use scans with other geometries to measure winds can enable greater insight into complex flows like wind turbine wakes (as in Smalikho et al., 2013 and Aitken et al., 2014a). Comparisons between in situ instruments such as unmanned aerial systems (Lawrence and Balsley, 2013) and DBS-based instruments can also help bound uncertainty.

The methodology presented here, which uses LES to calculate simulated observations, can be refined and extended to other applications. For example, the effects of the turbine tower, nacelle, and rotor tilt could be included (as in the actuator disk modeling of Aitken et al., 2014b). Simulation capabilities that fully resolve all elements of the turbine (Kang et al., 2014) can be compared with our results to determine if there are important effects from tip vortices. Because lidars are being used in urban meteorology (Lane et al., 2013), it is probably important to establish how the complex and heterogeneous flow in urban areas affects the error in the DBS technique used there. LES

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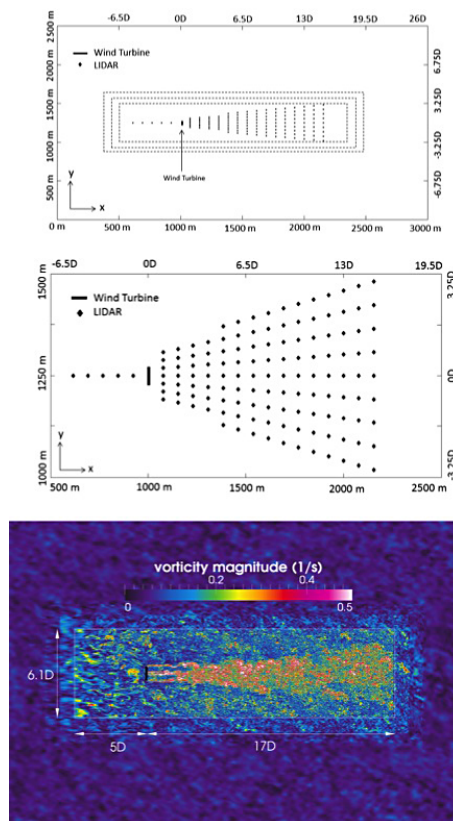
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Figure 1. Simulation domain for precursor and turbine-resolving domains (top), with zoomed-in version (center) identifying lidar locations in the wake of the wind turbine and contours (bottom) of vorticity in the turbine-resolving domain. The nests (top) denote the regions with grid refinement from 10 to 5 to 2.5 to 1.25 m resolution. Flow is from west to east at the turbine hub height.

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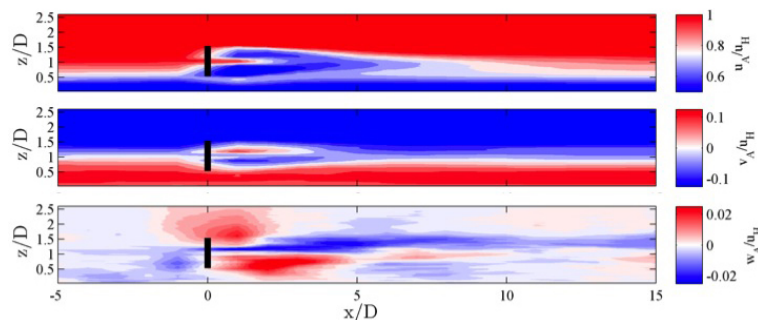


Figure 2. Ten-minute-averaged contours of wind speed in the stream-wise (top), cross-stream (middle), and vertical (bottom) directions, normalized by average hub-height inflow wind speed (6.5 m s^{-1}), taken along the turbine location at $y = 1250 \text{ m}$ (Fig. 1) after equilibration.

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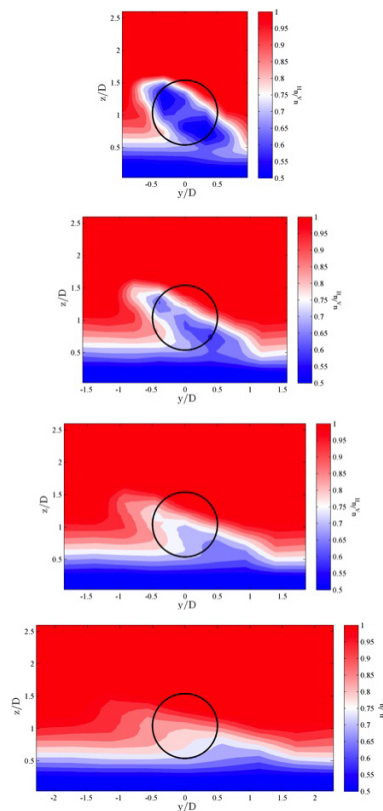


Figure 3. Cross-stream slices of stream-wise velocity, normalized by upwind hub-height velocity (6.5 m s^{-1}) at 3 D (top), 5 D, 7 D, and 10 D (bottom) downwind of the turbine. The perspective is looking upwind. The large black circle outlines the location of the turbine rotor disk inscribed by the actuator line model.

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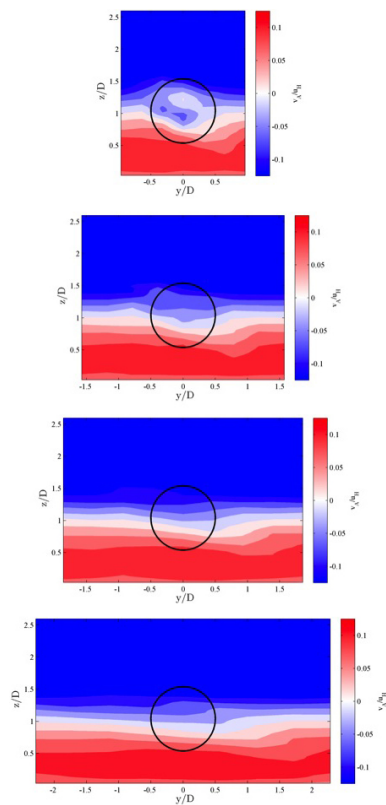


Figure 4. Cross-stream slices of cross-stream velocity, normalized by upwind hub-height velocity (6.5 m s^{-1}) at 3 D (top), 5 D, 7 D, and 10 D (bottom) downwind of the turbine. The perspective is looking upwind. The large black circle outlines the location of the turbine rotor disk inscribed by the actuator line model.

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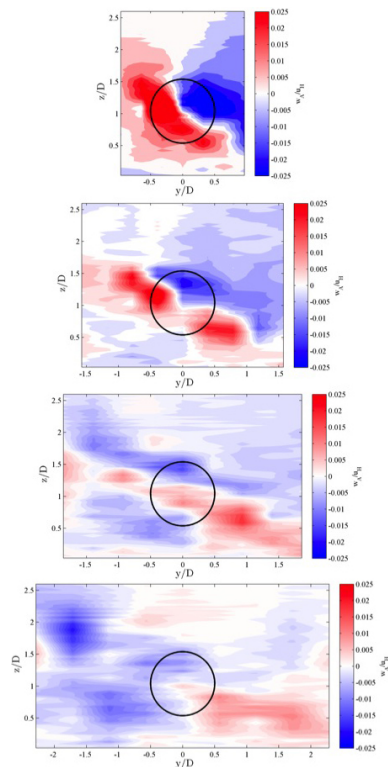


Figure 5. Cross-stream slices of vertical velocity, normalized by upwind hub-height velocity (6.5 m s^{-1}) at 3 D (top), 5 D, 7 D, and 10 D (bottom) downwind of the turbine. The perspective is looking upwind. The large black circle outlines the location of the turbine rotor disk inscribed by the actuator line model.

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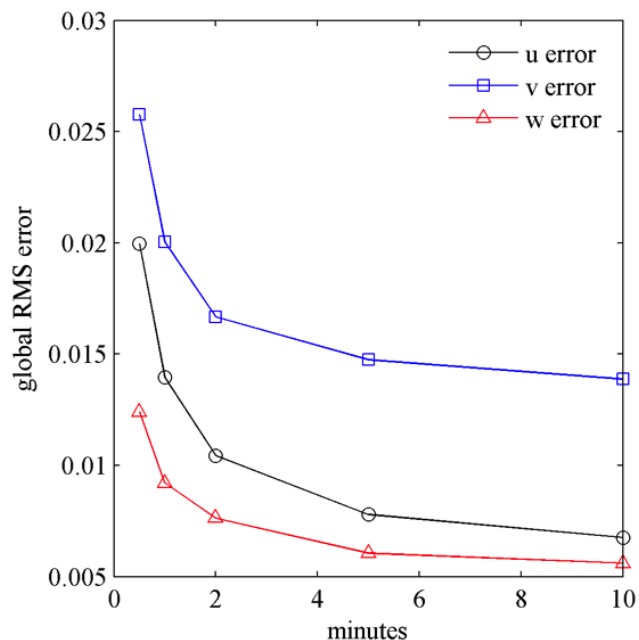


Figure 6. RMS global error (normalized by hub-height wind speed U_H of 6.5 m s^{-1}) at all lidar locations and all heights, normalized by the free-stream hub-height wind speed, as a function of averaging time.

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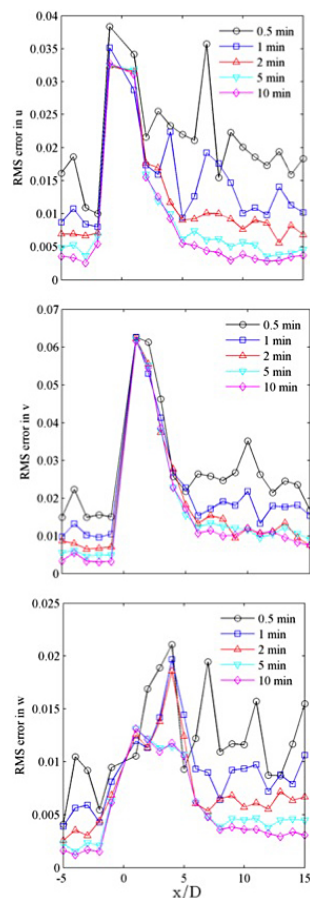


Figure 7. RMS global error (normalized by hub-height wind speed U_H of 6.5 m s^{-1}) for each lidar situated along the turbine-wake centerline ($y = 1250 \text{ m}$ and $y/D = 0$ in Fig. 1). Stream-wise error (top), cross-stream error (middle), and vertical velocity error (bottom). Each color represents a different amount of time averaging.

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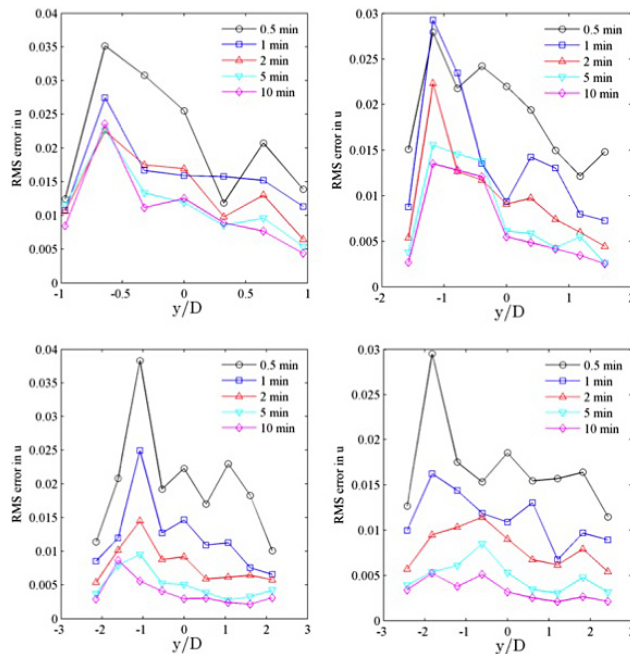


Figure 8. RMS global error (normalized by hub-height wind speed U_H of 6.5 m s^{-1}) in the stream-wise component across the wake at different distances downstream: $x/D = 3$ (top left), $x/D = 5$ (top right), $x/D = 7$ (bottom left), $x/D = 9$ (bottom right); the different colors denote averaging times.

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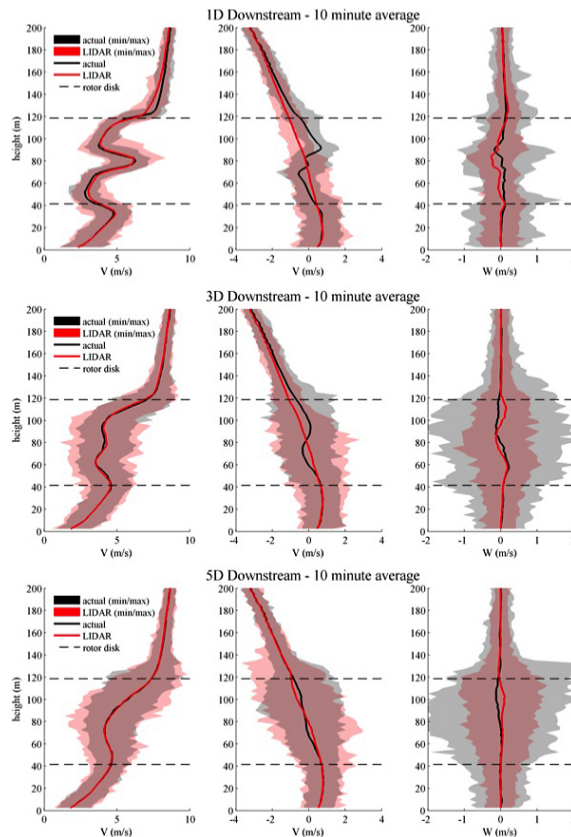


Figure 9. Vertical profiles of the stream-wise (left), cross-stream (middle), and vertical (right) components of wind speed at different locations downstream of the turbine on the wake centreline $y/D = 0$ as measured by the simulated lidars (red lines) and directly sampled from the LES (black line). The shaded regions represent the envelope of all sampled values from the simulated lidar (pink) and from the direct LES sampling (gray).

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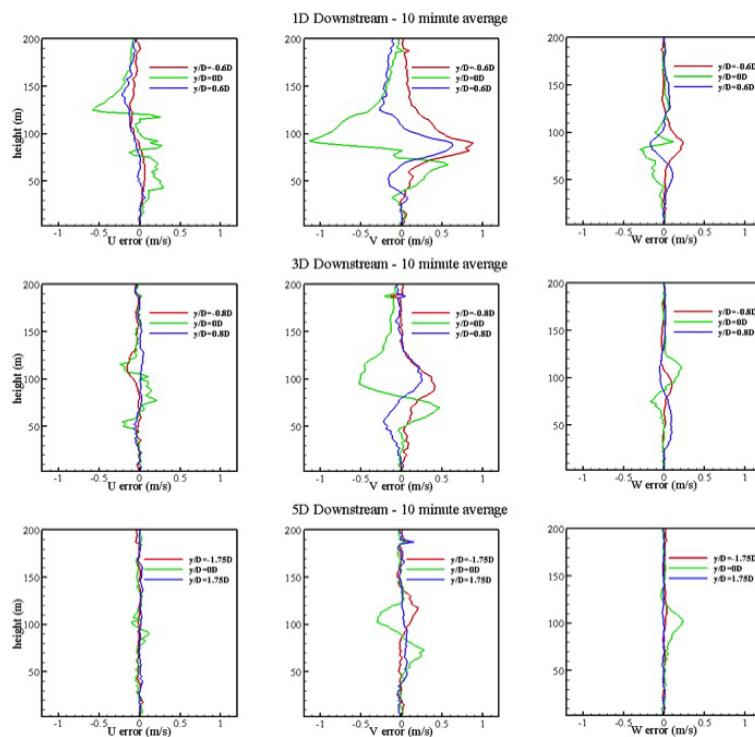


Figure 10. Profiles of error (Eq. 4) in lidar measurements of stream-wise (left), cross-stream (center), and vertical (right) velocity from lidars located 1 D (top), 3 D (center), and 5 D (bottom) downwind of the turbine. Locations of the lidars are at the center and the cross-stream edges of the wakes as labeled in the figures.

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