

## amt-2014-320: Response to reviews

We are very grateful for the appraisals of this two-part study, particularly given the time required to assess both papers together. We thank the reviewers for their positive feedback and valuable suggestions for improving the manuscripts. All comments have been taken into account. Detailed responses to each point are provided below (in bold type), followed by the revised manuscript with the changes indicated.

*Interactive comment on “Infrared and millimetre-wave scintillometry in the suburban environment – Part 1: Structure parameters” by H. C. Ward et al.*

*B. van Kesteren (Referee)*

The authors present a two-part study in which they present the results of the first long-term application of an optical-microwave scintillometer system over Swindon, UK. In the first part, they present the results in terms of structure parameters and in the second part they present the results in terms of the heat fluxes.

Indeed, both manuscripts present research novel in many aspects. The application of a combined optical-microwave scintillometer system has been presented before, but never for such an extensive time period, nor over the city centre. This first part is addressing many technical issues at a high scientific level. They show strengths and weaknesses of all the scintillometric methods, as well as those of eddy-covariance measurements. On occasion the first manuscript points a bit too much towards the second manuscript to my opinion; the technical results and the results of the structure parameters already have value in themselves. Nevertheless, the manuscript is generally of a high scientific quality, presenting innovative results, and very well written, so that I recommend publication after minor revisions.

P 11171 – 17773, Introduction – the introduction gives a remarkably good overview of the state of the art in recent and older literature. Nevertheless, the part describing the objectives of this study (P 11173, line 24ff) is rather limited. To my opinion it does not get clear to readers who are not so familiar with the topic what this study contributes to the literature. It is stated that the presented dataset is “by far the longest dataset that uses these techniques”, but it has not been stated yet, how long this period is. Furthermore, the sentence “Methodological considerations (...) and seasonality are explored” is rather vague and saying little. To my surprise, the conclusion, section 6, actually does a much better job in describing this relevance. Hence, the authors should make it more clear in the introduction already what this study contributes.

- **The length of the dataset (14 months) is now stated in the Introduction. The sentence beginning ‘Methodological considerations...’ has been deleted and the following text added to better describe the purpose of this paper: ‘The performance of the techniques under different conditions, and their strengths and weaknesses, are examined. This paper offers insight into the behaviour of the structure parameters and  $r_{Tq}$  at various timescales (daily, seasonal and inter-annual), including how they respond to energy and water availability, surface cover and changing meteorological conditions.’**

P 11170, Line 9 – “unique”, the use of this word is somewhat confusing here. It raises the thought that a rather exotic scintillometer is used, and with that the question on the representativeness of the results presented here. I would leave it out here.

- **‘unique’ has been deleted.**

P 11170, line 11-12 – “humidity fluctuations and the so-called”, add a comma between “fluctuations” and “and”.

- **Done.**

P 11170, line 12 – this sentence is hard to understand when one does not know the contents of the paper already. In itself the pairing of the two wavelengths already offers sensitivity to the humidity and temperature correlation. Mentioning the bi-chromatic method for this purpose is therefore unclear at this point when not introducing the two-wavelength method as well.

- **This has been rephrased as, ‘the correlation between wavelengths is also used to retrieve the path-averaged temperature-humidity correlation’.**

P 11170, line 15 – to what does “the techniques” refer?

- **Changed to ‘measurement techniques’.**

P 11170, line 20-21 – “The energy (...) companion paper.”, it is unclear to me what this sentence is meant to say here, because you already introduced the companion paper before (line 9).

- **We refer back to the second paper at the end of the abstract to emphasise that this is a two-part study and the analysis (in terms of structure parameters in Part 1) continues (in terms of fluxes) in Part 2.**

P 11171, line 12 – “refraction”, it results from diffraction. Rewrite.

- **Changed to ‘diffraction’.**

P 11171, line 12 – introduce a semicolon after “beam” for readability

- **This sentence has been rewritten (see response to next point).**

P 11171, line 13 – the refractive index of an eddy is not determined by the density of constituent ones as is written here. Instead, the refractive index is defined as the factor with which the speed of an electromagnetic wave (speed of light,  $c$ ) in a medium is reduced as compared to that in vacuum. Hence, the refractive index of an eddy is determined by the temperature and moisture content of the eddy itself. Rewrite.

- **This sentence has been rewritten as, ‘Variations in the received intensity result from diffraction as turbulent eddies move through the beam, their refractive indices determined by their densities which, in turn, can be related to their temperature and moisture content (e.g. Meijninger 2003).’**

P 11171, line 17 – “humidity fluctuations are also important”, writing it down like this suggests that temperature fluctuations are still important for millimetre or radiowaves, whereas their effect is rather limited. Rewrite

- **Changed ‘also important’ to ‘more important’.**

P 11171, line 18 – “Peak sensitivity”, sensitivity to what?

- **Changed to read ‘Scintillometers are most sensitive to fluctuations occurring towards the centre of the path’.**

P 11171, line 21 – suggest to delete “other”.

- **Done.**

P 11172, line 1-2 – “On the whole, (...) are-averaged fluxes.”, how did these studies determine the blending height, that this conclusion can be drawn from them?

- **The common approach (to-date) to assess scintillometry fluxes is through comparison of area-averaged fluxes derived from scintillometry with fluxes from several eddy covariance stations aggregated to match the footprint of the scintillometer (e.g. Meijninger et al. (2002b), Ezzahar et al. (2007), Evans et al. (2012)). Ezzahar et al. (2007) conclude that scintillometry can be used below the blending height (a value of 26 m is stated). Their setup comprised two scintillometers installed below the blending height over an olive yard with patches of contrasting soil moisture. Estimates of the sensible heat flux and refractive index structure parameter derived from scintillometry and eddy covariance were compared. Meijninger et al. (2002b) used two scintillometers at different heights over mixed agricultural land and found better agreement with the higher scintillometer (installed above the blending height), but that the agreement with the lower scintillometer (sometimes below the blending height) could be improved by accounting for the composition of the footprint. Evans et al. (2012) found good agreement between fluxes from a scintillometer installed above the blending height and aggregated EC fluxes, also over mixed agriculture. In these latter two studies, the blending height was estimated following Wood and Mason (1991).**

P 11174, line 8, This definition of structure parameters in this line does not suffice. It perfectly applies to variances as well. However, in contrast to variances, the structure parameter is not dependent on the ensemble average of  $\gamma(x)$ , because the structure parameter considers, as Tatarskii expresses, only fluctuations smaller than the spatial separation  $\delta$ . Rewrite.

- **For the purposes of the paper, the key point is that structure parameters are a measure of the strength of turbulent fluctuations (and they can be obtained from scintillometry and converted to fluxes via MOST). The sentence has been modified slightly to read, ‘Structure parameters describe the intensity of turbulent fluctuations in the atmosphere.’**

P 11175, line 1-4 – AT and Aq are given in Ward et al. (2013b) as AT and Aq. I guess the latter instance of AT should be At? Otherwise the sentence makes no sense.

- **Thank you for the correction. This appears to be an error introduced in the typesetting. Yes, the text should read, ‘...given in Ward et al. (2013b) as  $A_r$  and  $A_q$  (see their Table 2).’**

P 11175, line 10 and Eq. (4). – “can be approximated”, this formulation rightly suggest that the “=”-sign in Eq. (4) should be replaced by an “≈”-sign.

- **Done.**

P 11175, line 13 – “typical atmospheric conditions”. The question is: typical for where and when? Tropics? Swindon during summertime? Swindon during wintertime? Be more specific.

- **‘(T = 300 K and pressure (p) = 10<sup>5</sup> Pa)’ (Moene 2003) has been added to the text.**

P 11176, line 16 – put a comma after “method” and delete “obtained” for readability

- **Done.**

P 11177, line 1 – “most assumptions”, what is meant with this? Maybe, “MOST assumptions”?

- **Thank you for the correction. This appears to be an error introduced in the typesetting. Yes, the text should read, ‘If MOST assumptions’.**

P 11177, line 11 – this sentence is formulated somewhat confusing. I guess that plotting  $C_{n2n2}$  versus  $\beta$  “reveals” the minimum, rather than letting it “occur”.

- **Agreed: ‘occurs’ has been changed to ‘is revealed’.**

P 11177, line 16-18 – “In practice, (...) of the instrument.”, this sentence is vague. Please reformulate. So far as I get it, there is a region, where  $C_{n2n2}$  is biased due to the bad SNR. Is that correct?

- **Yes, that appears to be the case. These sentences have been reworded as follows: ‘In practice, zero  $C_{n2n2}$  will not be observed because the instrument has a finite noise floor (and  $r_{Tq} \neq 1$ ). Instead the scintillation signal may be close to, or below, the detection limit of the instrument, resulting in reduced sensitivity around the region of minimum  $C_{n2n2}$  and a tendency for the derived  $\beta$  to be biased away from (below) the value at which minimum  $C_{n2n2}$  occurs.’**

P 11177, line 19ff – do the authors describe a new aspect of the above presented equations from “For low  $\beta$ , (...)” onwards? If not, then it is unclear to me how the  $C_{n2n2}$  minimum relates to these last sentences.

- **These sentences have been moved earlier in the paragraph, after  $S_{22}$  is first introduced.**

P 11179, line 20ff – METsub was installed at a height of 10m a.g.l. Could the authors elaborate whether these measurements were scaled to fit the scintillometer effective height?

- **Temperature, relative humidity and pressure were not scaled from the 10.6 m measurement height to the scintillometer effective height of 45.0 m. Sensitivity to these input variables has been shown to be small (Hartogensis et al. 2003; Ward et al. 2014b).**

**Wind speed can be more important. The height of the wind speed measurement has been accounted for in the estimation of  $u_*$  for calculation of the fluxes.**

P 11181, line 26 –  $\sigma_{\chi}^2$  does not depict the covariance, maybe the authors can add  $\sigma_{\chi_1 \chi_2}$  (c.f. Eq. 14c)? Furthermore, the relation between the intensity measurements and the log-amplitude (co)variances does not become clear from this paper. I think it should be shown that  $\text{var}(\ln(I)) = 0.25\text{var}(\ln(\chi))$ , or change it in the equations altogether.

- **This sentence has been modified to read, ‘At 10-min intervals the variances, covariance and mean values of the signals were calculated, from which the log-amplitude variances ( $\sigma_{\chi_1}^2, \sigma_{\chi_2}^2$ ) and covariance ( $\sigma_{\chi_1 \chi_2}$ ) were obtained (Tatarski 1961).’**

P 11182, line 21-24 – “For the MWS (...) along the BLS-MWS path.”, does fog also affect the MWS signal?

- **Although the MWS beam can propagate further through fog than the BLS beam, the 94 GHz signal is still affected by water droplets in the atmosphere. Rejection of data is based on signal intensity thresholds, so it is not known whether the inferred beam obscuration is due to rain or fog, or other matter (e.g. dust, birds). The decision was taken to remove MWS data at times when the BLS signal intensity suggested the optical beam was obscured to ensure that the resulting datasets are of high quality, i.e. to exclude times when variations in signal intensity may be due to processes other than scintillation.**

P 11182, line 27 – what do the authors mean with “reasonable thresholds”?

- **Data were excluded when  $C_{n1n1} > 1.5 \times 10^{-14} \text{ m}^{-2/3}$ ;  $C_{n2n2} > 1.5 \times 10^{-12} \text{ m}^{-2/3}$ ;  $C_{n1n2} < -2.0 \times 10^{-13} \text{ m}^{-2/3}$  or  $C_{n1n2} > 3.0 \times 10^{-13} \text{ m}^{-2/3}$ . These thresholds were not explicitly given in the paper because they are fairly arbitrary, specific to this setup and the number of points outside these thresholds was very small (ten in total).**

P 11184, line 1 – could the authors elaborate on how well this methodology works during clouded weather or during winter time?

- **Using the positions of twice-daily minima in  $C_{n1n1}$  to mark a change of stability from unstable (daytime) to stable (night-time) generally worked well for this dataset. The transition times obtained are mostly similar to the transition times indicated by the EC station and the seasonal variation in identified transition times was as expected (i.e. more unstable hours in summer than winter). The EC data show that, for this suburban site, the atmosphere tends to be unstable during the day (although only for a short time around midday in winter) and stable at night (Ward et al. 2013a). Therefore, it is usually valid to assume there will be two stability transitions per day (at other sites this may not been the case and this methodology may not be suitable). The method was found to work less well in winter than summer as the transitions are often less well defined, stability can remain neutral (or close to neutral) throughout the day/night and there may be several transitions between slightly stable/slightly unstable conditions per day. Cloudy days were not usually problematic, although on a few occasions sudden cloud cover during sunny summer days led to a sharp dip in  $C_{n1n1}$  which were initially flagged erroneously as one of the minima indicating a stability transition. The algorithm was modified to include additional checks to**

handle these complications where possible. The cumulative daily net radiation was used to test if the minima identified could be due to sudden cloud cover; it was checked whether the positions of the identified minima were unrealistically close together; and time restrictions on the morning (after 0400) and evening (before 2100) transitions were imposed. If these checks were failed, the initial minimum identified was rejected and further minima were found.

- The following text has been added to Section 5.1.1: ‘Using the positions of  $C_{nInI}$  minima to indicate the stability transition times generally worked well for this dataset, although performance was poorer in winter when stability changes tend to be less well defined and conditions may remain close to neutral throughout the day. Following the method described in Samain et al. (2012a), additional restrictions were imposed on the times of morning (here after 0400 UTC) and evening (before 2100 UTC) transitions. In a few cases, cumulative daily net radiation was also used to distinguish  $C_{nInI}$  minima that were due to sudden cloud cover during daytime from  $C_{nInI}$  minima that were due to a change of stability.’

P 11185, line 14-15 – only experts will get what the authors imply here. I think they mean the path averaging over the licor and sonic sensors and their respective separation distance? Be more specific and give the corresponding references (Hill, 1991, Phys. Fluids A 3, 1572-1576 and Hartogensis, 2006).

- This sentence has been modified to read, ‘No corrections were made for spectral losses due to the spatial separation of the sonic and IRGA and their finite path lengths, which can be expected to result in underestimations of about 5–7% (Hill 1991; Hartogensis et al. 2002).’

P 11186, line 4 – “sharp minima”, sharp minima are not visible from the plots of figure 5a or 5b. The point the authors try to make in line 4-5, can only be illustrated when the corresponding figures have their y-axis logarithmically scaled. Hence, I would recommend to scale the y-axis of Fig 5a and 5b logarithmically, rather than linearly.

- Figure 5a, b has been changed to a log scale.

P 11188, line 9 – “means evaporation”, these two words seem to interrupt the flow of the sentence and work confusing to me. I would recommend suitable punctuation for readability.

- This has been rephrased as, ‘In terms of fluxes, evapotranspiration continues throughout winter because moisture is readily available, whereas energy is limited so  $Q_H$  is directed towards the surface for much of the daytime, only becoming positive for a short time around midday (Ward et al. 2013a).’

P 11190, line 20 – add a comma after “theory”.

- Done.

P 11193, line 16-17 – recommend to rewrite “higher in the atmospheric boundary layer than is ideal,” to read “to be above the surface layer,”

- **The text, ‘likely higher in the atmospheric boundary layer than is ideal’ has been changed to, ‘possibly above the surface layer’.**

P 11193, line 19ff – Solignac (2012) indicates that high-pass filters may artificially reduce  $C_n^2$  at low crosswinds, i.e. cause underestimation of  $C_n^2$ . To what extent do the authors think that their filter of 0.06 Hz affects the estimates of  $C_n^2$  and  $C_n^2$ ? This is an aspect that needs to be discussed at latest in this paragraph.

- **The suitability of different filter frequencies was investigated based on spectra and comparison of results (structure parameters and fluxes) for a range of different filter options. The value of 0.06 Hz used here is the same as that used by Lüdi et al. (2005). Altering this frequency slightly did not produce substantial changes to the results, whereas using much lower or higher frequencies was seen to impact both the spectra and magnitude of the results. The value of 0.06 Hz was therefore judged to be suitable for this dataset, but it is not critical that this exact value is used. Further research and development of a filter that varies according to atmospheric conditions (i.e. wind speed) may be an important area of future research. However, the poor performance at low crosswind speeds discussed in this paragraph could not be explained by the choice of filter frequency.**
- **The following text has been added to the end of the paragraph: ‘Given that the position of the spectrum is known to change with wind speed (Medeiros Filho et al. 1983; Nieveen et al. 1998; Ward et al. 2011), and that  $C_n^2$  can be underestimated if the filter excludes part of the scintillation signal under very low wind speed conditions (Solignac et al. 2012), the suitability of the bandpass filter was also re-examined. However, the choice of filter frequency did not seem to explain the poor performance and modifying the filter frequencies did not resolve the issues. Small changes in filter frequency generally did not produce substantial changes to the results, suggesting that the frequencies chosen are suitable for this dataset, but it is not critical that those exact values are used.’**

Another issue related to low crosswinds and recently analyzed in Lindenberg is the following: At low crosswind, the friction velocity usually is low as well, indicating that the inner scale length is large. Hill and Clifford (1978) indicate that  $D/l_0 > 20$  suffices for ignoring the spectral bump in the spectrum. Nevertheless, for the LITFASS set-up (4.8 km path, 43 m a.g.l.), a positive bias of  $C_n^2$ , resulting from ignoring the  $l_0$ -dependence of the spectrum, is as large as 30% for  $u^*$  going to zero. The issue is described in more detail in Hartogensis (dissertation from 2006), appendix 5a. The effect of ignoring the bump on  $C_n^2$  and  $C_n^2$  is negligible. This information is just given here for consideration, and it would be great if the authors could elaborate their thoughts on it.

- **In urban environments, the friction velocity is rarely very small (due to the roughness of the surface and additional energy supply from anthropogenic activities); the EC data indicate  $u^* < 0.1 \text{ m s}^{-1}$  for less than 3% of the dataset. The inner-scale effect is therefore expected to be relatively small for our setup, but we agree it may constitute another issue with the scintillometry technique at low (cross)wind speeds. This interesting topic would be a useful area for future study.**

P 11197, line 12 – add “of the first kind and zeroth and first order.” After “Bessel functions”.

- **'of the first kind' has been added after 'Bessel functions'.**

P 11198, Eq. A1 – the term  $J_0(K|d|)$  is only valid when the receivers and detectors of both scintillometers are identically separated at each side, otherwise the term should become  $J_0(K|d|(1-x/L)+dr(x/L)|)$ , see Lüdi et al., Eq. (9) or Hill and Lataitis (1989) Eq. (1).

- **$d$  is now defined as the beam separation.**

P 11198, line 6 – I recommend removing “is often applied”.

- **Modified accordingly.**

P 11198, line 11 – change “size of the Fresnel zone” to “maximal diameter of the first Fresnel zone”

- **Done.**

P 11198, line 11 – the variable “ $F$ ” has not been defined before. Furthermore, I recommend giving its definition as well “ $F = \sqrt{\lambda L}$ ”

- **Done.**



Interactive comment on “Infrared and millimetre-wave scintillometry in the suburban environment – Part 1: Structure parameters” by H. C. Ward et al.

Anonymous Referee #2

Single review of both of the companion papers:

----- Overall comments / thoughts: -----

\* A positive contribution to land-surface interactions, micro-meteorology, and scintillometry. This paper will certainly move science forward.

\* Excellent quality figures (science and presentation).

\* A very thorough work.

\* In particular, Fig1 in the second paper is very important and nicely laid out.

\* Language is almost flawless.

\* It is a rare pleasure to review work of both high quality science and presentation.

----- Suggestions for improvements in general throughout the manuscripts: -----

\* Can the uniqueness (a world first) of this work be more upfront, e.g. in the Highlights?

- **The Introduction has been modified to more clearly state the objectives and contributions of this work (please see responses to other comments).**

Some specific comments:

PAPER-A: ---

11172/6 » "derive" sounds exact/precise, maybe "estimate" is better.

- **‘derive’ has been changed to ‘obtain’.**

11172/3 » Blending height and roughness sublayer are not well used in our field. Often there are two issues being combined. Can you make it clearer? (a) Blending height - we are thinking about averaging out horizontal heterogeneities (even for different surfaces of similar height). (b) Roughness sublayer is about considering differences in obstacle height (even for the same surface type). (See also other places in text)

- **The roughness sublayer describes the portion of the atmosphere directly surrounding the roughness elements (obstacles such as trees, buildings, etc) and extending from the surface up to a height of about  $2z_H$  or more (Raupach et al. 1991). In the roughness sublayer, the flow is highly complex as it is distorted by the individual roughness elements.**
- **The concept of a blending height is used to describe the height above which the impact of surface heterogeneity is no longer important, i.e. where the influence of individual patches of different surface properties are averaged out, or blended together, by turbulent mixing.**

- **The term ‘roughness sublayer’ is not used in either paper but the blending height concept is now clarified in Section 3.1 (‘i.e. high enough that turbulent mixing averages out the influence of surface heterogeneity’).**

Table 1 » Do you need a column for  $z_H$  also?

- **Given that  $z_0$  and  $z_d$  have been estimated from  $z_H$  by a simple multiplication, we decided not to include  $z_H$  in Table 1 as well.**

Figure 5 » Is a log scale needed here?

- **Figure 5a, b has been changed to a log scale.**

Figure 6 » The figure would be easier to interpret if something else like  $Q_H$  or  $Q^*$  was plotted (or their sign), so one can see the transitions better.

- **Shading has been added to Figure 6 to indicate when  $Q^* > 0 \text{ W m}^{-2}$ .**

PAPER-B: ———

- **Please see Part 2 response.**

Interactive comment on “Infrared and millimetre-wave scintillometry in the suburban environment – Part 2: Large-area sensible and latent heat fluxes” by H. C. Ward et al.

J.-M. Cohard (Referee)

H. Ward et al. present a paper series called “Infrared and millimetre-wave scintillometry in the suburban environment” containing 2 parts. – Part 1 is about the different ways to obtain structure parameters for temperature and specific humidity from scintillometers at different wave lengths. The part 2 is about the way to derive average turbulent fluxes from these structure parameters. The first part evaluates the performance of 3 methods, namely the single wave length method, the bichromatic method and the 2 wave length method. The second part develops objectively advantages and limitations of the scintillometry techniques. Both parts analyse a 14 months data time series obtained from July 2011 to December 2012 above Swindon (UK).

Theoretical backgrounds are clearly exposed highlighting the assumptions and limitations of the techniques deployed during this experiment. Results give a complete and detailed panorama of what is to be done when using Infra Red and Microwave scintillometers. It is based on the longest time series ever obtained for such technique. This huge amount of results and remarks will be very useful for any one wants to apply scintillometry techniques in the future. Urban surface Bowen ratios are finally presented and compared to previous studies. This last part will certainly require further analysis, but it is clearly not the main objective of these papers

Finally, this matches very well with the AMT journal and have to be published after minor corrections.

Some comments on both parts are listed below.

Part I : Structure parameters

p6 - 11174 L-18 : Add a reference (Hill 1981) for example.

- **Reference to Hill et al. (1980) has been added.**

p7 - 11175 L-10 : recall what the Bowen ratio is (QH/QLE). It is well known from most of us except if you want to address other community

- **To avoid confusion with Equation 9, the Bowen ratio is not explicitly given here in terms of fluxes.**

p12 - 11180 L 21 :  $z_d=0.7z_h$  is really not confirmed for open complex canopies. An estimation from EC data would be more appropriate. At least a remark on the reliability of this relation could be added given that this  $z_d$  parameter is recognize to be one of the most sensible for flux calculation from  $CT^2$  values

- **Accurate estimates of the displacement height are difficult to obtain in complex environments, but the rule-of-thumb used here has also been used in other similar suburban areas. Moreover, the values obtained are within the range expected for similar environments (e.g. Grimmond and Oke 1999). Comparable values of  $z_d$  were estimated from the EC data for a reasonable range of  $z_0$ . In Part 2, Section 4.1.3, the impact on the fluxes of uncertainty in  $z_d$  is discussed and demonstrated to be unimportant given the**

**considerable beam height ('The displacement height is incorporated in the effective height, and as a change in  $z_d$  of  $\pm 0.5$  m is minor compared to  $z_{ef}$  itself, it has negligible impact (< 1 %) on the fluxes').**

p12 - 11180 L 15 - 25 : Is this paragraph on equivalent height necessary to only compare  $C_n^2$  values (what is done in this paper) ? For sure, you need to estimate  $C_n^2$  values at compatible heights (EC and SC). As scintillometers provide good estimations of  $C_n^2$  values, whereas EC  $C_n^2$  are indirect estimations, I would prefer move the EC  $C_n^2$  values from 12 to ...xx m (Explain in page 11184). In any case the difference in height from EC to scintillometer path should be discussed.

- **The effective height description here is part of the instrumental setup and is also needed for calculation of the S factors (see page 11183) which are used to scale the various scintillometer measurements to ensure they are representative of the same height (see Evans and De Bruin (2011) for details). The EC estimates of the structure parameters ( $C_T^2$ ,  $C_q^2$  and  $C_{Tq}$ ) are indeed scaled to match the effective height of the scintillometer system for comparison (see page 11184 and Figures 7-9). In Figure 8, structure parameters from EC are plotted both before and after height scaling to match the scintillometer height; these results are discussed in Section 5.1.3.**

p15 - 11183 L15 : This is not a question of height but of weighting function. The difference in the equivalent height is a result of the integration of the weighting function. What it has to be accounted for is the difference in the way the  $C_n^2$  values are averaged along the path. Don't forget that the sensor probe the same volume (more or less) at the same height.

- **Yes, the difference in path-weighting functions between the BLS and MWS means that the values of  $C_n^2$  and  $C_n^2$  (and  $C_n^2$ ) obtained are representative of different effective measurement heights. The wording has been modified to make this point clearer ('resulting from the combination of different weighting functions and changing beam elevation along the path').**

p15 - 11183 L25 : '3 techniques' appear not so clear to me as you just discussed 3  $C_n^2$  calculations but I understand you turn to a single, two wavelength and bichromatic method ....

- **Yes, that is correct.**

p16 - 11184 L11 : tau fixed at 1s . Does this can explain the weak correlation  $r_{Tq}$  found at night with EC data ? Please comment on that on page 11192 (if any answer !)

- **The nocturnal  $r_{Tq}$  values are fairly similar for different wind speeds and there is no clear indication that the values of  $r_{Tq}$  obtained are dependent on wind speed. Therefore the fixed time lag does not seem to explain the weak correlation. The spatial separation of the sonic and IRGA is probably responsible for the magnitude of  $r_{Tq}$  being underestimated. However, other studies have also indicated that absolute values of  $r_{Tq}$  are smaller at night than during the day. For example  $r_{Tq}$  was found to range between -0.5 and 0.9 (Meijninger et al. 2006) and Lüdi et al. (2005) find that the  $T-q$  anti-correlation at night is 'less pronounced' than the positive correlation during daytime. The following sentence has been added to the discussion in Section 5.2, 'According to Lüdi et al. (2005) the  $T-q$  anti-**

**correlation observed at night is 'less pronounced' than the positive correlation during daytime; Meijninger et al. (2006) also found  $r_{Tq}$  ranged between -0.5 and 0.9.'**

p19 - 11187 : line 19 and after please, use the same subscript code along the paper. you have define the substrict 1l, 2l and bc. just use it. If a SC is necessary to invite the reader considering all of the three techniques, define it. The BLS\_MWS notation is quite long and "heavy".

- **We agree the BLS-MWS subscript is fairly cumbersome, however it represents exactly what we wish to convey – quantities derived from the BLS-MWS system, using either the two-wavelength or bichromatic technique (but not the single-wavelength technique). We would therefore prefer to continue using BLS-MWS, rather than introduce yet more notation.**

p19 - 11187 : L19 -23 : Finally this paragraph say not so much. I would replace it with a clear invitation to the part II (1 sentence)

- **Done. The first two sentences have been deleted and the sentence referencing Part 2 has been moved to the end of the previous paragraph.**

p22 - 11190 : L1 ... this discussion on Bowen ratio should better take place around line 8 in page 11188. However as you mentioned it, the analysis of Beta will be easier with the fluxes. I suggest suppressing this paragraph and replacing it by extended comments on the differences between Beta\_EC and Beta\_SC (footprint differences, height differences, Beta calculation from SC and EC, the latest is not précised. Is it  $w'T'/w'q'$  or is it calculated with Eq 9, statistical issues ?). At least the Beta curves show few Beta differences using the 2 wavelength or the bichromatic method ...but is these estimates reliable? (Half the EC value!!)

More over the Beta estimates you mentioned in the text ( $Beta_{2\lambda} < 1.3$ ) doesn't match with what is plotted in figure 9 where these values are always under 0.5. Please clarify. Finally, you conclude (in the conclusion) the differences came from footprint differences, but this has not been discussed here.

- **The discussion on Bowen ratios in Section 5.1.4 has now been moved to the end of Section 5.1.3.**
- **The mean daytime Bowen ratio for each month is plotted in Figure 9.  $\beta$  was calculated from Equation 9 (this is now stated in the figure caption). The individual 10-min or 30-min values are spread around these means, and they vary both throughout the day and between days as the meteorological and surface conditions vary. It is these individual  $\beta_{2\lambda}$  values that appear to be limited to  $\leq 1.3$ . The fact that the BLS-MWS footprint is more vegetated than the EC footprint is also mentioned here now.**

p23 -n11191 : The  $r_{Tq}$  plateau at 1 is a rough approximation. I would precise this (0.8?)  $r_{Tq}$  for low wind speed (the same eddy can be probe several time which increase the correlation. Pb of the inversion for noisy data.

- **'close to +1' has been changed to 'around 0.8'.**
- **We are unsure of the meaning of 'Pb of the inversion for noisy data'.**

p27 11195 : The conclusion could be shorter. It is not necessary to recall equation (L 6 - 15). It could be re organized starting from the technical insights (appendix), the  $CT^2$   $Cq^2$ , ... consistency,  $r_{Tq}$ , Bowen ratio and method comparison.

Considering this conclusion, I would also reorganise the discussion to point out the different argumentations that lead to these conclusion (Like the one I have suggested for Beta).

- **The references to the appendix and equation have been deleted.**
- **Methodological differences as well as footprint differences (now mentioned in Section 5.1.3) are given as explanations for the observed differences in Bowen ratio.**

fig 4 precise somewhere how the spectra has been calculated (windowing, ...) especially for the black line. I guess the grey line is a direct calculation (rectangular window) over the 30 min segment and I suspect the black line to be a bin average.

- **Yes, the grey line is a direct calculation over the 30-min rectangular window; the black line is the smoothed spectrum (bin averages for the data divided into 100 bins). This is now mentioned in the Figure caption.**

fig 8 : I suspect an error in the axes legend  $r_{EC\_bc}$  in place or  $r_{Tq}$  ? More over the color line legend is missing in the figure and in the legend. It is also not clear to me on how these correlations have been calculated: 30min OK but with min data ?

- **The panels in the bottom row of Figure 8 show  $r_{Tq}$  calculated from EC (black) and  $r_{Tq}$  calculated from the bichromatic method (green). The legend is shown in the top right-hand panel and is the same for all panels. Meteorological structure parameters for the single-wavelength, two-wavelength and bichromatic-correlation methods were obtained at 10-min intervals from the 10-min refractive index structure parameters (Section 3.2.1). Due to the variability of the bichromatic method, the 10-min meteorological structure parameters were averaged up to 30-min.  $r_{Tq\_bc}$  was then calculated from these 30-min structure parameters.**

Part II : Large-area sensible and latent heat fluxes

- **Please see Part 2 response.**

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# Infrared and millimetre-wave scintillometry in the suburban environment – Part 1: structure parameters

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## Abstract

Scintillometry, a form of ground-based remote sensing, provides the capability to estimate surface heat fluxes over scales of a few hundred metres to kilometres. Measurements are spatial averages, making this technique particularly valuable over areas with moderate heterogeneity such as mixed agricultural or urban environments. In this study, we present the structure parameters of temperature and humidity, which can be related to the sensible and latent heat fluxes through similarity theory, for a suburban area in the UK. The fluxes are provided in the second paper of this two-part series. A ~~unique~~ millimetre-wave scintillometer was combined with an infrared scintillometer along a 5.5 km path over northern Swindon. The pairing of these two wavelengths offers sensitivity to both temperature and humidity fluctuations, and the ~~so-called 'bichromatic-correlation' method~~ correlation between wavelengths is also used to retrieve the path-averaged temperature-humidity correlation. Comparison is made with structure parameters calculated from an eddy covariance station located close to the centre of the scintillometer path. The performance of the measurement techniques under different conditions is discussed. Similar behaviour is seen between the two datasets at sub-daily timescales. For the two summer-to-winter periods presented here, similar evolution is displayed across the seasons. A higher vegetation fraction within the scintillometer source area is consistent with the lower Bowen ratio observed (midday Bowen ratio < 1) compared with more built-up areas around the eddy covariance station. The energy partitioning is further explored in the companion paper.

28 **Keywords:** bichromatic correlation; refractive index; temperature-humidity correlation; two-  
29 wavelength scintillometry; urban

## 30 **Highlights**

- 31 • First use of two-wavelength scintillometry in an urban area
- 32 • Temperature-humidity correlation coefficient measured by bichromatic-correlation
- 33 • Performance of techniques assessed under a range of conditions
- 34 • Extensive dataset enables analysis of seasonal and inter-annual variability

## 35 **1. Introduction**

36 Scintillometry provides turbulent heat fluxes representative of much larger scales than is possible  
37 with traditional point-based or small-area measurements, such as eddy covariance (EC). The  
38 technique relates fluctuations in the intensity of light ('scintillations', observed as shimmering or  
39 'heat-haze') to the strength of turbulence in the atmosphere. Scintillometry is suited to  
40 heterogeneous regions because the measurements are spatially integrated, providing average values  
41 representative of the area as a whole (Hoedjes et al. 2002; Meijninger et al. 2002b; Evans et al.  
42 2012). A transmitter unit provides the light source, a beam of electromagnetic radiation, which is  
43 detected some distance (0.1-10 km) away by the receiver. Variations in the received intensity result  
44 from ~~refraction-diffraction~~ as turbulent eddies move through the beam, their refractive indices  
45 determined by their ~~ir densit~~~~iesy of constituent air parcels~~ which, in turn, can be related to their  
46 temperature and moisture content (e.g. Meijninger 2003). The refractive index depends on the  
47 wavelength of radiation; in the optical or near-infrared range temperature-induced fluctuations  
48 dominate the refractive index fluctuations, whereas for longer wavelengths (millimetre or radiowave  
49 regions) humidity fluctuations are ~~also more~~ important. ~~Peak sensitivity is~~ Scintillometers are most  
50 sensitive to fluctuations occurring towards the centre of the path, i.e. away from the transmitter and  
51 receiver and their mountings. Thus the atmosphere above a city (or valley) can be sampled remotely  
52 – a major advantage in areas where it would be impracticable to install ~~other~~ equipment *in situ*.

53 Scintillometer measurements have been carried out at sites of varying complexity, from tests of  
54 the technique under simple conditions (Hill and Ochs 1978; De Bruin et al. 1993) to studies  
55 investigating the complications of non-ideal terrain, including heterogeneous land cover (Beyrich et  
56 al. 2002; Meijninger et al. 2002a; Meijninger et al. 2006; Ezzahar et al. 2007) and complex  
57 topography (Poggio et al. 2000; Evans 2009; Evans et al. 2012). On the whole, these studies have  
58 shown that scintillometers installed above or close to the blending height can provide valuable area-  
59 averaged fluxes.

60 With careful selection of a suitable path, the scintillometry technique has been successfully used  
61 in urban areas. Kanda et al. (2002), the first to ~~derive-obtain~~ the sensible heat flux in an urban  
62 setting, used two small aperture scintillometers installed at different heights on a 250 m path over a  
63 dense residential area of Tokyo. Other small aperture studies include measurements in Basel (Roth  
64 et al. 2006) and London (Pauscher 2010). Large aperture scintillometers are increasingly being used  
65 over longer urban paths (Lagouarde et al. 2006; Gouvea and Grimmond 2010; Mestayer et al. 2011;  
66 Wood et al. 2013; Zieliński et al. 2013). These infrared (or optical) scintillometers must rely on the  
67 residual of the energy balance if the latent heat flux is to be estimated. However, the complexity of  
68 the energy balance (Oke 1987) means this is usually not attempted in urban areas. In particular the  
69 significant storage heat flux (Oke et al. 1999; Offerle et al. 2005) and contribution from  
70 anthropogenic activities (Klyzik 1996; Allen et al. 2011) are both very difficult to measure.

71 Sensitivity to both humidity and temperature fluctuations can be achieved with a two-  
72 wavelength scintillometer system. In this case, the structure parameter of humidity can be obtained  
73 in addition to the structure parameter of temperature, from which both the sensible heat flux ( $Q_H$ )  
74 and latent heat flux ( $Q_E$ ) can be found (Hill et al. 1988; Andreas 1989). Several studies have reported  
75 successful estimates of  $Q_E$  using the two-wavelength method (Meijninger et al. 2002a; Meijninger et  
76 al. 2006; Evans 2009; Evans et al. 2010). This technique requires that a value of the temperature-  
77 humidity correlation coefficient,  $r_{Tq}$ , be assumed. Often  $r_{Tq}$  is taken to be  $\pm 1$ , indicating perfect

78 correlation, as in Green et al. (2001) and Meijninger et al. (2002a), but other values have also been  
79 used: Kohsiek and Herben (1983) used  $r_{Tq} = 0.87$ ; Evans (2009) used  $r_{Tq} = 0.8$ ; and Meijninger et al.  
80 (2006) used measured  $r_{Tq}$  from a nearby EC station with values between -0.5 and 0.9. Previous  
81 studies measuring  $r_{Tq}$  with fast-response sensors suggest daytime values tend to be smaller than 1,  
82 typically around 0.8. For example: 0.75 at a flat, homogeneous site (Kohsiek 1982); 0.76 over sandy  
83 soil with patchy vegetation (Andreas et al. 1998); 0.70-0.95 for unstable conditions over  
84 heterogeneous farmland (Meijninger et al. 2002a). Nocturnal values of  $r_{Tq}$  down to -1 are rarely seen  
85 (Andreas et al. 1998; Beyrich et al. 2005; Meijninger et al. 2006).

86 Some studies have suggested that  $r_{Tq}$  varies with stability (Li et al. 2011; Nordbo et al. 2013),  
87 although others have shown no clear relation (De Bruin et al. 1993; Roth 1993). Explanation of  
88  $|r_{Tq}| \neq 1$  is often related to surface heterogeneity (Roth 1993; Andreas et al. 1998; Lüdi et al. 2005)  
89 but low values have been obtained over homogeneous surfaces too (Kohsiek 1982; De Bruin et al.  
90 1993). In almost all previous studies, measurements of  $r_{Tq}$  were made using point sensors.

91 Lüdi et al. (2005) outlined a method to obtain path-averaged values of  $r_{Tq}$  using a two-wavelength  
92 scintillometer system. This 'bichromatic-correlation' method is an extension of the two-wavelength  
93 technique and involves correlating the signals from each scintillometer, thus enabling determination  
94 of the combined temperature-humidity fluctuations and  $r_{Tq}$ . The bichromatic-correlation method,  
95 applied for the first time during the LITFASS-2003 campaign, gave promising results (Beyrich et al.  
96 2005; Lüdi et al. 2005). An overview of the second study, during LITFASS-2009, is given in Beyrich et  
97 al. (2012).

98 Aside from enabling more accurate structure parameters and fluxes to be obtained from  
99 scintillometry, improved knowledge of  $r_{Tq}$  has wider applications. Correlations between scalars are  
100 thought to be useful indicators for the violation of Monin-Obukhov Similarity Theory (MOST) (Hill  
101 1989; Andreas et al. 1998). Correlations are also relevant to the understanding and modelling of  
102 turbulent transport processes through physical quantities such as eddy diffusivities.

103 The objectives of this research are to measure structure parameters and obtain large-area  
 104 sensible and latent heat fluxes for a suburban area. In this two-part study, a 94 GHz millimetre-wave  
 105 scintillometer was deployed alongside an infrared scintillometer over the town of Swindon, UK. This  
 106 is the first use of such a system in the urban environment. In Part 1, structure parameters from the  
 107 two-wavelength system are compared to structure parameters calculated from an EC system and  
 108 measured values of  $r_{Tq}$  are discussed. In Part 2, the sensible and latent fluxes are determined and  
 109 analysed (Ward et al. 2014a). These spatially-integrated observations represent the behaviour of the  
 110 suburban surface over an area of 5-10 km<sup>2</sup> and constitute by far the longest dataset (14 months)  
 111 that uses these techniques. ~~Methodological considerations, the~~ The performance of the techniques  
 112 under different conditions, and their strengths and weaknesses, are examined. This paper offers  
 113 insight into the behaviour of the structure parameters and  $r_{Tq}$  at various timescales (daily, seasonal  
 114 and inter-annual), and including how they respond to the influence of energy and water availability,  
 115 surface cover and changing meteorological conditions ~~vegetation cover and seasonality are~~  
 116 ~~explored.~~

## 117 2. Theory

118 Structure parameters describe the intensity of turbulent fluctuations in the ~~turbulent~~  
 119 atmosphere. The structure parameter for a variable,  $y$ , is defined (Tatarski 1961),

$$120 \quad C_y^2 = \frac{\overline{[y(x + \delta) - y(x)]^2}}{\delta^{2/3}}, \quad (1)$$

121 where  $\delta$  is the spatial separation between two points and  $y(x)$  is the value of the variable at location  
 122  $x$ . The cross-structure parameter between two variables is defined analogously, for example the  
 123 cross-structure parameter between temperature,  $T$ , and specific humidity,  $q$ , is written,

$$124 \quad C_{Tq} = \frac{\overline{[T(x + \delta) - T(x)][q(x + \delta) - q(x)]}}{\delta^{2/3}}. \quad (2)$$

125 2.1. Obtaining structure parameters from scintillometry

126 The refractive index structure parameter ( $C_n^2$ ) is fundamental to scintillometry. For each  
 127 wavelength,  $\lambda$ , it can be written (Hill et al. 1980),

$$128 \quad C_n^2 = \frac{A_T^2}{T^2} C_T^2 + 2 \frac{A_T A_q}{Tq} C_{Tq} + \frac{A_q^2}{q^2} C_q^2, \quad (3)$$

129 where  $C_T^2$  is the structure parameter of temperature,  $C_q^2$  the structure parameter of specific  
 130 humidity,  $C_{Tq}$  the temperature-humidity cross-structure parameter and  $A_T$  and  $A_q$  are the structure  
 131 parameter coefficients for temperature and specific humidity respectively, given in Ward et al.  
 132 (2013b) as  $A_T$  and  $A_q$  (see their Table 2). These coefficients contain the wavelength dependence of  
 133  $C_n^2$ , whereas  $C_T^2$ ,  $C_q^2$  and  $C_{Tq}$  are properties of the atmosphere. Each  $C_n^2$  measurement is made up  
 134 of a combination of the three unknowns:  $C_T^2$ ,  $C_q^2$  and  $C_{Tq}$ .

135 As  $C_n^2$  from large aperture optical or near-infrared scintillometers is almost entirely made up of  
 136 temperature fluctuations ( $C_T^2$ ), the (usually small) contributions from  $C_{Tq}$  and  $C_q^2$  can be  
 137 approximated using the Bowen ratio,  $\beta$  (Wesely 1976; Moene 2003):

$$138 \quad C_n^2 \approx \frac{A_T^2}{T^2} C_T^2 \left( 1 + \frac{A_q}{q} \frac{T}{A_T} \frac{c_p}{L_v} \beta^{-1} \right)^2 \approx \frac{A_T^2}{T^2} C_T^2 (1 + 0.03 \beta^{-1})^2, \quad (4)$$

139 where  $c_p$  is the specific heat capacity of air at constant pressure,  $L_v$  is the latent heat of vaporisation  
 140 and the value 0.03 is for typical atmospheric conditions ( $T = 300$  K, pressure ( $p$ ) =  $10^5$  Pa). The  
 141 required Bowen ratio may be found by using the available energy as an input to the iteration to  
 142 obtain the sensible heat flux (e.g. Green and Hayashi 1998; Meijninger et al. 2002b; Solignac et al.  
 143 2009). Calculation of the latent heat flux must rely on the energy balance (Ezzahar et al. 2009; Guyot  
 144 et al. 2009; Evans et al. 2012; Samain et al. 2012b). This is the single-wavelength scintillometry  
 145 method.

146 As demonstrated by Hill et al. (1988) and Andreas (1989), a two-wavelength scintillometer system  
 147 enables retrieval of both  $C_T^2$  and  $C_q^2$  via simultaneous equations (Equation 3 for each wavelength).  
 148 The two-wavelength method has the significant advantage of providing both sensible and latent  
 149 heat fluxes without resorting to the energy balance, but a value for the temperature-humidity  
 150 correlation coefficient  $r_{Tq}$  must be assumed in the substitution  $C_{Tq} = r_{Tq}(C_T^2 C_q^2)^{1/2}$ .

151 The bichromatic-correlation method uses the same combination of optical and millimetre  
 152 wavelength scintillometers as for the two-wavelength method, but additionally exploits the  
 153 correlation between optical and millimetre-wave signals to obtain a third equation for the cross-  
 154 structure parameter,  $C_{n1n2}$  (Lüdi et al. 2005),

$$155 \quad C_{n1n2} = \frac{A_{T1}A_{T2}}{T^2} C_T^2 + \left( \frac{A_{T1}A_{q2} + A_{T2}A_{q1}}{Tq} \right) C_{Tq} + \frac{A_{q1}A_{q2}}{q^2} C_q^2, \quad (5)$$

156 where the subscripts 1 and 2 refer to the different wavelengths. In this study,  $\lambda_1$  denotes optical  
 157 (specifically  $880 \times 10^{-9}$  m) and  $\lambda_2$  millimetre ( $3.2 \times 10^{-3}$  m) wavelengths. Thus all three unknown  
 158 meteorological structure parameters ( $C_T^2$ ,  $C_q^2$  and  $C_{Tq}$ ) can be found from the three measured  
 159 refractive index structure parameters by inverting the matrix equation (Lüdi et al. 2005),

$$160 \quad (C_{n1n1} \quad C_{n2n2} \quad C_{n1n2}) = \mathbf{M} \begin{pmatrix} C_T^2 \\ C_{Tq} \\ C_q^2 \end{pmatrix}, \quad (6)$$

161 where the inverse matrix  $\mathbf{M}^{-1}$  is given by,

$$162 \quad \mathbf{M}^{-1} = \frac{T^2 q^2}{(A_{T1}A_{q2} - A_{T2}A_{q1})^2} \begin{pmatrix} \frac{A_{q2}^2}{q^2} & \frac{A_{q1}^2}{q^2} & \frac{-2A_{q1}A_{q2}}{q^2} \\ -A_{T2}A_{q2} & -A_{T1}A_{q1} & (A_{T1}A_{q2} + A_{T2}A_{q1}) \\ \frac{A_{T2}^2}{T^2} & \frac{A_{T1}^2}{T^2} & \frac{-2A_{T1}A_{T2}}{T^2} \end{pmatrix}. \quad (7)$$

163 As mentioned above, the structure parameter coefficients  $A_T$  and  $A_q$  should be those formulated  
 164 using specific humidity.

165 For the bichromatic-correlation method, the value of  $C_{Tq}$  ~~obtained~~ can therefore be used to  
 166 effectively measure the temperature-humidity correlation coefficient:

$$167 \quad r_{Tq} = \frac{C_{Tq}}{\sqrt{C_T^2 C_q^2}}. \quad (8)$$

168 If MOST assumptions (i.e.  $T$ - $q$  similarity) are satisfied, the Bowen ratio can be calculated from the  
 169 structure parameters (Andreas 1990; Lüdi et al. 2005),

$$170 \quad \beta = \text{sgn}[C_{Tq}] \frac{C_p}{L_v} \sqrt{\frac{C_T^2}{C_q^2}}. \quad (9)$$

171 When the cross-structure parameter has not been measured, the structure parameters  $C_T^2$  and  
 172  $C_q^2$  can be calculated from the two-wavelength equations, after Hill et al. (1988):

$$173 \quad C_T^2 = \frac{A_{q2}^2 C_{n1n1} + A_{q1}^2 C_{n2n2} + 2r_{Tq} A_{q1} A_{q2} S_{2\lambda} \sqrt{C_{n1n1} C_{n2n2}}}{(A_{T1} A_{q2} - A_{T2} A_{q1})^2 T^{-2}}, \quad (10a)$$

$$174 \quad C_q^2 = \frac{A_{T2}^2 C_{n1n1} + A_{T1}^2 C_{n2n2} + 2r_{Tq} A_{T1} A_{T2} S_{2\lambda} \sqrt{C_{n1n1} C_{n2n2}}}{(A_{T1} A_{q2} - A_{T2} A_{q1})^2 q^{-2}}, \quad (10b)$$

175 where  $S_{2\lambda}$  is  $\pm 1$ . This choice of sign is an inherent ambiguity of the two-wavelength method and  
 176 represents two possible solutions to  $C_{n2n2}$  (Hill et al. 1988; Hill 1997). For low  $\beta$ , when humidity  
 177 fluctuations dominate  $C_{n2n2}$ , then  $S_{2\lambda} = +1$ , whereas  $S_{2\lambda} = -1$  is required at larger  $\beta$ . The sign of  $S_{2\lambda}$  is  
 178 not known a priori but must be assumed. Often the two solutions for  $\beta$  indicate which is the most  
 179 likely solution for the atmospheric conditions and site characteristics (Hill 1997). When expressed as  
 180 a function of  $\beta$ , a minimum in  $C_{n2n2}$  ~~occurs-is revealed~~ due to the coefficients  $A_T$  and  $A_q$  having  
 181 opposite signs at millimetre wavelengths. The contribution of  $C_{Tq}$  to  $C_{n2n2}$  (middle term in Equation



182 3) is negative when  $C_{Tq} > 0$ , so for moderate  $\beta$  the terms in Equation 3 can cancel out leaving  $C_{n2n2}$   
183 close to zero (Hill et al. 1988; Otto et al. 1996). ~~In practice, a finite instrumental noise floor (and  $r_{Tq} \neq$~~   
184 ~~1) means zero  $C_{n2n2}$  will not be observed. Instead a measurement problem of reduced sensitivity is~~  
185 ~~created around the region of minimum  $C_{n2n2}$  where the scintillation signal may be close to, or~~  
186 ~~below, the detection limit of the instrument. In practice, zero  $C_{n2n2}$  will not be observed because the~~  
187 ~~instrument has a finite noise floor (and  $r_{Tq} \neq 1$ ). Instead the scintillation signal may be close to, or~~  
188 ~~below, the detection limit of the instrument, resulting in reduced sensitivity around the region of~~  
189 ~~minimum  $C_{n2n2}$  and a tendency for the derived  $\beta$  to be biased away from (below, for  $S_{2k} = +1$ ) the~~  
190 ~~value at which minimum  $C_{n2n2}$  occurs.~~ The problematic region is expected to occur for  $\beta \approx 2-3$   
191 (Leijnse et al. 2007; Ward et al. 2013b). ~~For low  $\beta$ , when humidity fluctuations dominate  $C_{n2n2}$  then~~  
192  ~~$S_{2k} = +1$ , whereas  $S_{2k} = -1$  is required at larger  $\beta$ . The sign of  $S_{2k}$  is not known *a priori* but must be~~  
193 ~~assumed. Often the two solutions for  $\beta$  indicate which is the most likely solution for the atmospheric~~  
194 ~~conditions and site characteristics (Hill 1997).~~

## 195 2.2. Obtaining structure parameters from eddy covariance

196 Conversion between spatial and temporal domains enables calculation of structure parameters  
197 from point measurements, such as those from EC instrumentation. The spatial structure function,  
198  $D_{yy_{-x}}$  can be written (e.g. Stull 1988),

$$199 \quad D_{yy_{-x}}(\delta) = \overline{[y(x + \delta) - y(x)]^2} . \quad (11)$$

200 Analogously the temporal structure function,  $D_{yy_{-t}}$  is given by,

$$201 \quad D_{yy_{-t}}(\tau) = \overline{[y(t + \tau) - y(t)]^2} , \quad (12)$$

202 where  $\tau$  is the temporal separation and  $y(t)$  is the value of the variable at time  $t$ . Bosveld (1999) gives  
203 the conversion between temporal and spatial structure functions using the horizontal wind vector,  
204  $U$ , and the variances of the three wind components,  $\sigma_{u,v,w}^2$ :

$$D_{yy-x}(\delta) = \frac{D_{yy-t}(\delta/U)}{\left(1 - \frac{1}{9} \frac{\sigma_u^2}{U^2} + \frac{1}{3} \frac{\sigma_v^2}{U^2} + \frac{1}{3} \frac{\sigma_w^2}{U^2}\right)}. \quad (13)$$

Thus temporal structure functions (Equation 12) can be calculated from EC measurements, converted to spatial structure functions (Equation 13) and then structure parameters ( $C_y^2 = D_{yy-x}(\delta) \delta^{-2/3}$  defines  $C_y^2$  for  $\delta$  in the inertial subrange). Unlike fluxes, structure parameters are strongly height dependent.

### 3. Experimental details

#### 3.1. Instrumental setup and site description

A ~~unique~~ millimetre-wave scintillometer (MWS) (Evans 2009), designed and built by the Centre for Ecology and Hydrology (CEH) and Rutherford Appleton Laboratory (RAL), was used in combination with a commercially available large aperture infrared scintillometer, the BLS900 (Scintec, Rottenburg, Germany). Both scintillometers were installed on a 5.5 km path over the town of Swindon, UK. The path is orientated approximately north-south (170°) and extends from the edge of the settlement to the town centre (Figure 1). An EC system was positioned near the centre of the path, consisting of a sonic anemometer (R3, Gill Instruments, Lymington, UK) and open-path infrared gas analyser (IRGA) (LI-7500, LI-COR Biosciences, Lincoln, USA) mounted at 12.5 m above ground level (a.g.l.). The EC site was equipped with an automatic weather station (WXT [510/520](#), Vaisala, Finland) which provides the additional input data required to process the scintillometer data: temperature, relative humidity (RH), pressure (~~p~~) and wind speed ( $U$ ) are measured at a height of 10.6 m. A four-component radiometer (NR01, Hukseflux, The Netherlands) was installed at 10.1 m on the same mast and a tipping bucket rain gauge (0.2 mm tip, Casella CEL, Bedford, UK) near the base of the mast. These were located in the garden of a residential property approximately 3 km north of the town centre, where the surrounding land use is predominantly residential, consisting of 1-2 storey houses with gardens. Full details are given in Ward et al. (2013a). In addition to the meteorological instrumentation at the EC site ( $MET_{sub}$ ), a second weather station was established on

229 the rooftop of a modern office building close to the town centre ( $\text{MET}_{\text{roof}}$ ). The setup is summarised  
230 in Table 1. To provide a combined dataset of continuous input variables required for scintillometry  
231 processing,  $T$ , RH,  $p$  and  $U$  from  $\text{MET}_{\text{roof}}$  were linearly adjusted to gap-fill  $\text{MET}_{\text{sub}}$  (required for < 1% of  
232  $T$ , RH and  $p$  and < 2% of  $U$  data), based on regressions with concurrent data from  $\text{MET}_{\text{sub}}$  (9 May  
233 2011 - 31 December 2012).

234 Northern Swindon is typical of suburban areas in the UK. The area has a relatively large  
235 proportion of vegetation and there is a large nature reserve just north of the centre of the study  
236 area, which lies directly underneath the scintillometer path. The town centre at the south of the  
237 study area has the highest density of buildings and roads (Figure 1). Industrial areas to the east and  
238 southwest with little vegetation contribute to measurement source areas under stable conditions  
239 (see Part 2). Despite the variety of land cover types, many neighbourhoods appear fairly  
240 homogeneous at a scale of a few hundred metres. The area shown in Figure 1 has land cover that is  
241 14% buildings, 31% impervious, 53% vegetation, 1% water and 2% pervious. Land cover, topography  
242 and building and tree heights were derived from a spatial database for Swindon (5 m resolution, see  
243 Ward et al. (2013a) for more information).



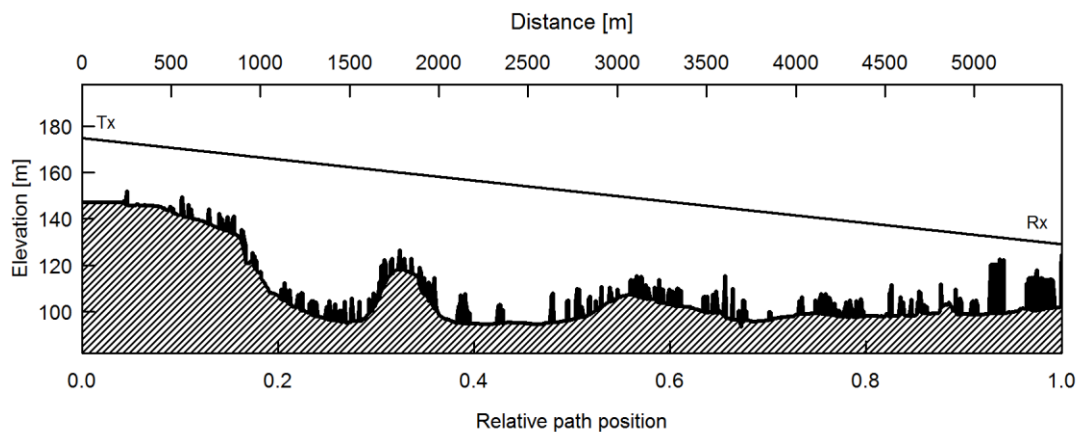
244

245 **Figure 1** Aerial photograph (2009, GeoPerspectives©) of the study area showing the locations of the two-wavelength  
 246 scintillometer path (BLS-MWS), eddy covariance station (EC) and two meteorological stations (MET<sub>sub</sub>, MET<sub>roof</sub>). The  
 247 location of Swindon within the British Isles is shown (top right).

Instrumentation	Height [m]	Location	Path length [m]	$z_0$ [m]	$z_d$ [m]
Two-wavelength scintillometer system	44.3	51°36'33.9" N 1°47'38.6" W (Tx) 51°33'38.1" N 1°46'55.3" W (Rx)	5492	0.7	4.9
EC station	12.5	51°35'4.6" N 1°47'53.2" W	-	0.5	3.5
MET <sub>sub</sub>	10.6 (WXT) 10.1 (NR01)	51°35'4.6" N 1°47'53.2" W	-	0.5	3.5
MET <sub>roof</sub>	2.0 (WXT) 1.1 (NR01)	51°34'0.3" N 1°47'5.3" W	-	-	-

248 **Table 1** The instrumental setup. For the scintillometers the mean height of the beam above the land surface ( $z_m$ ) is given  
 249 (for the effective measurement height ( $z_{ef}$ ) see Table 2); for MET<sub>roof</sub> the heights above the roof surface are given.  
 250 Roughness length,  $z_0$ , and displacement height,  $z_d$ , were not calculated for the rooftop site. Tx denotes transmitter, Rx  
 251 receiver.

252 To obtain representative measurements it is important to be high enough above the surface that  
 253 quantities are sufficiently well-blended (i.e. high enough that turbulent mixing averages out the  
 254 influence of surface heterogeneity), although recent studies have shown successful use of  
 255 scintillometers even below the blending height (Meijninger et al. 2002b; Ezzahar et al. 2007). Based  
 256 on the average height of the roughness elements (i.e. buildings and trees) the blending height is  
 257 estimated at about 15-30 m for the BLS-MWS source area (Pasquill 1974; Garratt 1978). The  
 258 scintillometer transmitters, mounted on custom-built brackets, were installed at 28 m a.g.l. on a  
 259 television transmitter mast. The receivers of the BLS-MWS system were mounted at 26 m a.g.l. on a  
 260 rooftop in Swindon town centre. The resulting path is slanted (Figure 2).



261  
 262 **Figure 2** Cross-section of the land surface (metres above sea level) and height of obstacles (buildings and trees) along the  
 263 BLS-MWS path. Tx denotes transmitter, Rx receiver.

264 The effective heights of the scintillometers are given in Table 2, calculated according to the  
 265 stability-independent approximation (Equation 15 of Hartogensis et al. (2003)). These estimates  
 266 include adjustment to account for the curvature of the earth and displacement height,  $z_d$  (Table 1).  
 267 Displacement heights were calculated from the mean height of the roughness elements,  $z_H$ , within a  
 268 distance of  $\pm 1000$  m perpendicular to the scintillometer path (and +500 m in the direction parallel to  
 269 the path), using the rule-of-thumb  $z_d = 0.7z_H$  (Garratt 1992; Grimmond and Oke 1999). In the case of  
 270 the EC station,  $z_H$  was calculated within 500 m of the EC mast. The difference in BLS and MWS path-

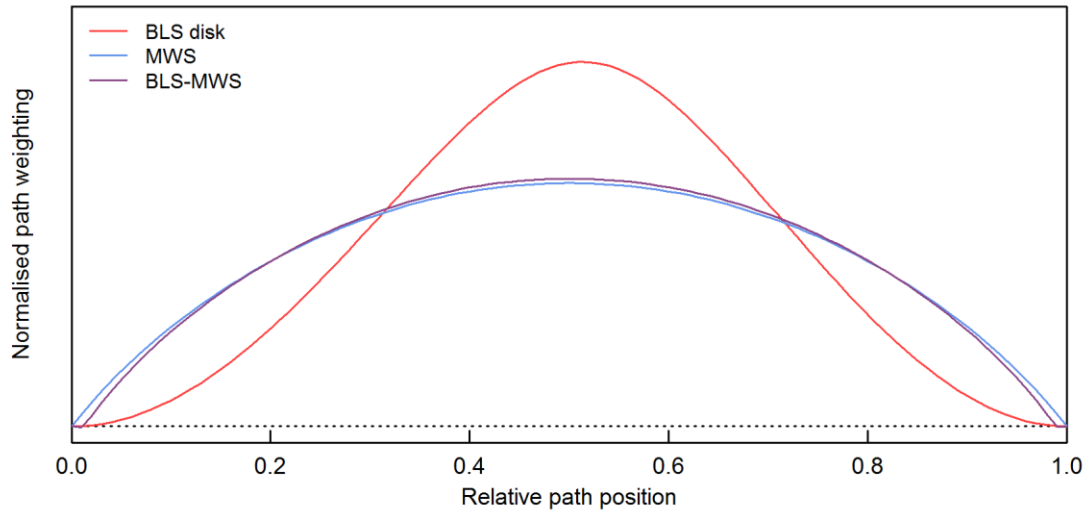
271 weighting functions (Figure 3) means that the BLS, MWS and combined BLS-MWS covariance  
 272 measurements are representative of different heights even though the BLS and MWS beams  
 273 essentially traverse the same path (Evans and De Bruin 2011).

274 For the two-wavelength scintillometer system the BLS and MWS beams must be close together  
 275 (Lüdi et al. 2005). The separation between beams was minimised ( $< 0.35$  m) and the relative  
 276 positions of the BLS and MWS were reversed at each end of the path so that the beams crossed near  
 277 the centre of the path. It was necessary to shield cables at the scintillometer sites to protect against  
 278 electrical interference. Scintillometer data can sometimes be affected by vibrations of the mounting  
 279 structures (Von Randow et al. 2008; Beyrich et al. 2012). However, mounting brackets were  
 280 designed with this in mind and the scintillometer spectra show little evidence of any vibrational  
 281 contamination.

282 The data presented here are for the complete months when the BLS-MWS system was  
 283 functioning: July-December 2011 and May-December 2012. From January 2012 to April 2012 the  
 284 MWS was not operational due to a fault.

Scintillometer	Instrument characteristics		Site-dependent characteristics		
	Wavelength [m]	Aperture diameter [m]	Fresnel zone [m]	Effective height [m]	Scaling ( $S$ ) factor
BLS ( $C_{n1n1}$ )	$880 \times 10^{-9}$	0.145	-	45.0	-
MWS ( $C_{n2n2}$ )	$3.2 \times 10^{-3}$	0.25	4	42.8	0.952
BLS-MWS ( $C_{n1n2}$ )	-	-	-	43.1	0.958

285 **Table 2** Instrument and site-dependent characteristics of the scintillometers and paired scintillometer system.



286

287 **Figure 3** Path-weighting functions for the infrared scintillometer (BLS disk), the MWS and the BLS-MWS combination,  
 288 normalised so that the total area under each curve equals one.

289 **3.2. Data collection, processing and quality control**

290 **3.2.1. Scintillometry**

291 In this study,  $C_{n1n1}$  is used to denote the refractive index structure parameter from the BLS, to  
 292 distinguish from  $C_{n2n2}$  (MWS) and  $C_{n1n2}$  (BLS-MWS cross-term). The BLS900 is a dual-beam  
 293 scintillometer with two transmitter disks (only one disk is used here for combination with the MWS).  
 294 The signal intensity of each BLS disk was sampled and stored at 500 Hz (raw data) and statistics  
 295 including the mean and standard deviation of signal intensity were provided at 30 s intervals by the  
 296 Scintec software (SRun v1-07). Additionally, the signal intensities of both BLS disks and of the MWS  
 297 were sampled at 100 Hz by a CR5000 datalogger (Campbell Scientific Ltd., Loughborough, UK). These  
 298 data were processed using code written in R (The R Foundation for Statistical Computing). Data were  
 299 subjected to initial quality control involving the removal of dropouts (when the BLS makes a  
 300 background measurement) and despiking. The BLS and MWS signals were bandpass filtered to  
 301 remove contributions below 0.06 Hz and above 20 Hz for the calculation of  $C_{n2n2}$  and  $C_{n1n2}$ . The low-  
 302 frequency cut-off reduces the influence of absorption fluctuations. ~~At 10-min intervals the variances,~~  
 303 ~~covariances and mean values of the signals were calculated, from which the log-amplitude~~  
 304 ~~(co)variances ( $\sigma_x^2$ ) were obtained.~~ At 10-min intervals the variances, covariance and mean values of

305 the signals were calculated, from which the log-amplitude variances ( $\sigma_{\chi 1}^2$ ,  $\sigma_{\chi 2}^2$ ) and covariance ( $\sigma_{\chi 1 \chi 2}$ )  
306 were obtained (Tatarski 1961). To convert between the log-amplitude (co)variances and refractive  
307 index (cross-)structure parameters the following equations were used:

$$308 \quad C_{n1n1} = 4.48D^{7/3}L^{-3}\sigma_{\chi 1}^2, \quad (14a)$$

$$309 \quad C_{n2n2} = 8.33k^{-7/6}L^{-11/6}\sigma_{\chi 2}^2, \quad (14b)$$

$$310 \quad C_{n1n2} = 8.93k^{-7/6}L^{-11/6}\sigma_{\chi 1 \chi 2}, \quad (14c)$$

311 where  $D$  refers to the aperture diameter of the infrared scintillometer,  $k$  to the wavenumber ( $2\pi/\lambda$ )  
312 of the millimetre-wave scintillometer and  $L$  to the path length (Table 1, Table 2). These equations  
313 can be derived from the full forms of the log-amplitude (co)variances, which express the path  
314 weighting of the instrument, aperture averaging by the finite size of transmitter and receiver, the  
315 turbulence spectrum (assumed to be the Kolmogorov spectrum, e.g. Monin and Yaglom (1971)) and  
316 separation of the beams if applicable (Equations A1, A2, Appendix A). Note that Equation 14c is  
317 specific to the setup described here (beam separation, path length and instrument characteristics)  
318 and could be expressed in terms of  $D$  rather than  $k$ . Equation 14b was obtained using the full  
319 formula (Equation A2) instead of the small aperture approximation (in which the Bessel functions  
320 accounting for aperture averaging are excluded) and is also specific to this setup. The approximation  
321 can result in an inaccuracy even for long paths (Appendix A). Equation 14a for the infrared  
322 scintillometer is a standard result and was first demonstrated by Wang et al. (1978).

323 Quality control procedures rejected data during periods of low signal strength (usually caused by  
324 rain or fog). BLS data were rejected when the received signal intensity dropped below 0.5 of the  
325 daily maximum value. For the MWS a threshold of 0.33 of the daily maximum intensity was used,  
326 and MWS data were also removed when the BLS signal intensity was below the 0.5 threshold  
327 indicating obscuration along the BLS-MWS path. The data points directly adjacent to those failing the



328 signal strength checks were also removed. Rain was recorded at the EC site for 10% of the dataset  
329 and fog often occurred, particularly during autumn and winter mornings (based on observations  
330 during site visits). Values of  $C_n^2$  ~~above-outside~~ reasonable thresholds were excluded (nine  $C_{n1n1}$   
331 values and one  $C_{n1n2}$  value). The resulting data available for analysis constitute 79% of the total  
332 possible 10-min values (N = 61776).

333 Kleissl et al. (2010) suggests an empirical threshold for the onset of saturation for infrared large  
334 aperture scintillometers of  $C_{n1n1} > 0.074D^{5/3}\lambda^{1/3}L^{-8/3}$ . Approximately 21% of the BLS data were above  
335 this threshold of  $3.2 \times 10^{-15} \text{ m}^{-2/3}$ . BLS data were corrected for saturation using a look up table of  
336 numerical values based on the modulation transfer function of Clifford et al. (1974). The correction  
337 increased  $C_{n1n1}$  by around 5% overall (~10% during summer daytimes). Where the estimated  
338 correction was larger than 25% data were removed instead (46 values in total). MWS data were well  
339 below the saturation threshold of  $5.0 \times 10^{-11} \text{ m}^{-2/3}$  (Clifford et al. 1974) and were not corrected. The  
340 BLS-MWS covariance was not corrected as a methodology is yet to be determined (Beyrich et al.  
341 2012). There is therefore increased uncertainty in these measurements due to the extent of  
342 currently applicable theory.

343 To use the refractive index structure parameters in Equation 6 (or Equation 10a-b),  $C_{n1n1}$ ,  $C_{n2n2}$   
344 and  $C_{n1n2}$  must be representative of the same height. The  $S$  factors (Evans and De Bruin 2011) given  
345 in Table 2 were applied to  $C_{n2n2}$  from the MWS and  $C_{n1n2}$  from the BLS-MWS to scale them to the  
346 same effective height as  $C_{n1n1}$  from the BLS. These factors account for the difference in effective  
347 heights between the three  $C_n^2$  measurements resulting from the combination of different weighting  
348 functions and changing beam elevation along the path (Section 3.1). The  $S$  factors are relatively close  
349 to unity as the height differences are reasonably small for this setup. The approximation of using  
350 stability-independent  $S$  factors was made here (incorporating stability would give values ranging  
351 from 1.0 under very stable conditions to 0.9 for free convection). Calculation of the meteorological  
352 structure parameters proceeds as described in Section 2.

353 Data were processed using each of the three techniques in order to investigate their respective  
354 merits, although the focus is on the two-wavelength and bichromatic-correlation methods. No  
355 Bowen ratio correction was applied for the single-wavelength method (Equation 4), given the  
356 uncertainties in estimating the available energy in urban environments. The impact is estimated to  
357 be a 6% overestimation in  $C_T^2$  (based on  $\beta$  from the two-wavelength method). The positions of  
358 twice-daily minima in  $C_{nlnl}$  were used to indicate stability transitions (Samain et al. 2012a) and  
359 assign positive or negative  $r_{Tq}$  for the two-wavelength method. For the two-wavelength method  $r_{Tq} =$   
360  $\pm 0.8$  was assumed and the solution corresponding to  $S_{2\lambda} = +1$  was chosen. To distinguish between  
361 the methods applied (single-wavelength, two-wavelength, bichromatic-correlation), the subscripts  
362 '1 $\lambda$ ', '2 $\lambda$ ' and 'bc' are used.

### 363 3.2.2. Eddy covariance

364 Structure parameters were also derived from 20 Hz raw EC data. Sonic and IRGA data were time  
365 aligned by seeking maximum covariance between variables. Initial quality control incorporated  
366 threshold checks, outlier detection and despiking. A fixed temporal separation of  $\tau = 1$  s was decided  
367 upon after investigation into suitable values in the inertial subrange. Calculation of  $C_T^2$ ,  $C_q^2$  and  $C_{Tq}$   
368 included the Schotanus et al. (1983) correction for sonic temperature as discussed in Braam (2008)  
369 and Braam et al. (2012). ~~No corrections for spectral losses were made, which can be expected to~~  
370 ~~result in underestimations of about 5–7%. No corrections were made for spectral losses due to the~~  
371 ~~spatial separation of the sonic and IRGA and their finite path lengths, which can be expected to~~  
372 ~~result in underestimations of about 5–7% (Hill 1991; Hartogensis et al. 2002).~~

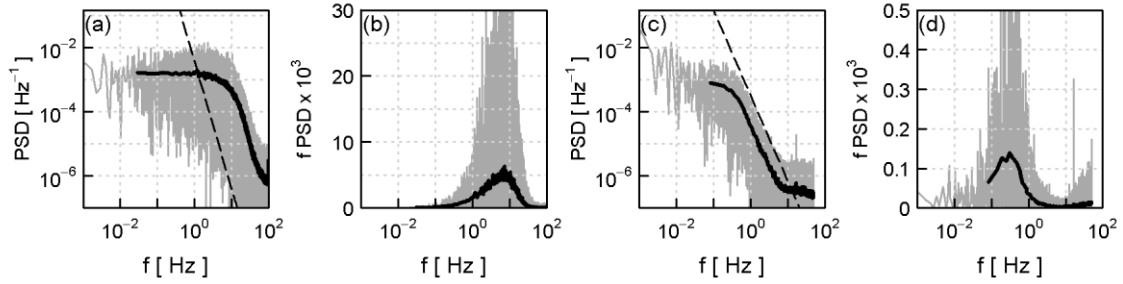
373 The resulting 30-min structure parameters were quality controlled in accordance with the  
374 corresponding EC fluxes. Data were removed during times of known instrument malfunction, when  
375 the IRGA diagnostic indicated obstruction of the optical path, when rainfall could adversely affect  
376 the measurements and if values exceeded physically reasonable ranges.

377 To facilitate comparison between EC and scintillometer datasets, the EC structure parameters  
378 were scaled to match the height of the scintillometer data using MOST functions (with the constants  
379 suggested by Andreas (1988) and assuming identical height-scaling of temperature and humidity,  
380 see Equation 2a, b in Part 2).

381 Since the source areas are different between EC and BLS-MWS systems, the structure  
382 parameters obtained are not expected to be in perfect agreement. The BLS-MWS footprint is  
383 generally more vegetated than the EC footprint (56% versus 44%). However, comparisons are useful  
384 for a number of reasons. As EC is a widely-used technique, it permits evaluation of the scintillometer  
385 system to a certain extent, through comparison of trends and patterns of behaviour even if absolute  
386 values differ. Both systems have merits and limitations: scintillometers are spatially representative;  
387 EC is a more direct measurement but (open-path IRGAs) cannot provide data after rainfall and there  
388 are issues with energy closure (Foken 2008). Analysis of both approaches can therefore provide a  
389 more complete picture of the environment studied.

#### 390 **4. Instrument performance**

391 An unidentified instrumental noise problem affecting the CEH-RAL MWS has been reported  
392 elsewhere (Van Kesteren 2008; Evans 2009; Beyrich et al. 2012). Following extensive testing, the  
393 cause of the issue was finally established and the instrument repaired in June 2011. The spectra  
394 obtained are now close to the ideal shapes predicted by theory and suggest good instrument  
395 performance with a low noise floor (Figure 4). An upper estimate for the MWS noise limit is  
396  $C_{n2n2} \sim 1 \times 10^{-15} \text{ m}^{-2/3}$ . The observed noise limit of the BLS is of the order of  $C_{n1n1} \sim 5 \times 10^{-17} \text{ m}^{-2/3}$  in  
397 agreement with the manufacturer's specification (Scintec 2009).



398

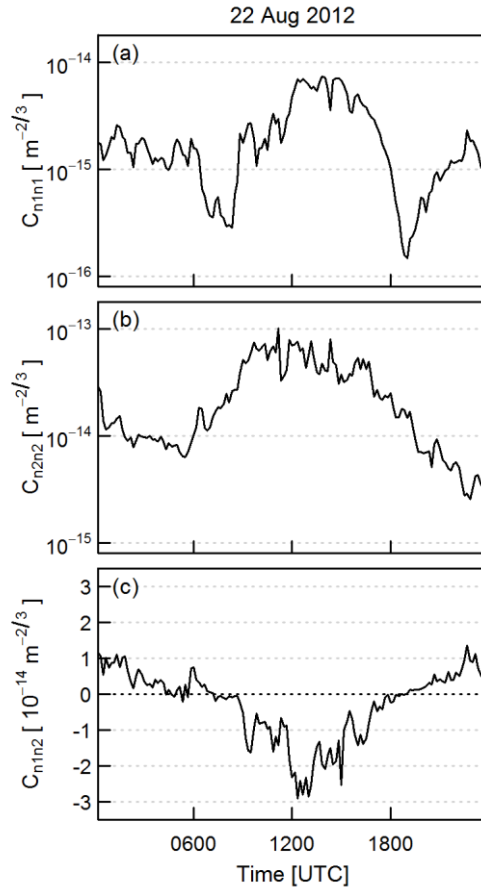
399 **Figure 4** Example power spectral density (PSD) and frequency ( $f$ ) spectra for (a, b) the BLS and (c, d) unfiltered MWS for  
 400 14:30-15:00 UTC on 02 July 2011. Smoothed spectra (data divided into 100 bins) are shown in black. The dashed lines  
 401 represent theoretically predicted slopes of  $-12/3$  and  $-8/3$  for the BLS and MWS respectively.

## 402 5. Results and discussion

### 403 5.1. Structure parameters

#### 404 5.1.1. Refractive index structure parameters

405 The refractive index structure parameters measured by the BLS ( $C_{n1n1}$ ) and MWS ( $C_{n2n2}$ ) and the  
 406 cross-structure parameter from the covariance of the BLS-MWS signals ( $C_{n1n2}$ ) follow clear diurnal  
 407 cycles. Data for an example day are plotted in Figure 5. Whilst  $C_{n1n1}$  and  $C_{n2n2}$  remain positive, the  
 408 cross-structure parameter can be positive or negative depending on whether the infrared and  
 409 millimetre-wave signals are correlated or anti-correlated.  $C_{n1n2}$  tends to be negative during the day  
 410 and positive at night. The sign change occurs at the morning and evening stability transitions.  
 411 Typically  $C_{n1n1}$  passes through sharp minima at these times, whereas the diurnal course of  $C_{n2n2}$  is  
 412 flatter and wider, without clearly defined minima. These findings are in broad agreement with data  
 413 from the LITFASS campaigns (Beyrich et al. 2005; Lüdi et al. 2005; Beyrich et al. 2012).

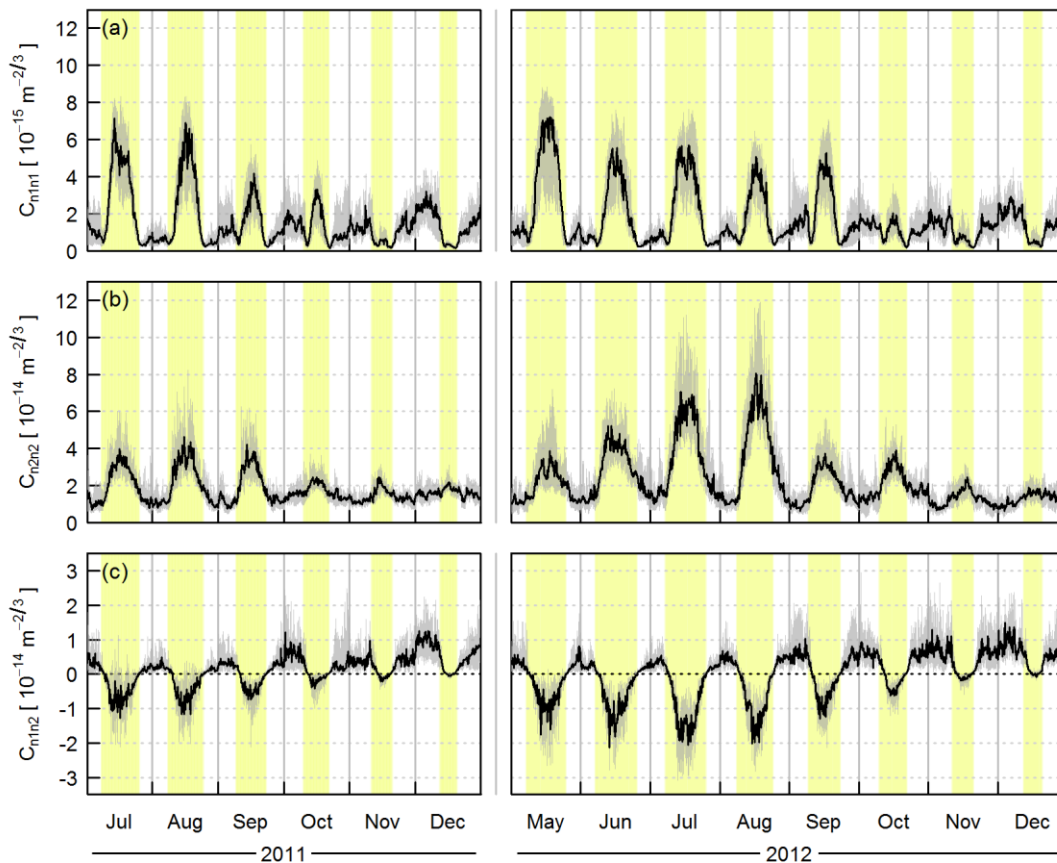


414

415 **Figure 5** Structure parameters of the refractive index as measured by (a) the BLS and (b) the MWS, and (c) the cross-  
 416 structure parameter as measured by the BLS-MWS combination for an example day (22 August 2012).

417 When averaged by month (Figure 6), the diurnal patterns are enhanced and seasonal trends are  
 418 revealed. The amplitudes of the diurnal cycles are largest in summer, except  $C_{n1n1}$  which peaks  
 419 slightly earlier in the year.  $C_{n1n1}$  is closely related to  $C_T^2$  and, in turn, the sensible heat flux. Hence the  
 420 peak in  $C_{n1n1}$  in late spring reflects the annual cycle of  $Q_H$ : approaching maximum insolation in mid-  
 421 summer, the total energy input is large but evapotranspiration rates are limited by phenological  
 422 development as maximal leaf area is not reached until later in the year. During winter, low radiative  
 423 input means the midday maximum in  $C_{n1n1}$  is small; larger values are observed at night. For  
 424 millimetre wavelengths  $C_{n2n2}$  tends to remain low throughout the night. The diurnal cycle in  $C_{n1n2}$  is  
 425 maintained across all months with changes in the position of the zero-crossings determined mainly  
 426 by atmospheric stability (usually the sign of  $Q_H$ , related to available energy and day length). In

427 December  $C_{nl2}$  is negative only for a very short period during the middle of the day. The effect of  
 428 day length is also seen in the positions of  $C_{nl1}$  minima, which move closer together as radiative  
 429 energy input decreases from summer to winter. Using the positions of  $C_{nl1}$  minima to indicate the  
 430 stability transition times generally worked well for this dataset, although performance was poorer in  
 431 winter when stability changes tend to be less well defined and conditions may remain close to  
 432 neutral throughout the day. Following the method described in Samain et al. (2012a), additional  
 433 restrictions were imposed on the times of morning (here after 0400 UTC) and evening (before 2100  
 434 UTC) transitions. In a few cases, cumulative daily net radiation was also used to distinguish  $C_{nl1}$   
 435 minima that were due to sudden cloud cover during daytime from  $C_{nl1}$  minima that were due to a  
 436 change of stability.

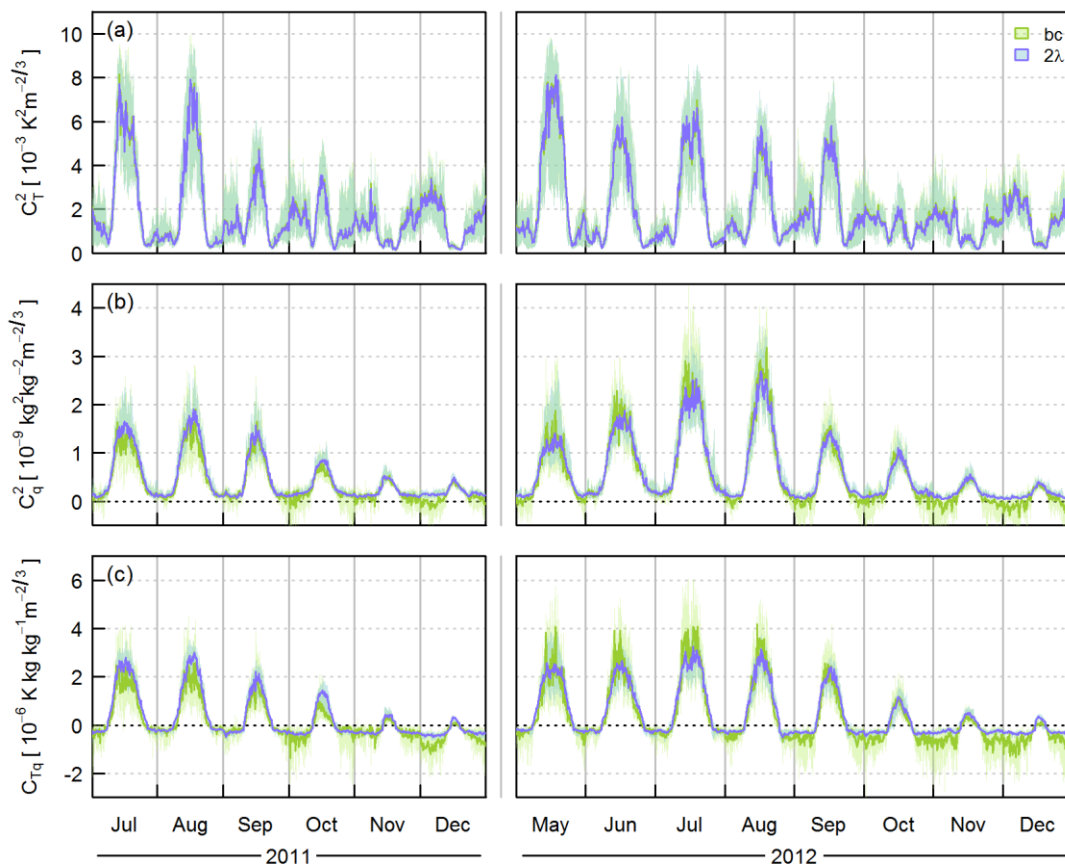


437

438 **Figure 6** Median diurnal cycles and inter-quartile ranges (shading) of the structure parameters of the refractive index as  
 439 measured by (a) the BLS and (b) the MWS, and (c) the cross-structure parameter as measured by the BLS-MWS  
 440 combination, separated by month. Yellow shading indicates periods when  $Q^* > 0 \text{ W m}^{-2}$ .

441 5.1.2. Meteorological structure parameters

442 There are clear parallels between the refractive index structure parameters (Figure 6) and the  
 443 meteorological structure parameters (Figure 7).  $C_{n1n1}$  is dominated by  $C_T^2$  with a small contribution  
 444 from  $C_{Tq}$  (of about 5%, which decreases as  $\beta$  increases (Green et al. 2001)). The cross-structure  
 445 parameter  $C_{n1n2}$  consists mostly of the  $C_{Tq}$  term and a contribution from  $C_T^2$ . When  $C_{n1n2}$  is negative  
 446  $C_{Tq}$  is positive. The dominant term in  $C_{n2n2}$  depends on the Bowen ratio:  $C_q^2$  usually dominates at low  
 447  $\beta$  but the  $C_{Tq}$  term is important too and forms a negative contribution to  $C_{n2n2}$  during daytime (when  
 448  $C_{Tq}$  is positive).



449

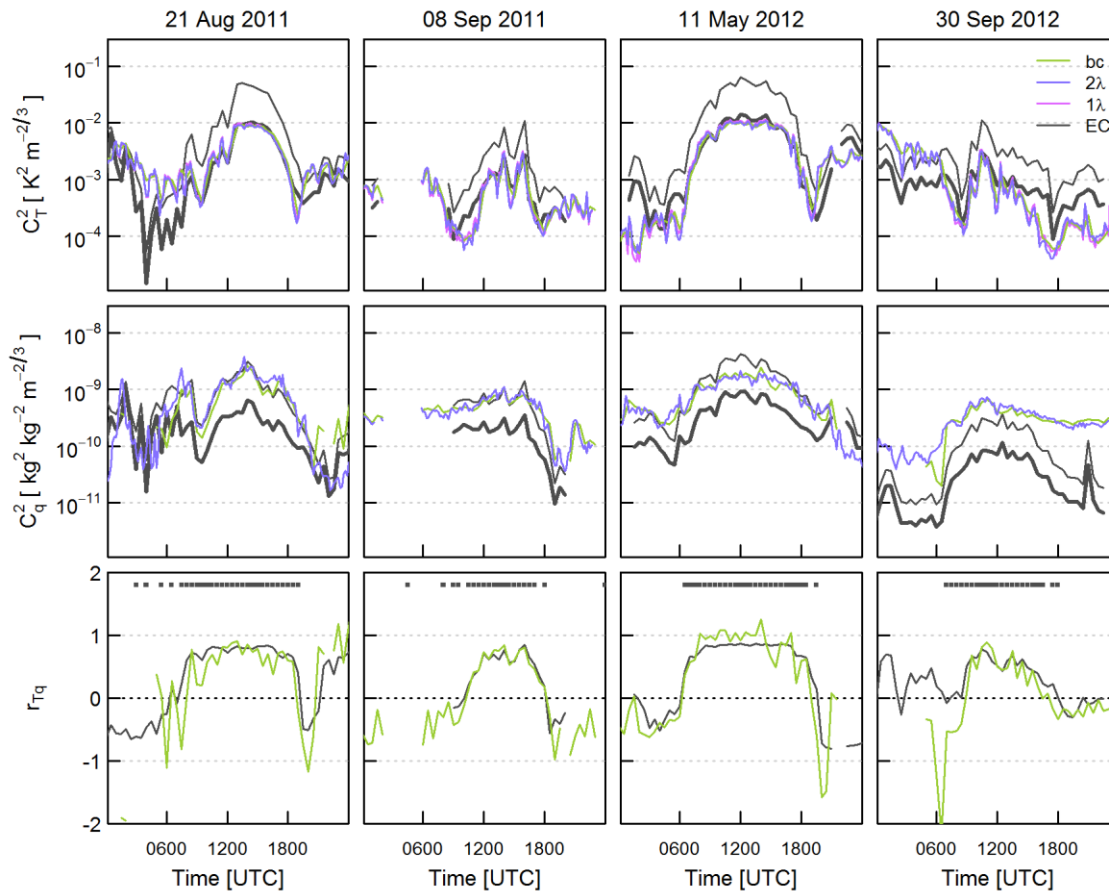
450 **Figure 7** Median diurnal cycles and inter-quartile ranges (shading) of the meteorological structure parameters (a)  $C_T^2$ , (b)  
 451  $C_q^2$  and (c)  $C_{Tq}$  calculated using the bichromatic (bc) and two-wavelength ( $2\lambda$ ) techniques. In (c)  $C_{Tq}$  for the two-  
 452 wavelength technique is given by  $\pm 0.8(C_T^2 C_q^2)^{1/2}$ .

453 5.1.3. Comparison of eddy covariance and scintillometry techniques

454 In Figure 8, meteorological structure parameters for individual days are compared to EC. As  
455 structure parameters are strongly height dependent, the EC values have been scaled to match the  
456 height of the scintillometry results ( $z_{ef} = 45.0$  m, Section 3.2.2). Scintillometer and EC values of  $C_T^2$   
457 and  $C_q^2$  are not expected to agree exactly due to the differences in source area and land cover  
458 composition, however, these independent measurements are often remarkably consistent. The  
459 correlation between the scintillometer and EC datasets gives confidence that the scintillometer  
460 setup is responding reasonably to changes in boundary layer conditions and measuring within the  
461 surface layer. The square of the correlation coefficient ( $r^2$ ) between the two-wavelength  
462 scintillometry and height-scaled EC data is 0.72 and 0.60 for  $C_T^2$  and  $C_q^2$  respectively. Considering  
463 daytime only,  $r^2$  increases to 0.86 for  $C_T^2$ , but remains about the same for  $C_q^2$  at 0.56.

464 ~~Height-scaled  $C_T^2_{-EC}$  closely matches  $C_T^2_{-BLS-MWS}$  with values being more similar during the day~~  
465 ~~than the night. On the other hand, height-scaled  $C_q^2_{-EC}$  is much smaller than  $C_q^2_{-BLS-MWS}$  with closer~~  
466 ~~agreement before height scaling.~~ These results suggest  $\beta_{EC}$  is larger than  $\beta_{BLS-MWS}$ , but the fact that  
467 the estimates of  $C_T^2$  are closely matched while  $C_q^2_{-BLS-MWS}$  is larger than  $C_q^2_{-EC}$  is indicative of a more  
468 complex situation (see Part 2).



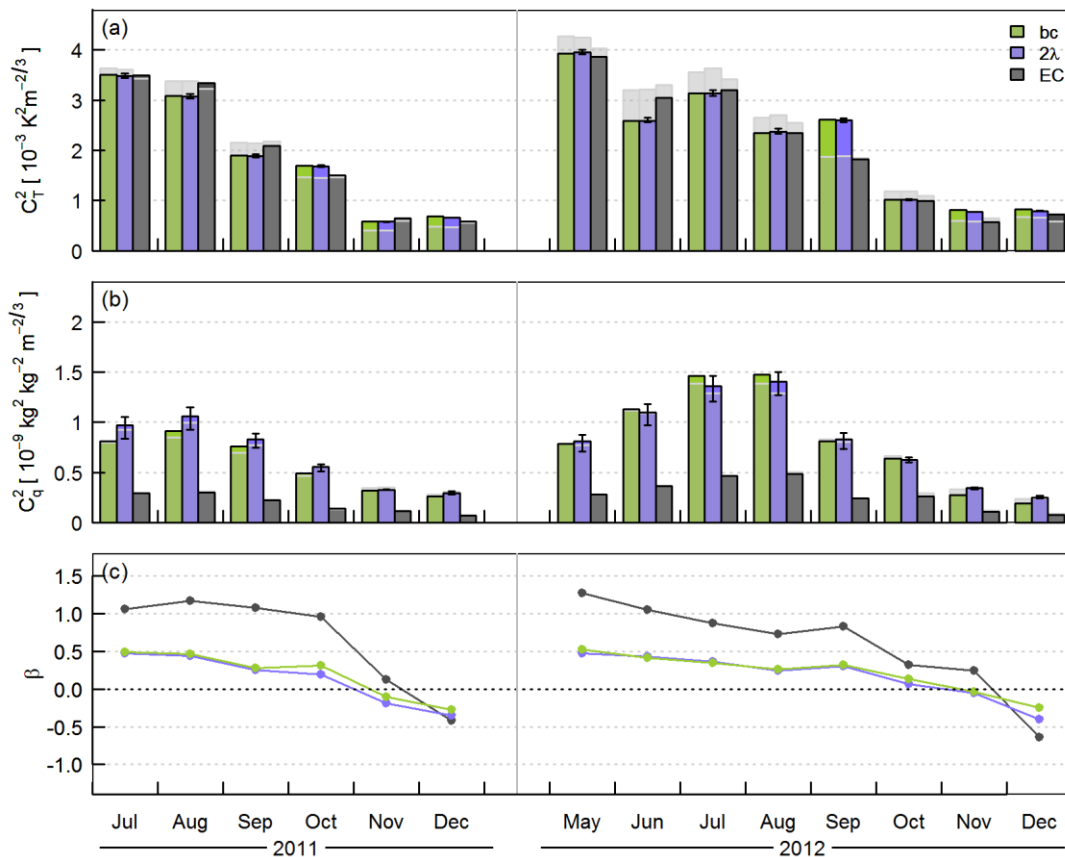


469

470 **Figure 8** Structure parameters of temperature and humidity and the temperature-humidity correlation coefficient for  
 471 selected days, derived from eddy covariance measurements (EC) and from the BLS-MWS system using the single-  
 472 wavelength ( $1\lambda$ ), two-wavelength ( $2\lambda$ ) and bichromatic-correlation (bc) methods. EC structure parameters are shown for  
 473 the EC measurement height (thin line) and scaled to the effective height of the scintillometry results (thick line). Unstable  
 474 times according to the EC data ( $L_{Ob} < 0$ ) are indicated by grey dots. Single-wavelength and two-wavelength data are for  
 475 10-min intervals; EC and bichromatic-correlation data are for 30-min intervals.

476 Structure parameters from the BLS-MWS and EC systems exhibit the same trends (but have  
 477 different magnitudes) over the course of the year (Figure 9).  $C_T^2$  is largest during late spring, whilst  
 478  $C_q^2$  peaks in July and August. There is variability between years attributed to drier conditions in 2011  
 479 than 2012 (July-August rainfall was 110 mm in 2011, 184 mm in 2012). In July-August 2011,  $C_T^2$  was  
 480 larger and  $C_q^2$  smaller than in the same months in 2012. In general, 2012 was much wetter than  
 481 2011 which explains consistently lower  $\beta$  in 2012 (Figure 9c). The BLS-MWS gives lower  $\beta$  compared  
 482 to EC (during summer daytime  $\beta_{BLS-MWS} \approx 0.5$  and  $\beta_{EC} \approx 1.0$ ), which is in accordance with the BLS-

483 MWS footprint being more vegetated, but similar seasonal behaviour is seen. In winter  $\beta$  becomes  
 484 negative as a result of reduced radiative input, and the difference between  $\beta_{BLS-MWS}$  and  $\beta_{EC}$   
 485 decreases. In terms of energy exchange fluxes, evapotranspiration continues throughout winter  
 486 because the availability of moisture is readily available, means evaporation continues throughout  
 487 winter whereas energy is limited so  $Q_H$  is directed towards the surface for much of the daytime, only  
 488 becoming positive for a short time around midday when there is sufficient energy (Ward et al.  
 489 2013a). Although it is more straightforward to consider this behaviour in terms of the fluxes  
 490 (discussed further in Part 2), the same conclusions could be inferred from the diurnal course of  $r_{Tq}$   
 491 (Figure 10) and positions of  $C_{nInl}$  minima (Figure 6a).



492  
 493 **Figure 9** Mean daytime (incoming shortwave radiation  $K_{\downarrow} > 5 \text{ W m}^{-2}$ ) (a-b) structure parameters (a-b) and (c) Bowen ratio  
 494 (c) calculated according to Equation 9 for each month calculated for the BLS-MWS system (bichromatic-correlation and  
 495 two-wavelength approaches) and eddy covariance data scaled to match the BLS-MWS height. For the two-wavelength

496 results  $r_{Tq_{2\lambda}} = \pm 0.8$ ; error bars in (a) and (b) indicate the effect of assuming  $r_{Tq}$  values of  $\pm 0.5$  and  $\pm 1.0$ . Light grey bars (a, b)  
497 indicate means calculated when both  $C_T^2$  and  $C_q^2$  from all three methods (bc, 2 $\lambda$  and EC) are available.

498 The performance of EC and scintillometry differs with atmospheric conditions. EC data from  
499 open-path gas analysers cannot be used if the instrument windows are wet, such as during and after  
500 rainfall (Heusinkveld et al. 2008). Consequently, water vapour measurements from open-path  
501 systems significantly under-represent these times and may result in an appreciable underestimation  
502 of mean  $Q_E$  (Ramamurthy and Bou-Zeid 2014) and  $C_q^2$ . Mean values for  $C_T^2$  calculated using daytime  
503 data only when all quantities are available concurrently (i.e.  $C_T^2$  and  $C_q^2$  from EC, two-wavelength  
504 and bichromatic-correlation methods (grey bars, Figure 9)) are larger compared to mean values  
505 calculated using all available daytime data (coloured bars) due to the exclusion of periods during and  
506 directly following rain (when  $C_T^2$  is typically relatively low  $Q_E$  is relatively high). In September 2012  
507 the opposite effect is seen because the EC data were limited by dirty IRGA windows when the  
508 weather was dry and sunny, hence it is generally high  $C_T^2$  values that are eliminated in this case.  
509 During summer, monthly mean  $C_q^2_{BLS-MWS}$  is reduced slightly for the concurrent dataset (grey bars)  
510 as times of high  $Q_E$  when water and energy are plentiful have been excluded. The overall results are  
511 not substantially changed for the restricted subset:  $C_T^2_{BLS-MWS}$  and  $C_T^2_{EC}$  are still similar whilst  
512  $C_q^2_{BLS-MWS}$  still exceeds  $C_q^2_{EC}$ , although the difference between  $C_q^2_{BLS-MWS}$  and  $C_q^2_{EC}$  is reduced  
513 slightly. The spectral correction (Section 3.2.2) would increase the EC structure parameters by 5-7%,  
514 which would further reduce the discrepancy between EC and BLS-MWS values.

515 As for most previous two-wavelength campaigns, typical Bowen ratios for this path are expected  
516 to lie below the problematic region of minimum  $C_{n2n2}$  (Section 2.1). Other urban studies suggest  
517 daytime  $\beta$  of around 1.0-1.5 for suburban sites, lower when precipitation is frequent (Grimmond and  
518 Oke 1995) and strongly dependent on the amount of vegetation (Grimmond and Oke 2002; Christen  
519 and Vogt 2004). However, although average  $\beta$  remains below 1.5 (Figure 9c), changing surface  
520 conditions can drive down the evapotranspiration on the timescale of a few days (e.g. drying of  
521 impervious surfaces (Ward et al. 2013a) or, at agricultural sites, senescing crops (Evans et al. 2012)),

522 producing substantial excursions from the average  $\beta$ . Such excursions are seen in this dataset,  
523 particularly for  $\beta_{FC}$ , whereas  $\beta_{2\lambda}$  seems to be limited to values  $\leq 1.3$ . There are two potential issues  
524 here: (a) the two-wavelength sign ambiguity and (b) the region of reduced sensitivity around the  
525  $C_{n2n2}$  minimum (Section 2.1). Selecting  $S_{2\lambda} = +1$  automatically restricts  $\beta_{2\lambda}$  to values below that at  
526 which the terms in Equation 3 cancel out ( $\beta_{2\lambda, min} = 2.0$ - $2.6$  for this dataset). For a few cases (when  $\beta$  is  
527 large), the ‘true’ structure parameters should be obtained from the alternative solution ( $S_{2\lambda} = -1$ ).  
528 Using the bichromatic-correlation results to identify times of high  $\beta$  suggests the impact is small ( $\beta_{bc}$   
529  $> \beta_{2\lambda, min}$  for a very small proportion of the data ( $< 0.3\%$  of daytime values)). A more significant issue  
530 appears to be reduced measurement capability for  $\beta_{2\lambda} > 1.3$ . As the true  $\beta$  increases, if  $C_{n2n2}$  does not  
531 decrease as much as expected from theory,  $\beta_{2\lambda}$  will likely be underestimated, and the corresponding  
532  $C_q^2$  (and  $O_E$ ) could be overestimated. It is thought that noise in the setup (instrumental or unwanted  
533 intensity fluctuations from absorption, for example) may constrain the measured value of  $\beta_{2\lambda}$  to a  
534 greater extent than suggested in the literature.

535 This region of reduced sensitivity of  $C_{n2n2}$  also compromises the performance of the bichromatic  
536 method, as measured  $C_{n2n2}$  will be mostly made up of noise contributions relative to the near-zero  
537 true value of  $C_{n2n2}$ . It follows that the correlation between BLS and MWS signals in this region is  
538 expected to be dominated by common instrumental or atmospheric effects such as absorption, or  
539 any electrical interference, mounting vibrations or obscuration along the path. Although these  
540 effects were not found to be problematic generally, they could become significant when the  
541 refraction signal diminishes at moderate  $\beta$ .

#### 542 5.1.4. Comparison of two-wavelength and bichromatic-correlation methods

543 The three estimates of  $C_T^2$  for the BLS-MWS path are similar (on average within 6%) whether the  
544 bichromatic-correlation, two-wavelength or single-wavelength approach is used. Larger deviations  
545 are seen between  $C_{q\_bc}^2$  and  $C_{q\_2\lambda}^2$  when measured  $r_{Tq\_bc}$  differs from the value assumed ( $\pm 0.8$ ) in the  
546 two-wavelength method (e.g. 21 August 2011, Figure 8). During daytime,  $C_{q\_2\lambda}^2$  is slightly larger than

547  $C_q^2$  in 2011 but the opposite is true for most of 2012 (Figure 7b, Figure 9b). This could be due to  
548 higher values of  $r_{Tq_{bc}}$  in 2012 (see Figure 10), which result in smaller  $C_T^2$  but larger  $C_q^2$  when  $r_{Tq} > 0$ .  
549 The value of  $r_{Tq}$  has a greater impact on  $C_q^2$  than  $C_T^2$  (compare error bars in Figure 9a, b). Had  $r_{Tq_{2\lambda}}$   
550 been assumed to be  $\pm 1.0$  instead of  $\pm 0.8$ ,  $C_q^2$  would have been 7% higher and  $C_T^2$  1% lower.

551 During winter night-times, large differences are observed between  $C_q^2$  and  $C_q^2$  which cannot  
552 be explained by differences in  $r_{Tq}$ . Negative values of  $C_q^2$  are frequently obtained (Figure 7b).  
553 These do not have a physical interpretation but are indicative of measurement limitations and  
554 coincide with large negative  $C_{Tq_{bc}}$ , which results from large positive  $C_{n1n2}$  (i.e. high correlation  
555 between BLS and MWS beams). Particularly during these times, but also in general, the bichromatic-  
556 correlation data show much greater variability than the two-wavelength data. To reduce this  
557 variability, bichromatic-correlation data are presented as 30-min averages, other than in Figure 7.

558 ~~As for most of the previous two-wavelength campaigns, typical Bowen ratios for this path are~~  
559 ~~expected to lie below the problematic region of minimum  $C_{n2n2}$  (Section 2.1). Other urban studies~~  
560 ~~suggest daytime  $\beta$  of around 1.0-1.5 for suburban sites, lower when precipitation is frequent~~  
561 ~~(Grimmond and Oke 1995) and strongly dependent on the amount of vegetation (Grimmond and~~  
562 ~~Oke 2002; Christen and Vogt 2004). However, although average  $\beta$  remains below 1.5 (Figure 9c),~~  
563 ~~changing surface conditions can drive down the evaporation on the timescale of a few days (e.g.~~  
564 ~~drying of impervious surfaces (Ward et al. 2013a) or, at agricultural sites, senescing crops (Evans et~~  
565 ~~al. 2012)), producing substantial excursions from the average  $\beta$ . Such excursions are seen in this~~  
566 ~~dataset, particularly for  $\beta_{ECT}$  whereas  $\beta_{2\lambda}$  seems to be limited to values  $\leq 1.3$ . There are two potential~~  
567 ~~issues here: (a) the two-wavelength sign ambiguity and (b) the region of reduced sensitivity around~~  
568 ~~the  $C_{n2n2}$  minimum (Section 2.1). Selecting  $S_{2\lambda} = +1$  automatically restricts  $\beta_{2\lambda}$  to values below that at~~  
569 ~~which the terms in Equation 3 cancel out ( $\beta_{2\lambda_{min}} = 2.0-2.6$  for this dataset). For a few cases (when  $\beta$  is~~  
570 ~~large), the true structure parameters should be obtained from the alternative solution ( $S_{2\lambda} = -1$ ).~~  
571 ~~Using the bichromatic correlation results to identify times of high  $\beta$  suggests the impact is small ( $\beta_{be}$~~

572  $> \beta_{2k\_min}$  for a very small proportion of the data (< 0.3% of daytime values)). A more significant issue  
573 appears to be reduced measurement capability for  $\beta_{2k} > 1.3$ . As the true  $\beta$  increases, if  $C_{n2n2}$  does not  
574 decrease as much as expected from theory  $\beta_{2k}$  will likely be underestimated, and the corresponding  
575  $C_q^2$  (and  $Q_L$ ) could be overestimated. It is thought that noise in the setup (instrumental or unwanted  
576 intensity fluctuations from absorption, for example) may constrain the measured value of  $\beta_{2k}$  to a  
577 greater extent than suggested in the literature.

578 The region of reduced sensitivity of  $C_{n2n2}$  also compromises the performance of the bichromatic  
579 method, as measured  $C_{n2n2}$  will be mostly made up of noise contributions relative to the near-zero  
580 true value of  $C_{n2n2}$ . It follows that the correlation between BLS and MWS signals in this region is  
581 expected to be dominated by common instrumental or atmospheric effects such as absorption, or  
582 any electrical interference, mounting vibrations or obscuration along the path. Although these  
583 effects were not found to be problematic generally, they could become significant when the  
584 refraction signal diminishes at moderate  $\beta$ .

## 585 5.2. Temperature-humidity correlation

586 Measured  $r_{Tq\_bc}$  follows similar seasonal and diurnal trends to  $r_{Tq\_EC}$  (Figure 10). During summer,  
587 there is a clear plateau of close to +1 around 0.8 during daytime and the transition times when  $r_{Tq}$   
588 changes sign are of short duration compared to the day length. In winter  $r_{Tq}$  remains below zero for  
589 most of the day but peaks at positive values around midday, though the average midday  $r_{Tq}$  is less  
590 than 1. The EC data rarely exceed the range -0.75 to 0.85, whereas inspection of the time-series  
591 reveals that  $r_{Tq\_bc}$  almost always follows a typical diurnal course but individual points may vary about  
592 the general trend (e.g. Figure 8). Some unrealistic values of  $|r_{Tq\_bc}| > 1$  are observed, even when  
593 averaged to 30 min (Figure 8; Figure 10). Lüdi et al. (2005) also reported frequent occurrences of  
594  $|r_{Tq\_bc}| > 1$ . Since  $r_{Tq}$  is a correlation coefficient these values ( $> 1$ ) do not have a physical  
595 interpretation, but result from uncertainties and thus indicate limitations of the measurement. The  
596 uncertainty in  $C_{nIn2}$  is around 20% at best (Lüdi et al. 2005). This inherent uncertainty associated

597 with individual measurements means the structure parameters from the bichromatic-correlation  
598 method show greater variability than from the two-wavelength method (Section 5.1.4), particularly  
599  $C_q^2$  and  $C_{Tq}$  which have a greater dependence on  $C_{nl\ln 2}$  than  $C_T^2$  does. For this reason, bichromatic  
600 results are presented at 30 min, rather than 10 min as for the two-wavelength method (Figure 8-  
601 Figure 11). In addition, to calculate  $r_{Tq}$ , the structure parameters must be combined (Equation 8) and  
602 so  $r_{Tq}$  amasses the uncertainties in each of the measurements.

603 Despite the high uncertainty, average  $r_{Tq}$  values provide information on the typical temperature-  
604 humidity correlation along the scintillometer path. This is an important quantity in its own right, as  
605 well as an indication of MOST violations. The literature suggests  $r_{Tq}$  is typically expected to be slightly  
606 less than +1 during the day, but negative and of smaller magnitude at night (Kohsiek 1982; Andreas  
607 et al. 1998; Meijninger et al. 2002a; Beyrich et al. 2005). According to Lüdi et al. (2005) the  $T$ - $q$  anti-  
608 correlation observed at night is 'less pronounced' than the positive correlation during daytime;  
609 Meijninger et al. (2006) also found  $r_{Tq}$  ranged between -0.5 and 0.9. Our measurements conducted  
610 in the suburban environment do not indicate lower  $T$ - $q$  correlation than over other surfaces. Indeed,  
611 it is thought that  $r_{Tq\_EC}$  likely underestimates the true values (as the sonic and IRGA are spatially  
612 separated). This supports the use of MOST and gives confidence that the measurements are made at  
613 sufficient height that the effects of surface heterogeneity are well-blended. Furthermore, the two-  
614 wavelength assumption  $r_{Tq} = +0.8$  is seen to be reasonable for unstable conditions, although  
615 probably  $r_{Tq} = -0.8$  is too large during stable conditions. Figure 10 suggests that these assumptions  
616 are less justified in winter.

617 In Figure 11 values of  $r_{Tq}$  measured in this study are separated into unstable and stable conditions  
618 (based on  $L_{Ob}$  from EC data and the timing of stability transitions according to  $C_{nl\ln 1}$  for the  
619 scintillometer data). During unstable conditions, measured  $r_{Tq}$  is positive and around 0.6 to 0.9  
620 whereas the stable values tend to be smaller at around -0.3 to -0.5 and more variable. In winter  $r_{Tq}$  is  
621 smaller and more variable (median  $r_{Tq\_EC}$  decreases from  $> 0.7$  in summer to  $< 0.5$  in December for

622 unstable conditions). Some studies have indicated a dependence of temperature-humidity  
623 correlation on  $L_{Ob}$ , with larger deviations from MOST as neutral conditions are approached (Li et al.  
624 2011; Nordbo et al. 2013), although other studies differ (De Bruin et al. 1993; Roth 1993). Part 2  
625 further explores the scaling of temperature and humidity structure parameters with stability.

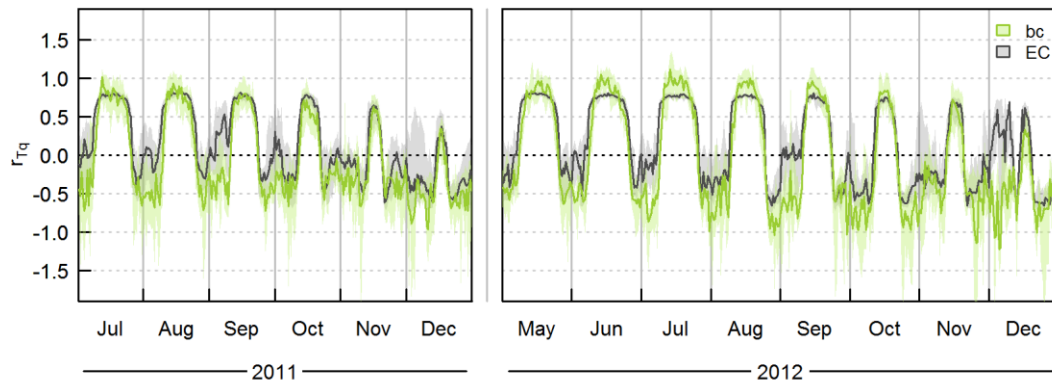
626 Some instances of positive nocturnal  $r_{Tq}$  are observed when the fluxes have the same signs – i.e.  
627 either unstable ( $Q_H > 0$ ) conditions prevail, or more frequently observed is dewfall ( $Q_E < 0$ ) under  
628 stable conditions (as on 21 August 2011 after 2130, Figure 8). In these cases the two-wavelength  
629 method is limited as negative  $r_{Tq}$  must be assumed in the absence of other information, whereas the  
630 bichromatic-correlation method often captures this behaviour. In general, nocturnal structure  
631 parameters (and fluxes) tend to be small so the absolute errors introduced by  $r_{Tq_{2\lambda}}$  of the wrong sign  
632 are fairly small, though they will always be biased in the same direction and so will accumulate over  
633 time.

634 The bichromatic-correlation data suggest larger daytime  $r_{Tq}$  in 2012 compared to 2011 but this is  
635 not seen in the EC data. The contrast between patches of hot, dry impervious areas and cool, wet  
636 vegetation may be reduced by altogether wetter surfaces in 2012, which is thought to increase  
637 correlation between temperature and humidity (Lamaud and Irvine 2006; Moene and Schüttemeyer  
638 2008; Ramamurthy and Bou-Zeid 2014). On the other hand, Lüdi et al. (2005) found lower  $r_{Tq}$   
639 coincides with lower  $\beta$ . Experiments designed to investigate the behaviour of  $r_{Tq}$  (and the  
640 performance of the bichromatic-correlation technique) under different conditions would be  
641 beneficial.

642 In winter, and also during night-time, turbulence tends to be less well-developed. This presents  
643 challenges to measurement theory. Measurements are also more likely to be outside the surface  
644 layer when stable stratification occurs and the boundary layer height is smaller. Due to the rough  
645 surface, near neutral conditions were far more common than stable and, for the most part, there  
646 remains a close match between the diurnal behaviour of EC and scintillometer measurements. On

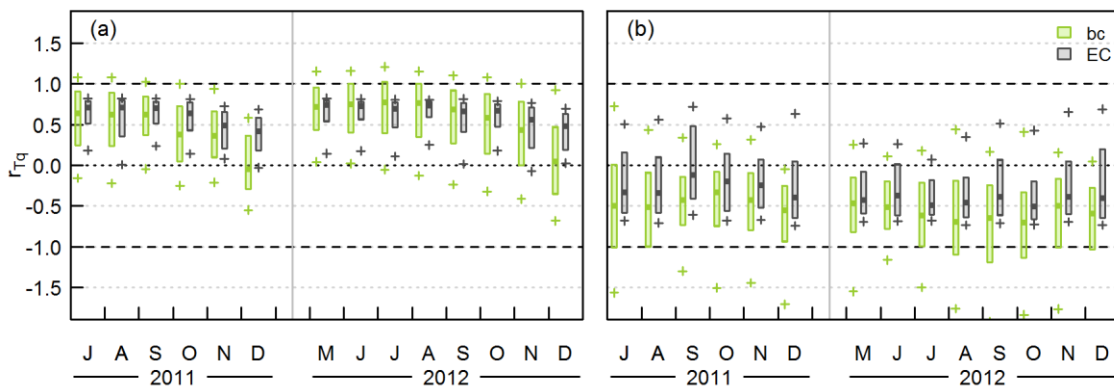


647 the few occasions when strongly stable conditions were observed at the EC station, comparison of  
 648 time-series indicated periods when the BLS-MWS was ~~likely higher in the atmospheric boundary~~  
 649 ~~layer than is ideal~~possibly above the surface layer, and thus potentially affected by other processes  
 650 not related to surface fluxes. However, these were relatively rare occurrences.



651

652 **Figure 10** Monthly median diurnal cycles and inter-quartile ranges (shading) of the temperature-humidity correlation  
 653 coefficient calculated from the BLS-MWS system via the bichromatic-correlation method and from EC.



654

655 **Figure 11** Boxplots of  $r_{Tq}$  from eddy covariance (EC) and the BLS-MWS bichromatic-correlation method for (a) unstable and  
 656 (b) stable conditions. Crosses indicate the 10<sup>th</sup> and 90<sup>th</sup> percentiles, boxes enclose the inter-quartile range (25<sup>th</sup> to 75<sup>th</sup>  
 657 percentiles) and heavy lines indicate the medians.

658 In this study, the performance of the bichromatic-correlation method was generally observed to  
 659 be poor under conditions of low crosswind speeds (the wind speed component perpendicular to the  
 660 BLS-MWS path). At times of low or near-zero crosswinds ( $< 2 \text{ m s}^{-1}$ ), the retrieved ~~values-quantities~~

661 are less robust,  $|r_{Tq_{bc}}| > 1$  is commonly observed and  $r_{Tq_{bc}}$  is highly variable frequently changing  
662 sign (even during the day when both turbulent fluxes are reasonably expected to be positive and EC  
663 data do not suggest otherwise). The reason for this is unknown, but two possible explanations are  
664 considered here. Firstly, Taylor's frozen turbulence hypothesis is assumed in order to relate intensity  
665 fluctuations to  $C_n^2$  (Clifford 1971; Wang et al. 1981). When crosswind speeds are low, this  
666 assumption is less justified and eddies decay as they are slowly blown through the beam. Correlation  
667 between the received scintillation pattern from one sample to the next is reduced compared to  
668 higher crosswind cases (Poggio et al. 2000). Correlation between the scintillation signals of the BLS  
669 and MWS will likely show greater variation too, depending on how the decay of eddies affects each  
670 beam, which would result in variability in  $C_{n1n2}$  that propagates through to  $r_{Tq_{bc}}$ . Secondly, when  
671 wind speeds are low, turbulence may be sporadic and not well-developed over the whole path  
672 length. Perhaps sudden gusts or turbulence events cause spuriously high correlation between BLS  
673 and MWS signals which outweighs the correlated scintillation signal the technique aims to measure.  
674 Given the complexity of this suburban site it is difficult to draw firm conclusions on this apparent  
675 effect of crosswind on bichromatic scintillometry at this stage. Given that the position of the  
676 spectrum is known to change with wind speed (Medeiros Filho et al. 1983; Nieveen et al. 1998; Ward  
677 et al. 2011), and that  $C_n^2$  can be underestimated if the filter excludes part of the scintillation signal  
678 under very low wind speed conditions (Solignac et al. 2012), the suitability of the bandpass filter was  
679 also re-examined. However, the choice of filter frequency did not seem to explain the poor  
680 performance and modifying the filter frequencies did not resolve the issues. Small changes in filter  
681 frequency generally did not produce substantial changes to the results, suggesting that the  
682 frequencies chosen are suitable for this dataset, but it is not critical that those exact values are used.

## 683 **6. Conclusions**

684 This study reports the first use of a two-wavelength scintillometer system in an urban area. The  
685 behaviour of structure parameters and temperature-humidity correlation is investigated at various  
686 timescales. By examining the structure parameters themselves, more direct insight into the

687 performance of the measurement techniques is gained; assessment of fluxes introduces additional  
688 uncertainties (e.g. similarity functions). Furthermore, structure parameters are important quantities  
689 in their own right. The spatial and temporal resolution of scintillometry observations offers  
690 advantages for assimilation into or evaluation of hydro-meteorological models. One approach for  
691 achieving this would be to work with structure parameters directly, rather than fluxes (e.g. Wood et  
692 al. 2013).

693 The structure parameters presented here extend previous observations to a different climatic  
694 region, different land cover type and, most importantly, across a much longer time period.  
695 Summertime behaviour is broadly in agreement with other published trials (Beyrich et al. 2005; Lüdi  
696 et al. 2005) but the long time-series presented here offers insight into seasonal variations. Day  
697 length, or more specifically, atmospheric stability, has a distinctive impact on the diurnal cycle of  
698 structure parameters and  $r_{Tq}$ . Overall, the structure parameters obtained from the BLS-MWS and EC  
699 systems exhibit remarkably similar tendencies. The Bowen ratio calculated from the measured  
700 structure parameters decreases across the two summer-to-winter periods studied here and  $\beta_{BLS-MWS}$   
701 is smaller than  $\beta_{EC}$ , attributed partly to different source area characteristics but also probable  
702 differences between the observational techniques. Part 2 explores energy partitioning further via  
703 turbulent fluxes.

704 As well as extending the two-wavelength technique to a new environment, several recently  
705 developed improvements have been implemented in the processing. To obtain the structure  
706 parameter of refractive index from the millimetre-wave scintillometer, the validity of the small  
707 aperture approximation is considered (~~Appendix A~~) and the more accurate full formula used instead  
708 (~~Equation 14b, for this setup~~). To adjust for the difference in effective heights between the BLS and  
709 MWS, the  $S$  factor approach of Evans and De Bruin (2011) was used. The structure parameters use  
710 the specific humidity formulation outlined in Ward et al. (2013b). The cross-correlation between BLS

711 and MWS signals enabled estimation of the temperature-humidity correlation coefficient, thus  
712 extending the application of the bichromatic-correlation method to the suburban surface.

713 The bichromatic-correlation method sometimes returns values outside the physically meaningful  
714 range  $|r_{Tq}| \leq 1$ . The inherent variability of the cross-structure parameter  $C_{n1n2}$  limits the accuracy of  
715 any particular measurement, whereas the two-wavelength results are more robust over shorter  
716 periods. On average, results closely follow the expected diurnal cycle of correlated temperature and  
717 humidity during the day and anti-correlated at night. Measured  $r_{Tq}$  is approximately 0.6-0.9 in  
718 unstable conditions; stable values are more variable but tend to be smaller in magnitude, averaging  
719 around -0.3 to -0.5. Observed  $r_{Tq}$  was furthest from  $\pm 1$  during winter and in near neutral conditions.  
720 Similar behaviour is seen in  $r_{Tq\_bc}$  and  $r_{Tq\_EC}$ , including times when the assumed two-wavelength  
721 value will be wrong.

722 Two-wavelength scintillometer systems have considerable potential to deliver large-area  
723 measurements representative of complex environments. Limitations of the two-wavelength method  
724 include the ambiguity due to two possible solutions for  $\beta$  and the region of reduced sensitivity  
725 around the  $C_{n2n2}$  minimum. Research is needed; firstly, to better understand the behaviour in this  
726 region and secondly, to investigate improvements to the instrumentation, setup or post-processing  
727 to minimise the impact. Advantages of the bichromatic-correlation method include additional  
728 information about the atmospheric conditions from  $r_{Tq\_bc}$ , e.g. the relative sign of the heat fluxes and  
729 to what extent MOST conditions are satisfied. For the minimal extra hardware requirements the  
730 recommendation is therefore to measure the bichromatic correlation even if the additional  
731 information is not used directly in data processing.

732 The large proportion of vegetation and cool, wet summers helped to maintain a low Bowen ratio  
733 in this study. In drier periods or at more built-up sites the results may have been less useable. Future  
734 work should focus on the performance of two-wavelength scintillometry under different conditions  
735 (notably low crosswind, high Bowen ratio, near neutral stability). Theoretical development (e.g.

736 modelling studies exploring the impact of differences in footprint and effective height between  
 737 instruments) combined with careful experimental testing is needed. Comparison data (structure  
 738 parameters and fluxes) from different methods will be required for thorough evaluation of these  
 739 techniques.

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## 746 **Appendix A. Validity of the small aperture approximation for millimetre-wave** 747 **scintillometers**

748 The log amplitude of a scintillometer system can be written in a generalised form (e.g. Lüdi et al.  
 749 2005),

$$\begin{aligned}
 \sigma_{\chi^1\chi^2} = & 4\pi^2 k_1 k_2 0.033 C_n^2 \int_0^\infty dK \int_0^L dx K K^{-11/3} \sin\left(\frac{K^2 x(L-x)}{2k_1 L}\right) \sin\left(\frac{K^2 x(L-x)}{2k_2 L}\right) \\
 & \times \left[ \frac{2J_1(0.5KD_{r1}x/L)}{0.5KD_{r1}x/L} \right] \left[ \frac{2J_1(0.5KD_{t1}(1-x/L))}{0.5KD_{t1}(1-x/L)} \right] \\
 & \times \left[ \frac{2J_1(0.5KD_{r2}x/L)}{0.5KD_{r2}x/L} \right] \left[ \frac{2J_1(0.5KD_{t2}(1-x/L))}{0.5KD_{t2}(1-x/L)} \right] J_0(K|d|)
 \end{aligned} \quad , \quad (A1)$$

751 where  $\sigma_{\chi^1\chi^2}$  is the covariance of log amplitude,  $C_n^2$  the refractive index structure parameter,  $K$  the  
 752 eddy wavenumber and  $x$  the position along the path of length  $L$ ;  $k$  is the optical wavenumber,  $d$  the  
 753 beam separation, and  $D$  the aperture diameter of the receiver (subscript  $r$ ) or transmitter (subscript  
 754  $t$ ) for each instrument (subscript 1 or 2) ~~separated by a distance  $d$~~ .  $J_0$  and  $J_1$  are Bessel functions of  
 755 the first kind. The three-dimensional Kolmogorov spectrum  $\Phi_n(K) = 0.033 C_n^2 K^{-11/3}$  is assumed.

756 For a single instrument, this reduces to the standard formula for a large aperture scintillometer  
 757 (Hill and Ochs 1978):

$$\begin{aligned}
 \sigma_{\chi}^2 = & 4\pi^2 k^2 0.033 C_n^2 \int_0^{\infty} dK \int_0^L dx K K^{-11/3} \sin^2 \left( \frac{K^2 x(L-x)}{2kL} \right) \\
 & \times \left[ \frac{2J_1(0.5KD_r x/L)}{0.5KD_r x/L} \right]^2 \left[ \frac{2J_1(0.5KD_t(1-x/L))}{0.5KD_t(1-x/L)} \right]^2.
 \end{aligned}
 \tag{A2}$$

759 For cases when aperture averaging is unimportant, the standard formula for small aperture  
 760 scintillometers,

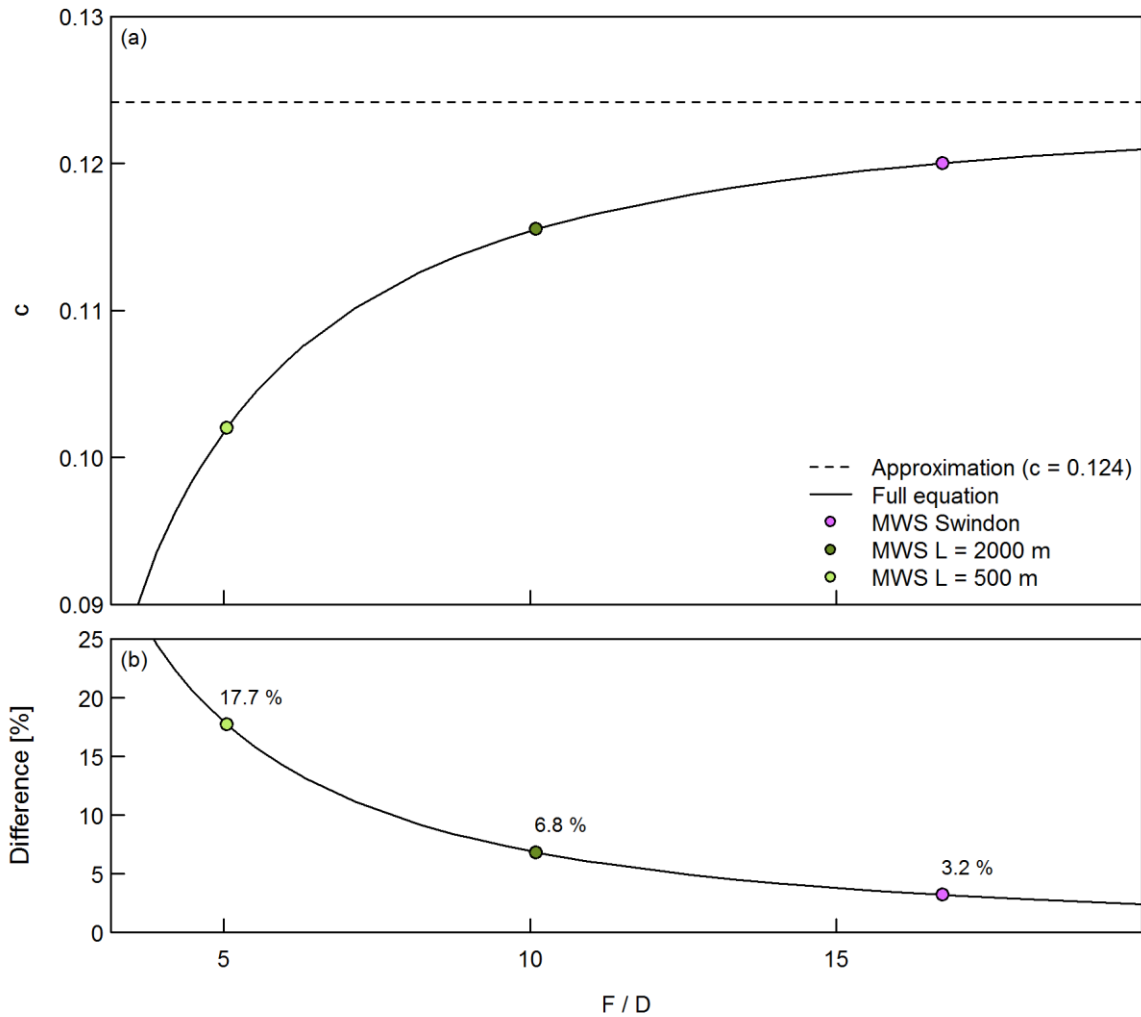
$$\sigma_{\chi}^2 = 4\pi^2 k^2 0.033 C_n^2 \int_0^{\infty} dK \int_0^L dx K K^{-11/3} \sin^2 \left( \frac{K^2 x(L-x)}{2kL} \right),
 \tag{A3}$$

762 which gives

$$\sigma_{\chi}^2 = ck^{7/6} L^{11/6} C_n^2
 \tag{A4}$$

764 on integration with  $c = 0.124$ , ~~is often applied~~ (Meijninger et al. 2002a; Lüdi et al. 2005; Meijninger  
 765 et al. 2006).

766 Here we consider the validity of applying the small aperture approximation to millimetre-wave,  
 767 microwave and radiowave systems. For the effects of aperture averaging to be insignificant, the  
 768 aperture diameter must be sufficiently small compared to the maximal diameter size of the first  
 769 Fresnel zone,  $F = (\lambda L)^{1/2}$ . With  $F$  around 10 times  $D$ , the small aperture approximation causes an  
 770 appreciable (7%) underestimation of  $C_n^2$  compared to evaluating the full formula (Figure A 1). The  
 771 relatively long path over Swindon means the difference between formulations is quite small here  
 772 (3%), but will be more important for shorter paths, shorter wavelengths or larger aperture  
 773 diameters. Use of the full equation also modifies the path-weighting function slightly; for Swindon  
 774 the difference in effective heights between using the approximation and full form is 0.15 m.



775

776 **Figure A 1** (a) Value of the multiplier,  $c$ , in Equation A4 when calculated using the full equation (Equation A2) as a function  
 777 of the ratio of Fresnel zone  $F$  to aperture diameter  $D$  and (b) percentage difference from the small aperture approximation  
 778 (Equation A3). Some example experimental setups are selected for the CEH-RAL MWS.

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