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Eddy-covariance data with low signal-to-noise ratio: time-lag determination, uncertainties and limit of detection

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Abstract

All eddy-covariance flux measurements are associated with random uncertainties which are a combination of sampling error due to natural variability in turbulence and sensor noise. The former is the principal error for systems where the signal-to-noise ra-

- ⁵ tio of the analyser is high, as is usually the case when measuring fluxes of heat, CO_2 or H_2O . Where signal is limited, which is often the case for measurements of other trace gases and aerosols, instrument uncertainties dominate. We are here applying a consistent approach based on auto- and cross-covariance functions to quantifying the total random flux error and the random error due to instrument noise separately. As with pre-
- vious approaches, the random error quantification assumes that the time-lag between wind and concentration measurement is known. However, if combined with commonly used automated methods that identify the individual time-lag by looking for the maximum in the cross-covariance function of the two entities, analyser noise additionally leads to a systematic bias in the fluxes. Combining datasets from several analysers
- and using simulations we show that the method of time-lag determination becomes increasingly important as the magnitude of the instrument error approaches that of the sampling error. The flux bias can be particularly significant for disjunct data, whereas using a prescribed time-lag eliminates these effects (provided the time-lag does not fluctuate unduly over time). We also demonstrate that when sampling at higher eleva-
- tions, where low frequency turbulence dominates and covariance peaks are broader, both the probability and magnitude of bias are magnified. We show that the statistical significance of noisy flux data can be increased (limit of detection can be decreased) by appropriate averaging of individual fluxes, but only if systematic biases are avoided by using a prescribed time-lag. Finally, we make recommendations for the analysis and reporting of data with low signal-to-noise and their associated errors.



1 Introduction

1.1 Motivation

Surface layer fluxes of gases such as carbon dioxide (CO₂) and methane (CH₄) are frequently determined using the eddy covariance (EC) technique. This approach has allowed direct measurements of canopy-scale emission/deposition rates which are rou-5 tinely incorporated into models of the carbon cycle and atmospheric chemistry. As with all measurements, the reported flux has an associated error, which should reflect both the systematic and random uncertainties of the measurement system. Systematic uncertainties arise e.g. from having an imperfect measurement system. For example, bandwidth limitations confine our ability to capture all the turbulent motions that contribute to the flux, and if uncorrected will introduce a bias. Another obvious systematic error is introduced by the uncertainty in the calibration standard. Identifying, minimizing and correcting sources of systematic bias in flux measurements remains an active area of research (Businger, 1986; Lenschow and Raupach, 1991; Lenschow et al., 1994; Mann and Lenschow, 1994; Massman, 2000; Massman and Lee., 2002). In contrast, 15 random errors do not bias the flux but reduce the overall confidence in an individual reported value. The main sources of random uncertainties in EC flux measurements are widely accepted as (i) the stochastic nature of turbulence sampling and (ii) instru-

focused on quantifying random uncertainties, ranging from rigorous theoretical investigations (Lenschow and Kristensen, 1985) to more practical approaches (Hollinger and Richardson, 2005). Usually these studies have addressed the problem from the perspective of an analytical system with good signal-to-noise ratio (SNR) e.g. fluxes of sensible heat, CO₂ or H₂O, because for these measurements the uncertainty in the flux is typically dominated by natural turbulence variability. For example, Maunder

ment noise and the resolution at which samples are recorded. Numerous studies have

et al. (2013) demonstrated that for fluxes of CO_2 and H_2O , the uncertainty associated with sensor noise was on the order of 1 % as opposed to stochastic errors which ranged between 20–30 %.



Increasingly, eddy-covariance is now being applied to measure fluxes of pollutants which are more difficult to measure precisely. Examples include measurements of volatile organic compounds (VOCs) (Karl et al., 2002; Langford et al., 2010; Park et al., 2013), ozone (O_3) (Coyle et al., 2009; Muller et al., 2009; Stella et al., 2013), nitric oxide (NO) (Rummel et al., 2002), nitrogen dioxide (NO₂) (Stella et al., 2013), nitrous oxide (NO) (Eugster et al., 2007; Famulari et al., 2010; Jones et al., 2011) and aerosols

- (N₂O) (Eugster et al., 2007; Famulari et al., 2010; Jones et al., 2011) and aerosols (Nemitz et al., 2008; Ahlm et al., 2009; Farmer et al., 2011, 2013). Measuring these scalars at a rate sufficient to meet the requirements for eddy covariance (i.e. several Hz) often results in a low SNR and increases the overall uncertainty in the flux.
- In addition, for many of these systems, co-location of anemometer and sensor is not possible. Closed path sensors require inlet lines that create a time-lag between the vertical wind velocities (w) and measured scalar concentrations (c). Correcting phase shifts between w and c is a key step in the calculation of fluxes and is routinely done by assessing the cross-covariance function between c and w which should reveal a max-
- ¹⁵ imum (in absolute terms), when the data are fully synchronised. Yet, when the random uncertainty is high, as is the case for many of these analysers, the cross-covariance becomes noisy, confounding the identification of a clear maximum. Through this data treatment, the low SNR in the concentration measurement, although a random error, may effectively introduce a systematic bias towards more extreme flux values. Recently,
- Taipale et al. (2010) reviewed the various options for determining time-lags with reference to VOC fluxes which often have low SNR. Three commonly used approaches are the maximum (MAX), average (AVG) and prescribed (PRES) methods, which are all well suited for the automated post-processing of eddy covariance data. Briefly, the PRES method involves using a constant time-lag, predicted on the basis of the physical
- ²⁵ characteristics of the sampling system, i.e. sample flow rate and inner diameter and length of the inlet. The MAX method systematically searches for the absolute maximum value in the cross-covariance function between w and c within a pre-defined time window. Finally, the AVG method proposed by Taipale et al. (2010) applies a centred running mean to the cross-covariance function and then selects the flux from the



unsmoothed cross-covariance function that corresponds to the maximum of the absolute running mean. The latter method was originally developed for use with VOC data measured by proton transfer reaction mass spectrometer (PTR-MS), but is generically applicable to any dataset with low SNR. There are currently no guidelines on the degree of smoothing that should be applied (i.e. the length of the running mean). In their study, Taipale et al. (2010) settle on a five second running mean, recognising that this is an arbitrary length.

With so many options available, it is clear that the calculated flux may differ depending on the chosen time-lag method. For example, in their study Taipale et al. (2010) confirm that using a prescribed time-lag may result in a systematic underestimation of

- the flux as the "true" time-lag is likely to vary over time due to fluctuations in pumping speed but also due to the degree of absorption/desorption with the inlet wall and its effect on the effective transport time through the tube. Especially for the more water soluble compounds this may change with humidity and or the aerosol coating of the in-
- ¹⁵ let. Similarly, systematically searching for a maximum within a noisy cross-covariance with multiple local maxima may well bias fluxes towards more extreme values (Laurila et al., 2012). The AVG method offers something of a compromise between the two approaches, but some systematic bias may still remain.

We hypothesise that the bias induced by using methods that search for a maximum in the cross-covariance is closely linked to the random error in the flux, which is in part a function of the SNR of the analytical instrumentation and in some cases may be greater than the systematic error induced from using a prescribed time-lag. In order to address this hypothesis an appropriate method is needed to quantify the random error in the flux and separate it into sampling and instrument error components.

1.2 Common approaches for quantifying random flux errors

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Assuming the time-lag is known, the random error of an eddy covariance flux can be estimated in a variety of ways (Lenschow and Kristensen, 1985). One traditional method is mainly used to estimate the flux error due to the limited sampling of the



stochastic nature of turbulence. It is based on the variance of the instantaneous values of w'c' and the integral time scale and is estimated as (Lumley and Pafanofsky, 1964; Wyngaard, 1973; Lenschow et al., 1994):

$$\mathsf{RE} = \left[\frac{2\sigma_{W'C'}^2 \tau_{\mathsf{FC}}}{L}\right]^{0.5}$$

- ⁵ where *L* is the length of the averaging period in seconds, $\sigma_{w'c'}^2$ is the variance of the time-series of instantaneous values of w'c' over a typical averaging period (~ 30 min) and τ_{Fc} is the integral time scale, i.e. the average time-scale over which correlation persists. The integral time scale can be directly estimated by integrating the area under the auto-covariance of $\overline{(w'c')}'$ to the point of first zero crossing. However, this gets more difficult for cases with high noise levels, as the auto-covariance becomes more scattered resulting in multiple zero crossings including some artificially close to the zero time-lag. This has the consequence that the integral timescale derived by this method becomes physically meaningless. In theory, additional sensor noise should increase the random error but in this case the reduction in the estimate of τ_{Fc} has the knock-on
- effect of minimising the error estimate. Consequently, this approach appears unsuitable in situations where signal is limited. An alternative approach, for conditions of neutral stability, is to approximate the integral time scale by dividing the measurement height (*z*) above the zero plane displacement (*d*), by the mean wind speed (\overline{u}). Yet, Rannik et al. (2009) found this method to overestimate the integral scale by a factor of two and consequently the random flux error by a factor of 1.4.

Mahrt (1998) offered an alternative method that negates the use of the integral timescale by splitting the time series into sub-records and formulating the error as the standard error between sub-records (Mahrt, 1998; Rannik et al., 2009):

$$\mathsf{RE} = \left[\frac{\sigma_{\mathsf{Fc.sub}}^2}{n}\right]^{0.5},$$

(1)

(2)

such that, *n* is equal to the number of sub records and $\sigma_{Fc.sub}^2$ is the variance of the *n* different fluxes calculated for the *n* different sub-records. This random error reflects a combination of the natural variability of the (genuine) atmospheric concentration and instrument noise, but since it calculates subsequent flux values, it appears likely that it s particularly sensitive to low frequency changes.

In cases where the time-lag is unknown, random flux errors are often assessed based on the statistical properties of the cross-covariance function used to identify the time-lag. This technique, first conceived by Wienhold et al. (1995) and developed further by Spirig et al. (2005), involves taking the SD of the cross-covariance func-

- ¹⁰ tion at a distance far from the zero time-lag (typically several times the integral time scale). In theory, the cross-covariance in this region reflects both random sensor noise and varibility of the (genuine) atmospheric signal/concentration thus, multiples of the SD can yield a random flux error at a given confidence interval (e.g. 1.96 × σ = 95th; 3 × σ = 99th). This technique is described further in Sect. 2.2.
- ¹⁵ While the cross-covariance method is widely used, few studies have attempted to go beyond this and isolate the effects of random sensor noise, mainly due to its negligible influence in many conventional eddy covariance systems. Noticeable exceptions include the work of Shurpali et al. (1993) who proposed a new technique for estimating random instrument uncertainty which was popularised in the mid-nineties (Clement
- et al., 1995; Billesbach et al., 1998). In this approach the flux of a tracer is measured while sampling air with a constant mixing ratio e.g. directly sampling from a gas standard, and hence any observed flux is purely a reflection of the random instrumental noise. This method has proved extremely robust, but has the obvious disadvantage of requiring routine data acquisition to stop while the random instrument uncertainty is assessed.

Billesbach (2011) proposed a more practical approach for quantifying random uncertainties from sensor noise. The so-called "random shuffle approach" involves random re-shuffling of one of the variables in time and thereby removing any covariance between source/sink terms and transport, leaving only accidental correlations which can



mostly be attributed to instrument noise. This is an intriguing option, yet, if we consider a measured time series c, which is made up of some genuine signal (x) as well as instrumental noise (ε), then the effective amplitude of a time shuffled time series is still composed of $x + \varepsilon$ and therefore the uncertainty is likely overestimated.

⁵ More recently Mauder et al. (2013) approximated errors associated with random instrument noise by first calculating the signal-to-noise ratio of the analyser using an auto-covariance function and then using a basic error propagation to estimate the contribution of that noise to the uncertainty in the cross-covariance:

$$\mathsf{RE}_{\mathsf{noise}} = \sqrt{\frac{\left(\sigma_{\mathsf{C}}^{\mathsf{noise}}\right)^2 \sigma_{w}^2}{N}},$$

¹⁰ In this approach, $\sigma_{\rm C}^{\rm noise}$ is the SD of the instrument noise, derived using an autocovariance function (see Sect. 2.1 for details), $\sigma_{\rm w}^2$ is the variance of the vertical wind velocity and *N* is the number of data points in the flux averaging period. This method, also implemented by Peltola et al. (2014) and Rannik et al. (2015) is relatively simple to apply but as yet, its effectiveness has not been fully validated for use with EC and DEC data.

In this study we explore a further possibility for estimating the portion of random error attributable to sensor noise by combining the ideas of Billesbach (2011) and Mauder et al. (2013), focusing in particular on the interplay between random instrument uncertainty, cross-covariance peak width and the systematic flux bias induced when de-

termining the flux through the use of a cross-covariance function (Taipale et al., 2010; Laurila et al., 2012). In understanding this linkage, our aims are to (i) validate the use of Eq. (3) for use with EC and DEC data sets, (ii) outline an optimal strategy for calculating and reporting random errors and (iii) for determining time-lags for eddy covariance data with low SNR and to draw conclusions on the value of flux measurements made with low SNR.



(3)

2 Methods

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2.1 Quantifying random white noise from analysers

Instrumental noise comes in both structured and unstructured forms. For example, the 50–60 Hz signal from a mains AC power supply might introduce a structured noise into

a time series, and optical fringes often introduce periodic features in optical spectroscopic approaches. By contrast, uncorrelated white noise can result from minor fluctuations in the mechanics of instrument components, or fluctuations in temperature, pressure or humidity. Here we focus our attention on unstructured, white noise only, and define the SNR for a given time series c as:

10 SNR =
$$\frac{\sigma_{\chi'}^2}{\sigma_{\varepsilon}^2}$$
,

where $\sigma_{x'}^2$ is the variance of the genuine signal of a measured timeseries, c ($c = x + \varepsilon$, where x is genuine signal and ε is noise) and σ_{ε}^2 is the variance of the noise. In order to establish the relative contributions of both signal and noise components of c we apply an auto-covariance to c' of the form:

$$AC_{(\tau)} = \overline{(x' + \varepsilon) (x'_{\tau} + \varepsilon_{\tau})}, \qquad (5)$$

where τ is the time-lag (in number of data points or sampling intervals) and primes denote fluctuations about the mean. White noise can only contribute to the autocovariance at $\tau = 0$ (Lenschow et al., 2000; Maunder et al., 2013) as it has no structure (i.e. the noise on an individual data point is uncorrelated to the noise of the adjacent data points). As the auto-covariance function moves away from zero, the contribution of instrument white noise is removed and thus the difference between AC₍₀₎ and AC₍₁₎ gives an estimate of random instrument noise. The underlying trend in the auto-covariance function of the genuine signal depends on the biophysical (source/sink



(4)

strength) signature of the compound being measured, and the structure within the turbulence signal which is itself a function of atmospheric stability. The presence of a trend or "structure" in the auto-covariance is a sign of genuine signal in the data, whereas an auto-covariance with no underlying trend is the definition of white noise. Where

- a genuine signal is present it is therefore necessary to extrapolate the positive auto-covariance function back to the zero point. This is typically done using only the first few points e.g. AC₍₁₋₅₎. The noise can then be estimated as the difference between AC₍₀₎ and AC_(1-5 extrapolated) and is depicted in Fig. 1a. In some cases the auto-covariance decreases exponentially and therefore it is appropriate to fit these points using an exponential extrapolation as opposed to the linear fit depicted in Fig. 1 and used throughout
- this study.

Using the auto-covariance function as opposed to the auto-correlation function means the calculated signal and noise are variances and retain their original units. Taking the square root gives the SD of both the signal and noise components.

- ¹⁵ The auto-covariance is a convenient method when working in the time domain, but alternatives are available when analysing the data in the frequency domain. Figure 1b shows the variance spectrum for w'T'. The red line shows the spectra of unmodified temperature data from an ultrasonic anemometer and the blue line shows the same temperature data deteriorated through the addition of Gaussian white noise with a SD
- of 1 K. In the frequency domain, on this plot, the fall-off towards higher frequencies in the inertial sub-range should follow a -5/3 slope, while white noise follows a +1 slope. This enables the noise variance to be quantified as the area between solid and dashed lines in Fig. 1b, although, visually, the area becomes proportional to the noise variance only on a log-linear plot as opposed to the log-log depiction shown here (Stull, 1988).
- It should be noted that the auto-covariance method is unsuitable if the measured time series (*c*) is not used with the original time resolution, e.g. if it was first re-sampled to a different sampling frequency in order to match the sonic time resolution. Similarly, this technique does not apply to structured noise, because $AC_{(1)}$ would still be affected



by such noise. In the auto-covariance approach, structured noise may or may not show up as a departure from the -5/3 slope at high frequencies.

Throughout this paper we utilise the auto-covariance method in the time domain as it is readily applicable to both eddy covariance and disjunct eddy covariance (DEC) datasets.

2.2 Quantifying random flux errors and the limit of detection

As discussed previously, the precision with which a flux can be measured is commonly approximated from the properties of the cross-covariance function between w' and c' $(f_{w'c'})$. For time-lags τ much different from the true time-lag, the SD of $f_{w'c'}(\tau)$ provides a measure of the random error affecting the flux (1995; Spirig et al., 2005). Multiplying this value ($\sigma_{f_{w'c'}} \times 3$) gives an estimate of the measurement precision at the 99th confidence intervals which can be used as the flux limit of detection (LoD). This threshold does not only depend on the SNR of the concentration measurement, but also varies with wind speed and atmospheric stability. Therefore, for each new averaging period it is necessary to recalculate the LoD. Whilst this technique allows for the separation of a "genuine" flux signature from the general noise of the covariance, the determination of the SD is often done using somewhat arbitrary boundaries (e.g. -150 to 180 and +150 to 180 s, or defined as some multiple of the integral timescale, Spirig et al., 2005), and thus as the turbulence structure evolves throughout the day, these limits

- may become more or less appropriate. Any correlation between c' and w' within these bounds is either purely accidental and reflects the random noise in the time-series or it is due to organised structures that persist over much longer time intervals suggesting that turbulence is not stationary or statistically not well covered in the measurement. Furthermore, a trend in scalar data can result in a cross-covariance which remains
- ²⁵ positive or negative over wide ranges rather than the expected fluctuation around zero. Figure 2a and b shows the calculation of the LoD via the SD (LoD (Wienhold/Spirig; blue dashed line) to sensible heat flux data from a forest site, for cases where the cross-covariance oscillates around zero and is offset from zero, respectively. In the lat-



ter case (Fig. 2b) many points of the cross-covariance function lie outside the limit of detection.

- A modification of the $\sigma_{f_{w'c'}}$ approach is to use the root mean squared deviation (RMS) of $f_{w'c'}$ from zero within the same specified region (greyed area – Fig. 2a and b), which reflects the variability in the cross-covariance function in these regions, but also its offset from zero. Figure 2c shows the LoD for sensible heat flux data calculated using both the RMS_{*f*_{w'c'}} and $\sigma_{f_{w'c'}}$ methods. The two methods agree very closely for periods where the cross-covariance fluctuates regularly around zero as in Fig. 2a, but where the covariance is predominantly of one sign the SD approach derives significantly smaller limits of detection, which we believe to be underestimates of the true uncertainty. Im-
- portantly, using linear detrending of the scalar data as opposed to block averaging reduces this effect but does not completely remove it. For this data set, 14% of block averaged data would have been rejected using the LoD based on $RMS_{f_{w'c'}}$ as opposed to 4% using the traditional $\sigma_{f_{w'c'}}$ method. In contrast, when applying linear detrending
- to these data the percentage of data rejected fall to 6 and 3% for the RMS_{*f*_{w'c'}} and the $\sigma_{f_{w'c'}}$ methods, respectively. In light of these findings we utilise the RMS_{*f*_{w'c'}} method for all calculations of the flux LoD in this study. Recommendations for the application of the RMS method to ozone eddy-covariance flux data are outlined in Nemitz et al. (2015).

2.3 Calculating the effect of instrument noise on the flux error

- ²⁰ Analysis of the statistical properties of the cross-covariance function seems to offer a practical approach for approximating the total random error of the flux, because the variability of the cross-covariance function comprises both instrument noise and the variability of the (genuine) atmospheric concentration. Yet, as discussed above, isolating the instrumental component of the total random error remains a challenge. Here,
- we attempt to untangle the two errors using an approach similar to the "random shuffle" method of Billesbach (2011). Rather than shuffling the measured scalar time series to remove any covariance between c' and w', we generate a new time series of equal length comprised purely of Gaussian white noise. The SD of the white noise



is set to match that of the instrument noise, ε' , which can be calculated using the auto-covariance method described in Sect. 2.1. The resulting time series shares the statistical properties of c', minus the contribution of the genuine analyser signal x' and therefore the effect of the instrument error on the flux error can now be calculated by combine the DMS method to the genuine and ε' .

⁵ applying the RMS method to the cross-covariance of $f_{w'}\varepsilon'$.

The six steps of this method are summarised as follows:

- 1. Perform an auto-covariance of the scalar prime c' to obtain the SD of the instrument noise ε' .
- 2. Generate a time series of white noise with a SD matching that of the instrument noise.
- 3. Calculate the cross-covariance $f_{w'c'}$.

10

- 4. Calculate the cross-covariance $f_{W'}\varepsilon'$.
- 5. Apply RMS method to $f_{W'C'}$ to obtain total random error (RE).
- 6. Apply RMS method to $f_{w'}\varepsilon'$ to obtain Instrumental random error (RE_{noise}).
- ¹⁵ In theory this numerical exercise seeks to quantify the same error approximated by Maunder et al. (2013) (Eq. 3), whilst making no assumptions on the shape of the distribution of w'. Therefore we can use this approach to validate Eq. (3) for use with both EC and DEC data sets and assess its performance when applied to data sets with varying levels of SNR. The random instrument errors calculated using both these ²⁰ approaches are compared in Sect. 3.1.

Although this proposed technique does not make any assumption about the distribution of w', it does make the assumption that the instrument noise follows a Gaussian distribution which is not always the case. For example, concentrations have often been found to be skewed towards larger values. In particular, tracers which show a high de-

²⁵ gree of variability at low mean concentrations may be log-normally distributed: concentrations are not constrained towards larger values, but cannot physically be negative.



The combined frequency distribution of w' and c' has been found to be more closely approximated by a Gram–Charlier equation than a Gaussian distribution (Milne et al., 2001). In addition, the statistical noise generated by instruments that derive concentrations from count events, e.g. counting particle number, ions (as the PTR-MS does for

5 VOC fluxes or the Aerosol Mass Spectrometer for submicron aerosol chemical fluxes), follows a Poisson distribution, which at low concentrations may act on the flux in a different way to a normally distributed instrument noise.

With this in mind we performed several tests to determine if the covariance between the vertical wind velocity and a time series of white noise is sensitive to the distribution

- ¹⁰ of the noise selected. For a single 30 min averaging period the covariance was calculated between w' and ε' whereby the artificially generated noise (ε') was either Gaussian, Poisson or log normally distributed as seen in Fig. 3a. The white noise flux for the same averaging period was repeatedly calculated, using a prescribed time-lag, for 5000 artificially generated time-series each, and the resulting distributions are shown
- in Fig. 3b. All three white noise distribution types are evenly distributed about zero, which demonstrates that unstructured white noise creates a random uncertainty in the flux but does not induce a systematic bias, regardless of its distribution. These findings provide assurances for eddy covariance systems that induce a Poisson counting noise that flux biases are not created.
- These findings confirm the theoretical considerations of Lenchow and Kristensen (1985), that, if the time-lag is known, the presence of uncorrelated noise induces a random uncertainty in the flux but does not induce a systematic bias. Nonetheless, this conclusion does not consider the interplay of this noise with the determination of a time lag, which is vital for sensors that are spatially separated from the vertical wind veloc-
- ity measurement, and its potential to introduce a bias that is a function of the random error.



2.4 Effect of instrument noise on time-lag determination

2.4.1 Signal-to-noise simulations

In order to investigate the influence of unstructured white noise from analysers and the method of time-lag determination on calculated fluxes, a series of simulations were performed using 31 days of sensible heat flux data (see Supplement). Time-lags were determined using the three main methods outlined above, MAX, AVG and PRES. For the AVG method, a further ten scenarios were implemented, whereby the running mean applied to the cross-covariance was increased from 0.5 to 5 s in 0.5 s intervals. In all scenarios the time-lag was sought within a 10 s window which ranged from -5 to +5 s, with the true time-lag obviously being 0 s. For the AVG method, the running mean was applied over a larger window to ensure the mean was properly centred for all data in the 10 s window. To accurately control the analyser noise level, the SNR of the temperature data was first quantified using the auto-covariance approach outlined above. The signal was then deteriorated by adding Gaussian white noise until a target signal-to-noise ratio was achieved to within a 1% tolerance. Sensible heat fluxes were calculated using

- block averaging and a reference flux was determined by calculating the flux with zero lag from the un-manipulated temperature time series. This process was repeated ten times for temperature data with a signal-to-noise ratio (SNR⁻¹) ranging between 200 and 0.05. In addition, the above simulation was repeated three more times to assess
- the impact of adopting disjunct sampling protocols of 2.5, 5 and 7.5 s as is common for measurements of VOC fluxes by PTR-MS and aerosol fluxes by Q-AMS. The overall bias between simulated time series and the reference was determined by the gradient of the regression between 31 days of reference data vs. those of the simulations.

2.4.2 Peak width simulation

The covariance between the genuine signals of c' (e.g. x') and w' gives a peak with respect to time-lag in the cross-covariance function. Superimposed on top of this peak



are the contributions from the covariance of the error components of c' and w' e.g. $w'_{\varepsilon}c'_{\varepsilon}$. It stands to reason that the broader the peak, the greater the probability of detecting an extreme local maximum i.e. detecting a peak in $w'_{c}c'_{c}$ on top of the genuine covariance, w'c'. Consequently, the peak width of the genuine covariance becomes an important consideration when assessing the potential bias induced through the choice of time-lag determination. In order to assess the sensitivity of flux measurements to the peak width, we ran a second set of simulations on two identical artificially generated chirp signals (e.g. a signal that decreases in frequency over time). This type of signal, generated within LabVIEW (National Instruments, Austin, Texa, USA), was chosen as a convenient means of producing time series to represent the "genuine" signals of x' and w' which contained multiple frequencies. In a series of 12 iterations, Gaussian white noise (ε') was added to x' until a target signal-to-noise ratio was met. In a second round of iterations the initial frequency of the chirp signal was decreased from 0.075 to 0.005 Hz in 0.005 Hz intervals. As the frequency was reduced, the full width at half the maximum (FWHM) of the covariance peak increased, resulting in a matrix of fluxes 15 calculated using 12 signal-to-noise ratios (100-0.05) vs. 15 covariance peak widths

ranging between 0.9 to 12 s (FWHM). For each point in the matrix the error relative to the flux calculated from the unmodified chirp signals was calculated.

2.5 Real world data

- ²⁰ Simulating the effects of different time-lag determination methods and the effects of SNR is a useful exercise, but it is important to verify that these are representative of real world data. We assessed the performance of each lag method on example data from a variety of analysers operated in field experiments with varying levels of signal-to-noise, bearing in mind that the SNR for a given application will depend on concen-
- trations and instrument operation. The analysers included ultrasonic anemometer (Gill HS), a condensation particle counter (CPC, TSI Model 3776), an Ultra High Sensitivity Aerosol Spectrometer (UHSAS, PMS, Boulder, USA), tuneable diode laser (TDL, Aerodyne Research Inc.) as well as disjunct data from a Proton Transfer Reaction Mass



Spectrometer (PTR-MS; Ionicon, Innsbruck, Austria). Figure 4, shows the frequency distribution of the SNR of 30 min averaging periods for each of the analysers.

A detailed description of each of the data sets used is supplied in the Supplement.

3 Results and Discussion

5 3.1 Calculation of random flux errors

The procedure for calculating random errors using the auto-covariance approach was applied to EC fluxes of sensible heat (A) and DEC fluxes of isoprene (B) and acetone (C), and the results are shown in Fig. 5. The error bars denote the total random error obtained from the cross-covariance function (3 × RMS_{*fw/c/*}) and the central panels show
¹⁰ how that error is divided between the random instrument error (RE_{noise}) and natural variability of turbulence and the (genuine) scalar concentrations (RE_{var}). For the fluxes of sensible heat the random instrumental error is very low reflecting the excellent SNR of the sonic anemometer. In contrast, the instrumental error for fluxes of acetone is very large, likely due to the very low atmospheric concentrations of acetone. For isoprene
¹⁵ a clear diurnal cycle is visible which shows the relative contribution of the instrument error is largest at night when the isoprene signal is lowest and the signal-to-noise ratio is low. During the daytime isoprene concentrations increase improving the SNR of the

analyser which sees the error due to natural variability of the (genuine) atmospheric concentration become the dominant source of uncertainty in the flux measurement. 20 Overall, absolute errors are larger during the day, when turbulence is larger.

The lower panels show scatter plots of the random instrument error calculated using the numerically calculated Gaussian white noise flux vs. the analytical approximation of Mauder et al. (2013), e.g. Eq. (3). The two methods give consistent results to within a few percent for both eddy covariance and disjunct eddy covariance data sets. There-

²⁵ fore, implementation of either method can enable operators to estimate the minimum detectable flux for their analyser under a given turbulence regime.



3.2 Bias effects of different time-lag determination methods

3.2.1 Dependence on signal-to-noise ratio

The simulations applied to sensible heat flux data reveal a distinct relationship between the signal-to-noise ratio of the analyser and the relative flux bias for both the MAX and

- AVG lag determination methods. Figure 6 shows the results for 10 Hz eddy covariance data. It is immediately apparent that methods that systematically search for a maximum (red trace) induce an average positive bias (towards more extreme emission or deposition) to the reported flux which increases exponentially as the analyser signal deteriorates. For this dataset, the relative bias can be as much as 18%. Adopting the
- AVG method can significantly reduce this error provided the applied running mean is of a suitable length. However, selection of an inappropriate running mean may allow the bias to persist and can also become negative when overly long. The reason for the negative lies in the fact that the shape of the peak in the covariance spectrum tends to be skewed, while the running average of the AVE peak fit is symmetrical. However, theory
- cannot currently explain the skewness which is therefore difficult to predict. By contrast, the use of a fixed time-lag (for the anemometer temperature data the time-lag is known to be zero), uncertainty increases as the signal is more and more deteriorated, but to a smaller degree, and its sign is random.

Figure 7 shows the same set of simulations for data that have disjunct sampling in-

- tervals of 2.5 (Fig. 7a), 5 (Fig. 7b) and 7.5 (Fig. 7c) seconds. It is well understood that adopting a disjunct sampling approach reduces the statistical sample size and thus increases the random error (Lenschow et al., 1994; Rinne and Ammann, 2012). However, it is frequently assumed that the increased random error does not translate to a systematic bias in the measured fluxes, but our simulations show this not to be the
- case. The poor sampling statistics and high instrument noise combined with the MAX method for time-lag identification can potentially lead to 100 or even 200 % overestimation in the mean flux.



The method used to determine the time-lag is a key factor in accurately resolving the flux as already demonstrated with the 10 Hz eddy covariance data. Additional random uncertainty incurred from disjunct sampling amplifies the bias at signal-to-noise ratios less than 100, and in this instance resulting in relative errors of about 300 % at SNR =

- 0.01 where Δ*t* is set to 7.5 s. Importantly, this offset appears avoidable if a prescribed time-lag is used. When using a prescribed time-lag, individual flux measurements are biased either high or low compared with the standard eddy-covariance approach that uses a larger number of data points, but when analysed collectively, the net error is close to zero. This implies that where the signal-to-noise ratio is very high it may be
 necessary to average over more data to reduce the relative random error and thus ensure no systematic bias is introduced.
 - These findings come with the caveat that in these simulations the prescribed timelag was a known quantity. When applied to real world data the adopted time-lag must be a well defined parameter that does not drift significantly over time. Failure to meet this requirement would undoubtedly result in a systematic underestimation of the flux,
- this requirement would undoubtedly result in a systematic underestimation of the flux, the magnitude of which would become a function of the cross-covariance peak width. This is discussed further in Sect. 3.2.2.

Of equal importance is the magnitude of the expected flux. Fluxes may be large even if the scalar mixing ratios are very noisy and thus the relative error is dependent on both the signal-to-noise ratio and the magnitude of the flux. Thus, although Figs. 6 and 7 describe the behaviour of the bias, the exact values depend on the magnitude of the fluxes and also the structure of the underlying turbulence data. However, these simulations do serve to highlight those aspects that make flux data more vulnerable to systematic errors.

25 3.2.2 Influence of peak width

Figure 8 shows the results of the peak width simulations on two artificially generated, multi-frequency signals. As well as reiterating the exponential increase in the relative error associated with the analyser signal-to-noise ratio, this plot serves to demonstrate



that the FWHM maximum of the covariance peak is an equally important parameter. Broader covariance peaks result in a higher probability of an extreme maximum being chosen and therefore both the probability of overestimating the flux and the magnitude of the bias are closely linked to the peak width. The logarithmic relationship between

- ⁵ turbulence and height mean trace gas and aerosol flux measurements at higher elevations above ground are more at risk to systematic bias when the MAX or AVG methods are employed. Conversely, the probability of systematic underestimation of the flux through the use of a prescribed time-lag at these measurement heights is somewhat reduced due to a greater tolerance afforded by the increased peak width. Massman
- (2000) and Hörtnagl et al. (2010) recognised that further broadening of the covariance peak is possible through the attenuation of scalars through long inlet lines and also through an increase in the analyser integration time. Therefore, when working on tall towers above forests or urban canopies one should be aware of the greater potential for systematic bias and should consider the use of a prescribed time-lag which may
- ¹⁵ provide the most representative (least biased) estimate of the flux. In general terms, when sampling at lower heights such as above crops or grassland, the potential for bias is lessened, whereas the likelihood of underestimating the flux through the use of a prescribed time-lag is increased. Nonetheless, during more unstable periods the potential for a greater influence of lower frequencies in the turbulence spectra cannot be overlooked (Horst, 2000).

When using a prescribed time-lag the attenuation of samples through long inlet lines, adsorption/desorption effects and fluctuations in pump flow rate are not typically considered. More often, the prescribed value is chosen purely on the basis of the inlet dimensions and a spot measurement of the flow rate, or through a single test where

a pulse in concentration and wind speed is created near the anemometer/inlet. In these cases the potential for underestimating the flux is large. It is therefore good practice to initially search for the time-lag using the AVG or MAX method and to plot the results as a histogram or time series. This may confirm that the time-lag was indeed constant or it may reveal a clear peak or trend in time-lags which can be used to set the prescribed



value. For instruments that measure multiple species (e.g. mass spectrometers, optical spectrometers), it may be suitable to use the average time-lag of a species that shows a clear flux (and thus clear time-lags) as a proxy for the other compounds being measured. However, difference between gases in terms of solubility and therefore adsorp-

tion/desorption characteristics need to be considered. For example, it is well known that for closed-path sensor measurements of CO₂/H₂O a longer time-lag is found for H₂O than for CO₂ (lbrom et al., 2007). While most appropriate for instruments that measure multiple species simultaneously, this approach can also be applied to instruments that measure species sequentially (e.g. the quadrupole-based PTR-MS or AMS) as long as
 the scan cycle is accounted for when assigning time-lags.

3.3 Real world flux measurements with low SNR

3.3.1 Mirroring

When measuring trace gas and aerosol fluxes, the fast sampling requirements of eddy covariance can result in low SNRs. Working in this region can see the random flux error equal or even exceed the magnitude of the flux, potentially introducing a bias as discussed above. In addition to these effects, where a maximum in the cross-covariance is still sought, the derived flux may switch between emission and deposition values of similar magnitude. This phenomenon, which we term "mirroring", is observed in the example flux data shown in Fig. 9 which were obtained using TDL, UHSAS and PTR-MS

- instruments and occurs because the random error in the flux is sufficiently large to span the zero line. It may be tempting to remove the negative (positive) fluxes on the basis of biophysical implausibility. For example, when measuring aerosol fluxes where only deposition fluxes are expected, it would be easy to dismiss positive fluxes as artefacts. Nevertheless, removal of these points is clearly incorrect and would only serve to bias
- the reported averaged data high (cf. Nemitz et al., 2002). Under such circumstances the reported flux is predominately driven by fluctuations in the amount of turbulence which evolves throughout the day to give a diurnal cycle which might be mistaken for



a flux. Adopting the MAX or AVG methods exagerates the mirroring by systematically choosing the furthest point away from zero which in the extreme case can result in the very unatural flux distributions shown in Fig. 10. Adopting the AVG method with 5 s running mean limits this effect to a certain extenent, but a noticible dip around zero remains. Importantly, the use of a prescribed time-lag eliminates the splitting of data from either side of zero to give a much more natural looking flux distribution.

In addition to the calculated fluxes, the red time traces show the Gaussian white noise flux (F_{GN}), i.e. the cross-covariance between an artificially generated white noise signal that shares the same SD as the analyser noise. Here, both tracer and Gaussian noise fluxes have been calculated using the MAX method. For acetone, F_{GN} is of a similar magnitude which indicates that in this example the fluxes shown are almost

- a similar magnitude which indicates that in this example the fluxes shown are almost entirely due to coincidental covariance between the vertical wind velocity and instrument noise. In contrast, the range of benzene and particle number fluxes both at least partially exceeds the Gaussian white noise flux and show sustained period of emission
- fluxes indicating the presence of a "genuine" flux which is, for certain periods, distinguishable from the random sensor noise flux. The remaining data would undoubtedly fall below conventional limits of detection and the individual 30 min flux measurements would ordinarily be rejected. Yet, the question remains whether any useful information on the net exchange can still be extracted from data such as these and is discussed in
- detail in Sect. 3.3.2. Finally, the TDL N₂O fluxes are consistently larger than the Gaussian white noise flux despite an apparent mirroring in the data. In this case it is likely that the instrument noise is comprised of both unstructured white noise and structured noise perhaps from optical fringes which our method does not take into account. It should be noted, that we here tried to identify data series which showed the effects
- ²⁵ of limited SNR. All these instruments obviously can perform better in situations where fluxes are larger or where instrumentation parameters are further optimised.



3.3.2 Limit of detection for individual and averaged fluxes

For data where mirroring is observed there are either no fluxes present or insufficient statistics to resolve them. If these data are to be utilised at a 30 min time resolution then they are of little use and should be rejected. In some cases extending the averaging

⁵ period may provide the additional statistical information required for resolving the flux, but it is also increasingly likely to violate the requirements for stationarity. Yet, in the literature measured fluxes are seldom utilised at the resolution with which they are collected, but are more typically aggregated either to establish longer term budgets, by time of day or by a meteorological parameter such as light or temperature in order to establish robust relationships for model parameterisations. Where data are averaged, presented and utilised in this way, the statistical significance of the average can be evaluated against the LoD of the ensemble average (LoD) calculated from the LoDs of the *N* individual data points that entered the average as:

$$\overline{\text{LoD}} = \frac{1}{N} \sqrt{\sum_{i=1}^{N} \text{LoD}^2}$$

¹⁵ For this reason, data that fail averaging period specific LoD criteria, such as the time series shown in Fig. 9, should not be discounted out of hand as they may retain useful information on the net exchange when averaged, but they need to be reported together with an estimate of the random error.

Figure 11a shows the averaged diurnal fluxes of the acetone time series shown in Fig. 9 for 1, 7, 14 and 21 day periods (Acton et al., 2015). The shaded areas represent the averaged LoD for the same period. Data falling within the shaded area cannot be resolved by the measurement system, but those points falling outside this area are statistically significantly different from 0 at the 95th percent confidence interval. The fluxes were determined using both the MAX and PRES time-lag methods, with the latter based on the average isoprepe time-lag (plus the duty cycle offset). We have already

 $_{\rm 25}$ $\,$ based on the average isoprene time-lag (plus the duty cycle offset). We have already



(6)

demonstrated that using the MAX method biases the fluxes high and consequently after two weeks of data are averaged, many of the fluxes appear to exceed the $\overline{\text{LoD}}$. In contrast, those fluxes calculated with a prescribed time-lag, which limits the bias, fail to exceed the $\overline{\text{LoD}}$ even when averaged over a three week period and would be rejected. This serves as an important example of how the choice of time-lag determination can lead to the reporting of a flux which in essence is not statistically different from zero.

Figure 11b shows the same plot for the much longer time series of benzene (Valach et al., 2015). In this case we observe how the averaged fluxes eventually exceed the LoD as the number of samples are increased. With this in mind, when targeting trace

- ¹⁰ gas or aerosol fluxes with instrumentation limited in signal or where the expected fluxes are small, it may be prudent to attempt to measure for longer to ensure statistically robust estimates on the net exchange are obtained. The improvement of LoDs for ensemble data does not only apply to temporal patterns. For example, Fig. 12 illustrates how benzene flux data can be averaged as a function of traffic density in order to pa-
- rameterise emission rates from vehicles. Provided that the 30 min LoDs are averaged according to Eq. (6), flux data with limited SNR can be used in numerous ways that should go beyond the reporting of average diurnal emission rates.

4 Conclusions and recommendations

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In this study we have carefully examined the key factors affecting the analysis of flux data with high noise level. Clearly, the effect of instrument noise on flux measurements has been studied before. Here we have developed a technique to quantify the uncertainty due to sensor white noise by first quantifying the amount of noise and then calculating a flux with this noise level. This numerical approach has been used to validate the approximations of Mauder et al. (2013) and shows consistent results when applied to both EC and DEC data sets. Both these methods can be easily implemented

²⁵ applied to both EC and DEC data sets. Both these methods can be easily implemented into eddy-covariance processing software and share the key advantage over the more



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traditional experimental approach of Shurpali et al. (1993) that measurements do not need to be interrupted for the assessment to take place.

Most of the earlier analyses of random errors have been carried out under the assumption that the time-lag between wind and concentration measurement is known.

- ⁵ To our knowledge, the systematic bias introduced through the interplay between random sensor noise and the techniques used to determine the time-lag has so far not been studied very systematically, although the problem has been highlighted in general terms in several publications and text books. Taipale et al. (2010) studied the effect of routines that are based on maximising the absolute value of the cross-covariance for
- disjunct data produced by PTR-MS and introduced the AVG approach to reduce this effect. We here show that, in general, the effectiveness of this approach depends on the length of the running mean chosen and the shape of the peak in the cross-covariance function.

Our work highlights the benefit of constraining the time-lag of the air sampling and quantifying it as precisely as possible by external means when working with noisy sensors. In practical terms, this might mean controlling the inlet flow carefully and heating the inlet line to minimise adsorption/desorption effects, or deriving the time-lag from a simultaneously measured compound with better SNR. Here we compile a list of general recommendations for the collection and processing of eddy covariance data with limited SNR.

- 1. Where possible log anemometer and scalar data to a single computer. This eliminates uncertainty in time-lags due to clock drift and should restrict time-lags to positive time shifts.
- 2. In-line flow meters should be used to monitor and record fluctuations in pumping speeds

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3. Use of pressure controllers to limit fluctuations in sample flow rate (this may not always be possible when high flow rates are required to maintain turbulent flow and increases the required pumping capacity and therefore power consumption).



- 4. For water soluble trace gases, heating of the entire inlet line should be considered to limit adsorption/desorption effects. Care needs to be taken not to generate aerosol evaporation artefacts for trace compounds that are distributed between the gas and aerosol phase according to a temperature dependent equilibrium.
- 5. On-line monitoring of sample humidity may be necessary to account for absorption desorption effects.
 - 6. Use of the MAX method to generate an initial histogram or time series of time-lags, followed by a second analysis using the PRES approach with a thus informed predefined time-lag may be preferable to either estimating the time-lag based on sampling flow rates alone or using the MAX method for final processing. This is because time-lags estimated from the sampling flow do not consider the potential for a phase shift in the cross-covariance due to either signal attenuation or limited response of the instrumentation (Massman, 2000; Hörtnagl et al., 2010).
 - 7. When reporting processed fluxes, results should be reported even if they are below the single-flux LoD, as long as they fulfil other quality control criteria. However, each individual flux value should be reported with its own quantification of the random uncertainty, so that uncertainties can be combined when fluxes are averaged.

We conclude that a significant number of fluxes (and derived values such as emission factors) reported in the literature are biased towards larger values (more distant from zero), because insufficient attention has been given the way the time-lag was estimated. By contrast, we demonstrate here the value of individual flux measurements even if they individually fall below the LoD, for obtaining statistically significant longerterm averages, as long as care has been taken during data processing.

²⁵ The Supplement related to this article is available online at doi:10.5194/amtd-8-2913-2015-supplement.

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Figure 1. Illustration of the two methods for determination of analyser variance attributable to unstructured white noise, though **(a)** the use of an auto-covariance function and **(b)** from the variance power spectra in the frequency domain. The inset plot in **(a)** shows how the first few points of the auto-covariance function can be used to extrapolate the contributions of signal and noise components at a lag of zero.





Figure 2. Cross-covariance functions for sensible heat fluxes (**a** and **b**) measured above a Douglas fir forest in Speuld, Netherlands, during two example measurement periods. (**c**) shows the limit of detection for sensible heat fluxes calculated either by block averaging or linearly detrending the vertical wind velocity and temperature data. The LoD were calculated using both the SD approach (Wienhold/Spirig) and the RMS approach. See text for further details.





Figure 3. (a) shows the frequency distributions of Gaussian, log-normal and Poisson noise (ε') of identical SD. **(b)** shows the frequency distributions of the flux calculated from the unstructured white noise over a period of 5000 iterations. The mean average flux for each noise distribution are marked with dashed lines, which are all close to zero and consistently confirm that no systematic bias is introduced to a flux measurement regardless of the type of noise used.





Figure 4. Signal-to-noise ratios of typical instruments used for the flux measurement of various trace gases and aerosols. Analysers include a sonic anemometer (temperature) and PTR-MS (isoprene, methanol and acetone) operated above a mixed Oak forest at a height of 32 m and above a city (benzene). Particle number concentrations were measured by a CPC and UHSAS (single size bin) above a Douglas fir forest and N₂O measurements were made above a grass land field in 2003 using the first generation of tuneable diode laser.





Figure 5. Sensible heat (a), isoprene (b) and acetone (c) fluxes and accompanying errors. Upper panels show the measured fluxes with error bars denoting the total random error (RE). The central panels show how the total random error can be divided errors associated with instrument noise (red, RE_{noise}) and the variability in turbulence at the genuine atmospheric concentration (blue, RE_{var}). The lower panels show scatter plots of the random instrument noise calculated using the analytical approximation of Mauder et al. (2013) and the numerical method outlined in this study.







Figure 6. The average relative bias of a half-hourly flux as a function of the analyser signal-tonoise ratio for 31 days of 10 Hz eddy covariance sensible heat flux data acquired at a height of 32 m. The signal-to-noise ratio of the temperature data was deteriorated to match pre-defined limits. The errors shown are relative to the sensible heat flux calculated using the unmodified temperature data and a constant (0 s) time-lag.



Figure 7. The average relative bias of a half-hourly flux as a function of the analyser signal-tonoise ratio for 31 days of 10 Hz disjunct eddy covariance data compared with the standard eddycovariance result. **(a)**, **(b)** and **(c)** correspond to disjunct sampling intervals of 2.5, 5 and 7.5 s, respectively. The signal-to-noise ratio of the temperature data was deteriorated to match predefined limits (see text for details). The errors shown are relative to the sensible heat flux (with no disjunct interval e.g. standard eddy covariance) which was calculated using the unmodified temperature data and a constant (0 s) time-lag.





Figure 8. Image plot depicting the exponential relationship between the average relative bias and both the signal-to-noise ratio of the analyser and the full width half maximum (FWHM) of the cross-covariance function peak for simulated eddy covariance flux data calculated using the MAX time-lag method.

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Figure 9. An example of "mirroring" in eddy covariance data with low SNR processed with the MAX time-lag method. The data were obtained by TDL **(a)**, UHSAS (Data from a single size bin - b) and PTR-MS (**c** and **d**) instruments during four separate measurement campaigns. Red circles show a flux calculated from a Gaussian white noise time series based on the signal-to-noise ratio of the raw data and also calculated using the MAX time-lag method.





Interactive Discussion





Figure 11. (a) Averaged diurnal profiles of acetone flux data obtained using a quadrupole PTR-MS. Increasing the number of data points averaged does not bring the PRES flux above the LoD (Greyed area indicating the LoD at the 95th percentile) indicating no detectable flux. By contrast, the MAX fluxes which are biased high, show some periods above the LoD which are an artefact of the MAX time-lag determination method. **(b)** Averaged diurnal profiles of benzene flux data obtained using a quadrupole PTR-MS. Increasing the number of data points averaged from 14 to 56 is sufficient to distinguish the flux calculated with a prescribed time-lag from the LoD (Greyed area indicating the LoD at the 95th percentile) and indicating a clear flux of benzene.







