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Application of locality principle to radio occultation studies of the Earth's atmosphere and ionosphere

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Abstract

A new formulation of previously introduced principle of locality is presented. The principle can be applied for modernization of the radio occultation (RO) remote sensing of the atmospheres and ionospheres of the Earth and planets. The principle states that significant contributions to variations of the amplitude and phase of the radio waves passing through a layered medium are connected with influence of the vicinities of tangential points where the refractivity gradient is perpendicular to the radio ray trajectory. The RO method assumes spherical symmetry of the investigated medium. In this case if location of a tangent point relative to the spherical symmetry center is known,

- the derivatives on time of the RO signal phase and Doppler frequency variations can be recalculated into the refractive attenuation. Several important findings are consequences of the locality principle: (i) if position of the center of symmetry is known, the total absorption along the ray path can be determined at a single frequency, (ii) in the case of low absorption the height, displacement from the radio ray perigee, and tilt of
- the inclined ionospheric (atmospheric) layers can be evaluated, (iii) the contributions of the layered and irregular structures in the RO signal can be separated and parameters of layers and turbulence can be measured at a single frequency using joint analysis of the amplitude and phase variations. Specially for the Earth's troposphere, the altitude distributions of the weak total absorption (about of 1–4 db) of the radio waves at
- GPS frequencies corresponding to possible influence of the oxygen and water vapor can be measured with accuracy of about 0.1 db at a single frequency. According with the locality principle, a new index of ionospheric activity is introduced. This index is measured from the phase variations of radio waves passing through the ionosphere. Its high correlation with S4 scintillation index is established. This correlation indicates
- ²⁵ the significant influence of locally spherical symmetric ionospheric layers on variations of the phase and amplitude of the RO signal passing through transionospheric communication links. Obtained results expand the applicable domain of the RO method as a powerful remote sensing technique for geophysical and meteorological research.



1 Introduction

The radio occultation (RO) remote sensing has been known during the last 50 years as a powerful tool for investigation of the atmospheres, ionospheres and planetary surfaces (Fjeldbo, 1964; Marouf and Tyler, 1986; Lindal et al., 1983, 1987; Hinson et al., 1997, 1999; Yunck et al., 2000; Yakovlev, 2002, and references therein). With regard to the study of near-Earth space the RO method should be competitive with other means of remote sensing (Gurvich and Krasilnikova, 1987; Yunck et al., 1988; Melbourne et al., 1994; Yakovlev, 2002; Liou et al., 2010). Assumption of spherical symmetry – cornerstone of RO method – should be carefully analyzed when the RO technology is applied to global monitoring of the Earth' ionosphere and atmosphere at different altitudes (Vorob'ev and Krasilnikova, 1994; Melbourne et al., 1994; Syndergaard, 1998, 1999; Yunck et al., 2000). In particular, effectiveness of the RO method applied for investigation of the Earth's ionosphere can be compared with radio tomographic approach (Kunitsyn and Tereshchenko, 2003). The tomographic method allows obtaining

- ¹⁵ 2-D distributions of electron density in the ionosphere using chain of ground-based receivers, which capture signals of Low Earth Orbital (LEO) or navigational satellites along a set of intersecting radio rays (Kunitsyn et al., 2011, 2013). Unlike the radio tomographic approach, the RO method used a set of nearly parallel radio ray's trajectories. This enforces to use for processing the assumption of spherical symmetry
- ²⁰ of the Earth's ionosphere and atmosphere with known location of the center of symmetry (Melbourne et al., 1994; Yakovlev, 2002; Melbourne, 2004). According with this assumption all resulting altitude profiles of atmospheric and ionospheric parameters are attached to vertical and horizontal coordinates of the radio ray perigee relative to the spherical symmetry center, which is close to or coincident with the center of the Earth or planet
- ²⁵ Earth or planet.

Highly stable signals synchronized by atomic frequency standards and radiated by GPS satellites at frequencies F1 = 1575.42 MHz and F2 = 1227.60 MHz, create at the altitudes from 0 to 20000 km radio fields that can be used for the development of the



radio occultation (RO) method as a new tool for global monitoring of the ionosphere and neutral atmosphere (Gurvich and Krasilnikova, 1987; Yunck, 1988). During 1995–2014 the LEO missions: GPS/MET (Melbourne et al., 1994; Ware et al., 1996; Gorbunov et al., 1996; Kursinski et al., 1997; Vorob'ev et al., 1997), SAC-C (Schmidt et al., 2005),
⁵ CHAMP (Wickert et al., 2001), FORMOSAT-3 (Liou et al., 2007; Fong et al., 2008), GRACE (Hajj et al., 2004; Wickert et al., 2005), METOP (Engeln et al., 2011; Joo et al., 2005), METOP (Engeln et al., 2011; Joo et al., 2005).

- demonstrated that the RO technique is a powerful remote sensing tool for obtaining key vertical profiles of bending angle, refractivity, temperature, pressure and water vapour
- ¹⁰ in the atmosphere and electron density in ionosphere with global coverage, high spatial and temporal resolution (Zhang et al., 2013). Important contributions have been introduced also in (i) the theory of radio wave propagation (Gorbunov and Gurvich, 1998a; Gorbunov et al., 2002; Benzon et al., 2003; Gorbunov and Lauritsen, 2004; Gorbunov and Kirchengast, 2005; Pavelyev et al., 2004, 2010), (ii) climate changes detection
- ¹⁵ (Kirchengast et al., 2000; Steiner et al., 2001; Foelsche et al., 2008), (iii) space weather effects and ionosphere monitoring (Rius et al., 1998; Jakowski et al., 2004; Wickert et al., 2004; Arras et al., 2008, 2010), (iv) deriving new radio-holographic methods of the RO remote sensing (Karayel and Hinson, 1997; Mortensen and Hoeg, 1998; Pavelyev, 1998; Gorbunov and Gurvich, 1998b; Mortensen et al., 1999; Hocke et al., 1999; Carburate 2000a, b. Carburate et al., 2002, 2010; Japager et al., 2002, 2004;
- Gorbunov, 2002a, b; Gorbunov et al., 1996, 2002, 2010; Jensen et al., 2003, 2004;
 Pavelyev et al., 2000, 2002, 2004, 2010a, b, 2012; Liou et al., 2010).

Recently, an important connection between the intensity and derivatives on time of the phase, eikonal, Doppler frequency of radio waves propagating through the ionosphere and atmosphere has been discovered by theoretical analysis and confirmed

²⁵ by processing of the RO radio-holograms (Liou and Pavelyev, 2006; Liou et al., 2007, 2010; Pavelyev et al., 2008a, 2012b). This connection escaped during 40 years of RO practice from attention of the RO community. Now this relationship gets a possibility to recognize that the phase (eikonal) acceleration (proportional to the time derivative of the Doppler shift) has the same importance for the theory of radio waves propagation



in a layered medium and solution of the RO inverse problem as the Doppler frequency, phase path excess, and refractive attenuation of the RO signal (Liou and Pavelyev, 2006; Liou et al., 2007; Pavelyev, 2008, 2013; Pavelyev et al., 2009, 2010, 2012, 2013). It follows from this connection that the phase acceleration technique allows one to con-

- vert the phase and Doppler frequency changes into refractive attenuation variations at a single frequency. Note that this is similar to classical dynamic when the derivations of the path and velocity on time and acceleration are connected by the second Newton's law. From such derived refractive attenuation and amplitude data, one can estimate the integral absorption of radio waves. This is important for future RO missions when
- ¹⁰ measuring water vapor and minor atmospheric gas constituents, because the difficulty of removing the refractive attenuation effect from the amplitude data can be avoided. The phase acceleration technique can be applied also for determining the location and inclination of sharp layered plasma structures (including sporadic Es layers) in the ionosphere. The advantages of the phase acceleration technique are validated by analyz-
- ¹⁵ ing RO data from the Challenging Minisatellite Payload (CHAMP) and the FORMOSA Satellite Constellation Observing Systems for Meteorology, Ionosphere, and Climate missions (FORMOSAT-3/COSMIC).

The locality principle generalizes the phase path excess acceleration/intensity technique to the practically important case in which the position of the center of symmetry

- of layered medium is unknown (Pavelyev, 2013; Pavelyev et al., 2012a). New relationships have been revealed that expanding the scope and applicable domain of the RO method. These relationships allow, in particular, measuring the real height, inclination, and displacement of atmospheric and ionospheric layers from the RO ray perigee relative to the Earth's (or planetary) surface. This implies the possibility of determining the
- position and orientation of the fronts of internal waves, which opens a new RO area in geophysical applications for remote sensing of the internal waves in the atmospheres and ionospheres of Earth and other planets (Gubenko et al., 2008a, b, 2011).

The goal of this paper is (i) to formulate a principle of locality, (ii) to present several important findings arising from the locality principle; and (iii) to introduce new index of



ionospheric activity. The paper is structured as follows. In Sect. 2 the formulation of locality principle is presented. Section 3 describes three important findings following from the locality principle: (i) a possibility to determine the total absorption at a single frequency, (ii) a possibility to evaluate the height, displacement from the radio ray perigee,

- and tilt of the inclined ionospheric (atmospheric) layers, (iii) method for separation of the contributions of the layered and irregular structures in the RO signal and technique for measurement of parameters of layers and turbulence at a single frequency using joint analysis of the amplitude and phase variations. In Sect. 4 a new scintillation index based on the refractive attenuation found from the phase variations of the RO signal is
 introduced and its correlation with the S4 index is established. Conclusions are given
- in the S4 index is established. Conclusions are given in Sect. 5.

2 Principle of locality

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The principle of locality is based on a previously established connection (Liou and Pavelyev, 2006; Liou et al., 2007; Pavelyev et al., 2008a, b, 2009, 2010), which relates the eikonal acceleration *a* and refractive attenuation $X'_{\rho}(t)$ of the RO signal emitted by a transmitter G and received by satellite L after passing through a spherically symmetric medium with a center of symmetry at point O' (Fig. 1):

$$1 - X'_{p}(t) = m'a, a = \frac{d^{2}\Phi(t)}{dt^{2}} = \lambda \frac{dF_{d}(t)}{dt}, m' = \frac{d'_{2}d'_{1}}{(d'_{1} + d'_{2})} (dp'_{s}/dt)^{-2};$$

$$p'_{s} = |O'D'|; \Phi(t) = \int_{G}^{L} n(I)dI - R_{0}$$
(1)

²⁰ where λ is the length of radio waves; d'_1, d'_2 , and R_0 are the distances along the straight lines GD', D'L and GL, respectively; D' is the projection of the center of symmetry O' onto the line GL; p'_s is the impact parameter of the straight line GL relative to the center



O'; $\Phi(t)$ is the difference between the eikonal of radio waves propagating along the trajectory GTL and the length GL as a function of time *t*; *n*(*I*) is the refractive index; *d*/ is the differential length of the radio ray GTL; and the point T is the radio ray perigee relative to the Earth's surface having the altitude *h* (Fig. 1). Another important geomet-⁵ ric parameter is the height *H* of the line of sight GDL above the surface. Point D is the projection of the center O on the straight line GL (Fig. 1). During a RO event the magnitude *H* changes from positive to negative values. The eikonal acceleration *a* (Eq. 1) is proportional to the time derivative of the Doppler frequency of radio waves $F_d(t)$. Equality (Eq. 1) is fulfilled under the following conditions (Liou et al., 2007; Pavelyev et al., 2008a, b):

 $\left| (p' - p'_{c}) \frac{\mathrm{d}R'_{1,2}}{\mathrm{d}t} \right| \ll \left| p'_{c} \frac{\mathrm{d}p'_{s}}{\mathrm{d}t} \right| : d'_{1} \gg d'_{2}:$

$$\left(p'-p'_{s}\right)\frac{\mathrm{d}}{\mathrm{d}t}\left(\frac{\partial\theta'}{\partial p'_{s}}\frac{\mathrm{d}p'_{s}}{\mathrm{d}t}\right)\right|\ll\left|\left(\frac{\mathrm{d}p'}{\mathrm{d}t}-\frac{\mathrm{d}p'_{s}}{\mathrm{d}t}\right)\frac{\partial\theta'}{\partial p'_{s}}\frac{\mathrm{d}p'_{s}}{\mathrm{d}t}\right|$$

where p' is the impact parameter of the ray GTL relative to the center O'; d'_1 , and d'_2 are the distances GD', D'L, respectively; point D' is projection of the center of spherical symmetry O' on the line of sight GL. In the case of the RO ionospheric research the center of spherical symmetry can be shifted relative to the center O, and the first and third conditions (Eq. 1) are satisfied only if the distance OO' is significantly less than the Earth's radius ρ_e (Fig. 1). The second inequality (Eq. 2) is necessary for excluding the uncertainty because of symmetry of the coefficient m' with respect to variables d'_2 , d'_1 . Inequalities (Eq. 2) are satisfied in the case of circular orbits of the satellites G and

L, when the center of spherical symmetry O' is almost identical to the center of Earth (or planet) O, and the point T' coincides with the perigee T of the ray GTL (Fig. 1). Location of the radio ray perigee T in accordance with solution of the RO inverse problem determines the temporal dependencies of the height *h* above the Earth's surface and horizontal coordinates of the atmospheric layers (Melbourne et al., 1994; Melbourne, 25 2004; Yakovlev, 2002).



(2)

When absorption is absent, the refractive attenuation $X'_{p}(t)$ found from Eq. (1) should be equal to the refractive attenuation $X_{a}(t)$ determined using the RO amplitude data (Liou and Pavelyev, 2006):

 $X_{\rho}'(t)\equiv X_{a}(t); X_{a}(t)=I/I_{0}$

- ⁵ where I_0 and I are the intensities of the RO signal before and after the moment when the radio ray enters the medium, respectively. Identity (Eq. 3) is fulfilled if the coefficient m' in Eq. (1) is evaluated in accordance with location of the tangential point T', which is the perigee of radio ray GTL relative to the center of symmetry O' (Pavelyev et al., 2013). The refractive attenuation $X_a(t)$ measured from the RO intensity data does not depend on position of the point T' on the ray GTL and, naturally, on coefficient m'. The calculated value of the refractive attenuation $X'_p(t)$ does depend on the coefficient m'(Eq. 1) and location of the tangent point T' on the ray GTL. This permits to formulate the principle of locality under the conditions of single ray radio wave propagation and absence of absorption (Pavelyev et al., 2012, 2013; Pavelyev, 2013): the refractive at-
- tenuations $X'_{p}(t)$ and $X_{a}(t)$ are equal if evaluation of $X'_{p}(t)$ is provided with the coefficient m' corresponding to the locations of the spherical symmetry centre O' and ray perigee T'. In accordance with the locality principle, the amplitude and phase variations of the radio waves registered at the point L may be considered as connected with influence of a small neighborhood of the ray perigee T' corresponding to the spherical symmetry 20 centre O'.
 - 3 Consequences of the locality principle

Next important findings follow from the locality principle.

3.1 Possibility of determination of the total absorption

If location of the symmetry center is known (for example, when the point O' coincides with the Earth's center O), the total absorption Γ in the atmosphere (ionosphere) can



(3)

be defined by eliminating from the value $X_a(t)$ the refractive attenuation $X_p(h)$ found from the eikonal variations.

$$\Gamma = 10 \lg \frac{X_a(t)}{X_p(t)}$$

Some results of determination of the refractive attenuations $X_a(h)$, $X_p(h)$, and total absorption Γ are considered below. Figure 2 (left and right plots) shows two vertical profiles of the refractive attenuations $X_a(h)$ and $X_{D}(h)$ highlighted by indices "a" and "p" (rough curves), respectively, and their polynomial approximation (smooth curves) measured at the first GPS frequency F1. The measurements were provided above two regions located in the Central Africa in 2008 (RO events 18 October 17:52 UT (left), and 11 April, 03:14 UT (right), with geographical coordinates 5.0° N 332.5° W, and 6.7° N 10 328.1° W, respectively) using the FORMOSAT-3 satellites. The altitude dependences of $X_a(h)$ and $X_p(h)$ and their polynomial approximations are described by corresponding pairs of rough and smooth curves indicated by indices "a" and "p", respectively. The values of the altitudes of the line of sight GDLH and the height of the ray perigee h are plotted on the horizontal axis. The $X_a(h)$ and $X_p(h)$ profiles and their polynomial ap-15 proximations are almost coincident at heights between 12 and 40 km, and significantly different below 8-9 km (Fig. 2, right and left plots). The correlation between variations of $X_a(h)$ and $X_p(h)$ gradually decreases with height H and magnitude of $X_a(h)$ is obviously well below the corresponding values of $X_p(h)$ in the 5–9 km altitude interval h.

²⁰ This indicates a possible influence of the total absorption of the radio waves in the atmosphere.

Other results obtained from the RO experiments carried out during four events on 5 June 2008, are shown in Fig. 3 (right part, groups of curves I–IV) and correspond to measurements of the refractive attenuations $X_p(h)$ and $X_a(h)$ at GPS frequency F1.

²⁵ These RO experiments were conducted in the following areas: Norwegian Sea (I), East Siberian Plateau (II), South (III), and Central (IY) Alaska. The time and geographical coordinates of these RO events are: 16:18 UT; 70.8° N 1.7° W (curves I); 13:28 UT;



(4)

60.6° N 252.5° W (curves II); 02:42 UT; 64.9° N 139.7° W (curves III); and 10:44 UT; 60.0° N 155.8° W (curves IV). A weak but perceptible absorption in 1–2 db interval at frequency F1 is observed below 8 km altitude. However, the altitude dependence of absorption Γ is very different in the considered regions. Two cases revealed significant decrease of absorption Γ in the 5–6 (IV) and 7–8 km (II) height interval. In the remaining

areas the total absorption changes from 1.5 (I) up to 3.5 db (III) below 7 km altitude *h*. Relevant to four RO events polynomial approximations of the measured at frequency F1 refractive attentuation $X_a(h)$, evaluated from the eikonal data at frequencies F1, F2 refractive attentuations $X_{p1}(h)$, X_{p1} , and estimated from the combined eikonal

- ¹⁰ $\Phi_0 = (F_1^2 \Phi_1 F_2^2 \Phi_2)/(F_1^2 F_2^2)$ refractive attentuation $X_{\rho 0}(h)$ are shown in Fig. 4. The measurement sessions correspond to four equatorial regions located in the Central Africa. Figure 4 (left plot) shows vertical profiles of the FORMOSAT-3 satellites found from data of four RO events carried out on 11 April 2008, 03:14 UT, 6.7° N, 328.1° W; 29 May, 21:41 UT 3.1° N, 329.5° W; 11 October, 00:56 UT, 5.7° N, 333.4° W; and 18 Octo-
- ¹⁵ ber, 17:52 UT, 5.0° N, 332.5° W; (curves 1–4, respectively). The values of the altitudes *h* of the ray perigee T and the height *H* of the straight line GL relative to the Earth' surface are marked on the horizontal axis. The $X_a(h)$ and $X_p(h)$ profiles are marked by indices "*a*" and "*p*", respectively. All three curves $X_p(h) = X_{p1}(h), X_{p2}(h); X_{p0}(h)$ are coincident in Fig. 4 (left plot). However, some distinction is seen in the right part of
- ²⁰ Fig. 4, where the altitude dependence of the total absorption is shown. This may be connected with influence of the ionosphere. The measured values of the total absorption coincide with a mean value of Γ equal to 0.0096 ± 0.0024 db km⁻¹ and correspond to the RO MIR-geostationary satellites data at the 32 cm wavelength (Pavelyev et al., 1996).



3.2 Determination of the tilt, height, and displacement of the inclined layers

If center of symmetry does not coincide with the expected location – point O, the principle of locality states:

$$X_{a}(t) \equiv X_{\rho}'(t); 1 - X_{a}(t) = m'a = \frac{m'}{m} [1 - X_{\rho}(t)]$$
(5)

⁵ where magnitudes of the refractive attenuation $X_p(t)$ and coefficient *m* correspond to position of the point O. Using relationship (Eq. 1) connecting coefficient *m'* with the distances d'_1, d'_2 and impact parameter p'_s , one can obtain

$$\frac{m'}{m} - 1 = \frac{d'_2 d'_1 (dp_s/dt)^2}{d_2 d_1 (dp'_s/dt)^2} - 1; d_1 + d_2 = d'_1 + d'_2 = R_0$$
(6)

If the displacement of spherical symmetry center satisfies the following conditions:

$$\int_{0} \frac{\mathrm{d}\rho_{s}}{\mathrm{d}t} \approx \frac{\mathrm{d}\rho_{s}'}{\mathrm{d}t}; \frac{d_{2}}{R_{0}} \ll 1; \frac{d_{2}'}{R_{0}} \ll 1$$
(7)

one can find from Eqs. (6) and (7):

$$X_{\rho}(t) - X_{a}(t) = \frac{d_{2}' - d_{2}}{d_{2}} \left[1 - X_{\rho}(t) \right] = \frac{d}{d_{2}} \left[1 - X_{\rho}(t) \right]$$
(8)

where *d* is the distance DD' (see Fig. 1). It follows from Eqs. (5) and (8) that amplitudes A_a, A_p of variations of the refractive attenuations $1 - X_a(h)$, $1 - X_a(h)$ and distance *d* are connected by equations:

$$m' = \frac{A_a(t)}{A_p(t)}m; d = \left[\frac{A_a(t)}{A_p(t)} - 1\right]d_2$$
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(9)

The coefficients m, m' are slowly changing as functions of time. Therefore the coefficient m' and layer's displacement d can be estimated in the time instant when the amplitude $A_p(t)$ achieves maximal magnitude. This allows finding, if absorption is absent, the displacement d of the tangential point T' with respect to the ray perigee T (Fig. 1) as well as the layer's height h' and inclination δ from following equations:

$$d = d'_{2} - d_{2} = d_{2}(\alpha - 1); \alpha = \frac{A_{a}}{A_{p}}; d_{2} = \sqrt{R_{L}^{2} - p_{s}^{2}}, h' = h + \Delta h, \Delta h = \frac{d\delta}{2}, \delta$$
$$= \frac{d}{r_{e}}, r_{e} = |\text{TO}|.$$
(10)

The amplitudes A_a , A_p of variations of the refractive attenuations $1 - X_a(h)$ and $1 - X_p(h)$, can be evaluated, for example, using the Hilbert numerical transform. The amplitude $A_p(t)$ of refractive attenuation $X_p(t)$ is evaluated using the coefficient *m* corresponding to the centre of Earth (or planet) O. Depending on the sign of the difference $A_a - A_p$, the value of *d* is positive (or negative), and the point T' is located on the *GT* or TL lines, respectively. Note that relationship (Eq. 9) is fulfilled if one of the satellites is much farther away from the center of symmetry than the other. This condition is usually satisfied during the Earth or planetary RO missions (Fjeldbo, 1964; Yakovlev, 2002).

The spherical symmetry of a medium with new center O' justifies application of the Abel transformation for solution of the inverse problem (Pavelyev et al., 2008a, b). The time derivative of the phase path excess $\Phi(t)$ is used to obtain the temporal dependence of the impact parameter p':

$${}_{20} \quad p' - p'_{s} = -m' \frac{\mathrm{d}\Phi}{\mathrm{d}t} \frac{\mathrm{d}p_{s}}{\mathrm{d}t} = -m\alpha \frac{\mathrm{d}\Phi}{\mathrm{d}t} \frac{\mathrm{d}p_{s}}{\mathrm{d}t} = \alpha \left(p - p_{s}\right). \tag{11}$$

To solve the inverse problem, the following formulas are used for the Abel transform (Hocke, 1997; Pavelyev et al., 2012a, b) (for simplicity, the bar in the designation of the



impact parameters p', p'_s is deleted):

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$$N(p) = -\frac{1}{\pi} \int_{p}^{\infty} \ln\left(\frac{x}{p} + \sqrt{\frac{x^2}{p^2} - 1}\right) \frac{d\xi(x)}{dx} dx$$

where p is the impact parameter corresponding to ray GTL in the instant of time t and N(p) is the refractivity. The vertical gradient of the refractivity dN(p)/dh can be found from Eq. (12) using a relationship:

$$\frac{\mathrm{d}N(p)}{\mathrm{d}h} = \frac{1+N(p)}{1-\frac{\mathrm{d}N(p)}{\mathrm{d}p}r_{\mathrm{T}}}\frac{\mathrm{d}N(p)}{\mathrm{d}p} \tag{13}$$

where r_T is the distance T'O' (Fig. 1). The derivative of the bending angle $\xi(p)$ on the impact parameter p can be found from the RO signal amplitude or the RO phase path excess data (Pavelyev et al., 2012, 2013), i.e.:

$$X(p) = \frac{p}{p_{s} \left| 1 - \sqrt{R_{2}^{2} - p^{2}} \sqrt{R_{1}^{2} - p^{2}} \frac{d\xi(p)}{dp} R_{0}^{-1} \right|};$$

$$\frac{d\xi(p)}{dp} = \left(1 - p_{s} p^{-1} X^{-1} \right) \frac{R_{0}}{\sqrt{R_{2}^{2} - p^{2}} \sqrt{R_{1}^{2} - p^{2}}} \approx \frac{\left(1 - X^{-1} \right) R_{0}}{\sqrt{R_{1}^{2} - p^{2}} \sqrt{R_{2}^{2} - p^{2}}}$$
(14)

The last Eq. (14) for $d\xi(\rho)/d\rho$ is valid under condition: $\rho \approx \rho_s$. Substitution Eq. (14) in Eq. (12) gives with accounting for relation $\frac{d\rho}{dt} = X(\rho)\frac{d\rho_s}{dt}$ (Kalashnikov et al., 1986):

$$N(p) = \frac{1}{\pi} \int_{-\infty}^{t(p)} \ln\left(\frac{x}{p} + \sqrt{\frac{x^2}{p^2} - 1}\right) \frac{[X(t) - 1]R_0}{\sqrt{R_1^2 - x(t)^2} \sqrt{R_2^2 - x(t)^2}} \frac{d\rho_s(t)}{dt} dt;$$

$$x(t) = p(t); -\infty < t \le t(p)$$
(15)

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(12)

From Eqs. (5), (14), and (15), one can obtain a modernized formula for the Abel inversion, i.e.,

$$N(p) = -\frac{1}{\pi} \int_{-\infty}^{t(p)} \ln\left(\frac{x}{p} + \sqrt{\frac{x^2}{p^2} - 1}\right) \frac{m' a R_0}{\sqrt{R_1^2 - x(t)^2} \sqrt{R_2^2 - x(t)^2}} \frac{d \rho_s(t)}{dt} dt;$$

$$x(t) = p(t); -\infty < t \le t(p)$$

where m' can be determined from the first Eq. (9).

- ⁵ When position of the spherical symmetry center is known (for example, a center of symmetry coincides with the center of the Earth), Eqs. (15) and (16) are new relationships for solution of the RO inverse problem. Unlike previous solution (Eq. 12), the relationships (Eqs. 15 and 16) do not contain the angle of refraction, and include only temporal dependences of the refractive attenuation *X*(*t*), eikonal acceleration, and impact parameter. Note that Eqs. (15) and (16) provide the Abel transform in the time domain where a layer contribution does exist. The linear part of the regular trend due to the influence of the upper ionosphere is removed because the eikonal acceleration *a*
- in Eq. (16) contains the second derivative on time. However, the influence of the upper ionosphere is existing because it may contribute in the impact parameter p(t). Also, the nonlinear contribution of the upper ionosphere remains in the eikonal acceleration *a*.
- Therefore, Eq. (16) approximately gives that part of the refractivity altitude distribution, which is connected with the influence of a sharp plasma layer. The electron density vertical distribution in the Earth's ionosphere $N_e(h)$ is connected at GPS frequencies with the refractivity N(h) via the following relationship:

$$_{20} N_{\rm e}(h) = -\frac{N(h)}{40.3} f^2 \tag{17}$$

where *f* is the carrier frequency [Hz], and $N_{\rm e}(h)$ is the electron content [elm⁻³].

Examples of application of Eqs. (12)-(16) for estimation of the location, inclination, and real height of ionospheric layers are given in Fig. 5. To consider a possibility to



(16)

locate the plasma layers, a CHAMP RO event 026 (4 July 2003, 02:27 UT; geographic coordinates 68.5° N 82.8° W) with strong quasi-regular amplitude and phase variations is used. The refractive attenuations of the CHAMP RO signals $X_a(h)$, $X_p(h)$ found from the RO signal intensity and eikonal data at frequency F1 are shown in Fig. 5a as func-

- ⁵ tions of the RO ray perigee altitude *h*. The eikonal acceleration *a* has been estimated by the double differentiation of a second-power least square polynomial over a sliding time interval $\Delta t = 0.5$ s. This time interval approximately corresponds to the vertical size of the Fresnel zone of about 1 km since the vertical component of the radio ray velocity was about 2.1 km s⁻¹. The refractive attenuation $X_p(h)$ is derived from the eval-
- ¹⁰ uated magnitude *a* using Eq. (1), and *m* value is obtained from the orbital data. The refractive attenuation $X_a(h)$ is derived from the RO amplitude data by a sliding least-square polynomial having the second power with averaging in the time interval of 0.5 s. In the altitude ranges of 50–60 and 75–85 km, the refractive attenuations variations $X_a(h)$ and $X_p(h)$ are strongly connected and may be considered as coherent oscilla-
- ¹⁵ tions caused by sporadic layers (Fig. 5a, curves 1 and 2). Using a Hilbert numerical transform, the amplitudes A_a , A_p of analytical signals related to $1 X_a(h)$ and $1 X_p(h)$ have been computed and are shown in Fig. 5b, curves 1 and 2, respectively. In the altitude range of 50–60 km, amplitudes A_a , A_p are nearly identical, but the magnitude of A_a is about 1.7 times below than that of A_p . Accordingly, the displacement *d* found
- ²⁰ from Eq. (9) is negative, and a plasma layer is displaced from the RO ray perigee T in the direction to satellite L (see Fig. 1). A similar form of variations of the refractive attenuations $1 - X_a(h)$ and $1 - X_p(h)$ allows locating the detected ionospheric layer. Displacement *d* corresponding to a plasma layer recorded at the 51 km altitude of the RO ray perigee is shown in Fig. 5c. Curves 1 and 2 in Fig. 5c correspond to amplitudes A_a, A_p . Curve 3 describes the displacement *d* found using Eq. (9) from amplitudes A_a, A_p in the 50.7–51.4 km altitude interval. The changes in *d* are concentrated in the altitude range of –900 to –950 km when the functions A_a, A_p vary near their maximal values of 0.75 and 1.36 in the ranges of $0.7 \le A_a \le 0.75$; $1.29 \le A_p \le 1.36$, respectively. The statistical error in the determination of ratio $\frac{A_a(t)}{A_p(t)}$ in Eq. (9) is minimal when $A_p(t)$



is maximal. If the relative error in the measurements of A_{ρ} is 5%, according to Fig. 5c, the accuracy in the estimation of d is about ± 120 km. The inclination of a plasma layer to a local horizontal direction δ calculated using Eq. (10) is approximately equal to $\delta = 8.2 \pm 0.2^{\circ}$. The vertical gradient $\frac{dN_{e}(h)}{dh}$ of the electron density distribution $N_{e}(h)$ for the given RO event is shown in Fig. 5d. Curves 1 and 2 correspond to the vertical gradient $\frac{dN_e(h)}{dh}$ retrieved using Eqs. (12) and (16), respectively. Curve 3 is related to the vertical gradient $\frac{dN_e(h)}{dh}$ retrieved using the refractive attenuation $X_a(h)$ and formula (Eq. 15). The real altitude of the ionospheric layers is indicated on the horizontal axis in Fig. 5d. Two ionospheric layers are seen (curves 1, 2, and 3 in Fig. 5d). The first layer is located on line TL at the 110 to 120 km altitudes at a distance of 10 900 km from point T (Fig. 5d, left). The second layer is located at a distance of 550 km from point T at the 95 to 105 km altitudes (Fig. 5d, right). From the comparison of the refractive variations $X_a(h)$ and $X_n(h)$ (Fig. 5a, curves 1 and 2) and the vertical gradients of the electron content (Fig. 5d), the width of the sporadic *E*-layers is nearly equal to the altitude interval of the intensity variations of RO signals. From Fig. 5d, 15 the variations of the vertical gradient of the electron density are concentrated in interval -0.4×10^{6} [el cm⁻³ km⁻¹] < $\frac{dN_{e}(h)}{dh}$ < 0.5 × 10⁶ [el cm⁻³ km⁻¹]. These magnitudes of $N_{\rm e}(h)$ are typical for sporadic E layers (Kelley and Heelis, 2009). The height interval of the RO signal amplitude variations is nearly equal to the height interval of the variations in the electron density and its gradient. It follows that the standard definition of 20 the perigee of the radio ray in the RO method as the minimal value of the distance to the surface of the ray path leads to an underestimation (bias) of layers altitude in the atmosphere (ionosphere) of Earth and planets. This error is zero for horizontal layers and increases with their inclination.



3.3 Separation of the layers and small-scale irregularities contributions in the RO signal

The principle of locality allows one to separate the contributions of layers and irregular inhomogeneities in the RO signal. According to Eq. (5), the coherent and incoherent components of the RO atmospheric signal C(h), I(h) due to the layers and irregularities influence can be estimated as:

$$C(h) = \left[X_a(h) + X_p(h)\right]/2 - P(h); I(h) = \left[X_a(h) - X_p(h)\right]/2$$
(18)

where P(h) is the polynomial approximation describing the main atmospheric contribution in the RO signal. If location of the spherical symmetry center is known, P(h)should be the same for the refractive attenuations $X_a(h)$, $X_p(h)$. Example of separation of the layers and inhomogeneities contributions in the RO signal is presented below. Figure 6 shows altitude dependences of the refractive attenuations $X_a(h)$, $X_p(h)$ for the CHAMP RO event 7 April 2003 carried out at 02:34 UT in the area with geographical coordinates 2.5° S 291.7° W. The vertical profiles of the refractive attenuations $X_a(h)$, $X_p(h)$ reveal the coherent variations of $X_a(h)$, $X_p(h)$ indicating contribution of the atmospheric layers (Fig. 6, left, top curves X_A , X_P displaced for comparison). Dotted curves in Fig. 6, left (displaced for comparison), describe the polynomial approximations P(h)

- of the slow changing altitude dependences of $X_a(h)$, $X_p(h)$. The coherent and incoherent parts of the RO signal C(h), I(h) are obtained using formulas (Eq. 18) as shown in the Fig. 6, left, bottom plot (curves 1 and 2, respectively). The intensity of the coherent component C(h) by an order of magnitude prevails the corresponding value of I(h), thus, indicating importance of the layers contribution in the RO signal. Usually this contribution is assigned to effects of the small-scale irregularities (Cornman et al., 2012). Analysis of spatial spectra of coherent and incoherent components is presented in the
- Fig. 6, right, top and bottom plots, respectively. The forms of spectra C(h), I(h) are similar in the interval of the vertical periods greater than 1 km. In the interval below 1 km, the power degrees of the spectra inclination are different and equal to 3.7 ± 0.2 and



2.1 ± 0.2 for components C(h) and I(h), respectively. This indicates a different origin of the components C(h) and I(h). The inclination of the I(h) spectrum is nearly 8/3 which corresponds to contribution of the turbulent irregularities in variations of the RO signal intensity (Gurvich and Yakushkin, 2004). The value 3.7 corresponding to the coherent component C(h) is near the inclination of spatial spectrum of anisotropic internal gravity waves according with theory developed by Gurvich and Chunchuzov (2008).

Parameters of coherent and incoherent components introduced in the Table 1 illustrate a possibility to separate the contributions of atmospheric layers and turbulent structures in the RO signal. The time and geographic coordinates are shown in the first

- ¹⁰ two columns of Table 1. The rms deviations σ_A , σ_P of the refractive attenuations $X_a(h)$, $X_p(h)$ and dispersion of the components C(h) and $I(h)\sigma_c$, σ_{in} are presented in the next four columns. The altitude interval $h_b - h_u$ of measurements of σ_A , σ_P ; σ_c , σ_{in} ; and correlation coefficient r_c between the refractive attenuations variations $X_A(h)$, $X_P(h)$ are indicated in the last two columns of Table 1. As a rule the rms deviation σ_c of the
- ¹⁵ coherent component *C*(*h*) is greater than that one of incoherent part *I*(*h*) σ_{in} by a factor of 4–5. This indicates on the prevailing contribution of the atmospheric layers as compared with influence of the irregularities in the RO signal. High level of correlation r_c (in the interval 0.84–0.96) between the variations of the refractive attenuations $X_a(h)$, $X_p(h)$ indicates the practical and theoretical importance of the locality principle for separation of the atmospheric layers and irregularities in the RO signal at a single
- frequency.

4 Relationships between the eikonal variations and intensity scintillations index S4

According to locality principle, there can exist a global correlation between the phase and amplitude variations of the RO signal. Index S4 (I), as measured from intensity variations, should be correlated with index S4 (F), defined by the second derivative on time of the eikonal of the RO signal at GPS frequencies F1 and F2. According to the



principle of locality in the case of spherical symmetric medium, there can exist the next connections:

$$S4(X_a) = \sqrt{\frac{\langle X_a^2 \rangle - \langle X_a \rangle^2}{\langle X_a \rangle^2}}; S4(X_p) = \sqrt{\frac{\langle X_p^2 \rangle - \langle X_p \rangle^2}{\langle X_p \rangle^2}}; S4(X_a) \equiv S4(X_p)$$
(19)

Figures 7 and 8 show the results of correlation of index S4(/), defined by the variations of the intensity / at the frequency F1 with indices S4(F1), S4(F2) measured from the 5 second derivative of the phase paths excess at frequencies F1, F2 during FORMOSAT-3 RO events held in January and February 2012. Circles in Figs. 7 and 8 correspond to the experimental values of index S4(1) (vertical axis) and S4 (F1), S4(F2) (horizontal axis). The solid curves in Figs. 7 and 8 are regression lines and have been found by least squares method. The correlation coefficient of index S4(/) to S4(F1) and S4(F2) 10 varies in the intervals 0.69 to 0.78 and 0.70-0.75, respectively. The correlation coefficient of index S4(I) with combined index [S4(F1) + S4(I)]/2 is very high and changes in the interval 0.91–0.97. Measured correlation values indicate a significant contribution of regular layered irregularities in the ionospheric variations of the amplitude and phase of the RO signals at frequencies F1, F2. High correlation between variations 15 of the indices S4(/) and S4 (F1), S4(F2) indicates substantially lower influence of the small-scale irregularities on the RO signal as compared with the contribution of the layered structures in the ionosphere.

5 Conclusions

Principle of locality remained unknown for 45 years radio occultation studies of the atmosphere and ionosphere of the Earth and planets. In implicit form, this principle was replaced by the assumption of spherical symmetry with known location of the symmetry center. This assumption allows one to determine location of the altitude profiles of



refractivity, air, and electron density, and other physical parameters using the vertical and horizontal coordinates of the RO radio ray perigee. Important relation connecting the refractive attenuation and eikonal acceleration found in explicit form by Liou and Pavelyev, 2006, was the basis for the formulation of the principle of locality in a general

- ⁵ case when the positions of the ray perigee and the center of spherical symmetry were unknown. The principle of locality revealed new laws that extended possibilities of the RO method as a powerful tool for bistatic remote sensing of the Earth and planets: (i) evaluation of the refractivity attenuation from the RO phase data allows one to estimate the total absorption using the RO amplitude variations at one frequency, (ii) evaluation
- ¹⁰ of the slope, altitude, and horizontal displacement of the atmospheric and ionospheric layers, (iii) separation of layers and irregularities contributions in the RO signal; and (iv) introduction of the new phase index of the ionospheric activity allows detecting predominant influence of layers to scintillations of the phase and amplitude in GPS signals observed in the transionospheric communications satellite-to-satellite links.
- ¹⁵ Therefore, the principle of locality extends the applicable domain of the RO method, widens possibilities and opens new directions of the RO geophysical applications to remote radio sensing, including the study of multilayered structures and wave processes in the atmospheres and ionospheres of the Earth and planets.

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AMTD 8, 721–758, 2015 **Application of** locality principle A. G. Pavelyev et al. **Title Page** Introduction Abstract Conclusions References Tables Figures **Discussion** Paper Close Back Full Screen / Esc Printer-friendly Version Interactive Discussion Paper

Discussion

Paper

Discussion Paper

Discussion

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Time (UT)	Location	σ_{A}	σ_P	σ_c	$\sigma_{\sf in}$	h_b/h_u , km	r _c
17 Apr 2003, 21:38	58.9° N 117.5° E	0.084	0.062	0.071	0.018	12/30	0.88
17 Apr 2003, 22:05	45.8° S 146.9° E	0.07	0.058	0.062	0.015	14/25	0.88
17 Apr 2003, 23:13	48.7° N 124.4° E	0.11	0.097	0.104	0.022	12/27	0.91
26 Apr 2003, 00:06	55.8° N 74.2° E	0.065	0.052	0.056	0.016	11/26	0.85
26 Apr 2003, 00:13	31.1° N 74.6° E	0.051	0.036	0.042	0.011	18/32	0.86
26 Apr 2003, 01:21	51.8° N 125.2° W	0.096	0.076	0.085	0.015	12/26	0.94
26 Apr 2003, 01:23	58.1° N 92.8° W	0.055	0.039	0.046	0.011	13/25	0.88
26 Apr 2003, 04:42	65.3° N 35.3° E	0.056	0.043	0.048	0.014	10/22	0.85
03 May 2003, 00:34	0.4° S 63.0° E	0.11	0.086	0.096	0.027	17.5/26	0.86
03 May 2003, 01:27	22.2° N 121.6° W	0.14	0.11	0.123	0.023	12/27	0.94
03 May 2003, 03:35	12.6° N 38.6° E	0.079	0.065	0.071	0.012	20/30	0.95
03 May 2003, 04:56	59.4° N 17.0° E	0.05	0.039	0.043	0.011	12.5/26.5	0.87
12 Apr 2003, 07:48	45.6° S 7.6° E	0.066	0.047	0.056	0.012	14/25	0.915
12 Apr 2003, 08:25	7.4° N 153.9° E	0.103	0.076	0.088	0.013	18/30	0.96
12 Apr 2003, 08:53	57.5° N 42.2° W	0.06	0.052	0.055	0.011	12/24	0.918
12 Apr 2003, 09:37	70.8° S165.0° E	0.069	0.054	0.06	0.015	12/22	0.88
12 Apr 2003, 10:08	52.2° N 150.9° E	0.085	0.069	0.075	0.016	12.5/27	0.92

 Table 1. Parameters of coherent and incoherent components.





Figure 1. Scheme of radio occultation measurements.





Figure 2. Comparison of the refractive attenuations $X_a(h)$ and $X_p(h)$ and their polynomial approximations, corresponding to the FORMOSAT-3 RO measurements carried out on 18 October and 11 April 2008 (left and right plots, respectively). Thick and thin rough curves (marked by indices "p" and "a") describe the vertical profiles of $X_p(h)$ and $X_a(h)$, respectively. Smooth curves describing polynomial approximations of the altitudes dependences of $X_p(h)$ and $X_a(h)$ are also highlighted by indices "p" and "a".



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Figure 3. Left plot. Comparison of the refractive attenuations $X_a(h)$ and $X_p(h)$ (groups of curves I–IV). Each group consists of four curves. In each group thick and thin rough curves (marked by indices "*p*" and "*a*") describe the experimental vertical profiles of $X_p(h)$ and $X_a(h)$, respectively. Smooth curves in each group describe polynomial approximations of the altitudes dependences of $X_p(h)$ and $X_a(h)$ and are also highlighted by indices "*p*" and "*a*", respectively. For convenience groups of curves II–IV are displaced by 0.6; 1.2; 1.8 units. Right. The total absorption Γ corresponding to the refractive attenuations $X_a(h)$, $X_p(h)$ measured at frequency F1 has been calculated from the smooth curves I–IV (marked by indices *a*, *p* in left panel). Curves II–IV are shifted for comparison by 1, 2, and 3 db, respectively.





Figure 4. Left plot. Comparison of the polynomial approximations of refractive attenuations $X_a(h)$, $X_p(h)$ (curves 1–4, indeces "p" and "a", respectively). Curves 2–4 are displaced for convenience by 0.6; 0.4; 0.2, respectively. Right. The total absorption Γ corresponding to the refractive attenuations $X_a(h)$, $X_p(h)$ has been calculated from the curves 1–4 (right panel). Curves 2, 3, and 4 are shifted for convenience by 2, 4, and 6 db, respectively.



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Figure 5. (a) Comparison of the refractive attenuations $X_a(h)$, $X_p(h)$ found from the RO intensity and eikonal data at GPS frequency F1 (curves 1 and 2, respectively). (b) The amplitudes A_a, A_a of analytical signals corresponding to the variations of the refractive attenuations $1 - X_a(h)$ and $1 - X_{p}(h)$ (curves 1 and 2), respectively. (c). Location of the first layer using amplitudes A_{a}, A_{p} . (d). Vertical profiles of the gradients of electron density in the layers.



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Figure 6. Left top. Comparison of the refractive attenuations $X_a(h)$, $X_p(h)$ found from the RO intensity and eikonal data at GPS frequency F1 (curves X_A and X_P , respectively, displaced for comparison). Dotted curves show the polynomial approximations of the refractive attenuations $X_a(h)$, $X_p(h)$. Left, bottom. Contribution of the atmospheric layers (coherent component of the RO signal) and small scale irregularities (incoherent component) (curves 1 and 2, respectively). Right. Spatial spectra of the coherent and incoherent components of the RO signal (top and bottom panels, respectively).





Figure 7. Correlation of index S4(*I*) measured from the intensity variations of the GPS RO signal at frequency F1 and parameters S4(F1) and S4(F2) found from the eikonal variations at GPS frequencies F1 and F2.





Figure 8. Correlation of indices S4(I) and [S4(F1) + S4(I)]/2.

