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Retrieval of sodium number density profiles in the mesosphere and lower thermosphere from SCIAMACHY limb emission measurements

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Abstract

An algorithm has been developed for the retrieval of sodium atom (Na) number density on a latitude and altitude grid from SCIAMACHY limb measurements of the Na resonance fluorescence. The results are obtained between 50 and 150 km altitude and ⁵ the resulting global seasonal variations of Na are analysed. The retrieval approach is adapted from that used for the retrieval of magnesium atom (Mg) and magnesium ion (Mg⁺) number density profiles recently reported by Langowski et al. (2014). Monthly mean values of Na are presented as a function of altitude and latitude. This data set was retrieved from the 4 years of spectroscopic limb data of the SCIAMACHY meso-¹⁰ sphere and lower thermosphere (MLT) measurement mode.

The Na layer has a nearly constant altitude of 90–93 km for all latitudes and seasons, and has a full width at half maximum of 5–15 km. Small but substantial seasonal variations in Na are identified for latitudes less than 40°, where the maximum Na number densities are 3000-4000 atoms cm⁻³. At mid to high latitudes a clear seasonal varia-

- tion with a winter maximum of up to 6000 atoms cm⁻³ is observed. The high latitudes, which are only measured in the Summer Hemisphere, have lower number densities with peak densities being approximately 1000 Na atoms cm⁻³. The full width at half maximum of the peak varies strongly at high latitudes and is 5 km near the polar summer mesopause, while it exceeds 10 km at lower latitudes. In summer the Na atom concentration at high latitudes and at altitudes below 88 km is significantly smaller than
- that at mid latitudes. The results are compared with other observations and models and there is overall a good agreement with these.



1 Introduction

The metal sodium, Na, was first isolated in the laboratory by Sir Humphry Davy in 1807 (Davy, 1808). This was achieved by the electrolysis of very dry molten sodium hydroxide, NaOH, with Na being collected at the cathode. More than one hundred years later

the Earth's atmospheric Na layer was discovered in 1929 by American astronomer Vesto Slipher (Slipher, 1929). The large scattering cross section and atmospheric column of Na in the upper atmosphere results in a relatively strong emission in the visible spectral range. Sydney Chapman, who had previously worked on explaining upper atmospheric ozone, proposed a reaction-cycle theory to explain the night-glow phenomenon and the Na emissions (see, e.g., Chapman, 1938, 1939).

There are two possible groups of Na sources for the upper atmosphere: terrestrial sources, such as volcanic eruptions and salt particles from the oceans, and extraterrestrial sources such as meteoroids and comet dusts. In the upper atmosphere meteoroids are the most likely sources of Na.

¹⁵ Meteoroids enter the Earth's atmosphere at supersonic speed and are decelerated and frictionally heated by collisions with air molecules. These processes lead to the meteoric ablation of metals and non metals into the upper atmosphere. The ablated metals are transported and react with the ambient neutral atmosphere. As a result metal layers are formed that have peak densities at around 85–95 km altitude (see,

- e.g., Plane, 2003; Plane et al., 2015 for a review). Although the metal concentrations of several thousand atoms per cubic centimeter are low, these metals are strong emitters of radiation because they have large resonance fluorescence cross sections. Therefore, the metals are readily observed by remote sensing methods. Due to their strong radiation signal and their relatively long atmospheric lifetime, metal species are used
- as trace species to investigate wave propagation effects and winds in the mesosphere and lower thermosphere (MLT). Furthermore, the total amount of extraterrestrial material input can be estimated from measurements of these metal layers. Additionally, metals play an important role in upper atmospheric chemistry. Their chemical trans-



formation impacts on ozone formation and loss both in the gas phase and through metal compounds acting as nucleation nuclei for the formation of aerosols and clouds in the middle atmosphere (see, e.g., Rapp and Thomas, 2006; Voigt et al., 2005; Curtius et al., 2005). A detailed understanding of the origin and the reactions of metals

⁵ in the upper atmosphere is required to understand the formation and loss of ozone and particles in the upper atmosphere. Also, metal ions are the principal component of ionospheric sporadic E layers and metal ions are found throughout the ionosphere.

Na has a large number density compared to other metals in the MLT, and the lower atmosphere is nearly transparent at the wavelength of the strongest Na transitions at 589 nm. This simplifies the observation from ground. As a result, the mesospheric Na

layer is the best understood metal layer in the MLT.

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As the metal layers reside at an altitude where the atmosphere is too thin for aircraft to fly, but too dense for satellites to orbit for longer time periods, in-situ measurements are only possible with rockets, which can only be launched at a limited number of locations on Earth and are expensive. Remote sensing methods are used and ground

Iocations on Earth and are expensive. Remote sensing methods are used and ground observations, e.g. by lidar, yield good vertical and time-resolved results, however, only at selected locations.

In the last decade global satellite observations of Na with long time series have been available. The first global space-based observations were reported by Fussen et al.

- (2004), using the GOMOS instrument on the satellite Envisat. Envisat also carries the SCIAMACHY instrument, the measurements of which are used in this study. Other observations have been reported from OSIRIS on the Odin satellite (Gumbel et al., 2007; Fan et al., 2007; Hedin and Gumbel, 2011), SCIAMACHY (Casadio et al., 2007) and GOMOS (Fussen et al., 2010). Results of the Na number density retrieval from the SCIAMACHY limb MLT measurements between 2008 and 2012 are presented in this.
- SCIAMACHY limb MLT measurements between 2008 and 2012 are presented in this study. These results are compared to other measurements and models.

This manuscript is structured as follows: in Sect. 2 the SCIAMACHY measurements and the Na density retrieval algorithm are explained. The results for Na number densities will be presented in Sect. 3, retrieved from both Na D lines at 589 nm. In Sect. 4



differences between results from both D lines are discussed and the results are compared to other measurements and model results. The seasonal and annual changes are investigated. Finally, the findings of this study are summarized in Sect. 5.

2 Instrument, retrieval algorithm and algorithm extension

5 2.1 SCIAMACHY

The limb observations of scattered solar electromagnetic radiation, observed by the Scanning Imaging Absorption Spectrometer for Atmospheric CHartographY (SCIA-MACHY) on board the Environmental Satellite (Envisat) are used for this study (see Burrows et al., 1995; Bovensmann et al., 1999 for more details). Envisat was launched
¹⁰ by the European Space Agency ESA on an Ariane-5 rocket on 28 February 2002 into a sun-synchronous, low Earth orbit with a descending node (southbound local equator crossing time) at around 10 a.m. local time. It made measurements in limb, nadir and occultation geometry. ESA lost contact with Envisat on the 8 April 2012.

- In the occultation mode SCIAMACHY observes either the sun or the moon through the atmosphere at sunrise and moonrise, respectively. In nadir mode the instrument points downward towards the Earth's surface and scans the upwelling radiation at the top of the atmosphere. The nadir mode delivers a good latitudinal and longitudinal coverage. In limb mode the instrument points tangentially to the Earth's surface at different tangent altitudes, resulting in an adequate vertical resolution in the scanned range of altitudes, but with a poorer latitudinal and longitudinal resolution than the nadir
- range of altitudes, but with a poorer latitudinal and longitudinal resolution than the nadir mode.

The highest tangent altitude of the nominal limb mode, which was performed daily during the whole SCIAMACHY lifetime, is about 91 km, which is just the altitude of the Na layer peak. However, from the middle of 2008 the limb MLT mode, which scans the altitude range between 50 and 150 km in 30 steps of 3.3 km with a good vertical resolu-

²⁵ altitude range between 50 and 150 km in 30 steps of 3.3 km with a good vertical resolution (also around 3.3 km) at the altitude of the metal atom and ion layers, was performed



for one day of measurements every two weeks. As the ion layers (e.g., Mg⁺, see Langowski et al., 2015) are located at slightly higher altitudes than the neutral layers, it was decided to exploit the MLT mode of SCIAMACHY first, prior to later investigation of the standard profiling mode. However, the retrieval results from the nominal limb and limb MLT measurements should not be too different and the data set presented here will be extended later. For each MLT limb scan, there is an additional measurement of the dark signal at 350 km tangent altitude. For Na this dark signal, which is subtracted from the signal at the other tangent altitudes, is much weaker than the signal at MLT tangent altitudes. At 590 nm SCIAMACHY has a spectral resolution of 0.44 nm. This is

sufficient to resolve the two Na D lines, D_1 at 589.756 nm and D_2 at 589.158 nm, which have a spectral seperation of ≈ 0.6 nm.

The SCIAMACHY data set employed in this study is Level 1 data Version 7.03 and 7.04 and was calibrated with ESA's calibration tool sciallc with options 1, 2, 4, 5, 7 and M-factors, which include option 3 (see Sherbakov and Lichtenberg, 2008 for more

- details.). The Level 1 data have been averaged using the same approach as used by Langowski et al. (2015) for Mg and Mg⁺. An average for same latitude and local time of the up to 15 orbits of SCIAMACHY data is formed before the retrieval. The multiannual monthly means of the results for the 2008–2012 data set are formed after the retrieval. Note that there is a larger latitudinal coverage for the Southern Hemisphere than the
- Northern Hemisphere, because the northern dayside high latitude measurements suffer from solar straylight contaminations. This is because the sun is partly in the field of view of the instrument (see Langowski et al., 2015; Langowski, 2015 for more details). There is also a larger coverage of high latitudes compared to the Mg/Mg⁺ retrieval by Langowski et al. (2015), because the better signal to noise ratio of Na produced less
- ²⁵ edge effects in the retrieval for the outermost measurements on the altitude-latitude grid.



2.2 Retrieval algorithm and adaption to Na

The retrieval algorithm presented in Langowski et al. (2014), which was used for magnesium atom and ion retrievals from the SCIAMACHY limb MLT measurements (Langowski et al., 2015), is used and adjusted to the specific parameters of Na atoms.
 ⁵ A forward model for the emission signal and absorption path of each limb measure-

A forward model for the emission signal and absorption path of each limb measurement of an orbit is set up and inverted for the number densities of the emitting species on a 2-D latitude–altitude grid.

The mathematical representation of the forward model is:

$$4\pi I = \int_{\text{LOS}} \gamma n(s_{\text{e}}) f(\int n(s_{\text{a}}) ds_{\text{a}}) ds_{\text{e}}$$

¹⁰ with emissivity γ , density *n* and an absorption part – along the line of sight (LOS) and the line from sun to the point of scattering into the LOS (LFS) (s_a stands for both absorption paths) – *f*. The signal is the integrated product of the density *n* and the emissivity γ along the emission path s_e , which is furthermore attenuated by self-absorption *f* (see Eq. 6 for *f*). Equation (1) is discretized on the 2-D latitude–altitude grid and ¹⁵ inverted for the number density *n*. The changes with respect to the Mg/Mg⁺ retrieval described by Langowski et al. (2014) lie in the emissivity γ and self-absorption *f* calculation, while the rest of the retrieval algorithm remained unchanged, beside marginal changes (e.g., there is no correction for inelastic scattering needed etc.). The emissivity γ is calculated as follows:

²⁰
$$\underbrace{\gamma}_{\frac{\text{photons}}{\text{s}}} = \underbrace{P(\theta)}_{\text{Phase function}} \times \int \underbrace{\pi F(\lambda)}_{\frac{\text{photons}}{\text{s cm}^2 \text{ nm}}} \times \underbrace{\sigma(\lambda)}_{\text{cm}^2} d\lambda \times \underbrace{\frac{A_{ji}}{\sum_{k} A_{jk}}}_{\text{rel. Einstein coeff.}}$$
, (2)

with the solar irradiance $\pi F(\lambda)$ (note that it is convention to use $\pi F(\lambda)$ (see, e.g., Chamberlain et al., 1958), and π belongs to the symbol and is not meant as a factor 3.14...) 7915



(1)

and

$$\int \sigma d\lambda = \frac{1}{4\pi\epsilon_0} \frac{\pi e^2}{mc^2} f_{ij} \lambda_{ij}^2$$

integ. abs. cross section in nm cm²

The process causing the emission is resonance fluorescence. A solar photon is absorbed by a Na atom, which is excited from the lower state *i* to the higher state *j* and is spontaneously and immediately re-emitted, which returns the atom to the lower state *i*. The two relevant transitions are from the lowermost excited states $3^2P_{\frac{1}{2}}$ for D₁ and $3^2P_{\frac{3}{2}}$ for D₂ to the ground state $3^2S_{\frac{1}{2}}$. The relative Einstein coefficient, the probability of the resonant transition compared to all other possible transitions from the upper state to lower states, is 1 for both lines, because only the two lowest excited states are involved as upper states and the transition between the *P* states is highly improbable. The Na specific parameters, i.e., oscillator strength f_{ij} and transition wavelength λ_{ij} are taken from the NIST atomic spectra database (Kramida et al., 2012). The scattering angle θ dependent phase function *P* is a linear combination of the phase function for Rayleigh scattering and an isotropic part:

¹⁵
$$P(\theta) = \frac{3}{4}E_1(\cos^2(\theta) + 1) + E_2.$$

P is normalized to 4π , which is already considered in Eq. (1). The factors E_1 and E_2 depend on the change in angular momentum Δj and are taken from Chandrasekhar (1960) (see Table 1). The factors E_1 and E_2 are different for both D lines. The D₁ line has a purely isotropic phase function ($E_1 = 0$ and $E_2 = 1$) while the D₂ line has a mixture of both components $E_1 = 0.5$ and $E_2 = 0.5$. The wavelength integrated absorption cross section has to be distributed over the correct shape function of the emission line and the resulting absorption cross section profile is multiplied with the wavelength dependent solar irradiance. This product is then integrated over all wavelengths yielding the true combination of the second and third factor of the emissivity in Eq. (2).

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(3)

(4)

Following McNutt and Mack (1963) the solar irradiance in the vicinity of the Na D_1 and D_2 lines can be calculated for x (x is defined further below):

$$I(x) = I_0 \times e^{\left(\frac{|x|}{x_e}\right)^A}.$$

The ratio $\frac{I_0}{I_{\text{baseline}}}$ of the intensity at the line center and the baseline intensity at the ⁵ edge of the Fraunhofer lines is stated in McNutt and Mack (1963). To scale this to the SCIAMACHY spectrum a solar irradiance of $5.44 \times 10^{14} \frac{\text{photon}}{\text{s cm}^2 \text{ nm}}$ is used for the edge of the line: for the D_2 line the following values are used:

$$I_0 = 0.0444 \times 5.44 \times 10^{14} \frac{\text{photon}}{\text{s cm}^2 \text{ nm}}$$

$$A = 2.16$$

$$x_e = \frac{\hat{\sigma}}{k_{\text{line center}}} = \frac{0.228 \text{ cm}^{-1}}{16\,973 \text{ cm}^{-1}} = 13.4 \times 10^{-6}$$

$$x = \frac{k - (k_{\text{line center}} - \text{shifts})}{k_{\text{line center}}} = \frac{k - k_{\text{line center}}}{k_{\text{line center}}} + \frac{\text{shifts}}{k_{\text{line center}}}$$

The formula is given for wavenumbers k and the parameters x and x_e are normalized to the wavenumber of the line center. The width parameter of the line in terms of wavenumbers is denoted by $\hat{\sigma}$ (see McNutt and Mack, 1963).

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Wavenumber shifts between the solar spectrum and the absorption cross section in the mesosphere are considered. Here, a positive shift value leads to a red shift as the line center is moved toward shorter wavenumbers and, therefore, longer wavelengths. Since the width of the solar Fraunhofer line is not much larger than the width of the lines in the mesospheric absorption cross sections, these shifts have a non-negligible influence on the emissivity. In McNutt and Mack (1963) a constant red shift for the solar 20 lines of $\frac{\text{grav}_{\text{shifts}}}{k_{\text{lines contart}}} = 2.7 \times 10^{-6}$ is measured, which is a combination of the gravitational red shift and other smaller shifts, e.g., pressure shifts. Additionally, Doppler shifts from



(5)

the rotation of Earth and the change of the Earth-sun-distance along the elliptical orbit of Earth are considered, which are similar in magnitude as the constant shift and have a combined maximum amplitude of $\pm 3.2 \times 10^{-6}$. For the D₁ line the following parameters are used:

⁵
$$I_0 = 0.0495 \times 5.44 \times 10^{14} \frac{\text{photon}}{\text{s cm}^2 \text{ nm}}$$

 $A = 2.14$
 $x_e = 12.8 \times 10^{-6}$.

Because there are hyperfine splittings for both D lines, the line center is the weighted average of the individual line wavelengths and strengths.

- ¹⁰ Na has only one stable isotope, i.e., ${}^{23}_{11}$ Na and therefore has no isotope effect. The stable isotope has a nuclear angular momentum of $I = {}^{3}_{2}$, which leads to a hyperfine splitting of the energy levels. The splitting for the lower $3^{2}S_{\frac{1}{2}}$ state is stronger than the splitting of the upper states $3^{2}P_{\frac{1}{2}}$ and $3^{2}P_{\frac{3}{2}}$. This can be explained phenomenologically by the smaller distance of the valence electron and the nucleus in the *S* state, which leads to a larger overlap of the nucleus and electron wave functions and therefore
- a stronger perturbation of the electron state. Due to the stronger splitting of the *S* state compared to the *P* states, the D_1 and D_2 lines each split into two groups of lines in close spectral vicinity (this is called a "s-resolved blend" in McNutt and Mack, 1963). The Doppler width of the Na lines in the mesosphere is approximately 1.25 pm. The two
- ²⁰ groups of adjacent lines have a separation of about 2 pm and thus can be separated. However, the lines inside a group are too narrow to be resolved in the mesosphere. The existence of several degenerate lines, however, is important for the correct weighting of the two s-resolved lines. This is, e.g., well explained in Chamberlain et al. (1958); McNutt and Mack (1963); Fricke and von Zahn (1985).
- The solar spectrum as well as the mesospheric absorption cross section for the Na D_2 line are shown in Fig. 2. The Na density is large enough that a non-negligible part of



the incoming solar irradiation is either absorbed along the path from the sun to the point of resonance fluorescence, or along the line of sight, after the emission. This reduction of emissivity is considered in the self-absorption factor f:

$$f = \frac{\int \sigma(\lambda) \pi F(\lambda) \times e^{-\sigma(\lambda)g} d\lambda}{\int \sigma(\lambda) \pi F(\lambda) d\lambda},$$

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with the integrated true slant column density $q = \int n ds$. Note that the integral in Eq. (1) 5 contains n as a linear factor, but also has a non-linear dependence on n because of the self-absorption factor f. The equation is linearized employing an iterative approach using the retrieved density of the previous step in the non-linear part to retrieve the linear density n. As noted by Langowski et al. (2014), setting f = 1, which corresponds to no self-absorption, is a good starting step for the iteration.

2.3 Extension for multiple scattering

In the previous section the optimization and adaptation of the single scattering retrieval algorithm developed for Mg and Mg⁺ for the retrieval of Na were described. However, the single scattering approximation for the background signal is only valid for wavelengths below about 300 nm. In the visible region radiation may be reflected from the Earth's surface or scattered back from the lower atmosphere into the mesosphere. As a result, a part of the incoming solar irradiation may pass the grid cells more than just once and can, therefore, produce more emission. This is considered by a factor multiplied to the solar irradiance, which will be called the albedo factor in the following.

Different correction methods for Na retrievals with OSIRIS are reported by Gum-20 bel et al. (2007) and Hedin and Gumbel (2011). In Hedin and Gumbel (2011) the background signal for the limb scan at 40 km tangent altitude is compared to a single scattering radiative transfer model considering Rayleigh scattering only. Because the lowest tangent altitude of SCIAMACHY limb MLT measurements is at 53 km, this approach cannot directly be used, because the background signal is too small at this



(6)

altitude compared to straylight contamination. Because SCIAMACHY can resolve both Na D lines, which are differently sensitive to self-absorption, another approach to determine the amount of radiation passing the Earth's atmosphere, being reflected at the Earth's surface and then being scattered into the limb field of view of the instrument is presented in Sect. 2.3.1. Unfortunately, this approach did not always yield reasonable results, so that another approach is presented in Sect. 2.3.2, which is similar to the one in Hedin and Gumbel (2011), and which was finally used.

2.3.1 Total to single scattering ratio estimation from direct comparison of the D_1 and the D_2 line

- ¹⁰ The albedo factor is determined as the factor for which both D lines yield the same Na number densities. For typical Na slant column profiles shown in Fig. 3 the identification of the optimal albedo factor is illustrated in Fig. 4. It should be noted that the phase function (Eq. 4) is changed to $P_{\text{new}} = \frac{P_{\text{old}} + (\text{albedo factor} - 1)}{\text{albedo factor}}$. This takes into account the increased part of multiply scattered radiation, which we assume is unpolarized and therefore effectively increases E_2 in Eq. (4). This approach is only reasonable if the retrieval result is nearly independent of the applied constraint parameters (e.g., vertical smoothing, necessary to reduce oscillation of the result). This is not the case for the Mg/Mg⁺ retrieval by Langowski et al. (2014). For Na the statistical errors are sufficiently small so that the Na retrieval is much less sensitive to smoothing constraints
- then that of Mg. However, the dependence on the variation of the constraint parameter is unfortunately not entirely negligible, especially when the densities are large, as is the case in Fig. 5. The meaning of the constraint parameter used here is explained in Langowski et al. (2014): it defines how strong the smoothness of the profile is weighted in the retrieval equation. Figure 5 shows retrievals for different constraint parameters.
- For moderate constraint parameter $(1 \times 10^{-7} \text{ to } 5 \times 10^{-10})$ the retrieved peak density is nearly independent of the choice of the constraint parameter for approximately two orders of magnitude. A factor of 5–10 in the constraint parameter has a similar effect to a change of the albedo factor of 0.1 in Fig. 4. The three highest constraint parameters



 $(5 \times 10^{-7} - 5 \times 10^{-5})$ show too strong smoothing while the lowest constraint parameters $(5 \times 10^{-9} - 5 \times 10^{-10})$ show oscillations at high altitudes. Note that a stronger smoothing leads to the need of a lower albedo factor to match the D₁ and D₂ density, so a systematic error in one property is rather reduced than increased if the other one is tuned, which results in some robustness in the method.

5

Unfortunately, this method failed quite often for the following reasons: The densities were too small and insensitive to the albedo factor, the D_2 slant column densities were already larger than the ones for D_1 or the differences between the D_1 and D_2 slant column densities initially were too large, so that the D_2 line could yield larger densities than the D_1 even for albedo factors smaller than 1. However, although this algorithm

than the D₁ even for albedo factors smaller than 1. However, although this algorithm failed the matching of densities retrieved from both Na lines is a good indicator for how good the calibration of the data and the used radiative transfer model work.

2.3.2 Total to single scattering ratio estimation from comparison of simulated single scattering limb radiance and measured limb radiance

- The Rayleigh scattered background radiance in the vicinity of the Na D lines can be used to calculate the total to single scattering ratio for a limb measurement. A simple approach to obtain the albedo factor is to use the ratio of the measured limb radiance and the limb radiance calculated with a radiative transfer model. The radiative transfer model SCIATRAN is able to calculate the single and total Rayleigh scattered electro-
- ²⁰ magnetic radiation for known measurement geometries and atmospheric parameters. Figure 6 shows the ratio of the measured limb radiance and the simulated single scattering radiance for different tangent altitudes, as well as the ratio for the simulated total scattered simulated radiance and the single scattered radiance for different ground albedos. As was reported by Oikarinen et al. (1999) the modelled total to single scat-
- tering ratio only shows a weak dependency on the tangent altitude. The measured limb radiance, however, has a completely different behaviour and shows a nearly exponential increase in the total to single scattering ratio above 50 km altitude. The true



Rayleigh-scattered limb radiance is roughly proportional to the density at the tangent altitude and exponentially decreasing limb radiances with increasing tangent altitudes are expected. We assume that there is a small straylight component from lower tangent altitudes that reaches the instrument for high tangent altitudes and that this component

- ⁵ is only weakly dependent on altitude. Above 50 km this additional straylight component is on the order of magnitude as the actual limb radiance at this tangent altitude and becomes much bigger than the actual Rayleigh scattered component. This nearly constant offset to the radiance along with the exponential decrease of the Rayleigh scattered radiance with altitude explains the nearly exponential rise of the measured
- to simulated single scattering ratio. In the troposphere and lower stratosphere clouds significantly influence the radiance and the simple approach using an albedo factor fails there. Therefore, we assume that in a region above 20 and below 45 km, there is a region where the limb measurement to simulated single scattering ratio is very close to it's simulated value with the right ground albedo.
- ¹⁵ Any unwanted straylight also affects the dark signal measurement at 350 km tangent altitude, which is usually subtracted from the limb radiances at the 30 other tangent altitudes. As a consequence this dark radiance is not simply subtracted for the following considerations. Instead of this we assume that a part of the total incoming radiation $I_{inc}(h,\lambda)$ is proportional to the simulated single scattering radiance $I_{ss}(h,\lambda)$, which we call the multiplicative part aI_{ss} with the multiplicative component *a*, while a part of the straylight component and the actual dark radiance is an additional component *b* of the light: $I_{inc}(h,\lambda) = a(h)I_{ss}(h,\lambda) + b(h)$ (with tangent altitude *h* and wavelength λ). To determine the multiplicative and additive components the wavelength region between 650
- and 660 nm is used. This spectral region is not affected strongly by atmospheric absorption in the mesosphere and upper stratosphere, and includes the H α Fraunhofer line at 656 nm, which is a clear solar signature, so that fitting the multiplicative and additive component is not an ill posed problem (where a smaller *a* could be compensated by a higher *b* etc.). The estimated value for the total to single scattering ratio is the minimum of the multiplicative component *a* above 20 km altitude. Figure 7 shows the



fit and Fig. 8 the results of the multiplicative and additive component for one example profile.

This estimation, however, can only be done for the nominal SCIAMACHY limb measurements measuring from ground to 90 km altitude. The MLT measurements start at

- around 53 km altitude, so that the minimum between 20 and 45 km can not directly be found. However, the latitudinal and longitudinal co-located nominal measurements from the days of the same time period show very similar profile shapes, which can be fitted to MLT-data to retrieve the albedo factor. Figure 9 shows the final fit of the albedo factor for an example measurement. First the multiplicative components for all nominal and
- ¹⁰ MLT measurements are found. The median for the days in the same time period (\pm 200 orbits were used here) of nominal limb measurements is formed for all altitudes. The albedo factor *A* for the median nominal measurements is found. Between 50 and 70 km the logarithms of the nominal and the MLT measurements are fitted as factor *B* (In MLT= *B* In nominal). Fitting the logarithm puts effectively more weight on the matching
- of the lower albedo factor values at lower altitudes, which considers that the perturbing effect is smallest there. The albedo factor for the MLT measurements is then given by the product *AB*. The resulting albedo factors show similarities to the simulated total to single scattering ratios, which are high at scattering angles at around 90° and close to 1 for low (around 0°) and high (around 180°) scattering angles.

20 3 Monthly averaged Na densities

25

The monthly mean Na number densities as a function of latitude and altitude are shown in Fig. 10. The average of both retrieval results $(\frac{1}{2}(D_1 + D_2))$ is used. The altitude of the density maximum is about 92 km and varies only by a few km during the year. Na shows a seasonal cycle in number density with a winter maximum, with peak densities in the winter mid latitudes of up to 6000 cm⁻³. In the summer the maximum density decreases to only ≈ 1000 cm⁻³ at high latitudes. The annual mean is shown in Fig. 11 and shows an average peak density of roughly 2000–4000 cm⁻³ apart from high latitudes, which



are only measured in the summer period and, therefore, only show the small summer densities. The results for both hemispheres are nearly symmetric.

The seasonal variation of the vertical profile for low, mid and high latitudes is shown in Fig. 12, and vertical profile shapes for selected latitudes in July are shown in Fig. 13.

- ⁵ At low latitudes a semi-annual variation with maxima in March and September is observed. This variation is well correlated with the semi-annual variation in temperature (see, e.g., von Savigny and Lednyts'kyy, 2013), which shows a maximum during this time. The semi-annual oscillation for Na was also found in model studies by Marsh et al. (2013). The vertical profiles at high latitudinal summer show a reduced width.
- Figure 14 shows the seasonal variation of the Na number density for the region between 80–105 km altitude, as well as the seasonal variation of the normalized Na profiles at 71°N, which is a high latitude and covered by SCIAMACHY observations for several months during boreal summer. The peak altitude at 71°N is about 93 km for most months. Not only is the density strongly reduced during summer, the profile also
- ¹⁵ becomes thinner: from a full width at half maximum (FWHM) of 11 km in spring and autumn to only 7 km in summer. Qualitatively a similar reduction is also observed for other width-defining parameters than 50% of the maximum value (e.g. 75, 25, 5% of maximum etc.). The reduction of the profile width occurs on both the lower and the upper edge of the profile. Figure 15 shows the vertical column densities (VCDs) for difforent menths and latitudes. The VCDs are formed by integration of the vertical profiles.
- ferent months and latitudes. The VCDs are formed by integration of the vertical profiles shown in Fig. 10. The VCDs also show the seasonal cycle with a summer minimum of slightly below 1×10^9 cm⁻² at high latitudes and up to 1×10^{10} cm⁻² at the highest latitudes covered in the winter hemisphere.



4 Error discussion and validation

4.1 Estimation of errors in the vertical profile

Four to eight individual day measurements have been used to form the multiannual monthly averages shown in the previous section. The errors of the measured limb radiances are linearly propagated into the error of the SCDs to estimate the error of daily average SCDs. As the inversion step includes non-linear operation, a further linear error propagation from the SCDs to the number densities is not carried out. Instead we use the same Monte-Carlo approach as Langowski et al. (2014). A random Gaussian error in the range of the typical error of a daily average SCD profile is applied to

- a daily average SCD profile and the number densities are retrieved. This is repeated a large number of times (here 1000 repetitions were used). The mean and the standard deviation of the large number of Monte Carlo realizations are determined. The so determined standard deviation quantifies the error of the profile. The result of this method is shown in Fig. 16. The error is smaller than the measured number density in the region between 90 and 100 km with the D. line begins a clightly employed and the stan-
- ¹⁵ the region between 80 and 100 km, with the D₂ line having a slightly smaller error than the D₁ line. In the maximum number density region the relative error is roughly 10%. In Fig. 16 both Na lines agree very well, however, this is not always the case, which will be discussed in the next section.

4.2 Differences between D₁ and D₂ retrieval results

For a comparison of the individual results based on the D_1 or the D_2 line only, Fig. 17 shows the absolute and relative differences for the VCDs of both lines. The overall agreement of the results for the D_1 and the D_2 line is good, showing relative differences of only \pm 10% for most months and latitudes. However, for the highest latitudes in southern hemispheric winter the differences are larger with absolute differences of up to 3×10^9 cm⁻² which correspond to relative differences of up to 40%. The large



discrepancies occur in a region where the Na density and therefore self-absorption is high.

There may be different reasons for the discrepancies, e.g., remaining issues with the calibration of the data. Furthermore, small inaccuracies in the assumptions for the radiative transfer model contribute to the differences. For instance, the self-absorption approximation only considers loss along the line of sight and no contribution of multiple scattering into the line of sight. Furthermore, a constant width of the Dopplerbroadened mesospheric absorption cross section is used; however, the width can slightly change with temperature. In addition to the resonance fluorescence dayglow, Na also shows a chemoluminescent nightglow (see, e.g., Fussen et al., 2010; Plane et al., 2012). This nightglow shows a lower ratio of the D₂/D₁ emission signal than 2, which is not caused by self-absorption. Thus, non-negligible small chemoluminescence, compared to the resonance fluorescence, could explain larger retrieved densi-

ties for the D_1 line with the current method.

15 4.3 Comparison to independent data sets

In the following, the SCIAMACHY data set is compared to ground- and space-based measurements. Figure 18 shows a comparison to ground-based ALOMAR (Arctic Lidar Observatory for Middle Atmosphere Research) lidar measurements at Andøya, Norway, at 69° N recorded between 2008 and 2013. The majority of these have been published by Dunker et al. (2015a) and show a mean peak altitude of around 92 km, which is in good agreement with the peak altitudes found in the SCIAMACHY data. The SCIAMACHY error bars are the standard deviation of measurements in each month. The errors bars of the respective daily mean Na column density measured by the lidar denote the standard deviation, which is a measure of the geophysical variation on that 25 day.

The SCIAMACHY and the ALOMAR results are similar and on the same order of magnitude (a factor 3 for the largest differences) and overall in quite good agreement. In the summer months June and July the ALOMAR and SCIAMACHY measurements



of Na column density sometimes agree, but on several days ALOMAR measures much smaller or much larger values. The ALOMAR Na lidar measures larger column density each time a sporadic Na layer appears in the lidar's observation volume. This usually happens during the night (see, e.g., Heinrich et al., 2008), but not during SCIAMACHY's

- time of observation (11 a.m.). The transience of sporadic Na layers results in larger geophysical variation in the red symbols of those particular nights in Fig. 18. We attribute the cases when ALOMAR observed much smaller column density than SCIAMACHY to (a) adsorption or absorption of Na atoms on NLC particles and smaller ice particles and (b) the temperature in the coldest phase of a gravity wave leading to a chemical balance with less atomic Na and more Na compounds. SCIAMACHY does not detect those strong variations, because the measurement volume is much larger than that of
- these strong variations, because the measurement volume is much larger than that of the lidar's, and because SCIAMACHY averages in longitude.

The ALOMAR VCDs are larger in April and September than in June and July, and thus are in general agreement with the SCIAMACHY seasonal variation. Lidar results for the winter month at Andoya are available from Tilgner and von Zahn (1988) showing

¹⁵ for the winter month at Andoya are available from Tilgner and von Zahn (1988) showing VCDs of around $5 \times 10^9 \text{ cm}^{-2}$ between December and February. In their Fig. 7, Dunker et al. (2013, 2015b) show VCDs between 3×10^9 and $7 \times 10^9 \text{ cm}^{-2}$ in December. Again the seasonal cycle for the two different techniques is clear.

Figure 19 shows a comparison to ground based lidar-measurements by She et al. (2000) at around 40° N. The overall agreement of the seasonal variation and density is quite good.

The peak altitude obtained by She et al. (2000) is also 90–92 km. The full width at half maximum (FWHM) of the peak is 9–10 km (not shown here), which is slightly smaller than the 11–14 km for SCIAMACHY. However, SCIAMACHY scans a much larger volume of space, which might in part explain this difference. The largest differences between SCIAMACHY and the the values presented by She et al. (2000) are about 20 % from July to November.

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The data set of She et al. (2000) was also used for comparison with other global satellite measurements by Fussen et al. (2010) (their Fig. 7) and the WACCM model



by Marsh et al. (2013) (their Fig. 10). There is a good qualitative and quantitative global agreement in seasonal variation with measurement results reported by Fussen et al. (2010) and Hedin and Gumbel (2011) as well as model with results by Marsh et al. (2013). The reduction of the profile width in the summer high northern latitudes is ten-

tatively explained by Marsh et al. (2013) by an increased ionization rate at the upper edge and the Na reaction into NaHCO₃. The latter is favored by low temperatures in the polar summer mesopause region at the bottom edge. A further reduction process at the bottom edge, which is, e.g., shown by Gardner et al. (2005), Fig. 9, is the uptake of atomic Na by NLC or smaller ice particles. This process also depends on low tem peratures so that both reduction processes at the lower edge are correlated and hardly distinguishable.

5 Conclusions

The extension of a retrieval approach previously used for the retrieval of mesospheric magnesium, to the retrieval of Na number density profiles in the MLT region is presented. Monthly mean Na number densities on a latitudinal and vertical grid retrieved from the SCIAMACHY limb MLT measurements from 2008 to 2012 are presented. The Na peak has a FWHM of 5–15 km which depends on latitude and season and is smallest at summer at high latitudes. The peak density varies from 1000 to 6000 cm⁻³ and shows a clear seasonal cycle with a summer minimum most pronounced at high latitudes. The retrieved SCIAMACHY data set is in good agreement with other mea-

Intitudes. The retrieved SCIAMACHY data set is in good agreement with other measurements and models. This data set provides a unique set of data for testing our understanding of the role of meteoroids and their release of Na coupled with the other metal and metal ions, e.g., Mg and Mg⁺ on upper atmospheric chemistry.

In the future, the SCIAMACHY Na data product will be extended to the period from 2002 to 2012 by applying the retrieval algorithm also to the nominal SCIAMACHY limb data, using the results of the MLT retrieval as a-priori information.



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Table 1. E_1 and E_2 depend on the change of angular momentum Δj (from Chandrasekhar, 1960).

Δj	E ₁	E ₂
+1	$\frac{(2j+5)(j+2)}{10(j+1)(2j+1)}$	$\frac{3j(6j+7)}{10(j+1)(2j+1)}$
0	$\frac{(2j-1)(2j+3)}{10j(j+1)}$	$\frac{3(2j^2+2j+1)}{10j(j+1)}$
-1	$\frac{(2j-3)(j-1)}{10j(2j+1)}$	$\frac{3(6j^2+5j-1)}{10j(2j+1)}$



Figure 1. Data of the solar extraterrestrial spectrum in the region 586–594 nm measured by SCIAMACHY on 3 June 2010 and from the Smithsonian Astrophysical Observatory (Chance and Kurucz, 2010). The Fraunhofer lines are readily observed and the left figure shows both the SCIAMACHY and the SAO 2010 spectrum, from which the baseline value of $5.44 \times 10^{14} \frac{\text{photon}}{\text{s cm}^2 \text{nm}}$, which agrees for both, is used in the approximate formula by McNutt and Mack (1963). The right figure shows the SAO 2010 spectrum compared to the fully resolved approximation of the D₁ and D₂ lines taken from McNutt and Mack (1963). Note that the approximate formula by McNutt and Mack (1963) is only valid close to the center of the Fraunhofer lines. The fully resolved Na Fraunhofer lines are much deeper than the lines in the SAO 2010 spectrum and the SCIAMACHY spectrum.





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Figure 2. Absorption coefficient for the D_2 line at temperature T = 220 K and solar irradiance spectrum for different shifts.



























Figure 7. Fit of the multiplicative and additive radiation component around the H α line at 656 nm.





Figure 8. Fit results for the multiplicative and additive component as well as the simulated values for the same ground albedo as in Fig. 6.









Figure 10. Latitude–altitude distribution of the monthly mean Na densities. The average of the results for both Na lines is used. Note that the highest covered latitude is at 82° N/S.

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Figure 11. Annual mean Na distribution. Note that the high latitudes are only measured in the hemispheric summer.

















Figure 14. Left: monthly mean Na number densities at 71°N. Right: profiles of the left figure normalized by the peak densities of each month.





Figure 15. Seasonal variation of the vertical Na column densities (VCDs).





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Figure 16. Mean and standard deviation (error bars) of the Na D_1 and D_2 line retrieval for the equatorial SCIAMACHY measurements on 20 March 2010.



Figure 17. Absolute (left, $D_1 - D_2$) and relative (right, $2\frac{D_1 - D_2}{D_1 + D_2}$) difference of the Na VCDs retrieved from the D_1 and D_2 lines.







Figure 18. Comparison of the SCIAMACHY VCD profile at 69° N with lidar observations at Andøya, Norway.



Figure 19. Left: comparison of the SCIAMACHY VCD profile at 40° N and the results from She et al. (2000). Right: comparison of the same profiles with profiles from Fussen et al. (2010) (their Fig. 7) and Marsh et al. (2013) (their Fig. 10).

