

## General Comments

The content of this manuscript aims at evaluating the impact from windmills on weather radars. More in depth, the work focuses on estimating the wind turbine clutter (WTC) reflectivity by means of a new proposed model, which in turn should allow quantifying this kind of affectation.

The proposed new model consists on a set of simplified reflectivity formulae. This set is valid for a wide frequency range and different wind turbines. The most part of this work focuses on providing an accurate Radar Cross Section (RCS) of wind turbine through characterizing numerical results from a Physical Optic (PO) simulation technique.

This work shows an effort into reproducing a real scenario, and hence, the new contribution seems to be useful for Weather Radar Services in the task of quantifying this kind of affectation. However, in an actual scenario, other elements like the terrain or secondary lobes can take an important role in a real WTC reflectivity map. In this regard, a little effort on a final validation to corroborate the WTC reflectivity model (model accuracy) would highly consolidate this work. Somehow, in the manuscript should appear some discussion that includes the disadvantages or limitations of the proposed model regarding the elements that have not been considered in the analysis.

On the other hand, with the aim to corroborate the proposed new work, the following general remarks (A-D) should be considered for the whole manuscript:

A) Consider depicting or representing more clear for the reader the coordinates used into the overall text, specially with the different angular coordinates (e.g. 'alfa' and 'tetha' in expression '(3)', and 'tetha' in figures 1 and 7).

B) Consider reorganizing Section 4 and 5, as some contents about results from simulations need to be linked better to Subsection 4.2. When doing this, consider creating a new subsection for the analysis, rewording its conclusions (paragraphs 3 and 4 in page 1486), in order to emphasize that these are the base for characterizing the backscattering in Section 6.

C) The expressions which are the base of the proposed formulae should have a better detailed deduction (e.g. expressions '(2)' and '(3)' in Section 6).

D) The references should be checked regarding each citation in the overall text. In this regard, peer-reviewed references should take a significant role.

These general remarks would be also included in the specific comments below.

*The authors would like to thank the referee for his/her constructive comments to improve the manuscript. We have carefully considered all the comments and revised the manuscript accordingly.*

*Please note that the changes have been applied to the version of the paper that was uploaded after the changes suggested by Anonymous Referee #1.*

## Specific Comments

### Abstract

#### 1. Page 1478, Second Paragraph

Consider mentioning how the scenario for the developed model is just to situate the reader.

*As suggested by the reviewer, an additional comment on the scenario has been included in the abstract:*

*“For the proposed model, a representative scenario has been chosen, where both the weather radar and the wind farm are placed on clear areas, i.e., wind turbines are supposed to be illuminated only by the lowest elevation angles of the radar beam.”*

### Section 1

#### 1. Whole section

Review the references citation. Regarding the references section 'Norin, 2012' should be 'Norin and Haase, 2012', 'Gallardo, 2011' does not appear and the same for 'Grande, 2015', 'ITU-R, 2009', etc.

*The references section and the references citations have been reviewed through the text.*

*In particular, citations to (Norin, 2012) have been changed to (Norin and Haase, 2012).*

*The references that correspond to (Isom et al., 2008), (Gallardo et al., 2011) and (Grande et al., 2015) have been included in the References section:*

*“Gallardo-Hernando B., Muñoz-Ferreras J.M., Pérez-Martínez F., Aguado-Encabo F.: Wind Turbine Clutter Observations and Theoretical Validation for Meteorological Radar Applications, Radar, Sonar & Navigation, IET, vol.5, no.2, pp.111-117, Feb. 2011.”*

*“Grande, O., Angulo, I., Jenn, D., Aguado, F., Guerra, D., and de la Vega, D.: Analysis of Wind Turbines Radar Cross Section for Analyzing the Potential Impact on Weather Radars, 2015 9th European Conference on Antennas and Propagation (EUCAP), 12-17 April 2015.”*

*“Isom, B. M., Palmer, R. D., Secrest, G. S., Rhoton, R. D., Saxion, D., Allmon, T. L., Reed, J., Crum, T., Vogt, R., Detailed Observations of Wind Turbine Clutter with Scanning Weather Radars, Journal of Atmospheric and Oceanic Technology, vol. 26, pp. 894-910, 2008.”*

*The reference that corresponds to (ITU-R, 2009) was already included in the paper:*

*ITU-R (International Telecommunication Union): Technical and Operational Aspects of Ground-Based Meteorological Radars. Recommendation ITU-R M.1849; International Telecommunication Union; Geneva, Switzerland, 2009.*

#### 2. Page 1479, Line 2

Add a reference to reinforce the factors proposed as the main factors.

*References to (Gallardo-Hernando, 2011), (Norin and Haase, 2012) and (Norin, 2015) have been included to reinforce the main factors mentioned in the text.*

### 3. Page 1480, Line 1

Avoid the use of the word 'interferences' in this context. Consider 'afectations', 'impacts' or a similar word in this case.

*As suggested by the referee, "interferences" has been replaced by "impacts" in this case.*

## Section 2

### 1. Page 1480

Avoid the use of pharentesis to enclose statements and use commas instead. Reword this paragraph.

*The first paragraph of Section 2 was already changed according to the comments of Referee #1:*

*"In weather radars, wind turbines may lead to misidentification of precipitation features and to erroneous characterization of meteorological phenomena. These errors may be due to: clutter caused by signal echoes from the wind turbines; signal blockage, as the physical size of the wind turbine creates a shadow zone behind them of diminished detection capacity; and interference to the Doppler mode of the radar, on account of frequency shifted echoes from the rotating blades (Angulo, 2014)"*

### 2. Page 1480, First Paragraph

'Norin and Haase, 2012' can be included to reinforce the statement about the error classification.

*The suggested citation has been included in the text.*

### 3. Page 1480, Fourth Paragraph

Consider adding some other reference about the impact due to signal blockage. See, for example, a suggested reference below this text. Mention that this non-desired phenomena is not treated in this manuscript.

*The suggested reference has been included in the text and cited in Section 2.*

*"Belmonte, A.; Fabregas, X., Analysis of Wind Turbines Blockage on Doppler Weather Radar Beams, IEEE Antennas and Wireless Propagation Letters, vol.9, pp.670-673, 2010"*

*In regard to the second suggestion, according to a comment from Referee #1, a sentence was added at the end of the third paragraph in order to make clear that this paper does not address the signal blockage estimates: "Consequently, this paper does not focus on addressing the signal blockage estimates."*

### 1. Page 1480, Fifth Paragraph

Avoid the use of parenthesis to enclose statements and use commas instead. Consider including some reference to reinforce the statement at the end.

*The text has been reworded to avoid the use of parenthesis and some references have been included to reinforce the statement.*

*“As the RCS of a wind turbine depends both on fixed parameters, such as the dimensions and materials of each component of the wind turbine, and on variable parameters, such as position of the rotating blades and rotor orientation with respect to the radar, RCS values may vary drastically according to wind turbine working regimes and illumination conditions (Angulo et al., 2011), (Grande et al., 2014)”.*

## **Section 4**

### **Section 4.1**

#### **1. Page 1481**

In a real scenario, the backscattering from windmills can contain important differences depending on the terrain surface: In a flat area or over a hill, the reflectivity will be different from irregular surfaces or with important mountains behind. Reword this section to indicate that, in a more realistic calculation, the texture of the terrain should be included.

*Please note that comments by Referee #1 led to a change in the organization of the paper. The considerations of the analysis are now included in Section 3.2.*

*According to the reviewer’s comment, a last point has been included in Section 3.2 – Considerations of the analysis, as detailed in the response to the next comment.*

#### **2. Page 1482**

Add some words to justify that both the effect of secondary lobes and the terrain are excluded from the analysis.

*The RCS concept is defined to be independent of both the propagation effects, including potential terrain interactions, and the radar characteristics, including radiation pattern. However, the calculation of the reflectivity values may include additional parameters to account for these effects. For example, at long distances, the beam curvature and losses due to propagation in the troposphere might be included in the radar equation; terrain reflections may be considered in the characterization of the radiation pattern of the radar; the gain value in Eq. (11), (12) and (13) might refer to the gain of secondary lobes, etc. In order to simplify the analysis of the reflectivity values presented in the paper, without loss of generality, the calculation of the reflectivity values shown in Section 5 does not include these additional effects.*

*Therefore, as indicated in the response to the previous comment, a remark about the potential effects of terrain and the secondary lobes has been included in Section 3.2 – Considerations of the analysis.*

*“- Reflectivity model. The calculation of the reflectivity value from a wind turbine is based on considering Line of Sight (LoS) propagation. In real scenarios, interactions from the ground and terrain should be taken into account, e.g., potential shadowing effects (Norin and Haase, 2012). Moreover, it is assumed that the wind turbine is being illuminated by the main lobe of the radiation pattern of the radar.”*

## **Section 4.2**

### **Section 4.2.1**

#### **1. Whole section**

Generally, simulation tools take into account some assumptions, as for example standard conditions for modelling the radar beam propagation in the troposphere. In this work, apart from the reference given (Jenn, 2005) about the simulation software used, add some extra information for the reader explaining its principal assumptions.

*Please note that the descriptions of the PO method and the software tool are now included in Section 3.1.1 - Simulation tool and wind turbine models.*

*The first paragraph of Section 3.1.1 has been modified to add extra information about the PO theory assumptions. Further details on the theory behind the software tool can be found in the references and are not included in the paper in order to avoid redundant information. With respect to modeling the radar beam propagation in the troposphere, as the simulation tool provides RCS values, propagation effects are not included.*

*The first paragraph of Section 3.1.1 is now as follows:*

*“The present study is based on the accurate assessment of RCS values of wind turbines by applying the Physical Optics (PO) theory. The PO theory is a high-frequency approximation method that provides accurate results for electrically large objects ( $L \geq 10\lambda$ ) and for observation points near the specular direction. More precisely, the software tool POfacets (Jenn, 2005) has been used to calculate RCS patterns of three different wind turbine models. To do so, detailed facets-based representations of these wind turbine models have been prepared for the application of numerical solutions of the PO method for RCS estimations. The software tool does not include the effect of multiple reflections, diffraction or surface waves. More in depth descriptions of the Physical Optics Method and the simulation tool can be found in (Jenn, 2005), (Grande et al., 2014), (Grande et al., 2015).”*

### **Section 4.2.2**

#### **1. Page 1484, Line 19**

Replace 'currently' with 'usually' or give some reference instead.

*Please note that wind turbine models are now described in Section 3.1.1.*

*“Currently” has been replaced by “usually” in the mentioned sentence.*

### **Section 4.2.3**

#### **1. Page 1484**

Replace 'accuracy' with 'precision'.

*"Accuracy" has been replaced by "precision" in the title of the new Section 3.1.2. – Simulation precision.*

#### **2. Page 1484, Line 22**

Replace 'previously' for the corresponded section. Add more information in this subsection about the requirements of the simulation procedure.

*Due to the changes in the organization of the paper proposed by Referee #1, the "previously" mentioned here was already removed from the text.*

*The first paragraph of Section 3.1.2 has been reworded to add more information about simulation conditions, as follows:*

*"The analysis is based on the assessment of backscattering patterns for a set of elevation angles (variation in  $\theta$ ), as detailed in Section 3.2; and different conditions of rotor orientation with respect to the radar (variation in  $\Phi$  from  $0^\circ$  to  $185^\circ$ ) and blades position (rotating blades)."*

#### **3. Page 1485, Second Paragraph**

Add a link at the end to indicate where in this manuscript the reader can find the separated analysis (mast, nacelle and single blades).

*The following sentence has been added at the end of the paragraph: "(...) as described in Section 4 and shown in Fig. 2 to Fig. 7."*

### **Section 5**

#### **1. Page 1485**

Consider combining this section with the previous one, as it seems that the analysis from simulation outputs is an important part of the methodology to characterise the scattering for the proposed model. Moreover, reword this section with the aim to reinforce all the conclusions of the analysis.

*Former Section 5, now Section 4 - Simulation results and analysis is, as commented by the reviewer, the basis for the proposed scattering model. Therefore, the authors consider that it is important to maintain the analysis of the simulation results as an independent section. In our opinion, this improves the readability and understandability of the paper, and helps the reader identify the results of the simulations as an important part of the contribution presented here.*

On the other hand, according to the referee's comment, the conclusions of the analysis have been reworded as follows:

*"A first important conclusion obtained from the extensive set of simulations carried out is that the main scatterer of the wind turbine for the different frequency bands used for weather radar is the supporting mast. Moreover, the main feature of the scattering pattern of the mast is a main lobe normal to the slant surface, extremely directive in the vertical plane and omnidirectional in the horizontal plane. The scattering from the mast can be approximated by the RCS of a right circular cylinder, which will be the basis of the proposed model for calculating the wind turbine RCS values, as later described in Section 5.1.*

*The blades, by contrast, provide variable levels of signal scattering depending on the rotor orientation and blade positions. Despite the variability of the scattering from the blades, their contribution to the total RCS of the wind turbine is always significantly lower than the amplitude of the main lobe due to the mast. Therefore, in order to provide a worst-case assumption with respect to the signal scattered by the blades, the proposed scattering model will provide an upper limit to the RCS values from the blades, as will be shown in Section 5.2."*

## 2. Page 1485, Line 10

Replace 'As previously mentioned' with a phrase to clarify in what section is mentioned.

*"As previously mentioned" has been replaced by "As mentioned in Section 3.2".*

## 3. Page 1485, Fifth Paragraph

Reword this paragraph to indicate better the coordinate system that is being used.

*Also in line with the comments from Referee #1, and in order to make the coordinate system clearer, Fig. 1 has been simplified. Moreover, theta and phi parameters have been explained in Section 3.1.1, "Simulation tool and wind turbine models", which was Section 3.2.1 before but has been moved to the beginning of Section 3 in order to clarify the coordinate system before explaining the considerations of the analysis (now in Section 3.2).*

*The last paragraph of Section 3.1.1 is now as follows:*

*"Fig. 1 shows the reference coordinate system for the analysis. The wind turbine rotor is supposed to be oriented towards the x-axis and R refers to the radar position. As shown in the figure,  $\theta$  is the angle from the zenith that defines the radar position in the vertical plane, and  $\Phi$  specifies the horizontal position of the radar with respect to the rotor orientation, i.e., with respect to the rotor shaft axis"*

*These changes aim at providing an easier interpretation of the results in Section 5.*

## 4. Page 1486, Line 7

Replace 'Obviously' with a more proper expression, as for example 'As it can be expected'.

*The mentioned expression has been replaced in the text according to the reviewer's comment.*

## Section 6

### Section 6.1

#### 1. Whole section

Consider reorganizing this subsection to describe better the angular coordinates, as in figure 7 seems that does not appear the half cone angle, 'alpha'.

Consider describing a little bit more in depth how is deduced the expression (2) from the formulae in Siegel (1995), as it is the base for the proposed model. If you prefer, include an appendix with the procedure.

*Figure 7 has been changed to include the representation of the half cone angle  $\alpha$ .*

*Regarding the deduction of the expression (2), the main simplifications from the formulae in (Siegel et al., 1995) are described in a previous reference from the authors (Angulo et al., 2013). Therefore, this reference has been cited and the text and the minor simplifications applied for the monostatic case described as follows:*

*"The expression proposed in (Siegel et al., 1995) was adapted to a circular cylinder and simplified to avoid indeterminate forms as described in Appendix A of (Angulo et al., 2013). As for radar applications only backscattering is of interest, the formulae in (Angulo et al., 2013) for a circular cylinder can be further simplified assuming that  $\theta_t = \theta_r$  and  $\Phi = 0^\circ$  and expressed as:"*

#### 2. Page 1488, Line 19

Avoid the use of parenthesis.

*The text has been changed as follows:*

*"For all the analyzed cases, i.e., for the three wind turbine models and three working frequencies under consideration, the mean (...)"*

### Section 6.2

#### 1. Page 1489, First Paragraph

Remove 'as demonstrated in the simulations' or replace it with a more concrete reference to the section number where it is demonstrated.

*The statement "as demonstrated in the simulations" has been replaced by "as shown in Fig. 5 and Fig. 6".*

#### 2. Page 1489, Second Paragraph

Reword this paragraph reorganizing the order of the statements.

*According to the referee's comment, the paragraph has been reworded as follows:*

*"Therefore, instead of obtaining a complete scattering model for the blades, a simpler approach to this issue is characterizing the maximum value of the scattering from the blades.*



*To do so, the maximum RCS value due to the blades for each wind turbine model will be obtained. In fact, as commented before and shown in Fig. 5, the maximum RCS due to the blades corresponds to the contribution of a single blade in vertical position.”*

3. Page 1489, Line 19

Replace 'Obviously' with the section where it is demonstrated the frequency dependence of maximum RCS.

*“Obviously” has been replaced by “As shown in Section 4 when comparing Fig. 2, Fig. 3 and Fig. 4,”*

4. Page 1489, Line 25

Justify a little bit more why the RCS must be proportional to their corresponding dimensions.

*The text has been completed as follows: “(...), the relation between the maximum RCS from the mast and the maximum RCS from the blades must be proportional to their corresponding dimensions, as the RCS of an object generally depends upon its physical size when its orientation relative to the LoS to the radar is such that a significant area of the object is illuminated (Knott, 2006), (Skolnik, 2008).”*

5. Page 1490, Line 1

Justify better the reason why to consider only the 50 % of impact regarding the blade design. There would be important differences in results considering other percentages?

*The assumption of 50% is related to the reference (Spera and Sengupta, 1994)*

*Spera, D.A., Sengupta, D.L., Equations for Estimating the Strength of TV Signals Scattered by Wind Turbines, NASA Contractor Report 194468, May 1994.*

*According to the referee’s comment, the text has been changed as follows:*

*“As a very simple approach, the blade can be represented by a triangle. However, in real blade designs, the profile of the blade rotates from hub toward to the blade tip in order to maintain the angle of attack (Gipe, 2004). Considering this twist angle of the blades, the area of this triangle will be never completely facing the radar. In (Spera and Sengupta, 1994) it is empirically obtained that the signal scattering efficiency of a blade  $\eta$  is dependent on the blade twist according to:*

$$\eta = \exp(-2.30\Delta\theta),$$

*where  $\Delta\theta$  is the total blade twist from root to tip (rad). This total twist depends on the blade length and design. In commercial wind turbines, total blade twist is typically about 20 degrees. For example, a Vestas V27 model has a total blade twist of 13 degrees (Gipe, 2004), which provides scattering efficiency values around 0.45-0.60.*

*As a rough approach, we will consider a scattering efficiency of 50% for the wind turbine blade. As later shown in Table 2 and Table 3, this assumption leads to a good approximation of the signal scattered by the blades.”*

*Additional reference included:*

*Gipe, P., Wind Power: Renewable Energy for Home, Farm, and Business, 2<sup>nd</sup> edition, Chelsea Green Publishing, April 1, 2004.*

#### 6. Page 1490, Fourth Paragraph

Consider including a new table with the values of the differences between results from Table 2 and 3, and the results obtained from expression (9).

*A comparison of the maximum RCS of the blades from PO simulations and the maximum RCS values calculated according to Eq. (10) (former Eq. (9)) is now shown in Table 4.*

#### **Section 6.4**

##### 1. Page 1492, Line 4

Replace 'This' with 'The proposed'.

*The suggested change has been included in the text.*

##### 2. Page 1492, Final paragraph

Consider rewording the first or the second 'is obtained' so that the text would be more readable.

*The first “is obtained” has been replaced by “is completed”.*

#### **Section 7**

##### 1. Page 1494, Fourth Paragraph

Secondary lobes have not been considered in the analysis of this manuscript. Consider rewording this paragraph in order to be more consistent with the previous analysis.

*For the sake of clarity, the following sentence has been changed to remove the term “main lobe” from the indicated paragraph: “This model takes the RCS from the mast as a reference to estimate the maximum value of the RCS pattern of the whole wind turbine, (...)”*

*However, it should be noted that the term “main lobe” in the previous sentence referred to the main lobe of the scattering pattern of the wind turbine, and not to the main lobe of the radar beam.*

#### **References**

##### 1. Whole section

Check all references in the manuscript, specially the ones that only appear in the previous text citation.

**Suggested references:**

Belmonte A., Fàbregas X., 2010: Analysis of Wind Turbines Blockage on Doppler Weather Radar Beams, IEEE Antennas and Wireless Propagation Letters, Vol. 9.

*The references section and the references citations have been reviewed through the text.*

*The suggested reference has been included and cited in the text.*

# 1 Estimating Reflectivity Values from Wind Turbines for 2 Analyzing the Potential Impact on Weather Radar Services

3  
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## 8 9 10 Abstract

11 The World Meteorological Organization (WMO) has repeatedly expressed concern over the  
12 increasing number of impact cases of wind turbine farms on weather radars. Current signal  
13 processing techniques to mitigate Wind Turbine Clutter (WTC) are scarce, so the most  
14 practical approach to this issue is the assessment of the potential interference from a wind  
15 farm before it is installed. To do so, and in order to obtain a WTC reflectivity model, it is  
16 crucial to estimate the Radar Cross Section (RCS) of the wind turbines to be built, which  
17 represents the power percentage of the radar signal that is backscattered to the radar receiver.

18 For the proposed model, a representative scenario has been chosen, where both the weather  
19 radar and the wind farm are placed on clear areas, i.e., wind turbines are supposed to be  
20 illuminated only by the lowest elevation angles of the radar beam.

21 This paper first characterizes the RCS of wind turbines in the weather radar frequency bands  
22 by means of computer simulations based on the Physical Optics theory, and then proposes a  
23 simplified model to estimate wind turbine RCS values. This model is of great help in the  
24 evaluation of the potential impact of a certain wind farm on the weather radar operation.

## 25 26 1 Introduction

27 The potential impact of wind turbines on weather radar performance has been extensively  
28 studied in the last few years, with several evidences of wind turbine clutter observations in

1 | meteorological radar applications (Isom [et al.](#), 2008), (Gallardo-[Hernando et al.](#), 2011),  
2 | (Norin [and Haase](#), 2012), (Vogt [et al.](#), 2011) (WMO, 2005, 2010). The main objective of  
3 | these studies is to characterize and try to mitigate the so-called Wind Turbine Clutter (WTC),  
4 | mainly by means of digital signal processing such as clutter-filtering techniques.

5 | Unfortunately, these solutions are not widely available yet. Meanwhile, the most practical  
6 | approach to this issue is the prediction of the potential impact on a certain weather radar  
7 | service before installing a wind farm. In most cases, the identification of a potential impact  
8 | allows the planning of alternative solutions in order to guarantee the coexistence of wind  
9 | energy and meteorological radar services.

10 | Wind Turbine Clutter reflectivity depends on many factors including wind turbine  
11 | dimensions, wind direction and velocity, angle of incidence and radar frequency ([Gallardo-  
12 | Hernando et al.](#), 2011), ([Norin and Haase](#), 2012), ([Norin](#), 2015). In order to measure how  
13 | efficiently radar pulses are backscattered by wind turbines, existing models of wind turbine  
14 | clutter and weather radar recommendations rely on the turbines' Radar Cross Section  
15 | (Tristant, 2006), (ITU-R, 2009), (Norin [and Haase](#), 2012)-. The RCS is the projected area  
16 | required to intercept and isotropically radiate the same power as the target scatters toward the  
17 | receiver, and thus it is normally expressed in dB with respect to a square meter (dBsm)  
18 | (Skolnik, 2008) (Rinehart, 1997).

19 | In this context, the goal of this paper is to propose simplified formulae for the estimation of  
20 | reflectivity values from wind turbines at frequencies used by weather radars. These formulae  
21 | aim at being easily implementable in software tools for estimating the potential impact of  
22 | wind farms on weather radars.

23 | For this purpose, first RCS patterns for different working conditions of the wind turbines are  
24 | obtained by means of Physical Optics simulations, and subsequently analyzed. Additionally,  
25 | separate RCS patterns of the parts of the turbine are also calculated, in order to compare the  
26 | relative contribution of each component. Based on these simulations, a simple algorithm to  
27 | evaluate the potential impact of a wind farm on a nearby weather radar is proposed.

28 | It should be mentioned that similar studies for characterizing RCS of wind turbines have been  
29 | carried out for evaluating the impact on different services such as maritime radars ([Grande \[et  
30 | al.\]\(#\)](#), 2014) or television ([Angulo \[et al.\]\(#\)](#), 2011). However, as scattering is very dependent on  
31 | working frequency and illumination conditions, results cannot be extrapolated. Moreover,  
32 | preliminary results of the analysis presented in this paper are included in a previous

1 | communication from the authors (Grande [et al.](#), 2015). Those results correspond to a single  
2 | wind turbine model and a single working frequency. In the present paper, results are extended  
3 | to three wind turbine models of different size and the three frequency bands assigned to  
4 | weather radar services; besides, based on the obtained results, a novel formulation for  
5 | estimating the WTC reflectivity values for weather radar applications is proposed. This work  
6 | aims at making ~~impact~~ studies for the prediction of potential ~~interferences~~ [impacts](#) between  
7 | weather radar services and wind farm deployments easier to conduct.

8

## 9 **2 Impact of wind farms on weather radars**

10 | In weather radars, wind turbines may lead to misidentification of precipitation features and to  
11 | erroneous characterization of meteorological phenomena. These errors may be due to: clutter  
12 | caused by signal echoes from the wind turbines; signal blockage, as the physical size of the  
13 | wind turbine creates a shadow zone behind them of diminished detection capacity; and  
14 | interference to the Doppler mode of the radar, on account of frequency shifted echoes from  
15 | the rotating blades (Angulo [et al.](#), 2014), ([Norin and Haase, 2012](#)), ([Belmonte and Fabregas,](#)  
16 | [2010](#)).

17 | The clutter from wind turbines is due to radar echoes coming from a turbine and reaching the  
18 | radar with a power level higher than the radar detection threshold, preventing from correctly  
19 | detecting the precipitation level in the affected area. Although most of current radars include  
20 | signal processing techniques that remove static scattering from turbine masts, the scattered  
21 | energy will increase the effective noise floor of the radar receiver, which degrades the  
22 | detection capacity, and therefore, the data quality obtained by the radar. Detection of  
23 | precipitation requires a signal that exceeds the noise floor by at least the signal to noise ratio.  
24 | Energy scattered from wind turbines results in the occurrence of increased noise that might  
25 | cause desired targets to be undetected. Although the signal processing techniques may  
26 | mitigate the display of false targets generated by the stationary clutter from a wind farm, it  
27 | will not eliminate effects that raise the noise floor of the radar (Tristant, 2006) (Lemmon [et](#)  
28 | [al.](#), 2008).

29 | Regarding the Doppler mode of the radar, as it is aimed at detecting moving targets, in order  
30 | to determine the influence of a wind turbine on this operation mode only the scattering from  
31 | the blades should be considered.

1 Therefore, both the clutter phenomenon and the interference to the Doppler mode depend on  
2 the scattering characteristics of wind turbines. By contrast, as the blocking of the radar beam  
3 is due to the physical obstruction of the radar beam by the wind turbine, the methodology to  
4 estimate a potential impact of a wind farm due to signal blockage is not related to the RCS of  
5 wind turbines but to the percentage of the beam section blocked by the wind turbine structure  
6 (Tristant, 2006), [\(Belmonte and Fabregas, 2010\)](#). Consequently, this paper does not focus on  
7 addressing the signal blockage estimates.

8 As the RCS of a wind turbine depends both on fixed parameters, ~~(such as the dimensions and~~  
9 ~~materials of each component of the wind turbine)~~, and on variable parameters, ~~(such as~~  
10 ~~position of the rotating blades and rotor orientation with respect to the radar)~~, RCS values  
11 may vary drastically according to wind turbine working regimes and illumination conditions  
12 [\(Angulo et al., 2011\)](#), [\(Grande et al., 2014\)](#).

13 The calculation of RCS values by conventional prediction methods, such as the method of  
14 moments (MoM) or the finite difference time domain (FDTD) method, provides accurate  
15 results, but rely upon extremely detailed representations of the turbine, which requires  
16 significant modeling and complex calculations with great computational effort. Consequently,  
17 these RCS prediction methods cannot be easily implemented in computer simulation tools for  
18 analyzing the potential impact of a specific wind farm.

19 On the contrary, and due to the absence of simplified formulation, some published guidelines  
20 for analyzing the impact of wind turbines on radar services use typical fixed RCS values,  
21 disregarding the particular features of each installation (ITU-R ~~M.1849~~, 2009), (Tristant,  
22 2006). This is a very simple way to deal with wind turbine scattering, but its main  
23 disadvantage is that the proposed RCS values do not take into account the characteristics of  
24 the real scenario under analysis: wind turbine dimensions, angle of incidence and working  
25 frequency, amongst others. As a result, these proposed typical constant RCS values may lead  
26 to important estimation errors.

27 In this paper, a simplified formulation for determining accurate WTC reflectivity values is  
28 proposed. The presented method requires neither complex calculations nor the use of a  
29 simulation tool, whereas it provides RCS values adapted to the particular features of the case  
30 under analysis: dimensions of the wind turbine models, illumination conditions and working  
31 frequency.

32

### 1   **3   Methodology**

2   The main objective of this paper is to develop an estimation model of wind turbine reflectivity  
3   values for weather radars, consisting in a simplified formulation, easy to apply in the  
4   development of the impact studies, without requiring a complex software tool or a high  
5   amount of resources.

6   The estimation model should fulfill the following conditions:

- 7       -   Despite being a simplified formulation, the model should provide accurate Radar  
8       Cross Section values, which are directly translated into reflectivity values.
- 9       -   The model should consider the variability of the RCS values, generated by the rotor  
10      orientation and the blades rotation, as the RCS values are very dependent on the  
11      specific relative positions of the different components of the turbine with respect to the  
12      radar.
- 13      -   The model should be applicable to turbine models of different size, different working  
14      frequencies and different radar illumination conditions.

#### 15   **3.1   Simulation conditions**

##### 16   **3.1.1   Simulation tool and wind turbine models**

17   The present study is based on the accurate assessment of RCS values of wind turbines by  
18   applying the Physical Optics (PO) theory. The PO theory is a high-frequency approximation  
19   method that provides accurate results for electrically large objects ( $L \geq 10\lambda$ ) and for  
20   observation points near the specular direction. More precisely, the software tool POfacets  
21   (Jenn, 2005) has been used to calculate RCS patterns of three different wind turbine models.  
22   To do so, detailed facets-based representations of these wind turbine models have been  
23   prepared for the application of numerical solutions of the PO method for RCS estimations.  
24   The software tool does not include the effect of multiple reflections, diffraction or surface  
25   waves. More in depth descriptions of the Physical Optics Method and the simulation tool can  
26   be found in (Jenn, 2005), (Grande et al., 2014), (Grande et al., 2015).

27   It should be noted that this tool provides accurate RCS values for a specific rotor orientation  
28   and blade position, but at the expense of having to design rigorous representations of the wind  
29   turbine models. Hence, estimations of RCS values for each specific position of the blades



1 must be conducted, and therefore, hundreds of RCS simulations are required in order to obtain  
2 a detailed characterization of the RCS patterns for different working conditions. The analysis  
3 of this huge set of RCS values is the basis of the proposed simplified model to be integrated in  
4 the prediction tools for potential interference from a wind farm. In fact, the main motivation  
5 of the proposed simplified model is precisely avoiding the need of such a simulation effort in  
6 future cases under study.

7 | As ~~previously~~ mentioned in Section 1, three commercial wind turbine models were chosen for  
8 the analysis, which constitutes a representative selection of the wind turbines that are  
9 | ~~currently-usually~~ installed. Typical horizontal-axis wind turbines are composed of a mast or  
10 supporting tower, commonly made from tubular steel; a nacelle that holds all the turbine  
11 machinery and rotates to follow the wind direction; and a rotor with three blades of complex  
12 aerodynamic surface, being the rotor shaft tilted above the horizontal to enable greater  
13 clearance between the blades and the mast. Characteristics of the selected models are  
14 summarized in Table 1. It should be noted that upper and lower radii of the masts are different  
15 because the geometry of the supporting tower of the wind turbines is not a perfect right  
16 circular cylinder but a tapered cylinder.

17 Fig. 1 shows the reference coordinate system for the analysis. The wind turbine rotor is  
18 supposed to be oriented towards the x-axis and  $R$  refers to the radar position. As shown in the  
19 figure,  $\theta$  is the angle from the zenith that defines the radar position in the vertical plane, and  
20  $\Phi$  specifies the horizontal position of the radar with respect to the rotor orientation, i.e., with  
21 respect to the rotor shaft axis.

### 22 **3.1.2 Simulation precision**

23 The analysis is based on the assessment of backscattering patterns for a set of elevation angles  
24 | (variation in  $\theta$ ), as detailed in Section 3.2; and different conditions of rotor orientation with  
25 | respect to the radar (variation in  $\Phi$  from  $0^\circ$  to  $185^\circ$ ) and blades position (rotating blades).

26 Calculations with particularly high resolution have been conducted for RCS vertical patterns  
27 (resolution of  $0.001^\circ$  in  $\theta$ ), as great variability is expected in this plane. The effect of the  
28 rotating blades has been analyzed by simulations with a difference of  $15^\circ$  in the rotation angle  
29 of the blades. In addition, these estimated RCS values have been obtained for different  
30 positions of the rotor with respect to the incident signal in the horizontal plane (aspect angles  
31 separated  $1^\circ$  in  $\Phi$ ).

1 In order to evaluate the relative significance of the signal backscattered by the different parts  
2 of the wind turbine, separated RCS patterns of the mast, nacelle and single blades have been  
3 obtained and compared with the RCS pattern of the whole wind turbine, as described in  
4 Section 4 and shown in Fig. 2 to Fig. 7.

### 5 **3.2 Considerations of the analysis**

6 The case under analysis is a wind farm located within the detection volume of a weather  
7 radar. When this situation occurs, some specific conditions are applicable. The thorough  
8 outline of these conditions allows the clear delimitation of the scenario under analysis:

- 9 - **Monostatic backscattering.** Weather radars only receive monostatic backscattered  
10 signals, so monostatic RCS values are analyzed in this paper.
- 11 - **Frequency bands.** The analysis is conducted for the frequency bands assigned to  
12 weather radar operation: 2700-2900 MHz in S band; 5250-5725 MHz (mainly 5600-  
13 5650 MHz) in C band; and 9300-9500 GHz in X band (ITU-R, 2008). In weather  
14 radars, S-Band is well suited for detecting heavy rain at very long ranges, up to  
15 300 km; C-Band represents a good compromise between range and reflectivity and  
16 cost, and they can provided rain detection up to a range of 200 km; and X-Band  
17 weather radars are used only for short range weather observations up to a range of 50  
18 km (ITU-R and WMO, 2008).
- 19 - **Materials.** The metallic mast can be considered as perfect electric conductor (PEC).  
20 Although modern blades are made of composite materials which are difficult to  
21 characterize, in the simulations, blades are supposed to be metallic, in order to  
22 consider the worst-case assumption for this component of the turbine.
- 23 - **Relative location of weather radar and wind turbine, and elevation angles.** As a  
24 proof-of-concept for the proposed model, a representative scenario has been chosen.  
25 This scenario considers that weather radars are usually located in open places that  
26 allow unobstructed scanning of a wide area, up to 300 km. Wind farms are also placed  
27 on clear areas, where potential wind energy is higher. As weather radar beams use  
28 quite directive lobes (usually 1° beam width), wind turbines are illuminated only when  
29 radar transmission is pointing to the wind farm. Therefore, the scenario that must be  
30 analyzed is the potential incidence of the lowest elevation angles of the radar beam on  
31 the wind turbines. Lowest elevation angles of the scanning routine are usually

1 transmitted just above horizon, for radar located in flat areas, or slightly below the  
2 horizon, for radars located on top of the hills. Accordingly, a reasonable range of the  
3 lowest elevation angles where the radar beam can illuminate a wind turbine is  $-2^\circ$  to  
4  $+4^\circ$  with respect to the horizon (WMO, 2014) (Grande et al., 2015). The previous  
5 assumption leads to incidence angles on the wind turbine nearly perpendicular to the  
6 vertical axis of the mast, in particular, within the range  $88^\circ < \theta < 94^\circ$ .

7 - Reflectivity model. The calculation of the reflectivity value from a wind turbine is  
8 based on considering Line of Sight (LoS) propagation. In real scenarios, interactions  
9 from the ground and terrain should be taken into account, e.g., potential shadowing  
10 effects (Norin and Haase, 2012). Moreover, it is assumed that the wind turbine is  
11 being illuminated by the main lobe of the radiation pattern of the radar.

#### 13 4 Simulation results and analysis

14 As ~~previously~~ mentioned in Section 3.2, simulations have been carried out for three  
15 frequencies representative of the different weather radar frequency bands (2.80 GHz, 5.65  
16 GHz and 9.40 GHz), and three wind turbine models based on actual commercial turbines.

17 As an example, Fig. 2 to Fig. 4 show the vertical variation of the RCS patterns of wind  
18 turbine models 1 to 3 for a specific rotor orientation for the three frequencies under analysis.  
19 It can be observed that the RCS patterns show great variability, and a very directive main lobe  
20 is noticeable in all cases.

21 This maximum value of the RCS corresponds to an illumination direction of  $\theta = 89.56^\circ$  with  
22 respect to the zenith in case of WT Model 1,  $\theta = 89.48^\circ$  in case of WT Model 2, and  $\theta =$   
23  $89.42^\circ$  for WT Model 3. Taking into account the slant surface of the masts, these directions  
24 correspond to the direction normal to the mast surface of each wind turbine model. As  
25 expected, the maximum RCS value is larger for the tallest wind turbine. Moreover, when  
26 comparing Fig. 2 to Fig. 4, it is clearly observed that the main lobe is both higher and  
27 narrower as the frequency increases. This maximum value of the RCS in the vertical pattern is  
28 maintained for all the azimuth values due to the symmetry of the mast in the horizontal plane.

29 In order to identify the contribution of the blades and nacelle, for the highest frequency and a  
30 specific rotor orientation, the RCS of WT Model 3 is depicted in Fig. 5 for different positions  
31 of the blades (every  $30^\circ$  in the rotation movement). The RCS pattern of the isolated mast is

1 also depicted in Fig. 5. As observed in the figure, whereas the contribution from the blades  
2 varies in amplitude and position with the rotation movement, the maximum RCS of the wind  
3 turbine is constant and it is clearly generated by the mast. Fig. 5 also shows that the main  
4 contribution from the rotor is due to a blade being in vertical position (see curves related to  
5 P000 and P060 in Fig. 5).

6 As it can be expected Obviously, the contribution from the blades is strongly dependent on the  
7 rotor orientation with respect to the incident radar signal, whereas the contribution from the  
8 mast remains invariable in the horizontal plane due to its symmetry with respect to the  
9 vertical axis of the mast. This statement is confirmed by Fig. 6, where the vertical RCS  
10 patterns of WT Model 2 are compared for different illumination directions in the horizontal  
11 plane (different  $\Phi$  values).

12 A first important conclusion obtained from the extensive set of simulations carried out is that  
13 the main scatterer of the wind turbine for the different frequency bands used for weather radar  
14 is the supporting mast. Moreover, the main feature of the scattering pattern of the mast is a  
15 main lobe normal to the slant surface, extremely directive in the vertical plane and  
16 omnidirectional in the horizontal plane. The scattering from the mast can be approximated by  
17 the RCS of a right circular cylinder, which will be the basis of the proposed model for  
18 calculating the wind turbine RCS values, as later described in Section 5.1.

19 The blades, by contrast, provide variable levels of signal scattering depending on the rotor  
20 orientation and blade positions. Despite the variability of the scattering from the blades, their  
21 contribution to the total RCS of the wind turbine is always significantly lower than the  
22 amplitude of the main lobe ~~from~~ due to the mast. Therefore, in order to provide a worst-case  
23 assumption with respect to the signal scattered by the blades, the proposed scattering model  
24 will provide an upper limit to the RCS values from the blades, as will be shown in  
25 Section 5.2.

26 ~~The clear characterization of the scattering from the mast, in contrast with the variable~~  
27 ~~scattering from the rotating blades, is the basis of the proposed model for calculating the wind~~  
28 ~~turbine RCS values, which will differentiate scattering from fixed and moving parts of the~~  
29 ~~turbine.~~

30

## 1 5 Proposed model

### 2 5.1 Scattering from the mast

3 As demonstrated in the previous section, the mast is the main scatterer of the wind turbine due  
4 to its large dimensions, as it generates the maximum value of the RCS pattern.

5 The geometry of the mast can be approximated by a right cylinder, as for commercial wind  
6 turbine models, the half cone angle  $\alpha$  that defines the slant surface of the mast is small (see  
7 Figure 7),

$$8 \quad \alpha = \tan^{-1} \left( \frac{r_2 - r_1}{H} \right). \quad (1)$$

9 For example, for the three models under analysis, the half cone angle is smaller than  $0.6^\circ$ .  
10 Therefore, a perfectly conducting right cylinder tilted at an angle  $\alpha$  is used to assess the  
11 backscattered RCS of the mast based on the PO theory.

12 In (Siegel [et al.](#), 1955) the RCS pattern of an elliptic cylinder is obtained as a function of its  
13 dimensions and the angular positions of the transmitter and receiver in both the vertical and  
14 the horizontal planes. [The expression proposed in \(Siegel et al., 1955\) was adapted to a](#)  
15 [circular cylinder and simplified to avoid indeterminate forms as described in Appendix A of](#)  
16 [\(Angulo et al., 2013\).](#) As for radar applications only backscattering is of interest, the formulae  
17 in ([Siegel](#)[Angulo et al.](#), [1955](#)[2013](#)) for a circular cylinder can be [further](#) simplified [assuming](#)  
18 [that  \$\theta\_t = \theta\_r\$  and  \$\Phi = 0^\circ\$  and](#) expressed as:

$$19 \quad \sigma_{cylinder} = \frac{2\pi}{\lambda} r L^2 \sin \theta \left( \frac{\sin \left( \frac{2\pi}{\lambda} L \cos \theta \right)}{\frac{2\pi}{\lambda} L \cos \theta} \right)^2 \quad (2)$$

20 where  $\lambda$  is the wavelength of the radar transmission,  $\theta$  is the aspect angle as defined in  
21 Figure 7,  $r$  is the cylinder radius and  $L$  is the cylinder height.

22 In order to adapt the previous expression to the actual geometry of the mast, two  
23 approximations are considered:

24 1.- In (Skolnik, 2008), it is stated that Eq. (2) may be used to estimate the RCS of a truncated  
25 right circular cone if the radius  $r$  is replaced by the mean radius of the cone and  $L$  is replaced  
26 by the length of the slanted surface.

27 2.- Taking into account the results of the previous section, it is clear that the backscattering  
28 pattern of the mast is extremely directive in the direction perpendicular to the slanted surface

1 of the mast. Therefore, Eq. (2) should be slightly modified in order to account for the half  
2 cone angle  $\alpha$ .

3 According to the above mentioned considerations, the proposed model to calculate the RCS of  
4 the wind turbine mast is given by

$$5 \quad \sigma_{mast} = \frac{2\pi}{\lambda} r L^2 \sin(\theta + \alpha) \left( \frac{\sin\left(\frac{2\pi}{\lambda} L \cos(\theta + \alpha)\right)}{\frac{2\pi}{\lambda} L \cos(\theta + \alpha)} \right)^2, \quad (3)$$

6 where  $\lambda$  is the wavelength of the radar transmission,  $\theta$  is the aspect angle as defined in  
7 Figure 7,  $\alpha$  is the half cone angle as given by Eq. (1),  $r$  is the mean radius of the truncated  
8 cone

$$9 \quad r = \frac{r_1 + r_2}{2}, \quad (4)$$

10 and  $L$  is the length of the slanted surface of the mast

$$11 \quad L = \frac{H}{\cos \alpha}. \quad (5)$$

12 In order to prove the validity of the proposed model, the obtained results are compared to the  
13 simulation values presented in the previous section. For all the analyzed cases, i.e., for the  
14 (three wind turbine models ~~and~~, three working frequencies) ~~under consideration~~, the mean  
15 error between the simulation values and the values obtained according to Eq. (3) is lower than  
16 0.85 dB. An example to demonstrate that simulation and modeling values are very well  
17 aligned is shown in Fig. 8.

## 18 **5.2 Scattering from the blades**

19 From the results of simulations of the RCS patterns, it is clearly shown that the scattering  
20 from the blades is significantly lower than the scattering from the mast. Moreover, it should  
21 be considered that, as demonstrated in the simulations shown in Fig. 5 and Fig. 6, the  
22 scattering from the blades is strongly dependent on the position of the rotor with respect to the  
23 radar. In order to analyze a potential impact situation, therefore, a detailed representation of  
24 the blades and all the possible movements of the wind turbine should be needed. However,  
25 obtaining detailed representations of actual wind turbine blades is quite difficult, as the blade  
26 design is property of the wind turbine manufacturer, and the analysis of hundreds of different  
27 combinations of rotor orientation and blades position requires a huge amount of time and  
28 effort.

1 Therefore, instead of obtaining a complete scattering model for the blades, a simpler approach  
2 to this issue is characterizing the maximum value of the scattering from the blades. To do so,  
3 the maximum RCS value due to the blades for each wind turbine model will be obtained. In  
4 fact, as commented before and shown in Fig. 5, the maximum RCS due to the blades  
5 corresponds to the contribution of a single blade in vertical position.~~A simpler approach to this~~  
6 ~~issue is considering a maximum value of the scattering from the blades. Therefore, instead of~~  
7 ~~a complete scattering model from the blades, the objective of this section is to characterize the~~  
8 ~~maximum RCS value due to the blades for each wind turbine model. In fact, as commented~~  
9 ~~before and shown in Fig. 5, the maximum RCS due to the blades corresponds to the~~  
10 ~~contribution of a single blade in vertical position.~~

11 From the set of simulations carried out in this analysis, the maximum RCS values from the  
12 mast and blades are shown in Table 2. ~~Obviously~~As shown in Section 4 when comparing Fig.  
13 2, Fig. 3 and Fig. 4, these maximum RCS values are frequency dependent. However, if the  
14 relation between the maximum RCS from the mast and the maximum RCS from the blades is  
15 obtained, it can be observed that this relation remains almost constant for the different  
16 frequency bands.

17 Although their complex geometry prevents from obtaining simple RCS models to characterize  
18 the scattering from the blades, the relation between the maximum RCS from the mast and the  
19 maximum RCS from the blades must be proportional to their corresponding dimensions, as  
20 the RCS of an object generally depends upon its physical size when its orientation relative to  
21 the LoS to the radar is such that a significant area of the object is illuminated (Knott, 2006),  
22 (Skolnik, 2008).

23 As a very simple approach, the blade can be represented by a triangle. However, in real blade  
24 designs, the profile of the blade rotates from hub toward to the blade tip in order to maintain  
25 the angle of attack (Gipe, 2004). Considering ~~the~~this twist angle of the blades, the area of  
26 theis triangle will be never completely facing the radar. In (Spera and Sengupta, 1994) it is  
27 empirically obtained that the signal scattering efficiency of a blade  $\eta$  is dependent on the  
28 blade twist according to:

$$29 \eta = \exp(-2.30\Delta\beta), \text{_____} (6)$$

30 where  $\Delta\beta$  is the total blade twist from root to tip (rad). This total twist depends on the blade  
31 length and design. In commercial wind turbines, total blade twist is typically about 20

degrees. For example, a Vestas V27 model has a total blade twist of 13 degrees (Gipe, 2004), which provides scattering efficiency values around 0.45-0.60.

-As a rough approach, we will consider ~~that only the~~ scattering efficiency of 50% ~~of for~~ the wind turbine blade ~~will be directly illuminated by the radar~~. As later shown in Table 2 and Table 3, this assumption leads to a good approximation of the signal scattered by the blades.

Therefore, the relative scattering area from the blades  $A_{blades}$  is calculated as:

$$A_{blades} = 0.5 \frac{w \cdot l}{2}, \quad (67)$$

where  $w$  is the maximum blade width and  $l$  is the blade length.

The mast, by contrast, will be constantly facing the radar with an area that can be approximated by a trapezoid:

$$A_{mast} = (r_1 + r_2)H, \quad (78)$$

Where  $r_1$  and  $r_2$  are the upper and lower radii of the mast, and  $H$  is the mast height.

Thus, the relation  $\Delta$  in dB between the relative scattering area of the mast and blades can be obtained as:

$$\Delta = 10 \log_{10} \left( \frac{4H(r_1+r_2)}{w \cdot l} \right). \quad (89)$$

According to the wind turbine characteristics gathered in Table 1, these relations are calculated and shown in Table 3. If values in Table 2 and Table 3 are compared, it can be stated that the relation in dB between the relative scattering area of the mast and blades can be considered a good approximation of the difference in dB between the maximum RCS from the mast and the maximum RCS from the blades. Taking this into account, the maximum RCS from the blades (dBsm) can be obtained as:

$$\sigma_{blades} = \max \{ \sigma_{mast} \} - \Delta = 10 \log_{10} \left( \frac{2\pi}{\lambda} r L^2 \right) - 10 \log_{10} \left( \frac{4H(r_1+r_2)}{w \cdot l} \right). \quad (910)$$

A comparison of the maximum RCS of the blades from PO simulations and the maximum RCS values calculated according to Eq. (10) is shown in Table 4. As shown in the table, the difference between the values provided by the simulations and the values calculated according to the proposed model are lower than 2 dB for all the analyzed cases.



### 1 5.3 Converting RCS values to WTC reflectivity values

2 In order to model wind turbine clutter, the RCS of a wind turbine must be converted to the  
3 equivalent radar reflectivity factor.

4 The weather radar equation, for distributed targets such as rain, is given by

$$5 \left| P_r = \frac{P_t G^2 \theta_0 \Phi_0 c \tau \pi^3 |K|^2 z}{1024 \ln(2) \lambda^2 R^2}, \right. \quad (4011)$$

6 where  $P_r$  is the power received back by radar,  $P_t$  is the power transmitted by radar,  $\theta_0$  and  $\Phi_0$   
7 are the elevation and azimuth beamwidths,  $c$  is the speed of light,  $\tau$  is the radar pulse length,  
8  $|K|^2$  is the complex index of refraction of the hydrometeor,  $\lambda$  is the wavelength of the radar  
9 pulse,  $R$  is the distance to the target and  $z$  is the radar reflectivity factor (ITU-R, 2009),  
10 (Rinehart, 1997), (Norin [and Haase](#), 2012). The radar reflectivity factor  $z$ , normally expressed  
11 in decibels of reflectivity (dBZ), is the quantity that is used to obtain the rain rate:

$$12 \left| z = \frac{P_r 1024 \ln(2) \lambda^2 R^2}{P_t G^2 \theta_0 \Phi_0 c \tau \pi^3 |K|^2}. \right. \quad (4112)$$

13 On the other hand, the radar equation for a point target, such as distant wind turbine contained  
14 within a range resolution cell, is given by

$$15 \left| P_r = \frac{P_t G^2 \lambda^2 \sigma}{64 \pi^3 R^4}, \right. \quad (4213)$$

16 where  $\sigma$  is the RCS of the wind turbine (Knott, 2006).

17 Assuming that the wind turbine is entirely included within the beam cell resolution of the  
18 weather radar, we can compare equations (4011) and (4213) and then obtain the radar  
19 reflectivity factor as

$$20 \left| z = C_1 \frac{\sigma}{R^2}, \right. \quad (4314)$$

21 where  $C_1$  is a constant that depends on the parameters of the radar system:

$$22 \left| C_1 = \frac{16 \ln(2)}{\pi^6 c} \cdot \frac{\lambda^4}{\theta_0 \Phi_0 \tau} \cdot \frac{1}{|K|^2}. \right. \quad (4415)$$

### 23 5.4 Complete model for estimating WTC reflectivity in weather radar bands

24 Results obtained in the previous subsections are the basis of the complete model to  
25 characterize the signal scattering from wind turbines in the weather radar bands proposed in

1 this paper. ~~This~~The proposed simplified model for estimating WTC reflectivity in weather  
2 radar bands is summarized in Table 45.

3 First, based on the specific characteristics of the wind turbine and the working frequency, the  
4 RCS pattern of the mast near the direction normal to the slant surface is obtained. The RCS  
5 from the mast is used to determine the main lobe of the RCS pattern of the whole wind  
6 turbine.

7 Then, the maximum RCS value from the blades is calculated, as the maximum RCS value of  
8 the mast minus the relation in dB between the relative scattering areas of the mast and blades.  
9 This maximum RCS value from the blades establishes an upper bound, in such a way that all  
10 the possible orientations of the nacelle and blades are considered.

11 In order to combine both patterns and obtain the simplified RCS pattern of the whole wind  
12 turbine, the RCS values from the mast are used for angles  $\theta$  near the incidence normal to the  
13 slanted surface of the mast, i.e. for  $\theta$  values such that  $\sigma_{mast} \geq \sigma_{blades}$ . This way, the main lobe  
14 of the RCS pattern of the whole wind turbine is estimated. For incidence angles off the main  
15 lobe due to the mast, and up to the limiting angles  $\theta$  due to the illumination characteristics of  
16 weather radars, the maximum RCS value from the blades is applied.

17 An example of the results of this proposed RCS model is shown in Fig. 9, together with the  
18 simulated results of the RCS pattern for different rotor orientations. In the figure, it can be  
19 seen that the maximum RCS of the mast is well approximated by the model, and the mask  
20 established off the main lobe covers the scattering from the blades for different rotor  
21 orientations.

22 Once the RCS pattern is ~~obtained~~completed, for a specific illumination condition and  
23 configuration of the radar, the estimation of the RCS of the wind turbine is obtained.

24 Finally, assuming that the whole wind turbine is included within the beam cell resolution of  
25 the radar, the corresponding reflectivity value is calculated, as described in Table 45.

## 27 **6 Conclusions**

28 In order to estimate the potential impact of a wind farm on a weather radar service, one of the  
29 main issues to be analyzed is Wind Turbine Clutter reflectivity, which is directly related to the  
30 Radar Cross Section of wind turbines.

1 A preliminary study about possible interference problems is the most appropriate way to  
2 proceed in order to make the coexistence of wind energy and meteorological services  
3 possible. To do so, an estimation of the RCS of the wind turbines to be installed is a must.  
4 Although it is possible to obtain RCS values by conventional methods such as MoM and  
5 FDTD, they require detailed representations of the wind turbines' design and complex  
6 calculations, which are too time-consuming and difficult to obtain. On the contrary, typical  
7 values that do not take into account the particular features of the case under analysis may lead  
8 to significant errors in the impact analysis.

9 In this paper, the RCS patterns of wind turbines for the weather radar working frequencies  
10 have been analyzed. From the obtained results, it can be concluded that the mast is the main  
11 scatterer of the wind turbine, featuring a very directive lobe in the direction perpendicular to  
12 the slanted surface of the mast. The blades, by contrast, contribute to the total RCS of the  
13 wind turbine with secondary lobes that depend on the rotor orientation with respect to the  
14 illumination direction and the blades' position.

15 Based on the above-mentioned conclusions, a simple RCS model to characterize  
16 backscattering from wind turbines in the weather radar bands has been proposed. This model  
17 takes the RCS from the mast as a reference to estimate the ~~main lobe~~maximum value of the  
18 RCS pattern of the whole wind turbine, and then calculates the maximum RCS from the  
19 blades taking into account the actual dimensions of the wind turbine model. Finally, and  
20 assuming that the whole wind turbine is included within the beam cell resolution of the radar,  
21 the WTC reflectivity can be directly obtained.

22  
23 The proposed RCS model can be used to estimate the maximum clutter due to the presence of  
24 a wind turbine, estimating the scattered power from the mast. On the other hand, even if the  
25 Doppler radar under study uses a clutter filter that suppresses stationary objects, the rotating  
26 blades of a wind turbine might still be detected. As proved in (Norin, 2015), weather  
27 information from radar cells affected by a wind turbine is not always lost. In fact, when  
28 precipitation gives rise to reflectivity values stronger than those due to wind turbines, radar  
29 data could still be used. Therefore, the reflectivity model proposed in this paper is of interest  
30 not only to assess a potential detrimental impact on the performance of a weather radar, but  
31 also to evaluate to which extent this degradation might exist, if reflectivity values from  
32 precipitation and wind turbine blades are compared.

1 This simple WTC reflectivity model aims at being implemented in software planning tools  
2 and is expected to make the preliminary impact studies of wind farms on weather radar  
3 services easier.

4

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29

1 Table 1. Wind turbine models selected for the simulations.

|                   | Model 1 | Model 2 | Model 3 |
|-------------------|---------|---------|---------|
| Mast height       | 78 m    | 100 m   | 119 m   |
| Mast upper radius | 1.15 m  | 1.80 m  | 2.40 m  |
| Mast lower radius | 1.75 m  | 2.70 m  | 3.60 m  |
| Rotor diameter    | 87 m    | 90 m    | 112 m   |
| Blade length      | 42.50 m | 44.00 m | 54.65 m |
| Rated power       | 2.0 MW  | 2.0 MW  | 3.3 MW  |

2

1 Table 2. Maximum RCS values from the mast and blades for the wind turbine models selected  
 2 for the simulations.

|             | WT Model 1     |                 |                             | WT Model 2     |                 |                             | WT Model 3     |                 |                             |
|-------------|----------------|-----------------|-----------------------------|----------------|-----------------|-----------------------------|----------------|-----------------|-----------------------------|
|             | Mast<br>(dBsm) | Blade<br>(dBsm) | $\Delta$ Difference<br>(dB) | Mast<br>(dBsm) | Blade<br>(dBsm) | $\Delta$ Difference<br>(dB) | Mast<br>(dBsm) | Blade<br>(dBsm) | $\Delta$ Difference<br>(dB) |
| 2.80<br>GHz | 55.97          | 45.92           | 10.05                       | 61.38          | 46.81           | 14.57                       | 64.00          | 48.81           | 15.19                       |
| 5.65<br>GHz | 59.95          | 49.42           | 10.53                       | 64.32          | 49.74           | 14.58                       | 67.03          | 52.10           | 14.93                       |
| 9.4<br>GHz  | 62.42          | 51.61           | 10.81                       | 66.45          | 52.00           | 14.45                       | 69.14          | 54.22           | 14.92                       |

3



1 Table 3. Relation  $\Delta$  between the relative scattering area of the mast and blades for the wind  
2 turbine models selected for the simulations.

| WT Model 1 | WT Model 2 | WT Model 3 |
|------------|------------|------------|
| 9.90 dB    | 12.65 dB   | 13.38 dB   |

3

1 Table 4. Comparison of the maximum RCS of the blades from PO simulations and the  
 2 maximum RCS values calculated according to the proposed model. The third column shows  
 3 the difference in dB between the values obtained in the simulations and the values calculated  
 4 according to the proposed model.

|                           | <u>WT Model 1</u> |               |                   | <u>WT Model 2</u> |               |                   | <u>WT Model 3</u> |               |                   |
|---------------------------|-------------------|---------------|-------------------|-------------------|---------------|-------------------|-------------------|---------------|-------------------|
|                           | <u>Simulation</u> | <u>Model</u>  | <u>Difference</u> | <u>Simulation</u> | <u>Model</u>  | <u>Difference</u> | <u>Simulation</u> | <u>Model</u>  | <u>Difference</u> |
|                           | <u>(dBsm)</u>     | <u>(dBsm)</u> | <u>(dB)</u>       | <u>(dBsm)</u>     | <u>(dBsm)</u> | <u>(dB)</u>       | <u>(dBsm)</u>     | <u>(dBsm)</u> | <u>(dB)</u>       |
| <u>2.80</u><br><u>GHz</u> | <u>45.92</u>      | <u>46.08</u>  | <u>0.16</u>       | <u>46.81</u>      | <u>48.72</u>  | <u>1.91</u>       | <u>48.81</u>      | <u>50.62</u>  | <u>1.82</u>       |
| <u>5.65</u><br><u>GHz</u> | <u>49.42</u>      | <u>50.05</u>  | <u>0.63</u>       | <u>49.74</u>      | <u>51.67</u>  | <u>1.93</u>       | <u>52.10</u>      | <u>53.65</u>  | <u>1.55</u>       |
| <u>9.4</u><br><u>GHz</u>  | <u>51.61</u>      | <u>52.52</u>  | <u>0.91</u>       | <u>52.00</u>      | <u>53.80</u>  | <u>1.79</u>       | <u>54.22</u>      | <u>55.77</u>  | <u>1.55</u>       |

5

1 | Table 45. Simplified model for estimating WTC reflectivity in weather radar bands.

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**Model for calculating wind turbine clutter reflectivity**

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1- Wind turbine RCS

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$$\sigma_{mast} = 10 \log_{10} \left( \frac{2\pi}{\lambda} r L^2 \sin(\theta + \alpha) \left( \frac{\sin\left(\frac{2\pi}{\lambda} L \cos(\theta + \alpha)\right)}{\frac{2\pi}{\lambda} L \cos(\theta + \alpha)} \right)^2 \right) \quad (\text{dBsm}) \quad \text{for } \theta |_{\sigma_{mast} \geq \sigma_{blades}}$$

$$\sigma_{blades} = 10 \log_{10} \left( \frac{2\pi}{\lambda} r L^2 \right) - 10 \log_{10} \left( \frac{4H(r_1 + r_2)}{w \cdot l} \right) \quad (\text{dBsm}) \quad \text{for } \theta |_{\sigma_{mast} < \sigma_{blades}}$$

Where:  $\alpha = \tan^{-1} \left( \frac{r_2 - r_1}{H} \right)$       and       $L = \frac{H}{\cos \alpha}$

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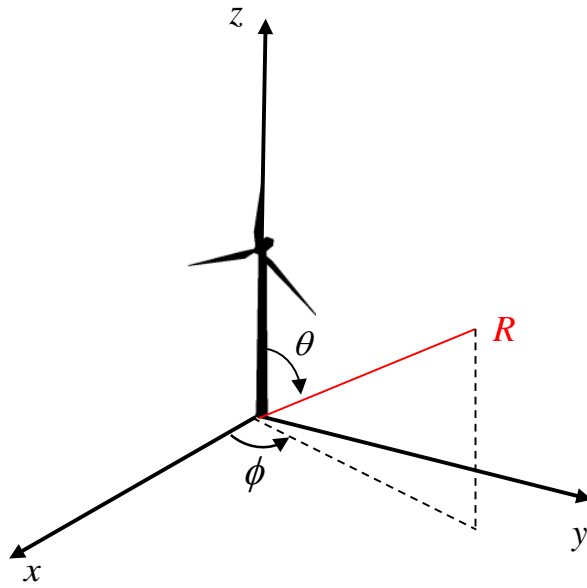
2- Wind turbine clutter reflectivity

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$$Z = \frac{16 \ln(2)}{\pi^6 c} \cdot \frac{\lambda^4}{\theta_0 \Phi_0 \tau} \cdot \frac{\sigma}{|K|^2 R^2}, \quad \text{where } \sigma \text{ is the RCS in linear values (m}^2\text{)}$$

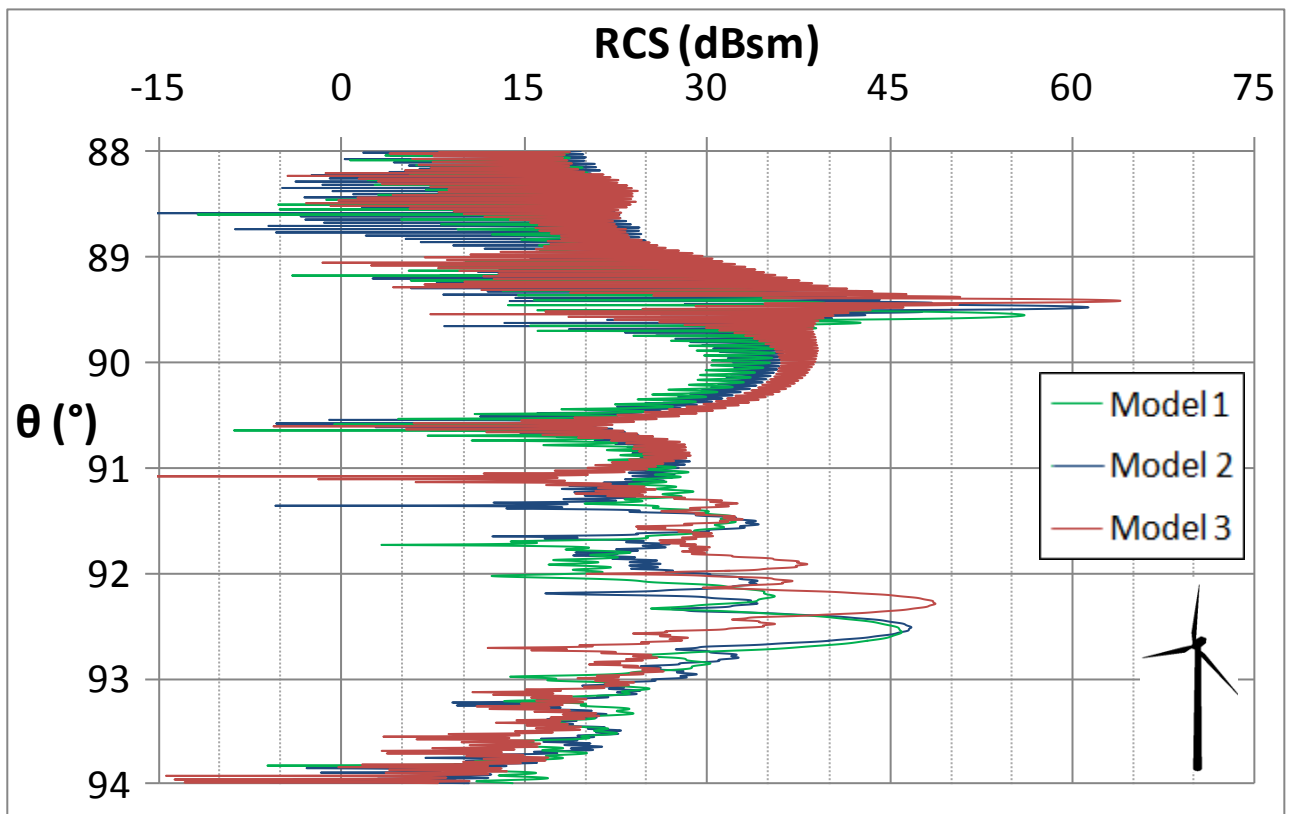

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2



1  
2  
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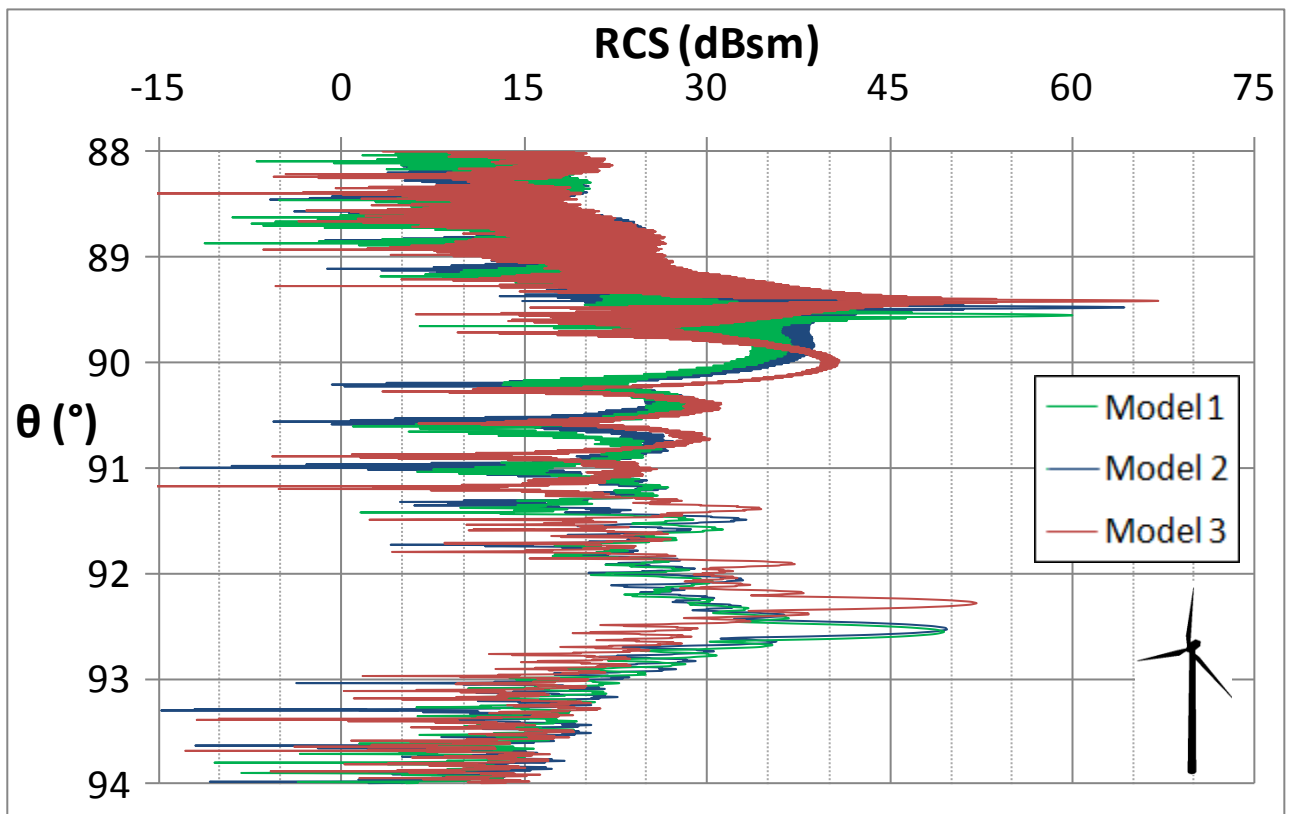
Figure 1. Spherical coordinate system used in the RCS calculations.  $R$  represents radar location.



1

2 Figure 2. Vertical sections of RCS patterns ( $\Phi = 5^{\circ}$ ) for wind turbine models 1 to 3 at  
 3 frequency 2.80 GHz. Rotor position is indicated in the lowest right corner.

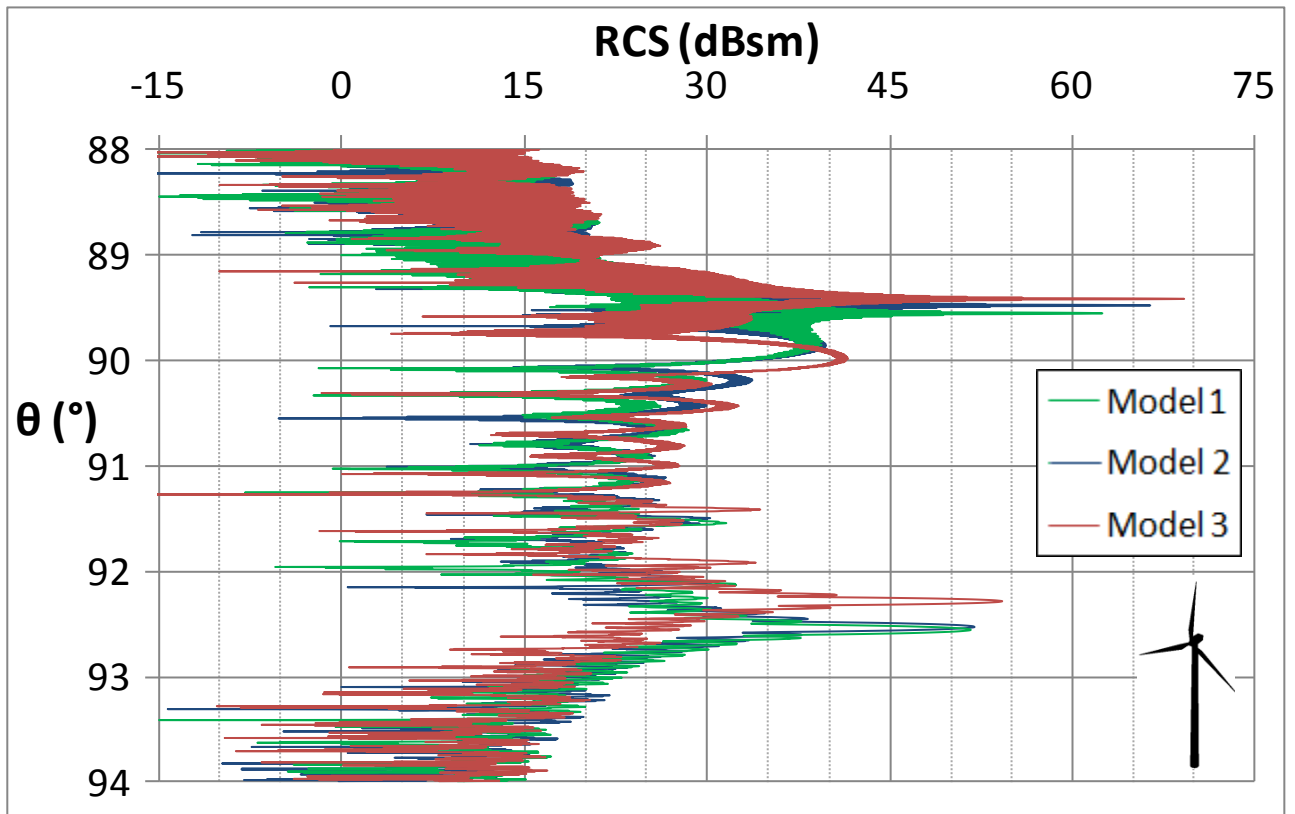
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1

2 Figure 3. Vertical sections of RCS patterns ( $\Phi = 5^{\circ}$ ) for wind turbine models 1 to 3 at  
 3 frequency 5.65 GHz. Rotor position is indicated in the lowest right corner.

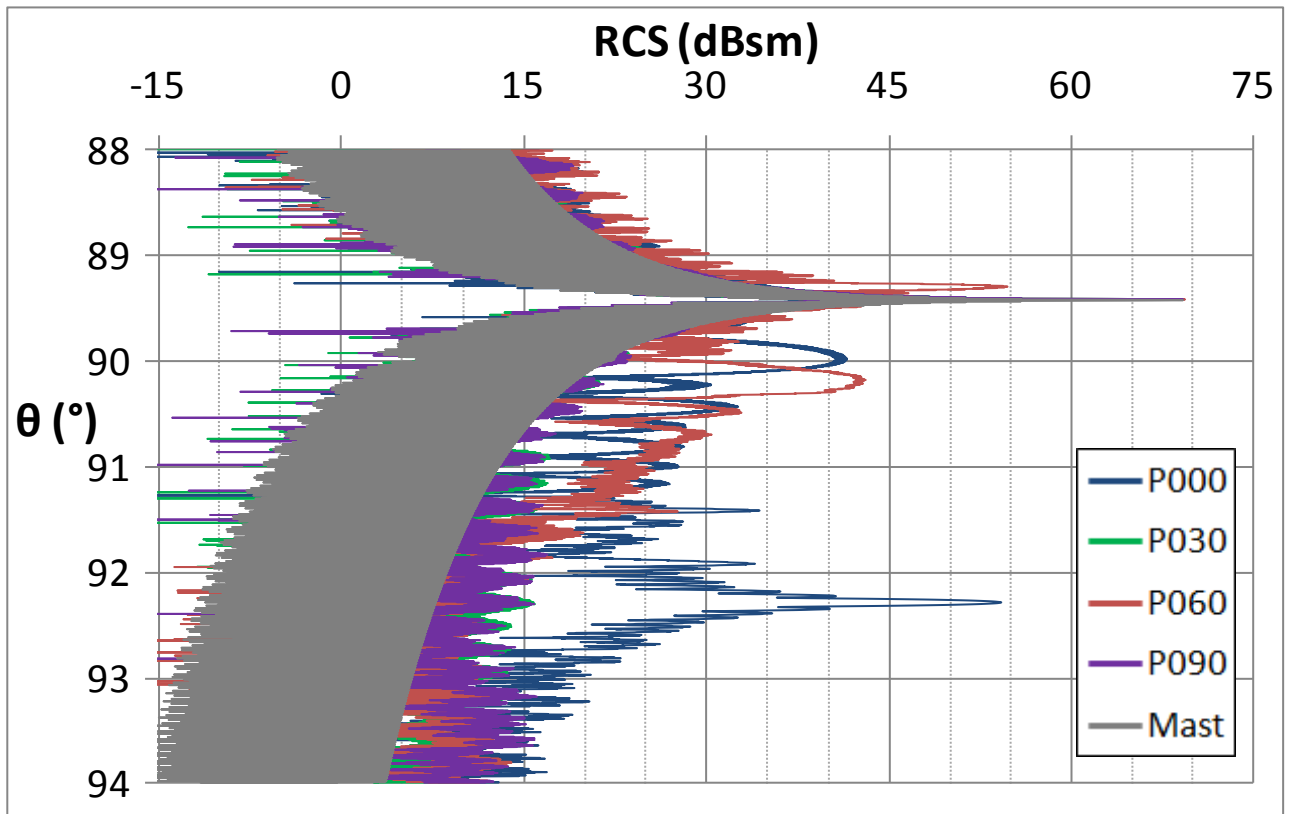
4



1

2 Figure 4. Vertical sections of RCS patterns ( $\Phi = 5^\circ$ ) for wind turbine models 1 to 3 at  
 3 frequency 9.40 GHz. Rotor position is indicated in the lowest right corner.

4

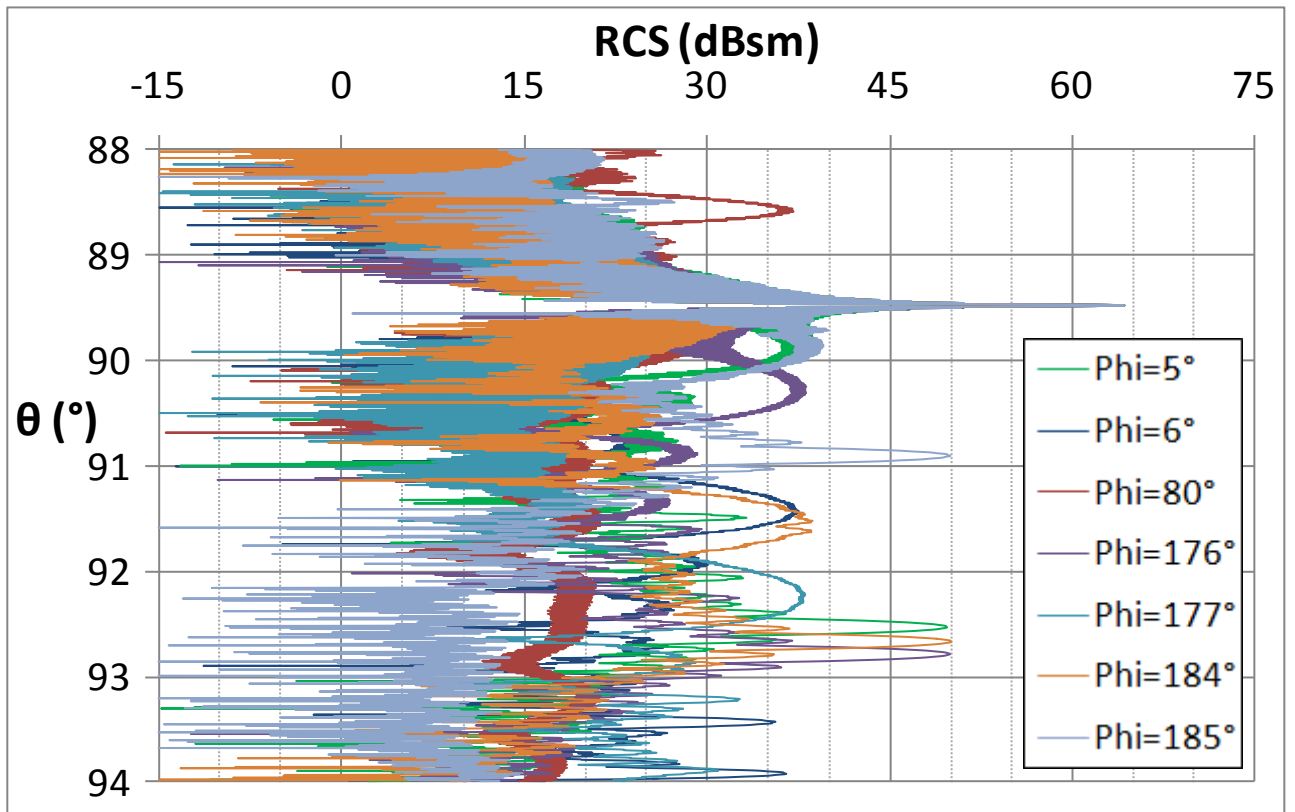


1

2 Figure 5. Vertical sections of RCS patterns ( $\Phi = 5^\circ$ ) for wind turbine model 3 at frequency  
 3 9.40 GHz. Legend entries starting with PXXX indicate the position of the upper blade (being  
 4 P000 vertical right position and P090 horizontal position).

5

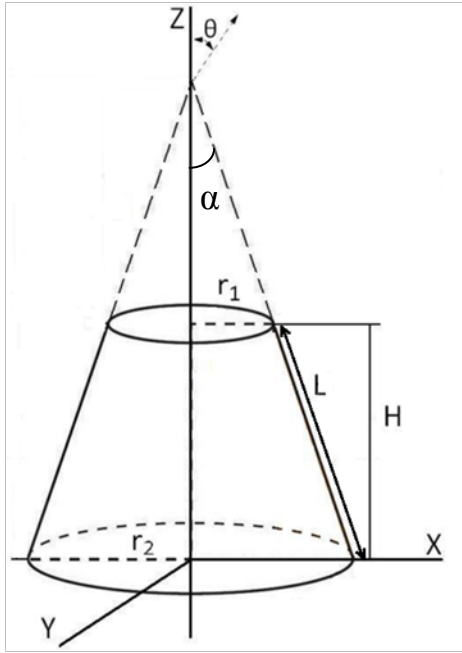




1

2 Figure 6. Vertical sections of RCS patterns ( $\Phi = 5^\circ, 6^\circ, 80^\circ, 176^\circ, 177^\circ, 184^\circ, 185^\circ$ ) for wind  
 3 turbine model 2 at frequency 5.65 GHz and rotor position P000.

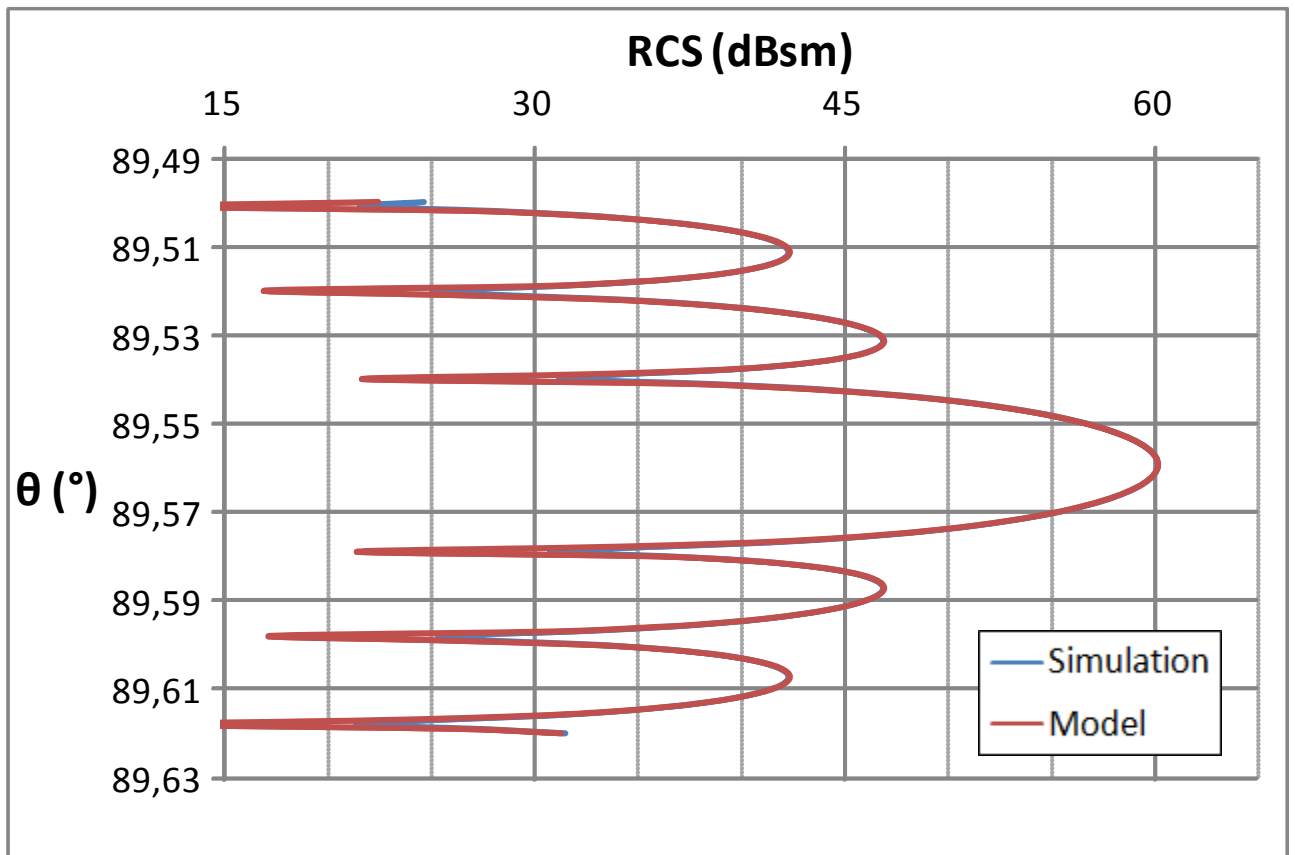
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1

2 Figure 7. Geometry for the RCS calculation of the mast

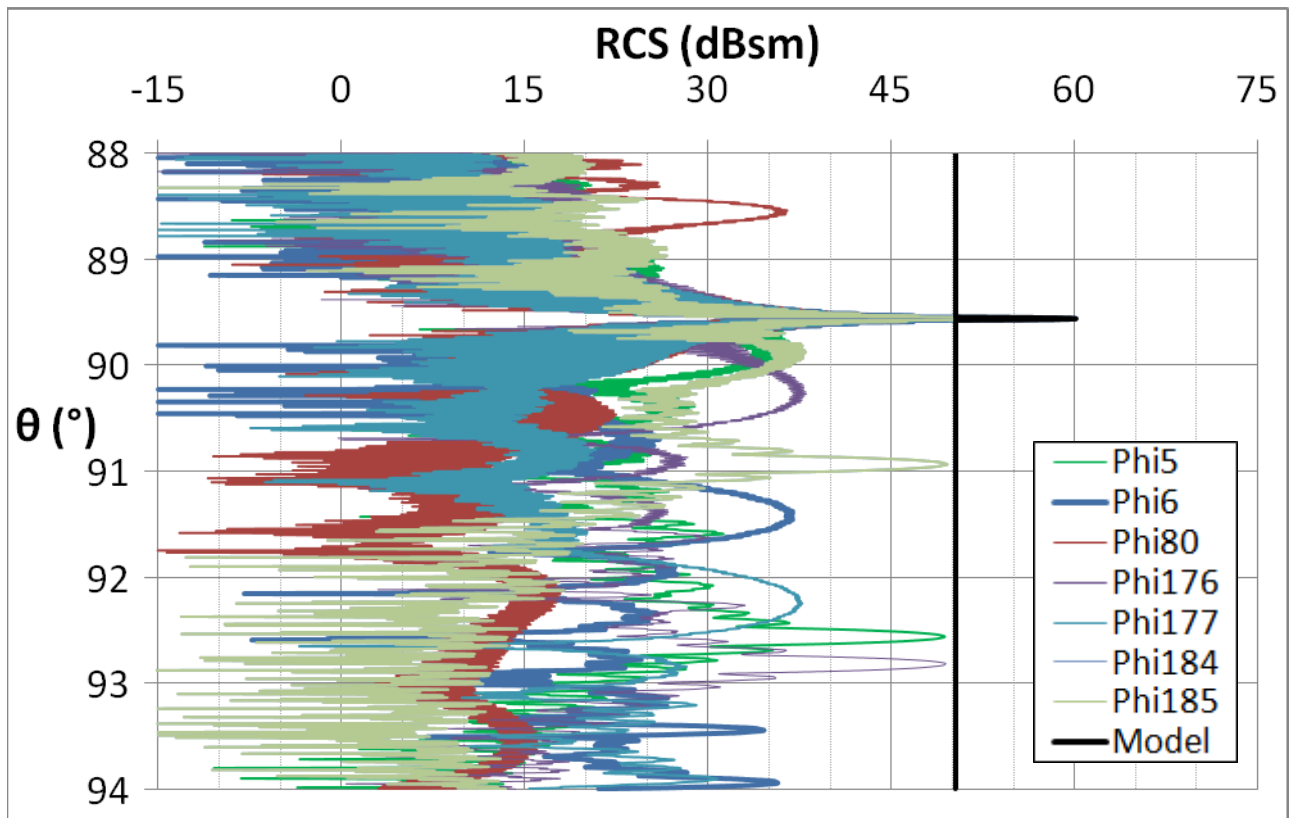
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1

2 Figure 8. RCS pattern obtained by simulation vs RCS values obtained by the proposed  
 3 simplified model for the mast of wind turbine model 1 and frequency 5.65 GHz.

4



1

2 Figure 9. Vertical sections of RCS patterns ( $\Phi = 5^\circ, 6^\circ, 80^\circ, 176^\circ, 177^\circ, 184^\circ, 185^\circ$ ) for wind  
 3 turbine model 1 (Frequency 5.65 GHz, Rotor position P000) and result of the proposed model  
 4 (black line).