

# Approaches to radar reflectivity bias correction to improve rainfall estimation in Korea

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## Abstract

Three methods for determining the reflectivity bias of single polarization radar using dual polarization radar reflectivity and disdrometer data (i.e., the equidistance line, overlapping area, and disdrometer methods) are proposed and evaluated for two low-pressure rainfall events that occurred over the Korean Peninsula on 25 August 2014 and 8 September 2012. Single polarization radar reflectivity was underestimated by more than 12 dB and 7 dB in the two rain events, respectively. All methods improved the accuracy of rainfall estimation, except for one case where DSDs were not observed, as the precipitation system did not pass through the disdrometer location. The use of these bias correction methods reduced the RMSE by as much as 50%. Overall, the most accurate rainfall estimates were obtained using the overlapping area method to correct radar reflectivity.

## 1 Introduction

Radar is a useful remote sensing instrument for measuring rainfall amount, due to its relatively high resolution in both space and time. Areal rainfall rate is not measured directly, but must be derived from radar reflectivity. This estimation of radar rainfall is based on the relationship between reflectivity ( $Z$ ) and rainfall rate ( $R$ ), known as the  $Z$ - $R$  relation ( $R(Z)$ ). Experimentally measured drop size distributions (DSDs) have been used extensively to obtain both radar reflectivity and rainfall rate (Compos and Zawadzki, 2000; Jang et al., 2004; You et al., 2004).

1 There is no unique  $R(Z)$ , since DSDs can be varied storm to storm and even within a single  
2 storm (Battan 1973; You et al., 2010).

3 However, radar rainfall estimation is complicated by a number of uncertainties including  
4 hardware calibration, partial beam filling, rain attenuation, brightband, and non-weather echoes  
5 (Wilson and Brandes, 1979; Austin, 1987). The correction of bias in  $Z$  caused by hardware  
6 calibration error is difficult to achieve using single polarimetric radar (SPOL) alone.  
7 Polarimetric radar (DPOL) provides a new method for the absolute calibration of reflectivity,  
8 which has been a longstanding problem with single polarization radar data. The method is based  
9 on the assumptions that  $Z$ , differential reflectivity ( $Z_{DR}$ ), and specific differential phase ( $K_{DP}$ )  
10 are independent of each other, and that  $Z$  can be estimated from  $Z_{DR}$  and  $K_{DP}$ , which are  
11 insensitive to radar miscalibration (Gorgucci et al., 1992, 1999; Goddard et al., 1994; Scarchilli  
12 et al., 1996; Vivekanandan et al., 1999).

13 The Korea Meteorological Administration (KMA) is in the process of replacing Doppler radars  
14 with S-band DPOLs (to be completed by 2019), and Ministry of Land, Infrastructure and  
15 Transport (MoLIT) has installed four S-band DPOLs for operational use since 2009. Until the  
16 DPOL installation is complete, it is necessary to use a combination of SPOLs and DPOLs to  
17 produce rainfall mosaics covering the whole Korean Peninsula. To obtain more accurate  
18 mosaicked radar rainfall, SPOL reflectivity should be corrected using the reflectivity of DPOLs  
19 and other instruments such as disdrometer. Accurate SPOL reflectivity is also required for  
20 climatological analysis using radar rainfall.

21 This paper discusses three methods for reducing errors in SPOL reflectivity using DPOL and  
22 DSD measurements. In Section 2, the dataset used for the analysis is introduced, and three  
23 approaches to correcting SPOL reflectivity are described, along with methods for bias  
24 correction of DPOL reflectivity and  $Z_{DR}$ , and for validation. In Section 3, the results obtained  
25 using the three correction methods are compared with gauge measurements. Finally, we  
26 summarize the results and provide conclusions in Section 4.

27

## 28 **2 Data**

29 Rainfall data from rain gauges operated by the KMA were used to evaluate the accuracy of  
30 radar rainfall. Rain gauges located between 5 and 134 km from the radar were included in the  
31 analysis. Figure 1 shows the location of all instruments used in this study. The PARSIVEL

1 (PARticle SIZE VELOCITY) disdrometer was installed ~9 km from PSN. PARSIVEL is a laser-  
2 optic system that measures 32 channels from 0.062 to 24.5 mm (for detailed specifications, see  
3 Loffler-Mang and Joss, 2000).

4 Data observed from PARSIVEL were regarded as unreliable and removed from the analysis in  
5 the case that any of the following conditions were met: 1 min rain rate was less than  $0.1 \text{ mm h}^{-1}$ ;  
6 total number concentration from all channels was less than 10; drop numbers were recorded  
7 only in the lower 10 channels (1.187 mm for PARSIVEL); or drop numbers were recorded only  
8 in the lower 5 channels (0.562 mm for PARSIVEL) (You et al., 2015).

9 Radar data were recorded at PSN (Pusan radar) is located at coastal line and BSL (Bisalsan  
10 radar) is located 76.9 km away from PSN (Fig. 1), which were installed and are operated by  
11 KMA and MoLIT, respectively. The transmitted peak power of BSL is 750 kW, the beam width  
12 is  $0.95^\circ$ , the frequency is 2.791 GHz, and the antenna is 1085 m above sea level. The  
13 polarimetric variables are estimated with a gate size of 0.125 km. The scan strategy consists of  
14 six elevation angles with a 2.5 min update interval. The transmitted peak power of PSN is 800  
15 kW, the beam width is 1.0 degrees, the frequency is 2.712 GHz and the antenna is 547 m above  
16 sea level. The reflectivity is estimated with a gate size of 0.25 km. The PSN scan strategy  
17 consists of 13 elevation angles with a 10 min update interval. Radar variables at an elevation  
18 angle of 0.5 (1.8) degrees were extracted from the BSL (PSN) data every 10 mins, to match the  
19 time interval for this study. Non-meteorological targets were removed from the PSN data using  
20 the texture and vertical gradient of reflectivity, as proposed by Zhang et al. (2004). Polarimetric  
21 variables were subjected to quality control using a threshold of 15 degrees for the standard  
22 deviation of the differential phase shift (You et al., 2014).

23 The quality controlled  $Z_H$ ,  $Z_{DR}$ ,  $K_{DP}$  measured from BSL were used to calibrate  $Z_{DR}$  and  $Z_H$  of  
24 BSL. The  $Z_H$  measured from PSN were then corrected by using calibrated  $Z_H$  of BSL using  
25 self-consistency method and  $Z_H$  measured by PARSIVEL. The gage rainfall data were used to  
26 assess the performance of three  $Z_H$  bias correction methods for PSN which is SPOL.

27 The accuracy of rainfall estimation using corrected reflectivity was evaluated to measure the  
28 effectiveness of each method for calculating the difference reflectivity between PSN and BSL  
29 (PARSIVEL). Two rainfall events were used, occurring on 25 August 2014 and 8 September  
30 2012 (Table 1). The August and September events were caused by low pressure systems over  
31 southern and northern Korea, respectively.

1 Figure 2 shows the time series of  $Z_H$  observed from BSL radar on 8 September in 2012 and 25  
2 August in 2014. The precipitation within radar coverage on 8 September in 2012 was occurred  
3 by low pressure with the front located at northern part of Korea. The core of the precipitation  
4 systems was elongated from south to north and moved to eastward. The maximum reflectivity  
5 of the core was more than 45 dBZ and caused rainfall at the western part of radar center at 0300  
6 LST (Fig. 2(a)), became more organized shape at the eastern part of radar center at 0400 LST  
7 (Fig. 2(c)), and moved to eastward and located out of land at 0500 LST (Fig. 2(e)) on 8  
8 September in 2012. The precipitation system on 25 August in 2014 was caused by the low  
9 pressure located at southern part of Korea. The two strong rainfall within the radar coverage  
10 were located at south-western part of radar center with distance between 120 km and 150 km  
11 and southern part of radar center with distance between 30 km and 90 km, respectively at 1200  
12 LST on 25 August in 2014 (Fig. 2(b)). The two convective cells moved to eastward, their  
13 strength were intensified and the area of rainfall was wider at 1300 LST (Fig. 2(d)). The two  
14 systems moved to eastward continuously, were merged together at 1400 LST (Fig. 2(f)).

15 Figure 3 shows the time series of hourly rainfall and daily accumulation measured by a gage  
16 which recorded highest daily rainfall within radar coverage on 8 September in 2012 and 25  
17 August in 2014. The highest daily accumulated rainfall was recorded from North Changwon  
18 (ID 255) and Geumjeong (ID 939) on each day, respectively. The daily accumulation of ID 255  
19 was 150 mm, the maximum hourly rainfall was around 40 mm, and the duration of the rainfall  
20 was 7 hours (Fig. 3(a)). The daily accumulation of ID 939 was around 270 mm, the maximum  
21 hourly rainfall was more than 100 mm h<sup>-1</sup>. The rainfall amount for 3 hours (1000 LST, 1400  
22 LST, and 1500 LST) were mainly contributed to the total rainfall accumulation on 25 August  
23 in 2014 (Fig. 3(b)).

## 24 **3 Methodology**

### 25 **3.1 Z and Z<sub>DR</sub> bias correction for BSL**

26 Before calculating reflectivity bias for PSN using BSL,  $Z_H$  and  $Z_{DR}$  must be corrected for bias.  
27  $Z_{DR}$  bias correction is important for the absolute calibration of the radar using a self-consistency  
28 method. Gorgucci et al. (1999) proposed using a vertical pointing scan of light rain, to take  
29 advantage of the nearly spherical shape of the raindrops as seen from below. Ryzhkov et al  
30 (2005) used the elevation angle dependency of  $Z_{DR}$  as an alternative technique and concluded  
31 that the high variability of  $Z_{DR}$  in rainfall prohibited the method from achieving the required

1 absolute calibration accuracy of 0.2 dB. They instead proposed a method that utilizes the  
 2 structural characteristics of the melting layer in stratiform clouds and the dry aggregated snow  
 3 present above the melting layer.  $Z_{DR}$  measurements from dry aggregated snow above the  
 4 melting layer resulted in a mean S-band value of 0.2 dB and an accuracy of 0.1–0.2 dB. Trabal  
 5 et al. (2009) evaluated two methods using the intrinsic properties of dry aggregated snow  
 6 present above the melting layer and light rain measurements close to the ground, and found that  
 7 a  $Z_{DR}$  calibration accuracy of 0.2 dB or better was achieved using either method.

8 Vertical pointing data were not available in the present case, and the scan strategy, with six  
 9 elevation angles, was unable to detect the melting layer. Therefore, in this study, light rain  
 10 measurements close to the ground were used to calibrate  $Z_{DR}$ . Light rain was defined using a  
 11 threshold of  $20 \text{ dBZ} \leq Z \leq 28 \text{ dBZ}$ , as proposed by Marks et al. (2011). The assumption of  $Z_{DR}$   
 12 is close to zero in case of the small rain drop like drizzle was chosen for this study. The  $Z_{DR}$   
 13 observed from BSL having with reflectivity in the range of 20 dBZ to 28 dBZ for given time  
 14 period were averaged. Then the averaged  $Z_{DR}$  was taken as a  $Z_{DR}$  bias.

15 The  $Z_H$  bias was calculated by self-consistency method using a 9-gate moving average of bias  
 16 corrected  $Z_{DR}$  in the range of 0.2 dB to 3.0 dB to improve the accuracy. This method depends  
 17 on the notion that  $Z_H$ ,  $Z_{DR}$ , and  $K_{DP}$  are independent in rain, and that  $Z_H$  can be estimated from  
 18  $Z_{DR}$  and  $K_{DP}$ . The difference between the computed and observed values of  $Z_H$  is referred to as  
 19 the  $Z$  bias. Following the method of Ryzhkov et al. (2005), the entire spatial and temporal  
 20 domain was divided into 1 dB intervals of  $Z_H$  between  $Z_{min}$  (30 dBZ) and  $Z_{max}$  (50 dBZ), and  
 21 the  $K_{DP}(Z_H)$  and  $Z_{DR}(Z_H)$  within each interval were calculated. The  $Z_H$  bias is then determined  
 22 by matching the integrals:

$$23 \quad I_1 = \sum_{Z_{min}}^{Z_{max}} K_{DP}(Z) n(Z) \Delta Z, \quad (1)$$

$$24 \quad I_2 = \sum_{Z_{min}}^{Z_{max}} 10^{0.1Z_m} f(Z_{DR}) n(Z) \Delta Z, \quad (2)$$

25 The function of  $f(Z_{DR})$  in Eq. (2) can be well approximated by a fourth-order polynomial fit for  
 26 certain range of  $Z_{DR}$  (Gourley et al., 2009) like Eq. (3).

$$27 \quad f(Z_{DR}) = 10^{-5} (a_0 + a_1 Z_{DR} + a_2 Z_{DR}^2 + a_3 Z_{DR}^3), \quad (3)$$

28 The estimated  $Z_H$  bias is determined from Vivekanandan et al. (2003) by

$$1 \quad Z_H \text{bias}(dB) = 10 \log\left(\frac{I_2}{I_1}\right), \quad (4)$$

2 If the radar is well calibrated,  $Z_H$  bias should be equal to 0. The coefficients of  $f(Z_{DR})$  were  
 3 calculated by T-matrix scattering method using long period DSD data and are 4.26, -4.67, 2.67,  
 4 and -0.54, respectively.

### 5 **3.2 Equidistance line method**

6 To calculate the reflectivity bias of PSN, which is single polarization radar, three approaches  
 7 were used: the equidistance line method, the overlapping area method, and the disdrometer  
 8 method. The first approach is to compare the reflectivities along the line that is equidistant  
 9 between the two radars. To determine this line for the two radars, the effective radius was set  
 10 to 100 km and the distance between the two radars and the azimuthal angle pointing from BSL  
 11 to PSN were calculated using their latitude and longitude values. The start and end azimuthal  
 12 angles for comparison of reflectivity were then calculated as follows:

$$13 \quad AZ_{st} = \beta - a \cos(0.5 \times dr / rc) \quad (5)$$

$$14 \quad AZ_{end} = \beta - a \cos(0.5 \times dr / rc) + 2 \times a \cos(0.5 \times dr / rc), \quad (6)$$

15 where  $AZ_{st}$  and  $AZ_{end}$  are the start and end azimuthal angles for the comparison, respectively;  $\beta$   
 16 is an azimuthal angle which is the angle between north and the bearing from BSL points to  
 17 PSN and  $rc$  and  $dr$  are the effective radius and distance from BSL to PSN, respectively. The  
 18 distance between the two radars is 76.9 km, and the start and end azimuthal angles of BSL (PSN)  
 19 are 79 (35) and 213 (261) degrees, respectively (Fig. 4).

20 To compare the reflectivity observed of targets at the almost same height from both radars, the  
 21 beam height was calculated assuming a standard atmospheric beam propagation (Rinehart,  
 22 2010), as follows:

$$23 \quad H = \sqrt{r^2 + (R' + H_0)^2 + 2r(R' + H_0) \sin \phi} - R', \quad (7)$$

24 where  $r$  is the slant range from the radar,  $\phi$  is the elevation angle of the radar beam,  $H_0$  is the  
 25 height of the radar antenna above sea level, and  $R' = (4/3)R$ , where  $R$  is the Earth's radius  
 26 (6,371 km). The radar antenna heights of PSN and BSL are 547 and 1085 m, respectively.  
 27 Figure 5 shows the beam height of PSN with blue solid line and BSL at the equidistance line

1 (blue dashed line as shown in Fig. 4). EL1 to EL6 show the elevation angles from smallest to  
2 largest. The smallest difference in beam height between the two radars is 149 m, which was  
3 obtained using the fourth elevation angle of PSN and the third elevation angle of BSL.  
4 Therefore, the reflectivity bias of PSN was calculated by averaging the difference of reflectivity  
5 along with the equidistance line observed from fourth elevation angle of PSN and third one of  
6 BSL.

### 7 **3.3 Overlapping area method**

8 In the second approach, the overlapping area for the two radars was calculated by matching the  
9 coordinates. The polar coordinate of two radars was converted to a Cartesian coordinate with a  
10 spatial resolution of 1 km. The overlapping area was then determined by considering the  
11 distances between the two radars in the east–west and north–south directions. Figure 6 shows a  
12 schematic diagram of the overlapping area for the two radars. The distance between two radars  
13 in east-west and north-south direction are 42 km and 64 km, respectively. The reflectivity  
14 observed from both radars at the pixels designated at the overlapping area as shown by blue  
15 rectangle in right panel of Fig. 6 were compared to calculate the  $Z_H$  bias of PSN. The extracted  
16 domain of PSN and BSL for the comparison is  $158 \times 136$  km.

### 17 **3.4 Disdrometer method**

18 The third and final approach is to use DSD observations from the PARSIVEL disdrometer. The  
19 reflectivity was calculated from the DSD at 1 min resolution, and averaged over 10 mins to  
20 match the radar time resolution. Figure 7 shows a schematic of the procedure used to match the  
21 radar and PARSIVEL data. The PARSIVEL disdrometer is located ~9 km from the radar, at an  
22 azimuthal angle of 87 degrees. The radar reflectivity was averaged over a domain of 13 gates  
23  $\times$  3 degrees in azimuth, centered at the PARSIVEL location. The reflectivity observed by BSL  
24 or PARSIVEL subtracted from that observed by PSN was taken as a  $Z_H$  bias and it will be  
25 applied to all pixels of PSN coverage.

### 26 **3.5 Validation**

27 The normalized error (NE), root-mean-square error (RMSE), and correlation coefficient (CC)  
28 between rainfall estimates and measurements from 121 gauges were calculated to measure the  
29 performance of each bias correction method. The rain gages were 0.5 mm tipping-bucket type.

1 Time resolution of gages is 1 min and data quality control was done by KMA. These quantities  
 2 are defined as follows:

$$3 \quad NE = \frac{\frac{1}{N} \sum_{i=1}^N |R_{R,i} - R_{G,i}|}{\overline{R_G}} \quad (8)$$

$$4 \quad RMSE = \left[ \frac{1}{N} \sum_{i=1}^N (R_{R,i} - R_{G,i})^2 \right]^{1/2} \quad (9)$$

$$5 \quad CC = \frac{\sum_{i=1}^N (R_{R,i} - \overline{R_R})(R_{G,i} - \overline{R_G})}{\left[ \sum_{i=1}^N (R_{R,i} - \overline{R_R})^2 \right]^{1/2} \left[ \sum_{i=1}^N (R_{G,i} - \overline{R_G})^2 \right]^{1/2}}, \quad (10)$$

6 where N is the number of radar rainfall ( $R_R$ ) and gauge rainfall ( $R_G$ ) pairs, and  $\overline{R_R}$  and  $\overline{R_G}$  are  
 7 the average hourly rain rates from radar and gauges, respectively. These quantities were  
 8 calculated using total accumulated rainfall amounts for analyzed time period from radar and  
 9 gauge measurements at each point. The radar rainfall value at each point was obtained by  
 10 averaging rainfall over a small area ( $1 \text{ km} \times 1^\circ$ ) centered on the corresponding rain gauge. The  
 11 radar rainfall was calculated using the relation  $Z = 200 R^{1.6}$  and  $Z = 300 R^{1.4}$ .

12

## 13 **4 Results**

### 14 **4.1 Equidistance line method**

15 Before estimating radar rainfall rates, reflectivity biases were calculated using each of the three  
 16 methods. Figure 8 shows time series of the average reflectivity difference between PSN and  
 17 BSL at the equidistance line and the number of samples used in each calculation, on 25 August  
 18 2014. The average difference over the entire time period was  $-7.85 \text{ dB}$ , and the largest  
 19 difference was  $-12.46 \text{ dB}$ . It means that the reflectivity observed by PSN was underestimated  
 20 comparing with BSL. The number of samples used for each calculation was determined using  
 21 a beam height difference threshold of  $0.1 \text{ km}$ . The number of samples was generally above 60,  
 22 but it was smaller than 60 after 1450 LST. The dominant peak of the averaged reflectivity  
 23 difference occurred from 1500 LST would be caused by the decreased sample number for the



1 comparison of reflectivity observed from both radars. Figure 9 shows the same information for  
2 8 September 2012. The average reflectivity difference over the entire time period was  $-2.56$   
3 dB, and the largest difference was  $-6.77$  dB. The number of samples was less than 50 until 0310  
4 LST, after which it increased to more than 50. This result suggests that the rainfall observed  
5 from both BSL and PSN radar was not located enough over the equidistance line to get a reliable  
6 comparison until 0310 LST.

7 Figure 10 shows the scatter plot of total accumulated radar rainfall amount for analyzed time  
8 period, calculated using  $Z = 200R^{1.6}$  and  $Z=300R^{1.4}$  and gauge rainfall, for 25 August 2014 and  
9 8 September 2012. The RMSE, NE, and CC of rainfall pairs for  $Z = 200R^{1.6}$  ( $Z=300R^{1.4}$ ) on 25  
10 August 2014 were improved from 65.7 (66.1) to 32.6 (27.0) mm, from 0.79 (0.81) to 0.36 (0.31),  
11 and from 0.88 (0.87) to 0.89 (0.88), respectively. On 8 September 2012, the RMSE, NE, and  
12 CC for  $Z = 200R^{1.6}$  ( $Z=300R^{1.4}$ ) changed from 30.0 (28.5) to 22.5 (20.0) mm, from 0.58 (0.56)  
13 to 0.41 (0.36), and from 0.81 (0.8) to 0.78 (0.76), respectively, by the use of bias correction. In  
14 both cases, the use of corrected reflectivity for rainfall estimation resulted in much better  
15 accuracy than did using raw reflectivity.

## 16 **4.2 Overlapping area method**

17 Figure 11 shows time series of the mean reflectivity differences between PSN and BSL in the  
18 overlapping area, and the number of samples used for calculation of  $Z_H$  bias on 25 August 2014.  
19 Bias values ranged from  $-11.7$  to  $-8.3$  dB over the period analyzed. The bias was stable until  
20 1440 LST, after which it fluctuated as the number of samples decreased. Figure 12 shows the  
21 same information for 8 September 2012. Bias values ranged from  $-4.66$  to  $0.22$  dB, and lower  
22 bias values were occurred from 0300 LST to 0400 LST. The fluctuation also would be caused  
23 by the sudden change of microphysical characteristics of rainfall pass through the overlapping  
24 area for both radars. It would reduce the accuracy of  $Z_H$  of BSL corrected by self-consistency.  
25 The radar rainfall estimation was done by using observed and corrected  $Z_H$  as an input of Z-R  
26 relations.

27 Figure 13 shows a scatter plot of total accumulated radar rainfall amount for entire analyzed  
28 time period, calculated using  $Z = 200 R^{1.6}$  and  $Z=300R^{1.4}$  and gauge rainfall, for 25 August  
29 2014 and 8 September 2012. The RMSE and NE of rainfall pairs for  $Z = 200R^{1.6}$  ( $Z=300R^{1.4}$ )  
30 on 25 August 2014 were improved from 65.7 (66.1) to 29.7 (25.8) mm and from 0.79 (0.81) to  
31 0.31 (0.28), respectively. On 8 September 2012, RMSE and NE for  $Z = 200R^{1.6}$  ( $Z=300R^{1.4}$ )

1 were improved from 30.0 (28.5) to 21.8 (19.1) mm and from 0.58 (0.56) to 0.40 (0.34),  
2 respectively, by the use of bias correction, while CC for  $Z=200R^{1.6}$  was unchanged at 0.81 and  
3 that of  $Z=300R^{1.4}$  were changed 0.8 to 0.79. Again, in both cases the use of corrected reflectivity  
4 for rainfall estimation was found to improve the accuracy compared with raw reflectivity.

### 5 **4.3 Disdrometer method**

6 Before using the disdrometer bias correction method to estimate rainfall rates, 10 min rain rates  
7 obtained directly from DSDs and from collocated gauges were compared. Figure 14 shows the  
8 time series of rain rate obtained by PARSIVEL and collocated gauges on 25 August 2014. Daily  
9 total rainfall amounts for PARSIVEL and the gauges were 129.4 and 116.0 mm, respectively.  
10 The difference in the totals is only 13.4 mm, and the RMSE and CC between the 10 min time  
11 series were  $0.52 \text{ mm h}^{-1}$  and 0.99, respectively. On 8 September 2012 (not shown), daily total  
12 rainfall amounts for PARSIVEL and the gauge were 54.4 and 55.0 mm, respectively. The  
13 difference between the total daily rainfall amounts was 0.7 mm and the RMSE and CC between  
14 the two 10 min series were  $0.62 \text{ mm h}^{-1}$  and 0.96, respectively. It is concluded that DSDs were  
15 sufficiently reliable to use as a reference with which to calculate the radar bias.

16 Figure 15 shows time series of reflectivity obtained by radar and by PARSIVEL, and the radar  
17 bias, on 25 August 2014. The bias was more stable before 1200 LST than after 1500 LST.  
18 PARSIVEL reflectivity fell to zero from 1230 to 1340 LST because the precipitation system  
19 moved away from the PARSIVEL site. The sudden change of rainfall would cause the unstable  
20 reflectivity difference from 1340 LST to 1500 LST. The threshold of reflectivity value observed  
21 from both PSN and PARSIVEL should be considered for the comparison to get more reliable  
22  $Z_H$  bias. The bias would be obtained more accurately when the reflectivity values observed from  
23 both instruments were higher than 15 dBZ in this event. Because of this discontinuity, the bias  
24 can be considered to be reliable only until 1200 LST. The bias values ranged from -13.4 to -3.1  
25 dB until 1200 LST. Figure 16 shows time series of reflectivity obtained by radar and by  
26 PARSIVEL, and the radar bias on 8 September 2012. On this occasion there was no reflectivity  
27 data from either PARSIVEL or radar until 0330 LST. The bias values were distributed from -  
28 14.3 to 12.7dB.

29 Figure 17 shows a scatter plot of total accumulated radar rainfall amount for the entire time  
30 period, calculated using  $Z = 200R^{1.6}$  and  $Z=300R^{1.4}$  and gauge rainfall, on 25 August 2014 and  
31 8 September 2012. The RMSE and NE of rainfall pairs for  $Z = 200R^{1.6}$  ( $Z=300R^{1.4}$ ) on 25

1 August 2014 were improved from 65.7 (66.1) mm to 42.0 (61.4) mm and from 0.79 (0.81) to  
2 0.40 (0.53), respectively. On 8 September 2012, RMSE and NE for  $Z = 200R^{1.6}$  ( $Z=300R^{1.4}$ )  
3 decreased from 30.1 (28.6) to 24.6 (23.9) mm, and from 0.58 (0.56) to 0.46 (0.44), respectively,  
4 while CC for  $Z = 200R^{1.6}$  ( $Z=300R^{1.4}$ ) decreased from 0.81 (0.8) to 0.65 (0.59). In both cases,  
5 using corrected rather than raw reflectivity for rainfall estimation improved accuracy as  
6 measured by RMSE and NE, but reduced accuracy as measured by CC.

#### 7 **4.4 Discussion**

8 Figure 18 shows RMSE of total rainfall amount for entire time period obtained by gage and  
9  $Z=200R^{1.6}$  from each of the different bias correction methods on 25 August 2014 and 8  
10 September 2012. Red, black, green, and blue bars show the RMSE obtained using the  
11 uncorrected, equidistance line, overlapping area, and disdrometer methods, respectively. The  
12 disdrometer method produced the lowest RMSE before 1200 LST and the highest RMSE after  
13 1200 LST (Fig. 18(a)). This behavior can be attributed to the varying stability of the reflectivity  
14 calculated by PARSIVEL (Fig. 15). The overlapping method is more accurate than the  
15 equidistance line method for the entire time period, except at 1400 LST. All the bias correction  
16 methods performed better than the uncorrected method, except for the period during which  
17 DSDs were unavailable. On 8 September 2012, the RMSE of the overlapping area method was  
18 lower than that of the other methods for the entire period, except at 0500 and 0600 LST (Fig.  
19 18(b)). The disdrometer method produced lower RMSE at 0600 LST, when DSDs were  
20 available, and the equidistance line method was more accurate at 0500 LST, when the sample  
21 number was high (Fig. 15). Comparing the RMSE between two events, the large fluctuation  
22 was occurred. It would be caused by the difference of total rainfall amount between two rainfall  
23 systems. The maximum total rainfall amount for both cases were around 250 mm for 25 August  
24 and 150 mm for 8 September 2012. Another reason of the fluctuation would be the difference  
25 of radar hardware calibration error for PSN between two events.

26 Considering the entire period covering both events, the overlapping area method showed the  
27 best performance, as measured by RMSE. The accuracy of radar rainfall estimates could be  
28 improved by combining the three approaches, using metrics such as DSD temporal stability and  
29 the number of samples available for the equidistance line method to select the best method for  
30 a particular situation. It is worth to noting that the result would be changed when the drop size  
31 distributions was fluctuated with height especially at the layer between radar beam and ground  
32 in case of disdrometer method.

## 1 5 Conclusions

2 Three methods for determining the reflectivity bias of single polarization radar using dual  
3 polarization radar reflectivity and disdrometer data were proposed and examined for two  
4 rainfall events caused by low pressure over the Korean Peninsula on 25 August 2014 and 8  
5 September 2012. Single polarization radar reflectivity was underestimated by more than 12 dB  
6 and 7 dB during the August and September events, respectively. All three methods improved  
7 the accuracy of estimated rainfall, except during a period when DSDs were not observed (as  
8 the precipitation system did not pass over the disdrometer location).

9 The rainfall estimation using  $Z = 200R^{1.6}$  and  $Z=300R^{1.4}$  and gauge rainfall were examined for  
10 25 August 2014 and 8 September 2012 to investigate the accuracy of each method. The RMSE,  
11 NE, and CC of rainfall pairs for  $Z = 200R^{1.6}$  ( $Z=300R^{1.4}$ ) on 25 August 2014 in case of using  
12 equidistance method were improved from 65.7 (66.1) to 32.6 (27.0) mm, from 0.79 (0.81) to  
13 0.36 (0.31), and from 0.88 (0.87) to 0.89 (0.88), respectively. On 8 September 2012, the RMSE,  
14 NE, and CC for  $Z = 200R^{1.6}$  ( $Z=300R^{1.4}$ ) changed from 30.0 (28.5) to 22.5 (20.0) mm, from  
15 0.58 (0.56) to 0.41 (0.36), and from 0.81 (0.8) to 0.78 (0.76), respectively.

16 The RMSE and NE of rainfall pairs for  $Z = 200R^{1.6}$  ( $Z=300R^{1.4}$ ) on 25 August 2014 in case of  
17 using overlapping method were improved from 65.7 (66.1) to 29.7 (25.8) mm and from 0.79  
18 (0.81) to 0.31 (0.28), respectively. On 8 September 2012, RMSE and NE for  $Z = 200R^{1.6}$   
19 ( $Z=300R^{1.4}$ ) were improved from 30.0 (28.5) to 21.8 (19.1) mm and from 0.58 (0.56) to 0.40  
20 (0.34), respectively, by the use of bias correction, while CC for  $Z=200R^{1.6}$  was unchanged at  
21 0.81 and that of  $Z=300R^{1.4}$  were changed 0.8 to 0.79.

22 The RMSE and NE of rainfall pairs for  $Z = 200R^{1.6}$  ( $Z=300R^{1.4}$ ) on 25 August 2014 in case of  
23 using disdrometer method were improved from 65.7 (66.1) mm to 42.0 (61.4) mm and from  
24 0.79 (0.81) to 0.40 (0.53), respectively. On 8 September 2012, RMSE and NE for  $Z = 200R^{1.6}$   
25 ( $Z=300R^{1.4}$ ) decreased from 30.1 (28.6) to 24.6 (23.9) mm, and from 0.58 (0.56) to 0.46 (0.44),  
26 respectively, while CC for  $Z = 200 R^{1.6}$  ( $Z=300R^{1.4}$ ) decreased from 0.81 (0.8) to 0.65 (0.59).

27 The use of these bias correction methods reduced rainfall RMSE by up to 50%. Overall, the  
28 accuracy of rainfall estimation was highest when the overlapping area method was used to  
29 correct radar reflectivity.

30 The reflectivity biases obtained using the disdrometer and equidistance line methods were more  
31 temporally variable than those obtained using the overlapping area method. There were several

1 hours during which the disdrometer method was more accurate than the overlapping area  
2 method. We suggest that combining the overlapping area method with the disdrometer method,  
3 using threshold criteria such as the temporal stability of reflectivity and the number of samples  
4 available would allow more accurate estimates of rainfall. However, optimum values for the  
5 domain size for the overlapping area method, the sample number threshold for the equidistance  
6 line method, and the reflectivity threshold for the disdrometer method should be determined in  
7 order to combine the three methods most effectively.

8

9

## 10 **Acknowledgements**

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12 and the Korean Meteorological Administration for providing radar data and AWS (Automatic  
13 Weather System) gauge data. This research was funded by the Korea Meteorological Industry  
14 Promotion Agency under Grant KMIPA 2015-1050. And this research was partly funded by  
15 the Korea Meteorological Industry Promotion Agency under Grant KMIPA 2015-1060

16

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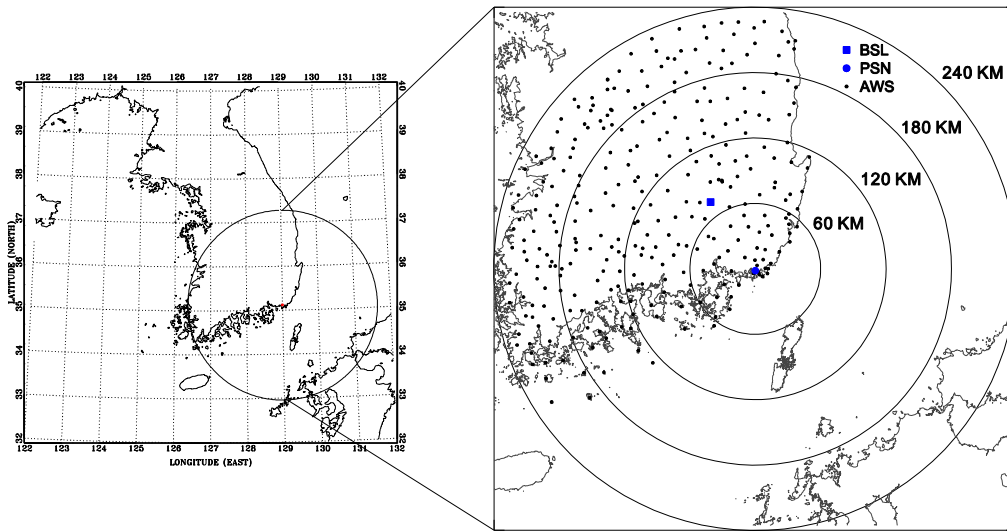
1 Table 1. Rainfall events used for the analysis.

Date	Source	Period of analysis
8 September 2012	Low pressure	0000 LST to 0600 LST
25 August 2014	Low pressure	0900 LST to 1600 LST

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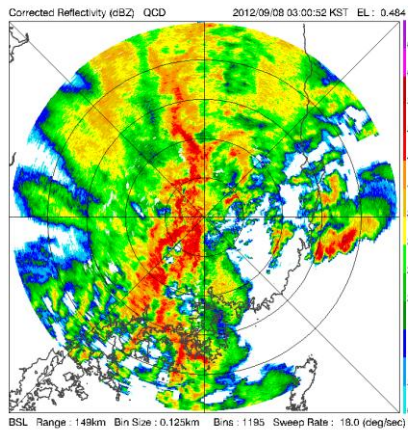


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Figure 1. Location of the Bislan radar (solid rectangle), the PARSIVEL disdrometer and Gudeok radar (solid circle), and rain gauges (black dots) distributed within 240 km of radar coverage. Circles indicate distance from the Gudeok radar, and are drawn at intervals of 60 km.

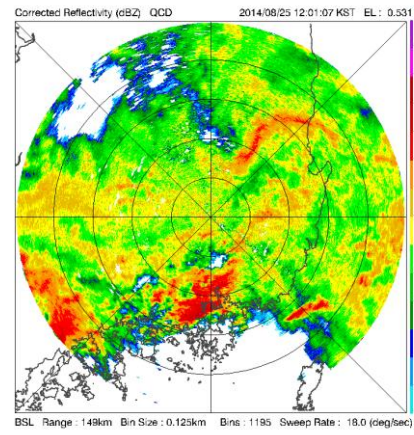
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(a)



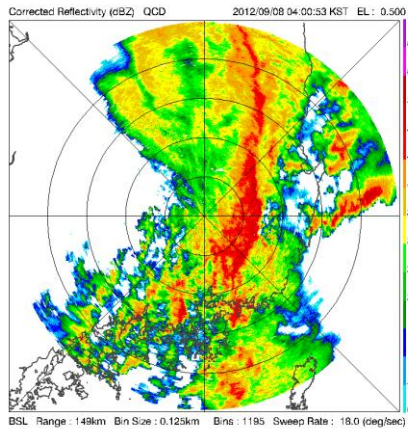
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(b)



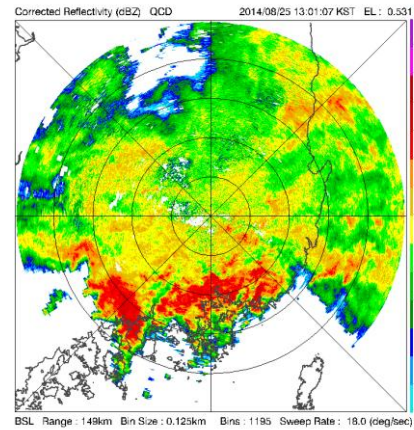
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(c)



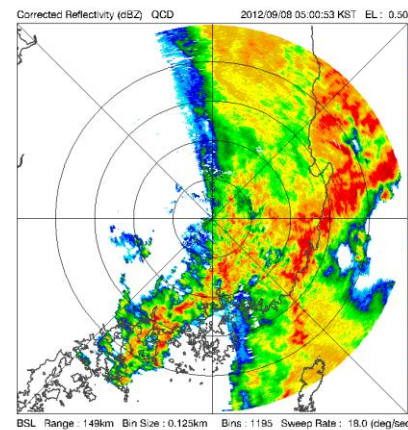
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(d)



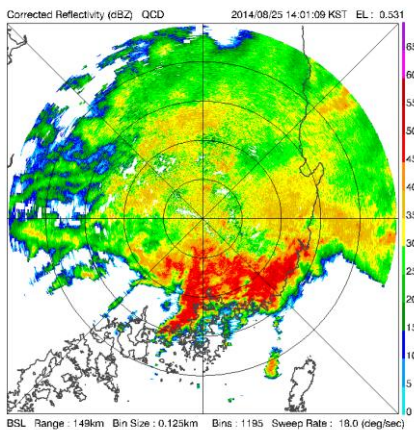
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(e)



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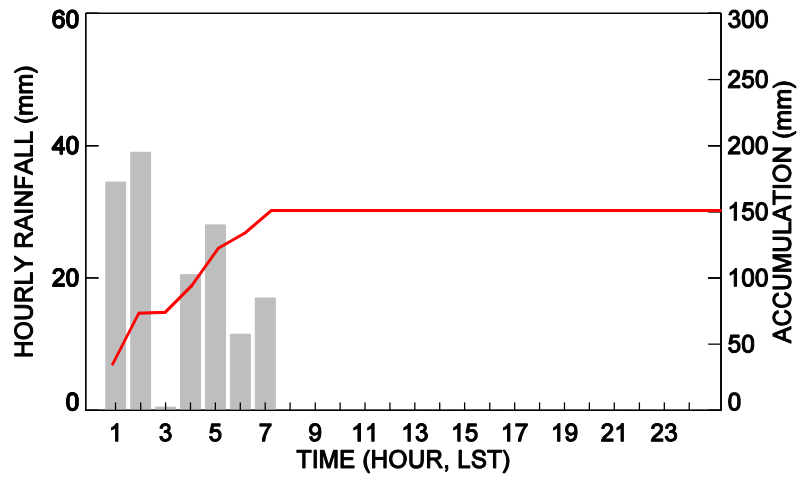
(f)



7 Figure 2. Time series of horizontal reflectivity (ZH) at 0.5 elevation angle observed from BSL  
 8 (a) 0400 LT, (c) 0500 LT, (e) 0600 LT on 8 September in 2012, (b) 1200 LT, (d) 1300 LT, (f)  
 9 1400 LT on 25 August in 2014.

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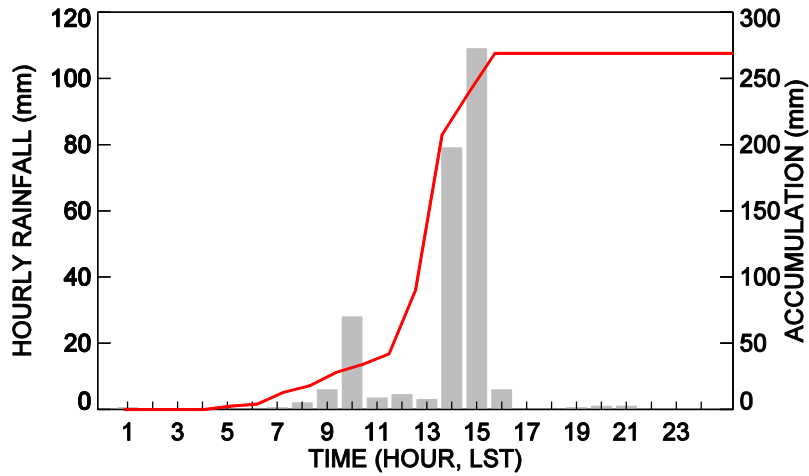
(a)



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(b)



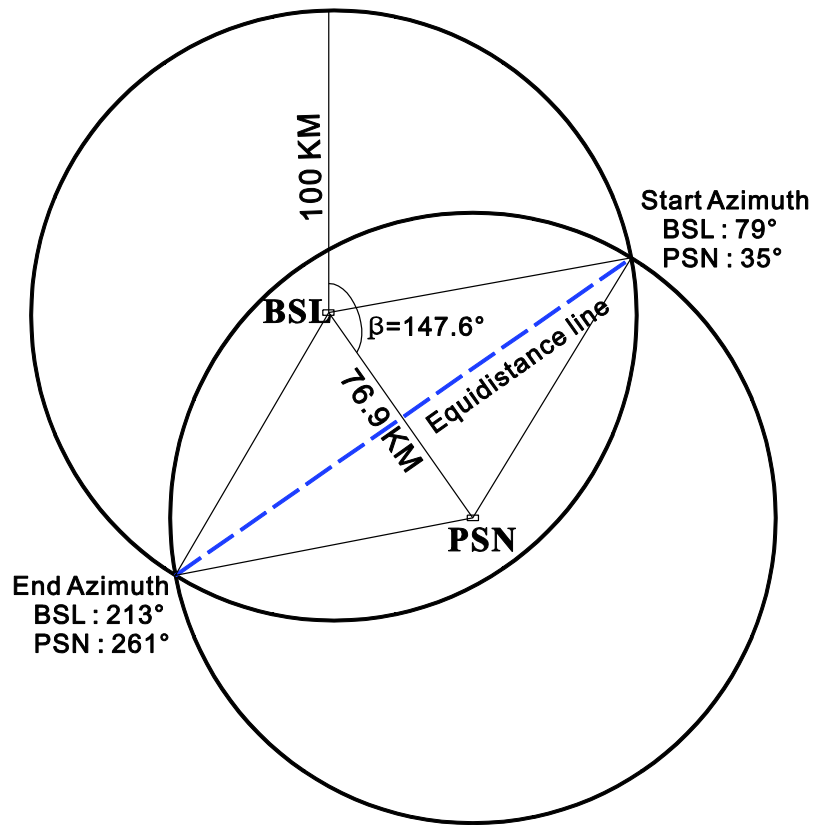
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5 Figure 3. Time series of 1 hour rainfall (bar) and daily accumulated (red line) measured from a  
 6 gage which recorded highest daily rainfall within radar coverage at (a) North Changwon (ID  
 7 255) on 8 September in 2012 and (b) Geumjeong (ID 939) on 25 August in 2014.

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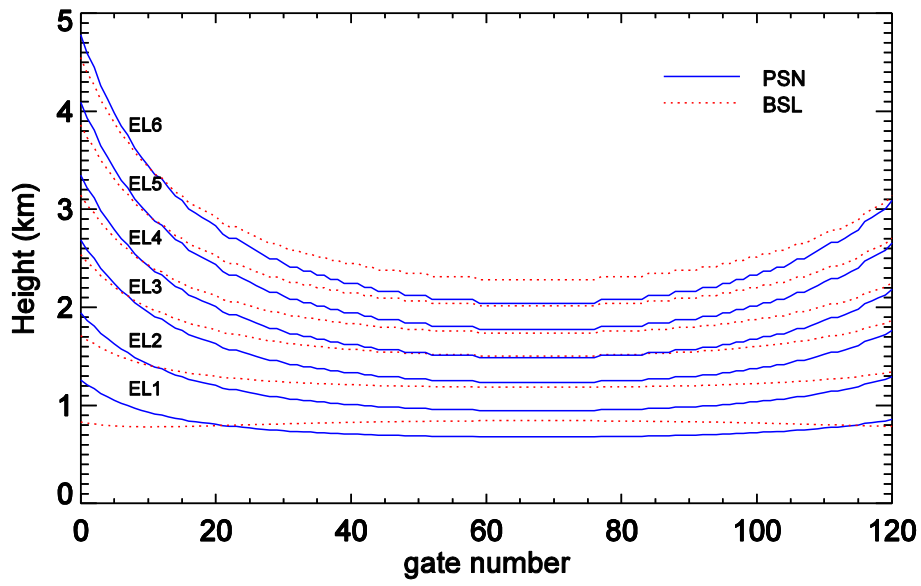
2 Figure 4. Schematic diagram showing the method used to calculate the line of equidistance  
 3 between two radars. The effective radius was set to 100 km and the distance between radars is  
 4 76.9 km. The azimuthal angle from BSL to PSN is 147.6 degrees. The start and end azimuthal  
 5 angles are 79 (35) and 213 (261) degrees for BSL (PSN), respectively. The blue dashed line  
 6 shows the equidistance line.

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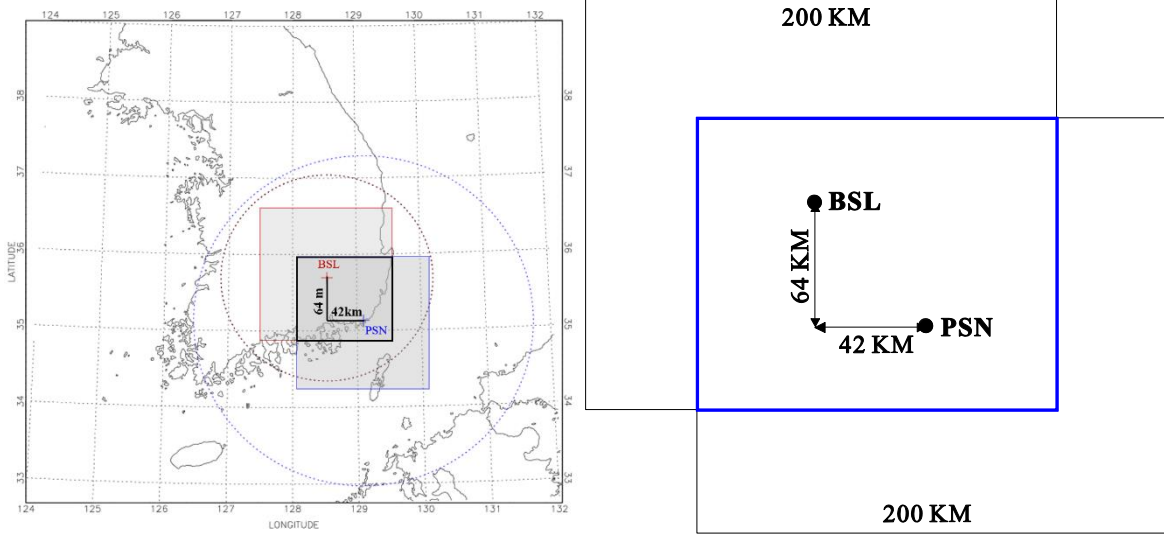
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Figure 5. Beam height of PSN (blue solid lines) and BSL (red dotted lines) at the equidistance line. EL1 to EL6 show the lowest, second, third, fourth, fifth, and sixth elevation angles, respectively.

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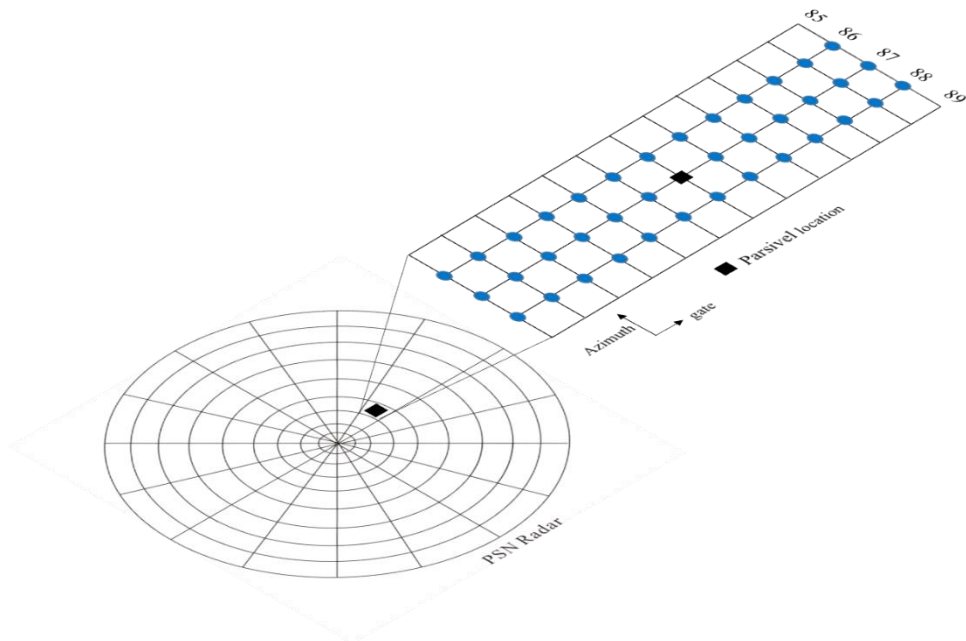


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3 Figure 6. Schematic diagram of the overlapping area for BSL and PSN. The east–west and  
4 north–south distances between the two radars are 42 km and 64 km, respectively. The red (blue)  
5 dotted circle shows the maximum range of BSL (PSN) and gray shaded area show 200 km by  
6 200 km extracted from each radar coverage in the left panel.

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2 Figure 7. Schematic diagram showing matching of the radar gate and the PARSIVEL  
 3 disdrometer. PARSIVEL is located ~9 km from the radar, at an azimuthal angle of 87 degrees.

4 The radar reflectivity was averaged over a  $3 \text{ km} \times 3^\circ$  domain centered at the PARSIVEL  
 5 location.

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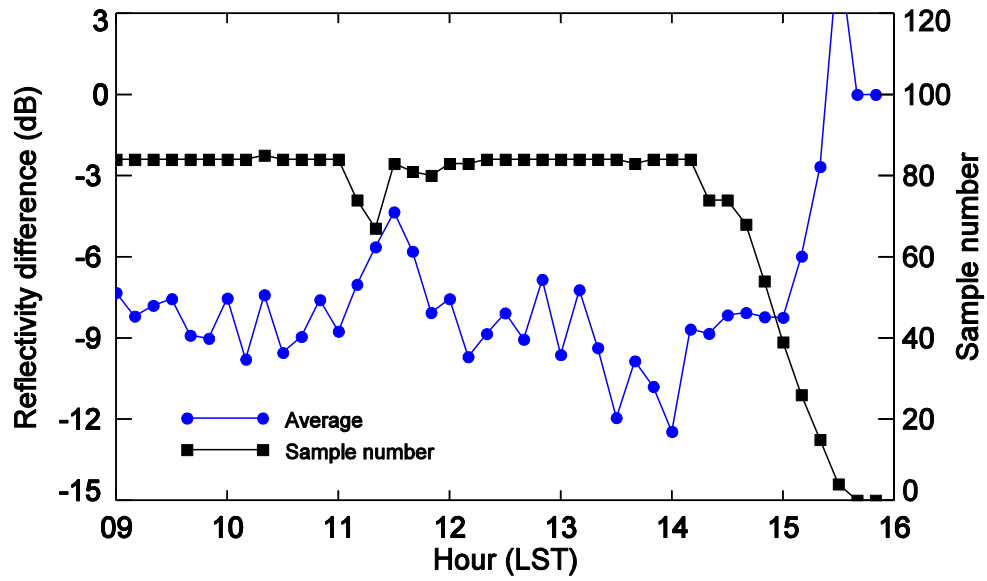
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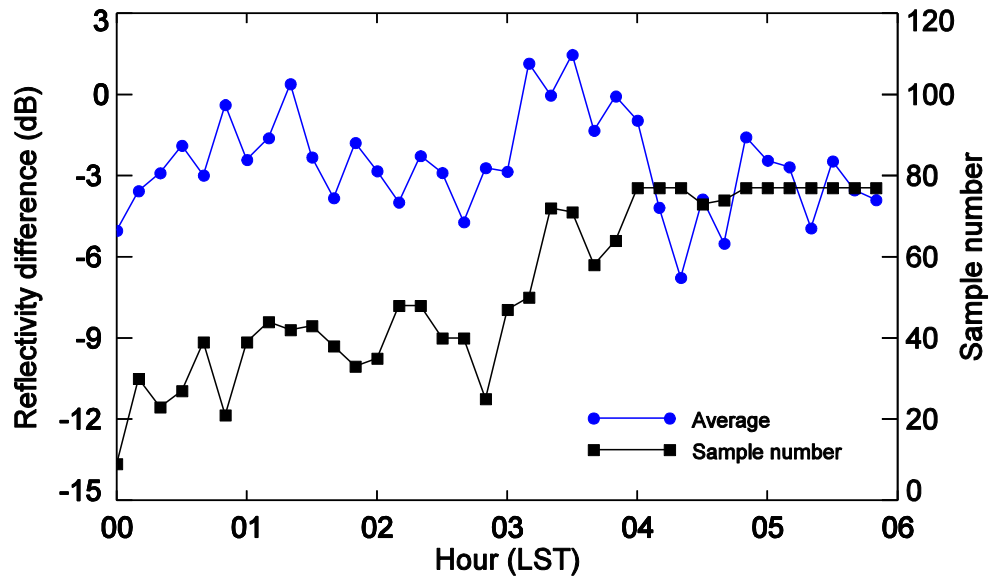


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2 Figure 8. Time series of the average reflectivity difference between PSN and BSL at the  
 3 equidistance line (blue circles) and the number of samples used in each calculation (black  
 4 squares) on 25 August in 2014.

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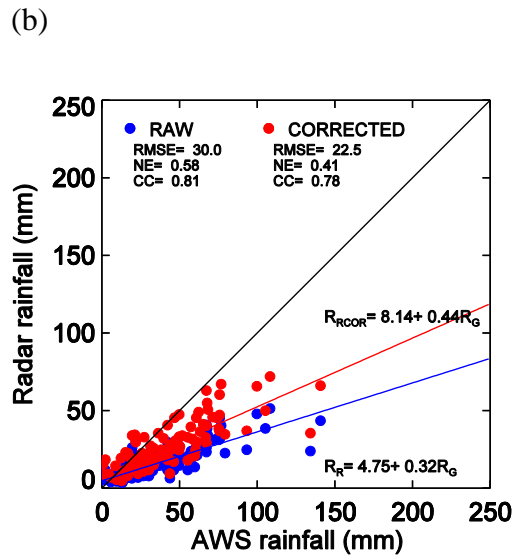
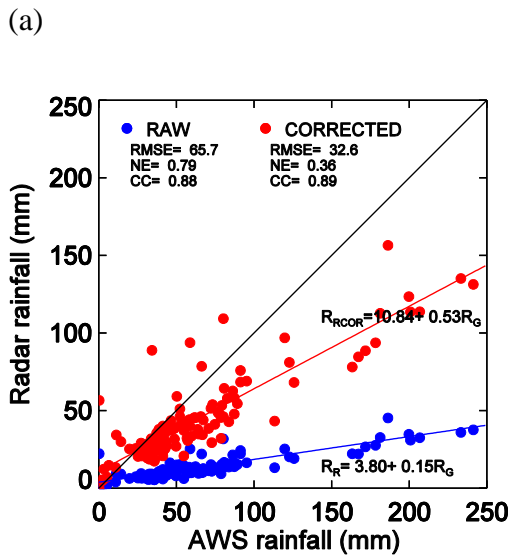


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2 Figure 9. As for Fig. 8 but for 8 September 2012.

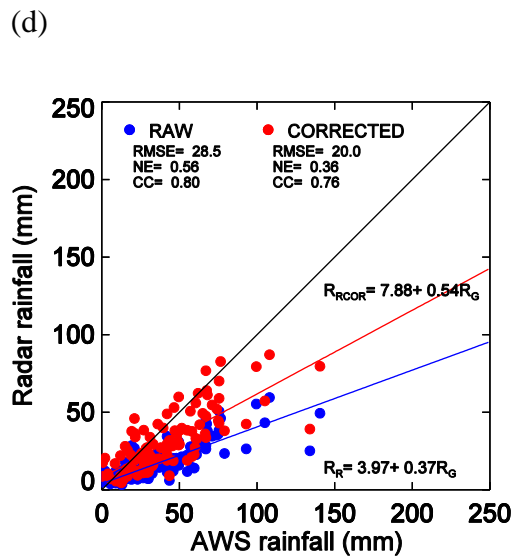
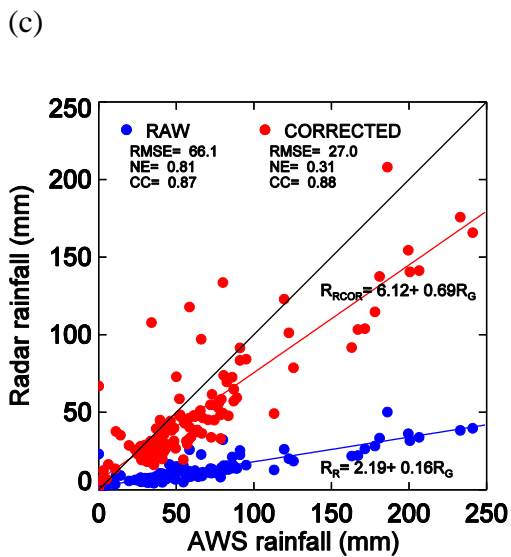
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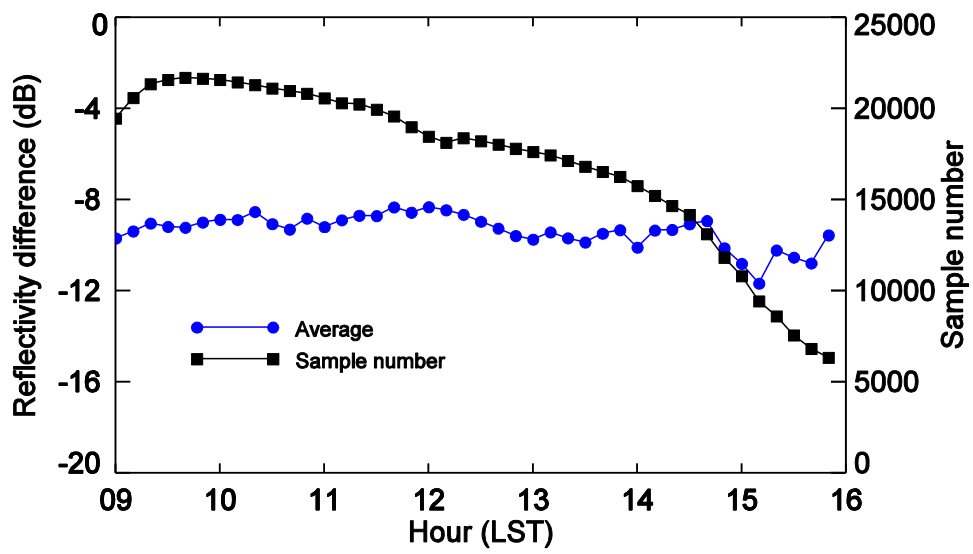
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5 Figure 10. Scatter plot of total accumulated rainfall for analyzed time period calculated by gage  
 6 and radar using (a and b)  $Z = 200 R^{1.6}$  and (c and d)  $Z = 300 R^{1.4}$  for 25 August 2014 and 8  
 7 September 2012, respectively. Blue circles show the rainfall pairs obtained using raw  
 8 reflectivity and red circles show those obtained using reflectivity corrected with the  
 9 equidistance line method.

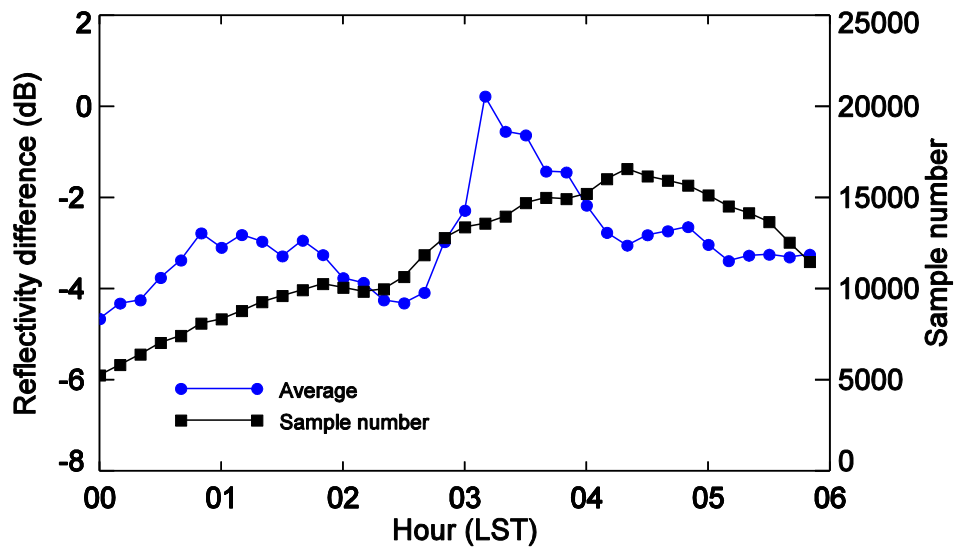
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2 Figure 11. Time series of the average reflectivity difference between PSN and BSL at the  
 3 overlapping area (blue circles) and the number of samples used in each calculation (black  
 4 squares) on 25 August in 2014.

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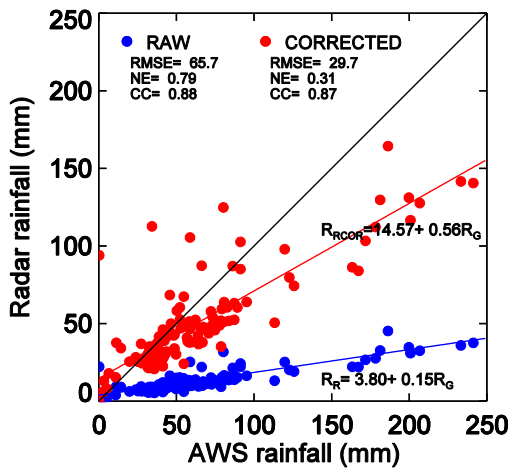
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2 Figure 12. Time series of the average reflectivity difference between PSN and BSL at the  
 3 overlapping area (blue circles) and the number of samples used in each calculation (black  
 4 squares) on 8 September in 2012.

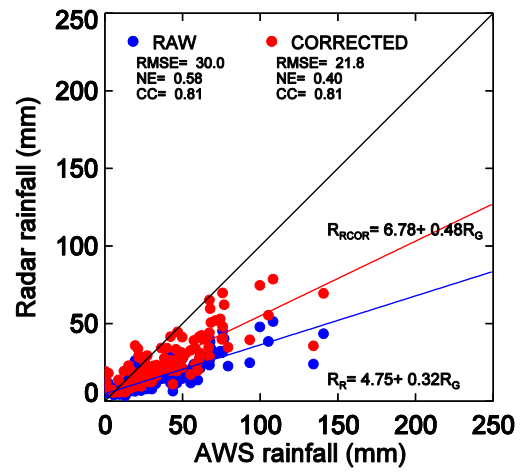
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(a)



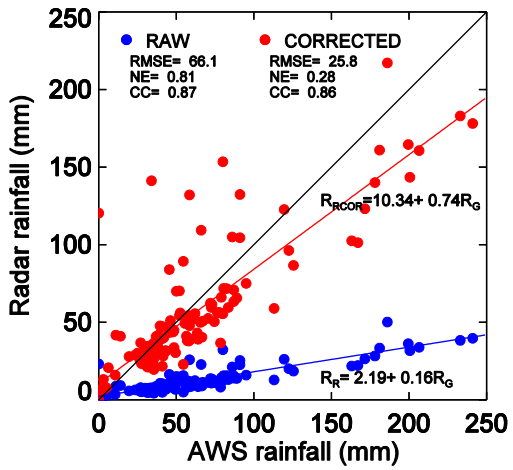
(b)



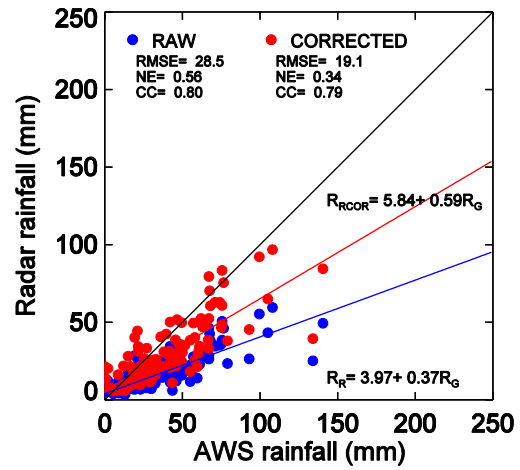
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(c)



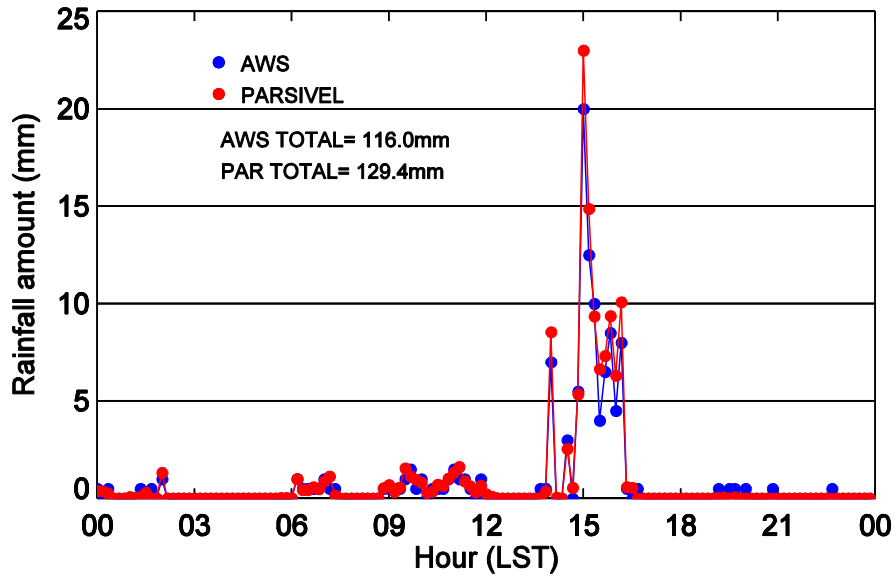
(d)



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5 Figure 13. As for Fig. 10 but for the overlapping area method.

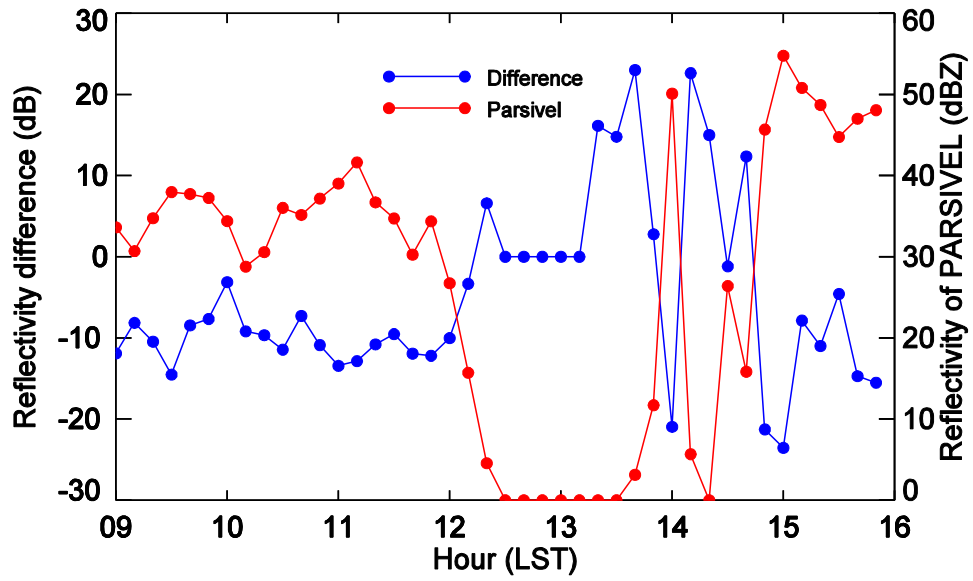
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2 Figure 14. Time series of 10 min rainfall amount as obtained by PARSIVEL (red circles) and  
 3 collocated gauges (blue circles).

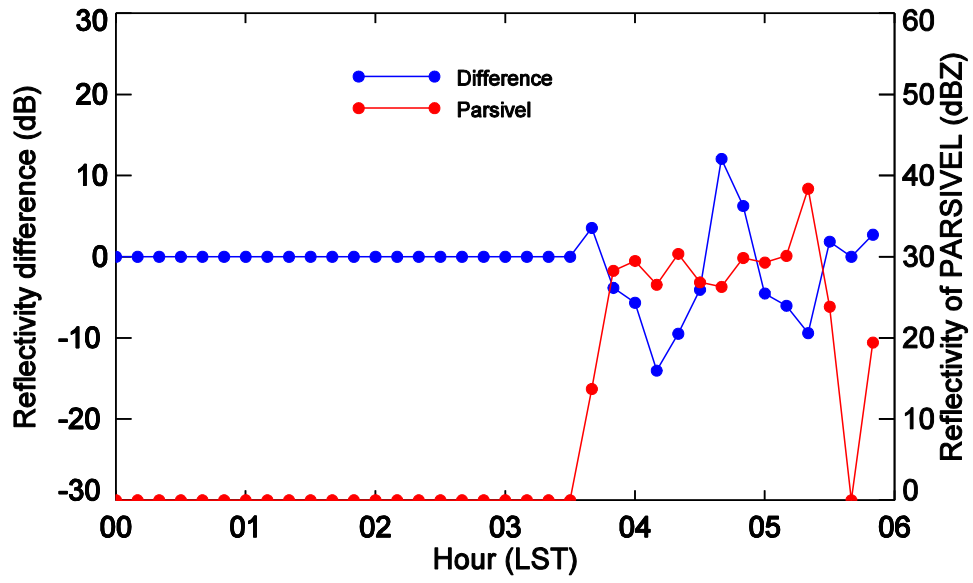
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2 Figure 15. Time series of reflectivity obtained by radar (black circles) and by PARSIVEL (red  
 3 circles), and the radar bias (blue circles) on 25 August 2014.

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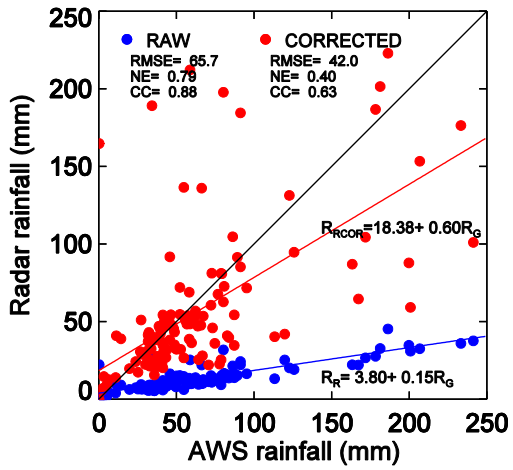
2 Figure 16. As for Fig. 15 but for 8 September 2012.

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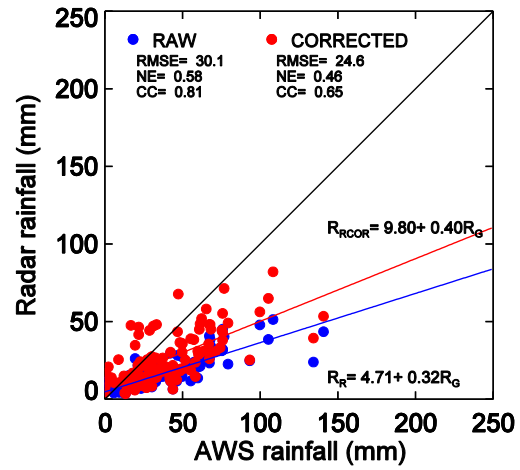


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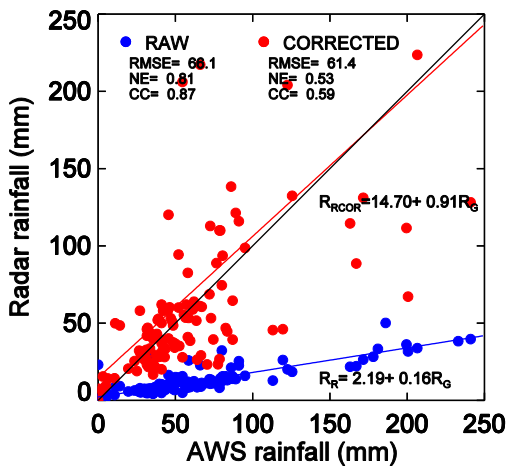
(b)



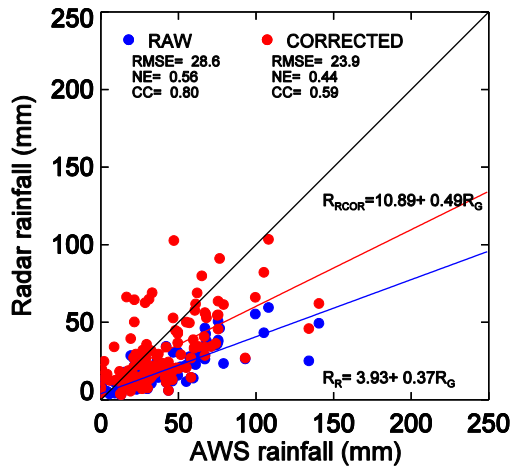
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(c)



(d)



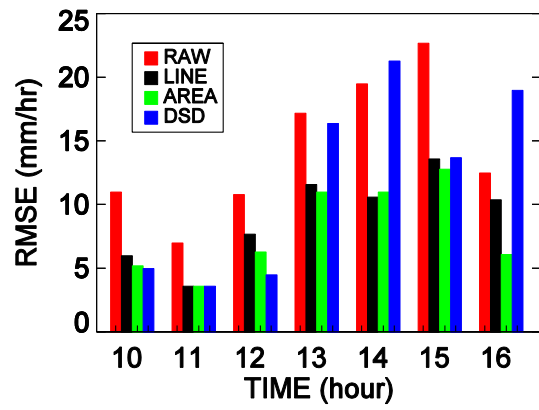
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5 Figure 17. As for Fig. 10 but for the disdrometer method.

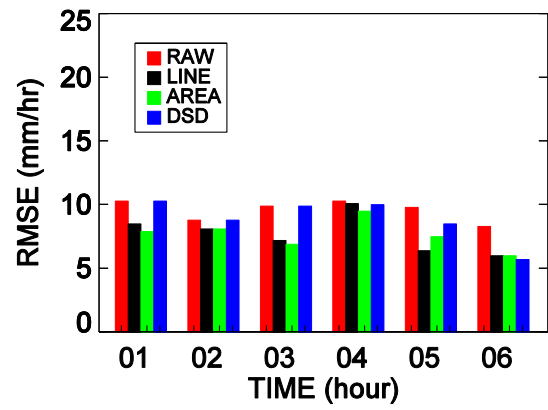
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(b)



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3 Figure 18. Accumulated rainfall RMSE calculated from radar and gage for different bias  
4 correction methods on (a) 25 August 2014 and (b) 8 September 2012. The bars with different  
5 colors show results obtained using the raw data, equidistance line method, overlapping area  
6 method, and disdrometer method, respectively.

7