



1 **Dual-polarization radar rainfall estimation in Korea**  
2 **according to raindrop shapes using a 2D Video**  
3 **Disdrometer**

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13

14 **Abstract**

15 The shapes of raindrops play an important role in inducing polarimetric rainfall algorithms  
16 with differential reflectivity ( $Z_{DR}$ ) and specific differential phase ( $K_{DP}$ ). The shapes of  
17 raindrops have a direct impact on rainfall estimation. However, the characteristics of raindrop  
18 size distribution (DSD) are different depending on precipitation type, storm stage of  
19 development, and regional and climatological conditions. Therefore, it is necessary to provide  
20 assumptions based on raindrop shapes that reflect the rainfall characteristics of the Korean  
21 peninsula. In this study, we presented a method to find optimal polarimetric rainfall  
22 algorithms on the Korean peninsula using the 2-Dimensional Video Disdrometer (2DVD) and  
23 Bislan S-Band dual-polarization radar. First, a new axis ratio of raindrop relations was  
24 developed for the improvement of rainfall estimation. Second, polarimetric rainfall  
25 algorithms were derived using different axis ratio relations, and estimated radar-point one-  
26 hour rain rate for the differences in polarimetric rainfall algorithms were compared with the  
27 hourly rain rate measured by gauge. In addition, radar rainfall estimation was investigated in  
28 relation to calibration bias of reflectivity and differential reflectivity. The derived raindrop  
29 axis ratio relation from the 2DVD was more oblate than existing relations in the  $D < 1.5$  mm



1 and  $D > 5.5$  mm range. The  $R(K_{DP}, Z_{DR})$  algorithm based on a new axis ratio relation showed  
2 the best result on DSD statistics; however, the  $R(Z_h, Z_{DR})$  algorithm showed the best  
3 performance for radar rainfall estimation, because the rainfall events used in the analysis  
4 were mainly weak precipitation and  $K_{DP}$  is noisy at lower rain rates ( $\leq 5$  mm  $hr^{-1}$ ). Thus, the  
5  $R(K_{DP}, Z_{DR})$  algorithm is suitable for heavy rainfall and  $R(Z_h, Z_{DR})$  algorithm is suited for  
6 light rainfall. The calibration bias of reflectivity ( $Z_H$ ) and differential reflectivity ( $Z_{DR}$ ) were  
7 calculated from the comparison of measured with simulated  $Z_H$  and  $Z_{DR}$  from the 2DVD. The  
8 calculated  $Z_H$  and  $Z_{DR}$  bias was used to reduce radar bias, and to produce more accurate  
9 rainfall estimation.

10

## 11 **1 Introduction**

12 Radar is a very useful monitoring tool for extreme weather forecasting, flood forecast  
13 and rainfall estimation because of its high spatial and temporal resolution. In particular, dual-  
14 polarization radar providing reflectivity ( $Z_H$ ), differential reflectivity ( $Z_{DR}$ ), differential phase  
15 ( $\Phi_{DP}$ ), specific differential phase ( $K_{DP}$ ), and cross-correlation coefficient ( $\rho_{hv}$ ) can estimate  
16 rainfall more accurately than single polarization radar. Dual-polarization radar provides  
17 characteristics of the precipitation by backscatter and differential propagation phase of  
18 hydrometeors, and therefore can obtain more information about DSD (Cifelli et al., 2011). In  
19 addition, the multi-parameters can distinguish precipitation type, and reduce the impact of  
20 DSD variability on the rainfall estimation. Therefore, rainfall estimators using a combination  
21 of  $Z_H$ ,  $Z_{DR}$ , and  $K_{DP}$  are better than using reflectivity factor only (Ryzhkov et al., 2005).

22 Several different polarimetric rainfall algorithms have been developed assuming  
23 raindrop shapes (Sachidananda and Zrnić, 1987; Chandrasekar et al., 1990; Ryzhkov and  
24 Zrnic, 1995; Gorgucci et al., 2001). This is because the shape of raindrops is one of the most  
25 sensitive parameters for representing the DSD properties of the rain. Some researchers have  
26 attempted to produce the mean shape of raindrops. Keenan et al. (2001) derived an empirical  
27 relation from observational data, and Pruppacher and Beard (1970), Green (1975), and Beard  
28 and Chuang (1987) investigated the shape of raindrops falling under the influence of gravity.  
29 The raindrop shape is defined by the shape-size relationship of a raindrop. These raindrop  
30 axis-ratio relations play an important role in deriving polarimetric rainfall algorithms that use  
31  $Z_{DR}$  and  $K_{DP}$  (Jameson 1983, 1985; Gorgucci et al. 2001). However, the characteristics of rain  
32 DSDs are associated with types of storms and stages of storm development as well as



1 climatic regimes (Bringi et al., 2003). Thus, it was necessary to determine the mean axis ratio  
2 of raindrops reflecting rainfall characteristic of the Korean peninsula, to optimize the  
3 polarimetric rainfall algorithm.

4 Polarization radar contains errors such as attenuation, bright band, ground clutter, and  
5 calibration bias (of  $Z_H$  and  $Z_{DR}$ ). These measurement errors affect rainfall estimation.  
6 Therefore, accurate measurement and calibration of  $Z_H$  and  $Z_{DR}$  are necessary to achieve  
7 accurate radar rainfall estimation (Park and Lee, 2010). The accommodation of calibration  
8 bias of single polarimetric radar is possible by monitoring the stability of the hardware, and  
9 measured  $Z_H$  and  $Z_{DR}$  can be corrected using ground validation equipment such as a  
10 disdrometer. Joss et al. (1968) calibrated radar reflectivity using the measured  $Z_H$  from the  
11 radar profiler (at vertical incidence) and disdrometer-inferred  $Z_H$ . The radar reflectivity was  
12 calibrated by comparing reflectivity between radar and disdrometer to check the calibration  
13 of the WSR-88D (Weather Surveillance Radars—1988 Doppler) at Greer, South Carolina  
14 (Ulbrich and Lee, 1999). Goddard et al. (1982) and Goddard and Cherry (1984) compared  
15 radar with disdrometer using the axis-ratio relations of Pruppacher and Beard (1970) and  
16 Pruppacher and Pitter (1971), respectively, and found that radar measures of  $Z_{DR}$  were 0.3 dB  
17 and 0.1 dB lower than the disdrometer estimates. In addition to use of disdrometers, there are  
18 various other ways to correct biases in radar data, such as using the self-consistency  
19 constraint between  $Z_H$  and  $K_{DP}$ , vertically pointing measurements, and comparison of  
20 measured data and mean  $Z_H$ - $Z_{DR}$  relationship (Kwon et al., 2015). Moreover, a variety of  
21 radar calibration methods were introduced in Atlas (2002).

22 In this study, we developed mean axis ratio relation and polarimetric rainfall  
23 algorithms using 2-Dimensional Video Disdrometer (2DVD) measurement from September  
24 2011 to October 2012 in Daegu, Korea. The four raindrop shapes assumption [after  
25 Pruppacher and Beard (1970), Beard and Chuang (1987), and Brandes et al. (2002)] and  
26 newly derived axis-ratio relation from 2DVD data were used to derive accurate polarimetric  
27 rainfall relation for rainfall estimation. In addition, the  $Z_H$  and  $Z_{DR}$  of Bislan dual-  
28 polarization radar were calibrated by comparing them with simulated  $Z_H$  and  $Z_{DR}$  by 2DVD.  
29 Thereafter, improvement of quantitative rainfall estimation was investigated by applying  
30 derived calibration bias. In Section 2, the data used in this study is described. The  
31 methodology for 2DVD data quality control, derived raindrop-axis ratio from 2DVD data,  
32 and simulated polarimetric parameters by the T-matrix scattering method are described in



1 Section 3. The results of the statistical validation of rainfall estimation are presented in  
2 Section 4. Finally, conclusions are drawn in Section 5.

3

## 4 **2 Data and instrument**

### 5 **2.1 Disdrometer**

6 The disdrometer data was used for development of mean raindrop axis ratio and  
7 polarimetric rainfall relations. The disdrometer data used in this study were measured using a  
8 2DVD, and the data were collected from September 2011 to October 2012 in Daegu, Korea  
9 (35.9°N, 128.5°E). The 2DVD consists of two orthogonal light sheets (referred to as A and B  
10 line-scan cameras). Line-scan cameras have single-line photo detectors. The particle shadows  
11 are detected on the photo detectors and the particle images are recoded from two sides and at  
12 different heights, when particles are falling through the measurement area (10 cm × 10 cm). A  
13 more detailed description of 2DVD is given in Kruger and Krajewski (2002).

14 The 2DVD measures drop size, fall velocity, and the shape of individual particles.  
15 From these, one can calculate precipitation DSDs including such as the rain rate, total number  
16 concentration, and water content.

17

### 18 **2.2 Radar**

19 The Ministry of Land, Infrastructure, and Transport (MLIT) operates the Bislan (BSL)  
20 dual-polarization radar in Bislan, Korea (35.7°N, 128.5°E). The BSL S-Band radar has a  
21 narrow observation range of 150 km and frequency of 2.5 min because it is used primarily for  
22 hydrological observations and flood forecasts. The BSL S-Band radar measured polarimetric  
23 parameters such as  $Z_H$ ,  $Z_{DR}$ ,  $K_{DP}$  and  $\rho_{hv}$  in real time. The data obtained were from six  
24 elevation angles (from  $-0.5^\circ$  to  $1.6^\circ$ ), with a gate size resolution of 125 m and radar beam  
25 width of  $0.95^\circ$ . The specifications of the BSL radar are shown in Table 1.

26 The BSL S-Band dual-polarization radar is located about 22.3 km ( $17^\circ$ ) away from the  
27 2DVD location (Fig. 1). These geographical locations were adopted to compare the two sets  
28 of observation data. We used radar data from September 2011 to October 2012. During this  
29 period, rainfall events were analyzed for products of calibration bias of  $Z_H$  and  $Z_{DR}$  and



1 rainfall estimation. In addition, the  $0.0^\circ$  plan position indicator (PPI) radar data were used to  
2 avoid effects from beam blocking and ground echoes on the measurements. The  $Z_H$ ,  $Z_{DR}$ ,  $\Phi_{DP}$ ,  
3 and  $\rho_{hv}$  radar parameters were averaged over five successive gate size resolutions and two  
4 adjacent azimuth angles, and  $K_{DP}$  was calculated from the filtered  $\Phi_{DP}$  as the slope of a least  
5 squares fit.

## 6 **2.3 Rain gauge**

7 A tipping bucket rain gauge was used to validate rainfall calculated from 2DVD data.  
8 The bucket size of the rain gauge was 0.2 mm and time resolution was 0.5 s. The rain gauge  
9 was installed in the same location as the 2DVD.

10

## 11 **3 Methodology**

### 12 **3.1 Quality control of 2DVD**

13 The 2DVD observation data is useful to investigate the characteristics of rainfall.  
14 However, a number of particle outliers were measured due to wind turbulence, splashing,  
15 break up of drops, and mismatching between camera A and B (Raupach and Berne, 2015).  
16 These results lead to incorrect information about the particles. Therefore, before using the  
17 2DVD data, a quality control process was needed.

18 Figures 2a and b show fall velocity and oblateness distribution according to raindrop  
19 diameter before data quality control was performed. For comparison, we plotted the axis-  
20 ratio-diameter relation of Pruppacher and Beard (1970). Some of the outliers of fall velocity  
21 and oblateness distribution were beyond the normal distribution. In particular, the outliers  
22 appeared prominently in the small raindrop ranges. To remove these outliers, velocity-based  
23 filtering was applied to the 2DVD measurement data (Thurai and Bringi, 2005).

$$|V_{measured}(D) - V_A(D)| < 0.4V_A(D)$$

$$V_A(D) = 9.65 - 10.3 \exp(-0.6D) \quad (1)$$

24 where,  $D$  [mm] is the drop diameter,  $V_{measured}$  [ $\text{ms}^{-1}$ ] is the fall velocity as measured by the  
25 2DVD, and  $V_A$  represents the Atlas velocity formula (Atlas et al. 1973). Despite the  
26 application of velocity-based filtering, significant bias still remained in the small drop size  
27 area. This was due to instrumental limitations, such as mismatch problems with the line-scan



1 cameras and the limited vertical resolution of the instrument. Therefore, the oblateness data  
2 corresponding to raindrop diameters smaller than 0.5 mm were removed when we calculated  
3 the new axis-ratio formula. The values outside the normal distribution (about 17%) were  
4 removed as a result of application filtering (Fig. 2c).

5 To analyze the reliability of the 2DVD data, we compared the rain rate calculated  
6 from the 2DVD data (Eq. 2) to collocated rain gauge measurements. The difference of  
7 accumulated rainfall represents the percent error (Eq. 3).

$$R = 6 \times 10^{-4} \pi \sum_{D_{min}}^{D_{max}} D^3 V(D) N(D) \Delta D \quad [mm \text{ hr}^{-1}] \quad (2)$$

$$PE = \frac{|AR_{rain \ gauge} - AR_{2DVD}|}{AR_{rain \ gauge}} \times 100 \quad [\%] \quad (3)$$

8 here  $D_{max}$  and  $D_{min}$  are the maximum and minimum diameters of the observed drops in mm,  
9  $N(D)$  is the drop number concentration in  $\text{mm}^{-1} \text{m}^{-3}$ ,  $V(D)$  is the drop fall velocity in  $\text{ms}^{-1}$ , and  
10  $\Delta D$  is drop interval ( $\Delta D = 0.2$  mm). The drop fall velocity formula was derived by Brandes  
11 et al. (2002);  $PE$  is the percent error, and  $AR$  is accumulated rainfall in mm.

12 During the period from September 2011 to October 2012, the rainfall cases were  
13 analyzed and an example of six cases is shown in Fig. 3. The six events are (i) 0000–0900  
14 UTC 14 October 2011, (ii) 1400–2359 UTC 2 April 2012, (iii) 0000–2359 UTC 21 April  
15 2012, (iv) 0000–0800 UTC 25 April 2012, (v) 0000–2359 UTC 23 August 2012, and (vi)  
16 1600–2359 UTC 27 August 2012. Figure 3a shows the accumulated rainfall computed from  
17 the 2DVD and rain gauge on 14 October 2011. The overall distribution between the 2DVD  
18 and rain gauge was good. The 2DVD recorded 13.14 mm and rain gauge recorded 13.52 mm,  
19 their difference was about 2.81%. As shown in Fig. 3b–f, percent errors from the five rainfall  
20 cases are 9.42, 0.24, 4.16, 7.88 and 8.25%, respectively. Generally, some papers show that  
21 rainfall differences between disdrometer and rain gauge were mostly from 10% to 20%  
22 (McFarquhar and List, 1993; Sheppard and Joe, 1994; Hagen and Yuter, 2003; Tokay et al.,  
23 2003). These differences might result from such issues as differences in instruments, effects  
24 from the measurement environment, and rainfall variability. Therefore, the 2DVD data within  
25 20% percent error were used in this study.

26 After the quality control process, a total of 33 rainfall cases were selected for  
27 investigating the characteristics of rainfall over the Korea Peninsula. The accuracy of 33



1 rainfall cases was in the range of 0.24–19.32% compared to in suit rain gauges. The dataset  
2 consisted of 15 stratiform rainfall cases, 12 convective rainfall cases, and 6 mixed rainfall  
3 cases (total of 33 rainfall event) with 17,618 min DSD samples. The type of precipitation,  
4 difference rainfall, and accumulated rainfall between 2DVD and rain gauge for the 33 rainfall  
5 events are listed in Table 2. Figure 4 shows hourly and total accumulated rainfall of 2DVD  
6 and rain gauge for the 33 rainfall cases. The overall rainfall distribution between 2DVD and  
7 rain gauge were good, total accumulated rainfall by rain gauge was larger than 2DVD by  
8 about 0.81%.

9

### 10 **3.2 Raindrop axis ratio**

11 A very small raindrop has an approximately spherical shape that becomes oblate as its  
12 size increases. The shape of a raindrop according to drop size can be expressed as the mean  
13 axis-ratio relation; this relation is one of the most sensitive parameters for representing the  
14 rainfall properties. Hence, in order to produce rainfall estimation algorithms reflecting  
15 rainfall characteristic of the Korean peninsula, the new mean axis-ratio relation, using the  
16 2DVD data listed in Table 2, was derived as a polynomial function. Although the measured  
17 maximum diameter from the 2DVD could reach axis-about 8.0 mm, the mean axis-ratio  
18 fitting was established to within 7 mm in order to obtain accurate information from the  
19 appropriate data. The third-order polynomial new mean axis-ratio relation ( $b/a$ ) is as follows  
20 in Eq. (4), which is reasonably extended to 7 mm.

$$21 \quad b/a = 0.997845 - 0.0208475D - 0.0101085D^2 + 6.4332 \times 10^{-4}D^3 \quad (0.5 \leq D \leq 7 \text{ mm}) \quad (4)$$

22 where,  $a$  and  $b$  are the major axis and minor axis, respectively.  $D$  is the raindrop diameter in  
23 mm.

24

### 25 **3.3 Disdrometer-rainfall algorithms**

26 In order to produce the polarimetric rainfall algorithms, the theoretical polarimetric  
27 parameters (e.g.,  $Z_H$ ,  $Z_{DR}$ , and  $K_{DP}$ ) were simulated from the 2DVD data using the T  
28 (transition) matrix method. Polarimetric parameters were simulated by making assumptions  
29 about the shape of the raindrops. First, we calculated the complex scattering amplitudes of



1 raindrops at the S-Band of wavelength 10.7 cm using mean axis-ratio relations. Second,  
 2 calculated scattering amplitudes about the axis ratio relations were used for production of  
 3 polarimetric parameters. The dual-polarimetric parameters were calculated using the  
 4 following Eq. (5–7) (Jung et al., 2010).

$$Z_h = \frac{4\lambda^4}{\pi^4 |K_w|^2} \int_0^{D_{max,x}} A |f_a(\pi)|^2 + B |f_b(\pi)|^2 + 2C Re[f_a(\pi)f_b^*(\pi)] N(D) dD \quad [mm^6 m^{-3}] \quad (5)$$

$$Z_v = \frac{4\lambda^4}{\pi^4 |K_w|^2} \int_0^{D_{max,x}} B |f_a(\pi)|^2 + A |f_b(\pi)|^2 + 2C Re[f_a(\pi)f_b^*(\pi)] N(D) dD \quad [mm^6 m^{-3}] \quad (6)$$

5 Where

$$6 \quad A = \langle \cos^4 \Phi \rangle = \frac{1}{8} (3 + 4 \cos 2\bar{\Phi} e^{-2\sigma^2} + \cos 4\bar{\Phi} e^{-8\sigma^2})$$

$$B = \langle \sin^4 \Phi \rangle = \frac{1}{8} (3 - 4 \cos 2\bar{\Phi} e^{-2\sigma^2} + \cos 4\bar{\Phi} e^{-8\sigma^2})$$

7 And

$$C = \langle \sin^2 \Phi \cos^2 \Phi \rangle = \frac{1}{8} (1 - \cos 4\bar{\Phi} e^{-8\sigma^2})$$

$$K_{DP} = \frac{180\lambda}{\pi} \int_0^{D_{max}} C_k Re[f_a(0) - f_b(0)] N(D) dD \quad [^\circ km^{-1}] \quad (7)$$

8 where  $C_k = \langle \cos 2\Phi \rangle = \cos 2\bar{\Phi} e^{-2\sigma^2}$ .

9 where,  $f_a(0)$  and  $f_b(0)$  are complex forward-scattering amplitudes, and  $f_a(\pi)$  and  $f_b(\pi)$  are  
 10 complex backscattering amplitudes for polarization along the major and minor axes. Here,  $f_a^*$   
 11 and  $f_b^*$  are their respective conjugates,  $\bar{\Phi}$  is mean canting angle, and  $\sigma$  is standard deviation of  
 12 the canting angle. The terms  $\bar{\Phi}$  and  $\sigma$  are assumed to be  $7^\circ$  and  $0^\circ$ , respectively (Huang et al.,  
 13 2008).  $D_{max}$  is 7 mm, the radar wavelength is  $\lambda = 10.7$  cm (S-Band), the dielectric factor for  
 14 water is  $K_w = 0.93$ , and  $N(D)$  was calculated using the 2DVD measurement.

15 Polarimetric rainfall relations between R and dual-polarimetric parameters are derived  
 16 when rain rate is greater than  $0.1 \text{ mm hr}^{-1}$ . Derived new polarimetric rainfall relations  
 17 according to axis ratio relations are presented in Table3.

18





### 1 3.4 Calibration of radar

2 The polarimetric radar contains systematic bias of the radar itself. Therefore,  
3 accommodation of the calibration bias of radar is necessary to improve quantitative  
4 precipitation estimation. The calibration of the radar was done for light rainfall events, and  
5 the new axis-ratio relation (Eq. 4) was used for simulation of the theoretical  $Z_H$  and  $Z_{DR}$   
6 parameters.

7 The calibration bias of  $Z_H$  and  $Z_{DR}$  were calculated from the comparison of measured  
8  $Z_H$  and  $Z_{DR}$  with the simulated  $Z_H$  and  $Z_{DR}$  from the 2DVD measurement. To compare  
9 polarimetric radar parameters, the cross-match point must first be determined. This is,  
10 because 2DVD data are point measurements and radar data are volume measurements. The  
11 BSL S-Band radar data were averaged over five successive gates and two adjacent azimuth  
12 angles centered on the 2DVD location. The elevation angle of  $0.0^\circ$  PPI was used.

13

## 14 4 Results

### 15 4.1 Comparison of raindrop axis ratio relations

16 We compared the new axis-ratio experimental fit with existing mean axis-ratio  
17 relations such as those of Pruppacher and Beard (1970), Beard and Chuang (1987), and  
18 Brandes et al. (2002) in Fig. 5. These have been approximated to various polynomial  
19 formulas, as follows:

$$20 \quad b/a = 1.03 - 0.062D \quad (1 \leq D \leq 9 \text{ mm}) \quad (8)$$

$$21 \quad b/a = 1.0048 + 5.7 \times 10^{-4}D - 2.628 \times 10^{-2}D^2 + 3.682 \times 10^{-3}D^3 - 1.677 \times 10^{-4}D^4 \quad (1 \leq D \leq 7 \text{ mm}) \quad (9)$$

$$22 \quad b/a = 0.9951 + 0.02510D - 0.03644D^2 + 5.303 \times 10^{-3}D^3 - 2.492 \times 10^{-4}D^4 \quad (1 \leq D \leq 8 \text{ mm}) \quad (10)$$

23 Equation 8 from Pruppacher and Beard (1970) is a linear relation from wind tunnel data, Eq.  
24 (9) is a fourth-order polynomial formula to the numerical model. Equation 10 is a polynomial  
25 empirical relation developed by Brandes et al. (2002) that was derived by combining drop  
26 shape observations. The Pruppacher and Beard (1970) linear relation (Eq. (8), green dash-dot  
27 line) falls below the new mean axis-ratio for  $1 \leq D < 5$  mm, and the Beard and Chuang (1987)  
28 polynomial relation (Eq. (9), black dashed line) is slightly lower than the result of the new  
29 mean axis-ratio in the range 2.5–6.5 mm. The new mean axis-ratio fit is more oblate than the



1 Brandes et al. (2002) polynomial empirical relation (Eq. (10), blue dotted line) when the  
2 raindrop sizes are greater than 5.5 mm and less than 2.5 mm. To the exclusion of this part, the  
3 new axis ratio of raindrops in the range 3–5.5 mm was similar to Eq. (10).

4 Thus, the new mean axis ratio relation is very similar to existing axis-ratio relations  
5 except for small particles ( $\leq 2$  mm) and large particles ( $\geq 5.5$  mm). This means that raindrops  
6 in South Korea are more oblate than the others. Although the difference in the axis ratio  
7 seems small, its impact on the rainfall estimation cannot be neglected.

8

## 9 **4.2 Verification of polarimetric rainfall algorithms**

### 10 **4.2.1 Variability of DSD in rainfall estimation**

11 To investigate the variability of DSD in rainfall estimation from polarimetric  
12 parameters, rain rate  $R_e$  was estimated from various combinations of polarimetric variables  
13 and compared with  $R$  from Eq. (2). The mean absolute error (MAE), the root-mean-square  
14 error (RMSE), and correlation coefficient (Corr.) are defined by the following equation:

$$MAE = \frac{1}{N} \sum |R - R_e| \quad [mm \ h^{-1}] \quad (11)$$

$$RMSE = \left( \frac{1}{N} \sum (R - R_e)^2 \right)^{0.5} \quad [mm \ h^{-1}] \quad (12)$$

$$Corr. = \frac{1}{N - 1} \frac{\sum [(R - \bar{R})(R_e - \bar{R}_e)]}{\sqrt{Var(R)Var(R_e)}} \quad (13)$$

15 where  $R$  is rain rate from observed 1-min DSDs and  $R_e$  is rain rate from estimated various  
16 combination of polarimetric parameters.  $R_e$  is then obtained from the same dataset. The  $N$  is  
17 the number of comparisons. Figure 6 shows the scatterplot of  $R$  and  $R_e$  for polarimetric  
18 rainfall relations based on the new axis-ratio relation and the scatter indicates the effect of  
19 DSD variability on rain estimation. The comparison between rain rates observed  $R$  and those  
20 estimated  $R_e$  shows good overall agreement. In particular, the statistic of scatter showed the  
21 best result (MAE = 0.23 mm hr<sup>-1</sup>, RMSE = 0.35 mm h<sup>-1</sup> and Corr = 0.10) when using the  
22  $R(K_{DP}, Z_{DR})$  based on the new axis-ratio relation. The use of the single parameter  $R(Z_H)$   
23 results in increase of the MAE = 0.96 mm hr<sup>-1</sup> and RMSE = 2.40 mm hr<sup>-1</sup>, and decrease of the  
24 Corr = 0.93 when compared with other polarimetric rainfall relations. Other polarimetric



1 rainfall algorithms based on mean axis-ratio relations showed similar results. Thus, the  
2 polarimetric parameters with  $K_{DP}$  and  $Z_{DR}$  from dual-polarization radar reduce the DSD  
3 variability in the rainfall estimation. A summary of statistics according to polarimetric  
4 rainfall algorithms and mean axis-ratio relations are presented in Table 3.

5

#### 6 **4.2.2 Validation of rainfall estimation**

7 In order to evaluate radar rainfall estimation according to different rainfall relations  
8 and raindrop shapes, we compared an estimated one-hour rain rate from the BSL S-Band  
9 radar to the hourly rain rate by rain gauge in Daegu, Korea. In addition, the rainfall estimate  
10 from the 2DVD was included for comparison. Statistical validation of the radar and 2DVD  
11 rainfall estimates for the different rainfall relations were performed for 18 rainfall events  
12 among the 33 rainfall cases. The mean absolute error (MAE) and the root-mean-square error  
13 (RMSE) are given by

$$MAE = \frac{1}{N} \sum |R_R - R_G| \quad [mm \ h^{-1}] \quad (12)$$

$$RMSE = \left( \frac{1}{N} \sum (R_R - R_G)^2 \right)^{0.5} \quad [mm \ h^{-1}] \quad (13)$$

14 where,  $R_R$  is the averaged one-hour rain rate [ $mm \ h^{-1}$ ] for the radar (or 2DVD), and  $R_G$  is the  
15 averaged one-hour rain rate [ $mm \ h^{-1}$ ] for the rain gauge. The results are presented in Table 4.

16 Rainfall estimation from the 2DVD showed good results in the following order:  
17  $R(K_{DP}, Z_{DR}) > R(Z_h, Z_{DR}) > R(K_{DP}) > R(Z_h)$ . According to the DSD statistics, the combined  
18 polarimetric rainfall relations using  $Z_{DR}$  and  $K_{DP}$  performed better than the single rainfall  
19 relation for estimated rainfall. As can be seen from Table 4,  $R(K_{DP}, Z_{DR})$  based on the new  
20 axis-ratio relation performed better on DSD statistics, with  $MAE = 0.61 \text{ mm hr}^{-1}$ , and  $RMSE$   
21  $= 0.86 \text{ mm hr}^{-1}$ . However, the  $R(K_{DP}, Z_{DR})$  algorithm showed the worst results for radar  
22 rainfall estimation, and the  $R(Z_h, Z_{DR})$  algorithm showed the best performance. These results  
23 can be found in Fig. 7, which shows a scatterplot of the one-hour rain rate from the rain  
24 gauge and the radar (or 2DVD) data, using the new axis-ratio relation for 18 rainfall events.  
25 The plus represents one-hour gauge rain rate versus radar rain rate from different rainfall  
26 relations and the square indicates gauge versus 2DVD rain rate.



1           According to the DSD results,  $K_{DP}$  is less sensitive to DSD variation and uncertainties  
2 in raindrop shapes; however, the accuracy of the rainfall estimation declined when the  $K_{DP}$   
3 parameter was used for radar rainfall estimation. Moreover, the radar rainfall estimations  
4 from  $R(K_{DP})$  and  $R(K_{DP}, Z_{DR})$  exceeded rainfall gauge measurements at lower rain rates ( $\leq 5$   
5  $\text{mm hr}^{-1}$ ), whereas rainfall estimations from  $R(Z_h, Z_{DR})$  were similar to rainfall by measured  
6 by gauges. In addition, the radar rainfall estimations from  $R(K_{DP})$  and  $R(K_{DP}, Z_{DR})$  perform  
7 better than those of  $R(Z_h, Z_{DR})$  for rain rates exceeding  $5 \text{ mm hr}^{-1}$ . In other words, as the rain  
8 rate increased, the uncertainty of  $K_{DP}$  from the radar declined. This was because  $K_{DP}$  is noisy  
9 in light rainfall. Thus, the  $R(K_{DP}, Z_{DR})$  relation is best used for heavy rainfall and  $R(Z_h, Z_{DR})$   
10 is suited for light rainfall.

11           In addition, the polarimetric rainfall relations based on the new axis-ratio relation also  
12 were better than the others. Although the difference in the value of the statistics seems small  
13 according to raindrop axis ratio relations, it has an effect on the accuracy of rainfall  
14 estimation. Therefore, rainfall characteristics should be reflected in polarimetric rainfall  
15 relations.

16

### 17 **4.2.3 Correction of calibration bias**

18           In this study, the calibration bias of  $Z_H$  and  $Z_{DR}$  was calculated for eight rainfall events,  
19 and the  $R(Z_h, Z_{DR})$  algorithm based on Eq. (4) was used to estimate rainfall. Figure 8 and 9  
20 shows comparison of the time series and scatter diagrams of  $Z_H$  and  $Z_{DR}$  for the 2DVD and  
21 BSL radar. The overall distribution of the observed  $Z_H$  corresponded well with the simulated  
22 parameter; however, the measured  $Z_{DR}$  at BSL was underestimated compared to the simulated  
23  $Z_{DR}$  value. The mean bias (= bias) of  $Z_H$  and  $Z_{DR}$  on 14 May 2012 was about 2.17 dBZ and  
24 0.28 dB, respectively (Fig. 8). The bias of  $Z_H$  and  $Z_{DR}$  on 23 August 2012 was 0.98 dBZ and  
25 0.10 dB (Fig. 9).

26           The accuracy of the radar rainfall estimation was investigated by applying calculated  
27  $Z_H$  and  $Z_{DR}$  bias. These results were evaluated by comparing with rain gauge measurements.  
28 Figure 10a shows the one-hour rain rate (left ordinate) and accumulated rainfall (right  
29 ordinate) estimated from the radar and rain gauge on May 14, 2012. The blue and green solid  
30 lines are estimated one-hour rainfall rates from before and after bias correction, and the bar  
31 graph is the one-hour rainfall rate measured by rain gauge. The blue and green dotted lines



1 are estimated accumulated rainfall from before and after bias correction, and the red dotted  
2 line is the accumulated rainfall by the rain gauge. In comparison with the rain gauge  
3 measurement, underestimated precipitation (12.67 mm) was corrected to 15.33 mm after bias  
4 correction. When the estimated rainfall was compared to the rain gauge as ground truth,  
5 rainfall estimation was improved about 13.71%. Figure 10b shows the results for the period  
6 00:00 to 23:59 UTC on August 23, 2012. The accumulated rainfall recorded was 83.86, 71.52,  
7 and 80.12 mm for the rain gauge, before bias correction, and after bias correction. Rainfall  
8 estimation was improved about 10.25%. For eight rainfall events, the total mean bias of  $Z_H$   
9 and  $Z_{DR}$  from the BSL radar was 1.03 dBZ and 0.22 dB, respectively. Moreover, MAE fell by  
10 1.03 to 0.93 mm hr<sup>-1</sup> and RMSE decreased by 1.41 to 1.26 mm hr<sup>-1</sup>. The bias of  $Z_H$  and  $Z_{DR}$ ,  
11 MAE and RMSE results for each of the eight rainfall events are presented in Table 5. As  
12 shown in Table 5, rainfall estimation tended to improve after bias correction.

13

## 14 5 Conclusion

15 The purpose of this study was to find an optimal polarimetric rainfall algorithm using  
16 2DVD measurement in Korea, and to improve rainfall estimation by correcting  $Z_H$  and  $Z_{DR}$   
17 calibration bias. First, we derived a new raindrop axis-ratio relation reflecting rainfall  
18 characteristics on the Korean peninsula, using data from 33 rainfall events, after checking the  
19 accuracy and quality control of the 2DVD measurements. The derived raindrop axis-ratio  
20 relation was compared with existing relations. Although the difference in relations seems  
21 small, its impact on the polarimetric rainfall algorithm cannot be neglected.

22 The polarimetric rainfall relations were derived based on various assumptions about the  
23 shape of raindrops, and the accuracy validation of one-hour rainfall rate for rainfall  
24 algorithms was conducted using 2DVD, BSL radar, and rain gauge. As a result,  $R(K_{DP}, Z_{DR})$   
25 based on the new axis-ratio relation was suited for rainfall estimation of the DSD statistic  
26 when compared with others. However, the  $K_{DP}$ -based algorithms had a large statistical error  
27 for radar rainfall estimation, and  $R(Z_h, Z_{DR})$  based on the new axis-ratio relation showed the  
28 best performance on BSL S-Band radar rainfall estimation. This was because the measured  
29  $K_{DP}$  parameter was weak at lower rain rates ( $\leq 5$  mm hr<sup>-1</sup>). To calculate the calibration bias of  
30 radar, measured  $Z_H$  and  $Z_{DR}$  were compared with those simulated. Calculated  $Z_H$  and  $Z_{DR}$  bias  
31 was used to reduce radar bias, and to produce more accurate rainfall estimation. After bias  
32 correction, rainfall estimated from radar was close to that measured using the rain gauge.



1           In this paper, different axis ratios of raindrops were used to derive new polarimetric  
2 rainfall relations, and the new polarimetric rainfall algorithms were assessed for point radar  
3 rainfall estimation. The effect of areal rainfall estimation and classification of rain rate on  
4 polarimetric rainfall relations will be studied in future work.  
5



## 1 **Acknowledgements**

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3 dual-pol radar harmonization (WRC-2013-A-1)" project of the Weather Radar Center, Korea  
4 Meteorological Administration.

5

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1 Table 1. Specification of dual-polarization radar in Bislan.

Parameters		Characteristics
Variables		$Z_H$ , $V_r$ , $SW$ , $Z_{DR}$ , $\Phi_{DP}$ , $K_{DP}$ , $\rho_{hv}$
Altitude of radar antenna		1085 m
Transmitter type		Klystron
Transmitter peak power		750 kW
Antenna diameter		8.5 m
Beam width of radar		0.95°
Frequency		2,785 MHz (S-band)
Observation	Range	150 km
	Gate size	125 m
	Elevations	-0.5°, 0°, 0.5°, 0.8°, 1.2°, 1.6° (6 elevation)

2  
 3  
 4  
 5  
 6  
 7  
 8  
 9



- 1 Table 2. Summary of the date, type of precipitation, and accumulated rainfall comparison
- 2 between 2DVD and rain gauge for the 33 rainfall events.

Date	Time of observation [UTC]	Type of Precipitation	Accumulated rainfall [mm]		PE [%]
			2DVD	Rain gauge	
`11.09.05	01:00-15:00	C	7.07	6.86	3.12
`11.09.09	15:20-21:20	S	4.26	4.31	1.17
`11.09.10	00:00-23:59	C	19.50	17.83	9.37
`11.09.29	00:00-17:00	S	3.81	3.72	2.38
`11.10.13	00:00-23:59	S	3.91	4.11	4.98
`11.10.14	00:00-09:00	S	13.14	13.52	2.81
`11.10.21	06:00-23:59	S	53.11	65.83	19.32
`12.04.02	14:00-23:59	M	17.79	16.26	9.42
`12.04.21	00:00-23:59	S	32.06	32.13	0.24
`12.04.25	00:00-08:00	S	18.57	17.83	4.16
`12.05.01	08:00-21:00	S	4.07	3.53	15.32
`12.05.08	07:00-11:00	C	8.98	9.60	6.50
`12.05.14	00:00-15:00	S	22.19	19.98	11.03
`12.05.28	06:00-07:00	C	15.26	14.50	5.22
`12.06.08	03:00-23:59	C	17.09	19.40	11.91
`12.06.23	00:00-08:00	C	13.48	14.50	7.05
`12.07.06	00:00-18:00	C	22.40	20.18	10.98
`12.07.12	17:00-21:00	M	7.49	7.45	0.58
`12.07.13	01:00-12:00	C	25.26	25.08	0.71
`12.07.15	00:00-12:00	C	8.22	7.64	7.55
`12.07.16	15:00-23:59	M	16.33	18.42	11.31
`12.07.21	09:00-10:30	C	5.85	5.68	2.99
`12.08.12	01:00-18:00	C	20.27	18.42	10.08
`12.08.13	00:00-15:00	C	37.19	34.09	9.10
`12.08.23	00:00-23:59	M	90.47	83.86	7.88
`12.08.24	00:00-23:59	S	7.32	7.45	1.64
`12.08.27	16:00-23:59	S	13.57	12.54	8.25
`12.08.29	19:00-23:59	S	6.23	5.29	17.72
`12.09.09	00:00-23:59	S	21.45	18.65	15.04
`12.09.16	00:00-23:59	S	82.68	69.88	18.32
`12.09.17	00:00-07:00	M	63.51	58.55	8.47
`12.10.22	06:00-11:00	M	13.60	14.92	8.81
`12.10.27	00:00-09:00	S	8.74	8.20	6.53



1 Table 3. List of different polarimetric rainfall relations used for rainfall estimation and MAE,  
 2 RMSE and correlation coefficient for estimated rain rate vs observations.

$R(Z_h) = \alpha  Z_h ^\beta$							
Polarimetric rainfall relation			Scatterplot R-R <sub>e</sub>			Assumptions	
$\alpha$	$\beta$		MAE	RMSE	Corr.		
1	0.0558	0.5894	0.96	2.39	0.93	Pruppacher and Beard (1970)	
2	0.0576	0.5867	0.96	2.41	0.92	Beard and Chuang (1987)	
3	0.0577	0.5871	0.96	2.41	0.92	Brandes et al. (2002)	
4	0.0565	0.5889	0.96	2.40	0.93	New axis ratio (Experimental fit)	
$R(K_{DP}) = \alpha  K_{DP} ^\beta$							
Polarimetric rainfall relation			Scatterplot R-R <sub>e</sub>			Assumptions	
A	B		MAE	RMSE	Corr.		
1	38.66	0.837	0.46	1.04	0.99	Pruppacher and Beard (1970)	
2	43.77	0.768	0.66	1.42	0.97	Beard and Chuang (1987)	
3	46.97	0.743	0.82	1.63	0.97	Brandes et al. (2002)	
4	42.28	0.833	0.45	1.14	0.98	New axis ratio (Experimental fit)	
$R(Z_h, Z_{DR}) = \alpha Z_h^\beta 10^{0.1\gamma Z_{DR}}$							
Polarimetric rainfall relation			Scatterplot R-R <sub>e</sub>			Assumptions	
$\alpha$	B	$\gamma$	MAE	RMSE	Corr.		
1	0.0110	0.89	-4.0808	0.45	0.77	0.99	Pruppacher and Beard (1970)
2	0.0091	0.88	-3.5197	0.46	0.83	0.99	Beard and Chuang (1987)
3	0.0088	0.88	-3.4789	0.47	0.85	0.99	Brandes et al. (2002)
4	0.0112	0.87	-3.7613	0.48	0.89	0.99	New axis ratio (Experimental fit)
$R(K_{DP}, Z_{DR}) = \alpha K_{DP}^\beta 10^{0.1\gamma Z_{DR}}$							
Polarimetric rainfall relation			Scatterplot R-R <sub>e</sub>			Assumptions	
$\alpha$	$\beta$	$\gamma$	MAE	RMSE	Corr.		
1	66.23	0.96	-1.3859	0.29	0.44	0.10	Pruppacher and Beard (1970)
2	83.78	0.93	-1.6703	0.44	0.66	0.10	Beard and Chuang (1987)
3	96.37	0.92	-1.8938	0.58	0.85	0.99	Brandes et al. (2002)
4	74.54	0.97	-1.5328	0.23	0.35	0.10	New axis ratio (Experimental fit)



1 Table 4. Mean absolute error and root mean square error of the radar estimates of hourly rain  
 2 rate for the different radar rainfall algorithms listed in Table 3.

$R(Z_H)=\alpha Z_H ^\beta$					
	MAE		RMSE		Assumptions
	RADAR	2DVD	RADAR	2DVD	
1	1.02	0.95	1.38	1.23	Pruppacher and Beard (1970)
2	1.03	0.96	1.39	1.24	Beard and Chuang (1987)
3	1.03	0.96	1.39	1.24	Brandes et al. (2002)
4	1.02	0.95	1.39	1.23	New axis ratio (Experimental fit)
$R(K_{DP})=\alpha K_{DP} ^\beta$					
	MAE		RMSE		Assumptions
	RADAR	2DVD	RADAR	2DVD	
1	6.04	0.68	6.98	0.92	Pruppacher and Beard (1970)
2	7.69	0.74	8.63	0.99	Beard and Chuang (1987)
3	8.67	0.75	9.62	1.00	Brandes et al. (2002)
4	6.80	0.70	7.79	0.92	New axis ratio (Experimental fit)
$R(Z_H, Z_{DR})=\alpha Z_H^\beta 10^{0.1\gamma Z_{DR}}$					
	MAE		RMSE		Assumptions
	RADAR	2DVD	RADAR	2DVD	
1	0.88	0.65	1.20	0.90	Pruppacher and Beard (1970)
2	0.86	0.67	1.19	0.93	Beard and Chuang (1987)
3	0.87	0.71	1.21	0.99	Brandes et al. (2002)
4	0.84	0.71	1.17	0.97	New axis ratio (Experimental fit)
$R(K_{DP}, Z_{DR})=\alpha K_{DP}^\beta 10^{0.1\gamma Z_{DR}}$					
	MAE		RMSE		Assumptions
	RADAR	2DVD	RADAR	2DVD	
1	8.56	0.62	10.03	0.88	Pruppacher and Beard (1970)
2	11.33	0.65	13.01	0.91	Beard and Chuang (1987)
3	13.16	0.68	15.01	0.94	Brandes et al. (2002)
4	9.61	0.61	11.23	0.86	New axis ratio (Experimental fit)

3

4

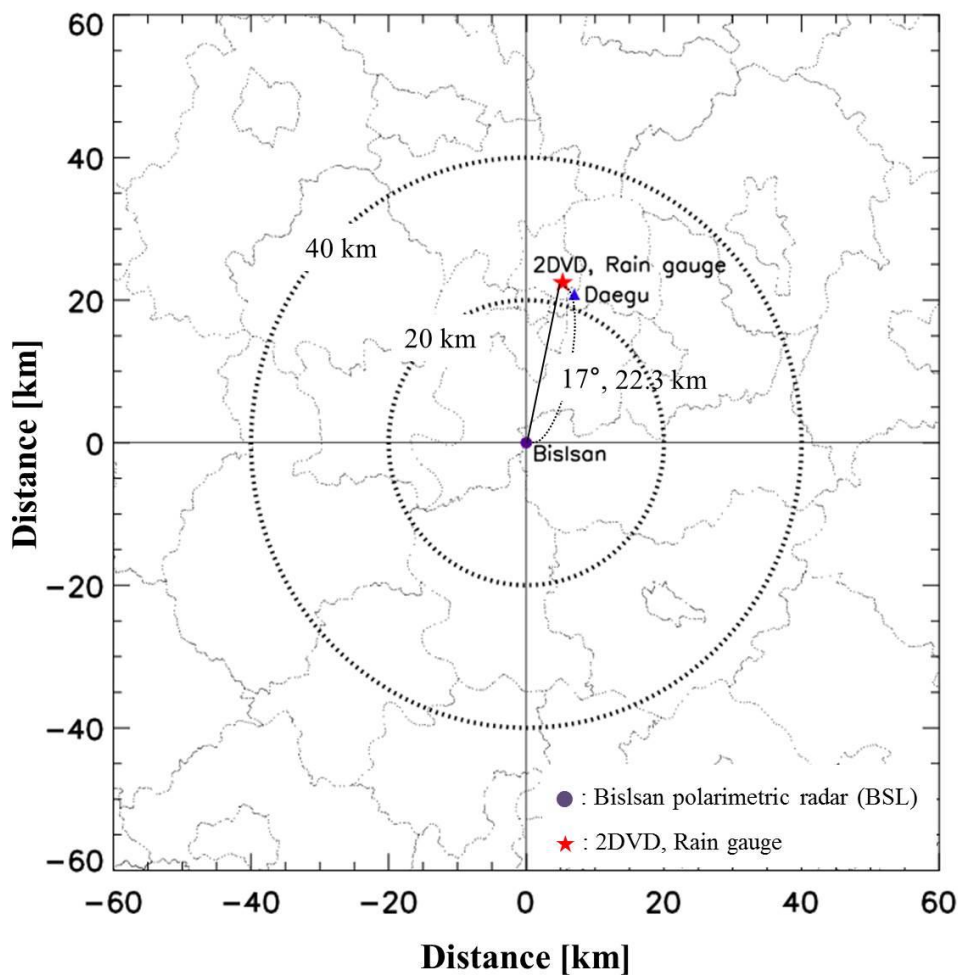


1 Table 5. Mean absolute error and root mean square error of rainfall estimates before and after  
 2 applying bias correction.

Date	Type of precipitation	Calibration Bias		MAE [mm hr <sup>-1</sup> ]		RMSE [mm hr <sup>-1</sup> ]		
		Z <sub>h</sub> [dBZ]	Z <sub>DR</sub> [dB]	Before BC	After BC	Before BC	After BC	
1	11.10.13	S	-0.01	0.10	0.48	0.38	0.59	0.47
2	10.21	S	1.16	0.28	0.75	0.74	0.98	0.97
3	12.04.25	S	1.40	0.43	1.31	1.26	2.00	1.89
4	05.14	S	2.17	0.28	0.58	0.43	0.80	0.59
5	08.23	M	0.98	0.10	0.80	0.64	1.33	0.91
6	09.09	S	0.44	0.18	0.73	0.67	1.16	1.07
7	09.16	S	0.90	-0.13	0.77	0.71	0.95	0.92
8	10.22	M	-1.44	-0.14	2.83	2.58	3.47	3.29
Avg			1.03	0.22	1.03	0.93	1.41	1.26

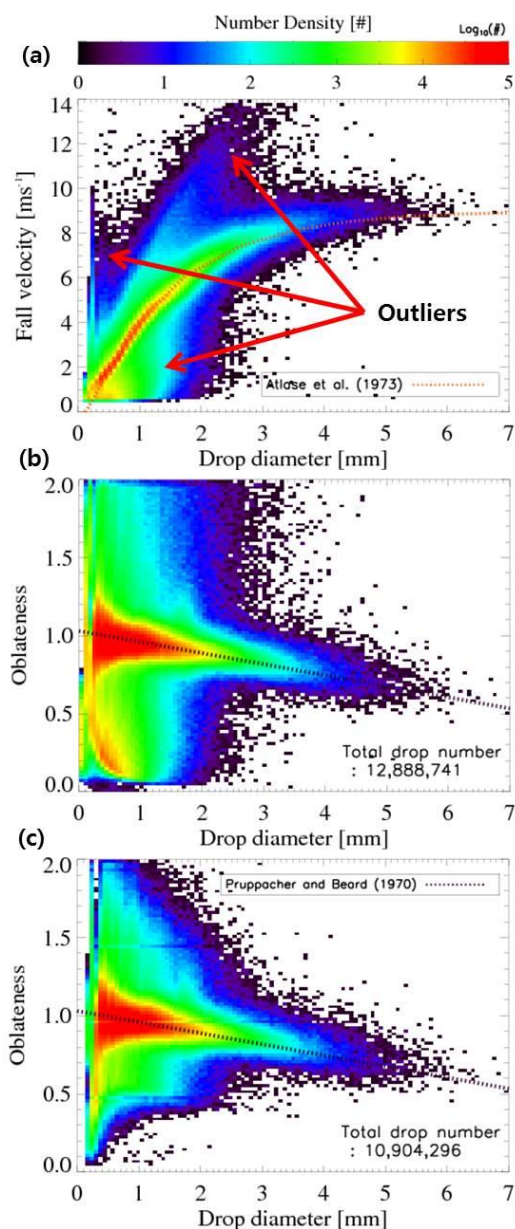
3

\* BC : Bias Correction



1

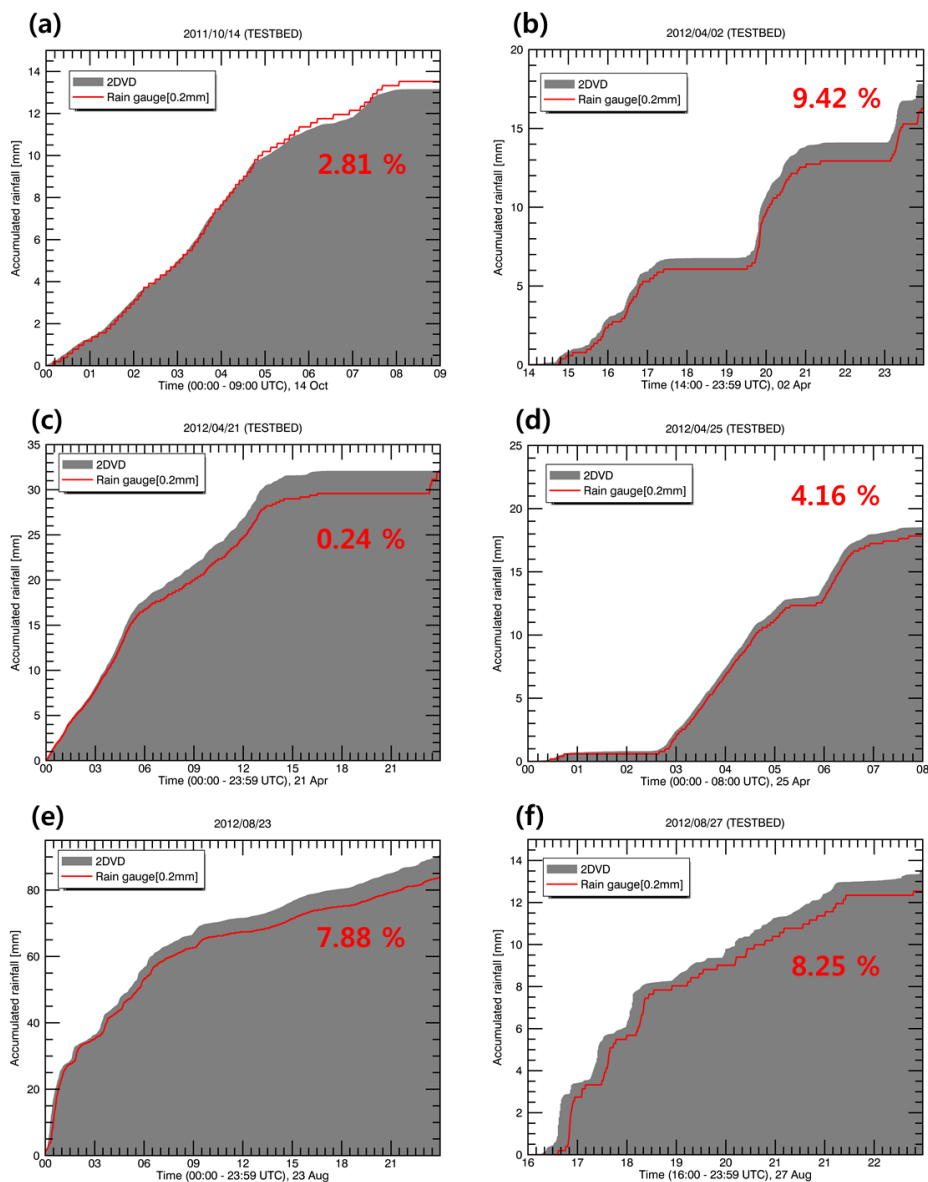
2 Figure 1. The location of the Bislsan polarimetric radar and the 2DVD with rain gauge site.



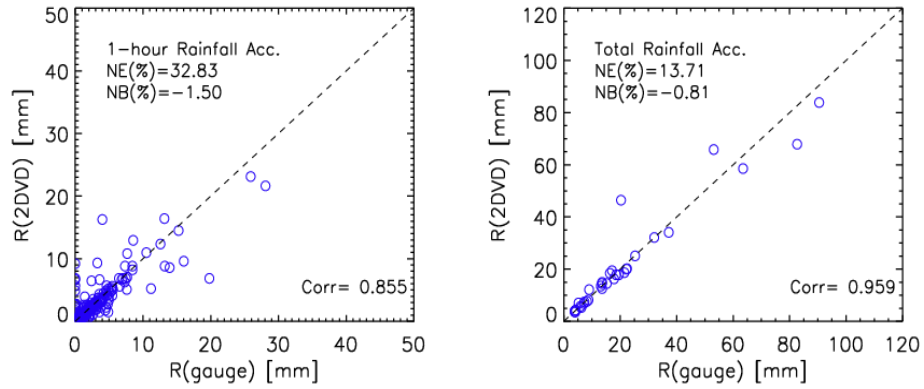
1

2 Figure 2. Distribution of fall velocity and oblateness according to drop diameter. (a) Velocity-  
3 based filter for the drop measurements. The color scale represents drop number density (log  
4 scale). (b) Drop axis ratios for all measured drops. (c) Drop axis ratios after removing  
5 mismatched drops.

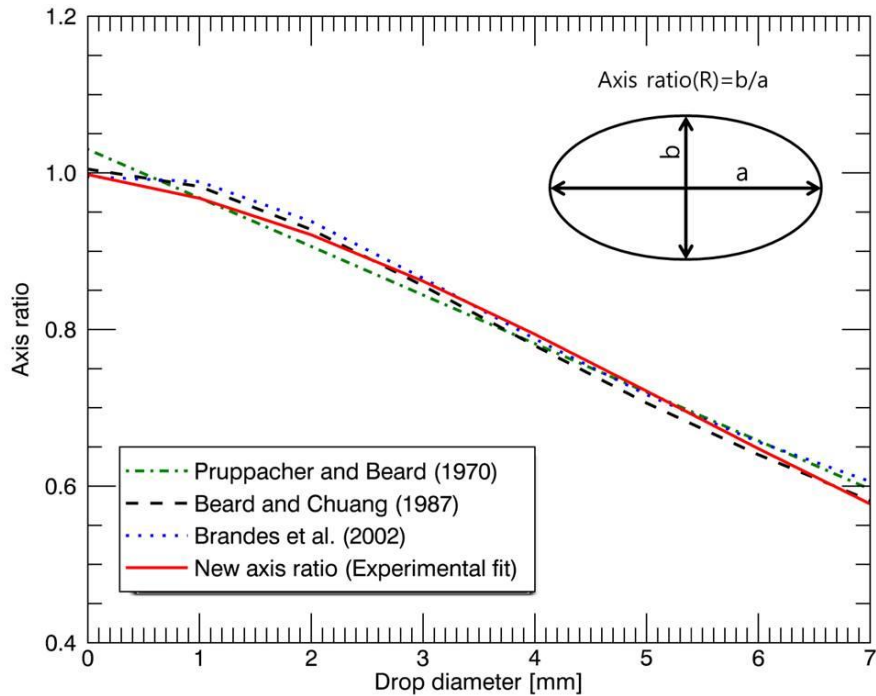




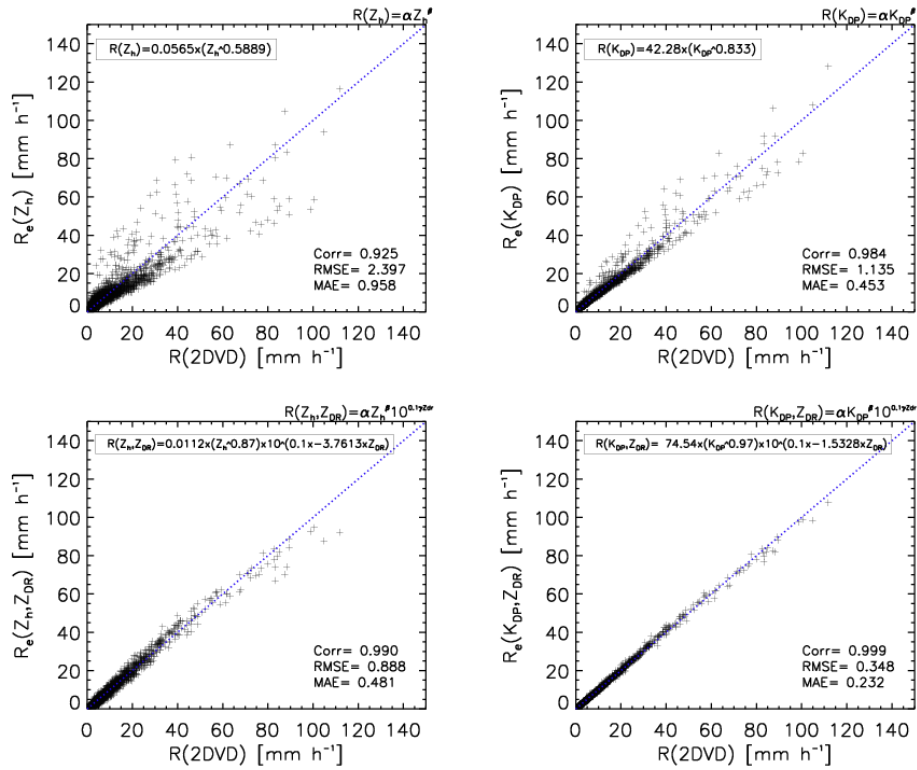
1  
2 Figure 3. Time series of accumulated rainfall measured from the rain gauge and estimated  
3 from the 2DVD: (a) 14 October 2011, (b) 2 April 2012, (c) 21 April 2012, (d) 25 April 2012.  
4 (e) 23 August 2012, and (f) 27 August 2012.



1  
 2 Figure 4. One-hour (left) and total accumulated rainfall (right) of 2DVD and rain gauge for  
 3 the 33 rainfall cases.

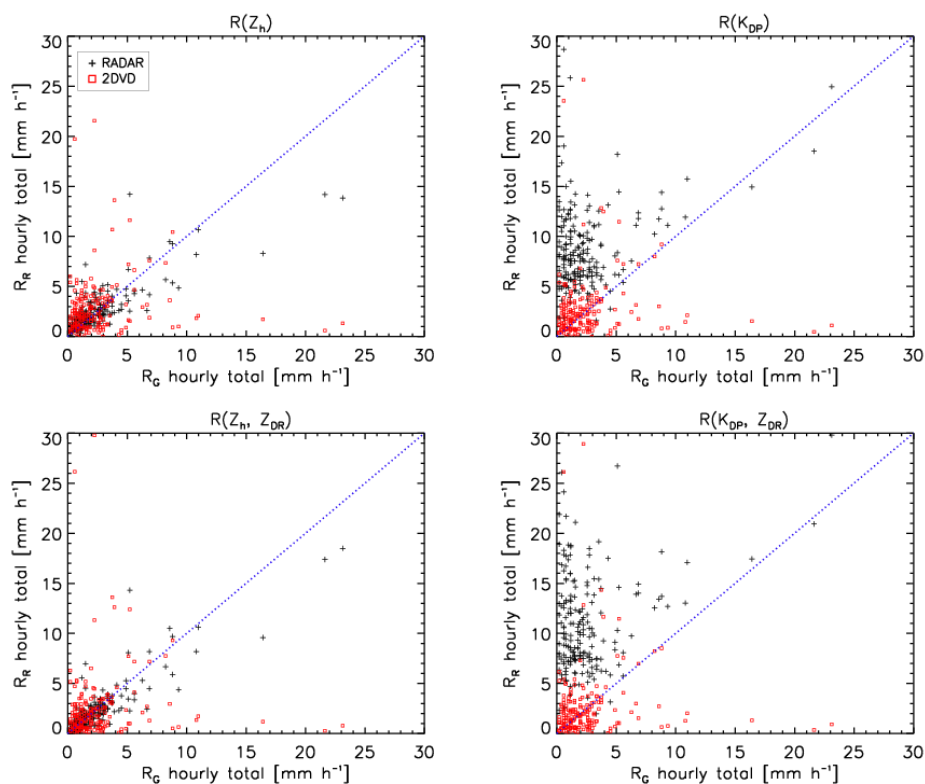


4  
 5 Figure 5. Different raindrop axis ratio relations for the oblate raindrop model. The upper right  
 6 subfigure illustrates the axis ratio of an oblate raindrop.

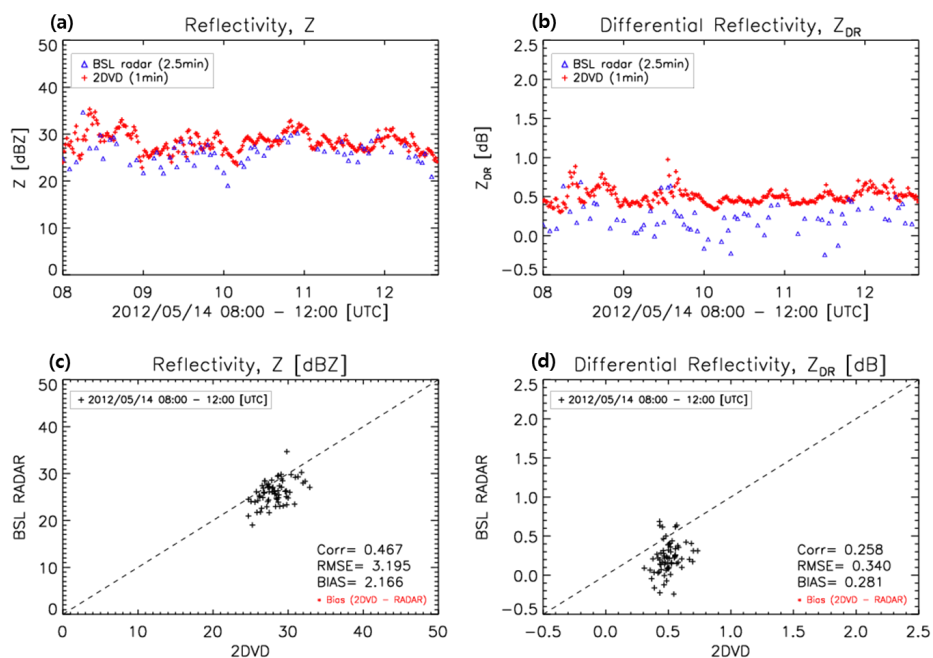


1

2 Figure 6. Scatterplot of R derived from observed DSDs of 17,618 min and  $R_e$  estimated from  
 3 combinations of polarimetric parameters.  $R_e$  is then obtained from the same dataset.

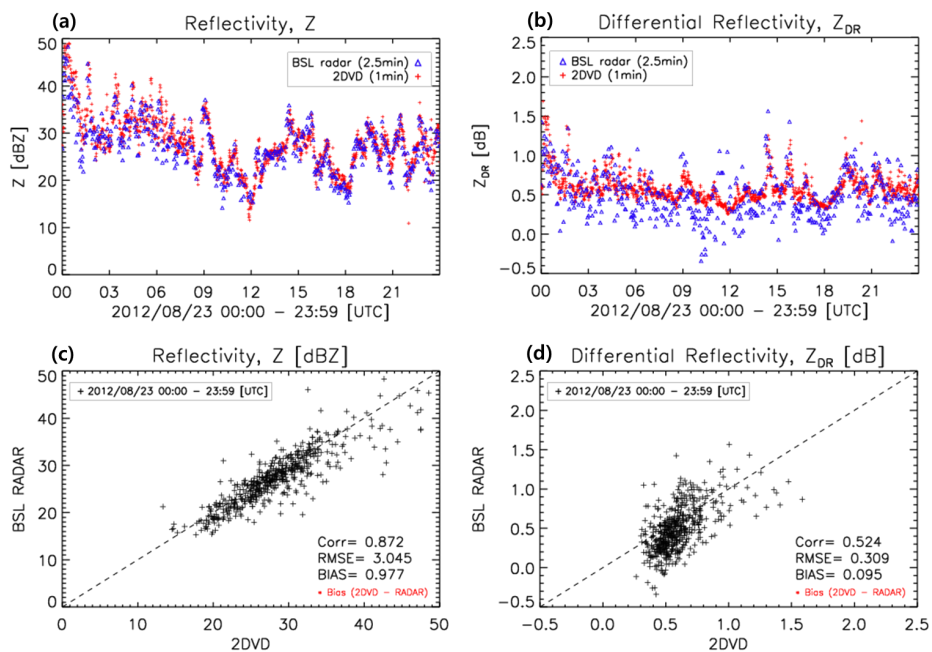


1  
 2 Figure 7. Scatter plot of one-hour rain rate from rain gauge ( $R_G$ ) and BSL S-Band radar (or  
 3 2DVD) based on Eq. (4) for 18 rainfall cases: The pluses represents one-hour gauge rain rate  
 4 versus radar hourly rain rate from polarimetric rainfall algorithms, and squares indicate gauge  
 5 and 2DVD rain rate by different polarimetric rainfall algorithms.



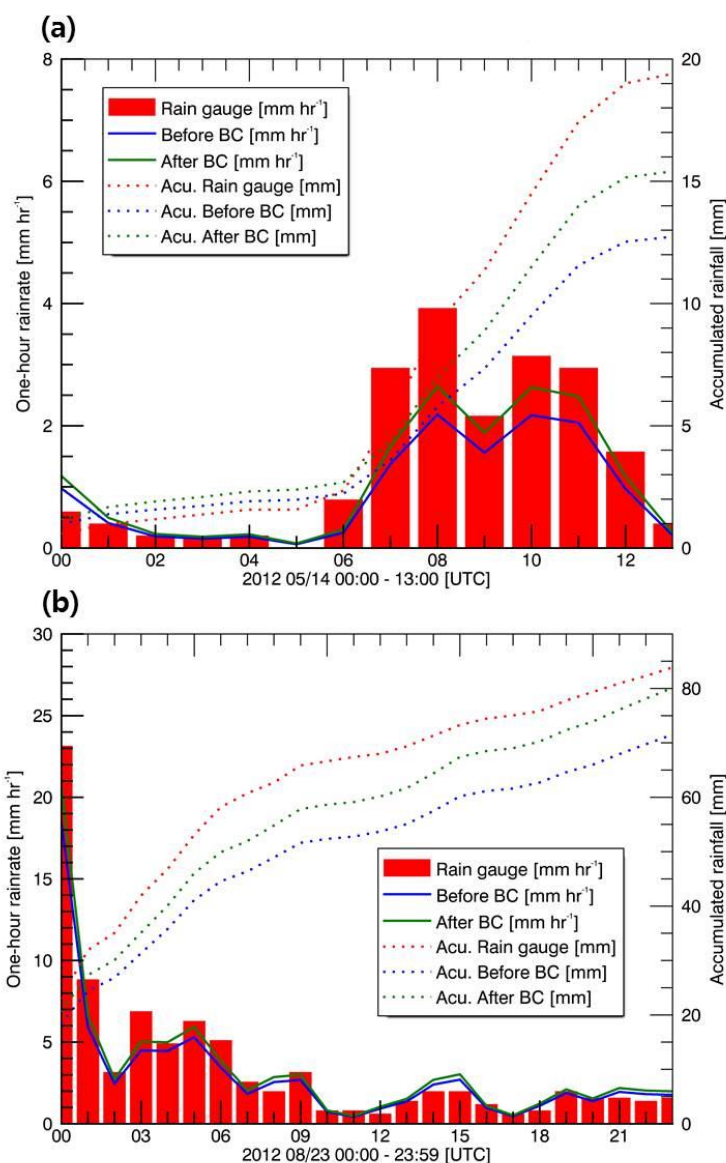
1

2 Figure 8. Time series of the (a) reflectivity, and (b) differential reflectivity by 2DVD and BSL  
3 S-Band radar: Scatter Plots of the 2DVD estimation and radar measurement for the (c)  
4 reflectivity and (d) differential reflectivity. Comparison statistics including correlation  
5 coefficient (Corr), RMSE, and bias are also presented (14 May 2012).



1

2 Figure 9. Same as Fig. 8, except that the data is for 23 August 2012.



1

2 Figure 10. Comparison of the one-hour rain rate (left ordinate) and accumulated rainfall (right  
 3 ordinate) obtained by BSL S-Band radar and rain gauge: The  $R(Z_H, Z_{DR})$  algorithm based on  
 4 Eq. (4) was used for rainfall estimation for (a) 14 May 2012 and (b) 23 August 2012. BC  
 5 represents Bias Correction.