



1	Exploring the potential of utilizing high resolution X-band radar for
2	urban rainfall estimation
3	Wen-Yu Yang ¹ , Guang-Heng Ni ¹ , You-Cun Qi ^{2,3} , Yang Hong ^{1,4} , Ting Sun ^{1*}
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5	1) State Key Laboratory of Hydro-Science and Engineering, Department of Hydraulic
6	Engineering, Tsinghua University, Beijing 100084, China
7	2) Cooperative Institute for Mesoscale Meteorological Studies, University of Oklahoma
8	3) NOAA/OAR/National Severe Storms Laboratory, Norman, Oklahoma
9	4) Department of Civil Engineering and Environmental Science, University of
10	Oklahoma, Norman, Oklahoma
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12	
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16	* Corresponding Author: sunting@tsinghua.edu.cn





17 Abstract:

18	X-band-radar-based quantitative precipitation estimation (QPE) system is increasingly
19	gaining interest thanks to its strength in providing high spatial resolution rainfall
20	information for urban hydrological applications. However, prior to such applications, a
21	variety of errors associated with X-band radars are mandatory to be corrected. In
22	general, X-band radar QPE systems are affected by two types of errors: 1) common
23	errors (e.g. mis-calibration, beam blockage, attenuation, non-precipitation clutter,
24	variations in the raindrop size distribution) and 2) "wind drift" errors resulting from
25	non-vertical falling of raindrops. In this study, we first assess the impacts of different
26	corrections of common error using a dataset consisting of one-year reflectivity
27	measurements collected at an X-band radar site and a distrometer along with rainfall
28	measurements in Beijing urban area. The common error corrections demonstrate
29	promising improvements in the rainfall estimates, even though an underestimate of 24.6%
30	by the radar QPE system in the total accumulated rainfall still exists as compared with
31	gauge measurements. The most significant improvement is realized by beam
32	integration correction. The DSD-related corrections (i.e., convective-stratiform
33	classification and local Z-R relationship) also lead to remarkable improvement and
34	highlight the necessity of deriving the localized Z - R relationships for specific rainfall
35	systems. The effectiveness of wind drift correction is then evaluated for a fast-moving
36	case, whose results indicate both the total accumulation and the temporal characteristics
37	of the rainfall estimates can be improved. In conclusion, considerable potential of X-
38	band radar in high-resolution rainfall estimation can be realized by necessary error





- 39 corrections.
- 40 Keywords: urban hydrology, X-band radar, quantitative precipitation estimation, error
- 41 correction, wind drift effect





42 **1. Introduction**

43 Urban flash flooding is one of the most severe hazards in cities (Schmitt et al., 2004; Yang et al., 2015a). Large coverage of impervious surfaces in cities will exaggerate the 44 flooding since heavy rainfall is more likely to transform into runoff instead of 45 infiltrating into the soil. To mitigate its detrimental effects, accurate prediction of runoff 46 at high spatiotemporal resolution is critical for emergency management and warning 47 48 operations. When conducting the hydrological and/or hydraulic simulations, the 49 spatiotemporal variability of rainfall is known to be the major source of a range of 50 uncertainties (Schellart et al., 2012; Schröter et al., 2015; Rafieeinasab et al., 2015; Rico-Ramirez et al., 2015), which thus warrants compelling need for high-resolutions 51 rainfall data (Schilling, 1991; Emmanuel, et al., 2012; Eldardiry et al., 2015). 52

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Weather radars have been worldwide recognized as essential tools to provide high-54 resolution rainfall measurements (Smith and Krajewski, 1991; Krajewski and Smith, 55 2002; Li et al., 2014; Li et al., 2015). The current operational weather radar systems 56 57 (e.g., NEXRAD in America, OPERA in Europe) based on C-band and/or S-band radars operating on long-range coverage. However, their spatiotemporal resolutions of 1 58 km/5-10 min are insufficient to support accurate estimations of precipitation variability 59 in urban area (Krajewski et al., 2002; Smith et al., 2007). For instance, recent studies 60 61 suggest that for urban areas less than 1 ha, rainfall input is required at the spatial resolution of ~ 100 m; while for urban areas between 1 ha and ~ 100 ha, the required 62 resolution is relaxed to 500 m (Faures et al., 1995; Berne et al., 2004). Considering the 63





- 64 high utility in monitoring rainfall in urban area, X-band radars are being deployed in a
- number of hydrometeorological applications (Chen and Chandrasekar, 2015).
- 66

Prior to the application of radar-based rainfall product in hydrological simulations, 67 68 quantitative precipitation estimation (QPE) systems are mandatory to be established, where multiple error sources should be appreciated (e.g. Krajewski and Smith, 2002; 69 70 Villarini and Krajewski, 2010). One of the error sources is associated with the 71 reflectivity measurement, which can be attributable to mis-calibration, beam blockage, 72 attenuation, non-precipitation clutter, and vertical profile of reflectivity (VPR). These errors may reduce the accuracy of reflectivity measured by weather radar (Germann et 73 al., 2006; Hazenberg et al., 2011a). The variability of Z-R relationship is another 74 75 important error source. The standard Z-R relationship (Chapon et al., 2008; Hazenberg et al., 2011b) takes the form of $Z = aR^{b}$ (Marshall and Palmer, 1948), in which the 76 parameters a and b depend on the raindrop size distribution (DSD). Inappropriate 77 determination of a and b will introduce errors into the estimated rainfall. The above 78 79 errors are termed as common errors in this study as they have to be corrected for most operational radars. 80

81

Besides the common errors, the rainfall estimates for X-band radar can be affected by other weather-related dynamic processes. For instance, the falling paths of raindrops are not perfectly vertical due to wind, implying a horizontal displacement may exist between the aloft measurement position and ground falling location of a raindrop, or





86	the "wind drift". The wind drift can lead to inconsistency between the estimated and
87	actual rainfall fields at the ground level (Fabry et al., 1994; Liu and Krajewski, 1996;
88	Sandford., 2015; Seo and Krajewski, 2015). Usually the wind drift is ignored for the S-
89	band and C-band radars due to their relatively coarse spatial resolution. However, this
90	effect can be remarkable for X-band radars given its high spatial resolution of ~100 m,
91	in particular under windy conditions that are common for convective rainfall events
92	(Sandford, 2015; Seo and Krajewski, 2015). As such, errors due to the wind drift should
93	be appreciated in the application of X-band radars in urban hydrometeorology.

94

In order to improve the quality of X-band radar based QPE systems in urban 95 hydrometeorological applications, different procedures have been explored to reduce 96 97 the aforementioned errors. Current research on X-band radar shows that using the differential phase shift can reliably resolve the attenuation which is the primary 98 disadvantage of X-band radar (Anagnostou et al., 2004, 2006a,b; Park et al., 2005; 99 Kalogiros et al. 2014). Specifically, Kalogiros et al. (2014) developed an algorithm to 100 101 correct the attenuation of horizontal-polarization reflectivity by using an iterative optimal parameterizations of specific differential attenuation and backscattering phase 102 shift. Besides the attenuation, Van de Beek et al. (2010) suggested that the effects of 103 non-precipitation clutter should also be carefully addressed for applications of X-band 104 105 radars in urban areas. Lo Conti et al. (2015) investigated the effect of calibration in the Z-R relationship of an X-band radar in Palermo (Italy), suggesting the high variability 106 of the Z-R relationships determined for specific events limited its wide applicability. 107





Matrosov et al. (2016) found no bright band rainfall has distinct Z-R relationship from 108 109 those of other rain types and should be distinguished from stratiform rainfall. For operational applications, Anagnostou et al. (2010) showed that adjusting the Z-R110 relationship for mean-field bias with the K_{DP} -R estimates as reference is a promising 111 technique for acquiring unbiased high resolution radar-rainfall estimates. Maki et al. 112 (2010) developed one X-band radar QPE system for three major metropolitan areas in 113 114 Japan, which may still underestimate the rainfall by $\sim 20\%$ compared with the gauge 115 measurement even though the effects due to non-precipitation clutter, beam blockage 116 and attenuation have been accounted for. Chen and Chandrasekar (2015) developed a high-resolution (250 m/1 min) QPE system in Dallas–Fort Worth urban area consisting 117 of polarimetric Weather Surveillance Radar 88 Doppler (WSR-88D) and X-band radars, 118 which demonstrated low overall biases and normalized standard errors in rainfall 119 accumulation products of different temporal scales (5-60 min). Although these studies 120 demonstrate the effectiveness of different measures in improving the X-band-radar-121 based QPE systems, the relative importance of different error sources contributing to 122 123 the overall errors remains to be unknown. Furthermore, given the errors of a specific radar QPE system strongly depend on the spatiotemporal characteristics of the local 124 rainfall system, an analysis of long-term rainfall characteristics is expected to enable a 125 better understanding of the potential of X-band-radar-based QPEs in urban 126 127 hydrometeorological applications.

128

129 In this study, we use a dataset consisting of one-year measurements by an X-band radar





- in Beijing to explore its potential in high resolution rainfall estimation. The study period
- 131 extends from July 2014 to September 2015 with 43 rainfall events. Specifically, we aim
- to answer the following two questions: 1) What is the relative importance of different
- error sources for the overall accuracy of a QPE in urban area; 2) What are the impacts
- 134 of wind drift on the ground-level rainfall estimation?
- 135
- 136 The paper is organized as follows. Section 2 describes the study area and the dataset.

Section 3 details the correction procedures for common error sources and wind drift in
X-band-radar-based QPEs. The relative importance of correcting each common error
for rainfall estimation is discussed in Section 4, followed by a case study to show the

- 140 implication of wind drift correction. Finally, the concluding remarks are provided in
- 141 Section 5.
- 142

143 2. Study Area and Data Description

Beijing, the capital city of China with more than 21 million residents, features complex topography, with mountains to its north and west and a highly urbanized area in its eastern part. Beijing is prone to summertime heavy rainfall events that occasionally lead to severe flash floods (Yang et al., 2014b).

148

The dataset used in this study consists of one-year measurements by a single-polarized
X-band radar (Fig. 1a, hereafter referred as Beijing Radar) in the northwest of Beijing.
Technical specifications of the Beijing X-band radar are given in Table 1. A full





- volumetric scanning by the Beijing Radar is performed every 7 min at 14 elevations
 (0.5°, 0.9°, 1.3°, 1.8°, 2.4°, 3.1°, 4.0°, 5.1°, 6.4°, 8, 10.0°, 12.0°, 15.6°, and 19.5°). Each
 scan has 400 gates along the beam with a gate resolution of 90 m and a maximum range
 of 36 km.
- 157 An OTT Parsivel disdrometer (Fig. 1b) deployed near the Beijing Radar (within 5 km,
- cf. Fig. 2) and a gauge network consisting of 8 standard tipping-bucket gauges (Fig. 2)
- are used to validate the QPE system for Beijing Radar. The disdrometer can archive 32
- 160 equivalent diameter classes (ranging from 0 to 26 mm with varying diameter increments
- 161 between 0.125 and 3 mm) and 32 different velocity classes at 1-min resolution. Other
- specifications of the disdrometer are provided in Table 2.
- 163
- In order to avoid the temporal bias among radar, disdrometer and rain gauge measurements, all the measurements are conformed at 1-h resolution for subsequent analysis. We note that the bias correction by assimilating gauge data were not performed in this study due to its shadow effect over the corrections in radar QPE system (Hazenberg et al., 2011a).

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170 3. Rainfall estimation algorithm

171 **3.1 Procedures for common error corrections**

The common errors introduced in reflectivity measurement are mostly due to radarmiscalibration, non-precipitating echo contamination, signal attenuation, beam





blockage and VPR, whereas the errors in *Z-R* conversion rely on the variability in *Z-R*relationships for different rainfall types. We note that the errors due to VPR are not
considered for two reasons: 1) the lack of required a priori knowledge of vertical profile
of rainfall in Beijing and 2) the minimal influence of VPR in this study since the
maximum effective measurement height of 2.5 km of Beijing Radar is lower than the
melting layer height of ~4 km for the warm-season rainfall (Cao and Qi, 2014).

180

181 **3.1.1 Radar calibration**

Radar calibration is conducted to fix the inappropriate parameter settings. Although the Beijing Radar has been calibrated before installation, post-installation calibration should be conducted to cancel the possible aging and thermal effects (Collier, 1989). Among all the available calibration approaches (Manz et al., 2000), calibration with disdrometer data would be the most straightforward one (Lee and Zawadzki, 2006). With the help of a nearby disdrometer (cf. Fig. 2 for its location), Beijing Radar is calibrated by comparing the radar measurements with disdrometer measurements.

189 The disdrometer-based estimate of *Z* can be expressed as (Delrieu et al., 1999):

$$Z = \frac{10^{6}\lambda^{4}}{\pi^{5}|K|^{2}} \int_{0}^{\infty} \sigma_{B}(D)N(D)dD,$$
 (1)

190 where λ is the operational wavelength of the radar (3.21 cm in this study), $|K|^2$ a 191 coefficient dependent on the dielectric constant of water. Assuming a raindrop is a 192 sphere of diameter *D* (cm), DSD spectra *N*(*D*) (cm⁻⁴) is defined as the raindrop 193 concentration in a given air volume as a function of *D* and $\sigma_B(D)$ is the backscattering





- 194 cross-section area (cm²) as a function of *D*. Note that the Mie calculation is adopted in 195 this study since the Rayleigh approximation does not satisfy the condition $D \le \lambda/16$ 196 when $\lambda = 3.21$ cm.
- 197

198 The comparison of the reflectivity measurement between radar and disdrometer demonstrates overall consistency with observed underestimates by radar for reflectivity 199 exceeding 35 dBZ (an example for the comparison of the 1th September 2014 event is 200 201 shown in Fig. 3). Except for the calibration error, this underestimation may be the joint 202 effect of attenuation and inconsistency between the ground-level point measurements and the aloft volume measurements. Therefore, although there is a calibration drift for 203 the Beijing Radar, it was decided not to apply any correction to the reflectivity 204 205 measurements for the 43 selected events.

206

207 3.1.2 Non-precipitating echo removal

Radar echoes may be contaminated by non-precipitating echoes that need to be 208 209 identified and removed before rainfall estimation. Ground clutters and anomalous propagations are the two main sources of non-precipitating echoes (Steiner and Smith, 210 2002). Ground clutters are caused by scattering in the antenna sidelobes hitting the 211 ground close to the radar site as well as by fixed objects (Villarini and Krajewski, 2010). 212 213 Anomalous propagations are contamination of radar reflectivity data from echoes normally not seen by the radar. In particular, anomalous propagations remain a serious 214 problem for situations when they are embedded in precipitation echoes (Steiner and 215





- 216 Smith, 2002).
- 217

For Beijing Radar, the ground clutter effect is corrected by removing the echoes with 218 radial Doppler velocity close to zero. As the more advanced polarimetric techniques 219 220 cannot be applied to the measurements by the Beijing Radar, the well-recognized Steiner and Smith (2002) algorithm is used for detecting anomalous propagations (e.g., 221 222 Hazenberg et al., 2011a, Hazenberg et al., 2014). This algorithm utilizes the three-223 dimensional reflectivity structure and builds upon three key parameters: the vertical 224 extent of radar echoes, their spatial variability and vertical gradient of intensity, which are available in the Beijing Radar measurements. 225

226

227 3.1.3 Attenuation correction

Radar signals can be attenuated during propagation (Atlas and Banks, 1951), in particular for X-band radars running at short wavelengths. For single-polarized radars, correction algorithms can be categorized into forward and backward algorithms (Delrieu et al., 1999). Among the forward algorithms, the HB algorithm (Hitschfeld and Bordan, 1954) is widely applied and thus adopted in this study for attenuation correction, whose key steps are recapitulated here.

234

235 For a well calibrated radar without blind-range attenuation (e.g. radome attenuation),

236 its measured reflectivity Z_m can be expressed as:

$$Z_m(r) = Z(r)A(r),$$
(2)





- 237 where Z(r) is the true reflectivity at the same range and A(r) =238 $\exp\left(-\frac{2\ln(10)}{10}\int_0^r k(s)ds\right)$ is the path-integrated attenuation (PIA) factor with the
- specific attenuation k(s) at a distance *s* being the only unknown to resolve.
- 240
- 241 Meanwhile the relationship between the true reflectivity Z and the specific attenuation
- 242 k can be given by:

$$Z = ck^d, (3)$$

where *c* and *d* are the DSD related parameters. Therefore, by canceling *k*, the relationship between $Z_m(r)$ and Z(r) can be obtained as follows:

$$Z(r) = \frac{Z_m(r)}{\left(1 - \frac{2\ln(10)}{10} \int_0^r \left(\frac{Z_m(s)}{c}\right)^{\frac{1}{d}} ds\right)^{d'}}$$
(4)

where the parameters c and d can be determined by Z-k regression (Eq.3) with distrometer measurements. To avoid the numeric instability known in the HB algorithm, a maximum PIA of 10 dB is specified in this study.

- 248
- Also, knowing the DSD, *k* can be calculated by:

$$k = c_k \int_0^\infty Q_t(D) N(D) dD, \tag{5}$$

where *D* (cm) denotes the raindrop diameter, Q_t (cm²) the Mie total attenuation cross sections (refer to Delrieu et al. (1999) for the calculation method of Q_t), *N* (cm⁻⁴) the raindrop concentration in a given air volume and $c_k = 0.4343 \times 10^6$ a constant.

254 By conducting Z-k regression (Eq. 3) with distrometer measurements from July 2014





to September 2015 without differentiating rainfall types (Fig. 4), the required parameters for Z_m -Z relationship (Eq.4) are determined as $c = 1.12 \times 10^5$ and d =

257 1.1.

258

259 3.1.4 Beam Integration

Due to the presence of obstructions on the beam path in terrain-complex contexts (e.g. urban, mountainous areas), beam blockage frequently occurs and thus compromise the accuracy of radar QPE. In particular, considering the radar are usually operated at the low elevation angles where more ground clutters exist, removal of beam blockage effect is of great importance for radar QPE systems. As such, beam integration, a technique to avoid the beam blockage by integrating measurements at different elevations for different azimuths, is conducted in this study.

267

In this study, the starting integral elevation, or the lowest optimal elevation, for a specific azimuth range is determined as the lowest elevation that at which the beam blockage of all ranges in this azimuth range must be less than 50% (cf. Fig. 2 for the starting integral elevations in this study). For instance, measurements at the elevation of 4.0 ° for the azimuth between 177 ° and 181 ° are used in this study since two tall buildings stand to the south of the Beijing Radar.

274

275 3.1.5 Convective–stratiform classification

276 Because of the distinct DSD characteristics between the convective and stratiform





rainfall, the *Z*-*R* relationships for the two types of rainfall differ significantly. It is thus
necessary to conduct the convective-stratiform classification before the *Z*-*R* conversion.
Due to the unavailability of real-time atmospheric temperature profiles that is
commonly used for convective-stratiform classification, a vertically integrated liquid
(VIL; Greene and Clark, 1972) based method (Zhang and Qi, 2010) is adopted in this
study.

284 With the volume scan reflectivity measurements, VIL can be obtained by:

$$VIL = \sum_{k} VILpar_{k},$$
(6)

where $\text{VILpar}_k = \text{LW} \cdot \text{DB}$ denotes the VIL within the k^{th} tilt with LW (kg km⁻³) and

286 DB (km) being the liquid water content associated with a particular value of reflectivity

and the depth of a radar beam, respectively, given by

$$LW = 3.44 \times 10^3 Z^{\frac{4}{7}},\tag{7}$$

$$DB = \begin{cases} BH \left[\theta_{k_{top}} + 0.5BW \right] - BH \left[0.5 \left(\theta_{k_{top}} + \theta_{k_{top}-1} \right) \right] & k = k_{top} \\ BH \left[0.5 (\theta_{k+1} + \theta_k) \right] - BH \left[0.5 ((\theta_k + \theta_{k-1})) \right] & 1 < k < k_{top}, \quad (8) \\ BH \left[0.5 ((\theta_1 + \theta_2)) \right] & k = 1 \end{cases}$$

288

where DB (km) is the depth of a radar beam, *Z* the radar reflectivity within a radar sample volume, BW the angular width of the radar beam between the half-power points, BH the beam center height for a given elevation angle and range under the standard atmospheric refraction conditions and θ_k the elevation angle at the k^{th} tilt.

293

294 Once the knowledge of VIL is obtained, the reflectivity pixels can be categorized into

stratiform with VIL < 6.5 kg m⁻² and convective with VIL \ge 6.5 kg m⁻².





296

297 **3.1.6 Derivation of local** *Z-R* relationships

The standard *Z*-*R* relationships are $Z = 200 R^{1.6}$ and $Z = 300 R^{1.4}$ for stratiform and convective situations, respectively. However, due to the large variability of *Z*-*R* relationship among different locations, localized *Z*-*R* relationships are mandatory for building radar QPE systems. As such, we use the DSD measurements collected at the distrometer sites near the Beijing Radar to establish the local *Z*-*R* relationships.

303

304 As can be seen in Fig. 5, by conducting Z-R regression without differentiating rainfall types, Z=428.4 $R^{1.2}$ is obtained from non-linear regression. Furthermore, considering 305 the rainfall types (stratiform for $Z \leq 39$ dBZ and convective for Z > 39 dBZ; cf. 306 Steiner et al., 1995), Z-R relationships Z=426.5 $R^{1.3}$ and Z=499.3 $R^{1.2}$ are obtained for 307 stratiform and convective event, respectively. It is noteworthy that the Z-R relationships 308 derived by this study distinguish from the standard forms, implying the necessity of 309 locally-derived forms in radar QPE systems. It is also noteworthy the convective events 310 311 comprise a large portion of the rainfall events, which is consistent with the previous findings that convective events are common in urban areas. (Yang et al., 2014a, Yang 312 et al., 2015b, Yu et al., 2015). 313

314

315 **3.2 Procedure for wind drift correction**

Wind drift means the horizontal displacement between the aloft measurement positionand ground falling location of a raindrop. Wind drift correction enables better rainfall





estimation at the ground level. The horizontal displacement Δx of a raindrop can be

stimated by integrating horizontal wind velocity
$$u(h)$$
 over falling duration (Caroline,

320 2015) as follows:

$$\Delta x = \int_0^t u(h)dt = \int_0^{h_b} \frac{u(h)}{w(h)} dh,$$
(9)

- 321 where w(h) is the falling speed at height h and h_b is the height of the radar beam at the
- 322 measurement location. And u(h) is given by:

$$u(h) = S \cdot h, \tag{10}$$

- 323 where *S* is a constant wind shear (Caroline, 2015).
- By assuming a zero wind speed at the ground level, the wind shear *S* can be calculatedby:

$$S = \frac{u(h_b)}{h_b}.$$
 (11)

326 Given the constant falling speed of 5 m s⁻¹ for raindrops blow the melting layer

327 (Caroline 2015), the Eq. (12) thus can be simplified as:

$$\Delta \mathbf{x} = \frac{1}{5} \frac{Sh_b^2}{2} = \frac{u(h_b)h_b}{10}.$$
 (12)

Furthermore, $u(h_b)$ can be determined by a pixel-based tracking algorithm for shortterm quantitative rainfall forecasting (Zahraei et al., 2012). The tracking algorithm can estimate the advection velocity of a rainy pixel (equal to the background wind velocity) by tracking its successive positions between radar images based on the maximum correlation of meshes in consecutive images.

333

334 4. Results and discussion

335 4.1 Importance of different common corrections





- 336 To assess the relative importance of different common error corrections, a rotation-
- 337 based strategy is conducted, which consists of two procedures as follows:
- 338 1) Complete-correction (CC) procedure: all the corrections described in Section 3.1
- are applied to the reflectivity measurements to obtain the rainfall field as the best
- 340 estimate;

2) Partial-correction (PC) procedure: all but one of the corrections as in the CC
procedure are used to estimate the rainfall, whereby the corresponding estimate can
be compared with the best estimate of CC procedure to assess the effectiveness of
a specific error correction (i.e., the excluded correction). By rotating the specific
correction in the PC procedure, rainfall estimates without different corrections can
thus be obtained.

347

Furthermore, to quantify the correction effectiveness so that get the relative importance of different error sources contributing to the overall errors, the radar-gauge ratio of daily accumulated rainfall *rd*, average radar-gauge ratio of total rainfall *ra*, the root-meansquare error RMSE, and the coefficient of determination r^2 are introduced as follows:

$$rd_{i,k} = \sum_{n} R_{n_{i,k}} / \sum_{n} G_{n_{i,k}},\tag{13}$$

$$ra = \frac{1}{8} \sum_{k=1}^{8} \sum_{n,k} R_{n,k} / \sum_{n} G_{n,k},$$
(14)

$$RMSE = \sqrt{\frac{1}{N} \sum_{n=1}^{N} (R_n - G_n)^2},$$
(15)

$$r^{2} = \frac{\left(\sum (R_{n} - \overline{R_{n}})(G_{n} - \overline{G_{n}})\right)^{2}}{\left(\sum_{n=1}^{N} (R_{n} - \overline{R_{n}})^{2}\right)\left(\sum_{n=1}^{N} (G_{n} - \overline{G_{n}})^{2}\right)}$$
(16)

where the subscript *i* and *k* denote the date number and gauge number, respectively; while the radar-based estimates R and gauge measurements G with n and N denoting





- the n-th hour and total number of hours, respectively. The first two metrics are chosen
- to describe the systematic bias, while the last two assess the average error magnitude
- and agreement at hourly scale.
- 357
- 358 To reduce the bias in the radar-gauge comparison, 33 events, during which at least three gauges have valid measurements, are chosen and investigated for the correction 359 360 effectiveness. For the 33 events, the ratio rd based on the CC procedure varies mostly 361 between 0 and 3 with the medians ranging between 0.5 and 1.5 (Fig. 6), suggesting a 362 promising performance of common corrections, though considerable variability can be observed for several events (e.g., events of July 29, 2015). Extending beyond the 33 363 chosen events to all the events in the study period, it is also noted that with the CC 364 procedure performed, the Beijing Radar underestimates the rainfall compared with the 365 gauges (cf. a linear radar-gauge regression slope of 0.69 and coefficient of 366 determination R^2 of 0.76 in Fig. 7) with an averaged underestimate of 24.6% in the total 367 rainfall. This result is comparable with that of the X-band radar at the Delft University 368 369 (cf. a linear radar-gauge regression slope of 0.65 reported in Van de Beek et al. (2010)). 370

The influence of the PC procedure on the rainfall estimates is then examined by comparing the above metrics between the radar-based estimates and gauge measurements during the study period (Table 3 and Fig. 8). Correction for anomalous propagations contributes a minimal improvement in the rainfall estimates (Fig. 8a) because this correction may reduce the estimated reflectivity and thus the rainfall.





376 However, such minimal influence does NOT suggest the non-necessity of anomalous 377 propagation correction since its improvement is largely screened by errors from other sources. The attenuation correction demonstrates improvement in the rainfall estimates 378 in terms of both ra and RMSE (Fig. 8b). As expected, the largest improvement is 379 380 resulted from the beam integration as indicated by the reduced RMSE (cf. RMSE from 3.18 for -BI to 1.95 for CC in Table 3) and by the increased coefficient of determination 381 382 r^2 for the radar-gauge linear regression (cf. from 0.54 to 0.76 in Fig. 8c). The increased 383 deviation for no beam integration suggests that larger ra (cf. 0.87 for -BI in Table 3) is 384 actually the results of offset of positive and negative deviations.

385

Furthermore, significant improvements are observed in the estimated rainfall when the variability in the DSD is taken into account: both the convective–stratiform classification and the local *Z-R* relationship derivation contribute to increases in ra and decreases in RMSE (Table 3). Such improvements are also demonstrated by the increases in the slope of radar-gauge linear regression (Fig. 8d and e).

391

In general, the DSD-related corrections (i.e., convective–stratiform classification and the local *Z-R* relationship) demonstrates greater improvement in the estimation of rainfall as compared with some of the reflectivity-related corrections (i.e., anomalous propagations removal, attenuation correction), implying the importance of appropriate DSD-related corrections.





398 4.2 Case study: a fast-moving event of 20150904

- Although considerable improvements can be observed in the rainfall estimates after the common error corrections, it should be noted the potential for improving the rainfall estimates may be realized by correcting the wind drift errors in radar QPE systems, in particular for X-band radars of high spatial resolutions. To examine the effect on the radar based rainfall estimates of wind drift correction, a long-duration event (~16 h) on 4th September 2015 featuring fast-moving storms with complex structures is analyzed here.
- 406

The event originated from low pressure system passing over Beijing from southwest towards northeast, where a high pressure zone resided over the urban area of Beijing. Taking an episode of ~30 min for instance, several convective cells rapidly grew in the southwest of Beijing (Fig. 9a and b), then quickly moved to northeast (Fig. 9c), and developed to a widespread precipitating system afterwards (Fig. 9d).

412

The influence of the wind drift correction on the hourly rainfall estimates is then examined by a radar-gauge linear regression (Fig. 10). After the wind drift correction, the slope and coefficient of determination R^2 of the radar-gauge regression increase from 0.46 to 0.58 and from 0.69 to 0.79, respectively, suggesting an evident improvement in the estimates of total rainfall. In addition, the temporal characteristics of rainfall estimates are refined as well. For instance of a gauge close to the radar, the correlation coefficient of the rainfall series between the radar and gauge is increased





420	from 0.79 to 0.86 and the RMSE of rainfall measurements is reduced from 27.4 to 18.8
421	after the wind drift correction (Fig. 11). It is also noteworthy that the wind drift
422	correction leads to an improved temporal consistency in the rainfall time series between
423	the gauge and radar with the more accurate rainfall estimate at the peaking time (i.e.,
424	17:00 shown in Fig. 11).

425

426 5. Concluding remarks

427	In this study, we analyzed 43 rainfall events between July 2014 and September 2015					
428	based on the measurements gathered by an X-band single-polarized radar, a					
429	distrormeter and 8 rain gauges in Beijing urban area. These measurements allow us to					
430	explore the potential for high-resolution rainfall measurement with X-band radar over					
431	complex urban region. The impacts and importance of common corrections (i.e., radar					
432	calibration, non-precipitating echo removal, attenuation correction, beam integration,					
433	convective-stratiform classification and local Z-R relationships) on the quality of the					
434	radar QPE is first studied, followed by an assessment of the effectiveness of wind drift					
435	correction. The major findings are summarized as follows:					
436	1) Although the radar QPE system underestimates the total rainfall accumulations by					

- 437 24.6% as compared with gauges, the common corrections demonstrate promising438 improvements in the rainfall estimates.
- 439 2) The greatest improvements in the radar based rainfall estimates can be attributed to
 440 the beam integration, which significantly outperforms the operation at the single
 441 lowest elevation without beam blockage (i.e., 4.0 °in this study). It is thus highly





442	suggested to conduct volumetric reflectivity measurements with the X-band radar
443	in particular for complex-terrain regions. Minor improvements on the radar rainfall
444	estimation are observed after the anomalous propagations removal as compared to
445	other common error corrections.
446	3) The DSD-related corrections (i.e., convective–stratiform classification and local Z-
447	R relationship) lead to significant improvements in the rainfall estimates. And the
448	local Z-R relationship plays a more crucial role in improving the rainfall estimates
449	compared with the other corrections, which highlights the necessity of deriving the
450	localized Z-R relationships for different types of rainfall.
451	4) The wind drift correction improve both the total accumulation and the temporal
452	characteristics of the estimated rainfall, which suggest the necessity of wind drift
453	correction for X-band radars of high spatial resolutions.
454	
455	The possible future improvement relies on the inclusion of vertical profile of reflectivity
456	(VPR) measurements of this region to correct the underestimation in reflectivity (Qi et
457	al., 2013). In addition, polarimetric radars, featuring the ability to capture two-
458	dimensional structure of rainfall, can provide new insight into rainfall microphysics and
459	make further improvements in monitoring urban rainfall.
460	

461

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- 621





622 Table 1 Main specifications of X-band radar used in this study.

Parameters	Value
Frequency	9.38 Ghz
Peak transmitted power	25 kw, 38 dB gian
Antenna	1.3 m
Beam width	1.8 °
Platform	44 m above ground level

623

Table 2 Specifications of disdrometer used in this study.

Parameters	Value
Optical sensor wavelength	780 nm
Dertiale size range	0.2–5 mm (liquid precipitation),
Farticle size range	0.2–25 mm (solid precipitation)
Particle velocity range	$0.2-20 \text{ m s}^{-1}$
Measurement time	
aggregation	1 min
interval setting	
Precipitation intensity range	0.001–1200 mm h ⁻¹
Radar reflectivity range	9.9–99 $\pm 20\%$ dBZ

⁶²⁵

Table 3 Impacts of the correcting different common errors on hourly accumulated

⁶²⁷ rainfall.

Statistial	CC procedure –	PC procedure ²				
Statistic		- AP	-Att	-BI	-Seg	-Z-R
ra	0.75	0.77	0.72	0.87	0.57	0.61
RMSE	1.95	1.97	2.02	3.18	2.17	2.34

628 Notes:

The statistics are calculated with hourly rainfall estimates. *ra* is the average radar-gauge
 ratio for 8 gauges and RMSE = √(1/N)∑_{n=1}^N(R_n - G_n)² is the root-mean-square error
 between the radar-based estimates *R* and gauge measurements *G* with *n* and *N* denoting
 the *n*-th hour and total number of hours, respectively.
 The minus sign (-) in PC procedure indicates the exclusion of a specific correction. The
 correction names are simplified as follows: AP for anomalous propagations correction, Att
 for attenuation correction, BI for beam integration, Seg for convective–stratiform rainfall





- 636 classification, *Z*-*R* for local *Z*-*R* relationship derivation.
- 637



- 639 Figure 1 The site view of (a) the Beijing Radar and (b) the disdrometer used in this
- 640 study.







Figure 2 The instrumentation layout of urban rainfall monitoring system of in Beijing.







644 Figure 3 The relationship between radar-measured reflectivity and distrometer-

645 estimated reflectivity.







647 **Figure 4** *Z*-*k* relationship derived from DSD data using a non-linear power-law fit.







Figure 5 *Z*-*R* relationships for different rainfall scenarios.







656

Figure 6 Radar-gauge ratios of the daily accumulated rainfall for events covering at
least 3 gauges. The dots denote the outlier values. Each box ranges from the 25th
percentile to the 75th percentile with the middle line denoting the median value.

660



661

Figure 7 The relationship of hourly rainfall accumulations from 8 rain gauges and the

663 corresponding radar pixels for all the events.







664

Figure 8 Performance in radar-based rainfall estimation of different corrections: (a) non-precipitation echo removal, (b) attenuation correction, (c) beam integration, (d) convective–stratiform segregation, and (e) using different *Z-R* relationships for converting the reflectivity to rainfall intensity. The blue and orange dots show the results of complete-correction and partial-correction procedures, respectively.







672 Figure 9 Snapshots of the radar-based rainfall fields for the fast-moving rainfall event

of 4th September, 2015 at (a) 14:45, (b) 14:59, (c) 15:13 and (d) 15:27.







675

676 **Figure 10** Performance in radar-based rainfall estimation of the wind drift correction.

677 The blue and orange dots show the results of complete-correction and partial-correction

678 procedures, respectively.

679



681 Figure 11 Rain gauge, QPE with wind drifting correction and QPE without wind





- drifting correction rainfall time series for fast-moving event, 4th-5th September 2015
- at the position of closest gauge to radar.