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# How big is an OMI pixel? 

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#### Abstract

. The Ozone Monitoring Instrument (OMI) is a push-broom imaging spectrometer, observing solar radiation backscattered by the Earth's atmosphere and surface. The shape of anOMI pixelincoming radiation is detected using a static imaging CCD detector array with no moving parts, as opposed to most of the previous satellite spectrometers, which used a moving mirror to scan the Earth in the across-track direction. The sensitivity function of the Field of View (FoV) of detector pixels, projected on the Earth, is defined as the point spread function (PSF). The OMI PSF is not quadrangular, which is common for scanning instruments, but rather Gattsian shaped as light from neighbouring pixels enters the Field of View (FoV)super-Gaussian shaped and overlapping with the PSF of neighbouring pixels. This has consequences for pixel-area dependent applications, like e.g. cloud fraction products, and visualisation.


The shape and sizes of OMI pixels-PSFs were determined pre-flight by theoretical and experimental tests, but never verified after launch. In this paper the OMI point spread function (PSF) PSF is characterised using collocated MODerate resolution Imaging Spectroradiometer (MODIS) reflectance measurements. MODIS measurements have a much higher spatial resolution than OMI measurements and spectrally overlap at 469 nm . The eptimat-OMI PSF was determined-verified by finding the highest correlation between MODIS and OMI reflectances for both-in cloud-free and partially clouded seenesscenes, assuming a 2D super-Gaussian function with varying size and shape to represent the OMI PSF. Our results show that the semi-offieial OMPIXCOR produet 75 FOW eorner coordinate courately fix OMPIXCOR product 75 FoV corner coordinates are accurate as the Full Width at Half Maximum (FWHM) of a super-Gaussian PSF model, when this pixel shape function is assumed. The expenent of the softness of the function edges, modelled by the superGaussian PSF is dependent on OMI pixel row number, from about $n=2$ at nadir 103.5 at the swath edges, due to the increase in pixel size. The optimal Gattsian expenent depends on seene changes between overpassesand reduces to about $n=1$ for exponents, is different in both directions, and view angle dependent.

The optimal overlap function between OMI and MODIS reflectances is scene dependent, and highly dependent on time differences between overpasses, especially with clouds in the scene. For
partially clouded scenesbefore 2008. Then, the time differenee, the optimal overlap function was represented by super-Gaussian exponents around 1 or smaller, which indicates that this function is unsuitable to represent the overlap sensitivity function in these cases. This was especially true for scenes before 2008, when the time differences between Aqua and Aura overpasses was about 15 minutes, instead of 8 minutes after 2008. Between-During the time between overpasses, clouds change the scene reflectance, reducing the correlation and ehanging influencing the shape of the optimal overlap function.

## 1 Introduction

The Ozone Monitoring Instrument (OMI) (Levelt et al., 2006) was launched in 2004 on-board the Aura satellite, with the main objective-in a polar, sun-synchronous orbit at approximately 705 km altitude, with a local equatorial crossing-time of 13:45 (ascending node). Its main objective is to monitor trace gases in the Earth atmosphere, especially ozone. It was built as the successor to the ESA instruments GOME (Burrows et al., 1999) and SCIAMACHY (Bovensmann et al., 1999), and NASA's TOMS instruments (e.g. Fleig et al., 1986; Bhartia et al., 2013). GOME and SCIAMACHY were the first space-borne hyperspectral instruments, measuring the complete spectrum from the ultraviolet (UV) to shortwave-infrared (SWIR) wavelength range with a relatively high spectral resolution (typically $0.2-1.5 \mathrm{~nm}$ ), from which multiple trace gases, clouds and aerosol parameters can be retrieved simultaneously. TOMS instruments have been monitoring the ozone column at a relatively high spatial resolution $\left(50 \times 50 \mathrm{~km}^{2}\right)$ with daily global coverage since 1978 . OMI was designed to combine those functions and measure the complete spectrum from the UV to the visible wavelength range (up to 500 nm ) with a high spatial resolution and daily global coverage. To this end, the imaging optics were completely redesigned.

Instead of a rotating mirror, in OMI a two-dimensional CCD detector array ( $780 \times 576$ pixels) is used to map the incoming radiation in the across-track and wavelength dimensions simultaneously. A swath of about 2600 km in the across-track direction is imaged along one dimension of the detector array. Spectrally, the radiation is split into UV two UV channels and a visible (VIS) channel and imaged along the wavelength dimension of the detector array, giving a- The spectral resolution of 0.63 nm for the VIS channel is 0.63 nm . The along-track direction is scanned due to the movement of the satellite. In default 'Global' operation mode, five consecutive CCD images, each with a nominal exposure time of 0.4 s , are electronically co-added during a two second interval. The sub-satellite point moves about 13 km during this time interval (Levelt, 2002). The consequence of this design is that the spatial response function of the OMI footprints is not box-shaped, but has a peak at the centre of the footprint. This new design, avoiding moving parts, was used in OMI for the first time, and is now being used in several new upcoming satellite missions.

The telescope Field of View (FoV) is determined by the projection of the OMI spectrograph slit on the Earth's surface from the point of view of a CCD pixel. This projection is affected by Fraunhofer diffraction of the imaging opticsand is not a sharply bounded funetion, but consists of a central response function with extending tails, which, for a circular aperture, can be modelled using an Airy function. For a rectangular slit, used in OMI, the solution can be approximated by a Gaussian function in two dimensions. The FoV has been determined pre-flight by measuring the intensity response to a star stimulus for all pixels. The response function was measured by exposing the pixels to a point source and rotating the instrument. The sensitivity curve found in this way was fitted to a Gaussian curve, of which the Full Width at Half Maximum (FWHM) was reported. This is proprietary information, but the results are summarised here. In the swath (across-track) direction the average peak position for each pixel was determined and fitted to a linear curve to determine the spatial sampling distance for the three channels, which gives the instantaneous FoVs in the across-track direction for individual pixels. For the VIS channel the FoV for the entire swath is $115.1^{\circ}$. The point spread function (PSF) in the across-track direction was not determined (or reported). However, a memo from the OMI Science Support Team from 2005 shows an across-track pixel size estimation from these measurements, where the sizes have been determined by assuming no overlap between adjacent pixels and computing the distances between the peak positions when imaged on the earth. This yields sizes in the across-track direction of 23.5 km at nadir and 126 km for far off-nadir ( 56 degrees) pixels.

In the along-track direction the FoV was characterised by tilting the instrument to simulate the movement in the flight direction. The measurements were fitted to a normal-Gaussian curve with variable width for different across-track angles and wavelengths. This width is reported as the Fult Width at Half Maximmm (FWHM) )FWHM in degrees, which is about 0.95 at nadir and 1.60 at 56 degrees for the VIS channel. This corresponds to a nadir pixel size in the along-track direction of about 15 km and a far off-nadir pixel size of about 42 km , when the Gaussian is convolved with a boxcar function whose width is the 13 km movement of the subsatellite point during the satlite motion during 2 -ssecond exposure.

The instantaneous FoV (iFoV) of the OMI instrument is influenced by a polarisation scrambler, that transforms the incoming radiation from one polarisation state into a continuum of polarisation states (as opposed to unpolarised light). The incoming beam is split into four beams of equal intensity, scrambled, and projected onto the CCD. Since the projections of the four beams are slightly shifted with respect to each other, the polarisation state of the incoming radiation still slightly determines the intensity distribution of the four beams and therefore the iFoV in the flight direction. The only property which is not dependent on the polarisation state of the incoming radiation is the centre of weight of the four beams. This corresponds to the centre of the ground pixels, which is therefore the only geolocation coordinate that can be determined unambiguously (van den Oord, 2006).

Therefore, centre coordinates are provided in the Level 1b data product, but corner coordinates are not. However, for mapping purposes, ground pixel area computations (e.g. for emission estimates per unit area) and collocation, an OMI corner coordinate product was developed, called OMPIXCOR, which is provided online via the OMI data portal (Kurosu and Celarier, 2010). Two sets of quadrangular corner coordinates are provided. One set contains tiled pixel coordinates, which are essentially the midpoints between adjacent centre coordinates, mainly useful for visualisation purposes, as no overlap between pixels is imposed. The other set contains so-called 75 FOV 75 FoV pixel coordinates, which, according to Kurosu and Celarier (2010), correspond to $75 \%$ of the energy in the along-track FoV. The authors assumed a $1^{\circ}$ FWHM for the iFoV to fix a Gaussian distribution and convolved it with a boxcar to model the satellite movement. The area under a Gaussian curve corresponds to about $76 \%$ at FWHM for a normal distribution (exponent of 2), however, the authors claim to have used a super-Gaussian with exponent of 4 for this. In this case the energy contained within the FWHM has increased to about $89 \%$. When this iFoV is convolved with the satellite metionboxcar function, the energy within the FWHM will have increased even more. The 75 FOV 75 FoV pixels generally overlap in the along-track direction, since radiation emanating from adjacent successive scans enter the FoV. The coordinates in the across-track direction, however, are still the half-way points between adjacent pixels.

The application of quadrangular pixel shapes for OMI can become problematic when pixel values are aggregated onto a regular grid (e.g. Level 3 products that are reported on a regular lat-lon grid). If pixels overlap, which might occur when several orbits are averaged or in case of 75 FOV 75 FoV pixels, extreme values may be smoothed and reduced due to averaging. A more realistic distribution that preserves mean values can be reconstructed using a parabolic spline surface on the quadrangular grid, resulting in a much better visualisation (Kuhlmann et al., 2014). In cases where values from OMI are compared with that of another instrument, especially with a higher spatial resolution, the approximate true shape of an OMI pixel is desired. For example, we intend to combine spectral measurements from OMI and MODIS to determine the aerosol direct effect over clouds (de Graaf et al., 2012). To this end, an optimal characterisation of the PSF of the OMI footprint is desired, to optimise the accuracy of the retrieval.

In this paper, the OMI PSF for the VIS channel is investigated by testing various predefined shapes and sizes under various circumstances and determining the maximal correlation between OMI and MODIS reflectances. In section 2, the consistency between overlapping OMI and MODIS reflectances is investigated. A cloud-free scene from 2008 is used to study the PSF under the most optimal circumstances. In chapter 3, a two dimensional super-Gaussian function with a varying exponent is introduced, which can change shape from a near-quadrangular to a sharp-peaked distribution. Furthermore, the sizes in both along and across-track directions can be varied. This function is used to define various PSFs, which are investigated for various scenes. The change in PSF is further investigated by looking into the effect of scene and geometry changes during the (varying) overpass times
of OMI and MODIS. The conclusions from this study are reported in section4 The geolocations of the pixels in the UV channels are slightly different from those in the VIS channel. However, the PSF cannot be determined in the same way for the UV, since MODIS measurements do not overlap with these channels spectrally.

## 2 Data

Aura-The Aura satellite flies in formation with Aqua-the Aqua satellite in the Afternoon constellation (A-train). Aqua was launched in 2002, to lead Aura in the A-train by about 15 minutes. The time difference between the instruments within the A-train is controlled by keeping the various satellites within control-boxes, which are defined as the maximum distances to which the satellites are allowed to drift before correcting manoeuvres are executed. Therefore, the time difference between OMI and MODIS is variable by up to a few minutes. A major orbital manoeuvre in 2008 of Aqua decreased the distance between the Aura and Aqua control boxes to about 8 minutes.

To investigate the correlation between OMI and MODIS observed reflectances, several scenes were selected. One reference scene will be discussed here in detail. It was an almost cloud-free scene over the Sahara desert on 4 November 2008, around 14:00 UTC (start of the first MODIS granule). At this point in time, the time difference between OMI and MODIS was reduced to 8 minutes and around $20-30$ seconds, depending on the pixel row. The differences between the pixel times arise from the fact that MODIS has a scanning mirror, while OMI has no scanning optics, but exposes the CCD to different scenes while moving in the flight direction. The scene is visualised in Figure 1, using MODIS channels 2, 1, and 3 to create an RGB picture at $1 \mathrm{~km}^{2}$ resolution. The MODIS granules are outlined in yellow, while the considered OMI scene is outlined in red. From June 2007 onward, OMI suffered from a degradation of the observed signal in an increasing number of rows, called the row anomaly (OMI row anomaly team, 2012). In November 2008 the anomaly was limited to only rows 53 and 54 for scenes near the equator. These rows were disregarded in the comparison. In order to stay within the MODIS swath the OMI swath was further reduced to rows 2 to 57. A total of 7,335 OMI pixels are left in the scene.

To compare reflectances from OMI and MODIS, the reflectance measured by OMI is convolved with the MODIS spectral response function. MODIS channel 3 at 469 nm overlaps with the OMI VIS channel ( $350-500 \mathrm{~nm}$ ). This is illustrated in Figure 2 where two OMI reflectance spectra from the VIS channel are plotted, together with the normalised MODIS response function of channel 3 (red curve). The reflectance spectra correspond to the darkest and brightest pixels (at 469 nm ) in Figure 1 , indicated by the green boxes. The darkest pixel is a vegetated area with an OMI reflectance of $\theta .0967$ 0.0935 and the brightest pixel is a cloud covered scene with an OMI reflectance of 0.50750 .5040 , both at 469 nm .

All the 7,335 OMI pixels in the scene in Figure1were compared to collocated MODIS pixels, see the left panel of Figure 3. Here, all the MODIS pixels that fall (partly) within an OMI quadrangular pixel, as defined by the OMPIXCOR 75FoV corner coordinates, are averaged with equal weight, which is the easiest and quickest averaging strategy. The MODIS reflectances are somewhat lower than the OMI reflectances; a linear fit through the points shows a slope of 0.959 and an offset of 0.0023. The MODIS reflectances show a Pearson's correlation coefficient $r$ of 0.9970 .998 with the OMI reflectances, and a standard deviation (SD) of 0.00433 . The MODIS refleetances are somewhat tower than the OMI reflectances; a linear fit through the peints shows a slope of 0.954 and an- fffset of 0.00100 .0039 . The SD refers to the RMS deviation of the measurements to the model fit.

## 3 OMI point spread function

The true PSF of an OMI pixel is expected to resemble a flat-top Gaussian shape. To investigate the OMI PSF, the response at 469 nm is compared to the MODIS channel 3 signals, weighted using different super-Gaussian functions in two dimensions, and checking the change in the correlation and SD between the OMI and MODIS reflectances. A 2D super-Gaussian distribution is defined by
$g(x, y)=\exp \left(-\left(\frac{x}{w_{x}}\right)^{n}-\left(\frac{y}{w_{y}}\right)_{-\sim}^{n m}\right)$,
where $x$ and $y$ are the along and across-track directions, and $w_{x, y}$ are the weights in either direction, defined by
$w_{\underline{x, y x}}=\frac{\mathrm{FWHM}_{x, y}}{2(\log 2)^{1 / n}} \frac{\mathrm{FWHM}_{x}}{2(\log 2)^{1 / n}} ; w_{y}=\frac{\mathrm{FWHM}_{y}}{2(\log 2)^{1 / m}}$.
$\mathrm{FWHM}_{x, y}$ are the full widths at half maximum in the along and across-track directions, respectively, defined in this paper by the 75 FOV 75 FoV pixel corner coordinates. The size of the PSF model can be varied to include more or fewer MODIS pixels from neighbouring pixels in the along and acrosstrack directions by varying $\psi_{x, y} w_{x}$ and $w_{y}$. All size changes are reported relative to $\mathrm{FWHM} \overline{\bar{x}, y} x$ and $\mathrm{FWHM}_{y}$.

The shape of the PSF model is determined by the Gaussian exponent exponents $n$, whieh defines and $m$, which define the 'pointedness' of the distribution. In one dimension, $n=2$ eorrespending corresponds to a normal distribution, $n<2$ resulting results in a point-hat distribution and $n>2$ resulting results in a flat-top distribution, see the illustration in ene dimension in-Figure 4 Various PSFs-PSF models are illustrated in Figure 5 The colours of the square MODIS pixels indicate the relative contribution of that pixel. The different panels show OMI pixels at different rows, to illustrate the change in orientation and number of MODIS pixels that fall inside an OMI pixel when the viewing zenith angle changes. Figure 5 5 shows the quadrangular OMI pixel, with all MODIS pixels within the OMI corner coordinates having equal weight, while all pixels outside the footprint have zero weight. Figure 5b shows a 2D flat-top super-Gaussian ( $n=8$ ) shape $n=m=8$ ) shape
using the 75 FoV corner coordinates to constrain the FWHM, resembling the quadrangular shape but with smoother edges, and using the 75 FOV corner coordinates to fix the FWHM. Figure 5 : shows a normally or 2 D Gaussian $(n=2)$ distribution, while super-Gaussian distribution, with $n=2, m=4_{2}$ which represents the optimal representation of the PSF using a super-Gaussian function. Figure 5] shows a 2D point-hat super Gatssian $(n=1)$ distributionsuper-Gaussian $(n=1, m=1.5)$ distribution, which is the optimal fit of this function when broken clouds are in the scene. Figures 5e and $f$ show the weights for pixels which are assumed to be twice as wide or long as the 75 FOV 75 FoV pixels and using a 2D nomal Gaussian distribution-super-Gaussian distribution with $n=2, m=4$.

The size and shape of the changing $n$ and 0.25 FWHM for a wide range of these parameters, and for from 0.5 to $16, \mathrm{~m}$ from 1 to 16, and the FWHM from 0.5 to 3 times the 75 FoV corner coordinates. For each configuration the correlation between the OMI and MODIS reflectances and the SD were determined, using all pixels from the scene in Figure 1. The correlation change is shown in Figure 6. The blue dashed-dotted curve shows the change in correlation for a changing expenent $n$, Gaussian exponent and $1 \cdot F W H M$, i.e. the change in PSF shape and fixed 75 FOV corner coordinate model shape and 75 FoV corner coordinates to constrain the FWHM. In the top panel the change in correlation coefficient $r$ is shown for a changing Gaussian exponent $n$ using the optimal Gaussian exponent found for the across-track direction $m=4$. For this function the optimal Gaussian exponent in the along-track direction is $n=2$. The blue dotted curve shows the goodness-of-fit $q$ corresponding to each of the correlation coefficients $r$ (the blue dashed-dotted line). It was determined using a constant error for OMI measurements, and a constant error for MODIS measurements but weighted by the number of MODIS pixels in each OMI pixel. It shows a reasonably good fit at the optimum $n=2$. In this ease, the highest correlation is obtained when aGaussian distribution with expenent $n=2.5$ is used, which is slightly more flat topped than a normal distribution. The red lines show

The red line shows the change in correlation when the shape of the distribution is fixed to a nermat distribution $(n=2)$. In that ease, the eorrelation peaks for an aross-track width of 0.8 FWWHM, eorrespending to a slightly more narrow pixel-along-track width is varied. The shown curve is for the optimal Gaussian parameters, $n=2, m=4$, and peaks at 1.0 , meaning that the 75 FoV corner coordinates are the optimal sizes to constrain the FWHM when a super-Gaussian model is used. The lower panel shows the same dependencies in the across-track direction. In the along-track direction the correlation peaks at 1 FWHM. If all three parameters are allowed to vary at the same time, the maximum correlation is found as before: $n=2.5$ and the pixel sizes corresponding to the 75 FOV eorner coordinatesin both directions. This is shown by the purple eurve, which shows the variation along the The change of $r$ for changing $m$ (the shown dashed-dotted line is for the optimal Gaussian exponent $n=2$ ) and the red curve is the width in the across-track direction for $n=2, m=4$. The red curve also peaks at one, again confirming the 75 FoV corner coordinates, while $m$ peaks at 4. However, the change for larger $m$ is minimal, meaning that the softness of the edges in the
across-track direction for the optimal parameters. Obviously, the make very little difference. Only the goodness-of-fit $q$ decreases significantly for larger $m$, so $m=4$ can be used as the optimal parameter. These four optimal parameters are also the absolute maximum in the purple eurve is the same as the one for the blte eurve: $r=0.9974$ entire parameter space, with $r=0.998$. This is noticeably higher than the correlation when quadrangular pixels are used.

The correlation between the OMI and MODIS reflectances and the SD, when the optimal PSF model for this scene is used, is shown in the right panel of Figure 3. The SD for the optimal PSF is 0.004090 .0036 . The change in SD for different shapes and sizes is not shown, because it is consistent with the change of the reciprocal of the correlation, in the sense that it is minimal when the correlation peaks and can be equally used to find the optimal PSF characterisation in this way.

### 3.1 PSF sensitivity

So, when-When a super-Gaussian form is assumed, the optimal OMI PSF-super-Gaussian model parameters for the reference scene ean be chafacterised using an expenent $n=2.5$ and 75 FOV are $\underset{\sim}{n}=2, m=4$ and the 75 FoV corner coordinates for the Gaussian FWHM. However, the correlation between OMI and MODIS reflectances is not a constant. A number of scenes were investigated to show the change in correlation between OMI and MODIS reflectances in time and space. They are treated below and illustrated in Figures $7-10$

First, another cloud-free scene was found over the Middle East on 7 October 2008, starting on 10:20 UTC, see Figure 7 The time difference between OMI and MODIS is about 8 minutes and $34-$ 45 s . This scene is entirely cloud-free over land, and the reflectance ranges from 0.12 over the ocean to 0.41 over the desert. The correlation between the OMI and MODIS reflectances is depicted in the right panel of Figure 7 which displays the same dependencies as in Figure6 The highest correlation $(f=0.9965)$ using 75FOV corner coordinates is found for a Gattssian distribution with anexpenent of $n=3$ (blue line). When the shape is fixed to anormal distribution $(n=2), r=0.9977$ ) was found for the highest correlation ( $r=0.9964$ ) is found for pixel sizes that are smaller ( 0.8 FWHM) in the arross-track direction, as for the referenee seene. This is also the absolute maximum and therefore the red across-track etrve coineides with the ptrple onesame super-Gaussian parameters as before, confirming the optimal OMI PSF model. Only the goodness-of-fit was slightly lower than before, indicating a lower correlation between the OMI and MODIS reflectances.

### 3.2 Viewing angle dependence

Next, a scene over Australia was selected on 11 October 2008 starting on 04:45 UTC, see Figure 8 . The time difference between OMI and MODIS is about 8 minutes and $35-43 \mathrm{~s}$. This scene has a large cloud-free part, but also a large cloudy part. Most cloud pixels, indicated by the red rectangles, were not used in the analysis. The correlation between OMI and MODIS for various shapes and sizes is again displayed in the right panel. The maximum correlation for this scene was
$=0.9907$, lower than before, $r=0.9927$, and obtained for a point-hat Gatesian distribution with expenent $n=1.75$ and super-Gaussian distribution with exponents $n=1.5$ and $m=2$, and FWHM corner coordinates. Note that the correlation-The goodness-of-fit is significantly lower than for the reference seenebefore.

The-One reason for the lower Gaussian exponents of the 2008 Australian scene also has the highest eorrelation for an expenent smaller than 2, but the presence of clouds only partly explains this. Most of the cloud pixels were removed, but keeping those pixels in the correlation experiment increased the optimal Gatissian expenent, to 2.5, rather than decreasing it. The reason for this is that the in the across-track direction is the removal of the pixels at the end of the swath, which were filtered because of the clouds in those pixels. The OMI PSF is dependent on the pixel row, and the PSF is wider or viewing angle, with wider PSFs at the swath ends. Most-Since most of the cloud pixels are at the swath ends, and-removing these pixels removes the larger exponents. This The viewing angle dependence of the PSF is treated here.

Since the OMI FoV is dependent on the polarisation of the scene, the PSF should also be dependent on the scattering geometry. To demenstrate this Furthermore, the diffraction at the edges of the FoV can be distinctly different for FoVs at nadir compared to those with a large viewing zenith angle (VZA). To investigate this effect, the OMI PSF was determined as a function of viewing zenith angle (VZA)characterised using a super-Gaussian function dependent on VZA. For all the scenes described abovein this paper, the optimal super-Gaussian shape was determined per OMI pixel row, by varying the Gaussian exponent and determining the maximum correlation between OMI and MODIS pixels for each pixel row. Then the optimal exponents of all five seenes presented above-were averaged and plotted as a function of pixel row. In this analysis, the 75 FOV 75 FoV pixel sizes were used, to reduce the number of variables and because the above analysis showed that the 75 FOV 75 FoV corner coordinates are good indicators of the pixel sizes for Gaussian shapes. The result is shown in Figure 9 The funetion shows a very erratic behaviour, due to the rather large steps in Gattssian expenents nodes that were used ( $0.25 n$ ), while the ehange in correlation for a change in Gaussian exponent is very small near the optimmm. As aconsequence, the pixel shape has only a super-Gaussian exponents are rather wildly fluctuating, because they have a limited sensitivity near the optimum, and the retrieved Gattssian expenent is rather witdly fluettatingespecially $m$. Averaging over the scenes reduces this, but is somewhat arbitrary. In Figure 9 a boxcar average over 5 neighbouring points is shown as well.

A general trend-Still, some change in Gaussian exponents can be observed from a flat topped Gatusian shape towards the edge of the swath with an expenent of about 3.5 to an expenent of areund 2 at nadir. Next to the faet that the OMI FOV is polarisation dependent, the as a function of VZA. The Gaussian exponent in the across-track direction $m$ changes from around $3-4$ at nadir to about 7 at far off-nadir. Also $n$ is VZA dependent, changing from about 1.5 at nadir to more than 2 at the swath edges. The reason for the increasing exponentexponents towards the swath edges is the
pixel size increase towards the swath edges. The pixel sizes are shown for reference. The OMI pixet sizes increase dramatically towards the edge for the aeross-track direction. Wide pixels have smooth edges and a flat interior, while the small pixels around nadir also have smooth edges, but are too small to display a flat interior. The left and right edges are just 'glted' together. This is expressed by a-Gatssian expenent of 2 or even lower. FoVs at larger VZA are much wider, changing the optimal super-Gaussian that fit the PSF. Furthermore, as observed before, the diffraction at the edges of the FoV will be different at larger viewing angle.

This effect is in the across track direction only, since the pixel size change in the

### 3.3 Scene dependencies

The smaller Gaussian exponents for the 2008 Australian scene (Figure 8) are only partly explained by the VZA dependence. The Gaussian exponent $n<2$ indicates a point-hat super-Gaussian distribution in the along-track directionis muth smaller. A Gatssian shape which is fixed in the along track direction and variable in the acress track direction will probably give aneven higher correlation, but this was not attempted., which is, as Figure 5 b shows, a distribution that is physically unlikely. For this scene, the super-Gaussian function is apparently not a good representation of the PSF of the OMI FoV. The reason for this mismatch are broken cloud fields in the scene, which change the scene reflectance between overpasses of Aqua and Aura. Scene dependencies will be investigated below.

### 3.4 Scene dependencies

Lastly, The overpass time between Aqua and Aura changed in 2008, when a correcting manoeuvre brought OMI closer to MODIS. To illustrate the effect, another Sahara cloud-free scene in the beginning of 2008 was selected, shown in Figure 10 At this time the correcting maneeurre bringing OMF eloser to MODIS-when the manoeuvre had not yet been performedand the-, see Figure 10. The time difference between the instruments for this scene is as large as around 14 minutes, up to 16 minutes and 26 s . The-In this case, the highest correlation is found for a Gatessian distribution with an expenent of super-Gaussian distribution with exponents $n=1.5$ (blue line), which is, $m=2$, which is again a point-hat super-Gaussian distributionwith wide wings. Similarly, when the shape is fixed to normaldistribution $(n=2)$ the optimal Gaussian exponents, the highest correlation is found for pixel sizes that are wider than the 75 FOV 75 FoV corner coordinates, which-see the red curves in Figure 10. This is different from the reference scene in Figure 1 . The mest striking difference, however, is the muth lower absolute value of the correlation. The-maximum correlation for this scene is $f=0.980 r=0.982$, which is $2 \%$-lower than for the reference scene, in December 2008. Even a 4 times wider pixel size in the referenee seene yields a mtreh higher correlation between the The goodness-of-fit $q$ shows much lower values, showing the difficulty with the used PSF model to correlate the OMI and MODIS reflectances. Apparently, the time difference between the Aqua and Aura of 15 minutes makes a comparison between the two instruments much more challenging,
even for almost cloud-free scenes. It is unlikely that the OMI FoV has changed much between January and December 2008. Furthermore, a cloud-free Sahara scene in 2006 (31 January 2006, around 13:55 UTC, not shown), showed the same lower correlation, peaking for a Gatssian expenent $n=1$, which is also a point hat distribution with wide tails. The maximum correlation for this seene was $f=0.971$, which is in the same order as this seene in Jantary 2008. the same Gaussian exponents.

The effect of changing scenes between overpasses can be illustrated by looking at the pixels with the highest SD between the OMI reflectances and the average collocated MODIS reflectances. Even for a scene after 2008, when the overpass time difference is reduced to about 8 minutes, the retrieved TOA reflectance can change significantly during this time in the case of broken clouds. The pixels with the highest SD for the reference scene were marked blue in the right panel of Figure 3. The marked points correspond to the blue coloured OMI pixels in Figure 1 which are the areas where the scene contains broken cloud fields. In the few minutes between Aqua and Aura overpasses these clouds change shape and position, changing the average reflectance in a pixel when the cloud fraction is changed.

This is the main reason for the small optimal super-Gaussian exponent for the 2006-2008 Sahara scene (Figure 10) and the Australian scene (Figure 8): due to scene changes during the different overpass times, the observed overlap function deviates from the true PSF, which closely resembles a Gaussian or flat-topped Gaussian. Instead a more point-hat distribution with wider wings is found. The centre of the pixel becomes more important, since this point will still have the highest correlation for both instruments. But since the signal becomes more spread out, the wider wings give coordinates have the relative highest correlation, but lower than before, while the correlation becomes smoothed over a larger area, giving the tails of the function a higher correlation than for the true PSF.

### 3.4 Accuracy of combining OMI and MODIS

The optimal PSF of OMI-overlap function for MODIS pixels within an OMI FoV can now be determined for practical purposes, i.e. mixed scenes with ocean, land and clouds. This is needed to determine the accuracy that can be expected when OMI and MODIS measurements are combined to reconstruct the reflectance spectrum for the entire shortwave spectrum. To determine the accuracy, the correlation between collocated OMI and MODIS reflectances and the SD was determined by comparing the instruments for the scene shown in Figure 11 This scene was taken on 13 June 2006, starting on 13:33 UTC when the time difference between the instruments was about 15 minutes. The scene contains a mixture of land and ocean scenes, with and without clouds, and also smoke from biomass burning on the African continent. Only OMI rows 10-50 were processed, which will often be the case to avoid problems with large pixels or extreme viewing angles. The optimal correlation was found for Gatssian expenent $n=1$ and 75 FOV super-Gaussian exponents $n=1, m=1.5$ and 75 FoV corner coordinates (not shown). The low Gaussian expenent can exponents can again be explained from the presence of clouds that change the scene between the overpasses, and the exclu-
sion of wide pixels at the swath edges. The correlation between the OMI and MODIS reflectances using this shape is shown in the right panel of Figure 11 Obviously, the correlation is a lot lower than for cloud-free scenes $(~ f=0.963 r=0.964)$. The SD is 0.03730 .0371 , which must be taken into account when OMI and MODIS reflectances are compared or combined. Furthermore, the slope of a linear fit between the OMI and MODIS reflectance is $\theta .9090 .941$, which is smaller than that for cloud-free scenes, which showed about $54 \%$ difference. This larger range in reflectances for cloud scenes apparently off-sets the difference between the instruments even further.

### 3.5 Geometry differences

The eorrelation-4-5\% difference between OMI and aggregated MODIS reflectances at 469 nm shows that OMI reflectances are consistently about 5\% larger than the aggregated MODIS reflectances (see (Figure 3) - These differenees can be governed by changes in viewing and solar conditions between OMI and MODIS. Since the optics and sub-satellite points differ for both instruments, the viewing angles are slightly different, even if the satellites roughly follow the same orbit. More importantly, since Aura is always behind Aqua, the solar zenith angle for OMI is always different from that of MODIS.

To investigate the effect of the differences in scattering geometry on the measured TOA reflectance, a cloud-free Rayleigh reflectance was modelled for each OMI pixel in the reference scene in Figure 1 Each pixel was simulated twice, once using the OMI scattering geometry and once using an average MODIS scattering geometry. In this way the expected reflectance difference can be determined due to the difference in overpass time, keeping all else the same. To determine the average MODIS reflectance, the simulated radiances were averaged over the OMI footprint using the optimal flat-top Gaussian distribution with $n=2.5 n=2, m=4$, as was determined for this scene (Figure 6). The average radiance was then divided by the cosine of the solar zenith angle of the MODIS pixel which is closest to the centre of the OMI pixel. In this way, the most representative solar zenith angle is used to normalise the radiances. A realistic surface albedo was taken for each pixel, in order to make the model results comparable to the observations. The surface albedo database used was the TERRA/MODIS spatially completed snow-free diffuse bihemispherical land surface albedo database (Moody et al., 2005). The monochromatic calculations were performed at 469 nm , using a standard Rayleigh atmosphere (Anderson et al., 1986) reaching to sea level, and an ozone column of 334 DU. The results are shown in Figure 12 ,

The reflectance ranges from about 0.085 to 0.28 , depending on the surface albedo, which is smaller than the observed reflectances (cf. Figure 3, right panel). This is mainly due to the clouds in the scene which are not simulated. The simulated OMI reflectances are larger than the simulated MODIS reflectances due to different geometries, like the observations. There is a small dependence on VZA, as shown in the right panel of Figure 12, where the relative differences between the OMI and MODIS reflectances are plotted as a function of either reflectance, to highlight the change for changing VZA
(in colours). However, the difference for the simtlationsbetween the simulated OMI and MODIS reflectances, with a slope of 0.9965 and an offset of -0.001 , is much smaller than for between the observations. Therefore, we conclude that geometry differences between OMI and MODIS introduce differences of less than $1 \%$ and cannot explain the observed slope between OMI and MODIS reflectances. Most likely, calibration differences are causing the difference between the observed reflectances. The simulated correlation and SD are also notably better than for the observed scene. As noted before, clouds have the largest impact on the correlation between the observed reflectances of a scene.

## 4 Conclusions

The correlation between OMI and collocated MODIS reflectances was determined, to inter compare intercompare the performance of the instruments and to find the PSF of the OMI footprint. MODIS channel 3 at 469 nm overlaps with OMI's visible channel, and the signals can be compared when the reflectance signal of OMI is eonvolved-multiplied with the MODIS spectral response function, and MODIS reflectances are aggregated over the OMI footprint.

Due to the design of the OMI CCD detector array and the optical path, the footprint of OMI is not quadrangular and light from neighbouring pixels-successive scans enters the OMI FoV. The shape and size of the much as possible, scene changes due to the different overpass times of Aura and Aqua. Assuming a super-Gaussian shape with variable expenentexponents and FWHM, the best characterisation of the OMI PSF is was found for an exponent $n=2 \quad 2.5$ and 75 FOV $n=2 . m=4$ and $1 \times 75 \mathrm{FoV}$ corner coordinates to define-constrain the FWHM. When the corner coordinates

The OMI PSF changes as a function of viewing angle. When the FWHM are fixed, the Gaussian exponent ranges from about $\mathcal{Z} 1.5$ at nadir to 3.5 -more than 2 at the swath edges, while $m$ ranges from about 3-7. This is partly because the OMI PSF is dependent on polarisation, mainly due to the presence of a polarisation scrambler. Therefore, the-OMI PSF changes as a function of viewing angle. However, the main reasen is the-increase in pixel size for off-nadir angles. For very wide pixels the signal flattens at the centre. This effect may become more pronounced when the super-Gattssian expenent in the aeross-track direetion is made independent of the one in the along-track directionFurthermore, the diffraction at the FoV edges is viewing angle dependent, and the OMI PSF is dependent on polarisation, due to the presence of a polarisation scrambler in the OMI optical path.

The OMI-MODIS overlap function is scene dependent. In particular, for larger time differences between the Aqua and Aura overpasses, the optimal overlap function shape is found for smaller Gaussian exponents 4, still with the FWHM at the 75 FOV corner coordinatesand wider overlaps. When the scene changes between overpasses the signal is spread over a larger area, centred around
the centre coordinate. Therefore, a more optimal overlap function is found for a point-hat distribution with wider wings. This is especially true for cloud scenes, which are most frequent. The correlation decreases, and the SD increases -when clouds are in the scene, and this can be used as an indication of the expected accuracy of a comparison between OMI and MODIS reflectances. For a scene with broken clouds over both land and ocean in 2006, an optimal Gaussian exponent of $n=1-n=1, m=1.5$ was found. However, in-In general, the changes in correlation coefficient are small for small changes of the Gaussian expenent around 2 exponents (much smaller than e.g. changes due to different-time differences). Therefore recommend that the-The true OMI PSF is approximated by a normal Gattssian-super-Gaussian distribution with exponent $n=2$ and 75 FOV eorner coordinates, as a trade-off between the reduction of the expenent becattse of seene changes (elouds), and the increase of the expenent at the swath edges.

In all of the investigated case the OMPIXCOR 75FOV corner coordinatesadequately fix the size of the pixet, $m=4$ and 75 FoV corner coordinates.

The use of non-scanning optics like that used in-those of OMI will be continued in new instruments, in particular TropOMI/Sentinel-5P (Veefkind et al., 2012), to be launched in 2016. For TropOMI, a cloud masking feature is anticipated from Suomi-NPP/VIIRS (Schueler et al., 2002). Sentinel-5P will fly in 'loose formation' with Suomi-NPP, with expected overpass time differences of about 5 minutes. The results from this study are relevant for that mission, since such an overpass time difference will significantly change the overlap function between TropOMI and VIIRS, and affect the accuracy of a cloud mask from VIIRS. High resolution VIIRS measurements can be used in the way presented in the prent this paper to study and characterise the TropOMI PSF and the accuracy of the cloud mask.

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## References

Anderson, G. P., Clough, S. A., Kneizys, F. X., Chetwynd, J. H., and Shettle, E. P.: AFGL Atmospheric constituent profiles, Tech. Rep. AFGL-TR-86-0110, Air Force Geophysics Laboratory, 1986.
Bhartia, P. K., McPeters, R. D., Flynn, L. E., Taylor, S., Kramarova, N. A., Frith, S., Fisher, B., and DeLand, M.: Solar Backscatter UV (SBUV) total ozone and profile algorithm, Atmos. Meas. Tech., 6, 2533-2548, doi 10.5194/amt-6-2533-2013, 2013.
Bovensmann, H., Burrows, J. P., Buchwitz, M., Frerick, J., Noël, S., Rozanov, V. V., Chance, K. V., and Goede, A. P. H.: SCIAMACHY: Mission Objectives and Measurement Modes, J. Atmos. Sci., 56, 127-150, doi 10.1175/1520-0469 1999.
Burrows, J. P., Weber, M., Buchwitz, M., Rozanov, V., Ladstätter-Weißenmayer, A., Richter, A., DeBeek, R., Hoogen, R., Bramstedt, K., Eichmann, K. -U., Eisinger, M., and Perner, D.: The Global Ozone Monitoring Experiment (GOME): Mission Concept and First Scientific Results, J. Atmos. Sci., 56, 151-175, doi 10.1175/1520-0469 1999.
de Graaf, M., Tilstra, L. G., Wang, P., and Stammes, P.: Retrieval of the aerosol direct radiative effect over clouds from spaceborne spectrometry, J. Geophys. Res., 117, doi 10.1029/2011JD017160, http://dx.doi.org/10.1029/2011JD017160, 2012.
Fleig, A. J., Bhartia, P. K., Wellemeyer, C. G., and Silberstein, D. S.: Seven years of total ozone from the TOMS instrument-A report on data quality, Geophys. Res. Lett., 13, 1355-1358, doi 10.1029/GL013i012p01355. 1986.

Kuhlmann, G., Hartl, A., Cheung, H. M., Lam, Y. F., and Wenig, M. O.: A novel gridding algorithm to create regional trace gas maps from satellite observations, Atmos. Meas. Tech., 7, 451-467, doi 10.5194/amt-7-451-2014, 2014.
Kurosu, T. P. and Celarier, E. A.: OMIPIXCOR Readme File, available at: http://disc.sci.gsfc.nasa.gov/Aura/data-holdings/OMI/documents/v003/OMPIXCOR_README_V003.pdf, 2010.

Levelt, P. F.: OMI Instrument, Level 0-1b processor, Calibration \& Operations, in: OMI Algorithm Theoretical Basis Document. Volume I, 2002.
Levelt, P. F., van den Oord, G. H. J., Dobber, M. R., Mälkki, A., Visser, H., de Vries, J., Stammes, P., Lundell, J. O. V., and Saari, H.: The ozone monitoring instrument, IEEE T. Geoscience and Remote Sensing, 44, 1093-1101, 2006.
Moody, E. G., King, M. D., Platnick, S., Schaaf, C. B., and Gao, F.: Spatially complete global spectral surface albedos: Value-added datasets derived from Terra MODIS land products., IEEE Trans. Geosci. Remote Sens., 43, 144-158, 2005.
OMI row anomaly team: Background information about the Row Anomaly in OMI, http://projects.knmi.nl/omi/research/product/rowanomaly-background.php, 2012.
Schueler, C. F., Clement, J. E., Ardanuy, P. E., Welsch, C., DeLuccia, F., and Swenson, H.: NPOESS VIIRS sensor design overview, in: Proc. SPIE, vol. 4483, pp. 11-23, doi 10.1117/12.453451 2002.
van den Oord, G. H. J.: OMI Field of View, OMI Science Team Document RP-OMIE-KNMI-XYZ, Issue draft, January 2006, 2006.


Figure 1. MODIS RGB image of the reference scene on 4 November 2008, 14:00 UTC (start of the central MODIS granule). The yellow lines indicate the MODIS data granules and the red lines the considered OMI swath, which was confined to rows 2-57, with the exception of pixels in the row anomaly (see text). The green pixels indicate the darkest (vegetated) and the brightest (cloud covered) areas in the scene. The OMI reflectance spectra of these pixels are shown in Figure 2 The blue OMI pixels correspond to the blue marked points in Figure 3

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Kleipool, Q., van Weele, M., Hasekamp, O., Hoogeveen, R., Landgraf, J., Snel, R., Tol, P., Ingmann, P., Voors, R., Kruizinga, B., Vink, R., Visser, H., and Levelt, P.: TROPOMI on the ESA Sentinel-5 Precursor: A GMES mission for global observations of the atmospheric composition for climate, air quality and ozone layer applications, Remote Sens. Environ., 120, 70-83, 2012.


Figure 2. OMI top-of-atmosphere reflectance spectra on 4 November 2008, 13:37:24 UTC, and 13:38:02 UTC, of the green pixels in Figure 1 (black/green); and the normalised MODIS response function of channel 3 (red).


Figure 3. Scatter plot of OMI and MODIS collocated reflectances for the scene in Figure 1 using quadrangular OMI pixels (left panel) and optimised super-Gaussian ( $n=2, m=4$ ) pixels (right panel). The red dashed line is the linear least squares fit to the measurements, given by the linear function $\mathrm{y}=a_{0}+a_{1} \mathrm{x}$ in the plot. $r$ is Pearson's correlation coefficient and $\sigma$ the standard deviation of the points to the fitted line. The blue marked points have the largest $\sigma$ and correspond to the blue OMI pixels in Figure 1 N is the number of points and max $R_{\text {OMI }}$ and $\min R_{\text {OMI }}$ the maximum and minimum value in the plot, respectively.


Figure 4. One dimensional normalised super-Gaussian distribution functions with varying exponents $n$. The normal distribution $(n=2)$ is plotted in blue.


Figure 5. OMI 75FoV corner coordinates (dark blue filled circles), with the OMI centre coordinate (dark blue diamond), and collocated MODIS centre coordinates (black and coloured squares). The colours of the squares indicate the weighting of the MODIS pixels as indicated by the colour bar. a) Quadrangular weighting, with all MODIS pixels within the corner coordinates having equal weights, everything else disregarded; b) a 2D flat-top super-Gaussian with exponents $n=m=8$, resembling the quadrangular shape with smoothed edges; c) a 2D super-Gaussian distribution with $n=2$ and $m=4$; d) a 2D point-hat super-Gaussian distribution with exponents $n=1, m=2$; e) a 2D super-Gaussian distribution ( $n=2, m=4$ ) with twice the width in the acrosstrack direction; f) a 2D super-Gaussian distribution ( $n=2, m=4$ ) with twice the width in the along-track direction. Different OMI row number are shown (see panel captions) to show the change in orientation and number of MODIS pixels for different rows.


Figure 6. Pearson's correlation coefficient $r$ for OMI and MODIS collocated reflectances in the scene of Figure 1 as a function of super-Gaussian shape and size of the assumed PSF. The blue line indicates the correlation as a function of exponent $n$ (top panel) and $m$ (lower panel), for fixed 75 FoV corner coordinates. The red lines are the relationships for varying pixel sizes when the optimal Gaussian exponents $n=2, m=4$ are chosen. Note that the scales are logarithmic on both x -axes.


Figure 7. Left panel: MODIS RGB scene on on 7 October 2008, 10:20 UTC over the the Middle East. Yellow and red lines as in Figure 1 while the individual red OMI pixels are cloud pixels that were manually discarded. Right panel: Dependence of Pearson's correlation coefficient $r$ between the OMI and MODIS observed reflectance for the scene in the left panel as a function of super-Gaussian shape and size, as in Figure 6 The optimum in this case was found for Gaussian exponents $n=2, m=4$ and $1 \times 75 \mathrm{FoV}$ corner coordinates in both directions.


Figure 8. Same as Figure 7 on 11 October 2008, 04:45 UTC over Australia. The optimum in this case was found for Gaussian exponents $n=1.5, m=2$ and $1 \times 75 \mathrm{FoV}$ corner coordinates in both directions. A fit of Gaussian exponents $n=2, m=4$ is best for slightly larger pixels $(1.25 \times 75 \mathrm{FoV}$, red line).


Figure 9. Super-Gaussian exponents $m$ and $n$ as a function of OMI pixel row, averaged over all scenes introduced in this paper. The FWHM was fixed to the 75 FoV pixel sizes, shown in the lower panel, to determine the optimal exponent. The fat lines are boxcar averages using 5 points.


Figure 10. Same as Figure 7 on 7 January 2008, 13:45 UTC over the Sahara desert. The optimum in this case was found for a Gaussian exponent $n=1.5, m=2$ and $1 \times 75 \mathrm{FoV}$ corner coordinates, or $n=2, m=4$ and $1.25 \times 75 \mathrm{FoV}$ corner coordinates in both directions.


Figure 11. MODIS RGB image on 13 August 2006, around 13:33 UTC (lower part of the image). The yellow lines indicate the MODIS data granules and the red lines the considered OMI swath, which was from rows 10-50. The optimal correlation between OMI and MODIS for this scene was found for Gaussian exponents $n=1, m=1.5$ and 75 FoV corner coordinates. The correlation for this pixel shape is shown in the right panel.


Figure 12. Left panel: Simulated clear-sky reflectances for the reference scene in Figure 1 using OMI scattering geometries ( $x$-axis) and MODIS geometries ( $y$-axis). The colours indicate the OMI viewing zenith angle of each simulated pixel. The reflectances were simulated at 469 nm , for a standard atmosphere reaching to sea level, and an ozone column of 334 DU . The surface albedo was varied according to a database (see text). The underlying red dashed line shows the linear fit to the simulations. Right panel: same data as in the left panel, but plotted as the relative difference between the OMI and MODIS reflectances.

