Information content in reflected signals during GPS Radio Occultation observations

Josep M. Aparicio[1,3], Estel Cardellach[2,3], and Hilda Rodríguez[2,3]

[1]Meteorological Research Division, Environement and Climate Change Canada (ECCC), 2121 Transcanada Hwy, Dorval, QC, Canada
[2]Institut de Ciències de l'Espai, Consejo Superior de Investigaciones Científicas (CSIC), Cerdanyola del Vallès, Spain
[3]Institut d'Estudis Espacials de Catalunya (IEEC), Cerdanyola del Vallès, Spain

Correspondence to: Josep M. Aparicio (Josep.Aparicio@canada.ca)

Abstract. The possibility of extracting useful information about the state of the lower troposphere from the surface reflections that are often detected during GPS radio occultations (GPSRO) is explored. The clarity of the reflection is quantified, and can be related to properties of the surface and the low troposphere. The reflected signal is often clear enough to be coherent, and can be tracked and processed as an extension of direct non-reflected GPSRO atmospheric profiles. A profile of bending

5 angle vs. impact parameter can be obtained for these reflected signals, characterized by impact parameters that are below the apparent horizon, and that is a continuation at low altitude of the standard non-reflected bending angle profile. If there were no reflection, these would correspond to tangent altitudes below the local surface, and in particular below the local mean sea level. A forward operator is presented, for the evaluation of the bending angle of reflected GPSRO signals, given atmospheric properties as described by a Numerical Weather Prediction system. The operator is an extension, at lower impact parameters, of standard bending angle operators, and reproduces both the direct and reflected sections of the measured profile. It can be

10 applied to the assimilation of the reflected section of the profile as supplementary data to the direct section. Although the principle is applicable also over land, this paper is focused on ocean cases, where the height of the reflecting surface, the sea level, is well known apriori.

1 Introduction

Signatures of the interaction of the GPS signal with the Earth's surface have been recorded during satellite-based radio occultation (GPSRO) events (Beyerle and Hocke, 2001; Beyerle et al., 2002; Pavelyev et al., 2011). When this happens, besides the usual refracted signal (hereafter named direct) at the limb, another signal is detectable at lower elevation, often among

20 distorting phenomena of multipath propagation, superrefraction and strong attenuation, and is not always clearly defined. Both signals merge when the tangent altitude of the direct propagation path is at the surface. The abovementioned studies show that

this is the expected behavior of a signal that would have reflected off the Earth's surface, and that was unintentionally captured by the receiver, while it was tracking the direct signal. This second signal will be hereafter named reflected.

This reflected signal has interacted with the low atmosphere and the surface, and therefore constitutes a potential source of information of their properties, in addition to the atmospheric information that is normally provided by the direct signals. In

5 this study, a large number of recorded occultation events are analyzed for the presence of reflections, in order to characterize when reflections are to be expected, which information can be found in these reflected signals, and how this information can be used within the context of atmospheric applications, and particularly Numerical Weather Prediction (NWP).

GPS satellites emit in several regions of the L-band. The most important in the context of this work is the L1 (near 1.575 GHz, wavelength approximately 0.19 m). The signal is a very pure and coherent tone, modulated by several predictable phase

10 shift patterns (Parkinson and Spilker (1996), Ch. 3), which are specific to each emitter. In this work we focus on the C/A Pseudo Random Noise (PRN), a 1.023 MHz binary modulation of the sinusoidal tone. Receivers collect signals from several emitters, overlapped. Thanks to the characteristic modulation, receivers can decompose the received overlap into a sum of components, identifying several emitters. Signals from the same emitter that have followed two propagation paths may also be identifiable as distinct (Parkinson and Spilker (1996), Ch. 2, Sec VI), provided their optical length is sufficiently different, by at least one

15 modulation bit, which at 1.023 MHz corresponds to 300 m. Each identified component can then be tracked separately.

During an occultation, the direct signal has low elevation over the horizon. Any reflection will be grazing the surface, also at very low angular elevation, and the difference in their path length will be relatively small, of up to several tens of meters. This is large compared to the wavelength, but small compared to the length of GPS's modulation pattern of 300 m. Direct and reflected paths therefore show nearly identical modulation. Similarly, their frequencies (affected by Doppler effects) are

20 also quite similar near the surface, separated by only few Hz, and within the usual receivers' bandwidth. Also, at this very low elevation, and unlike at higher incidence angles, a reflection does not lead to a reversal of the polarization. Although GPS receivers are designed to separate in most cases the different components of the received signal, either by polarization, or through PRN modulation, the specific case of the direct and reflected paths near the horizon appears as particularly challenging.

This separation is still possible, as detailed below, analyzing the spectral distribution (Hocke et al., 1999) of the sum of both

25 direct and reflected signals. Separability is possible if the spectral distributions of the direct and reflected signals are sufficiently compact and distinct. This is indeed often the case, and as shown below, the analysis of large amounts of occultations (over 4 million events, worldwide distributed over 9 years) indicates that in a substantial fraction both direct and reflected signals are sufficiently clear to be separable, and that both still substantially maintain the coherence of the emitted tone, which allows their use for further processing (Cardellach et al., 2008). Given that the signal phase plays a central role in GPSRO data, which is

30 after all an interferometric procedure, the narrow spectral distribution of these signals, and thus their coherence, is critical to their value as a source of interferometric data.

A test of the geographical distribution clearly indicates a correlation between the clarity (coherence) of the reflected signal captured by the receiver, and qualitative properties of the surface, being particularly common over comparatively smooth surfaces, and notably the oceans and ice in polar regions. This is the expected behavior for quasi-specular reflection, which

35 maintains signal coherence. Land, instead, with a generally much more irregular surface, is expected to produce diffuse scatter,

where signal coherence is lost. Boniface et al. (2011) showed that reflected signals in radio-occultation events could also contain geophysical information about the lowest layers of the troposphere (lowest few km), provide information about the state of the low troposphere, and are therefore potential sources of meteorological information, additional to the non-reflected profiles, which have suffered only refraction and that are already used as measurements of the profile of atmospheric refractivity.

5   This frequent clarity in the spectral separation between the direct and reflected signals implies that, in principle, it is possible to interpret their properties independently, and that both may provide useful geophysical information. This has been shown to be possible, for instance, in occultations over ice in polar regions (Cardellach et al., 2004), where the extracted quantity was the height of ice above sea level from interferometric phase data of the reflected signal. Besides the height of the surface, the reflection depends also on the refractive index of the atmosphere, mostly on the properties of the low troposphere, which is the

10 focus of the present study. It is attempted here to extract atmospheric information that would be usable in the context of NWP, particularly to provide additional information about the temperature and moisture profile in the lowest 5 km. This study is restricted to ocean reflections, where we can assume that the height of the reflecting surface is well known a priori: the average sea surface. The exact sea surface is continuously changing due to ocean waves, however departs vertically by at most few meters from the mean sea level. In limb-looking geometry, this departure of the actual sea surface from the mean sea surface

15 modifies negligibly the length of the propagation path. Over land, topography, albeit static, is a strongly irregular surface near the tangent point, whose reflective properties are spatially very variable. The exact vertical location of a reflection over land is in general unknown by tens or even hundreds of meters. Besides showing less cases of clear coherent reflection, the practical use of land reflections in those cases where it is coherent, would require solving, besides tropospheric properties, additional unknowns related to the topographic height of the reflecting surface. Therefore, the qualitative properties of reflections over

20 land are explored in this study, but the use of reflected interferometric products in NWP over land is, for this reason, considered out of scope.

    Atmospheric information normally extracted from radio occultations is derived only from direct data, which has interacted only with the atmosphere, through refraction. If atmospheric information can also be extracted from ocean reflected data in at least a significant fraction of the occultations, as indicated in this study, we may infer the existence of a significant pool of data

25 sensitive to the properties of the lower troposphere, which can be useful for applications in NWP, and which is so far unused. These would be additional to, and well collocated with, the standard radio occultation profiles.

    The fact that the open ocean shows better signatures, and that these can be interpreted as atmospheric measurements, rather than a combination of atmospheric and topographic, is well suited to the needs of data acquisition for weather forecast, as the pool of available low altitude information from other sources is particularly scarce over oceans. Radio occultation has

30 otherwise provided a very significant amount of atmospheric data worldwide, which has been of particular value over remote areas, including oceans and polar regions (e.g. Healy and Thépaut (2006), Cucurull et al. (2007), Aparicio and Deblonde (2008), Rennie (2008)). These same studies of forecast impact indicate that the low troposphere is the region where direct (refracted-only) radio occultations are less accurate, and therefore where adding supplemental information would be most helpful.

Recently, two spaceborne missions specifically dedicated to collect GPS reflected signals have been launched into Low Eart Orbit: UK's TDS-1, in 2014 (Unwin et al., 2016) and NASA's CYGNSS, in 2016, (Ruf et al., 2013). ESA is also planning a Global Navigation Satellite System (GNSS) reflectometry (GNSS-R) experiment from the International Space Station, the GEROS-ISS (Wickert et al., 2016). Although these missions use GPS and GPS-like signals to infer properties of the Earth's

5 surface, it must be noted that the technique described in this study is not the same. The main differences are, firstly, the geometry (near-nadir in these dedicated missions vs. grazing angles in this study) and the nature of the scattering. At near-nadir angles, the irregularity of the surface (topographic, ocean waves, etc) is larger than the GPS wavelength. Scattering is diffuse and incoherent. Receivers do not expect to collect a coherent electromagnetic signal. At grazing angles, as in this study, the path difference caused by the irregular surface may be negligible. The receiver is identifying a signal that still maintains

10 coherence, and where interferometry is still possible. A non-scaled sketch of both concepts is depicted in Figure 1. Table 1 also summarizes the main differences.

Another mission that it is interesting to compare against, is the active Synthetic Aperture Radar (SAR) component of the Soil Moisture Active–Passive (SMAP) mission (Piepmeier et al., 2017), which also studies the reflection on the Earth's surface of L-band signals, in this case at 1.26 GHz. The geometry of this mission is also near-nadir, and therefore comparable with the

15 dedicated missions just mentioned, which analyze the incoherent scatter.

This study is structured as follows. Section 2 overviews some properties of the GPS signals, that are relevant to the grazing reflections during limb observations. Section 3 explores a large sample of GPSRO events, looking for reflections. A number of qualitative properties are identifiable: average occurrence, ocean vs. land difference, qualitative properties of the surface, detectable seasonal cycles, and relationship with atmospheric properties. The statistics of reflection clarity and occurrence

20 indicate where and when it is to be expected to find clear coherent reflected signatures, and therefore where new interferometric information is present. Section 4 explores the separation of the reflected signal, for those cases where coherence allows it, and the creation of an interferometric profile product out of the reflected signal. This product is similar to the standard bending angle profile obtained from direct data, but supplementary to it. It is shown that these data are very sensitive to the refractivity of the low troposphere. An operator is presented that may use this information in the context of NWP. It is an extension to a

25 standard class of operators that already use direct radio occultation data in this context. Examples of use are provided. Section 5 comments the results obtained, and the potential lines of further exploration.

2   Received signals

GPS satellites carry atomic clocks, which produce pure sinusoidal tones. Before emission, these tones are modulated by characteristic bitstreams. Focus here is on the C/A signal, modulated by the PRN at 1.023 MHz, and also by a 50 Hz stream of

30 navigation bits. The receiver hardware can decompose and demodulate the received PRNs, and we assume that the navigation stream can be obtained from either direct measurement or from ancillary sources. Also, the orbits of both emitter and receiver are assumed to be known, from the analysis of navigation data, allowing the subtraction of any orbital Doppler. If an undisturbed signal is received, demodulation and Doppler subtraction will return the signal to the original unmodulated sinusoidal

carrier tone. This would happen, for instance, if propagation took place in a vacuum, and there was negligible electromagnetic noise. Since the propagation has instead traversed the ionophere, the atmosphere, and perhaps bounced off the surface, there may be delays, multipath, or focusing/defocusing. After demodulation and Doppler subtraction, the signal recorded by the receiver will not return to a pure constant tone. It may show a residual Doppler, amplitude variations, and frequency broadening.

5 These are the signatures of the interaction with the ionosphere, atmosphere, and eventually with the surface. They constitute the primary data for the analysis of atmospheric radio occultations (Kursinski et al., 1997), where they are interpreted as observations indicating the refractivity of air, at different altitudes. These are as well the primary data for the present purpose.

The profiles analyzed here are obtained from the Constellation Observing System for Ionosphere and Climate (COSMIC) mission (Anthes et al., 2000), which maintain a good signal to noise ratio at low altitude. Data from only one of the GPS

10 frequencies are considered: L1 (1.57542 GHz). After demodulation, it is sampled at 50 Hz. COSMIC also collects signals from GPS L2 (1.22760 GHz), but these measurements are noisier, both due to the lower emission power of L2, and because the signal structure requires the use of a different and less accurate tracking algorithm. During occultations, L2 can only rarely be tracked within the lower troposphere. This is not a particular limitation, neither for the standard processing of direct non-reflected signals (Zeng et al., 2016), nor for the processing of reflected signals presented here. L2 is required to identify and quantify

15 the effect of the ionosphere, and for such purpose it is sufficient to record and process L2 at higher altitude. Atmospheric radio occultation profiles of refracted-only data are also obtained with only L1 in the low troposphere (Zeng et al., 2016).

The measured record is thus a 1-dimensional (in time) stream of signal phase and amplitude, already demodulated and corrected from orbital Doppler. Following the principle of the radio-hologram (Hocke et al., 1999), another reference signal is created, intended to capture the main, low frequency evolution of the phase, but without fluctuations in amplitude, or in

20 high frequency in phase. The received signal is then counter-rotated by this reference, resulting in a signal that may contain activity, but rotates slowly, and occupies only a narrow frequency band. The target, in particular, is to not exceed one half of the sampling frequency, and to avoid aliasing.

The remaining activity is analyzed with a sliding Fourier Transform. The new representation is obviously redundant, as it is a 2-dimensional representation (time, frequency) of the initial 1-dimensional stream of data. In exchange, it allows a better

25 representation of the departure of the recorded signal from a pure tone. Besides the tone corresponding to the direct signal, a supplementary tone may be identifiable, which suggests the presence of a reflection (Beyerle and Hocke, 2001). One or both of the ordinary and supplementary tones may be broadened, or even split. Figure 2 shows an example of a radiohologram that presents a reflection. The broadening and splitting (multipath) are common, and suggest a complex refractivity structure in the low troposphere.

30 The direct propagation paths probe the low troposphere only when the tangent altitude is in the low troposphere. Reflected paths, instead, always probe the entire atmosphere, including the lower section, albeit at varying incidence angles. The accuracy of an atmospheric profile retrieved exclusively from direct propagation, at any given altitude, is limited by the accumulation of any error or distortion at all upper altitudes. The supplementary reflected tone may also present complex structure, especially at very low incidence, where it may even be difficult to differentiate from the direct path. However, reflected signals are also

35 detectable far from this complex broadening, when both paths are narrow and distinct. Whereas complex structure in the direct

path makes it difficult to probe the properties of the lower troposphere, the reflected tone may present sections that are less broadened, offering additional opportunities to provide information about these low layers.

3   General description of reflections in radio occultation

This section first briefly summarizes, and then extends, the preliminary studies presented in Cardellach et al. (2008, 2009),
5   a methodology applied to identify and quantify reflected signals in occultation profiles, to study the geographic and seasonal distribution of the occurrence of reflections during occultations, and to provide some quality indicators.

The identification of the presence of reflected signals is based on Support Vector Machines (SVM), a supervised computer learning method (Joachims, 2002). The algorithm allows the training of a computer for automatic identification of target features. The algorithm is applied here to the 2D radio-holographic representations of the event, an example of which is shown
10   in Figure 2. The details of the implementation for this particular process are compiled in Cardellach et al. (2009). The SVM is trained to identify the presence of the secondary (reflected) tone in the radio-hologram, and to provide a quantitative indicator of its clarity. The output of the SVM is a real-valued scalar, which is related to the likelihood of presence of a reflection signature: an above-noise, compact feature in the radio-hologram, with the appropriate shape and location in the time-frequency space to agree with the expected properties of a reflection. The scalar presents positive values for likely-reflection, and negative values
15   for a lack of it, and is normalized to provide values beyond ±1 when the algorithm has a very large confidence in the resulting classification, and between -1 and +1 when the system shows only some moderate confidence.

The SVM was trained (Cardellach et al., 2009) with a set of 6468 occultations, selected by visual inspection of the radio-hologram as representing events of clear reflection, and clear lack of reflection. Once trained, the SVM was validated with an independent set of GPSRO occultations observed with the COSMIC mission, and consisting in 3350 events in February
20   2007, and 2257 in November 2008, also visually inspected and manually flagged. The validation determined (Cardellach and Oliveras, 2016) that the percentage of error (false positives or negatives) of the SVM classification is acceptable for threshold values greater than 0.25 (97.81% success for the February 2007 sub-set, and 99.47% for November 2008).

This trained SVM is then able to automatically flag other occultations. It has been used here to study the statistics of reflection events in a much more extended set of occultations, which extensively includes several years of COSMIC data. This
25   set represents over 4 million radio-occultations, globally distributed and broadly covering the entire Earth, all seasons and local times, from the beginning of the COSMIC mission in 2006, to mid 2015.

For the purpose of this study, radio occultation events with SVM value greater than 0.25 are identified as reflections. Given the very large success rate of classification at this threshold (low ratio of false positives), there would be little gain in classification accuracy with a larger SVM threshold. Instead, it would greatly reduce the number of events identified as reflected, and
30   limit the usefulness of these as a potential source of data. The fraction of GPSRO events that present reflection is a substantial fraction of the total, and shows several several clear patterns of variability, mainly according to the type of surface, ocean or land, and by latitude. It is found that ∼50% of the GPSRO events in this dataset over extra-tropical oceans show a reflected signal, and ∼70% in near-polar oceans. Reflections over non-polar land occur rarely, up to 13% of the total land GPSRO cases

at latitudes $\leq 70°$. Over polar land or ice regions, the number increases significantly, up to 52%. According to these results, reflections are more likely over some surfaces, but might occur over any sort of surface (ocean, ice, land). A summary is compiled in Table 2.

3.1 Land events

5 The coherent reflected signal that the SVM is trying to identify, which presents power concentrated in a narrow frequency band, corresponds to a specular reflection. The land surface appears to be less prone to this kind of interaction with the signal. We must remind here that the GPSRO receiver, and the classification of the radiohologram identify coherent signals, and therefore specular reflection. Although soil moisture of vegetation may also be reflective in the L-band, irregular surfaces destroy coherence, and lead to non-specular diffuse scatter. Nevertheless, coherent reflection still appears to take place over

10 land, in a significant fraction of events, more frequently over areas known to be smooth, both in topography and when they are free of thick vegetation (see Figure 3). Among others, could be mentioned central Asia, near the Caspian and Aral seas, or certain areas of the central US and Canadian prairies. Reflections appear to be particularly common over continental ice (Greenland, Antarctica). Given the electromagnetic band at which GPS works (L-band, wavelength ~ 0.19m) and the very slant geometry of these observations, the general lack of reflections over rugged terrain, and where thick structures of vegetation

15 canopy are present, could be expected.

The presence in desert areas, generally not particularly reflective, of some of the events that the SVM classifies as reflections, suggests that we should not discard that these events include as well some cases of non-reflective interaction with the surface, such as a mirage. For the purpose of tracking this signal, and extracting information of the refractive index of the low troposphere, the difference between both is negligible: there is an effective quasi-specular surface at the ground, or very

20 near to it. We will hereafter use the label *reflection* meaning that the signal propagates at a grazing angle until the surface, and coherently proceedings forward to the receiver. Despite the low percentage of presence of a reflected signal over land surfaces, seasonal patterns can be noticed in the areas where reflections are more common. This is shown in Supplementary Movie 1, which presents the median SVM over land, in bi-monthly sections over the seasons, accumulating all 9 years of data.

Some of the seasonal patterns are found in near-polar land areas, where there is a winter cover of snow and ice, and little dif-

25 ference is to be expected during this period with respect to the behavior over neighboring ocean ice (northern coasts of Alaska, Canada, and Russia). Additional patterns are found (see Supplementary Movie 1) over certain regions that are topograhically flat, consistent with the seasonal thinning and thickening of deciduous vegetation. Examples are the Pampa region in Argentina, a steppe, and the Southern Great Plains in the US. In all these, more reflections appear during the local winter, as should be expected if reflection takes place at the moist or snow-covered ground, or is otherwise diffusely scattered by vegetation.

30 ## 3.2 Ocean events

As mentioned in Table 2, the percentage of captured ocean reflected signals strongly depends on latitude. Figure 4 displays the geographical distribution of the fraction of ocean events that show reflections, for two bi-monthly periods of the year: January-February, and July-August, both accumulated over the ensemble of events, which spans 2006-2015. These geographi-

cal distributions also show seasonal patterns, which are particularly prominent where larger gradients of reflection percentage appear, in the midlatitudes of both northern and southern hemispheres. The tropical oceans always present much lower percentage of reflections than mid-latitude ones. Comparison of the two panels in Figure 4, shows that this tropical region with less reflections is shifted southwards during austral summer, and northwards during boreal summer. The maps also show cer-

5 tain interesting geographic patterns: when compared against their latitude band, certain ocean regions show a systematically larger or smaller fraction. Areas that show larger fraction are, for instance, in the Pacific Ocean, the northeast (California) and southeast (Chile), and in the Atlantic Ocean, the southeast (Namibia), northwest (New Foundland), and the northwest African coast.

The ocean surface is much less rugged than land, and at these very slant geometries and for the L1 wavelength, it should

10 behave as a highly reflecting smooth surface (Ulaby et al., 1986). The fraction of events over open ocean is indeed larger than over land in general, with the exception of ice-covered surfaces. However, there is still a significant portion of the ocean GPSRO events that do not present clear reflected signals. As detailed below, we explore the possibility of this lower rate of tropical coherent reflections being caused by instrumental limitations, by the sea surface itself, or by the atmosphere.

Concerning instrumental limitations, these signatures appear at the deepest part of the occultation, when the direct radio link

15 scans the lower troposphere, and where the tracking algorithms might already have difficulties. This may explain a percentage of missing reflections in ocean GPSRO data, as well as the difference found between the percentage of reflections in rising and setting occultations (almost a factor of two). The depth that is reached by the GPSRO profile may be linked to the opportunity of capturing a reflection: if an event does not reach the low troposphere, it may as well be unable to collect the reflected branch of the signal. This hypothesis has been checked through the statistical distributions shown in Figures 5 and 6, and found to

20 be only partially true. The ocean events with likely presence of reflection (high SVM values) do tend to reach the lowest layers of the troposphere, especially the lowest 2 km (Figure 5), which is consistent with the hypothesis. However, as shown in Figure 6, the ocean GPSRO events that do reach the low troposphere may or may not present reflected signals. In Figure 6, the distribution is still well populated for negative SVM values (no clear reflection). Therefore, reaching the low troposphere during an occultation over the ocean seems to be a favorable but not a sufficient condition to capture a reflection.

25 The latitude profile of the percentage of reflections is shown in the upper panel of Figure 7. The profiles are evaluated over bi-monthly blocks through the seasonal cycle, accumulated over the entire study period. It shows that the pattern of lower fraction of reflections in the tropics and lower midlatitudes displaces smoothly in latitude following the seasons, and that the fraction of reflections at latitude $> 45°$ is always large and about 70%. This seasonally-driven meridional shift of the reflection percentage can also be clearly seen in the maps in Supplementary Movie 2, which shows the median SVM over ocean, evaluated over the

30 seasonal cycle, in bi-monthly sections, accumulating all 9 years of data.

The fraction of events that presents reflections shows a large meridional gradient in the bands at latitudes between 40°-50°, both north and south. In these bands the fraction of reflections changes quickly from sparse (20% in the tropics) to frequent (70% circumpolar). Due to this gradient, the local seasonal pattern presents in these two bands the largest seasonal amplitude. The lower panel of Figure 7 shows the monthly fraction of reflections in each of these two bands, over 2006-

35 2014, which also underscores this seasonal pattern, as well as the contrary phase between both hemispheres. These patterns,

consistently associated with geographic and seasonal features, do not suggest a direct relationship with instrumental problems or performance. They may, at most, be linked to instrumental performance issues if these arise under certain geophysical conditions related to seasons or geography. Therefore, the core variability of the lower fraction of GPSRO reflections in tropical oceans, or during the respective warmer season of midlatitude oceans, must be searched in environmental phenomena, either
5 atmospheric or oceanic.

Some indications about the associated geophysical phenomena can be found empirically, correlating certain weather parameters at the location/time of the event against the presence of reflection. The fields from the ECMWF ERA Interim analysis are used here to determine the weather state. The correlations presented in the following are all computed using monthly averages evaluated on cells of $10° × 10°$ over the oceans, with the reflection fraction compared against several environmental variables.
10 The number of pairs to correlate is therefore the number of ocean cells times the number of months considered.

We might think that, as for land reflections, the surface roughness might play some role. At these grazing angles of elevation, even the largest ocean waves are very small compared to the vertical scale that determines signal coherence, the Fresnel diameter (which is $> 100m$). The difference in path length d that would be associated to waves of height H in the surface is $d = 2H \sin(e)$, with e the elevation angle of either the emitter or receiver, seen from the reflection location. e is less than $1°$,
15 and d is thus a small fraction of the GPS wavelength for all realistic wave heights. At this incidence angle, the sea is effectively a very smooth surface, as sensed by at GPS wavelength, producing specular reflections. The surface roughness due to waves cannot be the prime driver that determines the presence or lack of reflected signals. Indeed, the correlation between percentage of reflections and significant wave height happens to be very low, at $r = 0.04$, which confirms the above estimation that the roughness produced by waves is not sufficient to affect the coherence of the reflection.
20 On the other hand, the correlation of the fraction of reflections against the sea surface temperature (SST) is strong and negative (r = -0.80): warmer sea surface temperatures are associated to a low fraction of reflections. The relationship between reflected signals and SST was also visible in Figure 4. The above mentioned features along the West coast of North and South America, West South Africa, Northwest Africa, West Australia and North-Eastern North America are all regions of cold surface water. Similarly, regions of typically warmer water in the Coral Sea, Caribbean, East Africa and the Arabian Sea
25 are also regions presenting comparatively less reflections. These features present as well (Supplementary Movie 2) seasonal variations consistent with sea surface temperature.

The dependence of the electromagnetic reflectivity with temperature at the air to sea water interface was explored as a potential cause, but was ruled out. Despite being true that the Fresnel reflection coefficients present some dependence on the temperature of the surface (Ulaby et al., 1986), the coefficients for the co-polar component of circularly polarized signals
30 (RHCP incident, RHCP reflected) do not change significantly with temperature at the grazing angles of observation: there is less than 0.1% variation over temperatures between $1°$ and $20°$ C, at incidence angles greater than $80°$.

As a consequence, the modulation of the occurrence of ocean reflected signals in GPSRO events must not be directly linked to the surface itself, its roughness or its temperature. Instead, it should be linked to the different atmospheric conditions that take place above the water surface, and associated to its temperature. Cross-correlations with other atmospheric variables were also
35 performed and are shown in Table 3. For instance, Figure 8 shows the percentage of reflections against the column of water

vapor (CWV). Most of these variables also show a meridional and seasonal dependence. The correlation, however, may be stronger or weaker than that of SST, which may help to identify the primary cause of clear or unclear reflections on ocean. The presence of coherent reflected signals also appears to correlate significantly with the column of water vapor, and the vertical integral of total energy, in all cases negatively, with correlation coefficients close to -0.8. The next variables, by strength of

5 the correlation, are the temperature in the low troposphere and water vapor pressure (correlation r around -0.7). However, the relative humidity does not seem to play a central role (r=0.26). As mentioned above, the significant sea wave height is nearly uncorrelated (r=0.04), although wind speed over sea has a moderate positive correlation (0.43). This was somewhat unexpected, as stronger winds correspond to rougher sea surfaces, which could seem to link to less chances of coherent reflections. The fact that the height of sea waves does not correlate with the presence of reflected signals, added to the fact that the wind-reflection

10 correlation is positive (more reflections for stronger winds), might indicate that wind itself is not the driving element either, but it would point to atmospheric conditions that tend to occur associated with wind.

A parameter that presents a high and positive correlation with the presence of reflected signals is the difference between the environmental temperature lapse rate (Γ) and the saturated adiabatical lapse rate (Γ_s), indicative of atmospheric stability. These conditions indicate that reflections appear more frequently with a stable layering of the atmosphere. The moderately

15 positive correlation with wind, which mixes air, and with stable layering, together with the large negative correlation with surface temperature, which weakens the stability, suggests that a likely root cause of the modulation of events that present a reflections may be the horizontal homogeneity of the atmosphere. The signal is propagating horizontally through the low troposphere, which can be optically very heterogeneous (strongly variable refractivity). The correlations found are compatible with coherent reflections appearing when the atmosphere is well stratified near the tangent point. It is interesting to note that

20 these stable conditions are also related to the appearence of propagation ducting (von Engeln and Teixeira, 2004), or super-refraction, which show a very similar spatial and seasonal distribution (Xie et al., 2010).

The relationship between the preservation of coherence and stability suggests that the physical relationship involved is the homogeneity/irregularity of the field of refractivity. The signal is traversing the atmosphere quasi-horizontally, through some 200 km of low troposphere. The atmosphere along this path may be optically irregular, presenting strong variations of

25 refractivity, distorting the propagation of the signal. This was tested verifying if the atmosphere was optically homogeneous in the vicinity of the occultation, in all ocean events (about 10000 occultations) over a period of 3 weeks (1-21 July, 2015). The standard deviation of the refractivity at a given altitude, within 200 km around the occultation, was taken as a measure of optical heterogeneity. Since atmospheric refractivity is mostly modulated by moisture whenever the amount of water vapor is significant, this is primarily a measure of irregularity in the field of water vapor. The horizontal heterogeneity in the refractivity

30 was evaluated from the background fields of Environment Canada's operational short-term global forecasts (Charron et al., 2012), whose grid resolution is 25 km. The correlation of coherent reflections against this parameter indicates that these are indeed less frequent with more heterogeneity. Correlation was performed against heterogeneity at different altitudes. This relationship is negative, and stronger (r=-0.64) against the optical heterogeneity at altitudes between 1.5-3 km. This corresponds approximately to the height of the atmospheric boundary layer, and is a physically expectable behavior, since there are indeed

35 particularly strong refractivity gradients at that altitude (Guo et al., 2011).

4 Numerical Weather Prediction value

The previous section presented the observed fraction of occultations that show a reflection signature. Over ocean, the fraction is large enough to contitute a large pool of available events, and therefore worth processing further.

Cardellach et al. (2008) noticed that radio-occultation events that have reflected signals tend to correspond to cases where the extracted atmospheric profile of refractivity, obtained in that case exclusively from direct signals, agrees better with the values estimated from an NWP model, than cases without clear reflected signals, as tested against the European Centre for Medium Range Weather Forecast (ECMWF). The presence of the reflection was there used as a flag, signaling a particular statistical behavior of the measured data within a subset of events, but no additional measurements were extracted. That study was then extended to nearly 170,000 GPSRO events over oceans in Cardellach and Oliveras (2016). The results of this second analysis confirmed a better agreement between direct data and the background field when reflections are present: both the bias and the RMS difference between the measured refractivity and the NWP background field, are significantly smaller in the lower 10 km of the troposphere. These results were also consistent with the study by Healy (2015). Although this does not mean that the data are of better quality, it does mean that the presence of reflection is at a minimum a marker for data that show better observation minus background (OMB) agreement than the average GPSRO event. It is interesting to note here, that the reflection flag, either a qualitative present/absent, or the quantitative SVM value, stems from the observation, and that the knowledge that an occultation is expected a priori to show lower OMB difference than an average occultation is already a supplemental NWP value to the standard profiles of direct non-reflected signals.

In those studies, the reflected portion of the signal was only an indicator for a distinct expected statistical distribution of the direct profile, and was not used in the construction of the output product. We try here to produce supplementary data to the standard output profile, using phase and amplitude data extracted from the reflection signature, and producing extended profiles with additional assimilable data.

Both the height of the reflective layer and the properties of the low troposphere have an effect on the optical path length, and on the relationship between path lengths at different angles of incidence. Therefore, as a first step, and in order to simplify the interpretation of the data, we will restrict to the case where we know a priori the topographic height of the surface with good accuracy (few meters), which in this study means the open ocean, whose topography we will assume to be equal to the mean sea level, as determined by the reference equipotential surface of a geoid model (NIMA, 2000). If finer precision of the reference surface was needed, tidal models could also be added.

4.1 Separation of the reflected signal

Occultation events that present high SVM values correspond to profiles with a clear reflected feature, such as the one that was shown in the radio-hologram in Figure 2. In these radio-holograms, the reference signal is a smoothed version of the total signal, which closely follows the direct radio link. A method based on the identification and isolation of the reflected branch in the spectral domain of these clear cases was implemented for this study. This is done with a 2D cross-correlation process between the radio-holographic image and a *template* 2D image. A mirror transformation in time is applied for rising occultations. The

cross-correlation identifies the time location of the reflection event, and the time section where it is identifiable. Within this interval, the complex spectral content of the radio hologram is set to noise level for frequencies higher than $f > -5$ Hz. This frequency margin is selected to avoid contamination from the direct signal, which can be noisy, with wide frequency spread, within the section of the GPSRO event in the low troposphere. This selection, within the radiohologram, of spectral content

5 from the reflected signal, is illustrated in Figure 9. This content is intended to include signal that is clearly part of the reflected signal, but not necessarily all of it. Some of the reflected power, especially near merging, has a frequency within less than 5 Hz of the reference signal. It may also present aliasing, and appear around $f \sim +25$ Hz. Both are here masked, and are not extracted.

An inverse Fourier Transform of this filtered complex spectrogram, results in a time series of complex phasors (delay/amplitude),

10 which are identified as the reflected signal. This interferometrically obtained reflected signal presents a frequency $f_I = f_R - f_D$, where f_D is the Doppler frequency of the reference direct link, and f_R the one of the reflected signal. Let us remember here that the reference f_D is known, as the interferogram was built as the interference beat the input signal against this reference, see Section 2. The Doppler frequency $f_R(t) = f_I(t) + f_D(t)$ of the reflected signal can be processed to bending angle and impact parameter by means of standard equations (Kursinski et al., 1997), normally used for profiles of direct signals. An example of

15 inversion to bending and impact parameter is shown in Figure 10. The reflected data leads to a supplementary section of the bending profile, at low impact parameter. As part of the 5Hz mask mentioned, the curve does not show the part of the reflected section that is near the direct profile, where the direct signal is tangent to the surface. In principle, both should merge, although it is difficult there to separate the fractions of signal that are direct and reflected. Instead, reflected data far from this tangent path, which can be clearly separated from the direct path, does provide a profile section. The formal precision of the inversion

20 of the holographically extracted signal, to Doppler and then bending vs impact parameter, is thinner than the thickness of the line.

4.2 Forward operator of the bending angle

Let us consider an occultation passing through a planetary atmosphere. We will assume a quasi-spherical planet. Locally, the shape of the atmosphere will be described by a tangent ellipsoid, which observed along a given azimuth, reduces to an

25 osculating circle of radius R. It will be assumed that the propagation can be described sufficiently with geometrical optics, or that through preprocessing (such as backpropagation), the list of measured phase/amplitude values has been reduced to an equivalent that is free of diffraction.

We will also assume that the atmosphere has a refractive index field n that, locally, is sufficiently well described by a function $n(r)$, dependent only on the distance r to the center of curvature, that n never deviates largely from the vacuum value $n = 1$,

30 and tends to it at large r. We also assume that the index of refraction mostly follows the trend $dn/dr < 0$, but allowing the presence of some exceptions, which may be caused by some temperature inversion layers, the presence of a moist layer, as well as in the ionosphere.

Let a be the impact parameter of a propagation ray with respect to the local center of curvature. If the refractivity field is spherically symmetric, a will be conserved along the path. Let $a_S = n(R) \cdot R$ be the impact parameter of a hypothetical ray

whose tangent point is exactly at the surface. A signal that propagates without ever reaching the surface, will present $a > a_S$. These are subject only to refraction, and we will name them as "direct rays." This is the standard situation (Kursinski et al., 1997): the ray reaches a minimum distance r_t, at the tangent point, where $a = n(r_t) \cdot r_t$, and proceeds away from the center of curvature. The bending suffered by refraction during its propagation will be:

$$5 \quad \alpha_D(a) = -2a \int_{r_t}^{\infty} \frac{d\ln n/dr}{\sqrt{n^2 r^2 - a^2}} dr \tag{1}$$

The integral represents the gradual accumulation of refractive bending, inwards from $r = \infty$ to the tangent point r_t, and again outwards from r_t to $r = \infty$, thus the factor 2. Since the quantity $\frac{dn}{dr}$ is most often negative, bending is generally curved towards the planet (net positive α_D). Of course, in cases where $\frac{dn}{dr} > 0$, as may happen in an inversion layer, and is normal in the ionosphere, the ray may be curved, locally, away from the planet.

10   A signal with impact parameter amaller than a_S, will reach the surface and, if the surface quality is appropriate, may reflect there. We will name these as "reflected rays". This is a physically new phenomenon that must be included in the evaluation of the bending angle of the ray as a function of the field of refractive index. The ray differs in two ways from the direct path described in Equation (1).

     Firstly, a reflection takes place exactly at the surface: $r = R$. The ray arrives there with a grazing angle $\alpha_G = \frac{\pi}{2} - i$ that is not yet zero, with i the incidence angle at the surface. By the Snell's law of refraction, the incidence at the surface follows $R \cdot n(R) \cdot \sin i = a$, and therefore the grazing angle:

$$\alpha_G = \arccos(\frac{a}{a_S}) \tag{2}$$

Due to reflection, the direction of the ray suddenly changes at the surface, by twice the grazing angle, away from the surface.

     Secondly, the integral does not extend from infinity to the tangent point. This tangent point is never reached, and the gradual refractive bending instead extends from $r = \infty$ to $r = R$ (instead of $r = r_t$), and equivalently for the outgoing portion of the ray. As a result, the expression of the bending of this "reflected" ray is:

$$\alpha_R(a) = -2a \int_{R}^{\infty} \frac{d\ln n/dr}{\sqrt{n^2 r^2 - a^2}} dr - 2\arccos(\frac{a}{a_S}) \tag{3}$$

Equation (3) shows bending to be partially caused by refraction (first term), associated to the atmosphere, which is generally positive, towards the surface, and partially by reflection (second term), which if present is always negative, away from the surface. For rays with low grazing angle (a only slightly smaller than a_S), the atmospheric bending dominates, with net positive bending. At progressively smaller impact parameters, the ray will reach the surface at larger grazing angles. The second term grows, reducing the bending, and leading eventually to negative total bending angles. The grazing angle is of course only defined for $a \leq a_S$, as for $a > a_S$ the ray never touches the surface. In general, and unlike in Equation (1), the lower extreme of the integral does not fulfill the tangent condition. That is, it is in general *not true* that $a = n(R) \cdot R$ for reflected rays. Equations (1) and (3) represent two branches of the bending profile, respectively for $a \geq a_S$ and $a < a_S$. These two branches join continuously at $a = a_S$, where it is true that $a = n(R) \cdot R$, and $\alpha_G = 0$.

The extended reflection branch shows a qualitative difference against the direct branch: bending normally decreases at lower impact parameter. In the purely refractive case, this would be associated to an inversion. A forward operator that does not consider the possibility of reflection, and faced to an observation where bending decreases quickly near the surface will therefore be forced to attribute it to a strong refractivity inversion near the surface. These are known to be moderately common

5 (von Engeln and Teixeira, 2004), although the operator should be able to estimate if a given event is a surface reflection, which will be most often the case, rather than an atmospheric inversion.

In the zoomed plot of Figure 10, the observed reflected section of the profile is compared against the calculated reflection, using several realistic estimations of the refractivity profile, applying Equation (3). The estimates of refractivity include the profile determined exclusively from direct data, an NWP-estimated profile (an ECMWF profile as provided by COSMIC),

10 and a 1DVar inversion using direct-only data. The difference between these is well above the formal precision of the reflected bending profile, and therefore the reflected bending is sensitive to their difference well above noise level.

Interestingly, the slope of the reflected profile is very sharp, when compared with the direct profile. Therefore, whereas several candidate profiles of refractivity, as seen in direct α versus a space would differ mostly in bending, the reflected data differ most in impact parameter space. The cause of this slope is the second term of Equation (3), which depends on the

15 apparent elevation of the horizon $a_S = n(R) \cdot R$. Indeed, the reflected curve sharply constrains observationally this value, directly related to the refractivity at the surface. It is to be noted that the direct profile may measure the atmosphere, perhaps down to the surface if conditions are appropriate, but the fact of having reached the surface, and therefore establishing that the profile is complete, is not determined observationally from direct data alone, but from our independent knowledge of the shape of the Earth. This supplementary data, instead, offers an observational determination of the completeness of the direct profile.

20 A notable feature of both Equations (1) and (3) is the Abel kernel.

$$K(r) = \frac{1}{\sqrt{n(r)^2 r^2 - a^2}} \tag{4}$$

This kernel represents the exposure of the ray to properties of different layers of the atmosphere, and therefore the sensitivity of that ray to the exact properties of each layer. In the case of bending, the property to which the ray is exposed at each layer is the relative refractivity gradient $d\ln n/dr$. For direct, non-reflected propagation paths, this dependency of the properties of the

25 bending with respect to the atmosphere, presents sharp peaks at the respective tangent altitudes. The peaks fall moderately fast above the tangent altitude, and very quickly below. This sharpness and very distinct nature of the weighting kernel functions $K(r)$ for different propagation paths allows well determined inversions to profiles of local quantities, produced exclusively from direct data, provided a wide sample of propagation paths is available.

On the contrary, since the integral in Equation (3) does not include a tangent point, reflected paths are qualitatively different:

30 they are dependent on the entire atmosphere, and do not show sharp peaks. Although slightly different, the kernels $K(r)$ in the equations for reflected paths are all very similar. An example comparing the sharp peaks of direct paths, and the smooth dependency of reflected data, is shown in Figure 11. The reflected kernels always include the entire atmosphere, and are always sensitive to the low troposphere. Among the direct paths, only a few are sensitive to the low troposphere, and some may be missing. The reflected kernels have therefore the ability to fill any section where direct data are not sufficiently sensitive.

Although we may expect to extract some new data, additional to the direct GPSRO, which helps our understanding of the atmospheric profile, and especially of the low atmosphere (Boniface et al., 2011), the similarity of the weighting functions of the reflected data implies that we may not expect, from exclusively reflected data, the high vertical resolution that is possible with direct-only data. This more limited ability to provide vertical resolution also occurs with mountain or airborne occultations
5   (Zuffada et al., 1999), and surface meteorological GPS observations (Bevis et al., 1992).

4.3   Value of reflected data under superrefraction

The reflected radio links, like the direct ones, also suffer atmospheric bending and each link can be associated to an impact parameter, too. Therefore, as for direct paths, each reflected path (in a sufficiently symmetric atmosphere) can be associated to one value of bending angle and one value of impact parameter, and it is possible to build the reflected bending-impact
10   parameter profile $\alpha_R(a)$ of a given radio occultation.

In Section 4.2, it was concluded that the $\alpha_R(a)$ profile of reflected signals contains information of the lower tropospheric layers, and can be expressed by Equation 3. It was also concluded that it could contribute to determine the atmospheric solution close to the surface. To illustrate the content of information of these reflected bending-impact profiles, a few examples are shown in Figure 12. A family of refractivity profiles is displayed on the left panel. They are all generated from a common
15   function, a simple exponential with altitude. An additional more refractive layer is added at low altitude (lowest 2 km), similar to the structure often found in the atmospheric boundary layer (ABL), and associated to the water vapor content, normally higher in the ABL than in the free troposphere. The additional refractivity is shaped as an error function, leading to a vertical gradient that may be strong. The family shown presents conditions close to superrefraction. The right panel in Figure 12 shows the relationship between the reflected ray's bending and impact parameter of each of the profiles, as given by Equation 3. It
20   is clear that the reflected impact parameter changes distinctively with variations of the surface refractivity value. The shape of the relationship between bending and impact parameter also changes, although less distinctively. Although a profile close to superrefractivity, such as this, is known to be difficult with direct data (Xie et al., 2010), the bending angle vs impact parameter relationship of the reflected profile is clearly sensitive to the superrefractive layer, and within the precision of the retrieved profiles. Furthermore, regions such as SE Pacific, where superrefractive layers are common, therefore where standard GPSRO
25   presents a weakness resolving the structure of the low troposphere, present a particularly large fraction of reflections.

5   Conclusions

From the descriptive analysis of a large collection of over 4 million occultations, and representing approximately 9 years of COSMIC data, we conclude that

1. it is possible to automatically detect reflected signals in GPSRO events;

2. these can happen on every type of Earth surface. Globally, about half of the occultations present a reflection signature. They are more frequent over ocean, ice, and smooth land areas, with up to 70% occurrence in medium to high latitude oceans;

3. occurrence of GPSRO reflections over land presents seasonal and geographic patterns that correlate with the smoothness of the surface, and particularly when there is a snow or ice cover;

4. occurrence of GPSRO reflections over ocean presents seasonal and geographic patterns. They do not depend on the sea wave height conditions, and instead anticorrelate with the ocean temperature.

5. the atmospheric conditions more favorable for GPSRO reflections to occur, correspond to a stable and well stratified atmosphere, with low energy (vertical integral) and water vapor, irrespective of its relative humidity. The physical mechanism is probably the optical homogeneity of the low troposphere, inside the occultation region.

6. strong reflected signals in a GPSRO event correlates with direct signals that have good apriori agreement with NWP.

The reflected signals frequently present a narrow spectral distribution, sufficient to be considered coherent, to be separable from the direct signal, and interpreted in terms of impact parameter and bending angle. This indicates that a large pool of bending angle data exists, which is not being used operationally, and that is additional to the standard GPSRO profiles. This pool of data is sensitive to both the refractivity of the atmosphere, and the height of the surface. If by geographic selection we limit to ocean events (known height), the reflection signature will then depend only on the atmospheric refractivity. This bending data can be simulated with an extension of standard bending angle observation operators, and is therefore usable in the context of NWP. The dependence weight of these data is concentrated in the low troposphere, but does not have the characteristic weight peak of direct data. Although the reflected section of the profile contains less independent information than the direct section, it contains a few unique capabilities. It can resolve voids in the direct profile, for instance in the event of loss of track. It provides sensitivity to the interior of superrefraction layers, and offers access to observationally estimate the atmospheric refractivity at the surface.

The interpretation of those data is facilitated when the GPSRO reflection takes place at a known altitude, and particularly the sea surface. On the other hand, further work will be required to allow the interpretation of cases where the reflection is perceptible, but the height of the reflecting layer is not known apriori. This includes land events, and notably the numerous cases over ice in the polar regions. It is also the case when the GPSRO reflection takes place on some elevated refractivity gradient, instead of the surface.

Data availability. The ensemble of occultations processed, with their attributed SVM flags, is available freely from www.romsaf.org as an experimental product (registration required).

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References

Anthes, R. A., Rocken, C., and Kuo, Y. H.: Applications of COSMIC to Meteorology and Climate, Terr. Atmos. Ocean. Sci., 11, 115–156, 2000.

Aparicio, J. M. and Deblonde, G.: Impact of the Assimilation of CHAMP Refractivity Profiles on Environment Canada Global Forecasts, Mon. Weather Rev., 133, 257–275, doi:10.1175/2007MWR1951.1, 2008.

Bevis, M., Businger, S., Herring, T. A., Rocken, C., Anthes, R. A., and Ware, R. H.: GPS meteorology: Remote sensing of atmospheric water vapor using the global positioning system, Journal of Geophysical Research: Atmospheres, 97, 15 787–15 801, doi:10.1029/92JD01517, 1992.

Beyerle, G. and Hocke, K.: Observation and simulation of direct and reflected GPS signals in Radio Occultation Experiments, Geophys. Res. Lett., 28, 1895–1898, doi:10.1029/2000GL012530, 2001.

Beyerle, G., Hocke, K., Wickert, J., Schmidt, T., Marcquardt, C., and Reigber, C.: GPS radio occultations with CHAMP: A radio holographic analysis of GPS signal propagation in the troposphere and surface reflections, J. Geophys. Res.-Atmos., 107, 4802, doi:10.1029/2001JD001402, 2002.

Boniface, K., Aparicio, J. M., and Cardellach, E.: Meteorological information in GPS-RO reflected signals, Atmospheric Measurement Techniques, 4, 1397–1407, doi:10.5194/amt-4-1397-2011, 2011.

Cardellach, E. and Oliveras, S.: Assessment of a potential reflection flag product, Tech. Rep. 23, EUMETSAT ROM SAF, www.romsaf.org, 2016.

Cardellach, E., Ao, C. O., de la Torre Juárez, M., and Hajj, G. A.: Carrier phase delay altimetry with GPS-reflection/occultation interferometry from low Earth orbiters, Geophys. Res. Lett., 31, L10 402, doi:10.1029/2004GL019775, 2004.

Cardellach, E., Oliveras, S., and Rius, A.: Applications of the reflected signals found in GNSS radio occultation events, in: GRAS SAF Workshop on Applications of GPSRO measurements, pp. 133–144, European Centre for Medium Range Weather Forecast, Reading, UK, 2008.

Cardellach, E., Oliveras, S., and Rius, A.: GNSS Signal Interference Classified by Means of a Supervised Learning Method Applied in the Time-Frequency Domain, in: Proceedings of 2nd International Congress on Image and Signal Processing, 2009. CISP '09, pp. 1–5, IEEE, Tianjin, China, doi:10.1109/CISP.2009.5302135, 2009.

Charron, M., Polavarapu, S., Buehner, M., Vaillancourt, P. A., Charette, C., Roch, M., Morneau, J., Garand, L., Aparicio, J. M., MacPherson, S., Pellerin, S., St-James, J., and Heilliette, S.: The stratospheric extension of the Canadian operational deterministic medium range weather forecasting system and its impact on tropospheric forecasts, Mon. Weather Rev., 140, 1924–1944, doi:10.1175/MWR-D-11-00097.1, 2012.

Cucurull, L., Derber, J. C., Treadon, R., and Purser, R. J.: Assimilation of Global Positioning System Radio Occultation Observations into NCEP's Global Data Assimilation System, Mon. Weather Rev., 135, 3174–3193, doi:10.1175/MWR3461.1, 2007.

Guo, P., Kuo, Y.-H., Sokolovskiy, S. V., and Lenschow, D. H.: Estimating Atmospheric Boundary Layer Depth Using COSMIC Radio Occultation Data, Journal of the Atmospheric Sciences, 68, 1703–1713, doi:10.1175/2011JAS3612.1, 2011.

Healy, S. B.: The use of the GPS radio occultation reflection flag for NWP applications, Tech. Rep. 22, EUMETSAT ROM SAF, www.romsaf.org, 2015.

Healy, S. B. and Thépaut, J. N.: Assimilation experiments with CHAMP GPS radio occultation measurements, Quart. J. Roy. Meteorol. Soc., 132, 605–623, doi:10.1256/qj.04.182, 2006.

Hocke, K., Pavelyev, A. G., Yakovlev, O. I., Barthes, L., and Jakowski, N.: Radio occultation data analysis by the radioholographic method, J. Atmos. Solar-Terr. Phys., 61, 1169–1177, doi:10.1016/S1364-6826(99)00080-2, 1999.

Joachims, T.: Learning to Classify Text Using Support Vector Machines, Methods, Theory and Algorithms, vol. 668, The Springer International Series in Engineering and Computer Science, 2002.

5   Kursinski, E. R., Hajj, G. A., Schofield, J. T., Linfield, R. P., and Hardy, K. R.: Observing Earth's atmosphere with radio occultation measurements using the Global Positioning System, J. Geophys. Res.-Atmos., 102, 23 429–23 465, doi:10.1029/97JD01569, 1997.

NIMA: Department of Defense World Geodetic System 1984, Its Definition and Relationships With Local Geodetic Systems, Tech. Rep. TR8350.2, National Imagery and Mapping Agency, 2000.

Parkinson, B. W. and Spilker, J. J.: Global Positioning System: Theory and Applications, Volume I, American Institute of Aeronautics and

10   Astronautics, Washington, DC, 1996.

Pavelyev, A. G., Zhang, K., Matyugov, S. S., Liou, Y. A., Wang, C. S., Yakovlev, O. I., Kucherjavenkov, I. A., and Kuleshov, Y.: Analytical model of bistatic reflections and radio occultation signals, Radio Sci., 46, RS1009, doi:10.1029/2010RS004434, 2011.

Piepmeier, J. R., Focardi, P., Horgan, K. A., Knuble, J., Ehsan, N., Lucey, J., Brambora, C., Brown, P. R., Hoffman, P. J., French, R. T., Mikhaylov, R. L., Kwack, E. Y., Slimko, E. M., Dawson, D. E., Hudson, D., Peng, J., Mohammed, P. N., Amici, G. D., Freedman, A. P.,

15   Medeiros, J., Sacks, F., Estep, R., Spencer, M. W., Chen, C. W., Wheeler, K. B., Edelstein, W. N., Neill, P. E. O., and Njoku, E. G.: SMAP L-Band Microwave Radiometer: Instrument Design and First Year on Orbit, IEEE Transactions on Geoscience and Remote Sensing, 55, 1954–1966, doi:10.1109/TGRS.2016.2631978, 2017.

Rennie, M.: The assimilation of GPS radio occultation measurements at the Met Office, in: GRAS SAF Workshop on Applications of GPSRO measurements, pp. 84–94, ECMWF, Reading, UK, 2008.

20   Ruf, C., Unwin, M., Dickinson, J., Rose, R., Rose, D., Vincent, M., and Lyons, A.: CYGNSS: Enabling the Future of Hurricane Prediction Remote Sensing Satellites, IEEE Geoscience and Remote Sensing Magazine, 1, 52–67, doi:10.1109/MGRS.2013.2260911, 2013.

Ulaby, F. T., Moore, R. K., and Fung, A. K.: Microwave Remote Sensing, Active and Passive, Vol.III, Arctech House, Inc., Norwood, MA., U.S.A., 1986.

Unwin, M., Jales, P., Tye, J., Gommenginger, C., Foti, G., and Rosello, J.: Spaceborne GNSS-Reflectometry on TechDemoSat-1: Early

25   Mission Operations and Exploitation, IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing, 9, 4525–4539, doi:10.1109/JSTARS.2016.2603846, 2016.

von Engeln, A. and Teixeira, J.: "A ducting climatology derived from the European Centre for Medium-Range Weather Forecasts global analysis fields", J. Geophys. Res.-Atmos., 109, doi:10.1029/2003JD004380, d18104, 2004.

Wickert, J., Cardellach, E., Martín-Neira, M., Bandeiras, J., Bertino, L., Andersen, O. B., Camps, A., Catarino, N., Chapron, B., Fabra,

30   F., Floury, N., Foti, G., Gommenginger, C., Hatton, J., Hoeg, P., Jäggi, A., Kern, M., Lee, T., Li, Z., Park, H., Pierdicca, N., Ressler, G., Rius, A., Roselló, J., Saynisch, J., Soulat, F., Shum, C. K., Semmling, M., Sousa, A., Xie, J., and Zuffada, C.: GEROS-ISS: GNSS Reflectometry, Radio Occultation, and Scatterometry Onboard the International Space Station, IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing, 9, 4552–4581, doi:10.1109/JSTARS.2016.2614428, 2016.

Xie, F., Wu, D. L., Ao, C. O., Kursinski, E. R., Mannucci, A. J., and Syndergaard, S.: Super-refraction effects on GPS radio occultation

35   refractivity in marine boundary layers, Geophys. Res. Lett., 37, doi:10.1029/2010GL043299, l11805, 2010.

Zeng, Z., Sokolovskiy, S., Schreiner, W., Hunt, D., Lin, J., and Kuo, Y. H.: Ionospheric correction of GPS radio occultation data in the troposphere, Atmospheric Measurement Techniques, 9, 335–346, doi:10.5194/amt-9-335-2016, 2016.

Zuffada, C., Hajj, G. A., and Kursinski, E. R.: A novel approach to atmospheric profiling with a mountain-based or airborne GPS receiver, Journal of Geophysical Research: Atmospheres, 104, 24 435–24 447, doi:10.1029/1999JD900766, 1999.

Table 1. Comparison between dedicated GNSS reflectometry missions, and reflected signals during GPSRO radio occultation events. Example past or planned missions are shown, with one or the other technology. Launch years are included. This paper is solely adressed to reflections during GPSRO.

	Dedicated GNSS-R	**Reflections in GPSRO**
Geometry:	near nadir ($\sim 45° - 90°$ elevation)	grazing angles, nearly tangential ($\sim 1°$ elevation)
Scattering:	mostly diffuse	only coherent component acquired
Existing, past, or planned:	TDS-1 (2014), CYGNSS (2016), GEROS-ISS	e.g. CHAMP (2000), COSMIC (2006), METOP (2006), etc
Peer-reviewed bibliography:	100+ articles	<10

Table 2. Percentage of reflected signals within different latitudinal belts, and reflecting surfaces. Reflection is here defined as SVM value >
0.25.

Latitudes [deg]	ALL	OCEAN	LAND
$\|lat\| \leq 20$	18	22	6
$20 < \|lat\| \leq 50$	35	45	10
$50 < \|lat\| \leq 70$	50	69	13
$70 < \|lat\| \leq 90$	60	68	52

Table 3. Cross-correlation between the percentage of reflected signals in COSMIC ocean events, and other atmospheric variables. Correlations are based on monthly averaged values over $10° \times 10°$ ocean cells (see an example in Figure 8), except the optical heterogeneity, which is a correlation of individual events. All the variables are obtained from ECMWF ERA Interim analysis, except those obtained from the occultation profiles (first two rows), and the heterogeneity, from Environment Canada's global forecasts (last row). ERA Interim variables that depend on height have been averaged over the lowest 10 km. Γ is the temperature lapse rate, and Γ_s is the Saturated Adiabatic Lapse Rate.

Variable:	Cross-correlation
Min. gradient of refractivity	0.63
Max. bending angle	-0.58
Sea surface temperature	-0.80
Column of water vapor	-0.78
Vertical integral of total energy	-0.77
Atmospheric temperature	-0.75
Water vapor pressure	-0.69
Sea wave height	0.04
Relative Humidity	0.26
Wind at the surface	0.43
$\Gamma - \Gamma_s$ (defined positive)	0.64
Optical Heterogeneity	-0.64
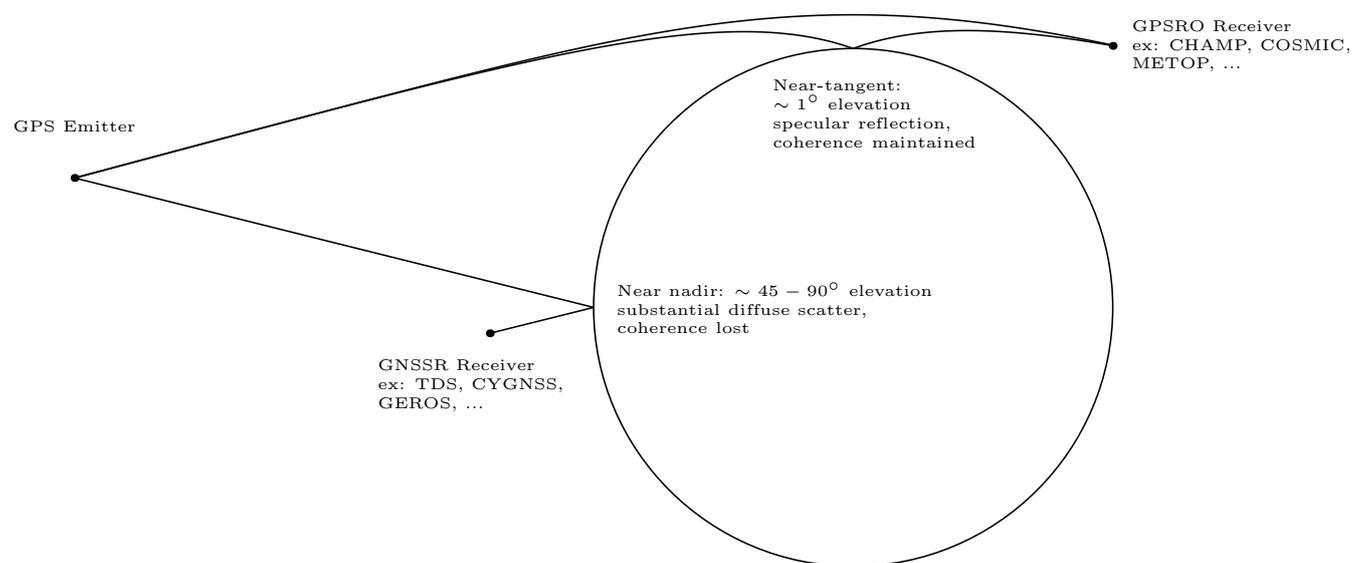
Figure 1. Diagram showing the concept of atmospheric occultation, together with the grazing reflection during the occultation, which is the focus of this study (upper part of the diagram). For comparison, the concept of GNSS reflections (GNSSR) at higher elevation is shown on the left. At very low elevation, the coherence of the emitted signal is often not lost, even if the signal bounces off a surface that is not perfectly smooth (for instance ocean waves, see main text). During a reflection at high elevation, which is the concept behind several recent missions (TDS, CYGNSS, GEROS,...), normal ocean waves destroy coherence.
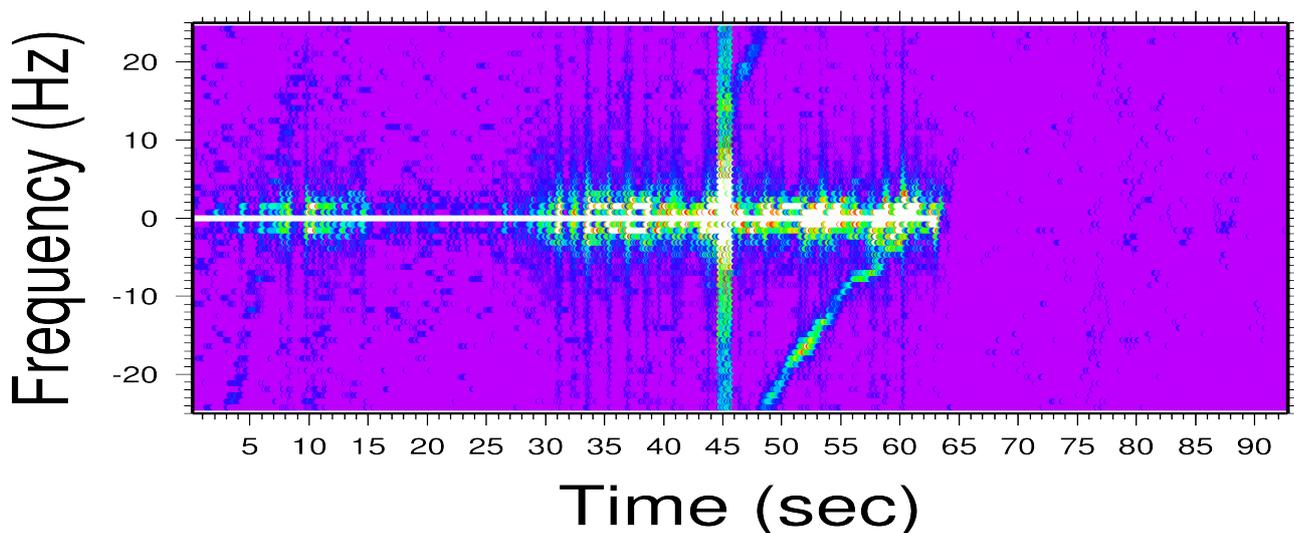
Figure 2. Example radiohologram of descending COSMIC occultation C001.2011.219.10.43.G15, which presents a reflection. The main signal has been nearly stopped by beating it against a filtered reference. Both components have a narrow spectral width, but the supplementary tone also shows aliasing and winding (at 46-48 s, +20 Hz). Both tones finally merge. This final section, where the low troposphere is being scanned, shows spectral broadening in both the direct and reflected signals.
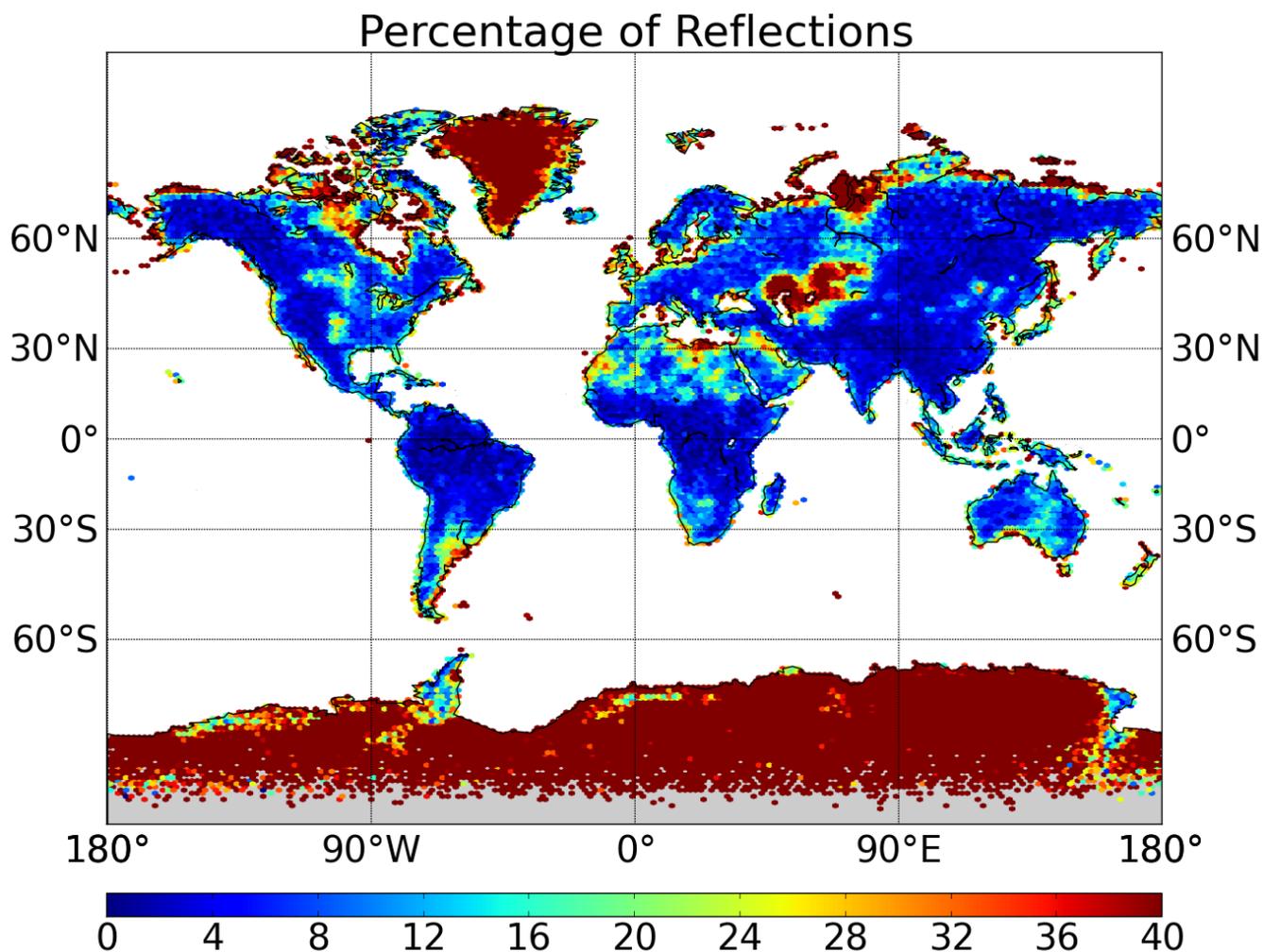
Figure 3. Map of percentage of GPSRO reflections over land. The map was compiled with ∼1,320,000 land events. Reflection events, here identified as those presenting SVM>0.25, mostly occur over smooth terrain, free of thick vegetation (deserts, tundra, grasslands), and over continental ice. The largest percentages are found over the ice sheets. The color scale is saturated at 40%.
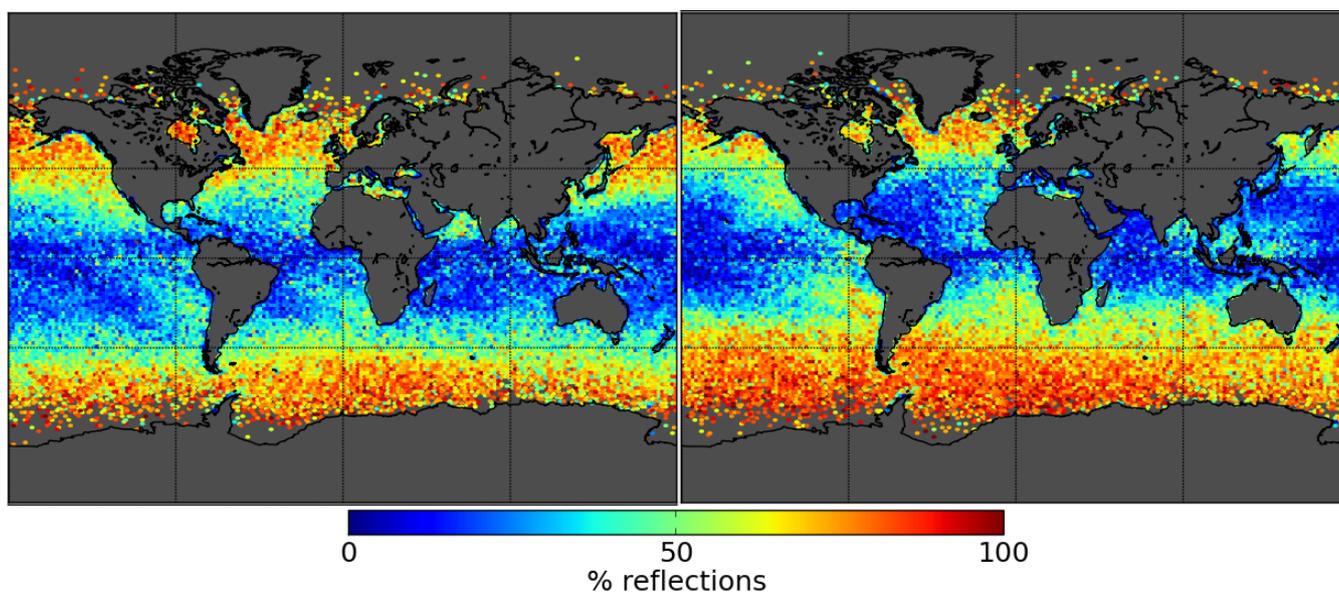
Figure 4. Statistics of GPSRO reflections over the ocean, obtained with the COSMIC constellation from 2006 to 2015. Percentage reflections on a gridded ocean during January and February (left), and during July and August (right). Note that the color scale is different from Figure 3. See also Supplementary Movie 2, which shows the seasonal cycle of the median SVM over ocean.
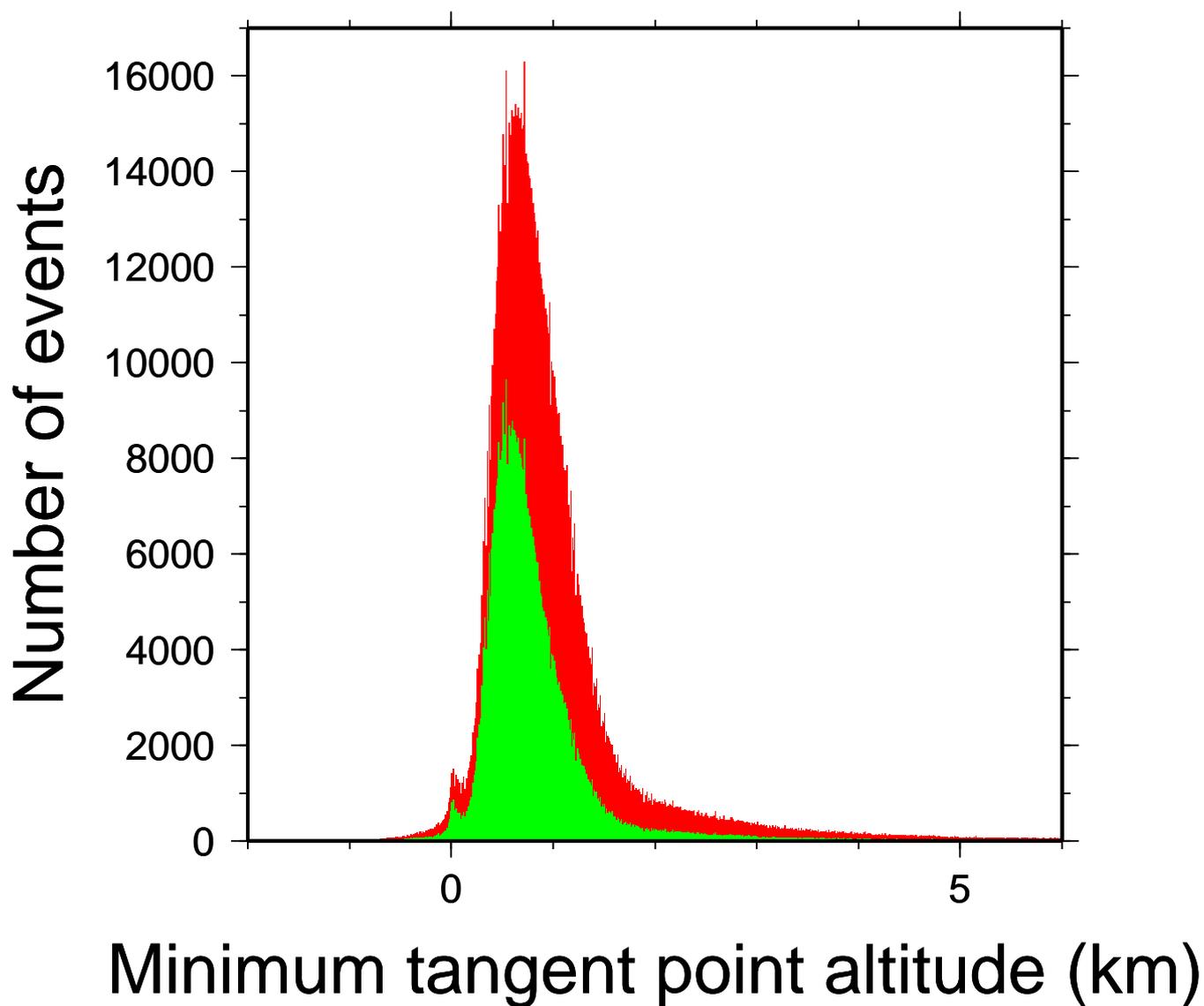
Figure 5. Histogram of lowest altitude profiled in ocean events that have been flagged as likely reflection (SVM>0.25, in red) and very likely reflection (SVM>1, in green).
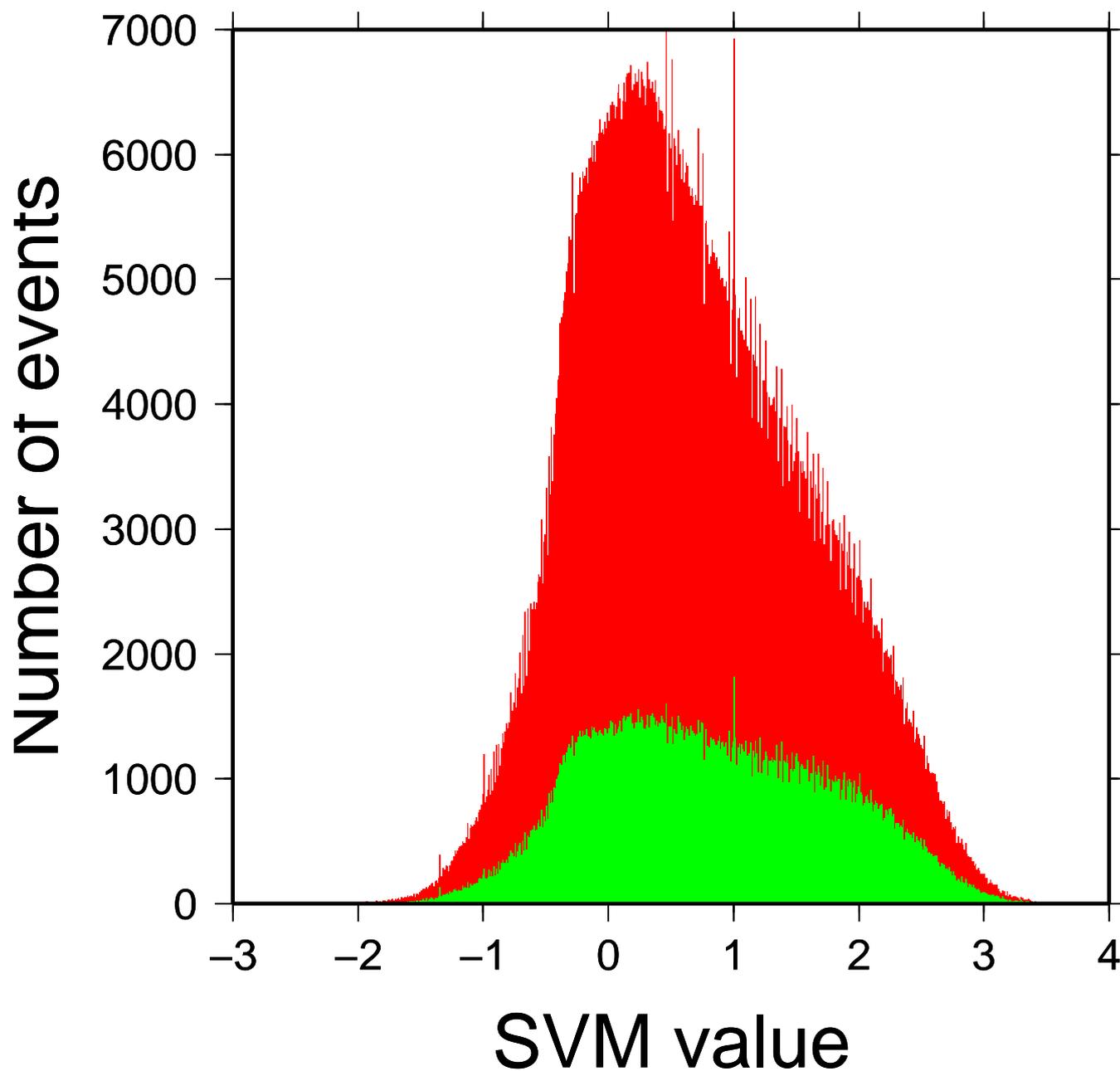
Figure 6. Histogram of SVM values for ocean events that reach the lowest kilometer of the troposphere ($H_{min} < 1km$, in red) and the lowest 500 meters ($H_{min} < 0.5km$, in green).
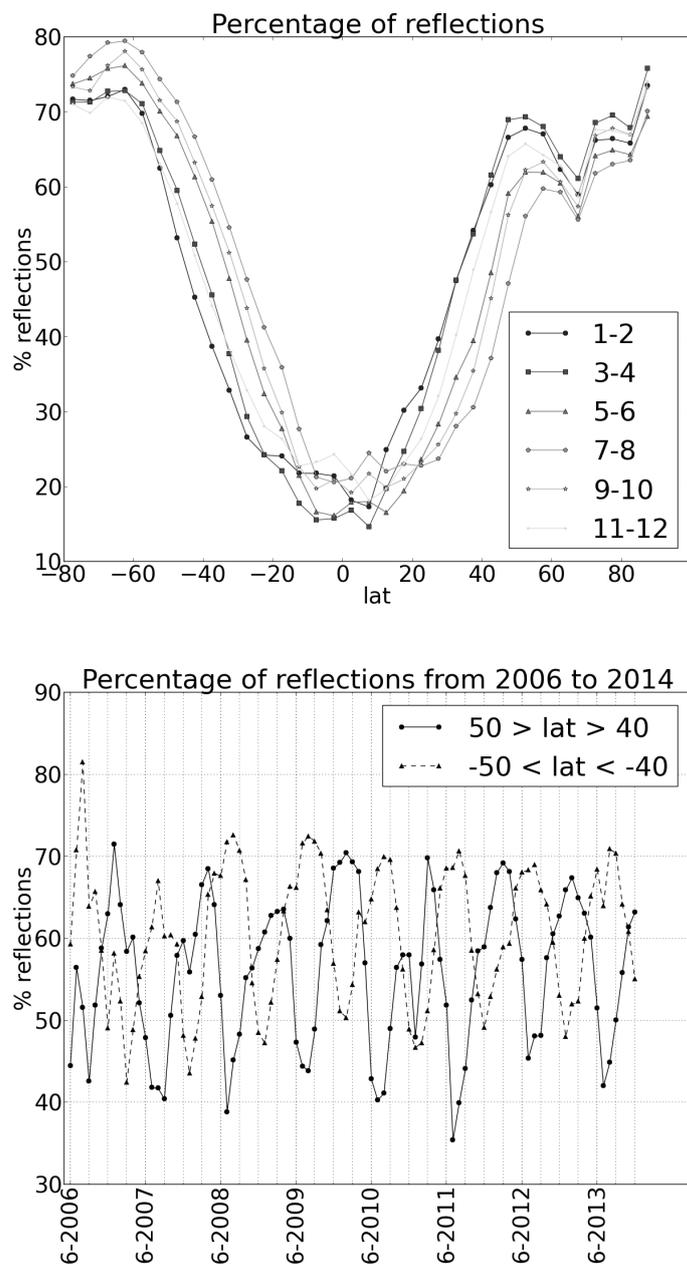
Figure 7. Statistics of reflection occurrence in events over ocean, obtained with the COSMIC constellation from 2006 to 2014. Top: percentage reflections as a function of the latitude, binned by bands of $5°$, over all 6 bi-monthly groups in the year. Bottom: monthly time series of percentage reflections in the northern and southern midlatitude belts, between $40°$ and $50°$.
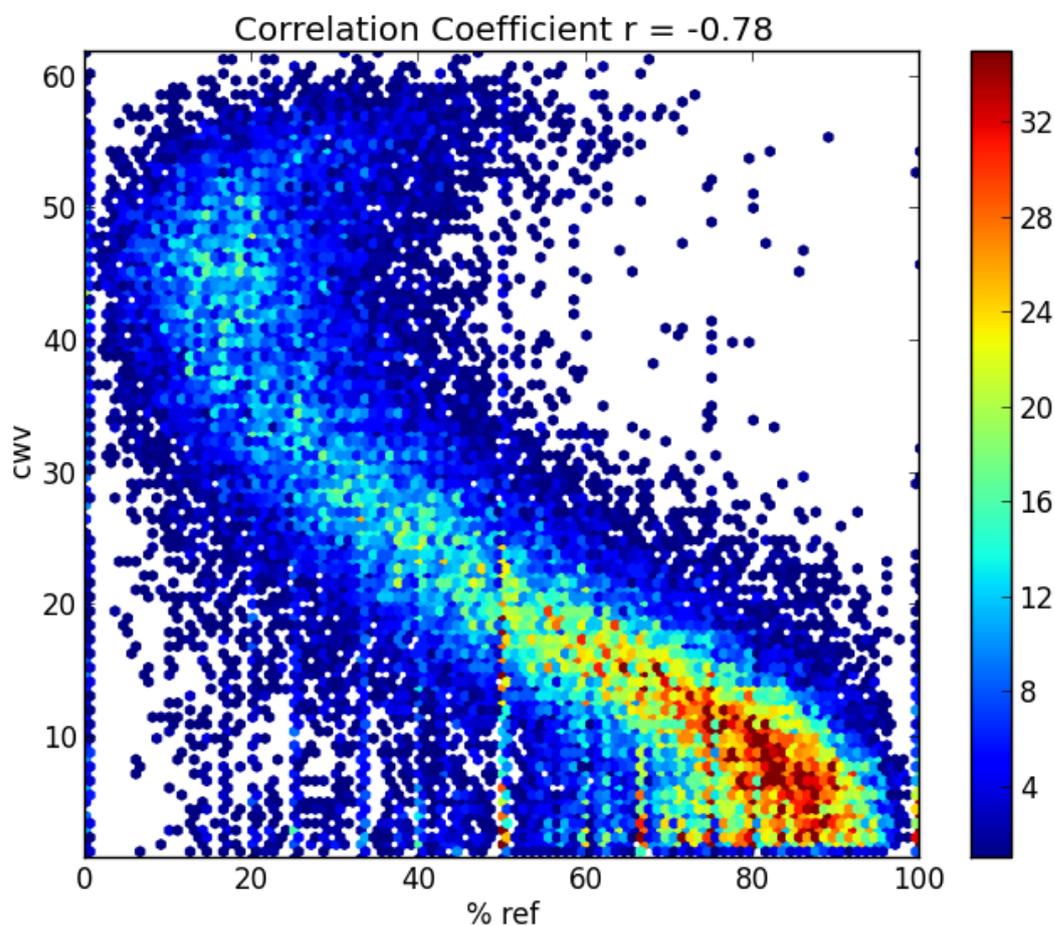
Figure 8. Two-dimensional histogram of occurrence of reflections, computed monthly on $10° \times 10°$ ocean cells, against the column of water vapor averaged over the same cell and month. ECMWF ERA Interim data have been used to estimate the values of the Column of Water Vapor (CWV). The color scale represents the number of (cell x month) counts, and it has been saturated to 35 for clarity. The resulting cross-correlation coefficient between reflection and CWV is $r = -0.78$.
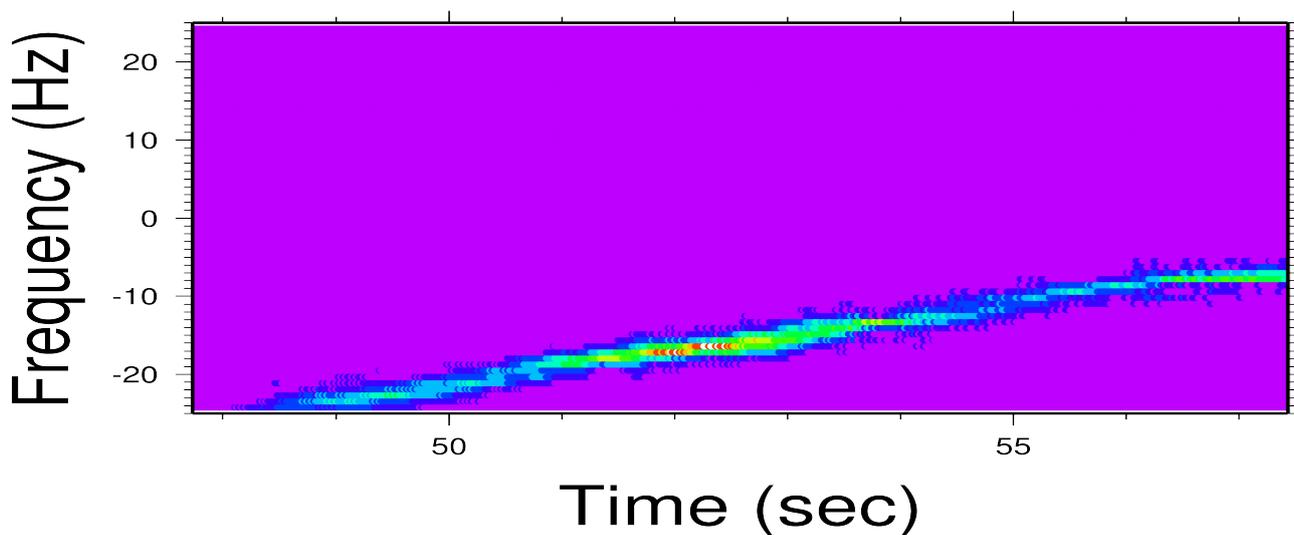
Figure 9. The location in time of the reflected signal is determined cross-correlating the radio-hologram and a template image. Once the time interval is identified, only this interval of the radio-hologram is analyzed, and the frequency components above -5 Hz are set to noise level. After inverse Fourier Transform of the filtered hologram a phase lock loop (PLL) can track the signal identified as the reflection, obtaining $f_R(t)$.
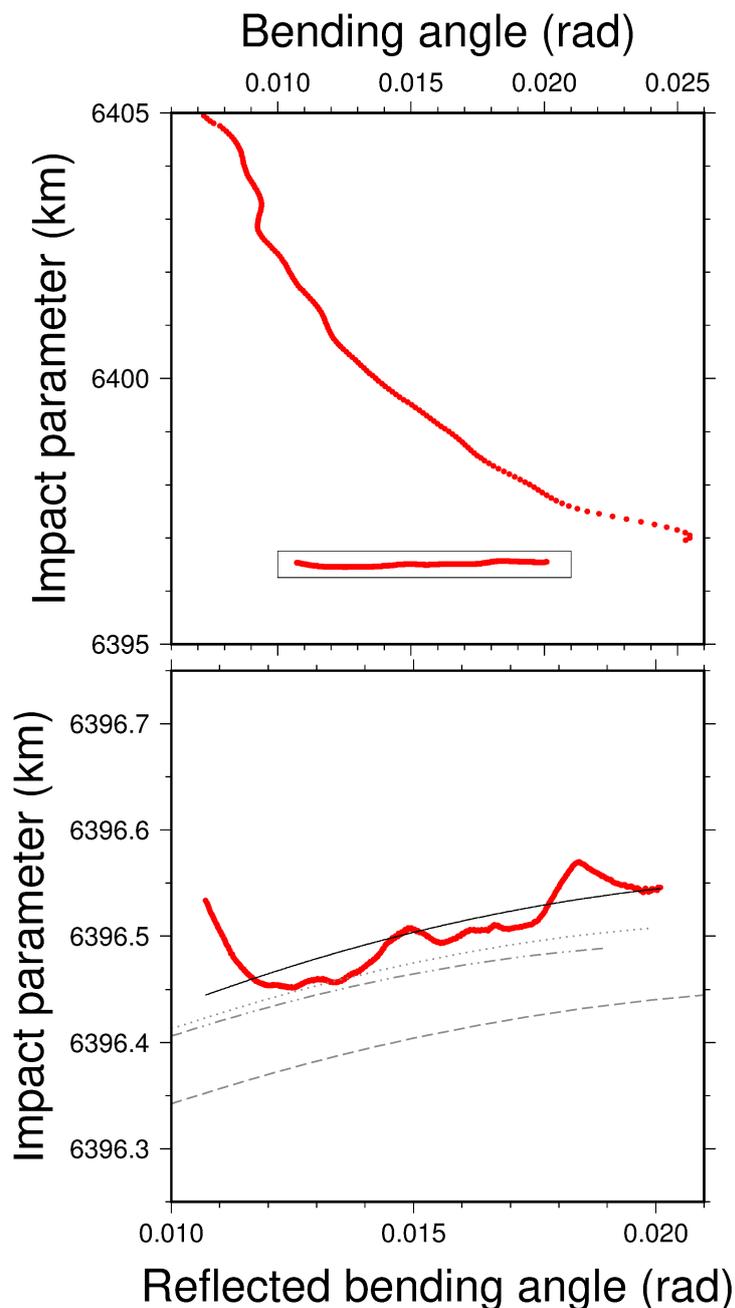
Figure 10. In the upper panel, profile of extracted bending and impact parameter, including the standard direct branch, as well as the reflected, from the same occultation in Figure 2. The box around the reflected branch is zoomed in the lower panel. The reflection was extracted as detailed in Section 4 (thick red). A parabolic fit to it is shown in solid black. The COSMIC Data Analysis and Archival Center (CDAAC) also offers profiles of refractivity $N(h)$, which allow the evaluation of the expected α_R and a using Equation (3). These are shown in grey, using refractivity obtained from the direct data (atmPrf file, dashed-dotted), from a background NWP (ecmPrf file, dashed), and from a 1DVar estimation (wetPrf file, dotted).
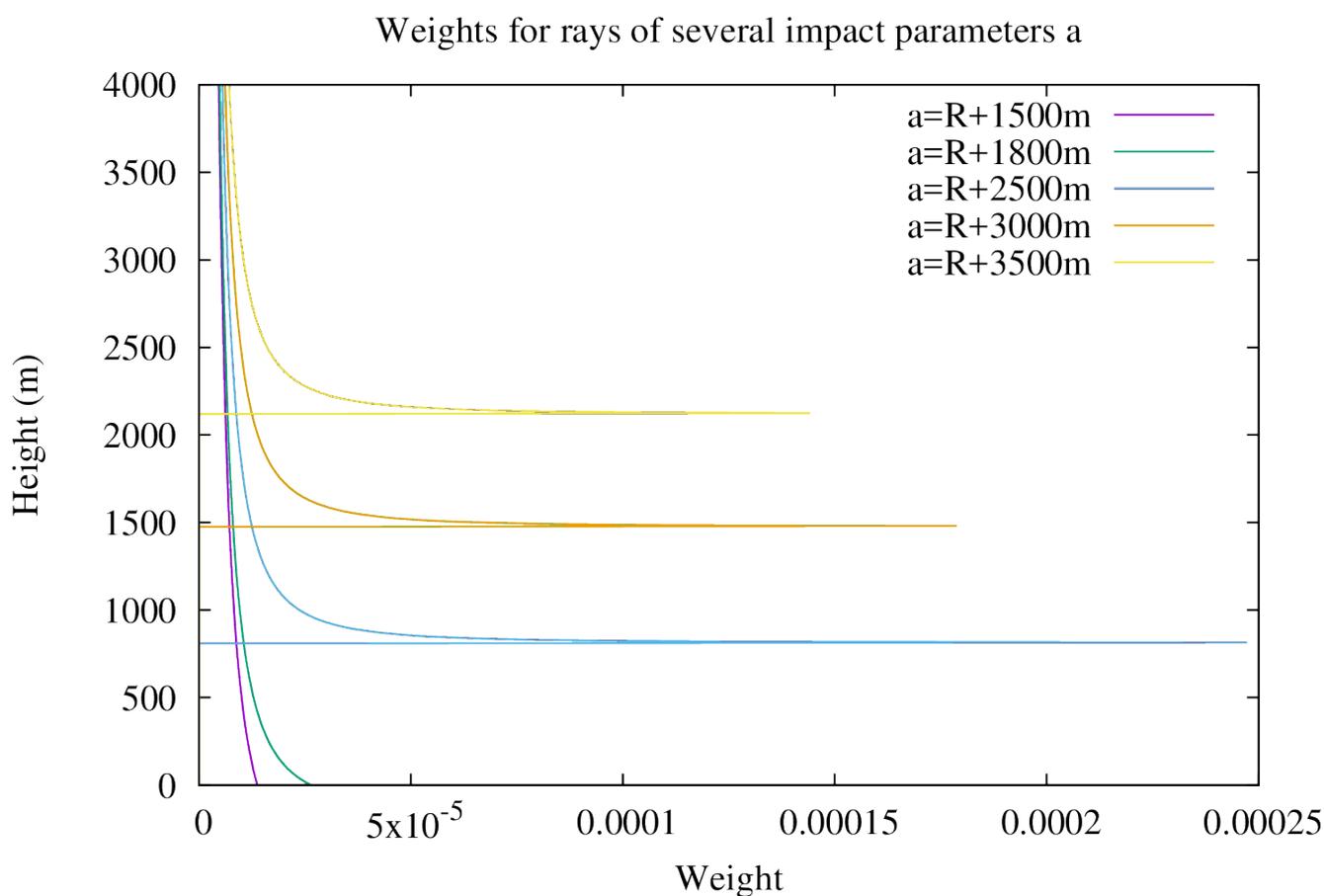
Figure 11. Kernel weight dependency of several paths, with respect to the local refractivity properties of the profile. Three direct paths are shown, those with larger impact parameter ($a = R+2500m, R+3000m, R+3500m$). They all present a sharp peak, providing information that is very independent from each other. Two reflected paths are shown, those with smaller impact parameter ($a = R+1500m, R+1800m$), which do not show any peak. They provide information that is different between them, but much less independent. With the refractivity profile used, the apparent horizon was approximately located at $a_S = R+1900m$.
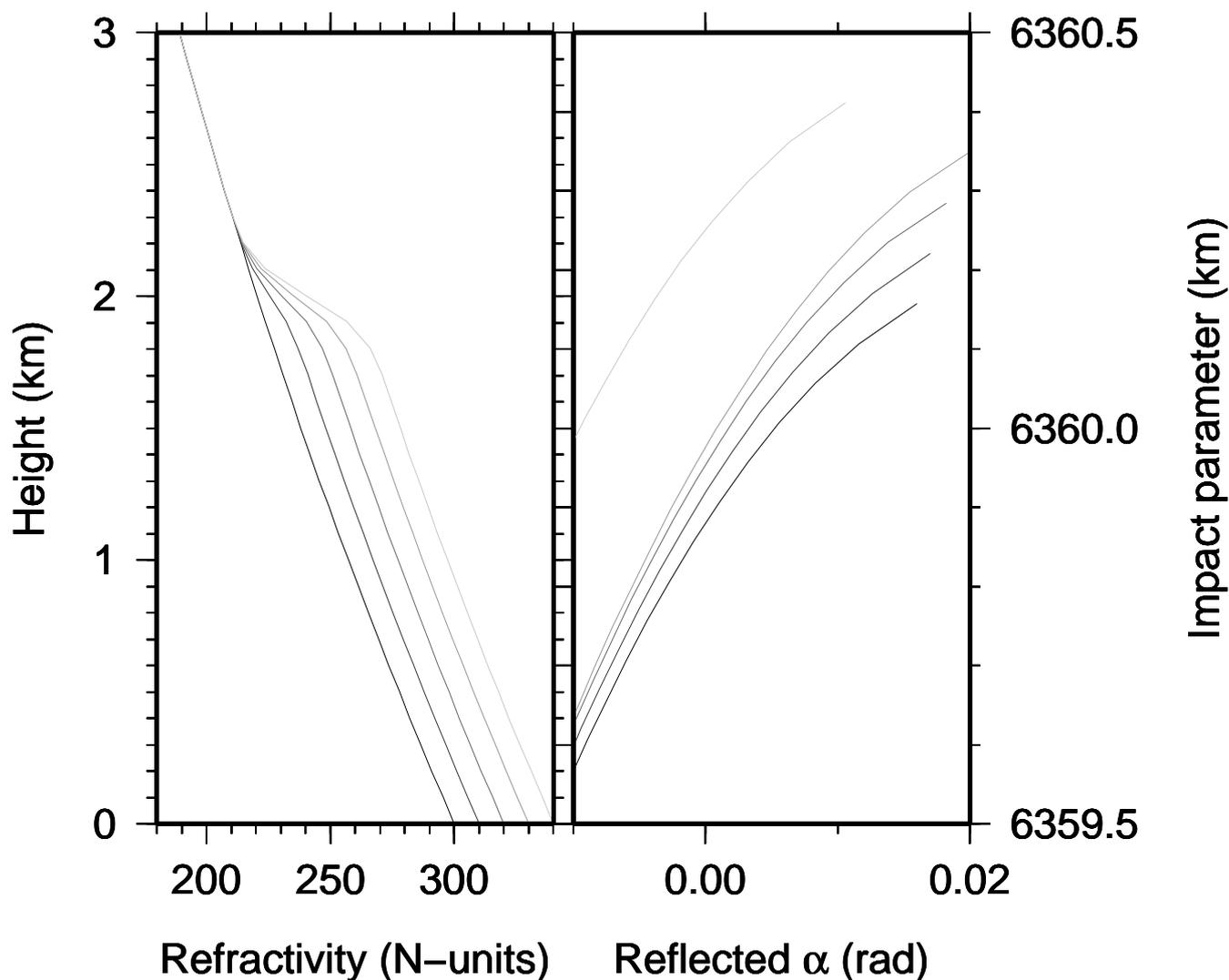
Figure 12. The left panel shows a family of atmospheric refractivity profiles, generated as an exponential function, intended to represent a smooth profile, with a more refractive lower layer, modeled as an error-function. The transition to this extra refraction is sharp, which is common in superrefractive layers. The righ panel shows the corresponding series of reflected bending and impact parameters, as evaluated by Equation (3), and indicates that the profile of reflected bending is sensitive to the amplitude of the extra layer.