

Aerosol particle size distribution in the stratosphere retrieved from SCIAMACHY limb measurements

Elizaveta Malinina¹, Alexei Rozanov¹, Vladimir Rozanov¹, Patricia Liebing^{1*}, Heinrich Bovensmann¹, and John P. Burrows¹

¹Institute of Environmental Physics (IUP), University of Bremen, Bremen, Germany

* now at Leiden Observatory, University of Leiden, Leiden, the Netherlands

Correspondence to: Elizaveta Malinina (malininaep@iup.physik.uni-bremen.de)

Abstract. Information about aerosols in the Earth's atmosphere is of a great importance in the scientific community. While tropospheric aerosol influences the radiative balance of the troposphere and affects human health, stratospheric aerosol plays an important role in atmospheric chemistry and climate change. In particular, information about the amount and distribution of stratospheric aerosols is required to initialize climate models, as well as validate aerosol microphysics models and investigate

5 geoeengineering. In addition, good knowledge of stratospheric aerosol loading is needed to increase the retrieval accuracy of key trace gases (e.g. ozone or water vapor), when interpreting remote sensing measurements of the scattered solar light. The most commonly used characteristics to describe stratospheric aerosols are the aerosol extinction coefficient and Ångström coefficient. However, the use of particle size distribution parameters along with the aerosol number density is a more optimal approach. In this manuscript we present a new retrieval algorithm to obtain the particle size distribution of stratospheric aerosol

10 from space borne observations of the scattered solar light in the limb viewing geometry. While the mode radius and width of the aerosol particle size distribution are retrieved, the aerosol particle number density profile remains unchanged. The latter is justified by a lower sensitivity of the limb-scattering measurements to changes in this parameter. To our knowledge this is the first data set providing two parameters of the particle size distribution of stratospheric aerosol from space borne measurements of scattered solar light. Typically, the mode radius and absolute distribution width can be retrieved with an

15 uncertainty of less than 20%. The algorithm was successfully applied to the tropical region (20°N-20°S) for 10 years (2002-2012) of SCIAMACHY observations in limb viewing geometry, establishing a unique data set. Analysis of this new climatology for the particle size distribution parameters showed clear increases of the mode radius after the tropical volcanic eruptions, whereas no distinct behaviour of the absolute distribution width could be identified. A tape recorder, which describes the time lag as the perturbation propagates to higher altitudes, was identified for both parameters after the volcanic eruptions. A Quasi

20 Biannual Oscillation (QBO) pattern at upper altitudes (28-32 km) is prominent in the anomalies of the analyzed parameters. A comparison of the aerosol effective radii derived from SCIAMACHY and SAGE II data was performed. The average difference is found to be around 30% at the lower altitudes decreasing with increasing height to almost zero around 30 km. The data sample available for the comparison is, however, relatively small.

1 Introduction

Stratospheric aerosols are of a great interest for researchers because of their impact on the climate. The radiative budget of the Earth is altered by stratospheric aerosol, which scatters electromagnetic radiation in the atmosphere. Large amount of aerosol emitted by volcanic eruptions significantly changes the radiative forcing affecting global temperatures. For example, the super-colossal Tambora eruption in 1815 is claimed to cause "the year without summer" in 1816. The more recent colossal eruption of Mount Pinatubo in 1991 caused a surface temperature cooling of a few tenths of a Kelvin (Robock and Mao, 1995). According to Solomon et al. (2011), smaller volcanic eruptions also noticeably affect the global temperature. Another important role of aerosols is their ability to act as condensation nuclei for polar stratospheric clouds (PSC) which provide surface for heterogeneous chlorine activation and denitrification processes, thus increasing ozone depletion (Solomon, 1999).

Accurate information about stratospheric aerosols is important for different research fields. Among others, stratospheric aerosol parameters are needed for modelling the processes related to the stratosphere, including aerosol microphysics model validation. Modellers require stratospheric aerosol climatologies as initial conditions for climate model simulations and predictions (e.g. Solomon et al., 2011; Fyfe et al., 2013). Fyfe et al. (2013) concluded that not only temperature is affected by the volcanic eruptions, but also precipitation, sea level pressure and wind speed change in response to the changing aerosol load. All the above mentioned data is needed not only for improving global climate models, but is also required for the investigation of geoengineering. In addition, accurate knowledge of the stratospheric aerosol loading is essential to improve trace gases retrievals from measurements of the scattered solar light (e.g. Rozanov et al., 2011; Arosio et al., 2017).

As summarized by Kremser et al. (2016), stratospheric aerosols are commonly described as spherical droplets composed of a mixture of sulfuric acid (H_2SO_4) and water (H_2O). They may also be comprised of meteoric dust as well as other nonsulfate material. The most important sources of stratospheric aerosols are carbonyl sulfide (OCS) and sulfur dioxide (SO_2) which are oxidized to sulfuric acid. Short lived SO_2 is mostly injected directly into the lower stratosphere by large volcanic eruptions, while OCS, the longest-lived sulfur gas, which has mostly marine origin, is transported from the troposphere into the stratosphere by convection in the tropics. Aerosol composition in the stratosphere is controlled by the Brewer-Dobson circulation, as well as by chemistry and microphysics during aerosol formation, growth and removal through sedimentation. Although some studies show increased SO_2 from fossil fuel combustion transported to the lower stratosphere via the Asian monsoon (Randel et al., 2010), stratospheric aerosol precursors have predominantly natural sources (e.g. volcanic eruptions and OCS emissions from the ocean) (Kremser et al., 2016). Biomass burning, which is mostly of anthropogenic origin, can also lead to the enhanced stratospheric aerosols by emitting SO_2 , OCS and black carbon. Multiple instruments registered the increase in the measured quantities during the Australian "Black Saturday" (e.g. Siddaway and Petelina, 2011).

One of the most commonly used characteristics to describe stratospheric aerosols is their extinction coefficient. Although it was employed in many previous studies dealing with space borne measurements in UV-visible-IR spectral range (Ovigneur et al., 2011; Taha et al., 2011; Ernst, 2013; Brinkhoff et al., 2015; Dörner, 2015; von Savigny et al., 2015; Rieger et al., 2015, 2018), the usage of this parameter is associated with several issues. First the extinction coefficient is wavelength dependent and this dependence is determined by the composition of the aerosol droplets and their particle size distribution. Second, while a

direct evaluation of the aerosol extinction can be done for occultation measurements, for limb measurements this parameter is dependent on the assumed particle size distribution parameters.

In contrast to the extinction coefficient, the retrieval presented in this manuscript characterizes not only the amount of the stratospheric aerosol but also its particle size distribution as it is widely done in in-situ measurements (Deshler et al., 2003). Most commonly, mode radius, distribution width and the particle number density are used to describe the particle size distribution of stratospheric aerosols. These parameters are, however, challenging to retrieve. Additionally, some information about the particle size distribution can be obtained from the Ångström coefficient, which is determined by the wavelength dependence of the aerosol extinction coefficient. However, the Ångström coefficient cannot be uniquely transformed into particle size distribution parameters. Generally, different combinations of the mode radius and distribution width may result in the same value of the Ångström coefficient. Furthermore, for each particular particle size distribution the resulting Ångström coefficient usually depends on the wavelength range.

Highly vertically resolved information on stratospheric aerosols is provided by in situ balloon borne and aircraft measurements, as well as by remote sensing measurements from ground-based lidars (Deshler et al., 2003). However, these measurements are quite sparse, and therefore satellite observations are commonly used to obtain knowledge about the global behaviour of stratospheric aerosols. Space borne measurements of the stratospheric aerosols started in the late 1970s with SAM (Stratospheric Aerosol Measurement), SAM II, SAGE (Stratospheric Aerosol and Gas Experiment) and SAGE II instruments (Yue et al., 1989). The latter was one of the most distinguished instruments of this era; it operated from 1984 till 2005 and used solar occultation technique. The current v7.0 SAGE II product provides the aerosol extinction at four wavelengths, and some information on particle size distribution parameters (more detailed in Sec. 5). In the beginning of 2000s several space borne instruments of a newer generation using stellar occultation and limb measurement techniques were launched. SCIAMACHY (Scanning Imaging Absorption Spectrometer for Atmospheric CHartographY) was one of these instruments operated on the Envisat satellite from 2002 till 2012. SCIAMACHY had three main measurement modes: nadir, solar/lunar occultation and limb scattering. Other instruments on board Envisat providing stratospheric aerosol information were Global Ozone Monitoring by Occultation of Stars (GOMOS) and the Michelson Interferometer for Passive Atmospheric Sounding (MIPAS). GOMOS made measurements using the stellar occultation technique and provides aerosol extinction coefficient (Vanhellemont et al., 2016), while the MIPAS instrument measured limb emission spectra (Fischer et al., 2008) and provides vertical profiles of SO₂ and sulfate aerosol (H₂SO₄) volume densities (Günther et al., 2017). OSIRIS (Optical Spectrograph and InfraRed Imager System), on board the Odin satellite, which was launched in 2001 and is still operating, measures scattered solar light in the limb viewing geometry (Llewellyn et al., 2004). Using this data aerosol extinction profiles and Ångström coefficient are retrieved (Bourassa et al., 2012; Rieger et al., 2014). The most recent instrument, which combines nadir and limb scattering measurements, is the Ozone Mapping Profiler Suite (OMPS) (Jaross et al., 2014). OMPS was launched by NASA in the end of 2011 and is still in operation. First results with respect to the retrievals of aerosol extinction coefficient from OMPS-LP (Limb Profiler) are presented in several publications (Taha et al., 2011; Arosio et al., 2017; Loughman et al., 2017). As well, it is important to mention the space-based lidar CALIOP (Cloud-Aerosol Lidar with Orthogonal Polarization Lidar) that provides measurements of aerosol backscatter coefficient, which is afterwards converted to the aerosol extinction coefficient. Profiles

of the aerosol extinction from CALIOP have the highest vertical resolution among the space borne instruments (Vernier et al., 2011).

This manuscript has the following structure: in Sec. 2 the most essential information about the SCIAMACHY instrument and the retrieval method used in the study is presented. In Sec. 3 the sensitivity of the retrieval algorithm is investigated. 5 Results of the SCIAMACHY data retrieval along with the discussion are presented in Sec. 4. In Sec. 5 retrieval results from SCIAMACHY are compared to the SAGE II particle size distribution product. Conclusions are given in Sec. 6.

2 Instrument and applied algorithm

2.1 SCIAMACHY on Envisat

SCIAMACHY was a joint German, Dutch and Belgian contribution to Envisat (European Environmental Satellite) launched 10 by ESA on 1 March 2002 into a sun-synchronous orbit at 800 km altitude with a 10:00 a.m. descending node equator-crossing time. SCIAMACHY provided data from August 2002 till April 2012, when the connection with the satellite was suddenly lost. The instrument operated in three observational modes: nadir, limb and solar/lunar occultation. Measurements of the solar irradiance were provided on daily basis. SCIAMACHY took measurements in 8 spectral channels, which covered the spectral interval between 214 and 2386 nm. Spectral resolution varied from 0.2 to 1.5 nm depending on the wavelength.

15 In this study, measurements taken in the limb viewing geometry were used. In this geometry the instrument observed the atmosphere tangentially to the Earth's surface in the altitude range from about 3 km below the surface, i.e., when Earth's surface is still within the field of view of the instrument, and then scanning vertically up to about 100 km. The measurements were performed with a vertical instantaneous geometrical field of view at the tangent point of 2.6 km and vertical sampling of 3.3 km. The horizontal cross-track field of view was 110 km. A horizontal scan with the total swath of about 960 km was 20 performed during each observation sequence. The horizontal cross-track resolution was mainly determined by the integration time during the horizontal scan, usually reaching about 240 km. For a typical limb measurement, the observed signal integrated by the instrument was read out four times per horizontal scan that resulted in four independent limb radiance profiles obtained during a horizontal scan. The horizontal along-track resolution is estimated to be about 400 km. Further information about the instrument can be found in Burrows et al. (1995); Bovensmann et al. (1999); Gottwald and Bovensmann (2011).

25 The retrievals performed for this study were done using version 8 of the SCIAMACHY Level 1 data with calibration flags 1, 2, 4, 5 and 7, i.e. the leakage current, pixel-to-pixel gain, straylight correction, wavelength calibration and radiometric calibration, respectively. Level 1 data was provided by the European Space Agency (ESA).

2.2 Aerosol parametrization

A balance of the processes creating and removing the stratospheric aerosols as well as of those influencing the size of aerosol 30 particles commonly results in a size distribution which is well described by a single or multiple mode log-normal shape (Hansen and Travis, 1974; Thomason et al., 1997; Deshler et al., 2003; Deshler, 2008; Rieger et al., 2014). For example, in some cases

Deshler et al. (2003) use a bimodal particle size distribution to achieve the best approximation to their measurements from in-situ optical particle counters (OPC). However, this approach is not suitable for remote sensing instruments working in the limb or occultation geometry. This is because six independent pieces of information at each altitude level are needed to describe a bimodal log-normal particle size distribution, while measurements from space borne instruments commonly provide two to
5 three parameters per altitude level (Bingen et al., 2004a; Thomason et al., 2008; Rieger et al., 2014). Here, similar to other studies cited above, the distribution is considered to be unimodal and is described by

$$\frac{dn}{dr} = \frac{N}{\sqrt{2\pi} \ln(\sigma)r} \exp\left(-\frac{(\ln(r_g) - \ln(r))^2}{2\ln^2(\sigma)}\right), \quad (1)$$

where N is the total number density of the aerosol particles, r_g is the median radius and $\ln(\sigma)$ is the standard deviation of the $\frac{d\ln(n)}{d\ln(r)}$ distribution. Though r_g is directly used in the formula and indicates the maximum of $\frac{d\ln(n)}{d\ln(r)}$ distribution, we prefer
10 to work with the mode radius $R_{mod} = r_g / \exp(\ln^2(\sigma))$, which determines the maximum of $\frac{dn}{dr}$ distribution, and, thus, is more evident for the interpretation of results. Furthermore, throughout this study a representation of the absolute distribution width by the standard deviation of the $\frac{dn}{dr}$ distribution will be used:

$$w = \sqrt{r_g^2 \exp(\ln^2(\sigma))(\exp(\ln^2(\sigma)) - 1)}. \quad (2)$$

For the visual interpretation, w is more convenient than σ , as the latter is defined relative to the r_g parameter. In the following
15 text σ is used when describing retrieval settings, while w is used when discussing the retrieval results.

2.3 Algorithm description

Unlike the algorithms aimed to retrieve aerosol particle size distribution parameters from the occultation measurements (e.g. Bingen et al., 2004a; Thomason et al., 2008), our algorithm does not include aerosol extinction retrieval as an intermediate step. Instead, the measured limb radiances at seven wavelengths are directly employed to obtain the parameters. The wavelengths
20 are chosen outside the intervals near the spectral channel boundaries to avoid artifacts of the optical system. In order to reduce the measurement noise the sun-normalized radiances are averaged in the following intervals $\lambda_1=750\pm 2$ nm, $\lambda_2=807\pm 2$ nm, $\lambda_3=870\pm 2$ nm, $\lambda_4=1090\pm 2$ nm, $\lambda_5=1235\pm 20$ nm, $\lambda_6=1300\pm 6$ nm, $\lambda_7=1530\pm 30$ nm. The wavelengths below 750 nm are not considered because of a lower sensitivity to aerosols, and those above 1530 nm are rejected because of an insufficient signal-to-noise ratio. The intervals are chosen to avoid absorption signatures of other atmospheric constituents, minimizing uncertainties
25 caused by incorrect absorber profiles knowledge. Limb radiances are normalized by the measured solar irradiance spectrum (I_{sol}).

Both forward modelling and the retrieval are performed with the software package SCIATRAN-3.8 (Rozanov et al., 2014). The retrieval approach employs an iterative regularized inversion technique similar to that described by Rodgers (2000) to solve the inverse problem. In this approach the inversion of the linearized radiative transfer equation is required, which is formulated
30 as:

$$\mathbf{y} - \mathbf{y}_0 = \mathbf{K} \hat{\mathbf{x}} + \epsilon, \quad (3)$$

where \mathbf{y} is the measurement vector, whose components $[\mathbf{y}]_m = \ln\left(\frac{I_{meas}(\lambda_j, h_k)}{I_{sol}(\lambda_j)}\right)$ are the logarithms of the normalized limb radiances at all selected wavelengths (λ) and tangent heights (h). Here, index m is defined as $m = (k-1)N_\lambda + j$, where N_λ is the total number of wavelengths, k runs over selected h and j runs over selected λ . Components of the vector \mathbf{y}_0 are given by $[\mathbf{y}_0]_m = \ln\left(\frac{I_{mod}(\lambda_j, h_k)}{I_{sol}(\lambda_j)}\right)$, where $I_{mod}(\lambda_j, h_k)$ are modelled limb spectra at wavelength λ_j and tangent height h_k . State vector $\hat{\mathbf{x}}$ contains relative deviations of the retrieved atmospheric parameters, \mathbf{x} , from their initial values, \mathbf{x}_0 , e.g. $[\hat{\mathbf{x}}]_i = \frac{[\mathbf{x}]_i - [\mathbf{x}_0]_i}{[\mathbf{x}_0]_i}$ is the i -th component of the vector $\hat{\mathbf{x}}$. $[\mathbf{K}]_{m,i} = \left. \frac{\partial [\mathbf{y}]_m}{\partial [\mathbf{x}]_i} \right|_{\mathbf{x}=\mathbf{x}_0}$ defines components of the weighting function matrix (Jacobian matrix). All kinds of errors are denoted by ϵ . The solution of the linear inverse problem given by Eq. (3) can be found according to Rodgers (2000) as

$$\hat{\mathbf{x}} = (\mathbf{K}^T \mathbf{S}_y^{-1} \mathbf{K} + \mathbf{S}_a^{-1})^{-1} \mathbf{K}^T \mathbf{S}_y^{-1} (\mathbf{y} - \mathbf{y}_0), \quad (4)$$

where, \mathbf{S}_a represents the a priori covariance matrix, and \mathbf{S}_y is the noise covariance matrix.

Taking into consideration the non-linearity of the inverse problem, an iterative approach is implemented. Here, we do not follow the maximum a posteriori probability (MAP) approach suggested by Rodgers (2000). As the inverse problem is strongly non-linear, the use of a reasonable a priori covariance in the MAP approach results in a diverging solution, while the a priori variance which results in a stable solution strongly constrains it to the initial guess. To overcome this issue the weighted regularized inversion similar to zeroth-order Tikhonov method is used in this study. Thereby, the weight of the a priori information is decreased by replacing the initial state vector \mathbf{x}_0 at each iterative step by the state vector obtained at the previous iteration, \mathbf{x}_n . The variance of \mathbf{x}_n is set to 1%. This parameter was selected empirically to achieve a trade-off between the retrieval stability and sensitivity. Thus the solution at the (n+1) step is given by

$$\tilde{\mathbf{x}} = (\mathbf{K}_n^T \mathbf{S}_y^{-1} \mathbf{K}_n + \mathbf{S}_a^{-1})^{-1} \mathbf{K}_n^T \mathbf{S}_y^{-1} (\mathbf{y} - \mathbf{y}_n), \quad (5)$$

where $[\tilde{\mathbf{x}}]_i = \frac{[\mathbf{x}_{n+1}]_i - [\mathbf{x}_n]_i}{[\mathbf{x}_n]_i}$.

The iterative process stops when the maximum difference between the components of the solution vector at two subsequent iterative steps does not exceed 1%, the relative change in the root mean square of the fit residuals at two subsequent iterations is less than 0.001 or the limit of 100 iterations is reached. Since a strict constraint is put to deviations from the a priori vector, there are typically 20-30 iterations needed for the retrieval process to converge.

The noise covariance matrix is assumed to be diagonal, i.e. the errors are spectrally uncorrelated. Signal-to-noise ratio was estimated for each scan from SCIAMACHY measurements and varies from 65 to 5000 depending on the wavelength and tangent height. For each of the particle size distribution parameters, the diagonal elements of the a priori covariance matrix are set empirically to 0.01, and the non-diagonal elements drop off exponentially with a correlation radius of 3.3 km, while the elements describing the correlation between different parameters are chosen to be zero.

At present, only the retrieval of R_{mod} and σ is performed, and from these parameters w is calculated using Eq. (2). The particle number density, N , profile is selected in accordance with the ECSTRA model climatology for background aerosol loading conditions (Fussen and Bingen, 1999). N is assumed to decrease exponentially from 15.2 cm^{-3} at 18 km to 0.5 cm^{-3} at 35 km, and remains unchanged during the whole retrieval process. This is justified by a low sensitivity of the retrieval to

this parameter (see Sec. 3 for details). The initial guess parameter values are arbitrarily chosen as $R_{mod}=0.11 \mu\text{m}$ and $\sigma=1.37$. Scattering phase functions as well as extinction and scattering coefficients per particle are calculated using the Mie scattering theory. Aerosol parameters are defined from 12 to 46 km, where the particles are assumed to be sulfate droplets (75% H_2SO_4 and 25% H_2O) with 0% relative humidity in the surrounding atmosphere. Below 12 km and above 46 km the aerosol number density is set to zero. The refractive indices are taken from the OPAC database (Hess et al., 1998). Although the chosen representation of the aerosol composition might be inadequate below the tropopause and/or above 35 km, it enables us to avoid jumps and unreasonable values at the lowermost and the uppermost retrieval altitudes and does not affect significantly the retrieval sensitivity region (18-32 km, see Sec. 3.2 for details).

The retrieval is performed for the tropical zone (from 20°S to 20°N) in the altitude range from about 18 km up to about 35 km (the actual altitudes depend on the latitude and season). The choice of the altitude range is justified by lower sensitivity below 18 km (Rieger et al., 2018) and higher biases due to stray light above 35 km. To minimize the need for constraints and to avoid additional errors, e.g. related to altitude interpolation, the measurement grid is used for the retrieval. The exact levels of the measurement grid depend on time and latitude, but usually the grid ranges from about 0 km to 100 km with 3.3 km step. Outside the retrieval range, for the altitudes lower than the minimum retrieval height down to 12 km, the initial guess profile scaled relative to the result at the lowermost retrieved altitude is used; while for the altitudes above the upper border up to 46 km no additional constraints are set. We focus our initial study in the tropics because the transport mechanisms here are less complicated which makes the interpretation of the obtained results more straightforward. To extend the retrieval to the extra-tropical latitude bands, issues related to the scattering angles close to backward and forward scattering as well as large solar zenith angles need to be dealt with.

To reduce the sensitivity of the retrieval to the reflection properties of the underlying surface, effective spectral Lambertian albedo is concurrently retrieved based on the limb radiances at the same tangent heights where the aerosol particle size retrieval is performed. As it will be shown further, at 35 km aerosol influence on the limb radiances is rather small, thus the information from this tangent altitude contributes mainly to the albedo retrieval, while other tangent altitudes are employed for the stability reason. The initial albedo guess is 0.5 for all wavelengths. As for the particle size parameters, albedo for different wavelengths is uncorrelated with the other parameters and with the albedo at the other wavelengths. Clouds below and within the field of view remain an issue, even with the albedo retrieval. Therefore, only completely cloud free profiles (from 0 km) are used in this work. For this research, instead of the standard SCODA cloud filtering algorithm (Eichmann et al., 2016), a cloud filtering algorithm based on a statistical approach was used (Liebing, 2016). The algorithm designed by Liebing (2016) is more preferable for use in aerosol retrievals, because the Eichmann et al. (2016) approach has the disadvantage of flagging the pixels with high aerosol loading (i.e. after the volcanic eruptions) as cloudy.

Atmospheric pressure and temperature background profiles are from ECMWF (European Center for Medium-Range Weather Forecasts) operational analysis data for the specific date, time and location of each SCIAMACHY limb measurement.

3 Sensitivity studies

3.1 Model simulations

In this section sensitivity of the limb radiances to the aerosol particle size distribution parameters is analyzed by performing simulations with the radiative transfer model SCIATRAN. For this study the model was run for an observational geometry typical for the tropical region in the middle of July (a solar zenith angle of 41° and solar azimuth angle of 141°). The extraterrestrial solar flux measured by SCIAMACHY for the chosen day was used. In the radiative transfer model, multiple scattering was taken into account and the albedo was set to 0 (representation of the ocean surface).

To understand the sensitivity of the retrieval to the different particle size distribution parameters, three sets of limb radiance simulations were performed. For each set, one of the particle size distribution parameters was varied, while the other two parameters were fixed. The modelled intensities for these simulation sets are presented in Fig. 1 at the tangent height of 25 km. As the results at other tangent heights show similar behaviour, we analyze the sensitivity only at this arbitrarily chosen geometry. Natural logarithms of the simulated sun-normalized intensities for different values of the selected parameter (this representation corresponds to the way, how intensities are treated by the retrieval algorithm) are shown as lines. The shaded areas represent the amplitude of the intensity variations resulting from variations of the other two parameters. In this study the following simulation sets were performed: the first set employed a fixed $\sigma=1.37$ and the same number density profile as used in the retrieval, while the mode radius varied from 0.05 to 0.15 μm (Fig. 1 A). Another set of conditions (Fig. 1 B) was simulated by changing σ from 1.1 to 2.0 with the fixed $R_{mod}=0.08 \mu\text{m}$ and the same number density as in previous simulation set. This resulted in the variation of w from 0.008 to 0.13 μm . The last set of simulations (Fig. 1 C) was made by scaling the whole number density profile by factors ranging from 1 to 2, with the fixed $R_{mod}=0.08 \mu\text{m}$ and $\sigma=1.37$. The parameter set with standard non-scaled particle number density profile with $R_{mod}=0.08 \mu\text{m}$ and $\sigma=1.37$ was chosen as a reference, as this set of parameters is considered to be typical for a background (free of volcanic perturbations) atmosphere. We note, that this investigation was aimed to analyze a relative sensitivity of the observed limb radiance to the variations in different parameters and, thus, its results are not influenced much by their absolute values. Nevertheless, the considered amplitude of the parameter variations is in qualitative agreement with the reported variations of R_{mod} , σ and N in the stratosphere (Deshler et al., 2003).

Analyzing Fig. 1 it is evident that variations of the limb radiance due to variations of the particle number density profile, N , are remarkably smaller than those due to variations of R_{mod} or σ (or w). The variation of N profile by a factor of 2 (or 200%) results in a similar response in the limb radiance as the variation of R_{mod} by 0.01 μm ($\approx 13\%$) or variation of σ by 0.13 ($\approx 10\%$). This effect can be explained as follows: in a rough approximation the scattered solar radiance observed by a limb-viewing instrument is proportional to the product of N , scattering phase function (p) and aerosol extinction cross section (α_{aer}) (see e.g. Chandrasekhar, 1960). Both, p and α_{aer} , depend on R_{mod} and σ . As the dependency of p and α_{aer} on R_{mod} and σ is non-linear, these parameters contribute to the radiance stronger than N . The weaker dependence is also illustrated by much smaller weighting functions for N , than those for R_{mod} or σ . The weighting functions (R_{mod} , σ and N) for each retrieved altitude are shown in Fig. 2. As the weighting functions (see Sec. 2.3) show the variations in the observed signal due to changes in the considered parameter, much smaller weighting functions of N (Fig. 2, right panel) mean much smaller

contribution due to variations of the parameter in the measured signal. As a consequence, the variations in N are neglected in the retrieval, and the altitudinal behaviour in the N profile considered to be constant with the time.

It is worth emphasizing again, that the number density profile used in the above described retrieval is derived from the ECSTRAT climatology for background aerosol loading conditions (see 2.3). Even though we increase the uncertainty for the volcanic active periods, for the background period the errors are rather small because we use the profile which is expected to be close to the reality. The magnitude of the errors in the retrieved R_{mod} , σ and w due to unknown N is discussed in the next section.

3.2 Characterization of the retrieval

The effect of the unknown number density on the retrieved R_{mod} and σ , as well as general retrieval characteristics are discussed in this section.

To characterize the sensitivity of retrieval algorithms averaging kernels are commonly used. In general, this characteristic is specific to the measurement setup, algorithm implementation, and retrieval parameters settings. Averaging kernels for the limb scatter space-borne instruments in the relevant altitude region are distinctly peaked at the tangent altitudes, where a bulk of information is originating from. Their shape characterizes the vertical sensitivity and resolution of the measurement-retrieval system and provides information on the contribution of the a priori information to the retrieved profiles.

In Fig. 3 averaging kernels for both R_{mod} (left panel) and σ (right panel) are presented for typical tropical observation conditions. Since variations in the observational geometry (viewing angle and solar zenith angle) in the tropics are rather small, only one specific example for typical illumination and background conditions is presented here. At all altitudes in the retrieval range (in this case 18.5-34.9 km), except for the uppermost one, averaging kernels for both parameters have pronounced peaks at the measurement tangent altitudes indicating that no significant smearing of the results in the vertical domain has occurred and optimal sensitivity of the retrieval is achieved for each tangent altitude. At the uppermost altitude (34.9 km) averaging kernels are clearly broader and the peak is much less distinct in comparison to the other altitudes. Such shape of the averaging kernels at this altitude is evidence of a strong influence of the neighboring altitude levels and partial loss of sensitivity.

As pointed out above, in the performed retrieval the relative deviations from the solution obtained at the previous iterative step are determined. The state vector variance is set to 1% of the parameter values resulting from the previous iteration. For this reason such widely used characteristics as the averaging kernel peak value, a posteriori covariance and measurement response are meaningful only within one iterative step but not applicable to the full iterative process.

An additional assessment of the retrieval performance was done by simulating the limb radiance using perturbed values for the retrieved parameters and then performing the retrieval using synthetic data. For all retrieval runs the same settings as in the nominal retrieval process were used. Ideally, the retrieved values are expected to be the same as those used to simulate the radiances. To test the retrieval under different conditions, five scenarios were used. All scenarios were simulated for one observation geometry (viewing and solar zenith angles) typical for SCIAMACHY limb measurements in the tropical region. A detailed information on the selected scenarios is presented in the Tab. 1. Generally, the scenarios can be divided into three types depending on the perturbation of the particle size parameters. The first type includes "small", "background" and "volcanic"

scenarios. The intensities for these scenarios were modelled using R_{mod} and σ as listed in Tab. 1 with the same particle number density profile, as assumed in the retrieval algorithm, i.e. only R_{mod} and σ were perturbed. The second type is represented by "volcanic (2N)" scenario, which was modelled with the same R_{mod} and σ as the "volcanic scenario", but the particle number density profile was multiplied by a factor of 2 between 12 and 23 km. The perturbation in the number density profile was performed only in the lower layers because significant changes in the aerosol loading due to volcanic eruptions during the SCIAMACHY life time were shown to reach maximum altitude of about 23 km (von Savigny et al., 2015). The third type is represented by the "unperturbed" scenario. For this scenario intensities were simulated with $R_{mod}=0.11 \mu\text{m}$, $\sigma=1.37$ and the particle number density profile assumed in the retrieval, i.e. with the same parameter values as used to initialize the retrieval algorithm. All these values with slight adjustments were taken from (Deshler, 2008) and are expected to be close to the reality.

As there is no reliable information on the altitudinal behaviour of R_{mod} and σ , the values for that parameters are kept constant with the height. In all the scenarios modelled surface albedo was assumed to be 0.15 at all wavelengths. Gaussian noise has been added to all simulated limb radiances based on the signal-to-noise ratios estimated from SCIAMACHY measurements. To ensure a reliable statistics 100 independent noise sequences were generated.

Figure 4 presents the retrieved profiles of R_{mod} (left panel) and their relative errors (right panel) for the above discussed scenarios. For σ , retrieved profiles and relative errors are plotted in Fig. 5. Solid lines in the left panels of Figs. 4 and 5 refer to the median retrieved profiles for the scenario, and dashed lines represent true modelled conditions. In the right panels of Figs. 4 and 5 solid lines show relative median errors of the retrieved profiles with respect to the true value. In both figures, shaded areas show ± 1 standard deviation from the median value.

Analysis of Figs. 4 and 5 shows, that the retrieval results using "unperturbed" profiles (brown lines) of R_{mod} and σ as well as the results for profiles with the perturbed R_{mod} and σ (cyan, blue and green lines) are very close to the true values. The relative error is within 20% for R_{mod} and within 5% for σ . Maxima of the absolute ($\epsilon = |retrieved - true|$) and relative errors for all scenarios and parameters are summarized in Tab. 1. It is worth mentioning that the maximum deviation for the scenarios with unperturbed N is about $\pm 0.01 \mu\text{m}$ for R_{mod} . For σ , the absolute error differs, but does not exceed 0.07. For the volcanic scenario with a perturbed N profile it is obvious that a wrong number density assumption influences the retrieved profile, although this influence is rather small. The relative error for that case is less than 20% for R_{mod} and less than 10% for σ , maximum absolute errors for R_{mod} and σ are respectively $0.04 \mu\text{m}$ and 0.1. The retrieval scenario with "unperturbed" particle size distribution parameters resulted in the profiles which differ less than 2% from the true values. This characterizes the retrieval error resulting from the measurement noise. The retrieved albedo varies from 0.11 to 0.23 depending on the scenario and the wavelength.

Referring to Sec. 2.2 it is important to remember that in this study we analyze w as given by Eq. (2) rather than σ . Even though σ as a parameter is widely used in the retrievals and in the climate models, it doesn't provide visually interpretable information about the width of the particle size distribution, because it is defined relative to r_g . Due to this reason we use σ as a retrieval parameter, while w is used in the interpretation and discussion of the retrieved results. For that reason it is important to assess retrieval uncertainties for w either.

Table 1. Selected scenarios and associated maximum of absolute (relative) errors.

name	true					colour *	perturbation	max.		
	$R_{mod}, \mu\text{m}$	$r_g, \mu\text{m}$	σ	$w, \mu\text{m}$	$\epsilon_{R_{mod}}, \mu\text{m}$			ϵ_{σ}	$\epsilon_w, \mu\text{m}$	
small	0.06	0.08	1.7	0.052	cian	R_{mod}, σ	0.01 (19%)	0.07 (5%)	0.001 (2%)	
background	0.08	0.10	1.6	0.055	blue	R_{mod}, σ	0.01 (9%)	0.04 (2%)	$5 \cdot 10^4$ (1%)	
unperturbed	0.11	0.12	1.37	0.041	brown	unpert.	0.002 (2%)	0.009 (1%)	$3 \cdot 10^4$ (1%)	
volcanic	0.20	0.21	1.2	0.039	green	R_{mod}, σ	0.01 (5%)	0.04 (3%)	0.005 (13%)	
volcanic (2N)	0.20	0.21	1.2	0.039	red	R_{mod}, σ, N	0.04 (19%)	0.1 (8%)	0.015 (40%)	

* Colour of the lines in Figs. 4-6. In the last 3 columns maximum absolute error for the profile is given by the number without brackets, while the maximum relative error is presented in brackets.

In the left panel of Fig. 6, profiles of the absolute distribution width (solid lines), derived from the retrieved R_{mod} and σ , for each scenario are depicted. As in the Figs. 4 and 5, the dashed lines depict the true values. In the right panel of Fig. 6 relative errors are plotted by solid lines. Shaded areas in both panels of Fig. 6 show the standard deviation. Looking at Fig. 6, it is obvious, that the retrieval errors from the distribution width for small (cyan lines), background (blue lines) and unperturbed (brown lines) scenarios are rather small: absolute errors (Tab. 1) are less than $0.001 \mu\text{m}$, and relative errors are smaller than 2%. In the volcanic case with unperturbed N (green lines) differences are within $0.005 \mu\text{m}$, which corresponds to 14%. On the contrary for the volcanic scenario with perturbed N (red lines), the derived w deviates from the true value by up to 40% ($0.015 \mu\text{m}$).

Although the differences for R_{mod} and σ are comparably small, it is important to mention, that from all the modelled scenarios w for the volcanic scenarios is generally the smallest, and larger relative errors are often associated with the division by a small true value. To test this hypothesis another volcanic scenario with larger w ("wide") was simulated ($R_{mod}=0.20 \mu\text{m}$, $\sigma=1.27$, N profile is perturbed by the factor of 2 in a layer between 12 and 23 km) and run through the synthetic retrieval. The retrieved profiles of R_{mod} , σ and absolute distribution width are shown in Fig. 7, where solid lines show the retrieved profiles and dashed lines represent true values. In red, the standard "narrow" volcanic scenario with perturbed number density is presented, whereas the magenta colours depict the "wide" scenario (see Tab. 2). Relative errors for these scenarios and parameters are presented in Fig. 8. From Figs. 7 and 8 it is clearly seen that even though the behaviour of R_{mod} and σ did not change significantly, and the absolute/relative errors are very similar for all three parameters, the maximum relative error for w decreased to 23%.

Summarizing Sec. 3 it can be concluded that for background conditions the algorithm is capable to retrieve R_{mod} with relative accuracy of better than 20% (absolute uncertainty of about $0.01 \mu\text{m}$) and σ better than 5% (absolute uncertainty less than 0.07). The relative accuracy of the derived w is dependent on its absolute value and is about 2% ($0.001 \mu\text{m}$) for background conditions. As particle number density is fixed in the retrieval, all uncertainties associated with this parameter are interpreted as changes in R_{mod} and/or σ . Considering previous studies on stratospheric aerosol size distribution (Deshler et al., 2003; Bingen et al., 2004a, b; Deshler, 2008), we believe that for the period from 2002 till 2012 a variation in N within a factor of 2

Table 2. Selected scenarios and associated maximum of absolute (relative) errors.

name	true				colour *	perturbation	max.		
	$R_{mod}, \mu\text{m}$	$r_g, \mu\text{m}$	σ	$w, \mu\text{m}$			$\epsilon_{R_{mod}}, \mu\text{m}$	ϵ_{σ}	$\epsilon_w, \mu\text{m}$
narrow	0.20	0.21	1.2	0.039	red	R_{mod}, σ, N	0.04 (19%)	0.1 (8%)	0.015 (40%)
wide	0.20	0.21	1.27	0.053	magenta	R_{mod}, σ, N	0.05 (24%)	0.1 (8%)	0.012 (23%)

* Colour of the lines in Figs. 7-8.

In the last 3 columns maximum absolute error for the profile is given by the number without brackets, while the maximum relative error is presented in brackets.

is a realistic assumption. Thus, possible retrieval errors after volcanic eruptions occurred during the SCIAMACHY observation period are estimated to be about 20-25% for R_{mod} and less than 10% for σ . For the volcanic scenarios the relative error for w can reach up to 40% while the absolute error does not exceed 0.015 μm .

4 Results and discussion

5 In this section, first results of the retrieval of the aerosol particle size distribution parameters from SCIAMACHY limb observations are presented. As it was mentioned above (see Sec. 2), the retrieval algorithm was applied to data for the tropical region and completely cloud free (from 0 km) scenes, resulting in 9727 profiles for the entire SCIAMACHY observation period. The cloud filtering algorithm by Liebing (2016) used in this study employs a probability approach, which means that there is still a 10% chance of cloud or its fraction to influence the profile. Thus, to reject possible unreasonable results, post-retrieval filtering
10 criteria were applied as follows: values with $R_{mod} < 0.03 \mu\text{m}$ were rejected, as they are laying outside the sensitivity range of the instrument, and aerosol extinction at 750 nm calculated using the retrieved particle size distribution parameters was not allowed to exceed 0.0015 km^{-1} . A similar approach to filter the aerosol extinction at 750 nm was used to reject cloudy scenes in SCIAMACHY V1.4 aerosol extinction product (Rieger et al., 2018). Non-converged retrievals with 100 iterations
15 maximum mode radius in the retrieved data set reached the value $R_{mod}=0.21 \mu\text{m}$, and σ varied from 1.02 to 2.9. All the values are considered to be realistic within the reported errors.

As the temporal sampling of the current product is not sufficient to analyze the volcanic plumes, monthly zonal (20°N-20°S) means were used to evaluate the overall state of the stratosphere during the SCIAMACHY observation period. These monthly averaged values of R_{mod} and w are presented in Figs. 9 and 10, respectively. Here, some obvious patterns such as the increase
20 of the values after most of the volcanic eruptions (dashed lines) can be readily identified. In addition, there is a pronounced seasonality in both R_{mod} and w . As the seasonal cycle of stratospheric aerosols has already been discussed by several authors (Hitchman et al., 1994; Bingen et al., 2004a), we focus our study on the analysis of the anomalies of the particle size distribution parameters. Anomalies or deseasonalized values for R_{mod} and w , as shown in Figs. 11 and 12, respectively, were obtained by subtracting from each monthly mean value an average over all corresponding months in the whole observation period (e.g.

the average value for all the Januaries of the 10 year period was subtracted from each January monthly mean value in the observation period).

Analyzing the anomalies for R_{mod} presented in Fig. 11 it can be noticed, that there is a distinct increase of R_{mod} in the lower altitudes after most of the volcanic eruptions, except for the eruptions of Ruang and Reventador in late 2002 and Merapi in late 2010. For these tropical eruptions only a slight increase in R_{mod} is observed. This may be related to a smaller amount of SO_2 released during these eruptions (see database of the Smithsonian Institution (2017) or Bingen et al. (2017)). Another important feature is a periodic variation of R_{mod} in the 28-32 km range, related to the quasi-biennial oscillation (QBO). A similar QBO signature in the aerosol extinction coefficients retrieved from SCIAMACHY limb measurement at altitudes around 30 km was reported by Brinkhoff et al. (2015) and explained by the influence of the secondary meridional circulation. The QBO pattern is also seen in the anomalies of w (Fig. 12). Volcanic eruptions influence aerosol w in different ways. As for R_{mod} there is an increase of w after Tavurvur, Kasatochi, Sarychev and Merapi eruptions, while a slight decrease of w at some altitudes after Nabro eruption and no change in w at all altitudes after the Manam eruption is observed.

Following the strong tropical eruptions (Manam, Tavurvur, Nabro) there is a well-defined increase of R_{mod} shortly after the eruptions in the 18 - 21 km altitudes, while at higher altitudes (22-26 km) the volcanic perturbation is observed with a specific time lag. This is the so called tape recorder effect, which is associated with the vertical transport of air masses in the tropical stratosphere. After strong mid-latitude eruptions (Sarychev, Kasatochi) the increase in R_{mod} is less pronounced as compared to the tropical volcanoes, though there is a definite increase in w . There are two possible explanations of this effect. First, the initial and longer term growth in particles is a result of the oxidation of SO_2 to H_2SO_4 with chemical rates depending on the physical conditions at a given altitude and latitude. Second, during the transport of the air masses from the mid-latitudes to the tropics the aerosol particle size distribution is modified as a result of sedimentation of heavier particles with large radii. Unfortunately the justification for these hypotheses can be provided only after implementing the current algorithm for the extra-tropical latitudes and modelling the eruptions accounting for the aerosol microphysics, which is outside the scope of this study.

For a better understanding of the variations in the particle size distribution after different volcanic eruptions, we considered in more detail the temporal evolution of the aerosol particle size distributions at 18, 22 and 25 km altitudes after the Manam and Tavurvur eruptions. This was done using the profiles retrieved from the individual measurements. The resulting distributions are presented in Fig. 13. For ease of comparison the distributions in the Manam series are plotted in the left column and for Tavurvur in the right column. As in Eq. (1), N is a multiplicative factor of $\frac{dn}{dr}$, $N=1 \text{ cm}^{-3}$ was used for each altitude to make the Fig. 13 more descriptive. In each panel of Fig. 13 four distributions corresponding to different time lags before and after the eruptions obtained at similar latitudes ($\pm 2^\circ$) are presented. There were four time slots chosen: before the eruption (green lines), in the first months after the eruption (red lines), more than half a year (blue lines) and over a year after the eruption (cyan lines). The exact dates corresponding to the curves are presented in the legend below the panels.

As mentioned above, the Manam eruption was characterized by an increase of R_{mod} , but almost no change of w after the eruption in comparison to the background conditions. This can be seen looking at the depicted distributions. At 18 km (upper left panel in Fig. 13) in the first months after the eruption (red line) the distribution shifts to the larger values in comparison to

the distribution before the eruption (green line). After around seven months after the eruption (blue line) distribution shifts to slightly smaller values, but its peak is still located at a distinctively larger radius value than for the background distribution. At the end of March 2006, 14 months after the eruption (cyan line), the atmosphere at this altitude is "relaxed" and returns to a state close to that before the eruption, albeit with a slightly larger R_{mod} . This can be related to a weaker eruption of Manam in the end of February - beginning of March 2006 (see database of Smithsonian Institution (2017) or Bingen et al. (2017)). It is interesting to mention that w after the eruption (red, blue and cyan lines) does not seem to change much in comparison to that of background conditions (green line), but it is obvious that the distribution before the eruption (green line) has a distinctively stronger relative contribution of larger particles than the one after the eruption. The distributions at 22 km (middle left panel in Fig. 13) before and shortly after the eruption look similar, with the perturbation to the particle size distribution shape being observed 7 and 14 months after eruption (blue and cyan lines). These time delays are attributed to the vertical transport velocity. For the same reason, the 25 km altitude (lower left panel in Fig. 13) distributions before the eruption, as well as two and seven months after the eruption are similar to each other, but the one 14 month after the eruption is shifted to larger radii. For all distributions there is no noticeable change observed for w .

The temporal evolution of the aerosol particle size distribution after the Tavorvur eruption showed a different behaviour than that after Manam. At the lowermost retrieved altitude (18 km, upper right panel) aerosol particle size distribution shifts to the larger R_{mod} and gets remarkably wider shortly after the eruption (red line). It appears that the stratospheric aerosol formed after the Tavorvur eruption superposed with the one after the weaker Soufriere Hills eruption, which occurred several months before (see database of Smithsonian Institution (2017) or Bingen et al. (2017)). Although the Soufriere Hills eruption might have influenced the observed distributions, it is not possible to distinguish between these two eruptions and we will consider them as one event. About eight months after the event, the distribution shifts to the smaller R_{mod} and gets narrower. After one year (cyan line) the distribution returns almost to the same shape as before the eruption (green line), similar to the evolution after the Manam eruption. At 22 km (middle right panel of Fig. 13) the distribution responds as expected with the time lag of around half a year, and at 25 km the changes are most likely dominated by other processes and not significant in general.

Another remarkable event was the eruption of Nabro in the middle of June of 2011. As presented by Figs. 11 and 12 it was characterized by an increased R_{mod} and a decreased w . The later might be a result of significant volcanic activity preceding the Nabro eruption. Since this eruption occurred less than a year before the connection to ENVISAT was lost, we cannot fully track it.

5 Comparison with SAGE II

As mentioned in Sec. 1, SAGE II was one of the key instruments providing aerosol particle size information. Operating from 1984 till 2005 SAGE II has a 3 years overlap with SCIAMACHY, enabling us to use SAGE II as a comparison instrument in the assessment of SCIAMACHY aerosol particle size distribution product.

In this study the current version v7.0 of the SAGE II stratospheric aerosol data was used (Damadeo et al., 2013). This version reports extinction coefficients at multiple wavelengths along with the effective radius. Assuming the unimodal log-

normal particle size distribution, effective radius can be related to the particle size distribution parameters as follows:

$$r_{eff} = r_g \exp(2.5 \ln^2(\sigma)). \quad (6)$$

As SAGE II is a solar occultation instrument, it provides 30 profiles (both sunrise and sunset events) per day. In contrast, SCIAMACHY is a limb scatter instrument, providing around 1400 measurements per day. However, only tropical and completely cloud free profiles were used, so the resulting sampling was much sparser. Taking into consideration this sampling, fairly loose collocation criteria of $\pm 5^\circ$ latitude, $\pm 20^\circ$ longitude and ± 24 hours were used for the comparison, resulting in 57 collocations during the 3 years of SCIAMACHY and SAGE II overlap. As SCIAMACHY vertical sampling is coarser than that of SAGE II, and SCIAMACHY retrievals were performed on a coarser altitude grid (3.3 km compared to 0.5 km by SAGE II), SAGE II data was first smoothed to the SCIAMACHY vertical resolution and afterwards interpolated onto the SCIAMACHY vertical grid.

Mean relative difference between the effective radius from SCIAMACHY and SAGE II is presented in Fig. 14. The relative difference is about 30% in the lower altitudes decreasing with increasing height to less than 20% at 26 km and around 0% at 30 km. As it can be seen in Fig. 15, where both collocated data sets are plotted versus time, the offset between SCIAMACHY (blue dots) and SAGE II (red dots) effective radii is constant with the time with SCIAMACHY being systematically lower at 18 and 21.3 km. One of the possible reasons of the observed differences is the low sensitivity of SAGE II to the particles with radius smaller than $0.1 \mu\text{m}$ (Thomason et al., 2008). In contrast, our investigations (not shown here) demonstrate that for SCIAMACHY limb measurements the sensitivity drops for particles smaller than $0.06 \mu\text{m}$. This is explained by the differences in the measurement techniques. According to text books on radiative transfer, e.g. Chandrasekhar (1960), the signal observed by an occultation instrument is determined by the aerosol extinction coefficient, while for the measurements of the scattered solar light the product of the aerosol extinction coefficient and the scattering phase function is relevant. As the period from 2002 to 2005 was considered to be volcanically quiescent, smaller particles were dominating at the time, increasing the possible biases. However, for a more detailed evaluation of this aspect, larger amount of collocations needs to be analyzed. Possible reasons for the observed lopsided differences are still under investigations.

6 Conclusions

In this study a retrieval algorithm to obtain two parameters of the stratospheric aerosol particle size distribution (R_{mod} and σ) from SCIAMACHY limb measurements was presented. In this retrieval a fixed vertical distribution of the aerosol particle number density, N , is assumed, and N is not retrieved. Wavelength dependent surface albedo is included in the retrieval. The algorithm uses the measurements of the scattered light at 7 wavelengths and a normalization to the extraterrestrial solar irradiance. Investigation of the averaging kernels showed a good sensitivity in the altitude range from 18 to 32 km for both retrieved parameters. Synthetic retrievals demonstrated, that using the presented algorithm for SCIAMACHY limb measurements, errors for R_{mod} are typically in the range 10-20% for the considered unperturbed N profile (the reported absolute error is $0.01 \mu\text{m}$). For σ , the errors are even smaller and lay within 5% (absolute error value is less than 0.07). For a perturbed N profile, errors

increase to 20% for R_{mod} and to 10% for σ . For easier interpretation of the retrieval results, the absolute distribution width, w , was used instead of σ . For w , the error is insignificant (less than 2%) for background conditions and can reach 40% after volcanic eruptions, it does not exceed however $0.015 \mu\text{m}$ in terms of the absolute differences. Implementation of this retrieval algorithm to SCIAMACHY measurements allowed us to generate the first, and for now, unique data set of two particle size distribution parameters from an instrument measuring scattered light in the limb viewing geometry. Analyzing the retrieval results, an increase of R_{mod} in the altitude range from 18 to 25 km after the volcanic eruptions was identified, while w after the volcanic eruptions did not show any distinct behaviour (can increase, decrease or remain unchanged). Tape recorder effect or delayed response of the parameters to the volcanic eruptions for higher altitudes was observed for both parameters. Variations in 28-32 km altitude range in both R_{mod} and w due to quasi biannual oscillation (QBO) were identified. The retrieval results were compared to the SAGE II data and showed an agreement within 30% for effective radii in the lower altitudes, getting better with increasing altitude to better than 10% above 25 km. For all altitudes a systematic negative bias was observed.

7 Data availability

SCIAMACHY aerosol particle size distribution data is available after registration at <http://www.iup.uni-bremen.de/scia-arc/>.

Competing interests. The authors declare that they have no conflict of interest.

15 *Acknowledgements.* This work was funded in parts by European Space Agency (ESA) through SQWG and SPIN projects, German Aerospace Center (DLR) through SADOS project, German Federal Ministry of Education and Research (BMBF) through ROMIC-ROSA project, University and State of Bremen. We thank ECMWF for providing pressure and temperature information. We also thank NASA for SAGE II data which was downloaded from the NASA Langley Research Center EOSDIS Distributed Active Archive Center.

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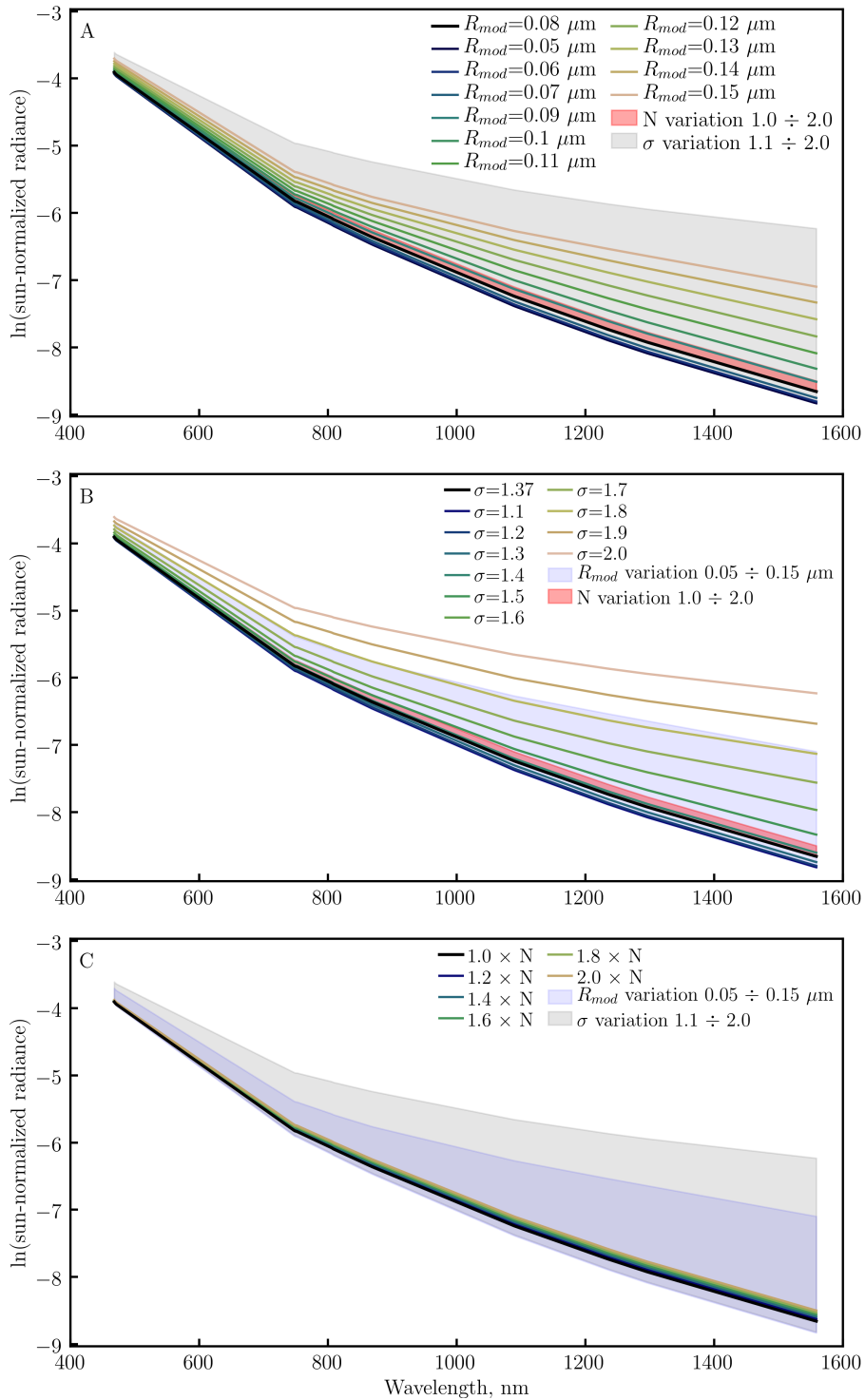


Figure 1. Logarithms of sun-normalized intensities spectra at a tangent height of 25 km, modelled with different particle size distribution parameters. Black line represents the "standard" background conditions.

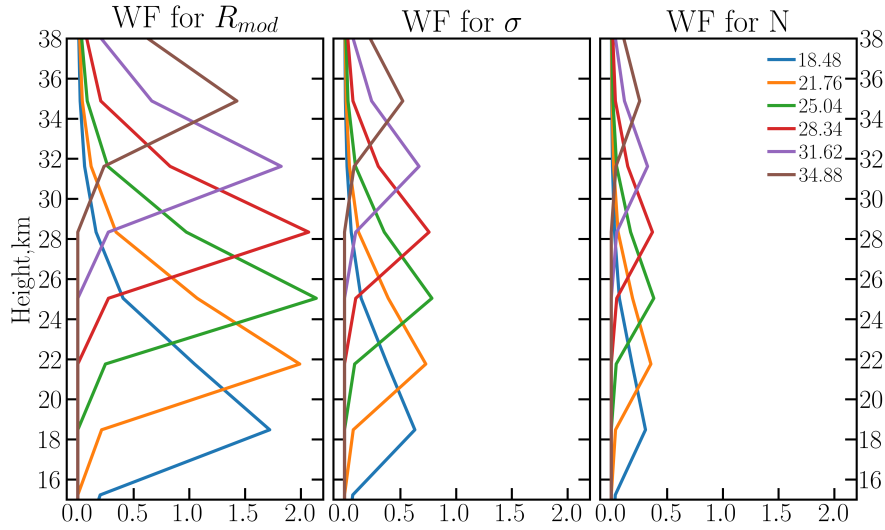


Figure 2. Relative logarithmic weighting functions at $\lambda_7=1530$ nm in the retrieval height range for R_{mod} (left), σ (middle) and particle number density N (right). Colour coded are the different tangent heights.

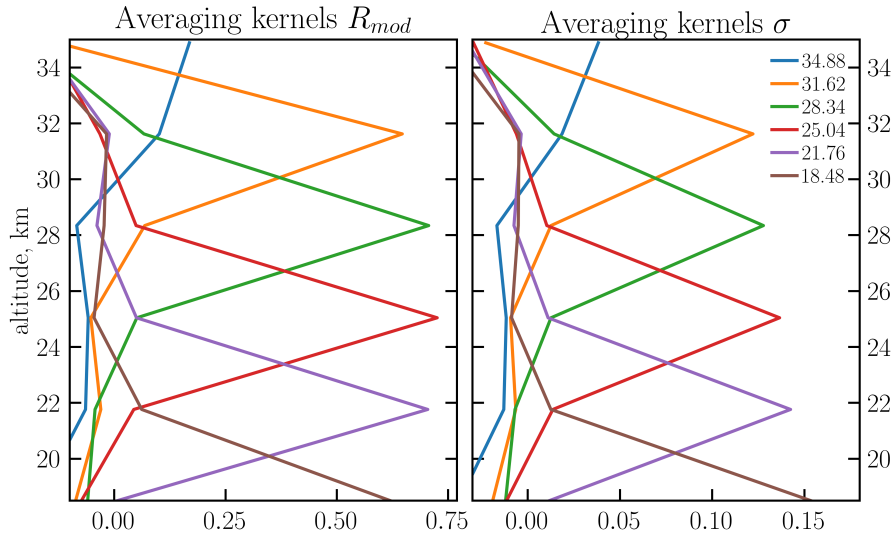


Figure 3. Averaging kernels for the aerosol particle size distribution parameters: R_{mod} (left) and σ (right). Results were obtained using the spectra modelled with perturbation of all three parameters. Colour coded are the different tangent heights.

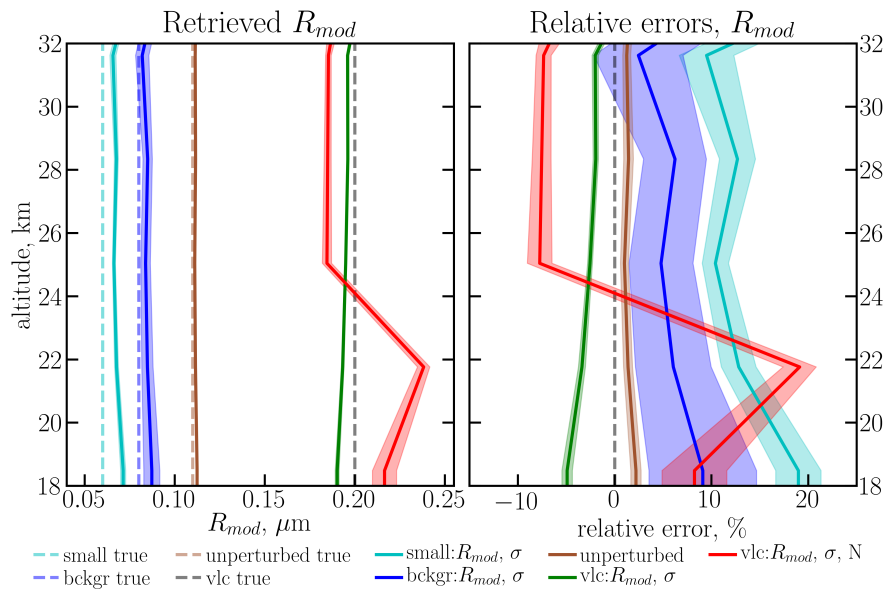


Figure 4. R_{mod} profiles (solid lines, left panel) and their relative errors (solid lines, right panels) for a typical tropical observation geometry. Synthetic retrievals for unperturbed parameters (brown lines), for small particles (cyan lines) and background case (blue lines) with perturbed R_{mod} and σ , as well as volcanic case with perturbed mode radius R_{mod} and σ (green lines), and with perturbed R_{mod} , σ and N in a layer (12-23 km) (red lines) with 100 different noise sequences were performed. True values are shown by dashed lines, shaded areas represent one standard deviation.

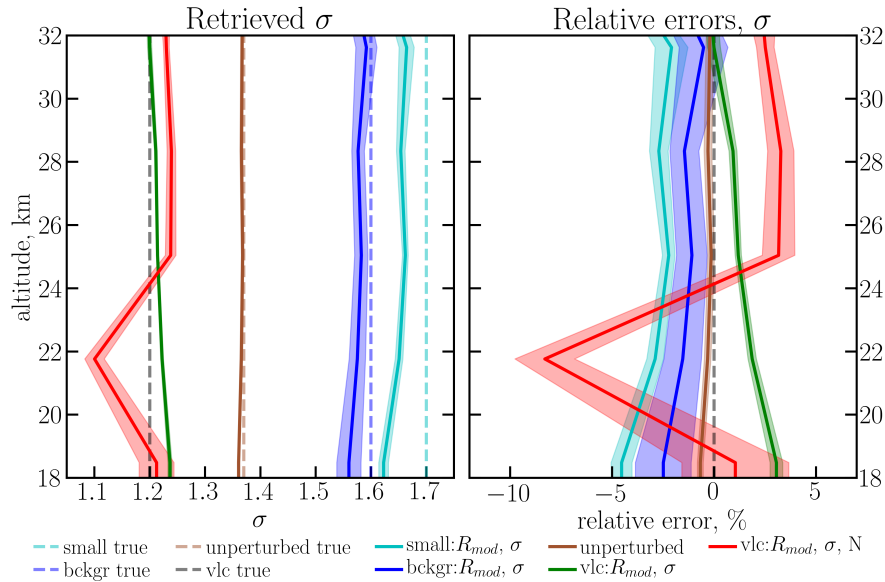


Figure 5. σ profiles (solid lines, left panel) and their relative errors (solid lines, right panels) for a typical tropical observation geometry. Synthetic retrievals for unperturbed parameters (brown lines), for small particles (cyan lines) and background case (blue lines) with perturbed R_{mod} and σ , as well as volcanic case with perturbed mode radius R_{mod} and σ (green lines), and with perturbed R_{mod} , σ and N in a layer (12-23 km) (red lines) with 100 different noise sequences were performed. True values are shown by dashed lines, shaded areas represent one standard deviation.

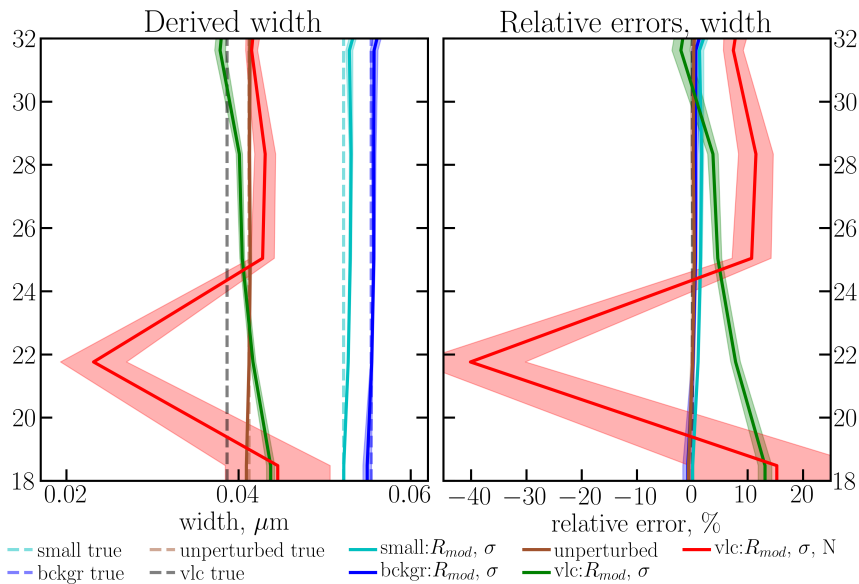


Figure 6. Absolute distribution width, w , profiles (solid lines, left panel) and their relative errors (solid lines, right panels) for a typical tropical observation geometry. Synthetic retrievals for unperturbed parameters (brown lines), for small particles (cyan lines) and background case (blue lines) with perturbed R_{mod} and σ , as well as volcanic case with perturbed mode radius R_{mod} and σ (green lines), and with perturbed R_{mod} , σ and N in a layer (12-23 km) (red lines) with 100 different noise sequences were performed. True values are shown by dashed lines, shaded areas represent one standard deviation.

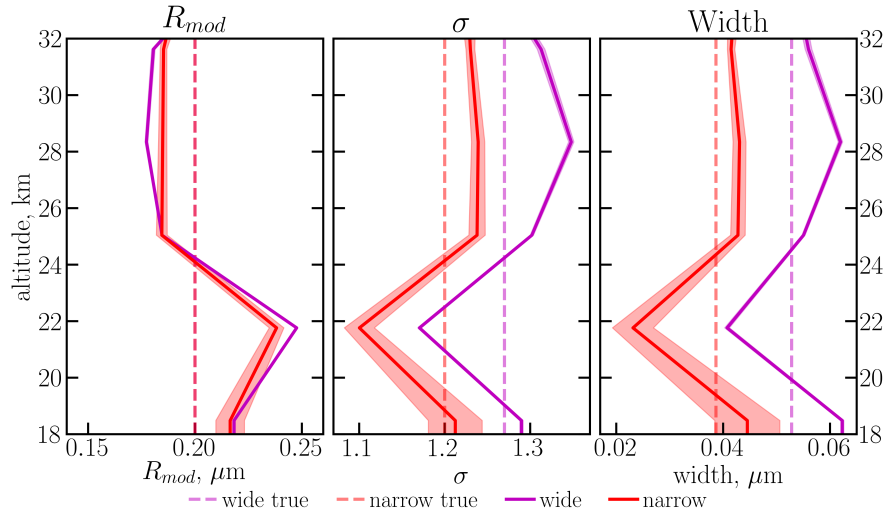


Figure 7. Retrieved profiles (solid lines) of R_{mod} , σ and derived values of w for the volcanic scenarios with perturbed R_{mod} , σ , N . Scenarios with smaller ("narrow", red lines) and larger ("wide", magenta lines) distribution width and 100 different noise sequences were considered. True values are shown by dashed lines, shaded areas represent one standard deviation.

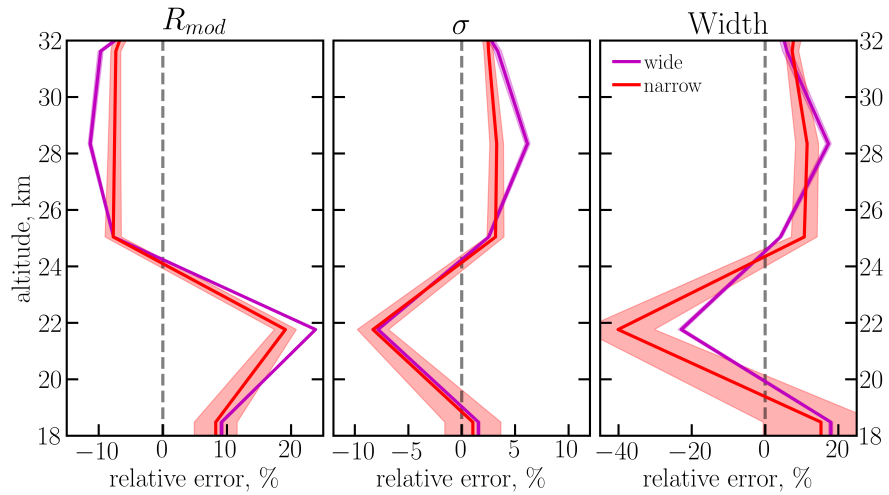


Figure 8. Relative errors for R_{mod} , σ and derived values of w for the volcanic scenarios with perturbed R_{mod} , σ , N . Scenarios with smaller ("narrow", red lines) and larger ("wide", magenta lines) distribution width and 100 different noise sequences were considered. Shaded areas represent one standard deviation.

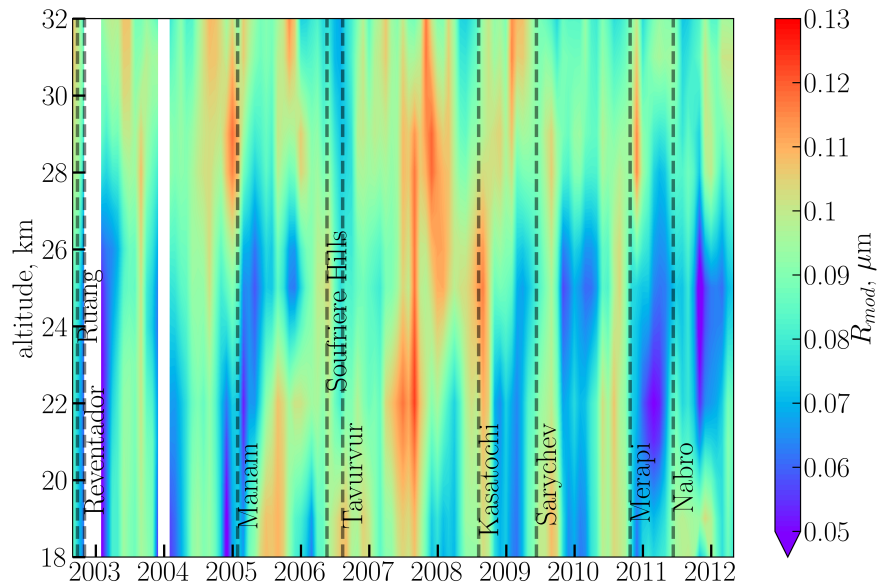


Figure 9. Monthly zonal mean values of R_{mod} retrieved from SCIAMACHY limb data in the tropics ($20^{\circ}\text{N} - 20^{\circ}\text{S}$).

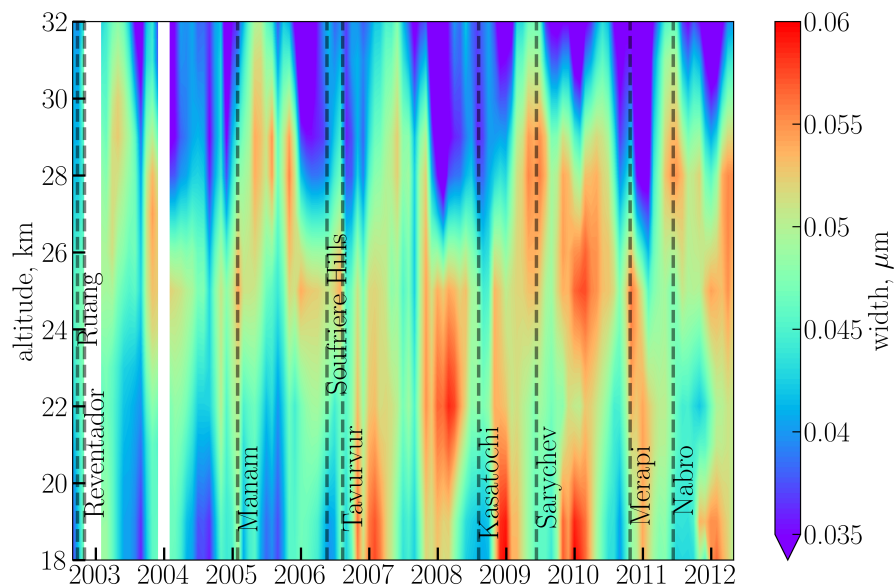


Figure 10. Monthly zonal mean values of w as defined by Eq. (2) retrieved from SCIAMACHY limb data in the tropics ($20^{\circ}\text{N} - 20^{\circ}\text{S}$).

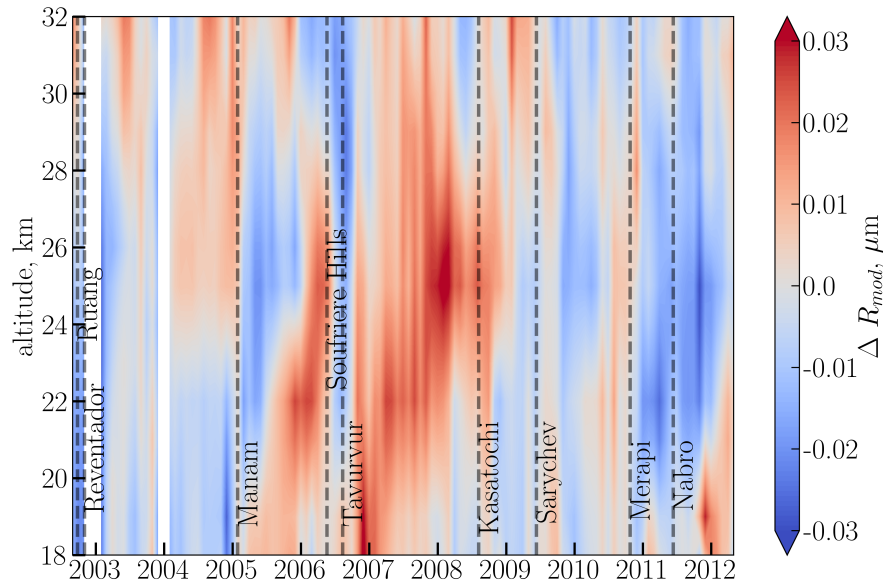


Figure 11. Deseasonalized time series (anomalies) of R_{mod} retrieved from SCIAMACHY limb data in the tropics ($20^{\circ}\text{N} - 20^{\circ}\text{S}$).

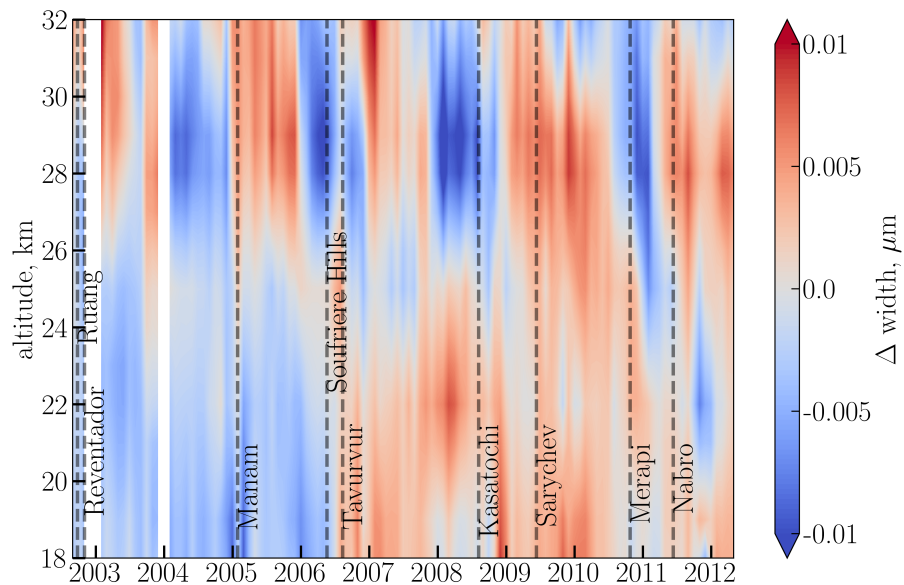


Figure 12. Deseasonalized time series (anomalies) of w as defined by Eq. (2) retrieved from SCIAMACHY limb data in the tropics ($20^{\circ}\text{N} - 20^{\circ}\text{S}$).

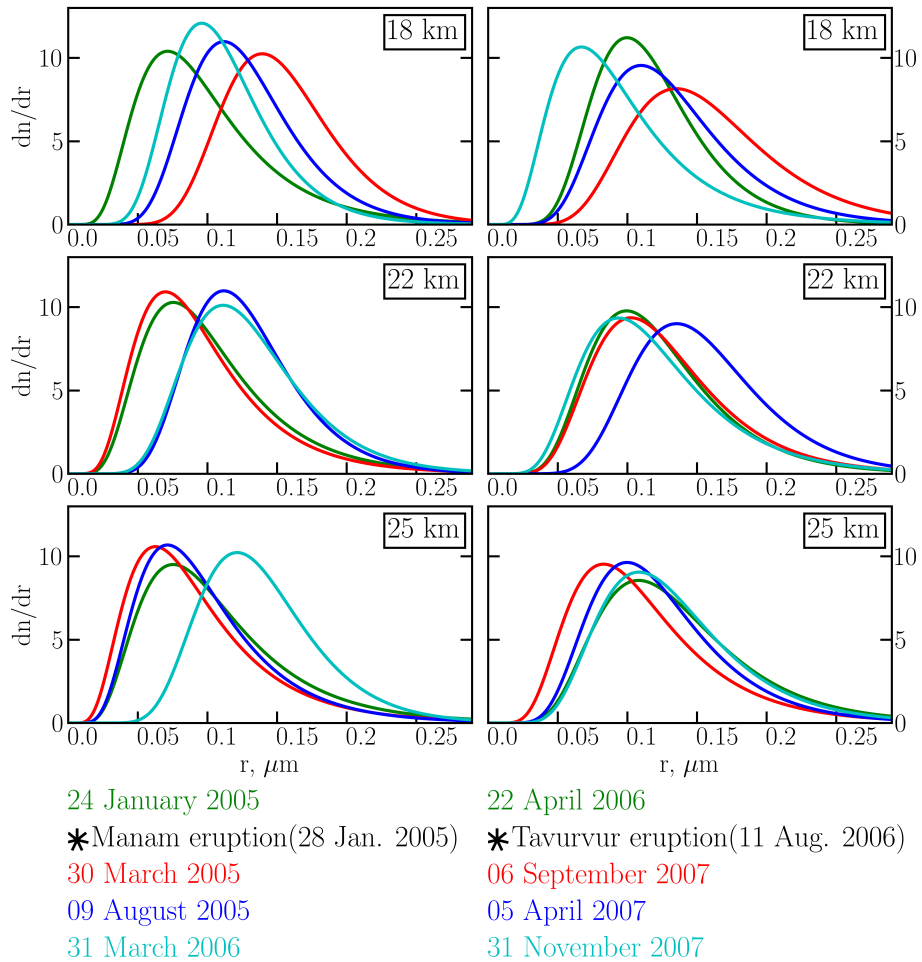


Figure 13. Evolution of the aerosol particle size distribution at different altitudes (18, 22, 25 km) after the Manam (left panels) and Tavurvur (right panels) eruptions.

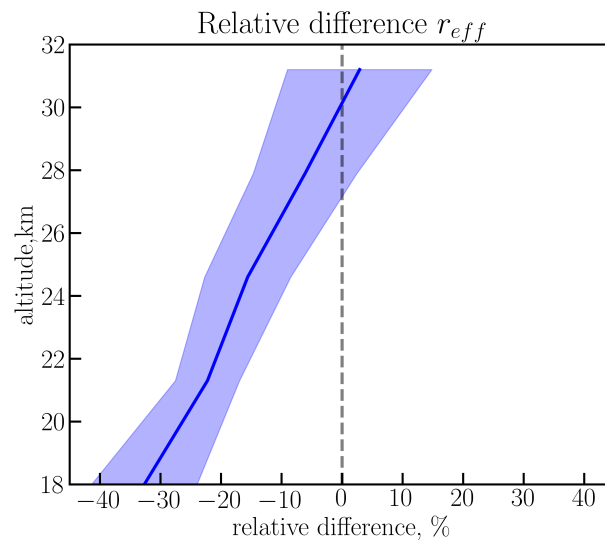


Figure 14. Mean relative difference $(\text{SCIAMACHY-SAGE II}) / \text{SAGE II}$ between effective radii from collocated SCIAMACHY and SAGE II measurements.

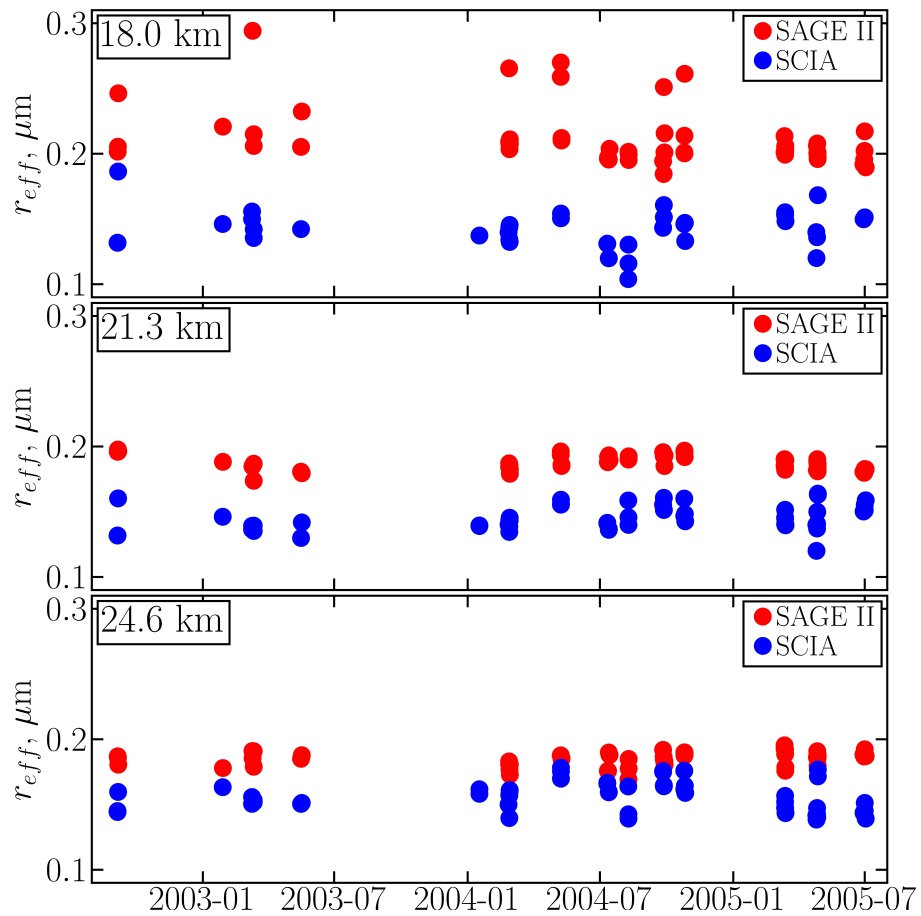


Figure 15. Effective radii from collocated SCIAMACHY and SAGE II measurements at 18, 21.3, 24.6 km altitude.