



1 Intercomparison of Open-Path Trace Gas Measurements with Two Dual Frequency Comb Spectrometers

2

3 Eleanor M. Waxman¹, Kevin C. Cossel¹, Gar-Wing Truong¹, Fabrizio R. Giorgetta¹, William C. Swann¹,

4 Sean Coburn², Robert J. Wright², Gregory B. Rieker², Ian Coddington¹ and Nathan R. Newbury¹

5 ¹Physical Measurement Laboratory, National Institute of Standards and Technology, 325 Broadway,

6 Boulder, CO 80305

7 ²Precision Laser Diagnostics Laboratory, University of Colorado Boulder, Boulder, CO 80309

8 Correspondence to: Eleanor Waxman

9 (eleanor.waxman@nist.gov)

10

11 Abstract

12 We present the first quantitative intercomparison between two open-path dual comb spectroscopy
13 (DCS) instruments which were operated across adjacent 2-km open-air paths over a two-week period.
14 We used DCS to measure the atmospheric absorption spectrum in the near infrared from 6021 to 6388
15 cm^{-1} (1565 to 1661 nm), corresponding to a 367 cm^{-1} bandwidth, at 0.0067 cm^{-1} sample spacing. The
16 measured absorption spectra agree with each other to within 5×10^{-4} without any external calibration of
17 either instrument. The absorption spectra are fit to retrieve concentrations for carbon dioxide (CO_2),
18 methane (CH_4), water (H_2O), and deuterated water (HDO). The retrieved dry mole fractions agree to
19 0.14% (0.57 ppm) for CO_2 , 0.35% (7 ppb) for CH_4 , and 0.40% (36 ppm) for H_2O over the two-week
20 measurement campaign, which included $23 \text{ }^\circ\text{C}$ outdoor temperature variations and periods of strong
21 atmospheric turbulence. This agreement is at least an order of magnitude better than conventional
22 active-source open-path instrument intercomparisons and is particularly relevant to future regional flux
23 measurements as it allows accurate comparisons of open-path DCS data across locations and time. We
24 additionally compare the open-path DCS retrievals to a WMO-calibrated cavity ringdown point sensor
25 located along the path with good agreement. Short-term and long-term differences between the two
26 systems are attributed, respectively, to spatial sampling discrepancies and to inaccuracies in the current
27 spectral database used to fit the DCS data. Finally, the two-week measurement campaign yields diurnal
28 cycles of CO_2 and CH_4 that are consistent with the presence of local sources of CO_2 and absence of local
29 sources of CH_4 .

30

31 Work of the U.S. Government and not subject to copyright.

32

33 1. Introduction

34 Quantitative determination of greenhouse gas fluxes over a variety of temporal and spatial
35 scales is necessary for characterizing source strength and intermittency and for future emissions
36 monitoring, reporting, and verification. To this end, techniques exist to measure greenhouse gas
37 concentrations on a variety of length scales, each of which has advantages and disadvantages. Point
38 sensors provide valuable information about local sources, but their use for continuous regional
39 measurements on sampling towers is complicated by local wind patterns, local sources, and mixing
40 within the planetary boundary layer (PBL), especially at night (Lauvaux et al., 2008; Ciais et al., 2010;
41 Lauvaux et al., 2012). Similarly, total-column measurements are particularly useful for sub-continental to
42 global scale measurements; however they are sensitive to atmospheric transport errors within the PBL
43 (Lauvaux and Davis, 2014), are affected by clouds and aerosols, are primarily limited to daytime
44 measurements, and lack either the revisit rates or mobility for regional flux measurements. Horizontal
45 integrated path measurements are complementary to point sensors and satellites: they cover spatial
46 scales from 1-10s of kilometers and provide measurements on the second to minute time scales with
47 portable instruments and are thus appropriate for regional studies. Active-source open-path sensors
48 such as open-path Fourier Transform Infrared spectroscopy (FTIR), differential optical absorption



49 spectroscopy (DOAS), differential LIDAR (DIAL), or tunable diode laser absorption spectroscopy (TDLAS)
50 are often used for these measurements and can retrieve path-averaged concentrations but typically
51 with 10% or greater uncertainties (EPA Handbook, and references therein). Recently, open-path dual-
52 comb spectroscopy (DCS) has emerged as a new technique that could potentially provide precise,
53 accurate continuous regional measurements of the mole fractions of CO₂, CH₄, H₂O, and HDO over
54 kilometer-scale open paths (Rieker et al., 2014), thereby providing a new open-path sensing capability
55 that falls between point sensing and total-column measurements.

56 Here we demonstrate that open-path DCS can indeed yield dry mole fractions over open-air
57 paths with a high level of intercomparability, over long periods of time, and with sufficient precision to
58 track variations in the ambient levels from local sources and sinks. Two completely independent open-
59 path DCS instruments are operated over neighboring open-air paths during a two-week measurement
60 campaign. Although both DCS instruments use fully stabilized frequency combs, they are portable
61 (Truong et al., 2016) and are operated nearly continuously during both day and night through laboratory
62 temperature variations from 17 to 25°C, strong atmospheric turbulence, and outdoor air temperature
63 variations from 4.6 to 28.9°C. The retrieved dry mole fractions for the two DCS instruments agree to
64 better than 0.57 ppm¹ (0.14 %) for CO₂ and 7.0 ppb (0.37 %) for CH₄. This agreement is achieved without
65 any “bias correction” or calibration of either instrument for absolute wavelength or for absolute
66 concentration. Instead, it is a direct consequence of the negligible instrument lineshape and precise
67 frequency calibration of the DCS instruments, which leads to measured atmospheric absorption spectra
68 that are identical to below 10⁻³ (limited by the instrument noise level). The measured path-averaged CO₂
69 precision over a 2-km path is 0.90 ppm in 30 seconds, improving to 0.24 ppm in 5 minutes. For CH₄, the
70 precision is 9.6 ppb in 30 seconds, improving to 2.1 ppb in 5 minutes. We also compare the DCS
71 retrievals to a WMO-calibrated, cavity ringdown point sensor located near the path. The agreement is
72 within 3.4 ppm and 17 ppb for CO₂ and CH₄ respectively, limited by differences in the sampling volume
73 and by the spectral database used to analyze the DCS transmission spectra.

74 Similar intercomparison measurements between conventional active, open-path sensors are
75 rare but have shown agreement of typically 1-20% (Thoma et al., 2005; Hak et al., 2005; Smith et al.,
76 2011; Shao et al., 2013; Conde et al., 2014; Reiche et al., 2014; Thalman et al., 2015). Here, we find
77 agreement between two DCS instruments that is an order of magnitude better and is comparable to
78 that achieved with highly-calibrated, state-of-the-art, solar-looking FTIRs that retrieve vertical column
79 measurements (Messerschmidt et al., 2011; Frey et al., 2015; Hedelius et al., 2016); however, open-path
80 DCS does not require instrument-specific calibrations (e.g. of the instrument line shape) and provides a
81 very different capability by retrieving the dry mole fractions across regional, kilometer-scale paths over
82 day and night in a mobile platform. Moreover, as the agreement between open-path DCS instruments is
83 below the level of natural background fluctuations, future measurements can facilitate accurate inverse
84 modeling to identify sources and sinks of carbon emission over regions. As an initial demonstration, we
85 discuss the observed diurnal variations from this two-week measurement campaign in the final section
86 of the paper.

87

88 2 Technique

89 2.1 Overview

90 DCS is based on a frequency comb laser source, which is a pulsed laser that outputs a spectrum
91 consisting of evenly-spaced, narrow modes (“comb teeth”) underneath a broad spectral envelope
92 (Cundiff and Ye, 2003; Hall, 2006; Hänsch, 2006). In DCS, two such frequency combs are used to
93 measure the atmospheric absorption on a comb-tooth-by-tooth basis across broad bandwidths

¹ In this work we use dry mole fraction. ppm is defined as micromoles of CO₂ per mole of dry air and ppb is defined as nanomoles of CH₄ per mole of dry air.



94 (Coddington et al., 2016; Ideguchi, 2017). As shown in Figure 1, two combs with nominal repetition
95 rates of f_r and offset by Δf_r are phase locked together, transmitted through a sample, and their
96 heterodyne signal measured on a photodetector. The resulting rf frequency comb can be mapped back
97 to the optical domain to generate an overall spectrum, as shown in Figure 1(b), that is the product of the
98 comb spectra and any atmospheric absorption. One important difference between DCS and other
99 broad-band laser techniques is that here all wavelengths are measured at once rather than sequentially
100 as would be the case for a swept laser system; as a result, DCS is much more immune to spectral
101 distortions from turbulence effects. Moreover, for a fully phase-locked comb, as is used here, the optical
102 frequency axis is stable and known to high accuracy, and the instrument lineshape is effectively the sum
103 of two delta-functions, as shown in the spectrum in Figure 1(b). Alternatively, DCS can be thought of as
104 high-resolution Fourier-transform spectroscopy with diffraction-limited light sources, no moving parts,
105 negligible instrument line shape, and a rapid scanning rate of $1/\Delta f_r$, which we tune to be faster than
106 turbulence-induced intensity variations. Here, both combs are transmitted over the open path yielding
107 the atmospheric absorption spectrum, but it is also possible to transmit only a single comb through the
108 air to measure both dispersion and absorbance (Giorgetta et al., 2015; Coddington et al., 2016).

109 Figure 2 provides an overview of our experiment. Two DCS instruments measured the
110 atmospheric absorption across a 2-km-roundtrip open path that extended from the top of a building at
111 the National Institute of Standards and Technology (NIST) Boulder campus to a pair of retroreflectors
112 located on a nearby hill. Both DCS instruments were based on a similar overall design and used self-
113 referenced, stabilized frequency combs (Sinclair et al., 2015), but one was built by a team at NIST and
114 the other by a team at the University of Colorado; they are hereafter referred to as DCS A and DCS B,
115 respectively. As outlined below, the two instruments differed in their exact design and physical
116 parameters. Nevertheless, no instrument-specific calibration or bias offset was applied to either system.
117 The acquired atmospheric absorption spectra were fit to retrieve the column density of CO_2 , CH_4 , and
118 H_2O (as well as HDO and $^{13}\text{CO}_2$ at lower precision) along with the path-averaged temperature from the
119 CO_2 spectrum. From these data, combined with the measured atmospheric pressure and the path length
120 (measured via time-of-flight laser ranging), we retrieved the path-averaged dry mole fractions as a
121 function of time, which are compared between DCS instruments and to a nearby cavity ringdown (CRDS)
122 point sensor.

123

124 2.2 Dual comb spectrometer

125 Figure 3(a) shows a simplified schematic of both DCS setups. Briefly, each DCS system used two
126 mutually coherent self-referenced erbium-doped fiber frequency combs based on the design of (Sinclair
127 et al., 2015) with nominal repetitions rates and Δf_r given in Table 1. Mutual optical coherence between
128 the combs is enforced by phase-locking an optical tooth of each to a common cw laser and the carrier-
129 envelope offset frequency of each to a common quartz microwave oscillator. Absolute frequency
130 accuracy is then enforced by a bootstrapped approach that effectively locks the common cw laser to the
131 same quartz microwave oscillator (Truong et al., 2016). The result is sub-Hz mutual coherence, ~ 120 -kHz
132 absolute linewidths, and $3.6 \times 10^{-5} \text{ cm}^{-1}$ absolute frequency accuracy (Truong et al., 2016). This linewidth
133 is orders of magnitude lower than the $\sim 5 \text{ GHz}$ or $\sim 0.2 \text{ cm}^{-1}$ width of pressure-broadened absorption
134 lines. The direct output of the combs is spectrally broadened in highly nonlinear fiber to cover 7140 -
135 5710 cm^{-1} (1.4 - $1.75 \mu\text{m}$) and then filtered to isolate the spectral region of interest from 6021 to 6388
136 cm^{-1} (1565 to 1661 nm).

137 The combined light from both combs is transmitted via single-mode fiber to a telescope, where
138 it is launched to a retroreflector. The returning signal is collected onto an amplified, 100 -MHz-
139 bandwidth InGaAs photodetector and digitized at f_r . We acquire a single interferogram at a period of
140 $1/\Delta f_r$ or 1.6 ms for DCS A; 100 such interferograms are directly summed in real time on a field-
141 programmable gate array (FPGA). These are transferred to a computer where they are carrier-phase



142 corrected and further summed over an acquisition time of ~ 30 seconds. These summed interferograms
143 are then Fourier transformed and scaled, using the known optical frequency comb tooth positions, to
144 generate a transmission spectrum (e.g. Figure 4a) spanning 367 cm^{-1} ($>10\text{ THz}$) with a point spacing of
145 0.0067 cm^{-1} .

146 The exact optical layout of DCS A is given in (Truong et al., 2016). While following the same
147 basic design, DCS B differs in several technical details. These include a slightly different output
148 spectrum, as well as slight different comb tooth spacings and offset frequency, minor differences in the
149 reference cw laser and its locking scheme, and different amplifier design, launched and received powers,
150 and telescope design. Some of these differences are laid out in Figure 3, Table 1, and Section 2.3 below.

151 We have found that the use of stabilized, phase coherent frequency combs is a necessary but
152 not sufficient prerequisite to reaching sub-percent agreement in retrieved gas concentrations. It is
153 critical that the spectrally-filtered comb output does not include stray unfiltered light. Similarly, any
154 stray reflections from the telescope that can “short circuit” the atmospheric path must be avoided. As
155 with FTIR systems, nonlinearities are problematic. In the optical domain, nonlinearities can arise when
156 the combs are combined in fiber with high optical power. These are minimized for DCS A by filtering the
157 light, which decreases the peak powers, before combining the combs. For DCS B the combs do not have
158 a booster amplifier and thus have significantly lower power. Nonlinearities in the photodetection can
159 also occur (Zolot et al., 2013); in laboratory tests with a CO reference cell, we verified no bias in
160 retrieved concentration as a function of received power up to $300\text{ }\mu\text{W}$, which is a factor of two higher
161 than the maximum power for the open path data. It was also critical to match the interferogram
162 amplitude to the full dynamic range of the analog-to-digital converters (ADCs) to avoid effective
163 nonlinearities in the digitization process.

164

165 2.3 Launch/Receive telescope

166 The two telescope systems are shown in Figure 3(a). Due to the large spectral bandwidth,
167 reflective optics are preferred to minimize chromatic dispersion. For DCS A, the launch/receive system
168 was based on a bi-directional off-axis parabolic telescope with a 3” aperture while for DCS B, it was
169 based on a 6”-aperture Ritchey-Chretien (RC) telescope with the light launched separately from behind
170 the secondary mirror. In both cases, the launched beam diameter was $\sim 40\text{ mm}$ and the light was
171 directed to a hollow corner-cube retroreflector of 2.5” (DCS A) or 5” (DCS B) diameter. A slow servo was
172 implemented for long-term pointing of the telescope to the retroreflectors. For this servo, a low-
173 divergence 850 nm LED is co-aligned with the telescope and its retro-reflected light is detected by a co-
174 aligned CMOS camera with a long focal-length lens and an 850-nm-bandpass optical filter. We then
175 servo the overall telescope pointing via its gimbal using the LED spot location on the camera. Further
176 servo details are described in Cossel et al. (2017).

177 Figure 3(b) shows the return power for both systems as a function of time. For reference, the
178 minimum return power required to obtain useful spectra was $\sim 15\text{ }\mu\text{W}$ (horizontal black line). At lower
179 powers, the acquired individual spectra are excluded. Turbulence-induced intensity variations are lower
180 for the RC-telescope than the off-axis parabolic telescope because of its larger aperture; however, the
181 long-term stability of the off-axis parabolic telescope was better due to a higher-quality gimbal system.
182 The collection efficiency of the 6” RC telescope system was about 10-20% in low to moderate turbulence
183 (C_n^2 of 10^{-14}). The collection efficiency of the off-axis parabolic telescope system was lower, at $\sim 2\text{-}4\%$ in
184 similar conditions, due to 1) the smaller collection aperture and 2) the 50:50 beam splitter, which causes
185 a factor of 4 loss. Attempts to replace the 50:50 splitter with a polarizing beam splitter and quarter-
186 wave plate combination increased the collection efficiency but introduced additional etalons across the
187 spectrum and for this reason was not used.

188

189 2.4 Data processing



190 The acquired transmission spectra are the product $S(\nu) = I_0(\nu) \times e^{-A(\nu)}$, where I_0 is the
191 geometric mean of the two individual comb spectra, $A(\nu)$ is the desired atmospheric absorbance, and ν
192 is the average optical frequency of the two participating comb teeth, (e.g. Fig. 1(b)). We fit the natural
193 logarithm of the transmission spectra, $-\ln[S(\nu)] = -\ln[I_0(\nu)] + A(\nu)$, where the first term is
194 represented by a piecewise polynomial and the second by an absorption spectrum calculated from a
195 spectral database with floated concentrations of $^{12}\text{CO}_2$, $^{13}\text{CO}_2$, $^{12}\text{CH}_4$, $^{13}\text{CH}_4$, H_2O , and HDO . For a spectral
196 database we use HITRAN 2008 (Rothman et al., 2009) and Voigt lineshapes as this generates a consistent
197 set of line parameters across our conditions and gases. The fit is performed in three steps: first, we fit
198 the polynomial (typically 7th order) over small windows (typically 100 GHz or 3.33 cm^{-1}) and include the
199 expected absorbance from relevant gas absorption lines. These polynomials are then stitched together
200 to generate the overall polynomial baseline, which is removed from the measured spectrum to
201 find $A(\nu)$. We then fit only the 30013 \leftarrow 00001 CO_2 band in order to retrieve the path-averaged
202 temperature. Finally, $A(\nu)$ is then re-fit over the entire spectral window by floating the gas
203 concentrations at the retrieved path-averaged temperature. The retrieved path-averaged
204 concentrations are converted to wet mole fractions by normalizing to the total number density of air
205 molecules, which is calculated from the fitted (or separately measured) air temperature combined with
206 the atmospheric pressure, as measured by a sensor co-located with the CRDS sensor and corrected for
207 the altitude difference. Finally, wet CO_2 , $^{13}\text{CO}_2$, and CH_4 are converted to dry values (X_{CO_2} , $X^{13}\text{CO}_2$, X_{CH_4})
208 using $X_{\text{S}} = S/(1 - X_{\text{H}_2\text{O}})$ where X_{S} is the dry species concentration, S is the retrieved wet species
209 concentration and $X_{\text{H}_2\text{O}}$ is the retrieved H_2O volume mole fraction.

211 3 Intercomparison Results and Discussion

212 3.1 Atmospheric spectrum comparison

213 Figure 4(a) shows the overall raw DCS transmission spectra from the two instruments averaged for a
214 three-hour period. They differ significantly because of the different comb intensity profiles, $I_0(\nu)$.
215 However, after the polynomial baseline fit discussed above is applied, the resulting 3-hour averaged
216 absorption spectra are nearly identical as shown in Figure 4(b). The inset of Figure 4(b) shows the data
217 sampling points (spaced at $\sim 200 \text{ MHz}$) across several absorption lines with width of $5 \text{ GHz } 0.2 \text{ cm}^{-1}$)
218 indicating we have sufficient optical resolution to over-sample the lines. The difference of the
219 absorption spectra, shown as the black line in Figure 4(c), has a standard deviation of 9×10^{-4} with no
220 observable structure at absorption lines. This difference is dominated by an etalon on the off-axis
221 telescope used with DCS A. After manually fitting out the etalon structure, DCS A and DCS B agree to
222 better than 5×10^{-4} (limited by the instrumental noise level) over the full spectral region (with the
223 exception of a 7 cm^{-1} section at 6290 cm^{-1}), and better than 2.5×10^{-4} over the region near 6100 cm^{-1}
224 where both DCS systems have significant returned optical power. This very high level of agreement
225 between the two spectra shows that there are no instrumental line shapes or detector nonlinearity
226 effects distorting the observed spectral line shapes; otherwise, structure would be observed in the
227 difference. Thus, the two DCS instruments measure the same comb-tooth-resolved atmospheric
228 absorbance spectrum.

229 Figure 4(d) shows the residuals after fitting the absorption lines in the DCS A spectrum to HITRAN
230 2008 and removing the etalon. The higher SNR of the DCS A yields an even lower broadband noise than
231 the difference spectrum, but there are clear residuals near spectral lines attributable to incorrect line
232 shapes/parameters in the HITRAN 2008 database. Nevertheless, the overall magnitude of the residuals
233 is very small in comparison to the spectral absorption.

234 235 3.2 Comparison of retrieved mole fractions from DCS A and DCS B

236 From the fitted concentrations, we retrieve the mole fractions as outlined in Section 2.4. The
237 retrieved time series for X_{CO_2} , $X^{13}\text{CO}_2$, X_{CH_4} , H_2O , and HDO are given in Figure 5 at ~ 30 second intervals.



238 Gaps in the data are due to either telescope misalignment (primarily on the 6" RC telescope due to the
239 lower-quality gimbal system) or, more rarely, a loss of phase lock of one of the four frequency combs.
240 Excellent agreement is observed between both systems for all retrieved concentrations. Figure 6 shows
241 the concentration differences, which exhibit a high-frequency white noise consistent with the
242 quadrature sum of the DCS precisions given in Section 3.3. In addition, the differences show a slow
243 wander about zero indicating slowly changing, small offsets between the two DCS instruments. CH₄ also
244 shows a small negative offset for the second week of the campaign. A Gaussian curve approximates the
245 distribution of the differences over the full two weeks reasonably well and is shown in Figure 7. At 32-
246 second averaging times, the mean and width of the distributions are $\Delta X_{\text{CO}_2} = 0.57 \pm 2.4$ ppm, ΔX_{CH_4}
247 $= -7.0 \pm 16$ ppb, $\Delta C_{\text{H}_2\text{O}} = 36 \pm 90$ ppm, and $\Delta C_{\text{HDO}} = 390 \pm 860$ ppm. These widths decrease to 1.5
248 ppm, 12 ppb, 66 ppm, and 480 ppm, respectively, for 5-minute averaging times. These mean values
249 correspond to a relative offset of 0.14 % CO₂, -0.35 % CH₄, and 0.4 % H₂O and are close to the WMO
250 compatibility standards of 0.1 ppm for CO₂ and 2 ppb for CH₄ (Tans and Zellweger, 2015). We emphasize
251 the agreement here is achieved over a two-week period despite outdoor temperature variations of 4.6
252 to 28.9 °C, DCS instrument ambient temperature variations from 17 to 25 °C, 10% to 90% relative
253 humidity fluctuations, and large turbulence-induced return power fluctuations.

254 Table 2 summarizes the systematic uncertainties of the DCS systems. The choice of spectral
255 model effectively sets the calibration that converts the measured absorbance spectrum to path-
256 averaged concentrations. The temperature primarily affects the conversion of the path-averaged
257 concentration to mole fractions (through the calculation of the overall air concentration). For the direct
258 intercomparison, both DCS data were analyzed with a common spectral model (HITRAN 2008) and
259 temperature in order to separate out instrument-specific systematics from the more fundamental
260 connection between absorption and concentration. Below we discuss these instrument-specific
261 systematics (given in the top part of Table 2). A discussion of the uncertainties from the spectral model
262 and temperature (given in the bottom part of Table 2) is given in Section 3.5.

263 To explore the source of the small systematic offsets between the DCS retrievals, we have
264 performed a number of control comparisons. In the processing, we have varied the initial concentration
265 guess in the fit with negligible effect. We have also varied the polynomial baseline fit by adjusting the
266 window size from 100 to 150 GHz and polynomial order from 7th to 9th order and again found negligible
267 variations of 0.02 % for CO₂ (<0.07 ppm), 0.07% for CH₄ (<1.4 ppb), and 0.05% (~4 ppm) for H₂O. In
268 laboratory tests, we verified that the two DCS instruments retrieve the same CO₂ concentrations to
269 within 0.04% for 8450 ppm of CO₂ in a 30-meter multipass cell (roughly mimicking the total absorption
270 over the open path). In open-path tests, we have separated effects of the detection/acquisition system
271 and optical system. First, the detected DCS A return signal was split to the two separate data acquisition
272 systems. The two processed signals yielded small differences of 0.16 ppm CO₂, 0.34 ppb CH₄, and 1.0
273 ppm H₂O, presumably due to residual nonlinearities and reflections in the rf system and digitization.
274 Second, the outgoing DCS A comb light was split and directed to the two different telescopes and
275 acquisition systems. These two processed signals yielded larger differences of 0.45 ppm CO₂, 1.5 ppb
276 CH₄, and 56 ppm H₂O, possibly due to scattered light or polarization dependences in the launch and
277 receive optical systems. Finally, residual phase noise between the two combs in a single DCS system can
278 cause small biases in the retrieved concentrations, but these should be well below 0.1% in this
279 configuration (Truong et al. 2017, in prep). All these instrument uncertainties are summarized in Table 2.

280

281 3.3 DCS precision

282 Figure 8 shows the precision versus averaging time (determined using the modified Allan
283 deviation) based on the scatter across a 6-hour period over which the CO₂ and CH₄ concentrations are
284 reasonably flat, shown as the highlighted part of Figure 5. (The Allan deviation for H₂O is not calculated
285 because the atmospheric H₂O concentration varies significantly over this time period.) Under perfectly



286 stable concentrations and white instrument noise, the precision should decrease as the square root of
287 averaging time, indicated as a grey line in Figure 8. Initially, the Allan deviations do follow this slope, but
288 the atmospheric concentrations, especially of CO₂, vary over this 6-hour period and the Allan deviations
289 reach a floor at ~ 1000 s.

290 The precision at 30-second and 5-minute averaging time is given at the bottom of Table 1. DCS
291 A has superior CO₂ precision because it has higher received optical comb power in that spectral region,
292 whereas the DCS instruments have similar received power in the CH₄ spectral region and therefore
293 similar CH₄ precisions. Regardless, the precision of either instrument is sufficiently high to measure the
294 characteristic atmospheric fluctuations of these gases on tens-of-seconds timescales.

295

296 3.4 Comparison of open-path DCS to a cavity ringdown point sensor (CRDS)

297 A commercial cavity-ringdown point sensor, Picarro Model 1301² (Crosson, 2008), was also located
298 along the path as shown in Figure 2. Its inlet was 30 m above ground on a radio tower, approximately
299 160 m perpendicular to the DCS beam path. Figure 9 compares the DCS A and CRDS (smoothed to 32-s
300 resolution) time series. In general, their overall shapes agree well with both systems tracking ~40 ppm
301 variations in XCO₂, 200 ppb variations in XCH₄, and 1% variations in H₂O over days. Nevertheless, there
302 are clear discrepancies in terms of both short-duration spikes and a long-term overall offset between
303 the DCS and CRDS time series.

304 The short-duration spikes are present in the CRDS time series and presumably arise from the very
305 different spatial sampling of the two instruments. The DCS system measures the integrated column over
306 one kilometer (one way), while the CRDS is a point sensor and therefore much more sensitive to local
307 sources. For example, a 1 m³ volume of air containing 500 ppm of CO₂ from a vehicle driving under the
308 sampling line will result in a sharp spike in the CRDS data as the air mass passes the sampling inlet.
309 However, that same air mass will result in only a 0.025% or 0.1 ppm increase in the DCS path-averaged
310 concentration (assuming a 400 ppm background). These spikes in the CRDS time series are damped here
311 by the 32-second smoothing but are occasionally evident especially during the second week. The general
312 scarcity of such events does suggest that the air over the open path is usually fairly well mixed.

313 The long-term overall offset between the CRDS and DCS data is a consequence of their very different
314 calibrations. The CRDS is tied to the WMO scale for CO₂ and CH₄ by directly injecting known dry WMO-
315 calibrated CO₂/CH₄ mixtures at different trace gas concentrations and different water vapor
316 concentrations into its temperature- and pressure-controlled sampling cavity. This instrument was
317 calibrated shortly after the measurement campaign and should thus have an absolute uncertainty close
318 to that of the WMO-scale uncertainties of ~ 0.07 ppm for CO₂ (Zhao and Tans, 2006) and ~1.5 ppb for
319 CH₄ (Dlugokencky et al., 2005). In contrast, the DCS has no instrument-specific calibration but relies
320 completely on a fit to a spectral database to extract the gas concentrations from the measured
321 absorbance across a wide range of ambient pressures and temperatures. Here, we use HITRAN 2008
322 which has ¹²CO₂ linestrength uncertainties of 1-2 %, ¹²CH₄ linestrength uncertainties of 10-20%, and
323 H₂¹⁶O linestrength uncertainties of 5-10% (Rothman et al., 2009), leading to a poorer absolute
324 calibration than the WMO-calibrated point sensor. From the data in Figure 9, the differences between
325 the CRDS and DCS data across the two-week period are -3.4 ± 3.4 ppm CO₂, 17 ± 15 ppb CH₄, and 580 ±
326 462 ppm H₂O at 5-minute averaging. These correspond to relative offsets of -0.85% for CO₂, 0.94% for
327 CH₄, and 6.9% for H₂O, well within the stated uncertainties of HITRAN 2008. In previous DCS
328 measurements, we found slightly different offsets, specifically 1.78% for CO₂, 0.20% for CH₄, and 1.74%
329 for H₂O in (Rieker et al., 2014) and ~1 % for CO₂ in (Giorgetta et al., 2015). However, these previous data

² The use of trade names is necessary to specify the experimental results and does not imply endorsement by the National Institute of Standards and Technology.



330 covered much shorter timespans, used an older CRDS point sensor calibration, and may have included
331 small systematic offsets in the DCS systems due to technical issues discussed in Section 3.2.

332 This basic discrepancy between retrievals based on lineshape parameters from a spectral database
333 and manometric calibrations (WMO standard) is not unique to DCS. Several studies have calibrated the
334 Total Carbon Column Observing Network (TCCON) retrievals against WMO-based instruments (Wunch et
335 al., 2010; Messerschmidt et al., 2011; Geibel et al., 2012; Tanaka et al., 2012). Although TCCON is not a
336 solely HITRAN-based analysis (Wunch et al., 2011), a correction factor of 0.9898 for CO₂, 0.9765 for CH₄,
337 and 1.0183 for H₂O (Wunch et al., 2010) is needed to bring the overall TCCON retrievals into agreement
338 with the WMO-based data. Additionally, theoretical calculations by (Zak et al., 2016) found an
339 approximately 0.5% difference between CO₂ line parameters from HITRAN 2012 and their density
340 functional theory calculations and an additional 0.5% difference between the calculations and new
341 measurements by (Devi et al., 2016) in the 1.6-micron region. Certainly this discrepancy between
342 retrievals from HITRAN and WMO-calibrated instruments is not fundamental and further experimental
343 work should lead to improved spectral database parameters and much better agreement. As noted in
344 earlier work on CO₂, it will be important to establish both the correct linestrengths as well as account for
345 complex lineshapes and line mixing (e.g. Devi et al., 2007; Thompson et al., 2012; Bui et al., 2014; Long
346 et al., 2015; Devi et al., 2016). A direct comparison of the open-path DCS spectra acquired here and
347 laboratory DCS spectra acquired for WMO-calibrated gas samples can contribute to these future
348 improvements and is planned. Finally, we emphasize that because the DCS instruments record the
349 atmospheric absorption without instrument distortions, as spectral models improve, past open-path
350 spectra can be refit with reduced uncertainty.

351 An accurate path-averaged air temperature is also important to avoid systematic offsets. Unlike
352 vertical total-column measurements through the entire atmosphere, km-scale open horizontal paths
353 should have relatively low temperature inhomogeneities of around a few degrees C, and thus the use of
354 a single “path averaged” temperature in the fit is sufficient for accurate retrievals. We verified this
355 through a sensitivity study comparing retrievals for simulated spectra with temperature gradients up to
356 10 °C over the path; the resulting bias was below 0.03 ppm CO₂ (0.007%) and 0.4 ppb CH₄ (0.022%), as
357 shown in Table 2. On the other hand, any error in the path-averaged temperature can bias the mole
358 fractions through two effects. First, the retrieved path-averaged concentration will vary weakly with
359 temperature because of temperature-dependent line parameters. Second and dominantly, the final
360 mole fraction calculation requires normalization by the air density. Here, this density is calculated from
361 the ideal gas law using the measured air pressure and path-averaged temperature. Therefore, a
362 fractional error in temperature leads to a corresponding fractional error in mole fraction. For example, a
363 0.15% uncertainty in mole fraction requires 0.5 °C uncertainty in the path-averaged air temperature.
364 (See Table 2.) We verified that this simple linear relationship is valid up to a temperature uncertainty of
365 10 °C in a sensitivity study. From the discussion in Appendix A, the use of a point temperature sensor
366 near the end of the open path is clearly insufficient to achieve <0.5 °C uncertainty at many times of the
367 day. Instead, for the data here, we have used the fitted path-averaged temperature, as discussed in
368 Section 2.4. The approach effectively relies on the spectral database but, in this case, on the variation in
369 the Boltzmann distribution of the J-level population with temperature. In Table 2, we have taken a
370 hopefully conservative uncertainty of 0.5 °C for the path-averaged temperature, but more work is
371 needed to establish the true uncertainty from these retrieved values. Finally, we note the fractional
372 uncertainty in the measured atmospheric pressure from the sensor or altitude-based pressure changes
373 across the optical path was below 0.36%.

374
375 4. Diurnal cycles and source analysis

376 The two weeks of open path data are analyzed for diurnal cycles, as shown in Figure 10 with the intent
377 of an initial understanding of CO₂ and CH₄ sources. For this analysis, the wind speed and wind direction



378 were taken from the NCAR Mesa weather data (<ftp://ftp.eol.ucar.edu/pub/archive/weather/mesa/>),
379 while the gas concentrations are from DCS A.

380

381 4.1 Carbon dioxide

382 As expected, the median of the diurnal cycle for CO₂ shows a peak in the early to mid-morning
383 from commuter traffic after which the CO₂ concentration decreases as the boundary layer rises. It
384 remains approximately steady throughout the afternoon, decreases to a minimum between 19:00 and
385 20:00, and then increases slightly overnight as the boundary layer collapses. We hypothesize that the
386 afternoon behavior is due to the change in wind direction. Often overnight and through early morning
387 the wind blows from the west to southwest, which brings in cleaner background air from the mountains
388 bordering Boulder. However, in late morning the predominant wind direction shifts to the east and
389 southeast, possibly bringing in higher CO₂ concentrations from the Denver metropolitan area – which
390 lies approximately 30 km to the southeast of Boulder – over the course of the afternoon. Typically, the
391 evening wind shifts back to out of the west, once again bringing in the cleaner mountain air and with it a
392 decrease in CO₂ concentration.

393

394 4.2 Methane

395 Methane has a significantly weaker diurnal cycle than carbon dioxide, which is consistent with a
396 species that lacks significant diurnally-varying local sources. Rather, its concentration follows expected
397 variations in the boundary layer height; the concentration increases overnight into the early morning as
398 the boundary layer collapses, and then decreases during the late morning through afternoon as the
399 boundary layer rises again. The largest likely methane source near Boulder is local oil/gas fields, but
400 these typically lie to the northeast, while the wind directions are generally out of the west to southeast.
401 It is also possible that the methane comes from leaking natural gas infrastructure within the city.

402

403 5 Conclusions

404 Here we provide the first quantitative comparison of open-path dual comb spectroscopy
405 instruments. The dual-comb spectrometers were based on fully phase-coherent and stabilized fiber
406 frequency combs and operated nearly continuously over a two-week period. We performed these
407 measurements over adjacent 2-kilometer round-trip paths to measure concentrations of dry CO₂, dry
408 CH₄, H₂O, and HDO. The measured atmospheric absorbance spectra agree to better than 10⁻³.
409 Correspondingly, we find excellent agreement between the retrieved concentrations from the two
410 instruments without the need for instrument calibration: over two weeks of near-continuous
411 measurements, the retrieved CO₂ concentrations agree to better than 0.14% (0.57 ppm), CH₄
412 concentrations agrees to better than 0.35% (7.0 ppb), and H₂O concentrations agrees to better than
413 0.4% (36 ppm). These values are very close to the WMO compatibility goals. The remaining
414 disagreement is likely due to scattered stray light, polarization dependencies, and residual comb phase
415 noise. We further compare the DCS measurements to a cavity ringdown point sensor located along our
416 path. The measured dry CO₂ mole fraction agrees to within 1%, the CH₄ dry mole fraction to within
417 1.2%, and H₂O mole fraction to within 6.2%. However, this CRDS point sensor is directly calibrated to
418 the WMO scale for CO₂ and CH₄ while the DCS results are based on HITRAN 2008; we attribute the
419 disagreement in CO₂ and CH₄ to inaccurate line parameters in the HITRAN database. (Most of the water
420 discrepancy is attributed to the imperfect absolute water calibration of the CRDS point sensor.) Further
421 improvements to the spectral database should reduce these discrepancies. Finally, this open-path DCS
422 can exploit even broader spectrum combs up to 2.3 μm and down to 1.1 μm (Zolot et al., 2012; Okubo et
423 al., 2015), which would enable measurements of similar quality for ¹³CO₂, NH₃, N₂O, and O₂. These
424 results make open-path DCS a promising new system for greenhouse gas flux measurements from
425 distributed sources.



426

427 The authors declare that they have no conflict of interest.

428

429 Acknowledgements: We thank T. Newburger and K. McKain for assistance with the CRDS calibrations, T.
430 Bullet and J. Kofler for assistance in setting up the CRDS sampling, and R. Thalman for detailed long-path
431 instrument correlation data, and A.J. Fleischer and A. Karion for assistance with the manuscript. This
432 work was funded by the Defense Advanced Research Program Agency DSO SCOUT program, ARPA-E
433 MONITOR program under Award Number DE-AR0000539, and the NIST Greenhouse Gas and Climate
434 Science Initiative. EMW and KCC are supported by National Research Council postdoctoral fellowships.

435

436 References

437

438 Bui, T. Q., Long, D. A., Cygan, A., Sironneau, V. T., Hogan, D. W., Rupasinghe, P. M., Ciuryło, R., Lisak, D.
439 and Okumura, M.: Observations of Dicke narrowing and speed dependence in air-broadened CO₂
440 lineshapes near 2.06 μm, *J. Chem. Phys.*, 141(17), 174301, doi:10.1063/1.4900502, 2014.

441 Ciais, P., Rayner, P., Chevallier, F., Bousquet, P., Logan, M., Peylin, P. and Ramonet, M.: Atmospheric
442 inversions for estimating CO₂ fluxes: methods and perspectives, *Clim. Change*, 103(1–2), 69–92,
443 doi:10.1007/s10584-010-9909-3, 2010.

444 Coddington, I., Swann, W. C. and Newbury, N. R.: Coherent multiheterodyne spectroscopy using
445 stabilized optical frequency combs, *Phys. Rev. Lett.*, 100(1), 013902,
446 doi:10.1103/PhysRevLett.100.013902, 2008.

447 Coddington, I., Newbury, N. and Swann, W.: Dual-comb spectroscopy, *Optica*, 3(4), 414,
448 doi:10.1364/OPTICA.3.000414, 2016.

449 Conde, V., Robidoux, P., Avard, G., Galle, B., Aiuppa, A., Muñoz, A. and Giudice, G.: Measurements of
450 volcanic SO₂ and CO₂ fluxes by combined DOAS, Multi-GAS and FTIR observations: a case study from
451 Turrialba and Telica volcanoes, *Int. J. Earth Sci.*, 103(8), 2335–2347, doi:10.1007/s00531-014-1040-7,
452 2014.

453 Crosson, E. R.: A cavity ring-down analyzer for measuring atmospheric levels of methane, carbon
454 dioxide, and water vapor, *Appl. Phys. B*, 92(3), 403–408, doi:10.1007/s00340-008-3135-y, 2008.

455 Devi, V. M., Benner, D. C., Brown, L. R., Miller, C. E. and Toth, R. A.: Line mixing and speed dependence in
456 CO₂ at 6227.9 cm⁻¹: Constrained multispectrum analysis of intensities and line shapes in the
457 30013 ← 00001 band, *J. Mol. Spectrosc.*, 245(1), 52–80, doi:10.1016/j.jms.2007.05.015, 2007.

458 Devi, V. M., Benner, D. C., Sung, K., Brown, L. R., Crawford, T. J., Miller, C. E., Drouin, B. J., Payne, V. H.,
459 Yu, S., Smith, M. A. H., Mantz, A. W. and Gamache, R. R.: Line parameters including temperature
460 dependences of self- and air-broadened line shapes of 12C16O₂: 1.6-μm region, *J. Quant. Spectrosc.*
461 *Radiat. Transf.*, 177, 117–144, doi:10.1016/j.jqsrt.2015.12.020, 2016.

462 Dlugokencky, E. J., Myers, R. C., Lang, P. M., Masarie, K. A., Crotwell, A. M., Thoning, K. W., Hall, B. D.,
463 Elkins, J. W. and Steele, L. P.: Conversion of NOAA atmospheric dry air CH₄ mole fractions to a
464 gravimetrically prepared standard scale, *J. Geophys. Res. Atmospheres*, 110(D18), D18306,
465 doi:10.1029/2005JD006035, 2005.



- 466 EPA: EPA Handbook: Optical Remote Sensing for Measurement and Monitoring of Emissions, [online]
467 Available from: <https://www3.epa.gov/ttn/emc/guid/nd/gd-052.pdf> (Accessed 2 March 2017), n.d.
- 468 Frey, M., Hase, F., Blumenstock, T., Groß, J., Kiel, M., Mengistu Tsidu, G., Schäfer, K., Sha, M. K. and
469 Orphal, J.: Calibration and instrumental line shape characterization of a set of portable FTIR
470 spectrometers for detecting greenhouse gas emissions, *Atmos Meas Tech*, 8(7), 3047–3057,
471 doi:10.5194/amt-8-3047-2015, 2015.
- 472 Geibel, M. C., Messerschmidt, J., Gerbig, C., Blumenstock, T., Chen, H., Hase, F., Kolle, O., Lavrič, J. V.,
473 Notholt, J., Palm, M., Rettinger, M., Schmidt, M., Sussmann, R., Warneke, T. and Feist, D. G.: Calibration
474 of column-averaged CH₄ over European TCCON FTS sites with airborne in-situ measurements, *Atmos
475 Chem Phys*, 12(18), 8763–8775, doi:10.5194/acp-12-8763-2012, 2012.
- 476 Giorgetta, F. R., Rieker, G. B., Baumann, E., Swann, W. C., Sinclair, L. C., Kofler, J., Coddington, I. and
477 Newbury, N. R.: Broadband Phase Spectroscopy over Turbulent Air Paths, *Phys. Rev. Lett.*, 115(10),
478 103901, doi:10.1103/PhysRevLett.115.103901, 2015.
- 479 Hak, C., Pundt, I., Trick, S., Kern, C., Platt, U., Dommen, J., Ordóñez, C., Prévôt, A. S. H., Junkermann, W.,
480 Astorga-Lloréns, C. and others: Intercomparison of four different in-situ techniques for ambient
481 formaldehyde measurements in urban air, *Atmospheric Chem. Phys.*, 5(11), 2881–2900, 2005.
- 482 Hedelius, J. K., Viatte, C., Wunch, D., Roehl, C. M., Toon, G. C., Chen, J., Jones, T., Wofsy, S. C., Franklin, J.
483 E., Parker, H., Dubey, M. K. and Wennberg, P. O.: Assessment of errors and biases in retrievals of XCO₂,
484 XCH₄, XCO, and XN₂O from a 0.5 cm⁻¹ resolution solar-viewing spectrometer, *Atmos Meas Tech*, 9(8),
485 3527–3546, doi:10.5194/amt-9-3527-2016, 2016.
- 486 Lauvaux, T. and Davis, K. J.: Planetary boundary layer errors in mesoscale inversions of column-
487 integrated CO₂ measurements, *J. Geophys. Res. Atmospheres*, 119(2), 490–508,
488 doi:10.1002/2013JD020175, 2014.
- 489 Lauvaux, T., Uliasz, M., Sarrat, C., Chevallier, F., Bousquet, P., Lac, C., Davis, K. J., Ciais, P., Denning, A. S.
490 and Rayner, P. J.: Mesoscale inversion: first results from the CERES campaign with synthetic data, *Atmos
491 Chem Phys*, 8(13), 3459–3471, doi:10.5194/acp-8-3459-2008, 2008.
- 492 Lauvaux, T., Schuh, A. E., Bocquet, M., Wu, L., Richardson, S., Miles, N. and Davis, K. J.: Network design
493 for mesoscale inversions of CO₂ sources and sinks, *Tellus B*, 64(0), doi:10.3402/tellusb.v64i0.17980,
494 2012.
- 495 Long, D. A., Wójtewicz, S., Miller, C. E. and Hodges, J. T.: Frequency-agile, rapid scanning cavity ring-
496 down spectroscopy (FARS-CRDS) measurements of the (30012)←(00001) near-infrared carbon dioxide
497 band, *J. Quant. Spectrosc. Radiat. Transf.*, 161, 35–40, doi:10.1016/j.jqsrt.2015.03.031, 2015.
- 498 Messerschmidt, J., Geibel, M. C., Blumenstock, T., Chen, H., Deutscher, N. M., Engel, A., Feist, D. G.,
499 Gerbig, C., Gisi, M., Hase, F., Katrynski, K., Kolle, O., Lavrič, J. V., Notholt, J., Palm, M., Ramonet, M.,
500 Rettinger, M., Schmidt, M., Sussmann, R., Toon, G. C., Truong, F., Warneke, T., Wennberg, P. O., Wunch,
501 D. and Xueref-Remy, I.: Calibration of TCCON column-averaged CO₂: the first aircraft campaign over
502 European TCCON sites, *Atmos Chem Phys*, 11(21), 10765–10777, doi:10.5194/acp-11-10765-2011, 2011.



- 503 Okubo, S., Iwakuni, K., Inaba, H., Hosaka, K., Onae, A., Sasada, H. and Hong, F.-L.: Ultra-broadband dual-
504 comb spectroscopy across 1.0–1.9 μm , *Appl. Phys. Express*, 8(8), 082402, doi:10.7567/APEX.8.082402,
505 2015.
- 506 Reiche, N., Westerkamp, T., Lau, S., Borsdorf, H., Dietrich, P. and Schütze, C.: Comparative study to
507 evaluate three ground-based optical remote sensing techniques under field conditions by a gas tracer
508 experiment, *Environ. Earth Sci.*, 72(5), 1435–1441, doi:10.1007/s12665-014-3312-8, 2014.
- 509 Rieker, G. B., Giorgetta, F. R., Swann, W. C., Kofler, J., Zolot, A. M., Sinclair, L. C., Baumann, E., Cromer,
510 C., Petron, G., Sweeney, C., Tans, P. P., Coddington, I. and Newbury, N. R.: Frequency-comb-based
511 remote sensing of greenhouse gases over kilometer air paths, *Optica*, 1(5), 290–298,
512 doi:10.1364/OPTICA.1.000290, 2014.
- 513 Rothman, L. S., Gordon, I. E., Barbe, A., Benner, D. C., Bernath, P. E., Birk, M., Boudon, V., Brown, L. R.,
514 Campargue, A., Champion, J. P., Chance, K., Coudert, L. H., Dana, V., Devi, V. M., Fally, S., Flaud, J. M.,
515 Gamache, R. R., Goldman, A., Jacquemart, D., Kleiner, I., Lacome, N., Lafferty, W. J., Mandin, J. Y.,
516 Massie, S. T., Mikhailenko, S. N., Miller, C. E., Moazzen-Ahmadi, N., Naumenko, O. V., Nikitin, A. V.,
517 Orphal, J., Perevalov, V. I., Perrin, A., Predoi-Cross, A., Rinsland, C. P., Rotger, M., Simeckova, M., Smith,
518 M. A. H., Sung, K., Tashkun, S. A., Tennyson, J., Toth, R. A., Vandaele, A. C. and Vander Auwera, J.: The
519 HITRAN 2008 molecular spectroscopic database, *J. Quant. Spectrosc. Radiat. Transf.*, 110(9–10), 533–
520 572, doi:10.1016/j.jqsrt.2009.02.013, 2009.
- 521 Shao, L., Wang, W., Griffiths, P. R. and Leytem, A. B.: Increasing the Quantitative Credibility of Open-Path
522 Fourier Transform Infrared (FT-IR) Spectroscopic Data, with Focus on Several Properties of the
523 Background Spectrum, *Appl. Spectrosc.*, 67(3), 335–341, doi:10.1366/12-06901, 2013.
- 524 Sinclair, L. C., Deschênes, J.-D., Sonderhouse, L., Swann, W. C., Khader, I. H., Baumann, E., Newbury, N. R.
525 and Coddington, I.: Invited Article: A compact optically coherent fiber frequency comb, *Rev. Sci.
526 Instrum.*, 86(8), 081301, doi:10.1063/1.4928163, 2015.
- 527 Smith, T. E. L., Wooster, M. J., Tattaris, M. and Griffith, D. W. T.: Absolute accuracy and sensitivity
528 analysis of OP-FTIR retrievals of CO_2 , CH_4 and CO over concentrations representative of “clean air” and
529 “polluted plumes,” *Atmos Meas Tech*, 4(1), 97–116, doi:10.5194/amt-4-97-2011, 2011.
- 530 Tanaka, T., Miyamoto, Y., Morino, I., Machida, T., Nagahama, T., Sawa, Y., Matsueda, H., Wunch, D.,
531 Kawakami, S. and Uchino, O.: Aircraft measurements of carbon dioxide and methane for the calibration
532 of ground-based high-resolution Fourier Transform Spectrometers and a comparison to GOSAT data
533 measured over Tsukuba and Moshiri, *Atmos Meas Tech*, 5(8), 2003–2012, doi:10.5194/amt-5-2003-
534 2012, 2012.
- 535 Tans, P. and Zellweger, C.: 18th WMO/IAEA Meeting on Carbon Dioxide, Other Greenhouse Gases and
536 Related Tracers Measurement Techniques, GAW, La Jolla, CA, USA. [online] Available from:
537 http://www.wmo.int/pages/prog/arep/gaw/documents/FINAL_GAW_REPORT_229.pdf (Accessed 8
538 February 2017), 2015.
- 539 Thalman, R., Baeza-Romero, M. T., Ball, S. M., Borrás, E., Daniels, M. J. S., Goodall, I. C. A., Henry, S. B.,
540 Karl, T., Keutsch, F. N., Kim, S., Mak, J., Monks, P. S., Muñoz, A., Orlando, J., Peppe, S., Rickard, A. R.,
541 Ródenas, M., Sánchez, P., Seco, R., Su, L., Tyndall, G., Vázquez, M., Vera, T., Waxman, E. and Volkamer,



- 542 R.: Instrument intercomparison of glyoxal, methyl glyoxal and NO₂ under simulated atmospheric
543 conditions, *Atmos Meas Tech*, 8(4), 1835–1862, doi:10.5194/amt-8-1835-2015, 2015.
- 544 Thoma, E. D., Shores, R. C., Thompson, E. L., Harris, D. B., Thorneloe, S. A., Varma, R. M., Hashmonay, R.
545 A., Modrak, M. T., Natschke, D. F. and Gamble, H. A.: Open-Path Tunable Diode Laser Absorption
546 Spectroscopy for Acquisition of Fugitive Emission Flux Data, *J. Air Waste Manag. Assoc.*, 55(5), 658–668,
547 doi:10.1080/10473289.2005.10464654, 2005.
- 548 Thompson, D. R., Chris Benner, D., Brown, L. R., Crisp, D., Malathy Devi, V., Jiang, Y., Natraj, V., Oyafuso,
549 F., Sung, K., Wunch, D., Castaño, R. and Miller, C. E.: Atmospheric validation of high accuracy CO₂
550 absorption coefficients for the OCO-2 mission, *J. Quant. Spectrosc. Radiat. Transf.*, 113(17), 2265–2276,
551 doi:10.1016/j.jqsrt.2012.05.021, 2012.
- 552 Truong, G.-W., Waxman, E. M., Cossel, K. C., Baumann, E., Klose, A., Giorgetta, F. R., Swann, W. C.,
553 Newbury, N. R. and Coddington, I.: Accurate frequency referencing for fieldable dual-comb
554 spectroscopy, *Opt. Express*, 24(26), 30495, doi:10.1364/OE.24.030495, 2016.
- 555 Wunch, D., Toon, G. C., Wennberg, P. O., Wofsy, S. C., Stephens, B. B., Fischer, M. L., Uchino, O., Abshire,
556 J. B., Bernath, P., Biraud, S. C., Blavier, J.-F. L., Boone, C., Bowman, K. P., Browell, E. V., Campos, T.,
557 Connor, B. J., Daube, B. C., Deutscher, N. M., Diao, M., Elkins, J. W., Gerbig, C., Gottlieb, E., Griffith, D. W.
558 T., Hurst, D. F., Jiménez, R., Keppel-Aleks, G., Kort, E. A., Macatangay, R., Machida, T., Matsueda, H.,
559 Moore, F., Morino, I., Park, S., Robinson, J., Roehl, C. M., Sawa, Y., Sherlock, V., Sweeney, C., Tanaka, T.
560 and Zondlo, M. A.: Calibration of the Total Carbon Column Observing Network using aircraft profile data,
561 *Atmos Meas Tech*, 3(5), 1351–1362, doi:10.5194/amt-3-1351-2010, 2010.
- 562 Wunch, D., Toon, G. C., Blavier, J.-F. L., Washenfelder, R. A., Notholt, J., Connor, B. J., Griffith, D. W. T.,
563 Sherlock, V. and Wennberg, P. O.: The Total Carbon Column Observing Network, *Philos. Trans. R. Soc.*
564 *Math. Phys. Eng. Sci.*, 369(1943), 2087–2112, doi:10.1098/rsta.2010.0240, 2011.
- 565 Zak, E., Tennyson, J., Polyansky, O. L., Lodi, L., Zobov, N. F., Tashkun, S. A. and Perevalov, V. I.: A room
566 temperature CO₂ line list with ab initio computed intensities, *J. Quant. Spectrosc. Radiat. Transf.*, 177,
567 31–42, doi:10.1016/j.jqsrt.2015.12.022, 2016.
- 568 Zhao, C. L. and Tans, P. P.: Estimating uncertainty of the WMO mole fraction scale for carbon dioxide in
569 air, *J. Geophys. Res. Atmospheres*, 111(D8), D08S09, doi:10.1029/2005JD006003, 2006.
- 570 Zolot, A. M., Giorgetta, F. R., Baumann, E., Nicholson, J. W., Swann, W. C., Coddington, I. and Newbury,
571 N. R.: Direct-comb molecular spectroscopy with accurate, resolved comb teeth over 43 THz, *Opt. Lett.*,
572 37(4), 638–640, doi:10.1364/OL.37.000638, 2012.
- 573 Zolot, A. M., Giorgetta, F. R., Baumann, E., Swann, W. C., Coddington, I. and Newbury, N. R.: Broad-band
574 frequency references in the near-infrared: Accurate dual comb spectroscopy of methane and acetylene,
575 *J. Quant. Spectrosc. Radiat. Transf.*, 118, 26–39, doi:10.1016/j.jqsrt.2012.11.024, 2013.
- 576
577



	DCS A	DCS B
Design Details		
Comb 1 repetition rate (f_r)	~200 MHz	~204 MHz
Difference in repetition rate (Δf_r)	624 Hz	870 Hz
Spectral filtering	Before combining combs	After combining combs
Booster amplifier	Yes	No
Average power launched	4 mW	1.5 mW
Filtered spectral output	6376 to 6023 cm^{-1}	6359 to 6003 cm^{-1}
Telescope design	Home-built 3"-diameter off-axis telescope	Modified commercial 6"-diameter Ritchey-Chretien telescope
Retroreflector	2.5" HCC, 5 arc seconds	5" HCC, 5 arc seconds
Round-trip path length	1950.17 m	1963.67 m
Typical averaging time	32 s	28 s
Performance Metrics		
30-second precision	0.90 ppm CO_2 , 9.6 ppb CH_4	2.15 ppm CO_2 , 11.5 ppb CH_4
5-minute precision	0.24 ppm CO_2 , 2.1 ppb CH_4	0.60 ppm CO_2 , 3.2 ppb CH_4

578
 579
 580

Table 1: Specifications of the two DCS systems. HCC: hollow corner cube



Systematic source [effect]	Effect on retrieved CO ₂	Effect on retrieved CH ₄	Effect on retrieved H ₂ O
Fitting procedure [initial guess, baseline polynomial order and window size]	0.07 ppm	1.4 ppb	4 ppm
Rf detection and processing [rf reflections, ADC nonlinearities]	0.16 ppm	0.34 ppb	1.0 ppm
Telescope system [Scattered light, polarization effects]	0.45 ppm	1.5 ppb	56 ppm
Spectral database [linestrengths in HITRAN 2008]	1-2%	10-20%	5-10%
Temperature path inhomogeneities [if <10 C across path]	0.024 ppm	0.36 ppb	3.52 ppm
Path-averaged temperature [for 0.5 C uncertainty]	0.64 ppm	2.9 ppb	8.6 ppm

581

582

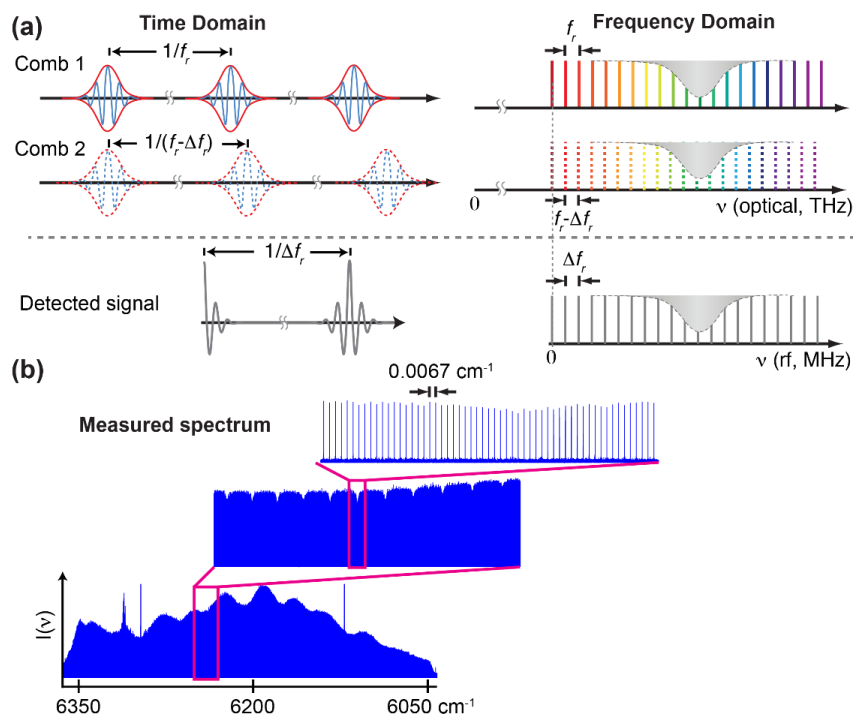
583

584

Table 2: List of systematic uncertainties. See discussion in Section 3.2 and 3.4 for more details. Upper half of table: systematics due to hardware and software. Lower half of the table: systematics due to spectral model and temperature uncertainties.



585



586

587

588

589

590

591

592

593

594

595

596

597

598

599

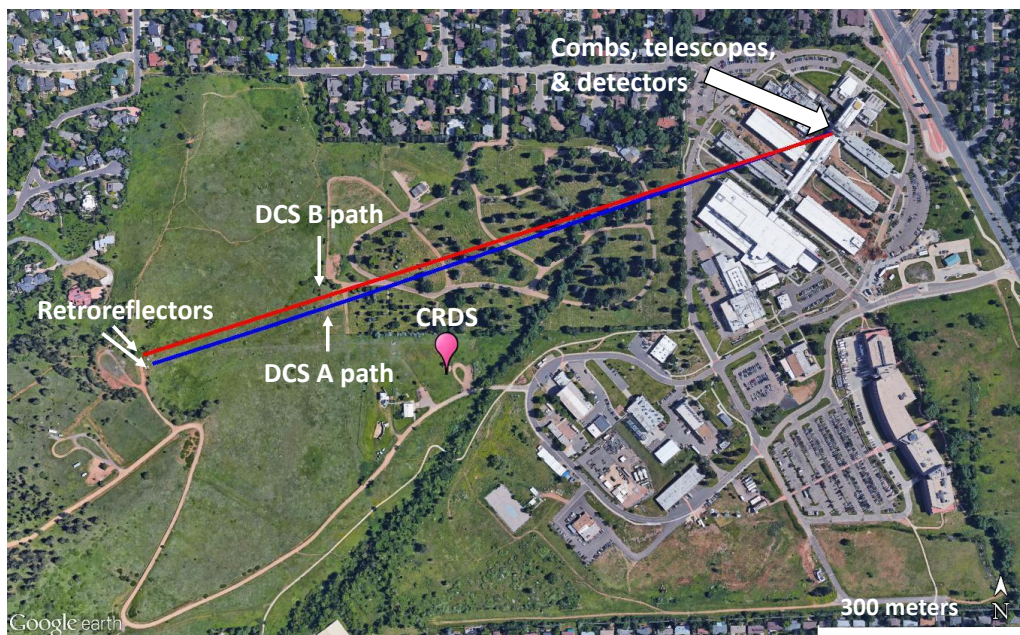
Figure 1. (a) Time and frequency domain overview of dual comb spectroscopy. Two frequency combs are phase-locked together with pulse repetition rates of f_r and $f_r - \Delta f_r$. Their detected heterodyne signal is a series of interferograms in the time domain, or equivalently a comb in the radio frequency (rf) domain. Provided the combs are sufficiently coherent and Nyquist sampling conditions are met, each rf comb tooth maps to a particular, known pair of optical frequency comb teeth (Coddington et al., 2008). As a result, the optical spectrum can be obtained from the magnitude of each rf comb tooth versus the average optical frequency of the relevant comb tooth pair. (b) Actual DCS spectrum acquired over 1.15 seconds for DCS A after transmission over 2-km air path. The overall shape is governed by the comb spectrum but there are narrow absorption dips present from atmospheric gases, as shown in the first expanded view. The second expanded view shows the fully resolved rf comb teeth with time-bandwidth limited widths. The highly resolved nature of these spectral elements translates to a negligible instrument lineshape, set by the narrow comb linewidths. The sample points are separated by 0.0067 cm^{-1} (or $f_r = 200 \text{ MHz}$). For long-term averaging, we implement coherent co-adding of interferograms that effectively measures the power at the individual rf comb teeth (Coddington et al., 2008)

600

601

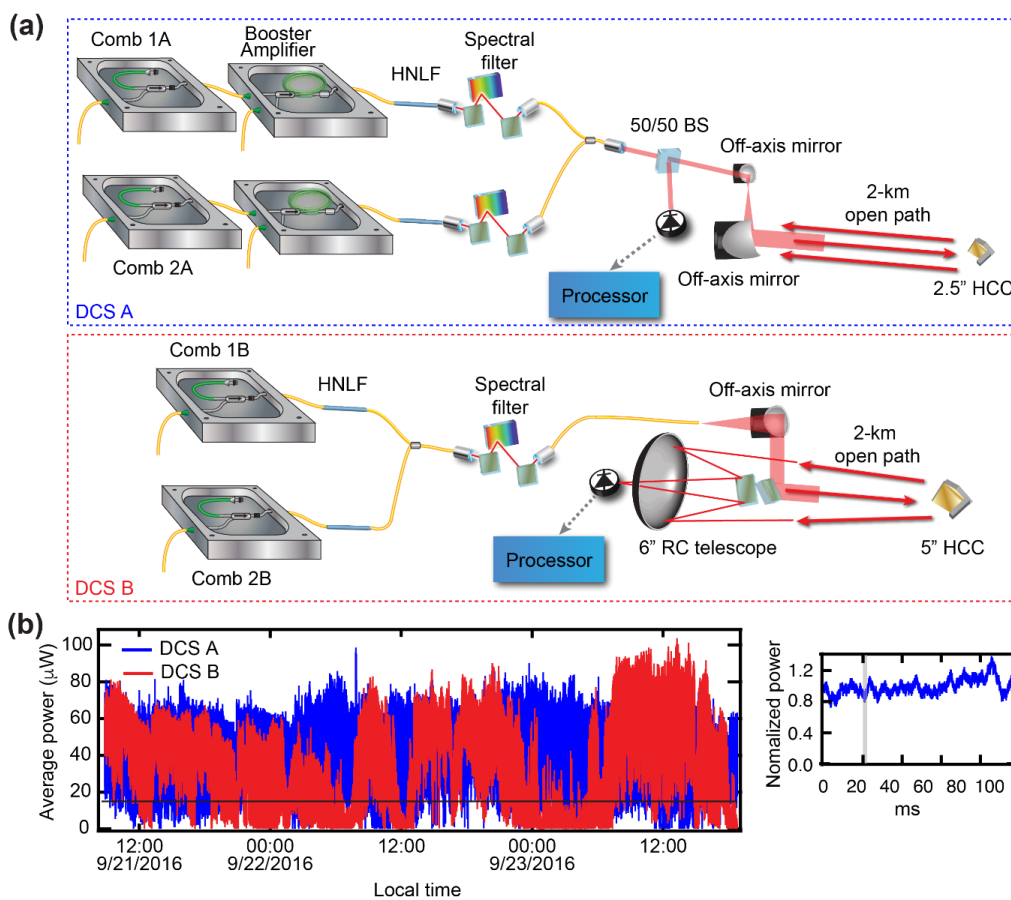


602



603
604
605
606
607
608
609

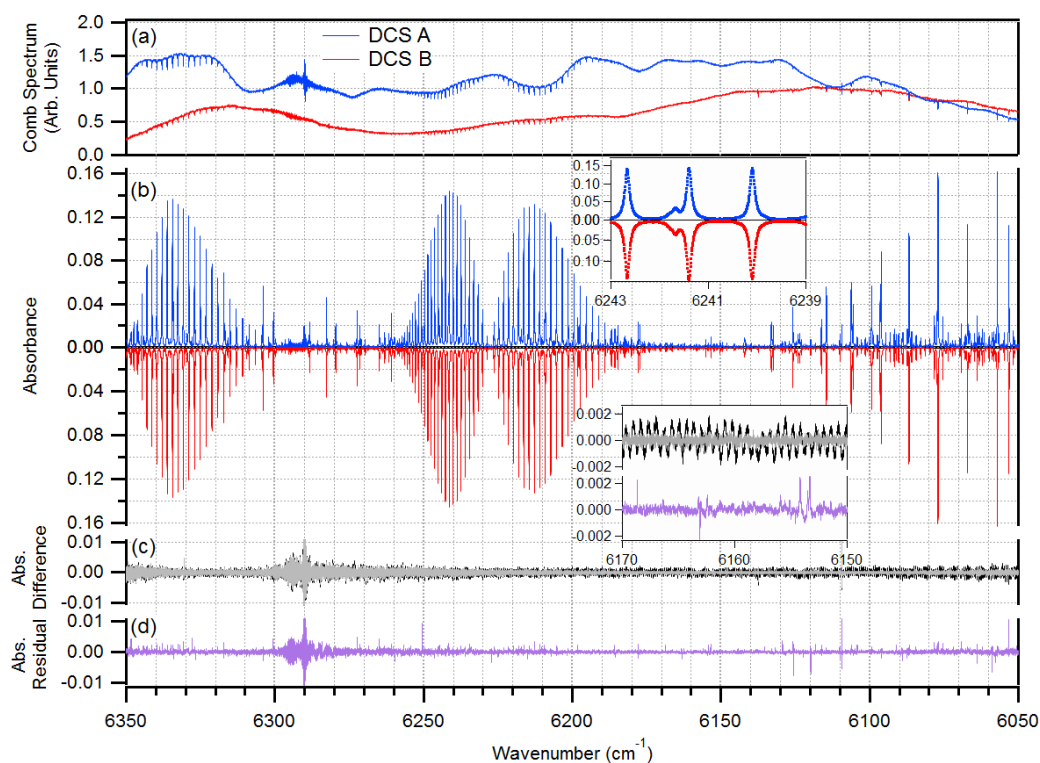
Figure 2. Setup for the open-path dual-comb spectrometer (DCS) comparison at the NIST Boulder CO campus. The main components for DCS A and DCS B are housed in a rooftop laboratory, including the frequency combs, telescope, receiver, and processor. For each DCS, the combined comb light is launched from a telescope, travels ~1 km through the atmosphere to a retroreflector, and returns to the telescope where it is collected, detected and processed. A separate cavity ringdown point sensor (CRDS) is located nearby with an inlet on a 30-m tower that is located ~160 meters from the nearest point of the free-space DCS paths.



610

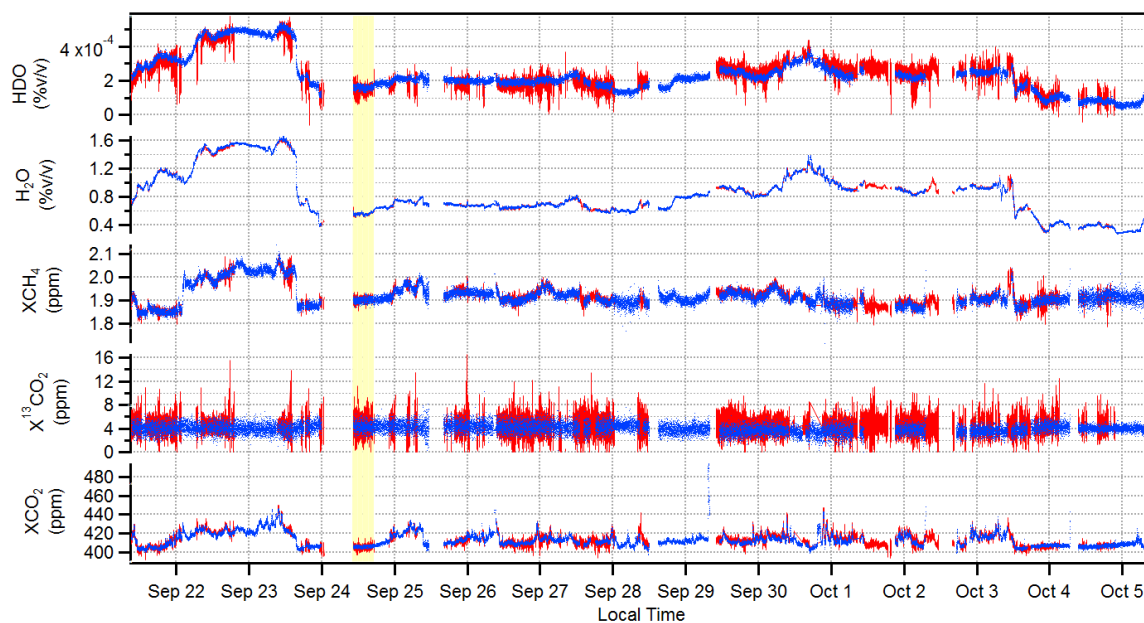
611 *Figure 3. (a) Configuration of DCS A and DCS B, both of which are based on fully self-referenced fiber-laser frequency combs. See*
 612 *text and Table 1 for details. DCS A includes a booster amplifier for higher launched optical power than DCS B. (b) Average optical*
 613 *return power for DCS A (blue) and DCS B (red) measured at the detector over about 2.5 days. The horizontal black line shows the*
 614 *approximate minimum power for useable SNR (15 μ W). Inset: The normalized power fluctuations for DCS A over 100 ms. The*
 615 *acquisition time for a single DCS spectrum is shown by the thickness of the vertical grey bar. RC: Ritchey-Chretien; HNLF: highly*
 616 *nonlinear fiber; HCC: hollow corner cube retroreflector; BS: beam splitter.*

617



618

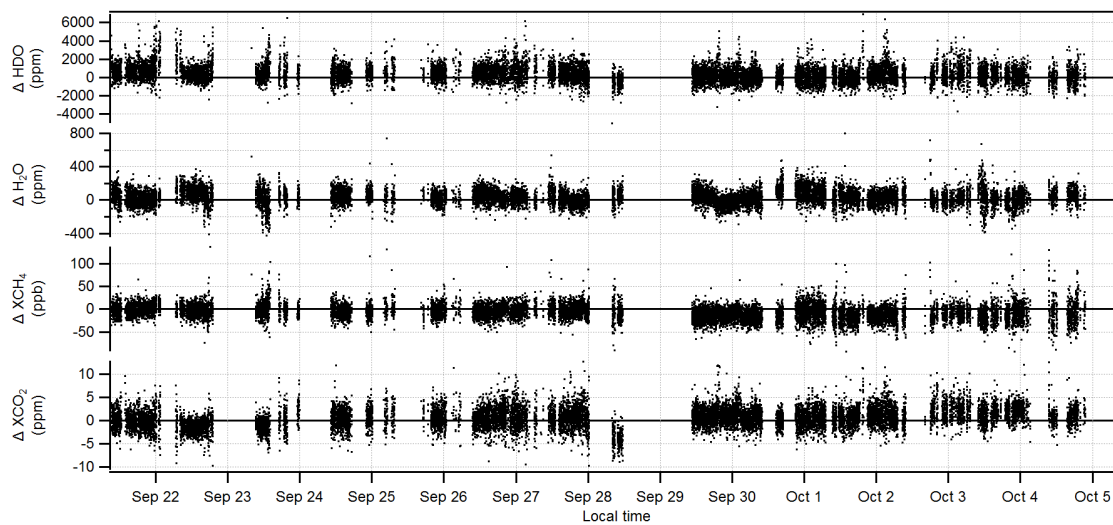
619 *Figure 4. Raw spectra from DCS A (blue) and DCS B (red). (b) Corresponding baseline-corrected absorption spectra averaged for*
620 *a three-hour period. The spectra overlap completely on this scale so the DCS A absorbance has been flipped about zero.*
621 *expanded view of several CO₂ lines. (c) Difference between the absorption spectra from DCS A and DCS B. The difference is*
622 *shown both before (black trace) and after (grey trace) removing an etalon structure and agree to better than 5×10⁻⁴ after the*
623 *etalon is removed. Inset: Expanded view. (d) Residuals from a fit of the DCS A spectrum to HITRAN 2008. In general, the residuals*
624 *are lower noise than the difference spectrum because of the higher signal-to-noise ratio of the DCS A than DCS B, but there are*
625 *clear structures present near absorption lines due to imperfect line shapes of the spectral database.*



626
627
628
629
630
631

Figure 5. Concentration retrievals from DCS A (blue dots) and DCS B (red lines) for HDO (% by volume) H₂O (% by volume), dry CH₄, dry CO₂ and dry ¹³CO₂ over two weeks at 30-second intervals. Excellent agreement is observed between both systems for all species, though it is clear that over this path length ¹³CO₂ does not provide a strong enough signal to retrieve reliably. Highlighted section: 6-hour, well-mixed period over which Allan deviations (Figure 8) are calculated. Missing data is primarily due to telescope misalignment and less frequently, phase lock by one of the combs.

632

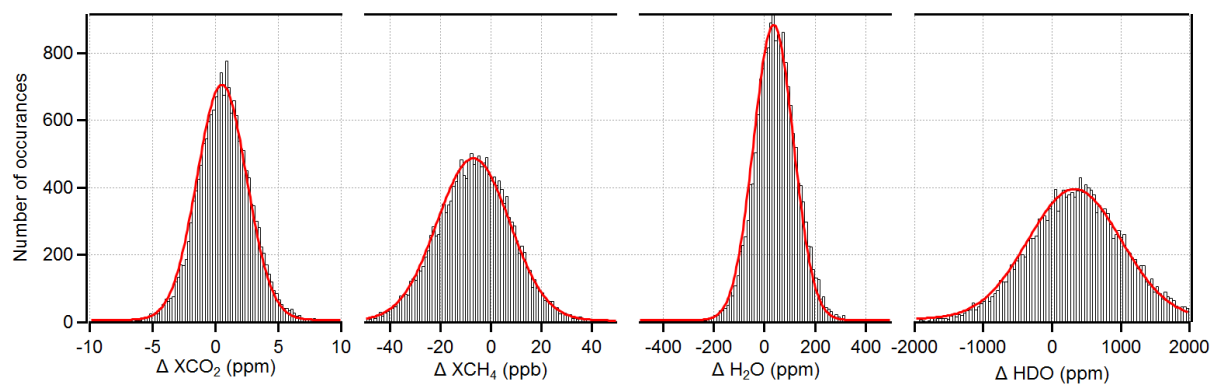


633

634

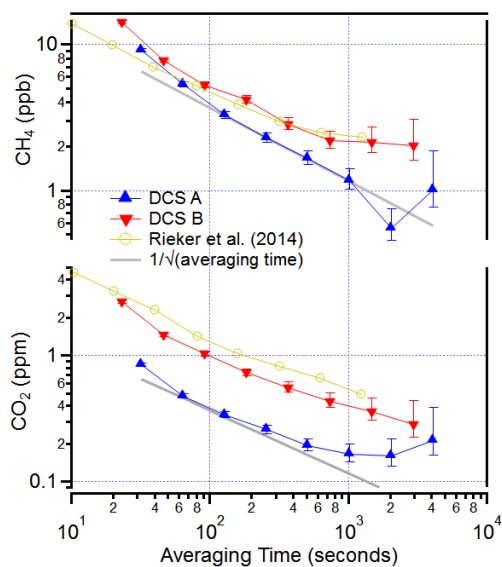
Figure 6. Time series of concentration differences, where difference is defined as DCS A - DCS B.

635

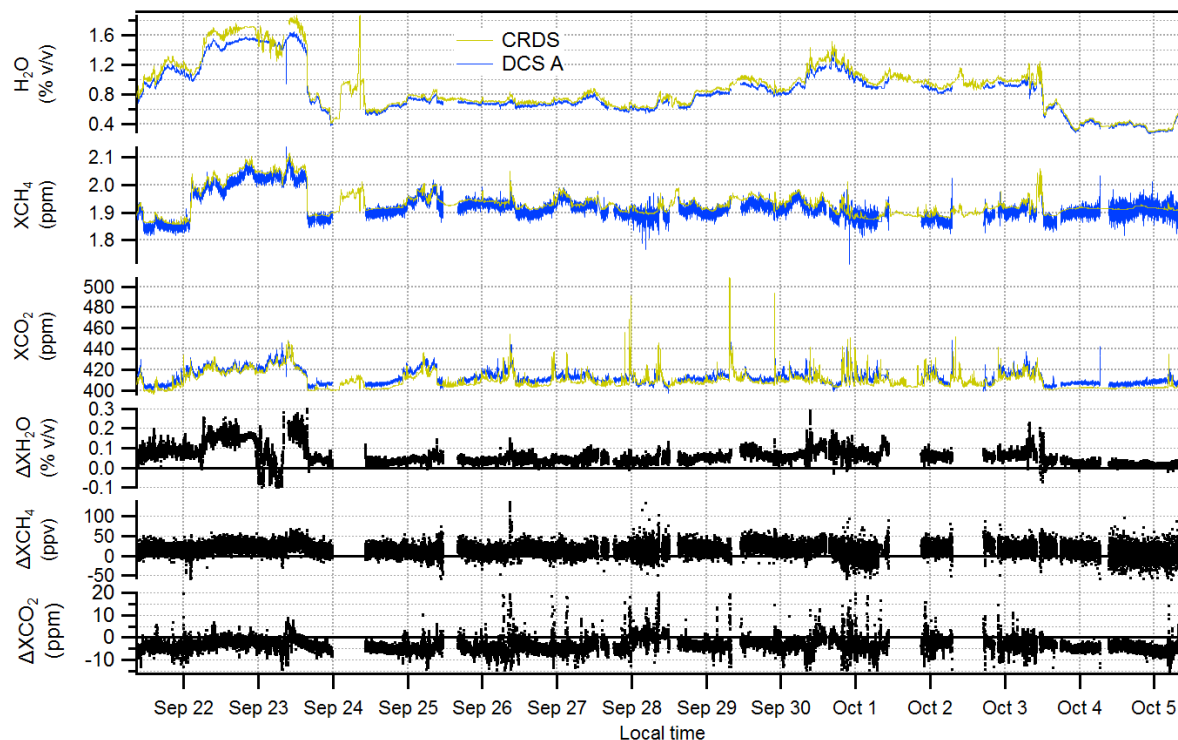


636
637 *Figure 7. Statistical distributions of the differences between DCS A and DCS B for dry CO₂, dry CH₄, H₂O, and HDO from Fig. 6.*
638 *Histograms are shown in black with a fit to Gaussian curves in red. These data are for ~30-second intervals; the widths are*
639 *approximately halved if the data is averaged to 5-minute intervals.*

640
641



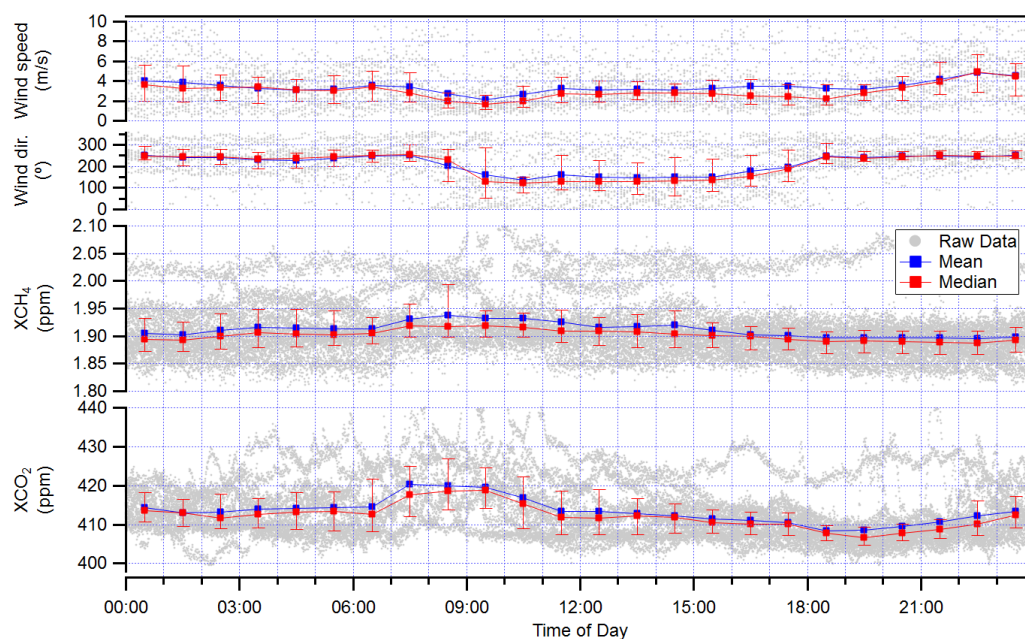
642
643 *Figure 8. Precision (Allan deviation) versus averaging time, τ , for CH_4 and CO_2 calculated for DCS A (blue) and DCS B (red) over a*
644 *2 km path for the time period highlighted in Figure 3. The previously-published precisions from Rieker et al. (2014) are also*
645 *shown (gold). The grey line illustrates the slope expected for white noise. For DCS A, at averaging times from 30s to 1000s, the*
646 *precision roughly follows $\sim 40 \text{ ppbv}/\sqrt{\tau}$ for CH_4 and $\sim 4 \text{ ppmv}/\sqrt{\tau}$ for CO_2 (gray lines).*



647
648
649

Figure 9. Comparison between the open-path DCS A data (blue) and the point CRDS data (gold) for H_2O , dry CH_4 , and dry CO_2 at 32-second intervals over two weeks. The lower three panels directly plot the corresponding difference between the two.

650
651



652
653 *Figure 10. Diurnal cycles for wind speed, wind direction, XCH₄, and XCO₂. Data from each day in Figure 5 is over-plotted in grey*
654 *along with the hourly mean (blue) and median (red) values. Uncertainty bars on the median values span the 75th quantile and*
655 *25th quantile.*

656



657 Appendix A: Temperature studies

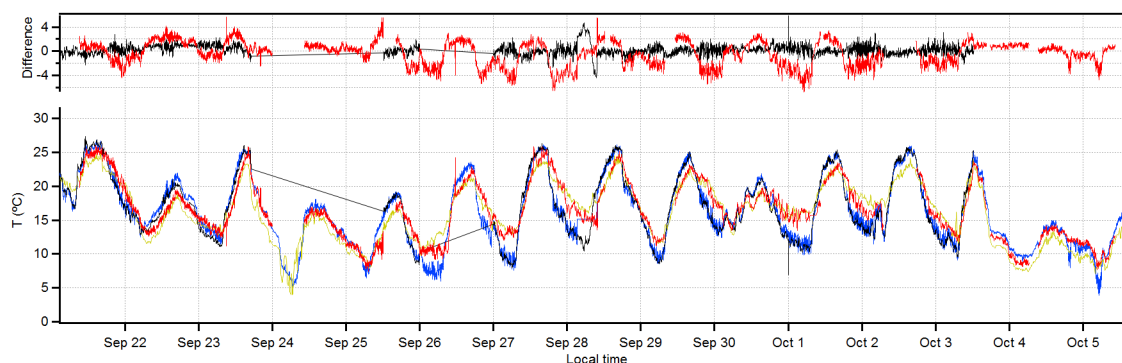
658

659 As described in Section 2.4, we extract the path-averaged temperature directly from a fit to the 30013
660 \leftarrow 00001 overtone band of CO_2 . We perform this fit on 5-minute averages, rather than 32-second
661 averages, under the assumption the temperature changes are still slow at that timescale. This path-
662 averaged temperature is then used in a subsequent fit over the full spectral region to extract the column
663 densities, and finally the mole fractions. We use a common temperature (from DCS A fit) to analyze
664 both data sets in order to separate out instrument effects from the temperature, but the fitted
665 temperatures between instruments show less than 0.25°C bias.

666 Figure A1 compares this fitted path-averaged temperature from DCS A to three point sensors,
667 two of which are located on the rooftop near the telescope launch point and one that is located ~ 2.2
668 km away at an altitude ~ 200 m above the overall open path. As shown in Figure A1, the two rooftop
669 temperature sensors located near the telescope agree well with each other, but do not agree with the
670 fitted path-averaged temperature. Moreover, that disagreement has a distinct diurnal character,
671 supporting the argument it arises from a real temperature gradient. In contrast, the path-averaged
672 temperature does often agree well with the temperature measured by the third temperature point
673 sensor located at similar or higher altitude as the open path on the NCAR Mesa building
674 (<ftp://ftp.eol.ucar.edu/pub/archive/weather/mesa/>). These data indicate that the point sensor located
675 at the telescope site is not a good proxy for the path-averaged temperature; instead, the fitted path-
676 averaged temperature should be used for the concentration fits because of temperature gradients. Note
677 that the temperature gradients themselves do not lead to appreciable errors in the retrieved mole
678 fractions if the correct path-averaged temperature is used (see Table 2 and Section 3.4).

679

680



681

682 Figure A1: The fitted path-averaged temperature over two-weeks at 5 minute intervals (red) compared
683 to the measured air temperature from a roof-top anemometer located near the telescope (blue), a
684 second thermistor temperature sensor also located on the roof but 100-m distant (black), and a third
685 rooftop temperature ~ 2.2 km distant at the NCAR Mesa facility (gold). Top panel: The difference
686 between the two rooftop temperature (black) agree to within 1°C , but the difference between these
687 rooftop sensors and fitted path-averaged temperature (red) shows larger $2\text{--}4^\circ\text{C}$ diurnal differences,
688 indicating it is not sufficient to measure the temperature at one “end point” of the open path. In fact,
689 the path-averaged temperature agrees better with the more distant, but higher elevation temperature
690 sensor located at the NCAR Mesa facility.

691