# Depolarization calibration and measurements using the CANDAC Rayleigh-Mie-Raman Lidar at Eureka, Canada

Emily M. McCullough<sup>1,2a,\*</sup>, Robert J. Sica<sup>1</sup>, James R. Drummond<sup>2</sup>, Graeme Nott<sup>2,4a</sup>, Christopher Perro<sup>2</sup>, Colin P. Thackray<sup>2</sup>, Jason Hopper<sup>2</sup>, Jonathan Doyle<sup>2</sup>, Thomas J. Duck<sup>2</sup>, and Kaley A. Walker<sup>3</sup>

<sup>1</sup>Department of Physics and Astronomy, The University of Western Ontario, 1151 Richmond St., London, ON, N6A 3K7 <sup>2</sup>Department of Physics and Atmospheric Science, Dalhousie University, 6310 Coburg Rd., PO Box 15000, Halifax, NS, B3H 4R2

<sup>3</sup>Department of Physics, University of Toronto, 60 St. George St., Toronto, Ontario, M5S 1A7

<sup>4</sup>Facility for Airborne Atmospheric Measurements, Building 146, Cranfield University, Cranfield, MK43 0AL, UK <sup>a</sup>Indicates present affiliation

Correspondence to: Emily M. McCullough (e.mccullough@dal.ca)

### Abstract.

The Canadian Network for the Detection of Atmospheric Change (CANDAC) Rayleigh–Mie–Raman Lidar (CRL) at Eureka, Nunavut, has measured tropospheric clouds, aerosols, and water vapour since 2007. In remote and meteorologically significant locations, such as the Canadian High Arctic, the ability to add new measurement capability to an existing well-tested facil-

- 5 ity is extremely valuable. In 2010, linear depolarization 532 nm measurement hardware was installed in the lidar's receiver. To minimize disruption in the existing lidar channels and to preserve their existing characterization so far as is possible, the depolarization hardware was placed near the end of the receiver cascade. The upstream optics already in place were not optimized for preserving the polarization of received light. Calibrations and Mueller Matrix calculations are used to determine and mitigate the contribution of these upstream optics on the depolarization measurements. The results show that with appropriate
- calibration, indications of cloud particle phase (ice vs. water) through the use of the depolarization parameter are now possible 10 to a precision of  $\pm 0.05$  absolute uncertainty (< 10% relative uncertainty) within clouds at time and altitude resolutions of 5 min and 37.5 m respectively, with higher precision and higher resolution possible in select cases. The uncertainty is somewhat larger outside of clouds at the same altitude, typically with absolute uncertainty  $\leq 0.1$ . Monitoring changes in Arctic cloud composition, including particle phase, is essential for an improved understanding of the changing climate locally and globally.
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# 1 Introduction

Clouds influence Earth's radiation budget, and thus its weather and climate. Clouds reflect sunlight (cooling), and trap heat from the ground (warming). The combined effect of these competing influences is poorly understood, especially in the Arctic, because it depends significantly on the structure and microphysical properties of the clouds, and the environment in which the

clouds exist (Curry et al., 1996). Ice clouds radiate differently than water clouds (Sun and Shine, 1994). Tropospheric clouds 20 occur frequently in the Arctic, with liquid content found at all times of year, often within mixed-phase clouds (Intieri et al., 2002; Shupe, 2011). In order to develop models with improved fidelity of the cloud phase, more observational measurement datasets are required (Shupe, 2011), with phase transitions being of particular interest (Kalesse et al., 2016). Measurements of cloud particle phase (ice vs. water) are therefore necessary in order to more fully understand the radiation balance of the Arctic atmosphere. Liquid droplets can exist well below  $0^{\circ}$  C, so cloud temperature is not sufficient to determine the phase of

5 cloud particles (e.g. Shupe et al., 2008; Boer et al., 2009; Curry et al., 1996; Sassen, 1991; Westbrook and Illingworth, 2013).
 Lidar depolarization measurements, which discern cloudy regions containing spherical particles (i.e. liquid droplets) from those containing nonspheres (i.e. ice particles), are one method by which cloud particle phase may be examined (Schotland et al., 1971; Sassen, 2005; Bourdages et al., 2009).

The Polar Environment Atmospheric Research Laboratory (PEARL) is located in Eureka, Nunavut (80° N, 86° W) in

10 Canada's High Arctic. PEARL has more than 25 instruments dedicated to the in situ and remote sensing study of atmospheric phenomena at a latitude where few measurements are typically available. With climate changes amplified at such latitudes (Serreze and Barry, 2011), PEARL's measurements are a valuable contribution to global atmospheric and environmental science.

The Canadian Network for the Detection of Atmospheric Change (CANDAC) Rayleigh–Mie–Raman Lidar (CRL), was installed at PEARL in 2007. It has since made measurements of visible and UV particulate backscatter coefficient, aerosol

- 15 extinction, water vapour mixing ratio, and other quantities using its 355 nm and 532 nm lasers and comprehensive detection package (Doyle et al., 2011; Nott et al., 2012). Adding 532 nm linear depolarization capabilities to this instrument is an economical way to add additional capacity to study Arctic clouds, in concert with other instruments at PEARL such as the Millimetre Cloud Radar (Moran et al., 1998), the E-AERI interferometer (Mariani et al., 2012), and the Starphotometer (Baibakov et al., 2015). To preserve continuity in the long-term data sets from other CRL channels, no existing optics were altered or
- 20 removed during the installation of the depolarization channels. Figure 1 is a diagram of the CRL's receiver, showing the seven original measurement channels, and indicating the locations of the new pellicle beamsplitter, Polarotor rotating Glan-Thomson prism, interference filter, focusing lens, and photomultiplier tube of the 532.1 nm depolarization channel. CRL uses a single PMT to measure light of two polarization planes on alternate laser shots, with a laser repetition rate of 10 Hz. This is similar to Platt (1977), which operated with a laser repetition rate of 1 to 5 Hz. CRL's higher repetition rate means that the assumption
- of simultaneous measurements in both polarization planes is reasonable. As the original lidar optics were not chosen for their polarization properties, the optical design of the CRL has made the calibration of the depolarization measurements challenging.

# **1.1** Depolarization lidar theory

With the new depolarization capabilities, we aim specifically to investigate "the atmospheric phenomena which change the polarization state of the light received by a lidar relative to the state of the transmitted light" (Gimmestad, 2008). Depending on
the optical qualities of the particles, a population of randomly oriented identical particles in the atmosphere should either a) not change the polarization state of the light (i.e. all light from that population will be returned polarized parallel with respect to the state of the transmitted light), or b) should cause the light to become completely unpolarized on its return. There may be more than one population of particles present in any given scattering volume. The calculation to determine the change in polarization requires a ratio of the intensity of light which is returned unpolarized to the total intensity of light which is returned in any



**Figure 1.** Diagram of CRL's receiver system, showing all 7 existing measurement channels plus the newly installed depolarization hardware. The new hardware consists of the pellicle beamsplitter, the Polarotor, and the interference filter, focusing lens, and PMT, to the right of the polarotor. Numbers correspond to calibration test numbers from Table 1, and indicate the test locations of the depolarizing sheet used in those tests. "7" also marks the location of the calibration cube polarizer added to the system for the calibrations in Sect. 5.1, and "8" is also the location of the lamp and depolarization sheet during the polarized light tests in that section. During regular lidar sky measurements, neither the depolarizing sheet nor the calibration cube polarizer remain in the optical path. This figure is based on Fig. 2 of Nott et al. (2012).

and all polarization states (Flynn et al., 2008; Gimmestad, 2008). Expressed in this manner, the quantity of interest is d, the depolarization parameter: the portion of the total light intensity I which has become depolarized through scattering. Similar descriptions, called depolarization factor, are given as early as van de Hulst (1957). The depolarization parameter is defined as:

$$d = I_{\text{unpol.}} / (I_{\text{pol.}} + I_{\text{unpol.}}).$$
<sup>(1)</sup>

5 In the event that the atmosphere does not depolarize the beam, there will be no intensity returned with polarization different than the transmitted light, and therefore d = 0. In the case of complete depolarization, d = 1.

Because lidars measure signals from photomultiplier tubes (PMTs), and not the backscattered light intensity directly, the equation for d and must be reformulated in terms of lidar observables. Gimmestad (2008) demonstrates this development using Mueller Matrix algebra, with normalized matrices. Two quantities are measured. The first is the signal in a channel which uses

10 a polarization analyzer to admit light polarized parallel to the polarization plane of the transmitted laser beam (the "parallel"

channel), and signal in a channel which uses a polarization analyzer to admit light polarized perpendicularly to this plane (the "perpendicular" channel). In this way, in the absence of any complicating factors, for linearly polarized transmitted light, the parallel channel will be sensitive to half of the backscattered light which has been unpolarized during scattering ( $\frac{1}{2}I_{unpol.}$ ) and all light which remains polarized during scattering ( $I_{pol.}$ ). The second signal is that in the perpendicular channel, which will

5 be sensitive only to half of the unpolarized light  $(\frac{1}{2}I_{unpol.})$ , and none of the light which remains polarized when backscattered. In Gimmestad's paper, the signals in the receivers, *S*, are individually "assumed to be calibrated", but no further details about these calibrations are provided. Presumably, this assumption considers the combined effects of all optics upstream of the PMT and the gain of the PMT, acting together as a constant attenuation factor for each individual channel. If the factors differ between channels, the overall effect in the system as a whole is that of partial polarizer.

10 Under these conditions, the equation for depolarization parameter is given as:

$$d = \frac{2kS_{\perp}}{S_{\parallel} + kS_{\perp}} = \frac{2k\frac{S_{\perp}}{S_{\parallel}}}{1 + k\frac{S_{\perp}}{S_{\parallel}}} = \frac{2}{\frac{1}{k}\frac{S_{\parallel}}{S_{\perp}} + 1},$$
(2)

in which:  $S_{\perp}$  is the signal measured by the perpendicular channel,  $S_{\parallel}$  is the signal measured by the parallel channel, and  $k = \frac{G_{\parallel}}{G_{\perp}}$  is the depolarization calibration constant, in which  $G_{\parallel}$  is the gain (or attenuation) of the parallel channel, and  $G_{\perp}$  is the gain (or attenuation) of the perpendicular channel. The third form for d in Eq. (2) is easier to handle experimentally as each measurement appears only once and thus uncertainties may be considered uncorrelated.

Historically, "depolarization" has also referred to  $\delta$ , the depolarization ratio. This quantity is proportional to the ratio of the perpendicular signal  $S_{\perp}$  to the parallel channel  $S_{\parallel}$  (e.g. Hohn, 1969; Schotland et al., 1971; Liou and Schotland, 1971; Freudenthaler et al., 2009). The depolarization parameter d is directly relatable to the expression for depolarization ratio,  $\delta$ , through the same signal measurements and the same calibration constant:

$$20 \quad \delta = k \frac{S_{\perp}}{S_{\parallel}}.$$
(3)

The conversion between the quantities d and  $\delta$  is:

$$d = 2\delta/(1+\delta). \tag{4}$$

A variety of expressions for "depolarization" are described in Cairo et al. (1999). The  $\delta$  described in the current paper is most closely related in meaning to the Pal and Carswell (1973) "volume linear depolarization ratio" cited therein, but it is not strictly equivalent because no claims are made here about the connection between  $\delta$  and backscatter coefficient. Rather,  $\delta$  is defined here only as a function of measured quantities. Gimmestad (2008) provides motivation for moving away from all  $\delta$ descriptions, pointing out that *d* is consistent with the rest of optical physics and scattering theory. Expressing depolarization as *d* has since been adopted in such publications as Hayman and Thayer (2009, 2012) and Neely III et al. (2013). Results in the present paper will be provided in terms of both *d* and  $\delta$  so that readers working under either paradigm can readily make use of

30 the figures and calculations.

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The expressions for d and  $\delta$  of Eq. (2) and Eq. (3) are all referred to in this paper as "traditional" in the sense that in each equation, a single k value determines the calibration.

### 1.2 Literature review of depolarization calibrations

The calibration constant k can be determined by introducing unpolarized light into the detector (i.e. setting  $d = \delta = 1$ ) or, equivalently, light polarized at  $\pm 45^{\circ}$  with respect to each of the planes of polarization for the detectors (also sets  $d = \delta = 1$ ) and measuring the signals in each channel. k is then the ratio of the two signals. The location of calibration optics or lamps

- 5 within the lidar determines how much of the system will be characterized through the calibration. The most strict meaning of k is the ratio of gains of the detectors, if the polarization state of the calibration light is defined directly before the polarizing beamsplitter. A wider interpretation for the meaning of k can include relative gains resulting from other receiver optics if the polarization state is defined earlier in the receiver, and can include relative gains of transmitter optics if the polarization state for the test is set within the transmitter. The laser is assumed to be completely linearly polarized. The orientation of the parallel
- 10 and perpendicular polarization analyzers must be correctly set at  $90^{\circ}$  to each other, and oriented correctly with respect to the usual polarized returns from the transmitted laser beam, before the calibrations for k commence. Using k as the only calibration factor ignores the possibility of any retarding and rotating effects which may exist in the transmitter and receiver, in all of the optical components. This is more likely to be appropriate for lidars which have few receiver optics before the polarization analyzer (e.g. Wang et al., 2009), and is less likely to be appropriate for lidars which have many receiver optics which are not
- 15 optimized for polarization measurements, such as the CRL.

Some groups begin the calibration for k with lidar returns from an atmospheric region which is assumed not to depolarize the light (or to depolarize only a known minimal amount as a result of molecular scattering) for the duration of the calibration. Then a half waveplate is included in the receiver to control the orientation of the polarized backscattered light as it enters the detectors, aligning it at  $\pm 45^{\circ}$  with respect to both polarization analyzers (Spinhirne et al., 1982; McGill et al., 2002; Alvarez

20 et al., 2006; David et al., 2012; Wang et al., 2009; Freudenthaler et al., 2009; Neely III et al., 2013; Bravo-Aranda et al., 2013; Freudenthaler, 2016). This type of calibration is not sensitive to polarization effects in the transmitter optics, nor to any optics upstream of the half wave plate. This typically means omitting at least the telescope, and sometimes more optics. A notable exception is Neely III et al. (2013), which has a waveplate optic in the roof window.

In an alternate version of the half waveplate calibration, this waveplate may be placed in the transmitter to control the orientation of the plane of polarization of the laser light transmitted to the sky (Liu and Wang, 2013; Neely III et al., 2013; Freudenthaler, 2016; Bu et al., 2017). Eloranta and Piironen (1994) uses a pockels cell in their laser to the same effect. Locating the calibration optic in the transmitter is a method which includes as many optics as possible in the calibration.

All calibrations using polarized light must be concerned with obtaining the correct orientation of the waveplate (or other relevant optic). Spinhirne et al. (1982) and some lidar examples in Freudenthaler et al. (2009) arrange the waveplate as well as

30 possible such that the output is at  $+45^{\circ}$  and/or  $-45^{\circ}$ , and report the calibration measurements only from those specific angles. Other groups show improved results for k by calculating its value at a variety of waveplate rotation angles, then using a fit to determine the optimal rotation angle from which to use the calibration values (Alvarez et al., 2006; Hayman and Thayer, 2009; Snels et al., 2009; Liu and Wang, 2013; Bu et al., 2017). Of those in the latter case, methods using both  $+45^{\circ}$  and  $-45^{\circ}$ measurements together (calibrations 90° apart from one another), can have error terms which compensate well for one another in the event that the waveplate is misaligned by the same amount in each case (Freudenthaler et al., 2009, some systems in Freudenthaler, 2016).

Sassen and Benson (2001) use a different method for simulating a  $d = \delta = 1$  situation. They introduce unpolarized lamp light to their detector from the point of focus of the telescope. This calibration method is not sensitive to any polarization

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effects in the transmitter optics or the telescope, but the polarization state of the calibration light is well-known, and there are no calibration optic rotation angles to introduce errors.

CRL calibrations for k use a sheet of depolarizing material in the receiver. This can be placed at a variety of locations within the receiver. The results of these tests provide the motivation for this paper. When using a depolarizing sheet directly upstream of the polarotor (see Fig. 1, location 1 and 4; same location as half wave plate used in e.g. Alvarez et al. (2006); Wang et al. (2009); Freudenthaler et al. (2009)), we find that k = 1. This is exactly as expected. Effectively, this is an estimate for the strict version of k: the ratio of PMT gains – and CRL uses the same PMT for each depolarization channel. Repeating the calibration measurements with a depolarizing sheet at the entrance to the receiver roof window suggest a value closer to  $k = 21.0 \pm 0.2$ for the whole CRL receiver (Sect. 6.3), indicating that optics upstream of the polarotor are significantly polarizing. Clearly a

more thorough instrument depolarization characterization is required for the CRL. If our optics are so highly polarizing, they may carry other optical consequences as well, which Eq. (2) and Eq. (3) are insufficient to describe.

Various approaches are available in the literature to account for non-ideal depolarization lidar hardware, each with their own assumptions. Some calibrations are tests with a temporarily-installed optic. These allow for calibration factors to be determined, which will then be applied to regular measurements made without the temporary calibration optic in place. Other calibrations consist of adjusting compensation optics (typically by adjusting their rotation angle) which will remain in the lidar

- 20 during regular measurements. Some of these are the same optics used for the calculations of k. At present, the lidar of Neely III et al. (2013) seems most capable of a whole-system calibration. Their calibration optics exist in multiple places within the transmitter, and multiple places within the receiver. The laser light can be rotated directly as it exits the laser, again as it exits the laboratory, again as it enters the telescope, and altered yet again as the light enters the PMTs. Further, the lidar was designed to make depolarization measurements, and optics could be selected and oriented with this in mind, as indicated in Hayman
- 25 and Thayer (2012). Their liquid crystal variable retarder has some effects related to laboratory temperature which must be considered, but the authors have accounted for these. No other lidar of which we are aware has all of these capabilities. The more common calibrations each assess only some of the possible complications. Two are discussed briefly here.

First, Sassen and Benson (2001) allow calibration for the effect of angular misalignment between the transmitter and receiver planes of polarization in their measurements and calibrations. Other groups have introduced methods of optical compensation

- for such an angular misalignment: The half wave plates used in the transmitters of Spinhirne et al. (1982); Liu and Wang (2013); Bu et al. (2017), in the receivers of McGill et al. (2002); Wang et al. (2009); Freudenthaler et al. (2009), and in both transmitter and receiver of Neely III et al. (2013) for the k calibration remain in the lidars. During regular measurements, the optics are aligned such that a maximum of non-depolarized backscattered light is directed to the appropriate channel. These calibrations to account for angular mismatch between transmitted and received planes of polarization generally depend on a
- 35 "known" sky depolarization of aerosol-free molecular-only scattering (e.g. Platt (1977)) or liquid-droplet-only stratospheric

clouds (e.g. Adachi et al. (2001), requiring additionally a total backscattering ratio measurement). Bravo-Aranda et al. (2016) and Freudenthaler (2016) analyze the effects of transmitter-receiver angular misalignment on uncertainties in the retrieved atmospheric depolarization values. The calculations therein are less relevant for CRL because both studies include the error that is induced by leaving an extra compensation optic in the lidar (the half-wave plate). The CRL (similarly to e.g. Alvarez

5 et al. (2006)), does not leave any calibration optics in the optical path during routine measurements. Thus, the uncertainties due to angular mismatch must be dealt with a different way. CRL carries out a polarotor start delay test in clear sky (see Sect. 2.3) to ensure angular alignment between transmitted and received planes, and an assessment of uncertainty is carried out using a simple model.

Second, lidars using a polarizing beamsplitter to separate received light to two separate PMTs have to account for different
efficiencies for each plane of polarization in their parallel and perpendicular channels, one being reflected and the other transmitted through the beamsplitter. These calculations are integral to some recent works (Liu and Wang, 2013; Bravo-Aranda et al., 2016; Freudenthaler et al., 2009), but are not relevant for CRL, in which both parallel and perpendicular measurements are made using the transmitted beam of light through the polarotor.

- In contrast to the methods discussed to address these two complications, which tend to be dealt with individually, the CRL's approach in this paper is to determine the optical effects of the receiver as a whole. The recent papers on depolarization calibration are moving away from a scalar description, and are moving toward a vector description of light, with matrix algebra describing the optical effects of the sky (Kaul et al., 2004; Hayman and Thayer, 2009, using Mueller Matrix algebra) and of the lidar itself (Biele et al., 2000; Hayman and Thayer, 2009, 2012; Neely III et al., 2013; Freudenthaler, 2016, using Mueller Matrix algebra and Bu et al., 2017, using Jones matrices).
- The Mueller Matrix algebra upon which this technique relies was introduced as lectures and conference proceedings by Hans Mueller in the early 1940s (e.g. Mueller (1946a, b, 1948)). These and his previous works (Mueller, 1943a, b) remain difficult to obtain, and those available (e.g. in summary report Bush (1946), which describes the design and use of the shutter described in Mueller (1943a)) do not explicitly demonstrate the matrix algebra. A better and more available source describing all of the Mueller Matrix algebra in considerable detail is the thesis of Mueller's PhD student, Nathan Grier Parke III (Parke III, 1948).
- In Hayman and Thayer (2012), there is a rigorous mathematical development of the Mueller matrices for lidar instrument optical contributions of various sorts. This is followed in a similar way by Freudenthaler (2016) and Bravo-Aranda et al. (2016), which use Mueller Matrix algebra to work out the expected signals for a sample of calibration and measurement situations, including errors. In those papers, and in Bu et al. (2017), many of the contributing matrices and vectors are considered to be standard forms for well-understood optics. In that sense, these works are a detailed forward-looking development intended to
- 30 account for possible errors in known parameters (e.g. introducing a term for error in the rotation of transmitter with respect to receiver, and then determining it for their lidar). For CRL, we also take the Mueller Matrix approach. We particularly follow the lead of Hayman and Thayer (2009, 2012) with regards to the mathematics, but with the opposite perspective: We initially presume to know nothing about the elements of the receiver optics Mueller Matrix, and then we measure them.

### 1.3 Mueller Matrix calibration goals for CRL

For the CRL, our approach is to use Mueller Matrix mathematics to more fully diagnose the optical properties of CRL's receiver as a whole, similar to the approach taken by Di et al. (2016) and Liu and Wang (2013). We do not require the specific contributions of each receiver optic in order to understand our measurements for d. Nor do we need to split the matrices into equivalent standard optics (e.g. Hayman and Thayer (2012), which describes optics as combinations of retarders, polarizers,

etc.). Neither do any of the specific examples given in Freudenthaler (2016) adequately describe the CRL.

The first goal for this paper is to use Mueller Matrix algebra to re-derive the equation for d, including calibration terms which describe the arbitrary optical effects of the upstream optics. These terms allow the collection of upstream optics to be represented using the most general single Mueller Matrix possible (See Sect. 3.1, Eq. (12)). We make no prior assumptions

10 regarding rotation, retardation, polarization properties of the optics. The beamsplitter and laser polarizations are assumed to be ideal in our expressions.

The second goal is to use calibrations to measure the relevant matrix elements for the upstream optics which will indicate whether or not the overall impact of CRL's optics is that of a partial polarizer. If not, and it shows behaviour similar to that of a wave plate or a polarization rotator, then Eq. (2) and Eq. (3) are insufficient to describe the depolarization parameter

- 15 and depolarization ratio for CRL, and the full equations for *d* from Sect. 3.1 will be required for routine measurements. The main tests introduce light of known polarization to the detector at a variety of rotation angles. This is generated by putting unpolarized light through a polarizing cube beamsplitter. Some compromises must be made, as we must at times exclude the telescope and focus stage from our calibrations, similar to calibrations made by Platt (1977); Spinhirne et al. (1982); Sassen and Benson (2001); Wang et al. (2009); Bravo-Aranda et al. (2013, 2016) and others. With careful characterisation of the remainder
- 20 of the lidar receiver, we show that the overall contribution of the optics is indeed found to conform to that of a partial polarizer, rendering Eq. (2) and Eq. (3) appropriate for CRL.

Third, we find the appropriate calibration constant k for the whole receiver, including the telescope and focus stage, and using the laser as a light source, and using a sheet depolarizer to force all light entering the receiver to be unpolarized.

Fourth, we carry out additional unpolarized-light tests to determine the contributions that individual optics make to the overall large k value for CRL. The largest contributor to k for CRL was found to be the Visible Long Wave Pass filter (Sect.

7.2, and Table 1).

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Finally, we demonstrate the use of the CRL's newly calibrated depolarization capability by showing some example measurements of ice clouds from 12 March 2013 in Sect. 8. The result for the CRL is a new depolarization data product tied into a scientifically significant long-term measurement record, all without compromise to the continued acquisition of the original

30 types of data. To date, linear depolarization measurements have been made for four polar sunrise seasonal campaigns at Eureka: 2013, 2014, 2016, and 2017 (no measurements were obtained during 2015 because no operator was available).

### 2 Installation of depolarization hardware

To make depolarization measurements, the lidar must be able to distinguish between backscattered light which is polarized parallel to the outgoing laser light, and that which is returned unpolarized. To this end, we make measurements in two orthogonal polarization planes: One parallel to the polarization plane of the outgoing laser light, and the other perpendicular to this

5 plane. While a polarizing beamsplitter and two additional photomultiplier tubes (PMTs) would accomplish this requirement, we opted to use a rotating polarizer which permits lidar returns in two orthogonal polarization planes to be measured by a single detector in an automated version of the measurement approach used in the very first depolarization lidars (Schotland et al., 1971). This design reduces the number of differences between the hardware of both depolarization channels because the backscattered light traverses identical optics and uses the same photomultiplier tube. Given that the basic depolarization calculation.

The priority during installation of the polarization capability was not to impact any of the well-calibrated measurements in the other pre-existing lidar channels (Nott et al., 2012). No optics for the other channels were changed or removed during the installation of the depolarization channel, as these changes could have affected the other measurements.

### 2.1 Polarotor

- 15 The Licel Polarotor rotating polarizer (Licel GmbH, 2006) was designed specifically for multispectral detection systems such as that of CRL. The polarotor acts as the master trigger for the lidar. Its  $\alpha$ -BBO Glan Thompson prism is spun steadily at high speed, and a synchronization pulse from the built-in timing disk triggers the lidar system at 10 Hz. This trigger signals the laser to fire and the detectors to record every time the prism rotates through 90°. The PMT is exposed to backscattered laser light which is polarized parallel to, and perpendicular to, the outgoing laser light, on alternate laser shots. Two recording buffers
- are used in the Licel Transient Recorder, one for parallel and one for perpendicular photocount profiles. The extinction ratio of the polarizer was characterized by the manufacturer to be  $5 \times 10^{-5}$  or smaller (Licel GmbH, 2006), leading to high-quality separation of the polarization states.

### 2.2 Positioning of depolarization channel within CRL

During manufacture, the CRL polychromator had two spare locations for potential expansion of the lidar. The depolarization channel was installed in the spare location between the 532 nm Visible Rayleigh Elastic channel and the 607 nm Nitrogen channel (Fig. 1). This location is on the visible light side of the polychromator, but it suffers from being "downstream" of many optics. The original Chroma 580DCLP Visible Long Wave Pass (VLWP) filter was chosen in 2007 specifically to reflect as much 532 nm light into the original Visible Rayleigh Elastic channel as possible (approximately 97 %). Part of this reflected light is used in two subsequent visible channels at 531.2 nm and 528.7 nm, thus the requirement for maximum reflectivity

30 around 532 nm for the VLWP (Nott et al., 2012). The depolarization channel uses the small amount of residual 532 nm light which is transmitted through this VLWP filter on its way to the 607 nm channel, where it would normally be rejected by the 607 nm channel's interference filter.

During depolarization channel installation, a partially reflective optic was installed to redirect the residual 532 nm light into the depolarization channel, allowing the 607 nm light to continue on to the final PMT. The 607 nm channel optics were already well aligned and characterized at the time of depolarization installation (Doyle et al., 2011; Nott et al., 2012). Therefore, a regular plate beamsplitter or dichroic mirror could not be used to pick off the light for the depolarization channel; this would

5 have translated the transmitted 607 nm light too much, and the downstream channel would have had to be realigned. A 3" CVI–Melles Griot 633 nm 50/50 pellicle beamsplitter is the most non-polarizing option available at 532 nm in reflectance, which still allows as much 607 nm light through as possible, with the smallest possible beam translation.

From the pellicle beamsplitter, the 532 nm light travels into the polarotor which is mounted on top of the polychromator. It sits on a 2" diameter beamtube which is 3" tall. The diameter of the light beam is slightly larger than 2" at the pellicle and, due

- 10 to a collimating lens just upstream of the pellicle, is slightly converging. The polarotor has an acceptance diameter of 20 mm, and a full acceptance angle of 15°. By placing the polarotor a sufficient distance from the pellicle, the entire beam is accepted by the polarotor without the need for extra optics in between. It is also convenient to have the cables from the polarotor to the electronics rack be accessible without the need to open the polychromator.
- Above the polarotor, there is a beamtube containing an interference filter, then a 1" diameter beamtube containing a 75 mm
  focusing planoconvex lens. Next, there is an adjustable focusing tube in which the Hamamatsu R7400-03 PMT is seated, which allows the active area of the photomultiplier tube to be positioned at an appropriate distance from the focusing lens. The interference filter specifications are: Andover Corporation Part Number 532FS02-25, 25 mm diameter, BW 1±0.2 nm centered at 532.0±0.2 nm, transmission greater than 45 %, 1×10<sup>-4</sup> average blocking from X-ray to far infrared wavelengths (Andover Corporation, 2015).

### 20 2.3 Start Delay calibration to define the "parallel" polarotor rotation angle

The polarotor is set to spin at a 2.5 Hz (1.11 ms/degree of rotation). It can be set to trigger the laser from any polarizer angle. Timing in the polarotor is controlled by a timing disk with four indicators 90° apart, each of which can trigger the laser. Thus, once we set the rotation angle such that trigger 1 corresponds with "parallel", triggers 2, 3, and 4 correspond automatically to perpendicular, parallel, and perpendicular respectively, each 90° of rotation after the other. One consequence of this arrangement is that although there may be error in the absolute angle during each measurement, the parallel and perpendicular

channels are exactly  $90^{\circ}$  apart.

In practice for the CRL, the reference rotation angle is controlled by the "start delay" time between the trigger pulse from the polarotor and the time the laser fires. We perform a calibration to define the angle of rotation at which the polarotor's prism needs to be in order for the parallel measurement channel to correspond with the polarized backscatter returns from the laser

beam. In this manner we effectively align our polarizer with the plane of polarization of the laser as it is transmitted to the sky.

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Start delay calibration measurements are made in a dark, clear sky, where the depolarization parameter should be approximately 0. Measurements are taken in both depolarization channels for several minutes at each of many start delay settings. The optimal start delay setting occurs at the location of maximum contrast, where as much of the clear sky signal as possible enters through the parallel channel, and as little as possible enters via the perpendicular channel. In Eureka we work on a campaign basis, so it is not possible to wait months for the perfect clear day to do this measurement. We reduce the effects of any clouds, aerosols, or other depolarizing particle, by using only values from a certain altitude range of interest which does not include clouds, and by using the Polarization-Independent Rayleigh Elastic channel as a check to indicate times where our calibration may be invalid. It is helpful to divide the photon count rates of parallel and perpendicular by the count rates in the

5 polarization-independent channel to eliminate the effect of laser power variations. If the sky depolarization is not truly zero for this test, some systematic error will be induced in all subsequent calibrated measurements of sky depolarization.

From the test, we obtain two cosine curves of photocounts as a function of polarotor start delay: One for parallel, and the other for perpendicular,  $180^{\circ}$  out of phase with one another. A fit to each curve allows us to find the start delay value.

Our start delay test is carried out in start delay steps of  $2560 \,\mu$ s, with allowable start delay values between  $20 \,\mu$ s and  $419000 \,\mu$ s, as this has sufficient resolution to determine the correct start delay while requiring few enough settings that the

10 419000 µs, as this has sufficient resolution to determine the correct start delay while requiring few enough settings that the calibration may be carried out during a single night. This test needs to be repeated any time the polarotor is uninstalled or reinstalled into the polychromator.

# 2.4 Effects of polarotor rotation angle errors on depolarization measurements

If we consider the angular start delay error to be equal to one-half of our measurement step size of 2560 μs, corresponding to
1.408° of error, we have the following errors in d: The worst case scenario is that for which d = 0. There, a 1.408° angle error corresponds to an error of ±0.0006. For d = 1, there is no uncertainty in d from this source. For a typical value of d = 0.2 the uncertainty is ±0.0005.

Next, we investigated the effect of the rotation of the polarizer during each laser shot measurement and found that has negligible impact on our interpretation of d. Again considering the worst offending case, that in which d = 0: A two-way maximum photon travel time for 16000 altitude bins is 0.0008 s, during which the polarotor rotates through 0.88°. The induced

20 maximum photon travel time for 16000 altitude bins is 0.0008 s, during which the polarotor rotates through  $0.88^{\circ}$ . The induced change in *d* (in units of *d*) results in an uncertainty in *d* such that  $d = 0.0000 \pm 0.0005$ . The more diagnostic case d = 0.2 results in  $d = 0.2 \pm 0.0004$ .

When combined, the rotational errors of the polarotor considered in this section contribute a maximum of total error of 2.288°, making the error from these sources approximately equal to ±0.003 for typical measured values of d. To put this in 25 context, other errors (see Sect. 8) contribute ±0.1 to ±0.2.

# **3** Theory for depolarization calculations

### 3.1 Mueller Matrix development

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A Mueller Matrix approach was used to understand the signals being measured by the depolarization channel, with as few simplifications and assumptions as possible. In the case of atmospheric lidar operation, the original laser light is described as a Stokes vector which will be operated on by several optical elements, each of which can be described by a  $4 \times 4$  matrix. We can

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thus determine the Stokes vector of the light which enters the PMTs, and predict the signal which will be measured in each of our channels:  $S_{\parallel}$  (parallel channel measurement), and  $S_{\perp}$  (perpendicular channel measurement).

In its most basic format, Mueller algebra functions as: L' = ML, in which L and L' are the Stokes vectors of incident and emerging radiation, respectively, and M is the  $4 \times 4$  real matrix effect of the instrument (Parke III, 1948). Stokes vectors add incoherently, and therefore the effect of any two components in series is equal to the product of their matrices. Thus, M can represent the product of two or more different optical matrices. Stated in terms of a matrix equation, the effects of the atmosphere  $M_{\text{atm}}$  and of the lidar's receiver optics  $M_{\text{receiver}}$  on the emitted laser light are:  $I_{\text{measured}} = M_{\text{receiver}}M_{\text{atm}}M_{\text{transmitter}}I_{\text{laser}}$ .

The CRL laser emits horizontally linearly polarized light, nominally  $I_{\text{laser}} = I_{\text{laser}} [1 \ 1 \ 0 \ 0]'$ . The laser intensity  $I_{\text{laser}}$  varies shot-to-shot with such quantities as laser voltage and flashlamp age. Using alternate laser shots to build up 300 shot sums

- 5 in each parallel and perpendicular in each one minute lidar scan allows these channels to measure simultaneously. Taking many shots into each sum allows the short timescale (< 1 second) laser voltage variations to average out in each measurement. Therefore,  $I_{\text{laser}}$  can be considered the same for both channels for each measurement pair. The polarization of the laser was measured with a cubic polarizing beamsplitter on a kinematic mount placed in front of a power meter which is permanently mounted on the optical table. A mirror wheel redirects the beam into the power meter from a location partway through the
- 10 transmitter. The precise location can be found in Nott et al. (2012). Thus, the polarization tests take into account all but four transmission optics on the optical table, as well as the one extra optic of the redirection mirror. This location is not ideal, but is accessible in this installation. The first three elements of the resulting normalized Stokes vector [*I*,*Q*,*U*,*V*]' were calculated at two laser powers. At lower power: [*I*,*Q*,*U*,*V*]' = [1±0,1.00±0.02,0.02±0.01,*V*±σV]'. At higher power: [*I*,*Q*,*U*,*V*] = [1±0,0.97±0.01,0.00±0.01, V±σV]'. Our test was not directly sensitive to the value of *V*. Since Q<sup>2</sup> + U<sup>2</sup> + V<sup>2</sup> ≤ I<sup>2</sup>, we
  15 can surmise that |*V*| ≤ 0.243. We consider *I*<sub>laser</sub> = *I*<sub>laser</sub>[1 1 0 0]' to be a reasonable laser Stokes vector for the calculations in

this paper.

The optical backscattering effects of the atmosphere can be described as  $\mathbf{M}_{\text{atm}}$ . Some authors assume ensembles of spheres, and others the full normalized backscattering matrix for any shape of particle (Mishchenko and Hovenier, 1995). The latter is similar to the description in van de Hulst (1957), who describes a matrix specifically for backscattering of a cloud of asymmetrical particles with rotational symmetry, for which each particle has a mirror particle, and where there is no preferred orientation. Such is the case for the left matrix in Eq. (5), which can be fully described by two scalar values  $a_1$  and  $a_2$ . Particularly interesting are changes in polarization during the scattering events. Gimmestad (2008) introduces variable d such

that the scattering matrix is normalized to have an intensity of 1. For generality, we include here a gain factor, *b*. The gain factor is not stable long term, but for any given minute of data it will be constant for both channels. Under these assumptions *b* cancels

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from the equations, demonstrating that the absolute scattering efficiency of the atmosphere has no effect on the measurements of depolarization.

$$\mathbf{M}_{\text{atm}} = \begin{pmatrix} a_1 & 0 & 0 & 0 \\ 0 & a_2 & 0 & 0 \\ 0 & 0 & -a_2 & 0 \\ 0 & 0 & 0 & a_1 - a_2 \end{pmatrix} = b \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 - d & 0 & 0 \\ 0 & 0 & d - 1 & 0 \\ 0 & 0 & 0 & 2d - 1 \end{pmatrix}$$
(5)

In Eq. (5) the quantity d is the depolarization parameter for the atmosphere above the lidar, as described in Eq. (2), and describes the extent to which the transmitted light has been depolarized by the atmosphere.

The backscattered light already acted upon by  $\mathbf{M}_{atm}$  passes through a first set of receiver optics which are shared by both the parallel and perpendicular beam paths: telescope, focus stage, beamsplitters, long-wave-pass filters, etc. We account for these upstream optics together as a  $4 \times 4$  matrix,  $\mathbf{M}_{upstream}$ , but we make no assumptions as to the values of the matrix elements:

$$\mathbf{M}_{\text{upstream}} = \begin{pmatrix} M_{00} & M_{01} & M_{02} & M_{03} \\ M_{10} & M_{11} & M_{12} & M_{13} \\ M_{20} & M_{21} & M_{22} & M_{23} \\ M_{30} & M_{31} & M_{32} & M_{33} \end{pmatrix}.$$
(6)

There is also the possibility of an instrumental influence which varies with altitude z: Geometric overlap is such a term, and is the largest influence in CRL's height-dependent calibration vector. Hence, all height-dependent variations will be attributed to geometric overlap, and we will subsequently call this the "overlap function", O(z). The overlap varies with changes to the lidar's alignment, so calibration values must be applied to measurements made within an appropriate time window (as alignment can change slowly with laboratory temperature), and must be re-determined after every routine alignment adjustment

15 procedure.

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Next, the light passes through the Glan–Thompson prism of the Licel Polarotor. This prism acts as either a horizontal or a vertical analyzing polarizer (for the parallel  $(\mathbf{M}_{\parallel})$  and perpendicular  $(\mathbf{M}_{\perp})$  measurement channels, respectively) depending on its orientation at a particular time. The laser beam has linear polarization in the horizontal direction. During setup, the "parallel" analyzer position was also oriented such that it can be represented as a horizontal polarizer (by aligning the parallel

20 direction with the direction of maximum signal in a low depolarization sky).

Finally, the light passes through the focusing lens and neutral density filter of the PMT tube, and onto the PMT itself. The lens is axially symmetric, and the neutral density filter is used at normal incidence. Therefore, the effect of these optics on any incident light will be identical regardless of incoming polarization orientation. These optics are downstream of the analyzing polarizer, so any rotation of the plane of polarization by these optics will have no impact on the signal registered by

- 5 the PMT, and is therefore unimportant. The only effect of these optics is to reduce the amplitude of the signal by a constant factor regardless of incoming polarization. They are well-described as a constant scalar factor. For lidars which have physically separate detectors or optical paths for the parallel and perpendicular channels, one such scalar factor will be required for each:  $G_{PMT\parallel}$  and  $G_{PMT\perp}$ . These terms are identical and cancel out of the equations below for CRL, but will be included explicitly in the equations below as long as possible for generality.
- 10 These Mueller matrices combine to make an overall equation for each channel which describes the action of all optical components on the light, and results in Stokes vectors  $I_{\parallel}$  (shown in full in Eq. (8)) and  $I_{\perp}$  (which differs from  $I_{\parallel}$  only by two minus signs in the polarizer matrix):

$$\boldsymbol{I}_{\parallel} = \frac{G_{\text{PMT}\parallel}}{2} \begin{pmatrix} 1 \ 1 \ 0 \ 0 \\ 1 \ 1 \ 0 \\ 0 \ 0 \ 0 \\ 0 \ 0 \ 0 \end{pmatrix} \begin{pmatrix} M_{00} \ M_{01} \ M_{02} \ M_{03} \\ M_{10} \ M_{11} \ M_{12} \ M_{13} \\ M_{20} \ M_{21} \ M_{22} \ M_{23} \\ M_{30} \ M_{31} \ M_{32} \ M_{33} \end{pmatrix} bO_{\parallel\perp}(z) \begin{pmatrix} 1 \ 0 \ 0 \ 0 \\ 0 \ 1-d \ 0 \ 0 \\ 0 \ 0 \ d-1 \ 0 \\ 0 \ 0 \ 0 \ 2d-1 \end{pmatrix} I_{\text{laser}} \begin{pmatrix} 1 \\ 1 \\ 0 \\ 0 \end{pmatrix}.$$
(8)

The signal  $S_{\parallel}$  measured by the lidar is the intensity element of the Stokes vector  $I_{\parallel}$ :

15 
$$S_{\parallel} = \frac{G_{\text{PMT}\parallel}bO_{\parallel\perp}(z)I_{\text{laser}}}{2}(M_{00} + M_{10} + (M_{01} + M_{11})(1 - d)).$$
 (9)

Similarly,  $S_{\perp}$  is the intensity element of the Stokes vector  $I_{\perp}$ :

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$$S_{\perp} = \frac{G_{\text{PMT}\perp} b O_{\parallel\perp}(z) I_{\text{laser}}}{2} (M_{00} - M_{10} + (M_{01} - M_{11})(1 - d)).$$
<sup>(10)</sup>

Using the signals  $S_{\parallel}$  and  $S_{\perp}$  from above for the complete matrix description of the lidar, we solve for the depolarization parameter d. The simplest method for combining lidar signals  $S_{\parallel}$  and  $S_{\perp}$  into an equation for depolarization parameter comes from creating the quantity

$$\frac{S_{\parallel} - S_{\perp}}{S_{\parallel} + S_{\perp}} = \frac{M_{10} + M_{11}(1 - d)}{M_{00} + M_{01}(1 - d)},\tag{11}$$

realizing that  $G_{PMT\perp} = G_{PMT\parallel} = G_{PMT\parallel\perp}$  for CRL because both channels are physically the same PMTs. Solving for d yields Eq. (12):

$$d = 1 - \frac{\frac{M_{10}}{M_{00}} \left(1 + \frac{S_{\perp}}{S_{\parallel}}\right) - \left(1 - \frac{S_{\perp}}{S_{\parallel}}\right)}{\frac{M_{01}}{M_{00}} \left(1 - \frac{S_{\perp}}{S_{\parallel}}\right) - \frac{M_{11}}{M_{00}} \left(1 + \frac{S_{\perp}}{S_{\parallel}}\right)}.$$
(12)

For calibration, we must determine the three instrument constants  $\frac{M_{01}}{M_{00}}$ ,  $\frac{M_{10}}{M_{00}}$ , and  $\frac{M_{11}}{M_{00}}$ . Note that we do not require the  $M_{xx}$  values individually, nor do we need to know the laser intensity.

### 3.2 Conditions under which the traditional equations are appropriate

Under the mathematical conditions  $M_{01} = M_{10}$  and  $M_{11} = M_{00}$ , the traditional expression for d (Eq. (2)) is equivalent to the more complete expression for d (Eq. (12)). In the case that CRL meets these conditions, it will be acceptable to use Eq. (2) in further calculations for this lidar. The matrix form of  $\mathbf{M}_{upstream}$  which is required for this condition has the effect of a partial polarizer on measurements of d: it acts with gain  $G_{up\parallel}$  for light polarized in the parallel direction, and  $G_{up\perp}$  for that polarized

perpendicularly. Under these simplified conditions, the relation between k and  $M_{xx}$  is:

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$$\frac{G_{\rm up}}{G_{\rm up}} = \frac{M_{00} + M_{01}}{M_{00} - M_{01}} = \frac{1 + \frac{M_{01}}{M_{00}}}{1 - \frac{M_{01}}{M_{00}}} = k.$$
(13)

Calibrations described in Sect. 5 demonstrate that the  $M_{01} = M_{10}$  and  $M_{11} = M_{00}$  conditions are met for CRL, allowing Eq. (3) to be used for the calculation of depolarization ratio, and Eq. (2) for depolarization parameter.

### 10 4 Optics for generating polarized and depolarized light during calibrations

Instrument calibration tests to determine k and the  $M_{xx}$  and  $G_{xx}$  values for CRL are described in the following sections. To carry out these tests, some additional calibration optics must be temporarily added to the lidar.

Calibration cube polarizer: The generating polarizer is a Newport 10BC16PC.3 Pol Cube Beamsplitter, 532 nm, 25.4 mm, Tp/Ts> 1000 : 1, a linearly polarizing cubic prism. It is placed immediately downstream of the focus stage (location label 7 in Fig. 1) and is rotated by hand. The rotating mount has markings in 2° steps, and there is about half a step of uncertainty in either direction, hence ± 1° uncertainty in the rotation angles θ.

The matrix describing the cube polarizer, allowing for an attenuation factor  $G_{\text{cube}}$ , is:

$$\mathbf{M}_{\text{cube}} = \frac{G_{\text{cube}}}{2} \begin{pmatrix} 1 & \cos 2\theta & \sin 2\theta & 0\\ \cos 2\theta & \cos^2 2\theta & \frac{1}{2}\sin 4\theta & 0\\ \sin 2\theta & \frac{1}{2}\sin 4\theta & \sin^2 2\theta & 0\\ 0 & 0 & 0 & 0 \end{pmatrix}.$$
 (14)

2. Glassine waxed paper depolarizer: Typically used to protect works of art, the depolarizing properties of Lineco Glassine 20 (Lineco Glassine Acid Free Tissue 16"  $\times$  20", 12 pack, product number 448-1626) were found to be highly satisfactory. As 20 tested by our group, after one sheet of glassine the residual polarisation is less than 1% (Polarization = 0.009 ± 0.006). Full 21 details of this characterization are available in McCullough (2015), Chapter 4.6.2.1 "Calibration tests of the optical qualities 22 of glassine waxed paper". The depolarizing properties were not affected by the product's exposure to damp, nor to wetting and 23 subsequent drying out. This product was mounted in such a way as to be held relatively taut in a frame, or held in place by other

25 mechanical means, depending on the specific calibration test. See McCullough (2015) for photographs of the arrangements used for the calibrations in this paper. Glassine is highly scattering material, so when the entire roof hatch window is covered with it, the received lidar signal is greatly reduced. The matrix for a perfect depolarizer with an attenuation parameter  $G_{gl}$  which is applicable to a real depolarizing optic (in this case, glassine waxed paper), is:

3. Industrial kitchen grade waxed paper: The depolarizing properties of this product were used for CRL calibrations before we were aware of glassine, which turned out to be the superior material. The depolarizing properties of various brands of waxed paper, and from batch to batch within a particular brand, vary widely; verification for each application is advisable. As for glassine, waxed paper is a highly scattering material which greatly reduces received lidar signals when they are measured with the waxed paper in place.

### 5 Calibrations to determine whether traditional equations are acceptable

10 Introducing polarized lamp or laser light to the detector provides the calibration values which indicate whether the simple equations are satisfactory for CRL, by testing whether the conditions  $M_{01} = M_{10}$  and  $M_{11} = M_{00}$  are satisfied.

# 5.1 Physical setup of the rotating polarizer test used at CRL

A light source (lamp or backscattered laser) is directed through two layers of glassine depolarizer sheet into a polarizationgenerating optic and through to the lidar's receiver system. The polarization generator is rotated through various angles  $\theta$  with

15 respect to the plane of polarization of the parallel channel, and signals are measured in the parallel and perpendicular channels as a function of this angle (Fig. 2). The glassine ensures that unpolarized light enters the polarizer, and thus we begin with equal numbers of photons exiting the polarizer regardless of its orientation.

Ideally, as many optics as possible are included after the polarization generating calibration optic, so that the contributions of as many "upstream optics" as possible are included in the Mueller Matrix  $\mathbf{M}_{upstream}$  during calibration. In practice, this is

- 20 difficult to accomplish for practical reasons at CRL. A light source which illuminates the entire 1 m CRL telescope is available if we employ backscattered laser light. A 1 m depolarizing optic to initially depolarize all the backscattered light received at the roof hatch level is also available (glassine waxed paper sheets). The problem is that no feasible polarizing optic has the required properties. We require a 1 m diameter optic which can be held completely flat and which can survive the harsh outdoor conditions of Arctic winter. The polarizing optic must be able to be easily and repeatably rotated to the appropriate orientation,
- and should have sufficient optical polarization quality. A variety of setups using sheet polarizers were attempted to overcome these problems, and none produced satisfactory results. Neither did the use of a smaller 25 cm diameter sheet polarizer installed in a smaller aperture above the lidar's telescope, with the rest of the entrance to the primary mirror masked. Repeating the test with the sheet polarizer held between the telescope's tertiary mirror and the focus stage worked better (location label 8 in Fig. 1), but still relied on a suboptimal optical quality sheet polarizer.

By removing the roof window, the lidar's telescope, and the focus stage from consideration in the calibration, the rotating polarizer test becomes possible at CRL. By the time the light reaches the entrance to the polychromator, the received light beam, originally 1 m diameter, is focused small enough to allow the use of the 25 mm polarizing cube beamsplitter of high optical quality described in Sect. 4. The cube beamsplitter can be rotated precisely and is stably mounted on a kinematic rotation mount on a 2" beam tube which leads into the polychromator from the focus stage (location label 7 in Fig. 1).

5 rot

The telescope and focus stage are being omitted in the test. If the lidar return were used as the light source, we could still take into account the height dependency of the optics. Light collected from different heights has different lightpaths and different incidence angles in the receiving modules (Freudenthaler, 2016), and this may have effects on the calibration. While there are in principle advantages to including any height dependent effects, in practice the glassine waxed paper depolarizer attenuates

- 10 the backscattered laser signal too much to be of use in the practical case for a laser of CRL's power in clear skies. Additionally, the atmospheric conditions would need to remain stable throughout the test. Thus, there is little advantage to using lidar returns as the light source; a current-stabilized constant lamp source provides more signal with better control of the experimental setup. It also does not rely on specific atmospheric conditions. The lamp is installed on the telescope frame such that it shines through a glassine depolarizing sheet held taut in a frame of foamcore between the tertiary telescope mirror and the focus stage
- 15 (location label 8 in Fig. 1). The resulting unpolarized light is sent through the focus stage, then through the cube polarizer, which produces the linearly polarized light which is sent through the rest of the polychromator, including the rotating Polarotor polarizer, and into the PMT.

Omitting the first optics in the detector chain means that this test does not give us a whole-system understanding, although it does allow us to say with certainty whether the downstream optics are contributing any effects other than relative gain (e.g. retardation, rotation, etc.) to the signals.

20 retardation, rotation, etc.) to the signals.

We pose the question, "If we consider the optics and detector starting after the focus stage, can we use the simplified Eq. (3) and Eq. (2) to find the calibration constant, and then to determine depolarization ratio and depolarization parameter?". This is answered in the remainder of Sect. 5. If yes, we can then ask "What is the best estimate for a polarization calibration constant which represents the entire system?", which is addressed in Sect. 6.

# 25 5.2 Matrix description and results of polarized light calibration

Linearly polarized light is introduced to the receiver. The orientation of the plane of polarization of this light is described as angle  $\theta$  with respect to the plane of polarization of the parallel channel. Then measurements are made in the parallel and

perpendicular channels. In this scenario, the final Stokes vectors are:

with corresponding signals:

5 
$$S_{\parallel\theta} = G_{\text{cube}} G_{\text{PMT}\parallel} G_{\text{gl}} \frac{I_{\text{lamp}}}{4} \left( M_{00} + M_{10} + (M_{01} + M_{11}) \cos 2\theta + (M_{02} + M_{12}) \sin 2\theta \right)$$
 (18)

$$S_{\perp\theta} = G_{\text{cube}} G_{\text{PMT}\perp} G_{\text{gl}} \frac{I_{\text{lamp}}}{4} \left( M_{00} - M_{10} + (M_{01} - M_{11}) \cos 2\theta + (M_{02} - M_{12}) \sin 2\theta \right).$$
(19)

There are very similar equations for the case in which we use backscattered laser light rather than lamp light.

The results of such a test from 5 March 2014 are plotted in Fig. 2. This plot shows the signals in the parallel channel (blue points) and in the perpendicular channel (red points) as a function of cube polarizer angle  $\theta$ . The cube polarizer was initially placed at an arbitrary angle to ensure that photons were visible in each channel. It was then rotated through a number of steps, spending several minutes at each angle. In total, it was rotated through just more than one full rotation, or  $2\pi$  radians. The absolute angles were determined in post-processing, such that the maximum in the parallel channel is  $\theta = 0$ . All measurements for each angle  $\theta$  have been combined for this plot. Photocounts are indicated in units of "photons per time bin per altitude bin", at a resolution of  $1 \min \times 7.5 m$  for each bin. There is approximately a 2° or 0.035 radian uncertainty in the rotation angles of the calibration cube polarizer when doing this calibration. Note the different scales for each panel in Fig. 2: The overall signals

in  $S_{\parallel}$  far exceed the overall signals  $S_{\perp}$ .

25

We could attempt to estimate all 7 unknown terms in Eq. (18) and Eq. (19) by allowing them as free parameters in a fit to these signals, but this does not return a unique solution. For CRL, there is a better way to proceed: Signal values at some diagnostic angles simplify the equations a great deal by constraining certain calibration constants.

# 20 5.2.1 First constraint: $M_{02} = 0$ and $M_{12} = 0$

The signal equations, Eq. (18) and Eq. (19), are simplified a great deal if  $M_{02} = 0$  and  $M_{12} = 0$ . There is no requirement that the constants  $M_{02}$  or  $M_{12}$  have these values for given lidar, but a test can verify whether it is the case:  $M_{02}$  and  $M_{12}$  will both be equal to zero if there is symmetry about  $\theta = \pi/2$  in the curves of both of the signals in Fig. 2, and in particular if the signals at  $\theta = \frac{\pi}{4}$  equal those at  $\theta = \frac{3\pi}{4}$  for both the parallel and the perpendicular. The results of these measurements are given in Table 2.



**Figure 2.** Polarized calibration measurements as a function of incident light polarization angle. Photocounts are given per 1 min, 7.5 m altitude bin. At angle  $\theta = 0$ , the calibration cube polarizer is aligned completely with the parallel measurement channel. At  $\theta = 0.5\pi$ , it is aligned completely with the perpendicular channel. The greyscale points indicate the extent of scatter in the measurements for each channel. The colourbar indicates the natural logarithm of the number of data points at each location, which is the result of producing a histogram for each angle  $\theta$ . Data points from from all 16000 altitude bins, for all individual minutes of measurement at the angle theta (typically 3 to 5 min), is included in the histograms. The truncated distribution of points (because only positive photons may be measured) is evident. Each histogram was fit with a 6th order polynomial in order to determine the location of the peak photocount rate. This often differed significantly from the mean of the photocount values at that angle, and was taken to be the most probable value. The most probable photocount values are given by the blue points (parallel channel; panel (a)) and red points (perpendicular channel; panel (b)). The thick blue and red lines trace these data points as a visual aid; they are not fit lines. The thin blue and red lines give the  $\pm 1\sigma$  standard deviation of the point distribution at each angle. Note the different y-axis limits for each plot; the parallel count rates are far larger than the perpendicular count rates.

For the parallel channel, the signals at these angles are:

$$S_{\parallel \theta = \frac{\pi}{4}} = G_{\text{cube}} G_{\text{PMT}\parallel} G_{\text{gl}} \frac{I_{\text{lamp}}}{4} \left( M_{00} + M_{10} + (M_{02} + M_{12}) \right)$$
(20)

$$S_{\parallel \theta = \frac{3\pi}{4}} = G_{\text{cube}} G_{\text{PMT}\parallel} G_{\text{gl}} \frac{I_{\text{lamp}}}{4} \left( M_{00} + M_{10} - (M_{02} + M_{12}) \right)_{19}$$
(21)

If our measurements are symmetric, with  $S_{\parallel \theta = \frac{\pi}{d}} = S_{\parallel \theta = \frac{3\pi}{d}}$ , then  $M_{02} = -M_{12}$ .

For the perpendicular channel,

15

$$S_{\perp \theta = \frac{\pi}{4}} = G_{\text{cube}} G_{\text{PMT}\perp} G_{\text{gl}} \frac{I_{\text{lamp}}}{4} \left( M_{00} - M_{10} + (M_{02} - M_{12}) \right)$$
(22)

$$S_{\perp \theta = \frac{3\pi}{4}} = G_{\text{cube}} G_{\text{PMT}\perp} G_{\text{gl}} \frac{I_{\text{lamp}}}{4} \left( M_{00} - M_{10} - (M_{02} - M_{12}) \right).$$
(23)

5 If our measurements are symmetric, with  $S_{\perp \theta = \frac{\pi}{4}} = S_{\perp \theta = \frac{3\pi}{4}}$ , then  $M_{02} = M_{12}$ .

Because the values for  $M_{02}$  and  $M_{12}$  must not change and are in common for parallel and perpendicular, then if *both* parallel and perpendicular are symmetric, both  $M_{02} = -M_{12}$  and  $M_{02} = M_{12}$  must be true simultaneously, so  $M_{02} = -M_{02}$  and  $M_{12} = -M_{12}$ . Thus,  $M_{02} = 0$  and  $M_{12} = 0$ .

This simplifies the calibration signal equations to:

10 
$$S_{\parallel\theta} = G_{\text{cube}} G_{\text{PMT}\parallel} G_{\text{gl}} \frac{I_{\text{lamp}}}{4} \left( M_{00} + M_{10} + (M_{01} + M_{11}) \cos 2\theta \right)$$
 (24)

$$S_{\perp\theta} = G_{\text{cube}} G_{\text{PMT}\perp} G_{\text{gl}} \frac{I_{\text{lamp}}}{4} \left( M_{00} - M_{10} + (M_{01} - M_{11}) \cos 2\theta \right)$$
(25)

Each channel's signal values at  $\theta = \frac{\pi}{4}$  and  $\theta = \frac{3\pi}{4}$  are equal within their respective uncertainties (Table 2). The mean signal values are  $S_{\parallel} = 9 \pm 1$  for parallel, and  $S_{\perp} = 0.8 \pm 0.5$  for perpendicular, with uncertainties calculated using standard error propagation. Therefore, both channels are symmetric about  $\theta = \pi/2$ , and the first simplification may be used. Hence, we see that for CRL,  $M_{02} = 0$  and  $M_{12} = 0$  are valid for the conditions of this test.

At this point, it is possible to combine Eq. (24) and Eq. (25) into one equation which includes both signals and only the desired calibration constants  $\frac{M_{10}}{M_{00}}$ ,  $\frac{M_{01}}{M_{00}}$ , and  $\frac{M_{11}}{M_{00}}$  which remain to be determined by a fit to the resulting curve:

$$\frac{S_{\parallel\theta} - S_{\perp\theta}}{S_{\parallel\theta} + S_{\perp\theta}} = \frac{\frac{M_{10}}{M_{00}} + \frac{M_{11}}{M_{00}} \cos 2\theta}{1 + \frac{M_{01}}{M_{00}} \cos 2\theta}.$$
(26)

Again, there is not a unique solution if all three calibration coefficients are free parameters in the fit. It is preferable to see 20 whether the signal measurements indicate any further constraints.

### 5.2.2 Second constraint: $M_{10} = M_{01}$ and $M_{00} = M_{11}$

Further simplifications may be made if the parallel and perpendicular channel signals each go to zero at their respective minima. For parallel, this is at integer multiples of  $\theta = \frac{\pi}{2}$ , where  $\cos 2\theta = -1$ . For perpendicular, this is at  $\theta = 0$  and at integer multiples of  $\theta = \pi$ , where  $\cos 2\theta = 1$ . If this is the case, then

25 
$$S_{\parallel\theta} = 0 = G_{\text{cube}} G_{\text{PMT}\parallel} G_{\text{gl}} \frac{I_{\text{lamp}}}{4} \left( M_{00} + M_{10} + (M_{01} + M_{11})(-1) \right)$$
 (27)  
 $0 = M_{00} + M_{10} - M_{01} - M_{11},$  (28)

and

$$S_{\perp\theta} = 0 = G_{\text{cube}} G_{\text{PMT}\perp} G_{\text{gl}} \frac{I_{\text{lamp}}}{4} \left( M_{00} - M_{10} + (M_{01} - M_{11})(1) \right)$$
(29)

$$0 = M_{00} - M_{10} + M_{01} - M_{11}. aga{30}$$

In the case that *both* signals go to zero at their respective locations, Eq. (28) and Eq. (30) are equal, so  $M_{10} = M_{01}$  and  $M_{00} = M_{11}$ .

This leaves the calibration signals as:

$$S_{\parallel\theta} = G_{\text{cube}} G_{\text{PMT}\parallel} G_{\text{gl}} \frac{I_{\text{lamp}}}{4} M_{00} (1 + \frac{M_{10}}{M_{00}}) (1 + \cos 2\theta)$$
(31)

$$S_{\perp\theta} = G_{\text{cube}} G_{\text{PMT}\perp} G_{\text{gl}} \frac{I_{\text{lamp}}}{4} M_{00} (1 - \frac{M_{10}}{M_{00}}) (1 - \cos 2\theta), \tag{32}$$

in which  $\frac{M_{10}}{M_{00}}$  is the only calibration constant needing to be determined. Note that we do not need to know the value of  $M_{00}$  or 10  $M_{10}$  individually for calculating depolarization parameter d.

For CRL, histograms of the numbers of counts at each angle show that the most probable value for the perpendicular count rate  $S_{\perp \theta=0}$  is zero photons per measurement interval. Similar histograms for the parallel channel show that it, too, goes to zero at its minimum (at  $\theta = \pi/2$  rad). Fitted histogram values were used rather than means. The raw lidar photon counting data does not report any values less than zero counts, and noise will artificially increase the total rate. When examining signals larger

15 than zero, the noise takes a Gaussian shape around the mean signal value. For situations in which the true signal is zero, a mean of the measured signal will be reported as a larger value, thus not being indicative of the most probable photon counting result.

As the count rates do indeed go to zero at their respective minima, this second constraint is also appropriate for CRL:  $M_{10} = M_{01}$  and  $M_{00} = M_{11}$ .

### 5.3 First result of rotating polarizer test: Traditional equations are appropriate for CRL

- 20 The value of  $\frac{M_{10}}{M_{00}}$  can now be calculated from the calibration data (see Sect. 5.4), but this is not the most important result from the polarized calibration test. Rather, what matters is that CRL's polychromator optics are acting only as a partial polarizer.  $M_{01} = M_{10}$  and  $M_{11} = M_{00}$  were identified in Sect. 3.2 as the necessary conditions for which the simpler traditional versions of the depolarization equations Eq. (3) and Eq. (2) are acceptable for CRL. These conditions are fulfilled for CRL. The calibration approach and equations for *d* and  $\delta$  used by others in the remote sensing community is appropriate, despite CRL's
- 25 many optics between the sky and the analyzing polarizer for the depolarization channel. This assumes that the Dall-Kirkham telescope does not contribute to these quantities in a significant way. This result is reasonable, as the total reflectivity of all telescope mirrors is high for unpolarized light, thus limiting the amount by which light of either polarization plane can be reduced relative to the other. The focus stage of the telescope contains four mirrors in two planes so that polarization induced by two of the mirrors will be cancelled out by that induced in the following two. Thus it is reasonable that the focus stage does
- 30 not contribute a large amount to d and  $\delta$ . Nevertheless, the exclusion of the telescope is a limitation of the calibration, and quantities calculated by this test will not be totally representative of the whole lidar system.

# 5.4 Determining $\frac{M_{01}}{M_{00}}$ from polarized calibration

The results from the polarized light calibration may be extended further to calculate a preliminary value of  $\frac{M_{10}}{M_{00}}$ . Combining Eq. (31) and Eq. (32), we can solve directly for  $\frac{M_{10}}{M_{00}}$ , the only remaining calibration constant:

$$\frac{M_{10}}{M_{00}} = \frac{\cos 2\theta - \left(\frac{S_{\parallel}\theta - S_{\perp}\theta}{S_{\parallel}\theta + S_{\perp}\theta}\right)}{\cos 2\theta \left(\frac{S_{\parallel}\theta - S_{\perp}\theta}{S_{\parallel}\theta + S_{\perp}\theta}\right) - 1}.$$
(33)

5

In such a calculation, for measurements made at angles  $\theta$  where either signal goes to zero, the result for  $\frac{M_{10}}{M_{00}}$  is a zerodivided-by-zero fraction. Thus, one must exclude such calibration angles.

This calculation was carried out for the test in Fig. 2. A histogram was made of the calculated  $\frac{M_{10}}{M_{00}}$  values, with a peak at  $\frac{M_{10}}{M_{00}} = 0.77 \pm 0.18$ . However, this value has limitations, and is not a good representative value for the CRL system: It is not representative of the whole receiver; rather of the polychromator only. It includes no effects of the telescope or focus stage.

Because of these limitations, it is preferable to determine  $\frac{M_{10}}{M_{00}}$ , and also k, using an unpolarized light test, as demonstrated in the following section (Sect. 6). This determination of the constant employs well-established techniques and has lower uncertainty. Furthermore, it can include all lidar optics. Obtaining a partial-polarizer-like form of the upstream optics Mueller Matrix as a result in our polarized calibration test (Sect. 5) allows us to proceed to Sect. 6 with confidence that the tests we will use to determine k and  $\frac{M_{10}}{M_{00}}$  for the whole receiver are applicable to the CRL.

# 15 6 Determining k and $\frac{M_{10}}{M_{00}}$ with traditional equations

The validity of the expressions in Eq. (2) (and therefore Eq. (3) also) has already been demonstrated for CRL in Sect. 5. Therefore these expressions can be used to determine k and/or  $\frac{M_{10}}{M_{00}}$  via calibrations in which  $d = \delta = 1$ . This mimics fully depolarized light returning from the sky. Two different methods were used to arrange a  $d = \delta = 1$  calibration setup. The first method forces backscattered lidar light to go through a depolarizing sheet of glassine waxed paper before being measured  $(\delta = 0)$ . The set of  $\delta = 0$  for the set of the s

20 (Sect. 6.2). The second method involves shining a lamp at the detector through a depolarizing sheet of glassine (Sect. 7). Either of these methods is preferable to using sky light alone without ensuring its total depolarization as it enters the window above the telescope. Even in atmospheric conditions which are thought to be depolarizing (e.g. clouds in which multiple scattering is expected, or ice clouds for which complete depolarization of d = 1 is possible), complete depolarization at all altitudes for the duration of the measurement cannot be ensured.

# 25 6.1 Mueller Matrix development of the calibration expressions for $\frac{M_{10}}{M_{00}}$ and k

The matrix equation for the intensity reaching the parallel channel, using the laser as the light source and a perfect depolarizer with attenuation parameter  $G_{gl}$  in front of the receiver is:

$$I_{\parallel} = \frac{G_{\rm PMT \parallel \perp}}{2} \begin{pmatrix} 1\ 1\ 0\ 0\\ 1\ 1\ 0\ 0\\ 0\ 0\ 0\ 0\\ 0\ 0\ 0\ 0 \end{pmatrix} \begin{pmatrix} M_{00}\ M_{01}\ M_{02}\ M_{03}\\ M_{10}\ M_{11}\ M_{12}\ M_{13}\\ M_{20}\ M_{21}\ M_{22}\ M_{23}\\ M_{30}\ M_{31}\ M_{32}\ M_{33} \end{pmatrix} \frac{G_{\rm gl}}{2} \begin{pmatrix} 1\ 0\ 0\ 0\\ 0\ 0\ 0\ 0\\ 0\ 0\ 0\ 0 \end{pmatrix} bO_{\parallel\perp}(z) \begin{pmatrix} 1\ 0\ 0\ 0\\ 0\ 1-d\ 0\ 0\\ 0\ 0\ d-1\ 0\\ 0\ 0\ d-1\ d \end{pmatrix} I_{\rm laser} \begin{pmatrix} 1\\ 1\\ 0\\ 0 \end{pmatrix}.$$
(34)

Thus, the signals in each channel are:

$$S_{\parallel d=1} = \frac{G_{\text{PMT}\parallel\perp}G_{\text{gl}}}{2}bO_{\parallel\perp}(z)I_{\text{laser}}(M_{00} + M_{10})$$
(35)

$$S_{\perp d=1} = \frac{G_{\text{PMT}} ||_{\perp} G_{\text{gl}}}{2} b O_{||\perp}(z) I_{\text{laser}}(M_{00} - M_{10}).$$
(36)

5 The signals from the parallel and perpendicular channel are combined so that we can solve for  $\frac{M_{10}}{M_{00}}$  with as many of the unknown factors cancelling out as possible:

$$\frac{S_{\parallel d=1} + S_{\perp d=1}}{S_{\parallel d=1}} = \frac{2M_{00}}{M_{00} + M_{10}}$$

$$\frac{M_{10}}{2}$$
(37)

$$\frac{\overline{M_{00}}}{M_{00}} = \frac{\overline{S_{\perp \ d=1}}}{\frac{S_{\perp \ d=1}}{S_{\parallel \ d=1}} + 1} - 1.$$
(38)

To calculate k, the equation is:

10 
$$k = \frac{S_{\parallel d=1}}{S_{\perp d=1}}$$
. (39)

Note that these equations for  $\frac{M_{10}}{M_{00}}$  and k work equally well for the case in which we use a lamp to illuminate the lidar as the several differences in the initial matrix equation cancel out: There is no overlap function, no atmospheric matrix, and we use  $I_{\text{lamp}}$  instead of  $I_{\text{laser}}$ , which also cancels out of the final calibration equations.

The constants  $\frac{M_{10}}{M_{00}}$  and k can be calculated from one another.  $\frac{M_{10}}{M_{00}}$  tends to be more "forgiving" in terms of accuracy than k 15 does. A small percentage error in  $\frac{M_{10}}{M_{00}}$  will yield a larger percent error in k. Thus, one must take care when making a selection of which to use despite the ease with which one may convert between them in the absence of estimates of their uncertainties.

# 6.2 Physical setup of unpolarized laser calibration to determine $\frac{M_{10}}{M_{00}}$ and k

To include all optics, the depolarized light should be introduced above the roof hatch window. Note that unlike the polarized calibration, we do have access to depolarizing optics which are practical to cover a 1 m diameter roof hatch window. However,

20 as the lamp is not bright enough when placed in this location, backscattered laser light is better used to test this location.

In this setup, we obtain the depolarized light by running the lidar as usual, with the laser transmitted to the sky and scattered back to the lidar, but we interrupt the optical path of the receiver with a depolarizing sheet (glassine) before the backscattered light enters through the roof window of the detector.

Using a flexible material like glassine was important in the Arctic winter. When the lidar is operating, the glassine sheet is exposed to wind, blowing snow, cold temperatures, and any humidity that may be in the air. Several 16" x 20" sheets were



**Figure 3.** Colour plot of perpendicular channel coadded and corrected photocounts. Magenta box below 3000 m between 05:00 UTC and 10:00 UTC indicates the region of interest to be used in the calibration analysis.

taped together with opaque black masking tape to create a larger sheet which could cover the 1 m diameter lidar roof window. To keep the photon count rates as high as possible during the test, only a single layer of glassine was used, although using two sheets in series ensures more complete depolarization. A 10 cm diameter circle was removed from the centre of the sheet so that the glassine would not obstruct the laser exit window. Glassine tears easily once its edge is compromised, so it was advantageous to pre-tape any line which was to be cut, and then to cut through the taped line. The sheet was placed over the roof window. A foam wedge with a circular hole was snugged down over the glassine sheet around the laser window such that the sheet would be secured and not blow into the laser beam. The four corners of the sheet were held down to the metal surface of the roof around the window, slightly below the level of the window's frame, pulling the glassine very gently taut over the window. Two 1x6 wooden planks with "feet" on each end provided sufficient tension, and these were wedged into place with foam.

#### 6.3 Measurements for unpolarized laser calibration, using example from 1 November 2013

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This test was carried out for over 22.8 h, between 22:40 UTC on 1 November 2013 and 21:00 UTC on 2 November 2013. Figure 3 is a plot of the perpendicular channel background-corrected photocount profiles for the entire calibration measurement, coadded with 10 x 10 binning to a resolution of  $5 \min \times 37.5 m$ . Data from altitudes below 500 m is routinely rejected from

15 CRL processing because of the differential geometric overlap function of CRL, and has been indicated in Fig. 3 in white. An appropriate time-altitude region of interest must be selected for the calibration. Regions with high-backscatter features, such as clouds, are desirable. The magenta box in Fig. 3 below 3000 m, between 05:00 UTC and 10:00 UTC shows the region



Figure 4. Parallel and perpendicular channel corrected photocounts within the calibration region of interest, with their associated signal-tonoise ratios (SNR) plotted to the right. Bottom left panel shows the ratio of the counts for each time-altitude point (k), with the associated uncertainties in k shown at bottom right.

of interest selected for the calibration calculations. This region encompasses a cloud which remained between 1 and 3 km altitude over the lidar for several hours, as determined by contemporaneous measurements with the Millimetre Cloud Radar and 532 nm Visible Rayleigh Elastic CRL lidar channel measurements. Analysis for calibration was attempted on the whole data set as well as just the region of interest which contains the cloud. It was repeated for a variety of coadding times and altitude resolutions. All resolutions provided similar results.

Regions with fewer than one photon per time-altitude bin in either channel, and/or signal-to-noise ratios below 0.1 for perpendicular, and 1.5 for parallel, are rejected from the calculation. Because of the attenuation from the depolarizing sheet, many areas have zero counts in the perpendicular channel, even at low altitudes. The top left (a) and centre left (b) panels of Fig. 4 plot the parallel and perpendicular photon counts from the region of interest with their respective signal-to-noise ratios plotted to the right in panels (d) and (e).

Once the measurements have been quality controlled, there are several approaches for determining k.

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- 1. Calculate a k value individually for each time-altitude bin (Fig. 4, panel (c), with associated uncertainty in panel (f)), and then combine k values into an overall mean constant. This method gives values of  $k = 20.2 \pm 0.6$ .  $\frac{M_{10}}{M_{00}} = 0.89 \pm 0.05$  is similarly calculated from a mean of individual values of  $\frac{S_{\perp}}{S_{\parallel}}$ .
- 2. Calculate a summed or mean count value for the whole calibration time-altitude space in each of the two channels,

5

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and then take the ratio of these to calculate one k representative of the whole region. The result using this method  $k = 21.0 \pm 0.2$ , and  $\frac{M_{10}}{M_{00}} = 0.910 \pm 0.002$ .

The two methods give values which are equal to within their uncertainties. As the uncertainty is smaller using the second approach, this method is selected.

The overall calibration factors for CRL are therefore  $\frac{M_{10}}{M_{00}} = 0.910 \pm 0.002$  and  $k = 21.0 \pm 0.2$ , calculated using all detector 10 optics. This is quite different from the value of k = 1 which would be expected for an ideal depolarization lidar in which no upstream optics were interfering with the polarization of returned light.

# 7 Determining contributions of individual optics

To determine which receiver optics contribute most to CRL's high value of k, further tests were carried out. These tests determined that the Visible Long Wave Pass optic is by far the largest contributor.

### 15 7.1 Physical setup of unpolarized lamp calibration

A lamp was placed directly upstream of the focus stage, similar to the setup of Sect. 5.1. A depolarizing sheet was installed at various locations within the detector to ensure that all light proceeding from that point was completely unpolarized. This test started with the depolarizing sheet directly before the polarotor and then moved sequentially upstream, placed between any two optics where there was room to safely insert it (Fig. 1, marked as numbers from 1 through 8). Industrial kitchen grade waxed

20 paper was used for this test, mounted between two frames of foam core to keep it rigid. Measurements were made with the polarotor in operation as usual. Mean values of parallel and perpendicular counts were used for each calculation of k and  $\frac{M_{10}}{M_{00}}$ . (Glassine was later found to be more consistently depolarizing from sheet to sheet than are general brands of waxed paper, but we elected not to re-do the test in Sect. 7.2, because the particular sheet of waxed paper used here was tested in our laboratory, and found to be sufficiently depolarizing.)

# 25 7.2 Results: Lamp test $\frac{M_{10}}{M_{00}}$ and k, setting d = 1

The lamp tests were carried out over a 2 h period on 1 April, 2013. The results are listed as Tests 1 through 8 in Table 1. The laser calibration test result from Sect. 6.3 is listed as Test 9 in this table, for comparison purposes.

The tests indicate which of our optics are contributing most to the large overall calibration factor of the system. The first test location (Test 1) is as far downstream as it was possible to begin. All subsequent optics (interference filter, focus lens, etc) are in a closed beamtube where it is not feasible to insert a depolarizer. The measurements here showed equal amounts of light in

the parallel and perpendicular channels, and k = 1. This indicates that the collection of optics in this beamtube, and the PMT, are not contributing to the value of k = 21 measured for the whole lidar. The "k" described for CRL must therefore include optics in the system, and not only the gain of the PMT.

Subsequent tests moving upstream each time indicate that most of the optics in the polychromator are indeed partially 5 polarizing the returned lidar beam, some favouring attenuation of parallel-polarized light (decrease in k and  $\frac{M_{10}}{M_{00}}$ ), and others attenuation of perpendicular-polarized light (increase in k and  $\frac{M_{10}}{M_{00}}$ ).

The largest contributor to the overall k value is the VLWP dichroic (compare Test 3 to Test 5). Its individual contribution is  $k_{\text{VLWP}} = 6$ . Other large contributors are the lenses at the entrance to the polychomator ( $k_{\text{poly entrance}} = 2.2$ ; compare Test 6 to Test 7) and the telescope and roof window ( $k_{\text{telescope+window}} = 3.12$ ; compare Test 8 to Test 9).

10 The unpolarized lamp tests of Test 7 at the entrance to the polychromator, with  $\frac{M_{10}}{M_{00}} = 0.719 \pm 0.001$ , were made at the same location as the polarized calibration tests of Sect. 5.2, with  $\frac{M_{10}}{M_{00}} = 0.77 \pm 0.18$ . These values are, as expected, equal to within their uncertainties. This provides a link between the two calibration methods.

Tests 7 and 8 took place on either side of the focus stage. Their  $\frac{M_{10}}{M_{00}}$  and k results change only by a small amount. Therefore, the focus stage does not contribute significantly to the whole-lidar values.

# 15 7.3 Discussion of results from unpolarized lamp tests

The tests in Sect. 7.2 are important for CRL future planning. First, they indicate that we *must* calibrate for *k* by placing the depolarizing optic at the beginning of the optical chain. Many lidar groups (Sassen and Benson, 2001; Alvarez et al., 2006; Wang et al., 2009; Freudenthaler et al., 2009) choose to use calibration lamps, or depolarization optics, part way through their system. An alternative is to use a lamp which scans or is projected over the whole entrance aperture at the first optic of the system. Notably, the lidar group at Howard University uses a mapping lamp applied to a water vapour lidar (Venable et al., 2011). CRL unfortunately does not have the capacity to install such a system at this time. Tests become easier farther downstream in the detector for several reasons: Any optic placed at the beginning of the detector chain must be as large as the first optic itself. In the case of CRL, this means a circle with diameter 1 m. Optics of this size are expensive and unwieldy, and are sometimes impossible to obtain. Any optic placed at the beginning of the detector chain will necessarily be outdoors,

- and will be exposed to the elements. In Eureka this includes temperatures colder than  $-50^{\circ}$  C, significant wind, blowing snow, and working on a roof. If a lamp is used for illumination, power is also needed on the roof, which is inconvenient. Going downstream brings the optic inside, and makes the required optics smaller. Any optics placed between the telescope and the focus stage must be about  $25 \text{ cm}^2$ . Optics after the focus stage may be as small as  $25 \text{ mm}^2$ . Smaller optics are easier to rotate in a controlled manner (e.g. for polarizer calibrations). At what cost to the calibration and science do these practical advantages
- 30 come? For CRL, k changes by a factor of 3.4 between the entrance to the polychromator and the entrance to the entire system; the more convenient calibration is insufficient. A second use for these test measurements is that they allow us to see which optics would be most advantageous to change the next time we upgrade optics in the lidar. Naturally, those such as the VLWP filter, which contributes the most to the reduction of the perpendicular signal, would be most advantageous to change.



Figure 5. Atmospheric depolarization ratio measurements ( $\delta$ ) from 12 March 2013, with associated absolute uncertainties ( $\sigma\delta$ ) in units of depolarization ratio. In the left panels of  $\delta$  (panel (a)) and  $\sigma\delta$  (panel (c)), all data points with absolute uncertainty greater than 0.2 have been eliminated. In the right panels of  $\delta$  (panel (b)) and  $\sigma\delta$  (panel (d)), points with relative uncertainty greater than 25% have been eliminated instead. Resolution is 5 min × 37.5 m.

#### 8 Sample atmospheric measurements

Using the best determination of the calibration constant,  $k = 21.0 \pm 0.2$ , (Sect. 6.3), we can determine d and  $\delta$  using Eq. (2) and Eq. (3) for a day's measurements to show the performance of CRL. Here we use measurements obtained on 12 March 2013, which we chose because two distinct cloud morphologies are present, as are a variety of signal levels in both depolarization

5 channels, and because some particular places in the plot require special interpretation, which is discussed below. The calibration constant k has been measured to be stable over several years for CRL. Therefore the time between the k calibration example shown in this paper (1 April 2013) and the date of the measurements given in Sect. 8 (12 March 2013) is of no consequence. Figures 5 and 6 show the depolarization ratio, depolarization parameter, and the uncertainties and relative errors for each. Many data points have uncertainties on the order of 10 % and smaller.

# 10 8.1 Uncertainty propagation

The uncertainty and errors were propagated using standard uncertainty propagation rules through low-level data processing equations, and then through the algebraic functions shown in this document, assuming uncorrelated errors (for a full account see McCullough (2015)). The Licel system uses simultaneous photon counting and analogue detection for the PMTs, and thus two signals are merged together for each "measurement channel". In all cases, the data is read into software and overflow



**Figure 6.** Atmospheric depolarization parameter measurements from 12 March 2013, with associated absolute uncertainties in units of depolarization parameter. In the left panels of d (panel (a)) and  $\sigma d$  (panel (c)), all data points with absolute uncertainty greater than 0.2 have been eliminated. In the right panels of d (panel (b)) and  $\sigma d$  (panel (d)), points with relative uncertainty greater than 25% have been eliminated instead. Resolution is 5 min × 37.5 m.

flagged bits are removed. Uncertainties are initially propagated separately for photon counting and analogue signals. Then they are combined.

For photon counting data, most of the uncertainty in the photon counting channel is derived from shot noise. This uncertainty is then propagated through the equations of the low level data processing in the following order: 1. Begin with photon shot

- 5 noise. This is applicable for both raw counts and raw background counts. This is a statistical uncertainty. 2. Propagate this uncertainty through the dead time equation, in which the dead time uncertainty is a systematic uncertainty (cannot improve by coadding or longer integration). 3. Propagate the uncertainty through the coadding equations. This generally reduces the overall size of the relative uncertainty (see Sect. 8.1) in the measurement. 4. Determine the uncertainty in the background level, which was determined from the dead time corrected background values at high altitudes. This is a statistical uncertainty, because
- 10 it incudes the shot noise uncertainty. 5. Add the dead-time corrected, coadded, shot uncertainty and the dead-time corrected, coadded, background uncertainty in quadrature to get a total photon counting uncertainty for each data point.

For analogue data, the procedure is different: 1. Begin with raw analogue digital signals. 2. Account for the analogue to-digital converter uncertainty. 3. Include the analogue shot noise uncertainty (a statistical uncertainty). 4. Account for the uncertainty in turning analogue count rates into range-scaled values. 5. Remove dark count profiles and account for this uncer-

15 tainty. 6. Determine the uncertainty in the sky background constant determined from background values at high altitudes. This is a statistical uncertainty, because it incudes the shot noise uncertainty. Then account for it during background subtraction.

7. Account for the uncertainty involved in converting analogue range-scaled voltage signals to equivalent photon count rates (uncertainty depends on precision when calculating the "gluing coefficients" or "merging coefficients" based on fits to lidar data).

- Finally, the two profiles, photon counting and analogue, are combined into a single resulting photocount profile for each measurement channel, for each (coadded) time bin. At each point, the raw photon counting rate determines which contributor's count value will be included: photon counting or analogue. The uncertainty at each point in the combined profile is then simply the uncertainty of the contributing data point. These combined profiles can then be used for higher analysis into useful data products such as depolarization ratio and depolarization parameter. The uncertainties in these profiles are the uncertainties on the values  $S_{\parallel}$  and  $S_{\perp}$  which appear in Eq. (2) and Eq. (3) of this paper. We then propagate these uncertainties through the
- 10 equations Eq. (2) and Eq. (3), again assuming uncorrelated errors, to arrive at an overall estimate for the absolute uncertainty in  $\delta$  and d.

The uncertainties given as "absolute uncertainty" are the 1-sigma combined effects of systematic and statistical uncertainties and errors, and are expressed as, for example,  $d = 0.200 \pm 0.003$ , in which the  $\pm$  uncertainty is given in the same units as d, and would directly give the size of an error bar on a 2-D plot. Some confusion may arise when comparing values of  $\delta$  and d

15 from this document to those given elsewhere. Because depolarization parameter can exist from values of 0 to 1, some authors express "d = 0.2" as "d = 20%", for example. This is never done in the present document, precisely to avoid ambiguity with the relative errors discussed next. All values of  $\delta$  and d are given as decimal, non-percent numbers, as are absolute uncertainty values. In other words, expressed with absolute uncertainty, we have  $x \pm \sigma_x$ .

Relative uncertainty aims to describe the uncertainty in relation to the measured size of the value of d, and is expressed as a 20 percent:  $d = 0.200 \pm (0.003/0.2) * 100\%$ , which is  $d = 0.2 \pm 1.5\%$ , for the same example. In other words, expressed as relative uncertainty, we have  $x \pm (\sigma_x/x)$ .

# 8.2 Interpretation of sample atmospheric measurements

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Just below 2 km altitude, a region of high depolarization is evident with low uncertainty. This implies that this region of the cloud is icy rather than made of liquid droplets. As altitude increases in the cloud, the depolarization drops. This could be because the cloud has suddenly turned into liquid droplets, but there are other factors to consider: First, the uncertainty is higher in these regions, but this does not tell the whole story. This calculated uncertainty expresses *only* the uncertainty in

- the calculated result from Eq. (3) based on the number of photons returned in each measurement channel, and the statistical uncertainty in each of these measurements. As Eq. (3) is not applicable in circumstances of multiple scattering, any value calculated using this equation for time-altitude locations experiencing such scattering will not be valid as a proxy for particle
- 30 phase despite our (possibly precise) ability to calculate it. In the example presented here, the assumption of no multiple scattering is decreasingly trustworthy high in the cloud, as photons have to pass through the thick cloud below twice. In future, it would be well to quantify the added uncertainty due to the likelihood of multiple scatters. The overall effect of multiple scattering is an increase in depolarization, but detailed effects are expected to differ for liquid and ice particle cases. According to laboratory experiments and theoretical calculations, multiple scattering from liquid droplets is likely to induce

depolarization of no more than 3 to 4% for a lidar with a field of view of 1 mrad, with depolarization depending also on particle number density (Liou, 1972; Liou and Lahore, 1974). Atmospheric measurements of water clouds support these estimates, and demonstrate a linear increase in multiple-scattering-induced depolarization with increased receiver acceptance angle (Sassen and Petrilla, 1986). More recent monte-carlo simulations of water clouds find that a third-order polynomial describes the

- 5 relation between depolarization ratio and multiple-scattering fraction (Hu et al., 2006). Ray tracing code for ice particles also indicates that multiple scattering leads to an increase in the depolarization ratio, however the magnitude of the increase showed a strong dependence on cloud optical thickness and particle shape (Noel et al., 2002). A full integration of these effects is beyond the scope of the present paper. Therefore care must be taken when interpreting the depolarization values presented herein, even those with low measurement uncertainty.
- 10 A further possible contributing factor is that the two channels may have differing amounts of extinction if the transmission function of the atmosphere is polarization-dependent. The most trustworthy depolarization values are those for which we have both low uncertainty *and* reasonable confidence that we have a low extinction single-scattering situation for every photon involved in the data for that time-altitude bin. Examples of such locations in this example night are the lower portions of the large cloud before 10:00 UTC, and, to a smaller degree, the entire small cloud between 15:00 UTC and 20:00 UTC.
- It may be most sensible to cut out regions which are not providing trustworthy depolarization values based on criteria discussed above. The values could be cut based either on relative error or on absolute error. The latter is chosen in this situation because a measurement of a depolarization parameter  $d = 0.01 \pm 0.01$  is still meaningful, despite having 100% relative error. Interpretations deal with cutoffs between different values of d and the measurements need to be sensitive enough to discern this cutoff, without eliminating an excessive number of measurements. Compare the data coverage of the upper left panel (panel
- 20 (a)) in either Fig. 6 or Fig. 5 with the coverage of its corresponding upper right panel (panel (b)). Far more low-depolarization values are kept by cutting off using the absolute uncertainty rather than the relative uncertainty, without losing any interpretation confidence. Extra information is available at 3 km just after 05:00 UTC: There are distinct regions of increased depolarization parameter which are retained when cutting depolarization parameter on absolute uncertainty rather than on relative uncertainty. Although these are above thick cloud, and so multiple scattering may influence the interpretation of the specific values of *d*,
- 25 the relative values can still be instructive, so it is useful to retain these. Features such as liquid layers within otherwise frozen clouds, or frozen parts within liquid clouds, would be detectable in similar situations, and regions of aerosols within clear air as well. Depending on the application, it may be of use to some lidar users to know simply that the cloud is inhomogeneous in cloud particle phase, or that an aerosol layer is present, without the specific microphysical details which are usually available with a well-constrained absolute depolarization parameter value.
- 30 Further coadding to lower resolution would help with the data coverage by increasing the number of perpendicular photoncounts per bin. On some dates, measurements can be retained in this way up to 8 to 10 km altitude. However, this can only be carried out to a certain point, after which the low resolution depolarization measurements will be misleading. For example, any instances of thin liquid layers (low d and  $\delta$ ) residing within an ice cloud (high d and  $\delta$ ) would, at low resolution, show a smooth region with intermediate values of d and delta. As such intermediate values of d and  $\delta$  are not actually present anywhere within

the binned region, it would be incorrect to use these values for interpretation of the cloud itself. For this reason, measurements are kept at as high a resolution as possible, while still retaining as many measurement points as possible.

# 9 Future work

CRL can now make depolarization parameter measurements at a precision of < 10 % relative uncertainty in clouds at a resolution of 5 min × 37.5 m (Sect. 8), despite the less than optimum optical configuration of CRL. The major difficulty for CRL is in receiving sufficient perpendicular signal at the depolarization PMT, as indicated by the very large calibration value of k = 21 found in the system, and by the low photocount rates in the perpendicular channel during atmospheric measurements. For any unpolarized light which scatters back to the roof window, the portion which would be allowed through the perpendicular analyzer near the PMT is preferentially suppressed by lidar receiver optics in comparison to the portion of unpolarized light which would be allowed through the parallel analyzer. There are several possibilities for improvement of the depolarization measurements: Changes to the depolarization parameter calculation method, and changes to lidar hardware. Suggestions for each of these are provided in Sect. 9.1 and Sect. 9.2, respectively.</li>

### 9.1 New analysis method

We have developed a new depolarization calculation method by extending the Mueller Matrix instrument characterization

- 15 method shown in this paper to a third CRL measurement channel: The unpolarized 532 nm Rayleigh Elastic channel. This method will be discussed in detail in a companion paper (McCullough et al., 2017), and is available in McCullough's PhD thesis (2015). In the new method, low resolution traditional *d* values, as calculated in the present paper, are used to create a nightly calibration profile. The improved calculation method produces depolarization parameters with similar uncertainties as the traditional method, but at much higher resolutions of 2 min × 15 m, and with far fewer data points lost to low signals, and therefore better measurement coverage of the atmosphere above the lidar. Alternately, the results can be expressed at similar
- 20 therefore better measurement coverage of the atmosphere above the lidar. Alternately, the results can be expressed at similar resolution to the traditional depolarization products for CRL, but with much higher precision.

# 9.2 Hardware upgrades

Hardware upgrades are the other option for improving the CRL depolarization measurements. Any or all of these would improve both calculation methods for *d* by increasing signals in the perpendicular channel. In the context of the calibrations
in this paper, hardware improvements seek to reduce the value of *k* by increasing the number of perpendicular photons which reach the depolarization PMT. These hardware improvements are also relevant for any other lidar which does not have access to

a polarization-independent channel at the same wavelength as its depolarization channels, and thus which cannot take advantage of the new calculation method from Sect. 9.1.

Specifically, any of the following hardware changes would improve signals in the perpendicular channel. First, the laser's polarization could be rotated by 90°, allowing the collection optics in the polychromator to suppress the large parallel signal while enhancing the small perpendicular signal. Second, putting a quarter wave plate at the entrance to the polychromator would also help balance the signals for the same reason stated above. Third, replacing the VLWP filter with one which is less polarizing, or less polarizing in the perpendicular-suppressing direction would reject as few as possible the perpendicular photons which enter the telescope. Fourth, using two depolarization PMTs would allow for different gain settings individually optimized for the parallel and perpendicular channels, but this change to the configuration is not possible with the current

- 5 electronics. CRL's setup uses a single PMT to make both parallel and perpendicular measurements, and there is no switching of PMT gain settings between laser shots. Therefore, the gain setting must be a compromise of what is best for the high-signal parallel measurements and the low-signal perpendicular measurements. In practice means a lower gain setting is required to optimize the parallel channel to avoid PMT saturation. The high dynamic range of the combined analogue and photon counting of the Licel recorders helps somewhat, but having intensities of more comparable levels to begin with would be a better choice.
- 10 Fifth, moving the depolarization PMT further upstream in the detector, perhaps with a pick-off beamsplitter at the beginning of the optical chain, would remove many of the partially-polarizing optics from the path to the depolarization PMT, thus rejecting fewer of the perpendicular photons than is currently the case. Any of the CRL hardware improvements here described would improve depolarization measurements made using the traditional equations for CRL or for any similar lidar, and would also improve measurements made using the newly-developed three-channel calculation technique.
- 15 Throughout this work, k values far from unity have been presented as being undesirable. There can, however, be advantages to a setup with  $k \neq 1$ , albeit with k < 1 rather than k > 1 as CRL has. Consider that the scattering properties of the atmosphere lead to maximum d and  $\delta$  values of 1 for total depolarization, and 0 for no depolarization. For d = 1, half of the backscattered intensity reaching the roof window would be admitted to an ideal (k = 1) parallel channel, and the other half of the intensity would be admitted to the perpendicular channel. For d = 0, all of the intensity is parallel, and none is perpendicular. Therefore,
- 20 the maximum perpendicular intensity ever possible to be backscattered to the lidar's roof window and through the receiver is only *half* the maximum parallel signal ever possible. With a whole-system calibration value k = 1, the maximum measured perpendicular signal will also be half of the maximum measured parallel signal. Values of k > 1 suppress the perpendicular signal even further. Therefore, k > 1 values for CRL are leading to the preferential attenuation of already-smaller signals. If CRL instead had k values just as far from unity, but with k < 1, the larger parallel signal would instead be preferentially
- 25 attenuated. This analysis leads to the interesting conclusion that for CRL, k < 1 optics would lead to better signal-to-noise ratios overall, and lower uncertainty in products derived from ratios of the two signals.

The new analysis technique makes it unlikely that the physical changes to CRL will be carried out in the near future, as they are less critical to the success of the CRL depolarization measurements than they would be if the traditional method was the only calculation possibility available. Therefore, all efforts have been directed toward the validation of the new analysis method.

### 10 Conclusions

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Depolarization measurement capability has been added to the CRL lidar at Eureka, Nunavut in the Canadian High Arctic. Characterization tests have demonstrated that the traditional depolarization ratio and depolarization parameter equations and their calibration methods are appropriate to be used for CRL, despite the lidar not having been built specifically to make polarization measurements.

A single Mueller matrix suffices to describe the collective effects of all receiver optical elements between the telescope's focus stage and the Polarotor polarizing beamsplitter. The following matrix elements, and ratios of matrix elements, were measured using a polarized lamp test:  $M_{02} = 0$ ;  $M_{12} = 0$ ;  $M_{11} = M_{00}$ ;  $M_{10} = M_{10}$ ;  $\frac{M_{10}}{M_{00}} = 0.77 \pm 0.18$ . Because  $M_{11} = M_{00}$  and  $M_{10} = M_{01}$ , we conclude that the optics represented by the "upstream optics" matrix act as a partial polarizer (without rotation, retardation, or other optical effects) on the calculation of d and  $\delta$ . Therefore, the traditional calculation equations for d (Eq. (2)) and  $\delta$  (Eq. (3)), which use the single calibration constant k, are valid for the CRL.

Using an unpolarized lamp light test from the same location, the results are  $\frac{M_{10}}{M_{00}} = 0.719 \pm 0.001$ , which is equal within 10 uncertainty to the polarized-light calibration value, and  $k = 6.12 \pm 0.02$ .

An unpolarized light test using laser returns from the sky, depolarized by a Glassine sheet above the receiver roof window, includes the optical contributions of the roof window, telescope, and focus stage, in addition to the upstream optics matrix. The results of this test are  $\frac{M_{10}}{M_{00}} = 0.910 \pm 0.002$  and  $k = 21.0 \pm 0.2$ . These values are representative of the entire lidar receiver, so are applied to CRL's routine atmospheric measurements of depolarization.

15 Detailed optic-by-optic measurements of  $\frac{M_{10}}{M_{00}}$  and k using unpolarized lamp light reveal that the Visible Long Wave Pass filter is the most highly polarizing optic, increasing k by a factor of 5.6. The next most polarizing optic is the combination of the telescope and roof window, which increase k by a factor of 3.1.

The  $\frac{M_{10}}{M_{00}} = 0.910 \pm 0.002$  and  $k = 21.0 \pm 0.2$  results are applied to a representative 24-hour long atmospheric measurement. This demonstrates the depolarization ratio and depolarization parameter for the sky above Eureka on 12 March 2013, at a

- resolution of  $5 \min \times 37.5 \text{ m}$ . During this period, a thick, partially frozen cloud was present before 10:00 UTC, and the reduced reliability of the depolarization measurements farther into the thick cloud is evident as multiple scattering becomes important. A non-frozen cloud with regions of higher depolarization material above it was present after 15:00 UTC. CRL was also found to be sensitive to the low depolarization regions of clear air below the 15:00 UTC cloud. Typical depolarization parameter absolute uncertainties are on the order of  $\pm 0.05$  ( $\leq 10\%$  relative uncertainty) within clouds at time and altitude resolutions of
- 25 5 min and 37.5 m respectively, with higher precision and higher resolution possible in select cases, and uncertainty somewhat larger  $(\pm 0.1)$  at the same altitude outside of clouds.

This work has resulted in a well-characterized depolarization measurement system at CRL. Using a similar Mueller algebra exercise, these calibration methods may be applied to other lidars to elucidate the properties of the optics. This work shows that it is possible to add depolarization capability to lidars which were not originally designed specifically for polarization measurements.

### 11 Data availability

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Data used in this paper available upon request from corresponding author (e.mccullough@dal.ca).

Author contributions. E. M. McCullough: Installation and calibration of depolarization hardware. Data analysis and development of method. Writing of analysis MATLAB code. Manuscript preparation. This work formed part of McCullough's doctoral thesis. R. J. Sica: Supervision of doctoral thesis. Contribution to manuscript preparation. J. R. Drummond: Principal Investigator of PEARL laboratory. Contribution to manuscript preparation. T. J. Duck: Principal Investigator of CRL lidar at the time of this work. Development of the CRL laboratory.

- 5 G. J. Nott: Original design of depolarization channel for CRL. Instruction in installation and initial data processing in Python. Extensive discussions regarding calibration and analysis. Contribution to manuscript preparation. J. Hopper: Maintenance and testing of depolarization hardware. Lidar operations. C. P. Thackray: Lidar operations. Assistance in the laboratory. Contribution to manuscript preparation. C. Perro: Instruction on lidar operations. Lidar operations. J. Doyle: Instruction on lidar operations. K. A. Walker: Principal Investigator of polar sunrise ACE/OSIRIS Arctic validation campaigns of which these CRL measurements are one component.
- 10 *Competing interests.* The authors declare that they have no conflict of interest.

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**Table 1.** Measuring calibration constants  $\frac{M_{10}}{M_{00}}$  and k using a depolarizer at various locations in the polychromator, illuminated with unpolarized lamp light. Test numbers correspond with locations marked in Fig. 1. The ratio of each k value compared to the previous value is given by  $\frac{k_i}{k_{i-1}}$ . This quantity gives the contribution of each optic to the cumulative  $\frac{M_{10}}{M_{00}}$  and k values shown in that row, and is effectively the "k" value for that individual optic. A value of  $\frac{k_i}{k_{i-1}} = 1$  indicates no partial polarization contribution (i.e. an ideal optic for depolarization measurement purposes). Test 9 is included for comparison purposes.

Test	Light source location	$\tfrac{M_{10}}{M_{00}}\pm\sigma$	$k\pm \sigma$	$\frac{k_i}{k_{i-1}}$	Contribution of additional optic included in each test
1,4	Directly upstream of polarotor	$0.001\pm0.004$	$1.002\pm0.002$	-	None. We expect $k = 1$ here, and it is.
2	Upstream of pellicle	$-0.250 \pm 0.002$	$0.601 \pm 0.003$	0.600	Moderate relative parallel attenuation by pellicle.
3	Upstream of collimating lens	$-0.211 \pm 0.003$	$0.652\pm0.004$	1.085	Minimal relative perpendicular attenuation.
5	Upstream of the Visible Long Wave Pass (VLWP) dichroic	$0.561\pm0.003$	$3.56\pm0.03$	5.598	Very large relative perpendicular attenuation by VLWP.
6	Upstream of the UV Long Wave Pass (UVLWP) dichroic	$0.472\pm0.003$	$2.78\pm0.02$	0.78	Small relative parallel attenuation by UVLWP.
7	At entrance of the polychromator	$0.719\pm0.001$	$6.12\pm0.02$	2.20	Large relative perpendicular attenuation by collimating optics at polychromator entrance.
8	Upstream of the focus stage	$0.741 \pm 0.001$	$6.73\pm0.01$	1.10	Minimal relative perpendicular attenuation by focus stage.
9	Upstream of roof window (from laser calibration in Sect. 6.3)	$0.910\pm0.002$	$21.0\pm0.2$	3.12	Large relative perpendicular attenuation by telescope and roof window.

**Table 2.** Parallel and perpendicular signals for angles diagnostic of symmetry in the measurements. Each signal is effectively the same at  $0.25\pi$  and  $0.75\pi$  radians and integer multiples thereof.

Angle $\theta$ (rad)	$S_\parallel\pm\sigma_\parallel$	$S_{\perp}\pm\sigma_{\perp}$
$-0.25\pi$	$9.358\pm2.5$	$0.666 \pm 1.3$
$0.25\pi$	$9.629 \pm 2.5$	$0.693 \pm 1.3$
$0.75\pi$	$9.269 \pm 2.5$	$0.701 \pm 1.3$
$1.25\pi$	$9.091 \pm 2.5$	$0.834 \pm 1.3$
$1.75\pi$	$9.875\pm2.5$	$0.789 \pm 1.3$
$2.25\pi$	$8.919\pm2.5$	$0.830\pm1.3$