

Dear Dr. Stoffelen,

On behalf of all the co-authors, I'd like to thank you and the reviewers for the time dedicated to our study and for the suggestions that helped us improve the quality of our paper.

We have addressed the comments from Anonymous Referee #1 below and updated the manuscript accordingly.

Please note, I will be out of office from December 18 to 29th. I shall answer any further requests as soon as I come back.

Kind regards,

Fabien Carminati

Anonymous Referee #1

Minor point, line 501. It is somewhat surprising that no cloud screening is applied. I assume this is not an issue since clouds are reported at the raob site. In the case of dense clouds, data is not used? Similar limitations on model side?

It is true that the presence of clouds along the path of the radiosonde may introduce what we could call a cloud-induced bias when comparing simulated brightness temperature from radiosonde profiles and from model fields. This point is discussed lines 386-395 and cloud screening strategies are suggested. The present study, however, does not aim at obtaining or analysing representative statistics of model biases and uncertainties, but rather focuses on the methodology to obtain them. The Lindenberg 2016 data set is used as a demonstrator, as stressed line 488 “For illustration purposes”, and the results, although in line with previous estimations, should not be taken as face value.

Line 501 “Note that no cloud screening is applied in this study” changed for:

Note that for simplicity, no cloud screening is applied in this case study. This caveat may, as suggested in the previous section, exacerbate the biases observed when comparing brightness temperature simulated from radiosonde profiles and from model fields. Future work dedicated to the in-depth analysis of model errors and uncertainties based on the Processor outputs will address the impact of clouds on the simulations.

It would be good to comment on impact of your work, if any, on the way NWP centers proceed with bias correction, assuming model has no bias. We see in Table 1 that biases seen at the two centers can vary significantly in 188 GHZ channels.

Added in the introduction, line 96:

It is also worth noting that bias correction schemes are generally applied to observations, especially satellite radiances, used in data assimilation systems. Corrections are performed with respect to the model background or analysis depending of the chosen scheme. Although this works for theoretical unbiased NWP models, real world data assimilation systems also use reliable observations whose role is to anchor the analysis. These anchoring observations although they may be slightly biased with respect to the truth are not corrected in the data assimilation system. As a result, background and analysis are weighted by the average of the non-zero biases in the model and in the anchor observations. Eyre (2016) however demonstrated that a risk inherent to bias correction schemes is a decrease of the weight given to anchor observations when the number of assimilated bias-corrected observations increases, which results in model background and analysis to be increasingly weighted toward the bias in the model. To avoid this situation, the Eyre (2016) suggests that correction should be derived from areas where NWP model bias are expected to be small, along with the use of numerous anchor observations.

Line 207 “Variational bias correction of satellite radiances (and aircraft temperatures) is based on Dee (2004) and Auligné et al (2007)” changed for:

Variational bias correction of satellite radiances (and, unlike the Met Office scheme, aircraft temperatures) is based on Dee (2004) and Auligné et al (2007).

Added in the conclusion, line 859:

GRUAN Processor-based studies also have the potential to refine and improve bias correction schemes used in NWP centres by helping identify regions where NWP model biases are small as suggested by Eyre (2016). Similarly, the processing and inter comparison of multiple radiosonde types can help determine which sets of observations could be use as anchors.

Other change:

Moved paragraph line 97-105 to line 55.

Reference:

Eyre, J. R., 2016: Observation bias correction schemes in data assimilation systems: a theoretical study of some of their properties, Q. J. R. Meteorol. Soc., 142(699), pp.2284-2291, DOI:10.1002/qj.2819.

Using reference radiosondes to characterise NWP model uncertainty for improved satellite calibration and validation.

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Abstract

The characterisation of errors and uncertainties in numerical weather prediction (NWP) model fields is a major challenge that is addressed as part of the Horizon 2020 Gap Analysis for Integrated Atmospheric ECV CLimate Monitoring (GAIA-CLIM) project. In that regard, observations from the GCOS (Global Climate Observing System) Reference Upper-Air Network (GRUAN) radiosondes are being used at the Met Office and European Centre for Medium-range Weather Forecasts (ECMWF) to assess errors and uncertainties associated with model data.

The software introduced in this study and referred to as the GRUAN Processor has been developed to collocate GRUAN radiosonde profiles and NWP model fields, simulate top-of-atmosphere brightness temperature at frequencies used by space-borne instruments, and propagate GRUAN uncertainties in that simulation. A mathematical framework used to estimate and assess the uncertainty budget of the comparison of simulated brightness temperature is also proposed.

One year of GRUAN radiosondes and matching NWP fields from the Met Office and ECMWF have been processed and analysed for the purposes of demonstration of capability. We present preliminary results confirming the presence of known biases in the temperature and humidity profiles of both NWP centres. The night-time difference between GRUAN and Met Office (ECMWF) simulated brightness temperature at microwave frequencies predominantly sensitive to temperature is on average smaller than 0.1K (0.4K). Similarly, this difference is on average smaller than 0.5K (0.4K) at microwave frequencies predominantly sensitive to humidity.

The uncertainty estimated for the Met Office – GRUAN difference ranges from 0.08 to 0.13K for temperature sensitive frequencies and from 1.6 to 2.5K for humidity sensitive frequencies. From the analysed sampling, 90% of the comparisons are found to be in statistical agreement.

This initial study has the potential to be extended to a larger collection of GRUAN profiles, covering multiple sites and years, with the aim of providing a robust estimation of both errors and uncertainties of NWP model fields in radiance space for a selection of key microwave and infrared frequencies.

1. Introduction

Space-borne observational datasets are EOS key-components that have led to significant advances in climate and weather applications (Joo et al., 2013; Bauer et al., 2015; Hollmann et al., 2013; Bojinski et al., 2014), and therefore must be subject to high standards of calibration and validation to meet user requirements. As part of an overall strategy for a harmonised and improved instrument calibration, the World Meteorological Organisation (WMO), Coordination Group for Meteorological Satellite (CGMS), and Global Space-based Inter-Calibration System (GSICS) have advocated the need to tie the measurements to absolute references and primary standards (WMO, 2011¹; GSICS, 2015²). In most cases however, commonly used validation techniques, as discussed by Zeng et al. (2015) and Loew et al. (2017), do not yet provide a full metrological traceability.

For a full metrological traceability and uncertainty quantification, Green et al (2018) suggested mirroring the measurement protocols as described by Immler et al (2010). Accordingly, consistency between two independent measurements, m_1 and m_2 , is achieved when:

$$|m_1 - m_2| < k \sqrt{\sigma^2 + u_1^2 + u_2^2} \quad (1)$$

where u_1 and u_2 are the total uncertainties associated with m_1 and m_2 , respectively. σ represents the intrinsic uncertainties of the comparison. In the case of a comparison between radiosonde and satellite observations for example, this term can represent the collocation uncertainty (Calbet et al., 2017). k is a coverage factor expanding the confidence interval for normally distributed error probability.

In this paper, we use the terms error and uncertainty as described in the International Vocabulary of Metrology (VIM) (JCGM, 2012³). The uncertainty is described in the VIM as a non-negative parameter characterizing the dispersion of the quantity values being attributed to the quantity intended to be measured, based on the information used. It is emphasized that all components of the uncertainty contribute to this dispersion. This includes systematic effects arising from, for example, corrections or reference standards. If a systematic effect is unknown it is unaccounted in the uncertainty budget but contributes to the error.

The error is defined as the measured quantity value minus the unknown true value and may be composed of a random and a systematic component.

For satellite data, pre-launch calibration characteristics are often provided by the instrument manufacturer or space agency. However at launch, an uncertainty chain that may have been metrologically traceable during the laboratory calibration phase can become compromised due to changes in the spacecraft during the launch process itself as well as changes in the satellite

¹ https://library.wmo.int/opac/doc_num.php?explnum_id=3710

² http://www.wmo.int/pages/prog/sat/documents/GSICS-RD002_Vision.pdf

³ <https://www.bipm.org/en/publications/guides/vim.html>

environment in orbit compared to the laboratory testing. Furthermore, the instruments also degrade over time, sometimes in quite a complex manner. These issues coupled with the current lack of true on-board traceable references makes creating a metrologically traceable uncertainty chain difficult for the satellite data record.

This aspect is being addressed by the Fidelity and Uncertainty in Climate Data Records from Space (FIDUCEO) project (<http://www.fiduceo.eu/>). The project aims to develop Fundamental Climate Data Records (FCDR) by reprocessing existing observations from raw satellite data to geolocated and calibrated radiances with traceable uncertainties from a set of different references at the pixel level. The uncertainty characterisation will account for the physical basis of the sensing process, the on-board calibration system, and an estimate for the uncertainties arising from the processing.

The (re)assessment of historical, well-established, and new space-borne instruments using data assimilation systems has become, over the past decade, common practice in numerical weather prediction (NWP) centres (Bell et al., 2008; Zou et al., 2011; Bormann et al., 2013; Lu and Bell, 2014). NWP models offer an interesting framework for the assessment of observational datasets due to a physically constrained, continuous, global, and homogeneous representation of the atmosphere. An optimal estimation of the state of the atmosphere is routinely performed in data assimilation systems by blending information from a large volume of observations (space-borne, air-borne, and ground-based) with a short-range forecast. Diagnostics are calculated in satellite observation space, typically in brightness temperature, thanks to the radiative transfer models used by data assimilation systems (Saunders et al., 2018). This forward approach is better posed than the inverse problem, that is to say comparing model geophysical fields to retrieved satellite profiles, since multiple atmospheric states can provide solutions to the retrieval, introducing further uncertainty. NWP representation of atmospheric temperature and humidity fields is of sufficient quality to enable the characterisation of subtle biases in satellite observations as demonstrated in the work referenced herein. Loew et al. (2017) reported model fields uncertainties in the satellite observation space ranging from 0.05 to 0.2K at frequencies principally sensitive to mid-tropospheric and lower stratospheric temperature, and from 1 to 2K at frequencies sensitive to mid and upper tropospheric humidity. However, those estimations arise from sensitivity studies and not from robust uncertainty analyses. Stochastic approaches, based on ensemble forecasting techniques, have been used to estimate forecast uncertainties, but with the caveat that they do not represent the systematic model biases (Leutbecher et al., 2017).

This lack of metrologically traceable characterisation has often hampered the recognition and consideration of model-based assessment outside of the NWP context, especially at space agency and instrument team levels. Key climate users can also benefit from this approach, which has begun to find resonance in the climate community (e.g. Massonnet et al., 2016).

It is also worth noting that bias correction schemes are generally applied to observations, especially satellite radiances, used in data assimilation systems. Corrections are performed with respect to the model background or analysis depending of the chosen scheme. Although this works for theoretical unbiased NWP models, real world data assimilation systems also use reliable observations whose

role is to anchor the analysis. These anchoring observations although they may be slightly biased with respect to the truth are not corrected in the data assimilation system. As a result, background and analysis are weighted by the average of the non-zero biases in the model and in the anchor observations. Eyre (2016) however demonstrated that a risk inherent to bias correction schemes is a decrease of the weight given to anchor observations when the number of assimilated bias-corrected observations increases, which results in model background and analysis to be increasingly weighted toward the bias in the model. To avoid this situation, the Eyre (2016) suggests that correction should be derived from areas where NWP model bias are expected to be small, along with the use of numerous anchor observations.

In this paper, we use the terms *error* and *uncertainty* as described in the International Vocabulary of Metrology (VIM) (JCGM, 2012⁴). The uncertainty is described in the VIM as a non-negative parameter characterizing the dispersion of the quantity values being attributed to the quantity intended to be measured, based on the information used. It is emphasized that all components of the uncertainty contribute to this dispersion. This includes systematic effects arising from, for example, corrections or reference standards. If a systematic effect is unknown it is unaccounted in the uncertainty budget but contributes to the error.

The error is defined as the measured quantity value minus the unknown true value and may be composed of a random and a systematic component.

The Gap Analysis for Integrated Atmospheric ECV CLimate Monitoring (GAIA-CLIM) project (Thorne et al., 2017) aims to address those challenges by improving the use of in-situ observations to rigorously characterise a set of atmospheric Essential Climate Variables (ECVs) derived from satellite observations as well as the geolocated and calibrated spectral radiances (level 1b) from which these quantities are derived (<http://www.gaia-clim.eu/>). The work presented here is embedded in that framework and focuses on developing NWP as a comprehensive reference by establishing traceability for the model fields through comparison with traceable comparator data.

The NWP model error and uncertainty budget can be expressed as a function of four main contributions:

- a) The error and uncertainty in NWP temperature and humidity fields mapped to observation space (brightness temperature).
- b) The error and uncertainty in the underlying radiative transfer modelling, including biases between fast radiative transfer models commonly used in NWP and reference line-by-line models, fundamental spectroscopic uncertainty, and surface emissivity uncertainty.
- c) The error and uncertainty due to scale mismatch. This encompasses the different scale at which observation and model are resolved, and the scale of natural variability that is, especially for humidity, much smaller than both observation and model scales.

⁴ <https://www.bipm.org/en/publications/guides/vim.html>

- d) The error and uncertainty due to residual cloud. Clear-sky scenes are generally preferred because simulated cloudy radiances are affected by uncertainties in model representation of cloud amounts and the absorption and scattering properties of hydrometeors.

This study aims to address the first contribution. To that end, the Met Office and European Centre for Medium-range Weather Forecasts (ECMWF) models are compared to radiosondes from the Global Climate Observing System (GCOS) Reference Upper-Air Network (GRUAN) in a stand-alone module based on the core radiative transfer modelling capability of the fast radiative transfer model RTTOV and the Radiance Simulator (both available on <http://www.nwpsaf.eu/>). This software, referred to as the GRUAN Processor, enables the collocation of geophysical fields and simulation of top-of-atmosphere (TOA) brightness temperatures (Tb) from radiosondes and NWP models, with GRUAN uncertainties propagated into the radiative transfer calculation.

Section 2 introduces the datasets used for this study, namely GRUAN radiosondes and the NWP models from the Met Office and ECMWF. Sections 3 and 4 describes the GRUAN Processor functionality and presents an illustrative case study. A methodology statistically assessing the uncertainties is presented in section 5. Section 6 concludes the study.

2. Datasets

2.1. GRUAN

With 17 sites across the world (including two inactive sites in the Pacific), GCOS is building on existing infrastructures to develop a reference network for upper-air observations (<http://www.gruan.org/>). GRUAN aims to provide long-term high-quality measurements of ECVs with vertically resolved uncertainty estimates. To meet the strict criteria for reference measurements, GRUAN data also includes a comprehensive collection of metadata and documentation of correction algorithms.

To date, only the Vaisala RS92 radiosonde is used to produce the GRUAN certified products (Sommer et al., 2016), referred to as RS92 GRUAN Data Product Version 2 (RS92-GDP), but a new product based on the Vaisala RS41 is in preparation. The RS92 GRUAN processing is documented by Dirksen et al (2014). This includes the correction of the radiosonde systematic errors, due to mainly solar radiation, and the derivation of the uncertainties for temperature, humidity, wind, pressure, and geopotential height. The total uncertainty budget accounts for correlated and uncorrelated contributions of both random sources of uncertainty and uncertainties from systematic error corrections, and it is expressed as the root sum square of all contributions. The uncertainty related to the short wave radiation correction (used in the temperature uncertainty budget), the correlated uncertainty related to systematic error corrections, and uncorrelated uncertainty (standard deviation) derived from the GRUAN processing are available in the RS92-GDP files, in addition to the total uncertainty of each variables. However, not all correlated and uncorrelated components are independently available (albeit used in the calculation of the total uncertainty) and some sources of partially correlated uncertainty are not yet modelled in GRUAN algorithms (e.g. the pendulum

motion of the radiosonde under the balloon). Therefore, only the total uncertainties of temperature, humidity, and pressure are considered in this study.

The results presented in this preliminary study focus on the profiles from Lindenberg (LIN), GRUAN lead centre, Germany (52.21°N, 14.12°E) for the year 2016.

2.2. Met Office NWP

Met Office model data files are extracted from the Managed Archive Storage System (MASS) and only $\pm 5^\circ$ latitude and longitude around the GRUAN launch site is kept to limit the data volume. For LIN, the model fields cover the area 47.109-57.109°N and 9.0234-19.102°E. Each model data file contains four time steps starting at T+0, the analysis, and three successive 3-hour forecasts referred to as T+3, T+6, and T+9. The Met Office data assimilation system is a hybrid 4-dimensional variational analysis (4D-Var) with 6-hour time window (Lorenc et al., 2000; Rawlins et al., 2007). Four analyses (and their successive forecasts) are available every day at 00:00, 06:00, 12:00, and 18:00 Coordinated Universal Time (UTC). Assimilated satellite radiances are corrected with a variational bias correction similar to the scheme described by Auligné et al. (2007). The operational forecast model in 2016 had a resolution of approximately 17km at mid-latitudes for 70 levels from surface to 80km (N768L70). The radiative transfer calculation was performed in 2016 by the fast radiative transfer model RTTOV version 9 (Saunders et al., 1999, 2007).

In the Met Office NWP system, the interpolation of background fields is performed twice, once for all observations and later just for those observations to be assimilated. The radiosonde profiles are averaged over the vertical model layers. Latitude, longitude, and time at each level are used in the first interpolation of background values, but fixed coordinates are used in the latter interpolation. A bias correction of radiosonde profiles is in place on a per station basis but is generally not applied where RS92 are used. As noted by Ingleby and Edwards (2015), radiation corrections are now often directly applied by the radiosonde manufacturer such as Vaisala, which reduces the need for correction in NWP system. Bias correction and quality controls operationally applied to radiosonde at the Met Office are detailed in the appendix 1 of Ingleby and Edwards (2015).

2.3. ECMWF NWP

ECMWF data are extracted from the Meteorological Archival and Retrieval System (MARS⁵). Data come from the operational data class atmospheric model long window 4Dvar stream (see MARS documentation for details). The covered area is the same as for the Met Office. Each model data file contains six time steps of three hours starting from T+0 to T+15. The ECMWF analysis/forecast system is documented by ECMWF⁶. A cubic octahedral reduced Gaussian grid is currently used with a resolution of TCo1279 (horizontal grid spacing of about 9 km) and with 137 levels in the vertical. Note that from February 2006 until June 2013, there were 91 vertical levels, and from January 2010 until March 2016 a linear reduced Gaussian grid was used with a horizontal spacing of around 16 km.

⁵ <https://software.ecmwf.int/wiki/display/UDOC/MARS+user+documentation>

⁶ <https://www.ecmwf.int/en/forecasts/documentation-and-support>

Data assimilation uses incremental 4D-Var (Courtier et al., 1994) with a 12-hour window, the nominal 00:00 UTC analysis uses data from 21:00 UTC to 09:00 UTC. Forecasts and ensembles are run twice daily from early-delivery 6-hour window 4D-Var analyses (Haseler, 2004). Flow-dependent ensemble information from the ECMWF ensemble of data assimilations is incorporated into the modelling of background-error covariances (Bonavita et al., 2016). Satellite radiative transfer calculations use the fast radiative transfer model RTTOV version 11.2 (Hocking et al., 2015) has been used operationally since May 2015 (Lupu and Geer, 2015). Variational bias correction of satellite radiances (and, unlike the Met Office scheme, aircraft temperatures) is based on Dee (2004) and Auligné et al (2007). ~~Variational bias correction of satellite radiances (and aircraft temperatures) is based on Dee (2004) and Auligné et al (2007).~~

The treatment of radiosondes in the ECMWF system differs from that of the Met Office in that there is no average on model levels and each level is treated as a point value. In addition, the balloon drift in space and time was not accounted for in 2016 (i.e. the ascension was assumed instantaneous and vertical). The treatment of the radiosonde drift (from BUFR reports) has been introduced in the operational system in 2018 (Ingleby et al., 2018). Also in contrast to the Met Office, radiosondes at ECMWF are bias corrected for temperature and humidity. The correction, described by Agustí-Panareda et al (2009), uses monthly statistics of background departure based on night-time RS92 and is applied as a function of radiosonde type, pressure, and solar elevation angle.

3. Processor design

The GRUAN Processor, a software based on the NWP Satellite Application Facility (SAF) Radiance Simulator (Smith, 2017), is designed to collocate NWP model fields from the Met Office or ECMWF with radiosondes from the GRUAN network and simulate TOA Tb from those collocated profiles. The simulations are performed at frequencies used by meteorological space-borne instruments and supported by RTTOV. Figure 1 illustrates the Processor top-level design with its main processing steps.

3.1. Inputs

The Processor requires as input a GRUAN and a model data file. Supported products are GRUAN RS92-GDP, Met Office Unified Model (UM) Fieldfiles (or PP files, see Smith (2017)), and ECMWF GRIB files. Both model file types must contain the minimum set of required variables as described by Smith (2017) for the Radiance Simulator. Processing options and RTTOV attributes are provided via a text file read by the Processor. This file includes the instrument characteristics (e.g. channels) to be simulated and output options (output in unit of radiances or Tb for example). Optionally, RTTOV bias and root mean square error (rmse) estimated from comparisons between RTTOV and line-by-line model calculations, as provided by NWP SAF⁷, can be written to the output files. Finally, an option allows to opt for a model-radiosonde collocation following the balloon drift (in space and time, see

⁷ <https://www.nwpsaf.eu/site/software/rttov/download/coefficients/comparison-with-lbl-simulations/>

section 3.3) or assuming no drift. Note that all collocations presented in this paper account for the radiosonde drift.

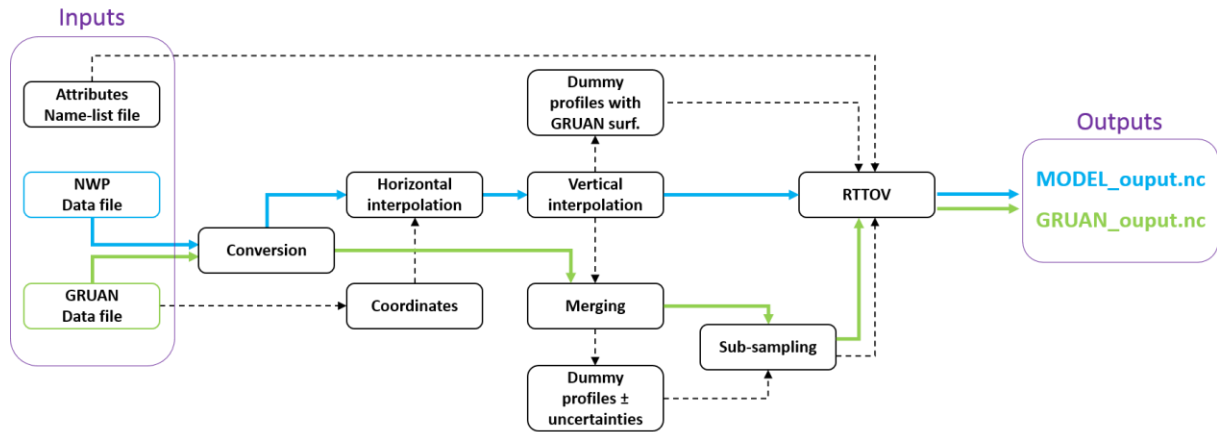


Figure1: GRUAN Processor top-level design. Solid arrows show the main processing steps from input (blue for NWP model data and green for GRUAN data) to output. Dashed arrows represent the internal processing.

3.2. Conversion

The conversion step ensures that both model and GRUAN variables (e.g. temperature or humidity) are expressed in the same units and that those units are compatible with RTTOV (see section 3.5). Two main types of conversion are supported: temperature from potential temperature and specific humidity from relative humidity.

Model data files may sometimes contain potential temperature instead of temperature profiles, as is the case for the Met Office. Temperature (T) is therefore calculated as a function of potential temperature (θ) and pressure (P) as follows:

$$T = \theta \left(\frac{P}{P_0} \right)^\kappa \quad (2)$$

where P_0 is the standard reference pressure equal to 1000hPa and κ the ratio of the gas constant of air to the specific heat capacity at constant pressure.

Similarly, it is worth noting that model data files may not directly contain pressure profiles (e.g. in ECMWF files) or the pressure may be expressed on a different set of levels with respect to other variables (e.g. Met Office files). In both cases however, the pressure on model levels can be calculated from coefficients provided in the model data files.

The expression of humidity also needs to be harmonised. GRUAN provides profiles of relative humidity (RH), whereas the humidity from both NWP models is expressed in specific humidity (q), in units kg.kg^{-1} . GRUAN RH is converted to q as follows:

$$q = \frac{\varepsilon RH e_s}{(P - (1 - \varepsilon) RH e_s)} \quad (3)$$

where ε is the ratio of the molecular weight of water vapour to the molecular weight of dry air and e_s the saturation vapour pressure over liquid. For consistency with GRUAN and Vaisala processing, e_s is expressed as defined by Hyland and Wexler (1983), such that:

$$\ln(e_s) = \frac{C_1}{T} + C_2 + C_3 T + C_4 T^2 + C_5 T^3 + C_6 \ln(T) \quad (4)$$

with:

$$C_1 = -5.8002206 \times 10^3$$

$$C_2 = 1.3914993 \times 10^0$$

$$C_3 = -4.8640239 \times 10^{-2}$$

$$C_4 = 4.1764768 \times 10^{-5}$$

$$C_5 = -1.4452093 \times 10^{-8}$$

$$C_6 = 6.5459673 \times 10^0$$

for e_s in Pa and T in K.

3.3. Interpolations

The GRUAN Processor generates a set of model profiles (i.e. one profile per variable), on model levels, interpolated in space and time along the radiosonde path, which are then vertically interpolated on a fixed set of 278 levels as follows.

First, model fields are linearly interpolated at the radiosonde coordinates (latitude-longitude-time), weighted by the distance to the eight closest grid points. Therefore, for an observation at the coordinate $p=[x_p, y_p, z_p]$, as illustrated on figure 2, in a cube of vertices $[(x,y,z), (x+dx,y,z), (x,y+dy,z), (x,y,z+dz), (x+dx,y+dy,z), (x+dx,y,z+dz), (x,y+dy,z+dz), (x+dx,y+dy,z+dz)]$, where dx and dy represent the grid point interval in latitude and longitude, respectively, and dz the interval between the time $T+n$ and $T+(n+3)$, with associated field values F_p and $[F_{000}, F_{100}, F_{010}, F_{001}, F_{110}, F_{101}, F_{011}, F_{111}]$, respectively, F_p is calculated as follows:

$$\begin{aligned}
F_p = & F_{000}(1 - w_x)(1 - w_y)(1 - w_z) \\
& + F_{100}w_x(1 - w_y)(1 - w_z) \\
& + F_{010}(1 - w_x)w_y(1 - w_z) \\
& + F_{001}(1 - w_x)(1 - w_y)w_z \\
& + F_{101}w_x(1 - w_y)w_z \\
& + F_{011}(1 - w_x)w_yw_z \\
& + F_{110}w_xw_y(1 - w_z) \\
& + F_{111}w_xw_yw_z
\end{aligned} \tag{5}$$

314

315 where w_x , w_y , and w_z are the weights defined as:

$$w_x = (x_p - x)/dx \tag{6}$$

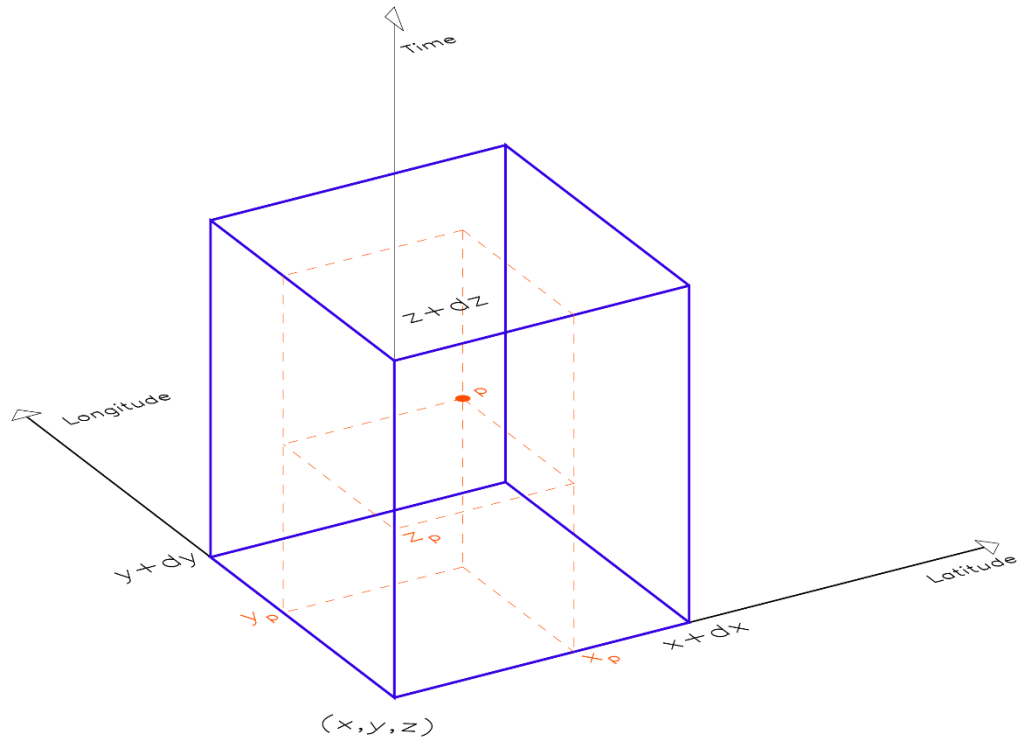
$$w_y = (y_p - y)/dy \tag{7}$$

$$w_z = (z_p - z)/dz \tag{8}$$

316

317 This operation is repeated along the radiosonde path with a time-step of 15 seconds based on the
318 radiosonde time profile. A unique model profile (one for each variable) is reconstructed by
319 combining the model fields from the pressure levels crossed by the radiosonde between two
320 consecutive interpolated model profiles.

321



322

323 Figure 2: illustration of an observation of coordinate (x_p, y_p, z_p) in a cube that vertices represent the
324 model latitude (x axis), longitude (y axis), and forecast time (z axis).

325

The reconstructed set of profiles is then interpolated on a fixed vertical grid of 278 pressure levels. The fixed grid, referred to as Processor grid (Pg), has been designed to have at least one Pg level between any two levels of the coarser model (Met Office or ECMWF) grid, referred to as Coarse grid (Cg). Therefore, for Pg of dimension n equal to 278 and Cg of dimension m (equal to 70 for the Met Office, 91 or 137 for ECMWF), the interpolation is calculated by weighting the fields with respect to the pressure via the interpolation matrix W of dimension $n \times m$, such as:

$$Pg = W Cg \quad (9)$$

where for the j^{th} pressure (P) level of Pg located between the i^{th} and $i+1^{\text{th}}$ levels of Cg :

$$Pg_j = W_{j1} Cg_1 + W_{j2} Cg_2 + \dots + W_{jm} Cg_m \quad (10)$$

$$W_{ji} = \frac{P_{i+1} - P_j}{P_{i+1} - P_i} \quad (11)$$

$$W_{ji+1} = 1 - W_{ji} \quad (12)$$

$$W_{jk} = 0 \text{ where } k \neq i, i + 1 \quad (13)$$

The vertical interpolation of model profiles as well as the subsampling of the radiosonde profiles (see section 3.4) to the Processor grid aims to provide a homogenised number of vertical levels on which the radiative transfer equation is calculated. Although the coarse model grid and the fine radiosonde grid could be directly used as input in RTTOV, it was observed that the lack of homogenisation between model and radiosonde profiles causes a bias in radiance space. It was therefore decided to interpolate the model profiles and provide a way to estimate the uncertainty associated to this interpolation (see section 5).

Figure 3 illustrates the change from a collocated Met Office temperature profile (LIN 31 December 2016, 16:00 UTC) on model levels (70 levels) (a) to a collocated Met Office profile interpolated on the Processor grid (278 levels) (b).

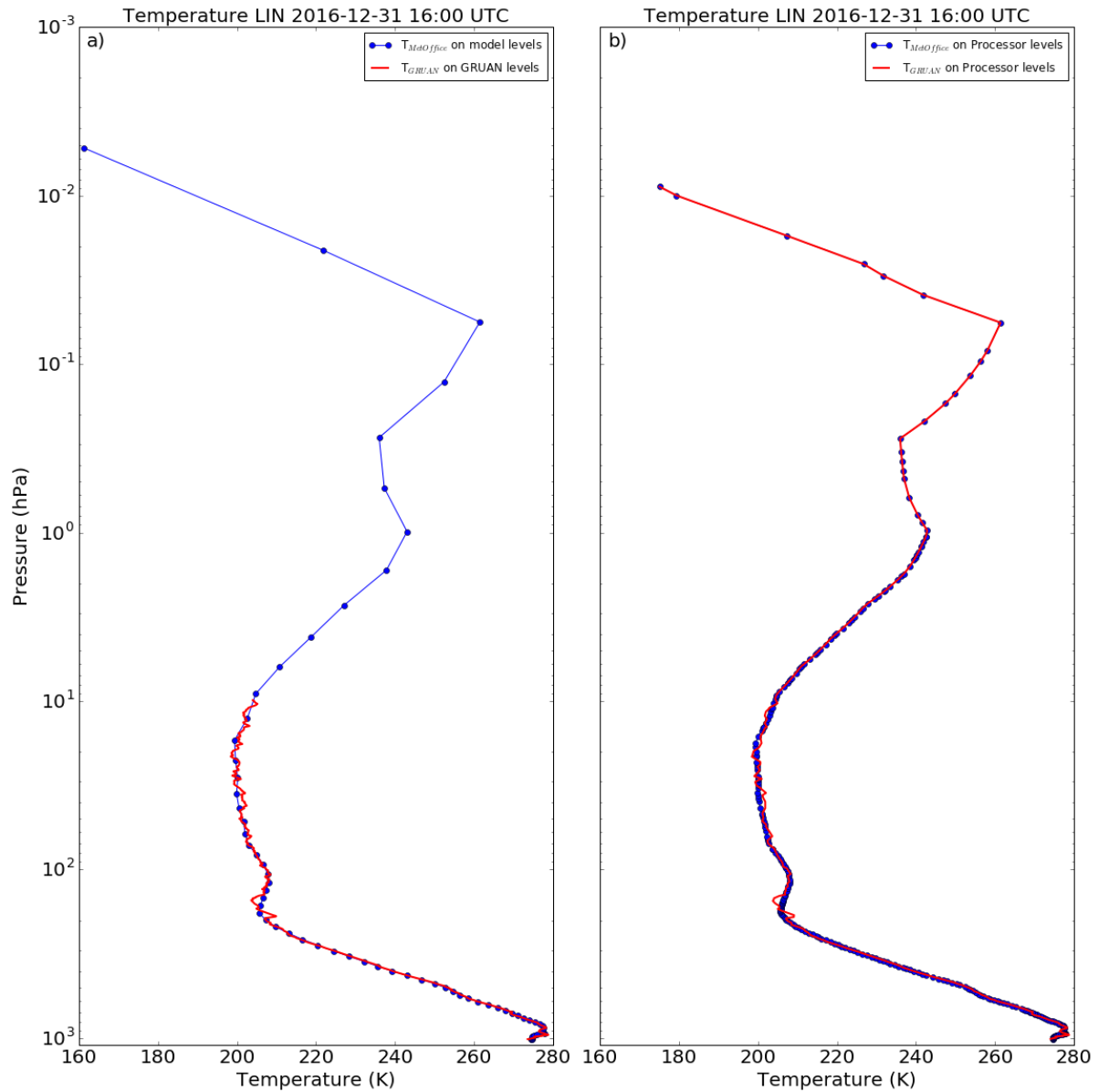


Figure 3: (a) GRUAN temperature profile (red line) from Lindenberg on 31 December 2016, 16:00 UTC as provided in the RS92-GDP data file with full GRUAN vertical resolution and collocated Met Office temperature profile (blue dotted line) on the model vertical levels. (b) GRUAN temperature profile subsampled at the Processor 278 pressure levels and merged with the Met Office profile above 9.8 hPa (red line) and collocated Met Office temperature profile interpolated on the Processor vertical levels (blue dotted line).

3.4. Merging and subsampling

A caveat of processing radiosonde profiles in RTTOV is the lack of information between the top of a profile (bursting point of the balloon) and the TOA. This is addressed by merging the radiosonde profiles with the model profiles above the last available point of the radiosonde. Note that this step occurs after the interpolation of the model profiles so that the upper merged part of the radiosonde and model profiles are strictly identical.

Similarly, RTTOV requires surfaces information: 2m temperature and humidity, surface pressure and altitude, 10m wind (u and v components, used for microwave simulations over ocean), and skin temperature. While GRUAN provides the surface pressure, temperature, relative humidity, and altitude at launch site in all the data files, the skin temperature (T_{skin}^G) has to be derived from the difference between the model skin (T_{skin}^M) and the 2m temperature (T_{2m}^M) applied to the GRUAN surface temperature (T_{2m}^G) such as:

$$T_{skin}^G = T_{2m}^G + (T_{skin}^M - T_{2m}^M) \quad (14)$$

Although the 10m wind could be provided by the Vaisala wind profiles (available in GRUAN data files) or calculated from GRUAN profiles of wind speed and direction, the chaotic rotation of the radiosonde just after launch results in unreliable wind information near the surface. Therefore, the model 10m wind (u and v components) is also merged with the GRUAN data. Note that 10m wind is used to calculate the sea surface emissivity (for microwave simulations) and therefore only concerns GRUAN sites on small island sites (i.e. La Reunion, Nauru, Manau, Ny-Ålesund, Graciosa, and Tenerife).

In the raw RS92 data and GRUAN data, the samplings are provided every second but filtering reduces the effective resolution of temperature to approximately 10s at low levels; the effective resolution of humidity is similar but it is reduced to 40-50s at upper levels (Dirksen et al., 2014). As a result, GRUAN profiles count several thousand levels in the vertical that need to be reduced to the number of levels on the Processor grid. This is achieved with a subsampling of the radiosonde profiles to the nearest levels for each of the 278 Processor pressure levels, at levels where data are available, with the imposed constraint that the ratio radiosonde pressure by Processor pressure must be less than 0.1%.

The subsampling of GRUAN profiles has been preferred over layer-averaging or convolution techniques for several reasons. First, we aimed to avoid all unnecessary modification of the GRUAN profiles, used as reference in this study. Second, GRUAN uncertainties are vertically resolved and their processing would have resulted in an information loss. Third, the aim of the Processor is to evaluate uncertainties in radiance space. During the testing phase, we observed that neither the choice of averaged layers nor sub-sampled levels significantly affects the calculation of radiative transfer and the resulting brightness temperatures.

Fig. 3 shows the changes from a GRUAN temperature profile (LIN 31 December 2016, 16:00 UTC) as provided in the RS92-GDP data file (5821 levels, from the surface to 9.88 hPa) (a) to a Processor merged and subsampled profile (278 levels, from the surface to 0.008 hPa) (b).

3.5. RTTOV and uncertainties

The radiosonde and model profiles, both on the Processor vertical grid, and their respective surface parameters are passed to RTTOV for the calculation of the TOA Tb. RTTOV version 11.3, currently used by the GRUAN Processor, is documented by Hocking et al. (2015).

The surface emissivity depends on the surface type. For land and sea ice, the Processor uses a fixed value, 0.95 and 0.92, respectively. Those estimates are potentially far from the truth, but any bias introduced by fixed emissivity terms is expected to cancel out when the difference in simulated Tb is calculated. Note that RTTOV allows the use of the emissivity atlases over land and sea ice, but this option has not yet been investigated. Over sea, the surface emissivity is calculated by the RTTOV FAST Emissivity Model (FASTEM) version 5 (Kazumori and English, 2015). Although the version 5 is the default version, this can be changed in the input attribute file. It is worth noting here that although the radiosonde may drift from above land to above sea (ice) (or the opposite), the surface type can only be of one kind. The land surface type is typically used as most radiosonde launch sites are well inside land masses. However, for the small island sites of La Reunion, Nauru, Manau, Ny-Ålesund, Graciosa, and Tenerife, the radiosonde is expected to rapidly drift over sea and therefore the sea surface type is used instead. The difference between sea and sea ice is controlled by the sea-ice mask used by the NWP model.

The viewing angle is set by default to nadir (0°) for all simulations. However, different angles could potentially be used for the purpose of better comparisons with real satellite data, for example.

All simulations assume clear sky scenes and uses RTTOV direct mode (ignoring the scattering) with the cloud liquid water option off (data not available from GRUAN data file). It is acknowledged that this may introduce discrepancies in the comparison between model and radiosonde in situations where the radiosonde encounters one or several cloud layers. The brightness temperatures calculated from the radiosonde data perturbed by the presence of clouds (e.g. peaks in the humidity profile and to a lesser extent in the temperature profile) will differ from those calculated from the model data that assume clear sky conditions. Because the RS92-GDP does not provide a cloud flag, indirect screening may be required for fine comparisons. To that end, one can use the precipitable water column from the RS92-GDP metadata as a proxy for cloud and or assume the presence of cloud when the relative humidity exceeds a threshold value.

Finally, note that RTTOV interpolation mode (used to interpolate the input levels to the coefficient levels for the calculation of the atmospheric optical depth, and then back from the coefficient levels to the input levels for the calculation of the radiative transfer equation) uses the log-linear on weighting function mode as described by Hocking et al. (2015). This is aimed to avoid a known issue causing the oscillation of the temperature Jacobians.

It was observed that the interpolation of the model fields at the GRUAN launch site coordinates results in large discrepancies, especially affecting surface parameters (surface pressure and elevation) and the lower part of the profiles, when the local orography presents large variations at scales of the same order as the model grid resolution. The interpolation, using the weighted average of the four neighbouring grid points at a given forecast time may result in the model surface being below or above the actual GRUAN launch site surface. A typical example is the site at La Réunion where the radiosondes are launched from the Maïdo observatory at an altitude of 2200m, compared to which the interpolation of the ECMWF model gives an altitude of 980m and the interpolation of the Met Office model 0m. In Lindenberg by comparison, the radiosondes are launched from the altitude of 103m while both models estimates the altitude to be 57m. To estimate the associated error, a set of dummy model profiles are generated with the surface pressure forced to that

provided in the GRUAN metadata. If the model has a surface below that of the observations, the model profiles are linearly interpolated and cut at the observed surface pressure, and the surface parameters become those of the lowest level. If the model has a surface above that of the observations, the model profiles are linearly extrapolated to the observed surface pressure, and the model surface parameters become those of the new lowest level. The difference between the T_b calculated from those modified profiles and the T_b calculated from the original profiles provides an estimation of the associated error. This is referred to as u_surf_bt in the Processor output.

Finally, the GRUAN uncertainties are propagated into radiance space. As described by Calbet et al. (2017), this can be achieved by multiplying the GRUAN profiles of uncertainty by the Jacobians derived by RTTOV from the GRUAN atmospheric profiles, or by applying the radiative transfer to the input atmospheric GRUAN profiles perturbed with their associated uncertainties. The GRUAN Processor is designed to follow the second method although the first one will be further discussed in section 5. In the Processor, two sets of perturbed profiles are created, one containing the GRUAN profiles of temperature, pressure, and humidity, incremented by their respective total uncertainty ($T+u_temp$, $P+u_press$, and $q+u_q$), and one containing the GRUAN profiles decremented by their total uncertainty ($T-u_temp$, $P-u_press$, and $q-u_q$). The resulting brightness temperatures calculated by RTTOV based on those two sets of perturbed profiles, referred to as Tb^+ and Tb^- , respectively, are compared to Tb , calculated with the unperturbed profiles, to estimate the associated uncertainty in radiance space. The greatest difference between $|Tb - Tb^+|$ and $|Tb - Tb^-|$ is given in output as u_gruan_bt . Note that the eight combinations of sign that this approach can allow have been tried during the test phase. The resulting uncertainty was not found significantly different from that obtained with Tb^+ and Tb^- , but the processing time significantly increased. Tb^+ and Tb^- were therefore retained as the best compromise.

It should be noted that the simplified nature of this approach, which applies a perturbation of constant sign in the vertical, ignores the complicated fluctuations that the propagation of uncertainty via a multiplication by the Jacobians would induce (see section 5). Here, we assume that the GRUAN profiles of uncertainty used to perturb the atmospheric profiles are fully correlated at all levels. This assumption differs from the truth in that GRUAN total uncertainty consist of a root sum square of correlated and uncorrelated components (Dirksen et al., 2014). Nevertheless, assuming a fully correlated perturbation enables the estimation of the total GRUAN uncertainty upper bound in radiance space allowed by this approach. The lower bound, not addressed in the GRUAN Processor, can be obtained by assuming the uncertainty profiles completely uncorrelated, and lies close to zero as demonstrated by Calbet et al. (2017).

Ideally, the correlated and uncorrelated components of GRUAN uncertainty should be treated separately with, for example, the Monte Carlo method described in the Guide to the expression of Uncertainty in Measurement (GUM) (JCGM, 2008⁸). However, those components are not all independently available and it is currently not possible to differentiate them in the RS92-GDP. Note that the radiosonde (random and/or systematic) errors are not provided. Instead, GRUAN algorithm corrects the systematic errors in the radiosonde measurements, acknowledging that the correction

⁸ <https://www.bipm.org/en/publications/guides/gum.html>

is not perfect and introduces an associated residual uncertainty (accounted for in the total uncertainty).

For completeness, perturbations to the surface parameters could be added to the total uncertainty budget in radiance space, but GRUAN does not provide uncertainties associated with these measurements. An alternative is discussed in section 5.

3.6. Outputs

For each pair of collocated radiosonde and NWP model fields, the GRUAN Processor generates two outputs files in netcdf format. The first file contains the model-related fields including, but not limited to, the profiles of temperature, humidity, and pressure on the Processor vertical grid, the interpolation matrix W , the simulated brightness temperature, the temperature, humidity, and pressure Jacobians, and a quality control flag (qcflags). Note that for successful simulations, qcflags is equal to zero. The second file contains the GRUAN-related fields, including e.g. GRUAN atmospheric profiles and associated uncertainties on the Processor vertical grid, the Jacobians, and the T_b and T_b uncertainties estimated from the perturbed GRUAN profiles (u_gruan_bt).

Both files also contain metadata documenting the GRUAN Processor version number (here 6.2); the NWP model, model validity time, and model version number; the simulated satellite name, platform, and channel; the RTTOV version, RTTOV coefficients creation date, and bias and root mean square error (when available); and the metadata available from the original RS92-GDP.

Note that some GRUAN Processor simulated brightness temperatures have been ingested into the GAIA-CLIM Virtual Observatory (<http://gaia-clim.vo.eumetsat.int/>) for the purposes of visualisation, manipulation, and extraction of collocated GRUAN-NWP-Satellite data.

4. Data analysis illustration

For illustration purposes, one year of collocated profiles and simulated T_b is presented. The dataset corresponds to 1160 radiosondes launched from Lindenberg, Germany, in 2016, compared to the Met Office and ECMWF models. T_b values have been simulated at the Advanced Technology Microwave Sounder (ATMS) 22 channel frequencies, a microwave radiometer with sounding capability in the oxygen band (53-57GHz), sensitive to tropospheric and lower stratospheric temperature, and in the water vapour band (around 183GHz), sensitive to mid-to-upper tropospheric humidity (Bormann et al., 2013).

The dataset is divided into two samples composed of day and night-time profiles, respectively. This is aimed at discriminating the GRUAN profiles affected by solar radiation, the dominant source of uncertainty according to Dirksen et al. (2014). All profiles with a solar zenith angle (calculated as a function of latitude, longitude, and UTC) smaller (greater) than 90° at launch time is considered as day (night) time. Note that for a refined analysis, the whole profile (not just launch time) should be checked and only profiles with the sun below (or above) the horizon throughout should be used.

Note that for simplicity, no cloud screening is applied in this case study. This caveat may, as suggested in the previous section, exacerbate the biases observed when comparing brightness temperature simulated from radiosonde profiles and from model fields. Future work dedicated to the in-depth analysis of model errors and uncertainties based on the Processor outputs will address the impact of clouds on the simulations.~~Note that no cloud screening is applied in this study.~~

After screening, 573 pairs of GRUAN Processor outputs are available in daytime and 587 in night-time for each model. The mean difference $NWP - GRUAN$ in temperature, humidity, and simulated Tb is shown in figures 4 (daytime) and 5 (night-time) together with the number of available comparisons as a function of the pressure. Note that at pressures less than 10hPa, the data sampling decreases rapidly as less balloons reach those levels. An arithmetic mean is used to average the uncertainty over the sampling according to Immler et al. (2010) Eq. (4). For temperature and humidity, the GRUAN total uncertainty as provided in the RS92-GDP is used (the relative humidity uncertainty is converted into specific humidity uncertainty in the GRUAN Processor), while the uncertainty in Tb shows the GRUAN uncertainties propagated in radiance space via the perturbation of the atmospheric profiles. Note that the model uncertainty and the uncertainty associated with the vertical interpolation are ignored in this section, but addressed in section 5.

It is important to note that both Met Office and ECMWF are operationally assimilating the radiosonde profiles from the GCOS Upper Air Network (GUAN), which, in Lindenberg, are the same as the GRUAN profiles but without the specific GRUAN processing (and without uncertainty characterisation). Therefore, unlike the forecasts, the model analyses (T+0) are not completely independent from the observations. However, this is not expected to affect significantly the mean comparison as only about 5% of the profiles fall in the first time window (i.e. interpolation between T+0 and T+3).

In Figs 4 and 5, the main feature for ECMWF is a 0.5K cold bias in the stratosphere (100-10hPa), observed both day and night. This bias has also been detected by Shepherd et al. (2018) in the ERA5 reanalysis that are based on IFS cycle 41r2, the operational model in 2016. It is attributed to an excess of moisture transported into the lower stratosphere, which lead to a cold bias by radiative cooling. The model also presents a 50-75% wet bias peaking between 200 and 100hPa, slightly more pronounced during the day. This is consistent with the results from Ingleby (2017) who showed a similar behaviour for several kinds of radiosonde.

The Met Office model presents a persistent 0.2 to 0.5K cold bias at pressure greater than 300hPa and a 0.25K warm bias between 200 and 100hPa seen at night-time only. This is consistent with Ingleby and Edwards (2015) who showed similar features in the comparison between radiosondes and the Met Office regional model covering the United Kingdom. The Met Office tropospheric humidity fits generally the radiosonde profiles well but presents a 50-60% wet bias with a peculiar double peak at 200 and 100hPa. A wet bias peaking at 300hPa was already observed by Ingleby et al. (2013), the coarser vertical resolution used by the authors potentially explaining the different pressure level at which the bias is observed. However, the second maximum (at 100hPa) seems to be a new feature that appears in 2015 and persists in 2017 (not shown). This remains unexplained to date.

In radiance space, it is important to distinguish between frequencies representative of the difference $NWP - GRUAN$ and those significantly affected by the surface and the mid to upper stratosphere where the GRUAN profiles are merged with the model. Hence, ATMS frequencies sensitive to the surface (23.8-54.4 and 88.2-165.5GHz, channel 1-7 and 16-17, respectively) and to the upper stratosphere ($57.29 \pm 0.3222 \pm 0.022$ - $57.29 \pm 0.3222 \pm 0.0045$ GHz, channel 13-15, respectively) should be considered with caution and not used for scientific applications. On the contrary, frequencies sensitive to the upper tropospheric-lower stratospheric temperature (peaking between 300 and 20hPa) and to the mid tropospheric humidity (peaking between 650 and 350hPa) cover the same vertical domain as the information provided by GRUAN. For those frequencies, ATMS channel characteristics and mean Tb difference are provided in Table 1.

Table 1: Mean difference $NWP - GRUAN$ in simulated Tb for ECMWF (ΔTb_{ECMWF}) and Met Office ($\Delta Tb_{MetOffice}$) and 1σ standard deviation for ATMS channels 8-12 and 18-22 at day and night-time.

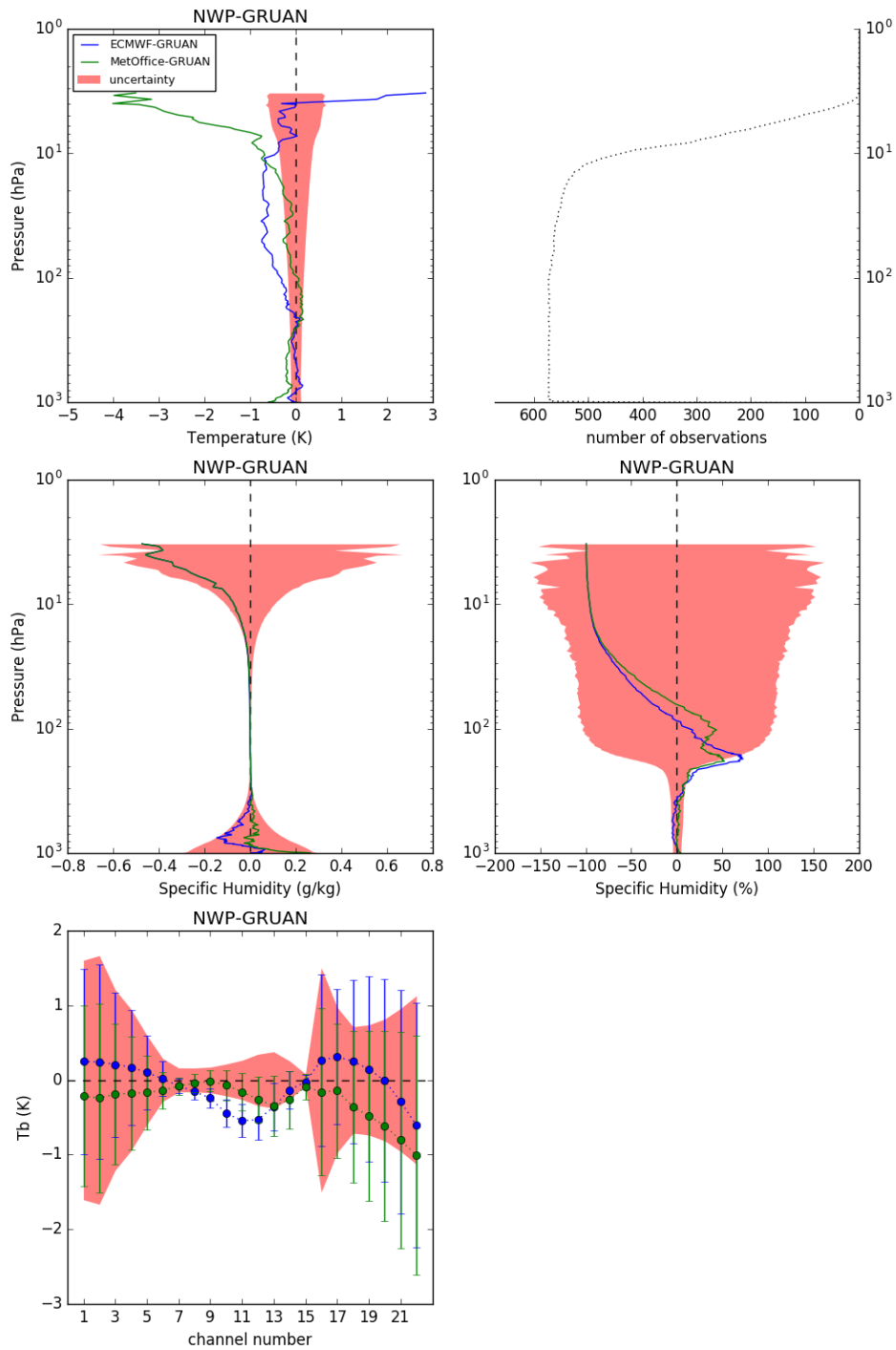
Channel	Frequency (GHz)	$\Delta Tb_{ECMWF} (1\sigma) (K)$		$\Delta Tb_{MetOffice} (1\sigma) (K)$	
		night	day	night	day
8	54.94	-0.08 (0.09)	-0.16 (0.10)	-0.00 (0.11)	-0.04 (0.12)
9	55.5	-0.15 (0.12)	-0.24 (0.13)	0.04 (0.13)	-0.02 (0.14)
10	57.29	-0.32 (0.18)	-0.45 (0.18)	0.01 (0.16)	-0.07 (0.20)
11	57.29 ± 0.217	-0.39 (0.21)	-0.54 (0.22)	-0.04 (0.20)	-0.16 (0.25)
12	$57.29 \pm 0.3222 \pm 0.048$	-0.34 (0.25)	-0.53 (0.27)	-0.09 (0.28)	-0.26 (0.31)
18	183.31 ± 7.0	0.35 (0.91)	0.25 (1.09)	0.02 (0.83)	-0.36 (1.02)
19	183.31 ± 7.0	0.37 (1.13)	0.15 (1.24)	-0.09 (1.03)	-0.48 (1.14)
20	183.31 ± 3.0	0.34 (1.31)	-0.01 (1.36)	-0.18 (1.22)	-0.61 (1.27)
21	183.31 ± 1.8	0.22 (1.48)	-0.29 (1.50)	-0.31 (1.42)	-0.81 (1.45)
22	183.31 ± 1.0	0.04 (1.61)	-0.61 (1.64)	-0.46 (1.57)	-1.01 (1.60)

At frequencies sensitive to temperature (54-57GHz, channels 8-12), hereafter referred to as temperature channels, the mean difference for ECMWF varies from -0.08 to -0.39K at night, mostly outside GRUAN uncertainty (red shading, Fig. 5), reflecting the cold bias observed in the stratosphere. Note that a difference greater than GRUAN uncertainty does not mean a statistical disagreement since the uncertainty related to the model is unaccounted for (i.e. the total uncertainty of the comparison as expressed in Eq. (1) is larger than the GRUAN uncertainty alone). The difference is slightly larger in daytime (-0.16 to -0.54K). Similarly, the difference at frequencies sensitive to humidity (around 183GHz, channels 18-22), hereafter referred to as humidity channels, varies from 0.04 to 0.37K at night (-0.01 to -0.61K during the day), within GRUAN uncertainty.

The mean difference in Tb for the Met Office is always found within GRUAN uncertainty and varies from -0.09 to 0.04K during the night (-0.02 to -0.26K in daytime) for the temperature channels and from -0.46 to 0.02K during the night (-0.36 to -1.01K in daytime) for the humidity channels.

584 The standard deviation of the differences is similar for both centres and does not vary much from
 585 day to night.

586



587

588 Figure 4: Mean difference ECMWF – GRUAN (blue) and Met Office – GRUAN (green) calculated from
 589 573 daytime collocation from Lindenberg in 2016. The temperature difference (top left) is expressed
 590 in K, the humidity difference is expressed in g.kg^{-1} (middle left) and in percentage ($\frac{\text{NWP} - \text{GRUAN}}{\text{GRUAN}}$) (middle right), and the difference in simulated brightness temperatures for the 22 ATMS
 591

channels is expressed in K (bottom) with the 1σ standard deviation (vertical bars). The red shading shows GRUAN uncertainty. The number of observations is shown as a function of the pressure (top right).

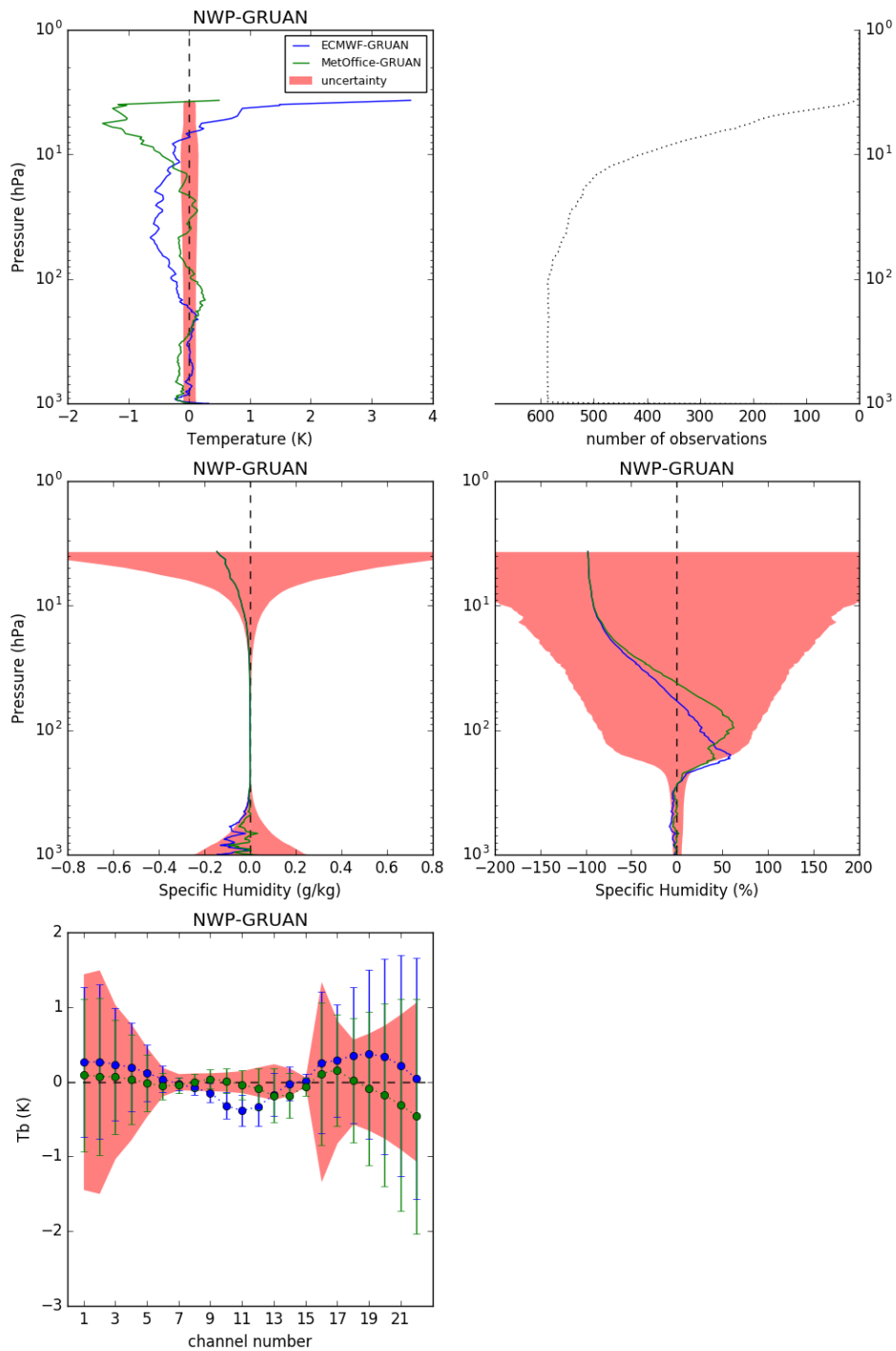


Figure 5: Same as figure 4 but for the 587 night-time collocations.

5. Comparison assessment

The previous section gives insights into the GRUAN uncertainty propagated in radiance space by the GRUAN Processor. The approach offers a rapid but incomplete evaluation of the *NWP – GRUAN* comparison, but several aspects are overlooked in the final budget, that for various reasons are not part of the internal Processor processing. This includes: a) the uncertainty associated with surface parameters, not provided in RS92-GDP and likely to change from station to station, b) the NWP model uncertainty, often expressed as a covariance matrix and used in the data assimilation process by the NWP centres, but not available in the input data files, and c) the uncertainty associated with the vertical interpolation operated by the Processor for which estimation requires information on the last two points.

In this section, a mathematical framework is elaborated to estimate a robust uncertainty budget for the comparison between NWP fields and GRUAN observations, in radiance space, and statistically assess this comparison. This includes uncertainties in the GRUAN observations, in the vertical interpolation of the GRUAN Processor, and in the model fields. Note that, as previously mentioned, any comparison to satellite radiances should also include other sources of uncertainty such as in the underlying radiative transfer models and cloud detection. For this study, we focus on the comparison to the Met Office model fields, but the same method could be applied to the comparison with ECMWF fields.

We define \mathbf{x}_{rs} as the radiosonde profiles and \mathbf{x}_m as the model profiles (temperature, humidity, and pressure, with a pressure coordinate). Note that \mathbf{x}_{rs} and \mathbf{x}_m are on different vertical grids. \mathbf{x}_{rs} is on the GRUAN Processor vertical grid, composed of 278 levels, hereafter referred to as the fine grid (f), subsampled from the original GRUAN profiles (noting that with a ratio radiosonde pressure by Processor pressure less than 0.1%, the subsampling uncertainty is assumed negligible). \mathbf{x}_m is on the model vertical grid, hereafter referred to as the coarse grid (c), as given in input.

Given H , the observation operator, we can express the simulated Tb as follows:

$$\mathbf{y}_{rs} \equiv H(\mathbf{x}_{rs}) \quad (15)$$

$$\mathbf{y}_m \equiv H(\mathbf{W}\mathbf{x}_m) \quad (16)$$

where \mathbf{W} is the interpolation matrix.

Eq.s (15) and (16) can be further expanded as a function of the profiles true value on the fine and coarse grid, hereafter \mathbf{x}_f^t and \mathbf{x}_c^t , respectively, and the errors associated with the radiosonde and the model fields, hereafter $\boldsymbol{\varepsilon}_{rs}$ and $\boldsymbol{\varepsilon}_m$, as follows:

$$\mathbf{y}_{rs} = H(\mathbf{x}_f^t + \boldsymbol{\varepsilon}_{rs}) \quad (17)$$

$$\mathbf{y}_m = H(\mathbf{W}\mathbf{x}_c^t + \mathbf{W}\boldsymbol{\varepsilon}_m) \quad (18)$$

with \mathbf{x}_c^t defined as $\mathbf{x}_c^t \equiv \mathbf{W}^* \mathbf{x}_f^t$ where an expression for \mathbf{W}^* , the pseudo-inverse of \mathbf{W} , is given in Appendix B.

The comparison carried out in this study is in radiance space and the observation operator used to simulate the brightness temperatures is identical for both radiosonde and model fields simulations.

For this reasons, we consider the radiance space as our reference and ignore any errors associated with observation operator, that would cancel out in the difference anyway since mainly systematic. Note that those errors need however to be taken into account if a simulated product is compared to real satellite observations.

Defining the vertical interpolation error ϵ_{int} as:

$$\epsilon_{int} \equiv \mathbf{W}\mathbf{x}_c^t - \mathbf{x}_f^t \quad (19)$$

Eq. (18) can be written as follows:

$$\begin{aligned} \mathbf{y}_m &= H(\mathbf{W}\mathbf{x}_c^t - \mathbf{x}_f^t + \mathbf{W}\epsilon_m + \mathbf{x}_f^t) \\ &= H(\mathbf{W}\epsilon_m + \epsilon_{int} + \mathbf{x}_f^t) \end{aligned} \quad (20)$$

Given \mathbf{H} , the Jacobian matrix provided by RTTOV and containing the partial derivatives of $\partial\mathbf{y}/\partial\mathbf{x}$ (i.e. the change in radiance, $\partial\mathbf{y}$, for a change in the state vector, $\partial\mathbf{x}$), Eq.s (17) and (20) can be approximated, assuming small errors, as follows:

$$\mathbf{y}_{rs} \cong H(\mathbf{x}_f^t) + \mathbf{H}_{\mathbf{x}_f^t} \epsilon_{rs} \quad (21)$$

$$\mathbf{y}_m \cong H(\mathbf{x}_f^t) + \mathbf{H}_{\mathbf{x}_f^t}(\mathbf{W}\epsilon_m + \epsilon_{int}) \quad (22)$$

Therefore, the *NWP – GRUAN* comparison in radiance space is expressed as follows:

$$\begin{aligned} \delta\mathbf{y} &\equiv \mathbf{y}_m - \mathbf{y}_{rs} \\ &\cong \mathbf{H}_{\mathbf{x}_f^t}(\mathbf{W}\epsilon_m + \epsilon_{int} - \epsilon_{rs}) \end{aligned} \quad (23)$$

Assuming a complete uncorrelation between the interpolation error and those of the radiosonde and the model, the covariance of the difference is expressed as follows:

$$\mathbf{S}_{\delta\mathbf{y}} \equiv E\{(\partial\mathbf{y} - E\{\partial\mathbf{y}\})^T(\partial\mathbf{y} - E\{\partial\mathbf{y}\})\} \quad (24)$$

where E is the expectation operator. We can approximate Eq. (24) as:

$$\mathbf{S}_{\delta\mathbf{y}} \cong \mathbf{H}\mathbf{R}_f^{rs}\mathbf{H}^T + \mathbf{H}\mathbf{W}\mathbf{B}_c^m\mathbf{W}^T\mathbf{H}^T + \mathbf{H}\mathbf{S}_f^{int}\mathbf{H}^T \quad (25)$$

where \mathbf{R}_f^{rs} , \mathbf{B}_c^m , and \mathbf{S}_f^{int} are the error covariance matrices of GRUAN measurements (on the fine grid), the forecast (on the coarse grid), and the vertical interpolation (on the fine grid), respectively, as described below.

We first define the GRUAN covariance matrix. GRUAN does not provide a full covariance matrix with the measurements, therefore \mathbf{R}_f^{rs} is built as a diagonal matrix accounting for the different sources of uncertainty such as:

$$\begin{aligned}
\mathbf{H}\mathbf{R}_f^{rs}\mathbf{H}^T &= \mathbf{H}_T\mathbf{R}_T\mathbf{H}_T^T + \mathbf{H}_q\mathbf{R}_q\mathbf{H}_q^T + \mathbf{H}_P\mathbf{R}_P\mathbf{H}_P^T \\
&+ \mathbf{h}_{skinT}u_{skinT}^2\mathbf{h}_{skinT}^T + \mathbf{h}_{T2m}u_{T2m}^2\mathbf{h}_{T2m}^T \\
&+ \mathbf{h}_{q2m}u_{q2m}^2\mathbf{h}_{q2m}^T + \mathbf{h}_{P2m}u_{P2m}^2\mathbf{h}_{P2m}^T
\end{aligned} \tag{26}$$

where \mathbf{R}_T , \mathbf{R}_q , and \mathbf{R}_P are diagonal matrices whose diagonals are the square of GRUAN profiles of total uncertainty for T , q (converted from RH), and P , respectively, on the Processor vertical grid; u_{skinT} , u_{T2m} , u_{q2m} , and u_{P2m} the uncertainties associated with the surface parameters (i.e. skin temperature, 2m temperature, 2m humidity, and 2m pressure) set to 0.3K, 0.3K, 0.04 RH, and 0.1hPa, respectively (Dr. S. Brickmann, DWD, private communication), estimated for the Lindenberg site. \mathbf{H}_T , \mathbf{H}_q , and \mathbf{H}_P are the Jacobians of the temperature, humidity and pressure profiles, respectively, and \mathbf{h}_{skinT} , \mathbf{h}_{T2m} , \mathbf{h}_{q2m} , and \mathbf{h}_{P2m} the Jacobians of the surface parameters.

\mathbf{R}_T , \mathbf{R}_q , and \mathbf{R}_P are diagonal which precludes a proper propagation of the correlation in radiance space. In this suboptimal case, \mathbf{R}_f^{rs} , and by extension, $\mathbf{S}_{\delta y}$, the covariance of the comparison, will not capture the most accurate representation of the uncertainty budget.

Then, we define the forecast error covariance matrix. For the purposes of this study, the forecast covariance matrix from the operational Met Office Observation Processing System, a one-dimensional variational analysis (1D-Var) performed ahead of the main variational process, is used for \mathbf{B}_c^m . Alternatively, the forecast error covariance matrix can be estimated from an ensemble of NWP profiles as described in Appendix A.

Finally, we define vertical interpolation covariance matrix. To estimate \mathbf{S}_f^{int} , the interpolation error must be quantified.

From Eq. (19) we have:

$$\begin{aligned}
\boldsymbol{\varepsilon}_{int} &= \mathbf{W}\mathbf{W}^*\mathbf{x}_f^t - \mathbf{x}_f^t \\
&= (\mathbf{W}\mathbf{W}^* - \mathbf{I})\mathbf{x}_f^t
\end{aligned} \tag{27}$$

where the random vector \mathbf{x}_f^t , representing the true state on the fine grid, is assumed to have mean $E\{\mathbf{x}_f^t\}$, the (unknown) mean model forecast profile on the fine grid, and covariance $E\{(\mathbf{x}_f^t - E\{\mathbf{x}_f^t\})^T(\mathbf{x}_f^t - E\{\mathbf{x}_f^t\})\} \equiv \mathbf{B}_f^m$, the covariance of \mathbf{x}_f^t in model space on the fine grid. It follows that we can express the covariance of the interpolation uncertainty as:

$$\begin{aligned}
\mathbf{S}_f^{int} &\equiv E\{(\boldsymbol{\varepsilon}_{int} - E\{\boldsymbol{\varepsilon}_{int}\})^T(\boldsymbol{\varepsilon}_{int} - E\{\boldsymbol{\varepsilon}_{int}\})\} \\
&= (\mathbf{W}\mathbf{W}^* - \mathbf{I})\mathbf{B}_f^m(\mathbf{W}\mathbf{W}^* - \mathbf{I})^T
\end{aligned} \tag{28}$$

Note that when the model grid coincides with the fine grid we have $\mathbf{W}^* = \mathbf{W}^{-1}$ and $\mathbf{S}_{int} = \mathbf{0}$ as expected. Replacing \mathbf{W}^* by its form expressed in Appendix B we obtain:

$$\mathbf{S}_f^{int} = \mathbf{B}_f^m (\mathbf{I} - \mathbf{W}(\mathbf{W}^T \mathbf{B}_f^{m-1} \mathbf{W})^{-1} \mathbf{W}^T \mathbf{B}_f^{m-1}) \quad (29)$$

Note that in practice (i.e. for numerical calculations) it is more convenient to use the form expressed in Eq. (28) to get \mathbf{S}_f^{int} as a symmetric and positive definite matrix.

This methodology has been applied to the 587 profiles of the night-time dataset described in the previous section. The covariances $\mathbf{S}_{\delta y}$ of each comparison as approximated in Eq. (25) have been averaged (arithmetic mean, hereafter $\overline{\mathbf{S}_{\delta y}}$) and the square root of the diagonal (i.e. the 1σ standard deviation of the comparison total uncertainty distribution) is shown in figure 6. In practice, we calculate $\mathbf{S}_{\delta y}$ as the sum of the covariance matrices of each variable: the surface measurements covariance (\mathbf{S}_{surf_rs}); the model surface covariance (\mathbf{S}_{surf_m}); the total humidity covariance (\mathbf{S}_{q_total}); the total temperature covariance (\mathbf{S}_{T_total}); and the GRUAN pressure covariance (\mathbf{S}_{P_rs}). The square root of their diagonal is also shown in figure 6. In addition, \mathbf{S}_{q_total} and \mathbf{S}_{T_total} can be further decomposed into the sum of the covariance matrices of each of their components: the GRUAN humidity and temperature covariance (\mathbf{S}_{q_rs} and \mathbf{S}_{T_rs}); the model humidity and temperature covariance (\mathbf{S}_{q_m} and \mathbf{S}_{T_m}); and the covariance of the vertical interpolation of the model humidity and temperature profiles ($\mathbf{S}_{q_m_int}$ and $\mathbf{S}_{T_m_int}$). The square root of their diagonal is also shown in figures 7 and 8.

Note that on some occasions, the Processor fine grid does not capture the lowermost or upper most model levels, which caused missing values in \mathbf{W} . The calculation has consequently been done, for those cases, on the remaining levels of \mathbf{W} . It is planned to refine the Processor grid in the future version in order to avoid such missing data in the interpolation matrix.

As expected, the surface components of the total uncertainty are dominant at frequencies where the radiance is sensitive to the surface (ATMS channels 1-7 and 16-17). Amongst them, the surface component from the model is the largest due to the low confidence in surface emission and properties. Channels with frequencies sensitive to temperature and humidity are dominated by the temperature and humidity total components, respectively.

The decomposition of the temperature and humidity total uncertainties in the temperature channels (fig. 7) and in the humidity channels (fig. 8), respectively, shows that, again, the model components are largely dominant. Note that for the highest peaking temperature channel (channel 12) the second largest uncertainty is the GRUAN pressure component. Also, the lowest peaking humidity channels (channels 18-19) are significantly affected by the surface uncertainty, although this may vary with the location and the water vapour burden making those channels peak more or less high in the atmosphere and therefore more or less sensitive to surface.

The total uncertainty ranges from 0.08 to 0.13K for the temperature channels in figure 7, and from 1.6 to 2.5K for the humidity channels in figure 8. Compared to the mean difference $\Delta T_{b_{MetOffice}}$ documented in Table 1, the night-time sampling satisfies the consistency requirement of Eq. (1) with $k=1$, noting that the σ term in Eq. (1) that should represent the uncertainty associated with the tri-linear horizontal interpolation, is currently unknown, although assumed small, and therefore

ignored. Future work will be dedicated to the estimation of this σ term using high resolution regional model.

These preliminary results are in line with the uncertainty range provided by Loew et al. (2017). This should however be confirmed with the careful evaluation of multiple GRUAN sites over longer time periods, beyond the scope of this paper but planned to be addressed in the near future.

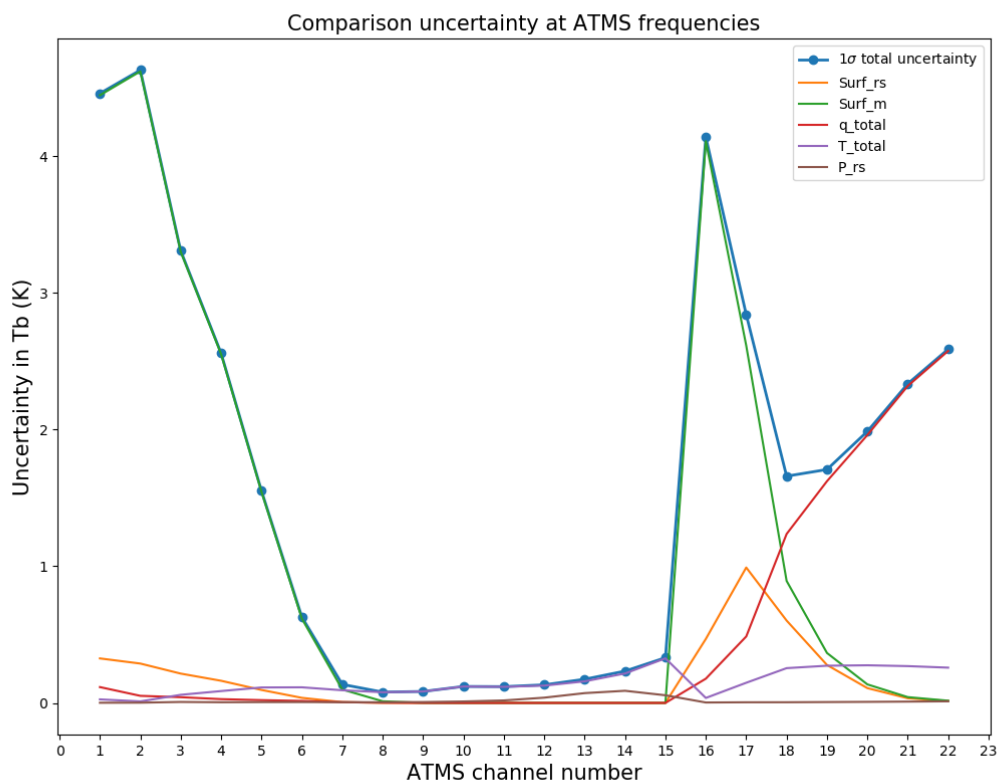
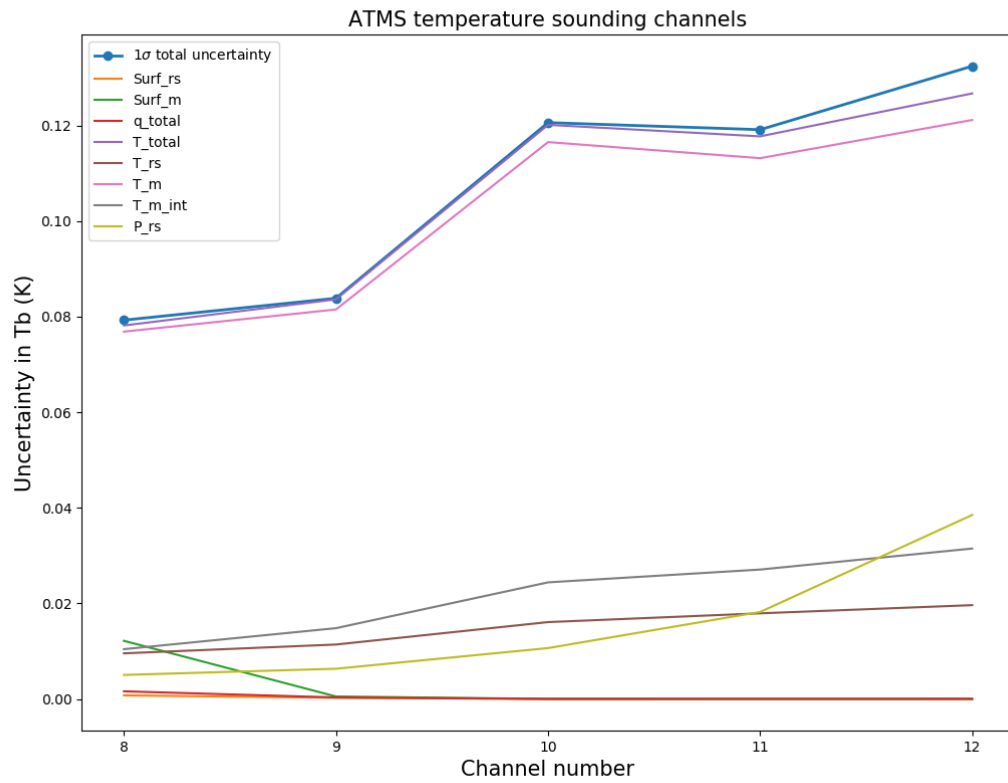


Figure 6: 1σ standard deviation of the total uncertainty distribution expressed as the square root of the diagonal of the mean comparison covariance $\overline{\mathbf{S}}_{\delta y}$ (blue dots), and the square root of the diagonal of the components forming $\overline{\mathbf{S}}_{\delta y}$, namely, the GRUAN surface uncertainty (Surf_rs, orange), the model surface uncertainty (Surf_m, green), the humidity total uncertainty (q_total, red), the temperature total uncertainty (T_total, purple), and the GRUAN pressure uncertainty (P_rs, brown).



729

730 Figure 7: Same as figure 6 but only for ATMS temperature upper tropospheric-lower stratospheric
731 channels 8-12, with in addition the square root of the diagonal of the components forming $\mathbf{S}_{T_{total}}$,
732 namely, the GRUAN temperature uncertainty (T_{rs} , olive), the model temperature uncertainty (T_m ,
733 pink), the model vertical interpolation uncertainty (T_m_int , grey).

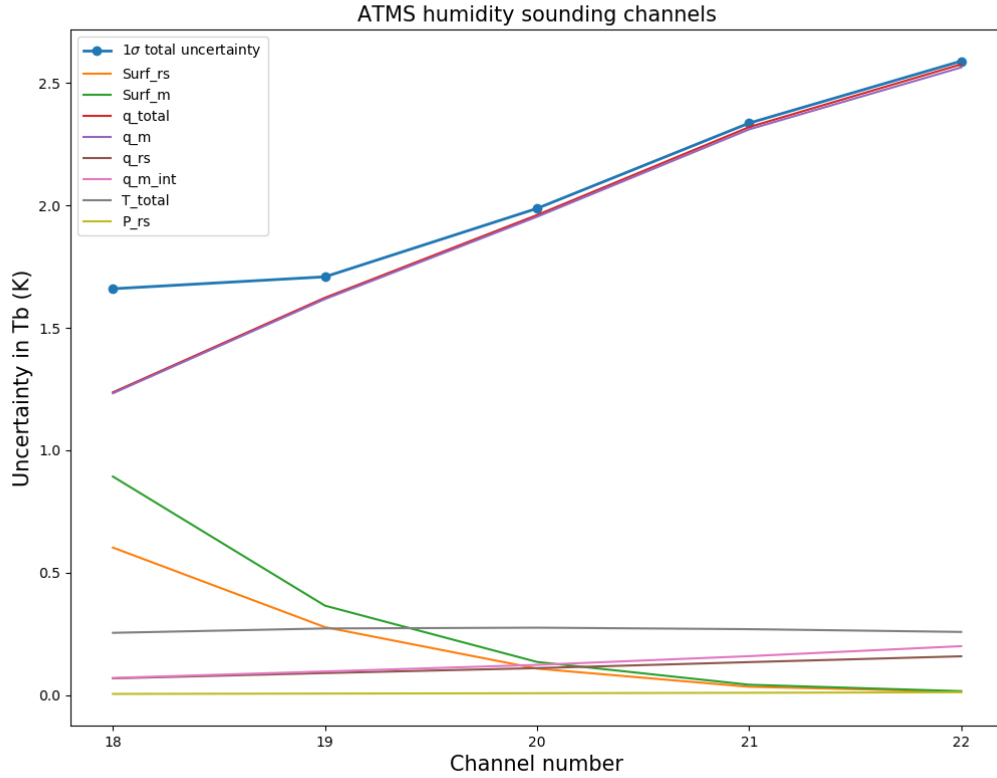


Figure 8: Same as figure 6 but only for ATMS humidity tropospheric channels 18-22, with in addition the square root of the diagonal of the components forming \mathbf{S}_{q_total} , namely, the GRUAN humidity uncertainty (q_rs , olive), the model humidity uncertainty (q_m , pink), the model vertical interpolation uncertainty (q_m_int , grey).

It is interesting to compare the GRUAN processor upper bound uncertainty, calculated assuming a complete correlation, i.e. u_gruan_bt , with the GRUAN contribution to $\overline{\mathbf{S}}_{\delta y}$. Ignoring the uncertainties associated with the surface parameters, the GRUAN contribution to $\overline{\mathbf{S}}_{\delta y}$ can be calculated as the square root of the first three term of Eq. (26). Figure 9 shows that u_gruan_bt is consistently four times larger than the 3σ standard deviation of the GRUAN contribution to $\overline{\mathbf{S}}_{\delta y}$ at the frequencies of interest. It may indicate that the assumption of complete correlation in the uncertainty (i.e. the use of GRUAN total uncertainty as if correlated at all levels), associated with the calculation of the maximal total uncertainty in Tb results in a large overestimation of the uncertainty in radiance space. In addition, it should be remembered that the use of diagonal matrices in Eq. (26) is suboptimal and may not capture the full extent of the uncertainty. The lack of explicit systematic and random errors associated with the radiosonde profiles and the lack of discretisation between correlated and uncorrelated uncertainty components in GRUAN products is also suboptimal. This stresses the need for the GRUAN community to provide proper covariance matrices, better defined error profiles, and better discretisation of correlated and uncorrelated uncertainties. Finally, it is possible, although not likely, that a violation of the assumption of ‘small’ uncertainties in Eq.s (21-

22) could result in non-linear perturbations potentially causing the GRUAN contribution to $\overline{\mathbf{S}_{\delta\mathbf{y}}}$ to be underestimated.

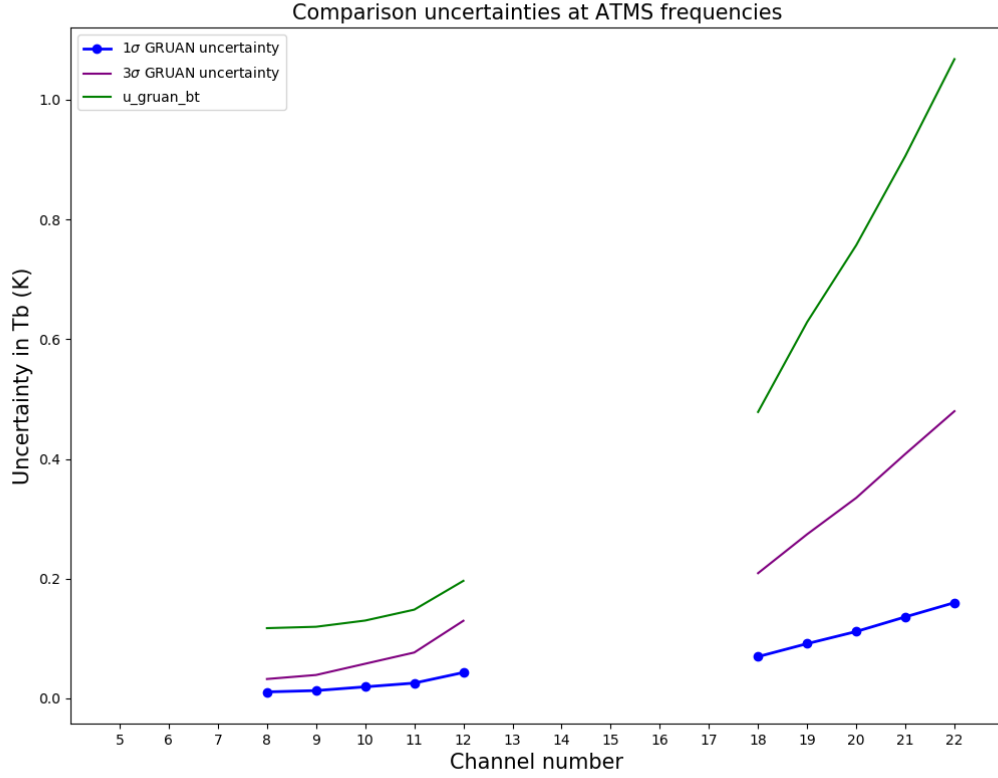


Figure 9: 1σ standard deviation of the uncertainty distribution from GRUAN contribution to $\overline{\mathbf{S}_{\delta\mathbf{y}}}$ is shown in blue (dotted line). It is calculated as the square root of the first three term of Eq. (26), i.e. $\sqrt{\text{diag}(\mathbf{S}_{q_{rs}} + \mathbf{S}_{T_{rs}} + \mathbf{S}_{P_{rs}})}$. The 3σ standard deviation of the uncertainty distribution is shown in purple (solid line). $u_{\text{gruan_bt}}$, the GRUAN uncertainty propagated into radiance space by the GRUAN Processor and averaged over the night-time sample is shown in green (solid line).

Next, the overall agreement between the Met Office model and GRUAN, in radiance space, is assessed via a χ^2 test. Here, a reduced χ^2 , hereafter $\tilde{\chi}^2$, is estimated for each profile as follows:

$$\tilde{\chi}^2 = \frac{1}{c} (\delta\mathbf{y}_i - \overline{\delta\mathbf{y}})^T \mathbf{S}_{\delta\mathbf{y}}^{-1} (\delta\mathbf{y}_i - \overline{\delta\mathbf{y}}) \quad (30)$$

where $\delta\mathbf{y}_i$ is the $NWP - GRUAN$ difference in Tb for the i^{th} comparison, $\overline{\delta\mathbf{y}}$ the mean comparison over the sample. The number of degrees of freedom c , in this context, is the number of channels regardless any constraints as defined in Rodgers, 2000 (section 12.2).

Comparing calculated and theoretical \tilde{X}^2 will allow, in theory, the assessment and eventually revision of the uncertainty estimates used for the NWP model and GRUAN. Figure 10 shows the distribution of \tilde{X}^2 calculated for the night-time sampling (blue line) and how it compares to the theoretical \tilde{X}^2 estimated from random data of similar sampling size (green line). Dashed lines show the 95-percentile of each distribution. \tilde{X}^2 values beyond the theoretical 95-percentile line reflect the comparisons where the model and GRUAN are significantly different. For this example, the 95-percentile of the calculated \tilde{X}^2 (blue dashed line) is 5% larger than the theoretical one (green dashed line): i.e. about 10% of the calculated \tilde{X}^2 are greater than the theoretical 95-percentile threshold. This relatively good match between calculated and theoretical \tilde{X}^2 rules out the hypothesis of the violation of small uncertainties in Eq.s (21-22). However, it might be that one (or more) component of $S_{\delta y}$ have been underestimated and could be revised until both 95-percentiles match. It is also possible that unforeseen sources of uncertainty have been unaccounted for in Eq. (25). In both cases, the increased total uncertainty will reduce the number of comparisons failing the test and reduce the difference between the calculated and theoretical 95-percentile threshold.

A refined assessment using a larger sample spanning several years and several GRUAN sites will be addressed as part of future work, but is out of scope of this study.

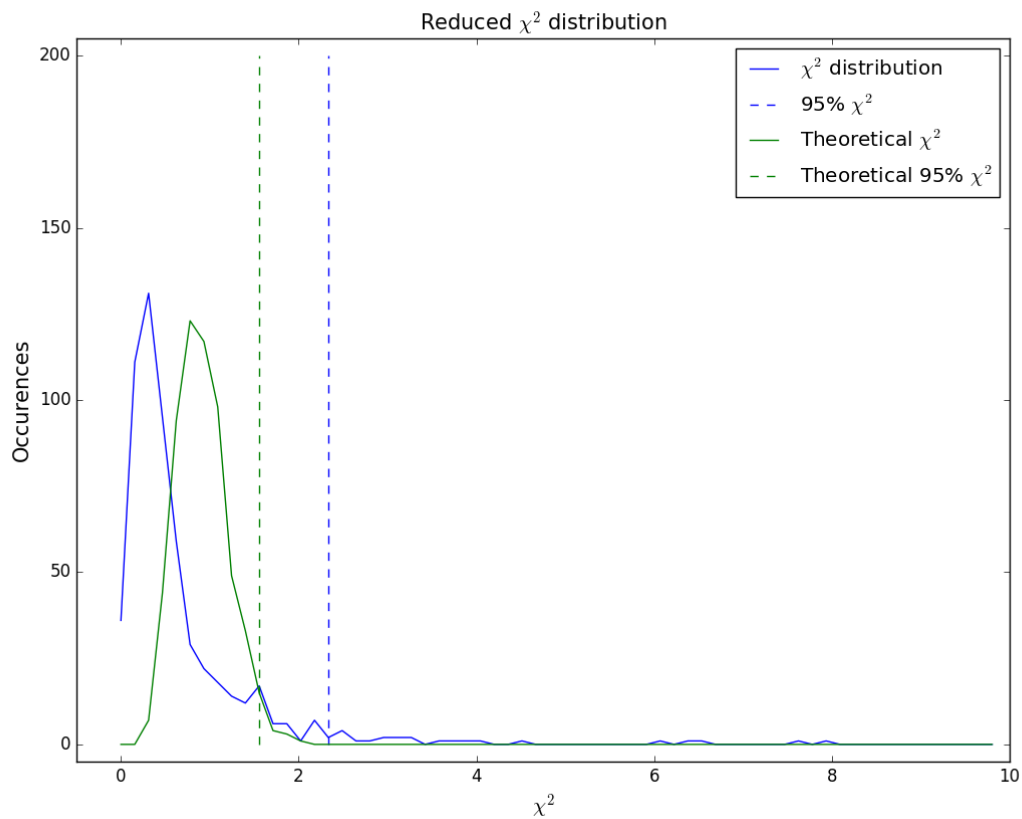


Figure 10: Reduced X^2 distribution from the NWP – GRUAN night-time sampling (blue) and

theoretical reduced X^2 estimated from a random sampling of equal size and equal degrees of freedom (blue). Dashed lines show the 95-percentile of each distribution.

6. Conclusion

Numerical weather prediction models have demonstrated ability to act as suitable reference comparators for the calibration and validation of satellite instruments. Model analysis and short-range forecast uncertainties are incrementally reduced by progressive improvements in data assimilation techniques and the ingestion of a large and growing number of observations from multiple sources. From the state-of-the-art of NWP output fields, biases as small as a tenth of a Kelvin can be highlighted in some satellite datasets. In addition, NWP models provide global fields, which allow for the evaluation of satellite data across the full dynamic range of the instrument. Yet model uncertainty estimates do not meet international metrological traceability standards as provided by other reference datasets, such as the GRUAN radiosondes.

In order to address the missing links in the traceability chain of model uncertainty, a collocation and radiance simulation tool (the GRUAN Processor) has been developed in the framework of the GAIA-CLIM project. This allows us to quantify differences between GRUAN radiosonde profiles of well-defined uncertainties and NWP fields, in both observation and radiance space.

Based on the radiative transfer core capability of the radiance simulator developed and maintained by NWP SAF, the Processor collocates model fields to GRUAN radiosonde profiles in space and time, then simulates top-of-atmosphere brightness temperatures for both datasets at frequencies used by satellite instruments, and propagates GRUAN uncertainties in radiance space. The details of the GRUAN Processor have been described in this paper and a mathematical methodology aimed at assessing *NWP – GRUAN* comparisons in radiance space has been expounded.

For this study, a small sampling of 573 daytime and 587 night-time GRUAN radiosonde profiles from Lindenberg, Germany, in 2016, and matching NWP fields from the Met Office and ECMWF global models have been processed and analysed to demonstrate the GRUAN Processor capability.

In the geophysical space of the radiosonde observations, the *NWP – GRUAN* comparison has highlighted 0.5K cold biases located in the stratosphere of the ECMWF model and in the lower troposphere of the Met Office model. A wet bias ranging from 50 to 75% of the local specific humidity is visible in both models at pressure between 200 and 100hPa.

In radiance space, the Met Office and ECMWF T_b are found to be within $\pm 0.09K$ and $\pm 0.39K$, respectively, to GRUAN night-time profiles (when GRUAN biases are minimal), at frequencies predominantly sensitive to temperature (54-57GHz) in the vertical domain where GRUAN radiosonde observations are available. Similarly, the Met Office and ECMWF T_b are found to be within $\pm 0.46K$ and $\pm 0.37K$, respectively, to GRUAN night-time profiles at frequencies predominantly sensitive to humidity (around 183GHz).

829

830 The propagation of GRUAN uncertainties in radiance space is performed in the GRUAN Processor via
831 perturbation of the temperature, humidity and pressure profiles by plus and minus their total
832 uncertainty as provided in the RS92-GDP data files. This process assumes a complete correlation of
833 the uncertainties at all levels. This is a pessimistic assumption and the resulting uncertainty obtained
834 in radiance space is therefore representative of a maximum uncertainty of the GRUAN component
835 (the model uncertainty is not accounted for). The true GRUAN uncertainty in radiance space is
836 smaller than that calculated as only a fraction of GRUAN total uncertainty (in observation space) is
837 really correlated over the entire profile.

838 Independently from that maximum GRUAN uncertainty estimate, a rigorous estimation of the
839 uncertainties in radiance space associated with the *NWP – GRUAN* difference is proposed in this
840 study as a post-processing application based on the GRUAN Processor outputs. The covariance of
841 this difference, $\mathcal{S}_{\delta y}$, is calculated as the sum of the GRUAN, model, and interpolation uncertainties
842 propagated in radiance space.

843 Tested with the Met Office background error covariance, the NWP component of $\mathcal{S}_{\delta y}$ is found to be
844 the dominant source of uncertainty. The total uncertainty of the difference ranges from 0.08 to
845 0.13K at frequencies sensitive to temperature and from 1.6 to 2.5K at frequencies sensitive to
846 humidity, satisfying, on average, the consistency check (Eq. 1) for night-time profiles.

847 The GRUAN component of $\mathcal{S}_{\delta y}$ is found to be four times smaller (at 3σ) than the maximum GRUAN
848 uncertainty estimated in the Processor, demonstrating the large overestimation of the complete
849 correlation assumption. However, it is worth stressing that in absence of covariance information,
850 error (random and systematic) characterisation, and discretisation between correlated and
851 uncorrelated uncertainty components in GRUAN data files, the estimation of $\mathcal{S}_{\delta y}$ remains
852 suboptimal.

853 The X^2 distribution calculated for the comparisons between model-based (Met Office) and GRUAN-
854 based simulated Tb revealed that the number of significantly different comparisons is close although
855 slightly larger than that of the corresponding theoretical X^2 distribution. Implications are that either
856 one or several components of $\mathcal{S}_{\delta y}$ are underestimated, or that a source of uncertainty has been
857 overlooked.

858

859 The next step will be to process and analyse collocated profiles spanning several years and multiple
860 GRUAN sites. This will provide a better, although incomplete, geographical distribution of model
861 biases as well as their evolution in time. Away from the surface, NWP model biases are to first order
862 a function of latitude and height, and can usefully be studied for polar, mid-latitude and tropical
863 bands. For northern latitude bands, the NWP uncertainties can be studied by comparison with
864 GRUAN observations, but for the tropics and southern latitudes, where there are few or no GRUAN
865 data, these could to be supplemented with other high quality radiosonde reports. The aim will be to
866 provide a refined set of model uncertainty for selected frequencies spanning both microwave and
867 infrared domains. Ultimately, the contribution from this work will help draw the full model
868 uncertainty budget (composed of uncertainties in radiance space, radiative transfer modelling, scale

mismatch, and cloud residual) for more robust assessment of satellite observations. Finally, the larger sampling will also ensure a more robust X^2 analysis and, if deemed necessary, help revise the model covariance matrices used in operation at the Met Office and ECMWF.

The quantitative estimate of errors and uncertainties in NWP models, both temperature, humidity, and radiance space, could aid in the interpretation of observation minus short-range forecast statistics for satellite instruments, for example by helping to identify whether biases in observation-minus-model background values could be due to systematic errors in the NWP model short-range forecasts. In future work, it is planned to use the GRUAN processor output to evaluate biases in observation-minus-model background statistics of satellite data.

GRUAN Processor-based studies also have the potential to refine and improve bias correction schemes used in NWP centres by helping identify regions where NWP model biases are small as suggested by Eyre (2016). Similarly, the processing and inter comparison of multiple radiosonde types can help determine which sets of observations could be use as anchors.

Finally, the GRUAN processor will also evolve with the evolution of RTTOV. For example, a parallel version of the Processor is currently being tested with the fast radiative transfer model RTTOV Ground-based (RTTOV-gb). RTTOV-gb is a modified version of RTTOV that allow for simulations of ground-based upward-looking microwave sensors (De Angelis et al., 2016). Model and GRUAN simulated Tb and propagated uncertainties are expected to help estimate the uncertainties in the microwave radiometer observations for which RTTOV-gb has been developed. It is also planned to upgrade the Processor in order to support RTTOV 12 (Hocking et al., 2017). This upgrade will allow the better handling of surface emissivity and give the option to output principal components (PC) used for the new generation of hyperspectral infrared sounders. Note that other fast radiative transfer models, such as the Community Radiative Transfer Model (CRTM), could potentially be tested with the GRUAN Processor, although there is no immediate plan to do so.

Appendix A: Forecast error covariance matrix estimation

If the forecast error covariance matrix from the NWP forecast model used as input to the Processor is not available, it can be determined from an ensemble of K NWP profiles, with $K > N$ where N is the number of vertical levels, such that:

$$\mathbf{B}_c^m = \frac{\mathbf{X}' \mathbf{X}'^T}{K - 1} \quad (\text{A1})$$

where $K - 1$ gives the best estimate of the covariance of the population from which the sample K is drawn, and with \mathbf{X}' such as:

$$\mathbf{X}' = (x_c^{m_1} - \overline{x_c^m}, \dots, x_c^{m_j} - \overline{x_c^m}, \dots, x_c^{m_K} - \overline{x_c^m}) \quad (\text{A2})$$

where $\mathbf{x}_c^{m_j}$ is the j^{th} model profile of the K ensemble, and $\overline{\mathbf{x}_c^m}$ is the mean of the K profiles, both on the coarse model vertical grid.

Appendix B: Interpolation matrix pseudo inverse

The interpolation matrix \mathbf{W} is not square and therefore its inverse cannot be calculated. Instead, a pseudo inverse, \mathbf{W}^* , can be expressed using, for example, the weighted least square estimate of \mathbf{x}_c^t (Rodgers, 2000). For that, we need to minimize:

$$\mathbf{r} = \frac{1}{2} (\mathbf{x}_f^t - \mathbf{W} \mathbf{x}_c^t)^T \mathbf{B}_f^{m-1} (\mathbf{x}_f^t - \mathbf{W} \mathbf{x}_c^t) \quad (\text{B1})$$

where, for the weight, we use the forecast error covariance matrix expressed on the fine grid, \mathbf{B}_f^m , since we interpolate the model profiles on that grid.

By taking the derivative with respect to \mathbf{x}_c^t and setting it to zero, we find:

$$\mathbf{x}_c^t = (\mathbf{W}^T \mathbf{B}_f^{m-1} \mathbf{W})^{-1} \mathbf{W}^T \mathbf{B}_f^{m-1} \mathbf{x}_f^t \quad (\text{B2})$$

where.

$$\mathbf{W}^* = (\mathbf{W}^T \mathbf{B}_f^{m-1} \mathbf{W})^{-1} \mathbf{W}^T \mathbf{B}_f^{m-1} \quad (\text{B3})$$

In order to find an expression for \mathbf{B}_f^m , we refer to \mathbf{B}_c^m , the forecast covariance matrix on the coarse model grid, to calculate the forecast error correlation matrix \mathbf{C}_c^m , on the coarse model grid. The correlation matrix is then reconditioned on the fine Processor grid, and referred to as \mathbf{C}_f^{rec} , as explained below.

Defining $\mathbf{\Sigma}$, a diagonal matrix representing the square root of \mathbf{B}_c^m variance, such as:

$$\mathbf{\Sigma} = \sqrt{\text{diag}(\mathbf{B}_c^m)} \quad (\text{B4})$$

\mathbf{C}_m can be expressed as:

$$\mathbf{C}_m = \mathbf{\Sigma}^{-1} \mathbf{B}_c^m \mathbf{\Sigma}^{-1} \quad (\text{B5})$$

We can then define \mathbf{C}_f^m as:

$$\mathbf{C}_f^m = \mathbf{W} \mathbf{C}_c^m \mathbf{W}^T \quad (\text{B6})$$

However, Eq. (B6) does not guarantee that \mathbf{C}_f^m diagonal elements are equal to one. This constraint needs to be imposed such as:

$$\mathbf{C}_f^{rec} = \mathbf{W} \mathbf{C}_c^m \mathbf{W}^T - \text{diag}(\mathbf{W} \mathbf{C}_c^m \mathbf{W}^T) + \mathbf{I} \quad (\text{B7})$$

Given σ_m , a vector composed of the square root of the variance of $\mathbf{\epsilon}_m$ variance, \mathbf{B}_f^m is expressed as follows:

$$\mathbf{B}_f^m = \text{diag}(\mathbf{W}\sigma_m)\mathbf{C}_f^{rec}\text{diag}(\mathbf{W}\sigma_m) \quad (\text{B8})$$

924

925 Data availability

926 For further information on the GRUAN Processor source code and/or outputs availability, please
927 contact the lead author (fabien.carminati@metoffice.gov.uk).

928

929 Author contribution

930 FC developed the GRUAN Processor code, analysed the data, and prepared the manuscript with
931 contributions from all co-authors. SM developed the mathematical framework presented in section
932 5. BI and HL provided ECMWF datasets and helped with code design and data analyses. WB and SN
933 helped with code design and data analyses. JH develops and manages RTTOV. AS developed the
934 Radiance Simulator.

935

936 Competing interests

937 The authors declare that they have no conflict of interest.

938

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945

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Tables

Table 1: Mean difference $NWP - GRUAN$ in simulated Tb for ECMWF (ΔTb_{ECMWF}) and Met Office ($\Delta Tb_{MetOffice}$) and 1σ standard deviation for ATMS channels 8-12 and 18-22 at day and night-time.

Channel	Frequency (GHz)	$\Delta Tb_{ECMWF} (1\sigma) (K)$		$\Delta Tb_{MetOffice} (1\sigma) (K)$	
		night	day	night	day
8	54.94	-0.08 (0.09)	-0.16 (0.10)	-0.00 (0.11)	-0.04 (0.12)
9	55.5	-0.15 (0.12)	-0.24 (0.13)	0.04 (0.13)	-0.02 (0.14)
10	57.29	-0.32 (0.18)	-0.45 (0.18)	0.01 (0.16)	-0.07 (0.20)
11	57.29±0.217	-0.39 (0.21)	-0.54 (0.22)	-0.04 (0.20)	-0.16 (0.25)
12	57.29±0.3222±0.048	-0.34 (0.25)	-0.53 (0.27)	-0.09 (0.28)	-0.26 (0.31)
18	183.31±7.0	0.35 (0.91)	0.25 (1.09)	0.02 (0.83)	-0.36 (1.02)
19	183.31±7.0	0.37 (1.13)	0.15 (1.24)	-0.09 (1.03)	-0.48 (1.14)
20	183.31±3.0	0.34 (1.31)	-0.01 (1.36)	-0.18 (1.22)	-0.61 (1.27)
21	183.31±1.8	0.22 (1.48)	-0.29 (1.50)	-0.31 (1.42)	-0.81 (1.45)
22	183.31±1.0	0.04 (1.61)	-0.61 (1.64)	-0.46 (1.57)	-1.01 (1.60)