- 1 Using reference radiosondes to characterise NWP model uncertainty for improved satellite
- 2 calibration and validation.
- 3
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- 10 Abstract
- 11 The characterisation of errors and uncertainties in numerical weather prediction (NWP) model fields
- 12 is a major challenge that is addressed as part of the Horizon 2020 Gap Analysis for Integrated
- 13 Atmospheric ECV CLImate Monitoring (GAIA-CLIM) project. In that regard, observations from the
- 14 GCOS (Global Climate Observing System) Reference Upper-Air Network (GRUAN) radiosondes are
- 15 being used at the Met Office and European Centre for Medium-range Weather Forecasts (ECMWF)
- 16 to assess errors and uncertainties associated with model data.
- 17 The software introduced in this study and referred to as the GRUAN Processor has been developed
- 18 to collocate GRUAN radiosonde profiles and NWP model fields, simulate top-of-atmosphere
- 19 brightness temperature at frequencies used by space-borne instruments, and propagate GRUAN
- 20 uncertainties in that simulation. A mathematical framework used to estimate and assess the
- 21 uncertainty budget of the comparison of simulated brightness temperature is also proposed.
- 22 One year of GRUAN radiosondes and matching NWP fields from the Met Office and ECMWF have
- been processed and analysed for the purposes of demonstration of capability. We present
- 24 preliminary results confirming the presence of known biases in the temperature and humidity
- 25 profiles of both NWP centres. The night-time difference between GRUAN and Met Office (ECMWF)
- 26 simulated brightness temperature at microwave frequencies predominantly sensitive to
- temperature is on average smaller than 0.1K (0.4K). Similarly, this difference is on average smaller
- 28 than 0.5K (0.4K) at microwave frequencies predominantly sensitive to humidity.
- 29 The uncertainty estimated for the Met Office GRUAN difference ranges from 0.08 to 0.13K for
- 30 temperature sensitive frequencies and from 1.6 to 2.5K for humidity sensitive frequencies. From the
- 31 analysed sampling, 90% of the comparisons are found to be in statistical agreement.
- 32 This initial study has the potential to be extended to a larger collection of GRUAN profiles, covering
- 33 multiple sites and years, with the aim of providing a robust estimation of both errors and
- 34 uncertainties of NWP model fields in radiance space for a selection of key microwave and infrared
- 35 frequencies.
- 36

#### 37 1. Introduction

- 38 Space-borne observational datasets are EOS key-components that have led to significant advances in 39 climate and weather applications (Joo et al., 2013; Bauer et al., 2015; Hollmann et al., 2013; Bojinski 40 et al., 2014), and therefore must be subject to high standards of calibration and validation to meet 41 user requirements. As part of an overall strategy for a harmonised and improved instrument 42 calibration, the World Meteorological Organisation (WMO), Coordination Group for Meteorological 43 Satellite (CGMS), and Global Space-based Inter-Calibration System (GSICS) have advocated the need to tie the measurements to absolute references and primary standards (WMO, 2011<sup>1</sup>; GSICS, 2015<sup>2</sup>). 44 45 In most cases however, commonly used validation techniques, as discussed by Zeng et al. (2015) and
- 46 Loew et al. (2017), do not yet provide a full metrological traceability.
- 47 For a full metrological traceability and uncertainty quantification, Green et al (2018) suggested
- 48 mirroring the measurement protocols as described by Immler et al (2010). Accordingly, consistency
- 49 between two independent measurements,  $m_1$  and  $m_2$ , is achieved when:

$$|m_1 - m_2| < k \sqrt{\sigma^2 + u_1^2 + u_2^2} \tag{1}$$

- 50 where  $u_1$  and  $u_2$  are the total uncertainties associated with  $m_1$  and  $m_2$ , respectively.  $\sigma$  represents the
- 51 intrinsic uncertainties of the comparison. In the case of a comparison between radiosonde and
- 52 satellite observations for example, this term can represent the collocation uncertainty (Calbet et al.,
- 2017). *k* is a coverage factor expanding the confidence interval for normally distributed error
  probability.

- 56 For satellite data, pre-launch calibration characteristics are often provided by the instrument
- 57 manufacturer or space agency. However at launch, an uncertainty chain that may have been
- 58 metrologically traceable during the laboratory calibration phase can become compromised due to
- 59 changes in the spacecraft during the launch process itself as well as changes in the satellite
- 60 environment in orbit compared to the laboratory testing. Furthermore, the instruments also degrade
- over time, sometimes in quite a complex manner. These issues coupled with the current lack of true
- on-board traceable references makes creating a metrologically traceable uncertainty chain difficult
- 63 for the satellite data record.
- 64 This aspect is being addressed by the Fidelity and Uncertainty in Climate Data Records from Space
- 65 (FIDUCEO) project (<u>http://www.fiduceo.eu/</u>). The project aims to develop Fundamental Climate Data
- 66 Records (FCDR) by reprocessing existing observations from raw satellite data to geolocated and
- 67 calibrated radiances with traceable uncertainties from a set of different references at the pixel level.
- 68 The uncertainty characterisation will account for the physical basis of the sensing process, the on-
- 69 board calibration system, and an estimate for the uncertainties arising from the processing.

<sup>&</sup>lt;sup>1</sup> <u>https://library.wmo.int/opac/doc\_num.php?explnum\_id=3710</u>

<sup>&</sup>lt;sup>2</sup> <u>http://www.wmo.int/pages/prog/sat/documents/GSICS-RD002\_Vision.pdf</u>

71 The (re)assessment of historical, well-established, and new space-borne instruments using data 72 assimilation systems has become, over the past decade, common practice in numerical weather 73 prediction (NWP) centres (Bell et al., 2008; Zou et al., 2011; Bormann et al., 2013; Lu and Bell, 2014). 74 NWP models offer an interesting framework for the assessment of observational datasets due to a 75 physically constrained, continuous, global, and homogeneous representation of the atmosphere. An 76 optimal estimation of the state of the atmosphere is routinely performed in data assimilation 77 systems by blending information from a large volume of observations (space-borne, air-borne, and 78 ground-based) with a short-range forecast. Diagnostics are calculated in satellite observation space, 79 typically in brightness temperature, thanks to the radiative transfer models used by data assimilation 80 systems (Saunders et al., 2018). This forward approach is better posed than the inverse problem, 81 that is to say comparing model geophysical fields to retrieved satellite profiles, since multiple 82 atmospheric states can provide solutions to the retrieval, introducing further uncertainty. NWP 83 representation of atmospheric temperature and humidity fields is of sufficient quality to enable the 84 characterisation of subtle biases in satellite observations as demonstrated in the work referenced 85 herein. Loew et al. (2017) reported model fields uncertainties in the satellite observation space 86 ranging from 0.05 to 0.2K at frequencies principally sensitive to mid-tropospheric and lower 87 stratospheric temperature, and from 1 to 2K at frequencies sensitive to mid and upper tropospheric 88 humidity. However, those estimations arise from sensitivity studies and not from robust uncertainty 89 analyses. Stochastic approaches, based on ensemble forecasting techniques, have been used to 90 estimate forecast uncertainties, but with the caveat that they do not represent the systematic model 91 biases (Leutbecher et al., 2017).

92 This lack of metrologically traceable characterisation has often hampered the recognition and

93 consideration of model-based assessment outside of the NWP context, especially at space agency

and instrument team levels. Key climate users can also benefit from this approach, which has begun

to find resonance in the climate community (e.g. Massonnet et al., 2016).

96

97 In this paper, we use the terms error and uncertainty as described in the International Vocabulary of 98 Metrology (VIM) (JCGM, 2012<sup>3</sup>). The uncertainty is described in the VIM as a non-negative 99 parameter characterizing the dispersion of the quantity values being attributed to the quantity 100 intended to be measured, based on the information used. It is emphasized that all components of 101 the uncertainty contribute to this dispersion. This includes systematic effects arising from, for 102 example, corrections or reference standards. If a systematic effect is unknown it is unaccounted in 103 the uncertainty budget but contributes to the error. 104 The error is defined as the measured quantity value minus the unknown true value and may be

105 composed of a random and a systematic component.

106

The Gap Analysis for Integrated Atmospheric ECV CLImate Monitoring (GAIA-CLIM) project (Thorne
 et al., 2017) aims to address those challenges by improving the use of in-situ observations to

<sup>3</sup> <u>https://www.bipm.org/en/publications/guides/vim.html</u>

- 109 rigorously characterise a set of atmospheric Essential Climate Variables (ECVs) derived from satellite
- 110 observations as well as the geolocated and calibrated spectral radiances (level 1b) from which these
- 111 quantities are derived (<u>http://www.gaia-clim.eu/</u>). The work presented here is embedded in that
- 112 framework and focuses on developing NWP as a comprehensive reference by establishing
- 113 traceability for the model fields through comparison with traceable comparator data.
- The NWP model error and uncertainty budget can be expressed as a function of four maincontributions:
- a) The error and uncertainty in NWP temperature and humidity fields mapped to observationspace (brightness temperature).
- b) The error and uncertainty in the underlying radiative transfer modelling, including biases
   between fast radiative transfer models commonly used in NWP and reference line-by-line
   models, fundamental spectroscopic uncertainty, and surface emissivity uncertainty.
- c) The error and uncertainty due to scale mismatch. This encompasses the different scale at
   which observation and model are resolved, and the scale of natural variability that is,
   especially for humidity, much smaller than both observation and model scales.
- d) The error and uncertainty due to residual cloud. Clear-sky scenes are generally preferred
   because simulated cloudy radiances are affected by uncertainties in model representation of
   cloud amounts and the absorption and scattering properties of hydrometeors.
- 127 This study aims to address the first contribution. To that end, the Met Office and European Centre
- 128 for Medium-range Weather Forecasts (ECMWF) models are compared to radiosondes from the
- 129 Global Climate Observing System (GCOS) Reference Upper-Air Network (GRUAN) in a stand-alone
- 130 module based on the core radiative transfer modelling capability of the fast radiative transfer model
- 131 RTTOV and the Radiance Simulator (both available on <a href="http://www.nwpsaf.eu/">http://www.nwpsaf.eu/</a>). This software,
- referred to as the GRUAN Processor, enables the collocation of geophysical fields and simulation of
- 133 top-of-atmosphere (TOA) brightness temperatures (Tb) from radiosondes and NWP models, with
- 134 GRUAN uncertainties propagated into the radiative transfer calculation.
- 135
- 136 Section 2 introduces the datasets used for this study, namely GRUAN radiosondes and the NWP
- 137 models from the Met Office and ECMWF. Sections 3 and 4 describes the GRUAN Processor
- 138 functionality and presents an illustrative case study. A methodology statistically assessing the
- 139 uncertainties is presented in section 5. Section 6 concludes the study.
- 140
- 141 2. Datasets
- 142 2.1. GRUAN
- 143 With 17 sites across the world (including two inactive sites in the Pacific), GCOS is building on
- 144 existing infrastructures to develop a reference network for upper-air observations
- 145 (http://www.gruan.org/). GRUAN aims to provide long-term high-quality measurements of ECVs
- 146 with vertically resolved uncertainty estimates. To meet the strict criteria for reference
- 147 measurements, GRUAN data also includes a comprehensive collection of metadata and
- 148 documentation of correction algorithms.

149 To date, only the Vaisala RS92 radiosonde is used to produce the GRUAN certified products (Sommer 150 et al., 2016), referred to as RS92 GRUAN Data Product Version 2 (RS92-GDP), but a new product 151 based on the Vaisala RS41 is in preparation. The RS92 GRUAN processing is documented by Dirksen 152 et al (2014). This includes the correction of the radiosonde systematic errors, due to mainly solar 153 radiation, and the derivation of the uncertainties for temperature, humidity, wind, pressure, and geopotential height. The total uncertainty budget accounts for correlated and uncorrelated 154 155 contributions of both random sources of uncertainty and uncertainties from systematic error 156 corrections, and it is expressed as the root sum square of all contributions. The uncertainty related 157 to the short wave radiation correction (used in the temperature uncertainty budget), the correlated 158 uncertainty related to systematic error corrections, and uncorrelated uncertainty (standard 159 deviation) derived from the GRUAN processing are available in the RS92-GDP files, in addition to the 160 total uncertainty of each variables. However, not all correlated and uncorrelated components are independently available (albeit used in the calculation of the total uncertainty) and some sources of 161 162 partially correlated uncertainty are not yet modelled in GRUAN algorithms (e.g. the pendulum 163 motion of the radiosonde under the balloon). Therefore, only the total uncertainties of temperature,

164 humidity, and pressure are considered in this study.

The results presented in this preliminary study focus on the profiles from Lindenberg (LIN), GRUAN
lead centre, Germany (52.21°N, 14.12°E) for the year 2016.

167

## 168 2.2. Met Office NWP

169 Met Office model data files are extracted from the Managed Archive Storage System (MASS) and 170 only ±5° latitude and longitude around the GRUAN launch site is kept to limit the data volume. For 171 LIN, the model fields cover the area 47.109-57.109°N and 9.0234-19.102°E. Each model data file 172 contains four time steps starting at T+0, the analysis, and three successive 3-hour forecasts referred 173 to as T+3, T+6, and T+9. The Met Office data assimilation system is a hybrid 4-dimensional 174 variational analysis (4D-Var) with 6-hour time window (Lorenc et al., 2000; Rawlins et al., 2007). Four 175 analyses (and their successive forecasts) are available every day at 00:00, 06:00, 12:00, and 18:00 176 Coordinated Universal Time (UTC). Assimilated satellite radiances are corrected with a variational 177 bias correction similar to the scheme described by Auligné et al. (2007). The operational forecast 178 model in 2016 had a resolution of approximately 17km at mid-latitudes for 70 levels from surface to 179 80km (N768L70). The radiative transfer calculation was performed in 2016 by the fast radiative 180 transfer model RTTOV version 9 (Saunders et al., 1999, 2007).

181 In the Met Office NWP system, the interpolation of background fields is performed twice, once for 182 all observations and later just for those observations to be assimilated. The radiosonde profiles are 183 averaged over the vertical model layers. Latitude, longitude, and time at each level are used in the 184 first interpolation of background values, but fixed coordinates are used in the latter interpolation. A 185 bias correction of radiosonde profiles is in place on a per station basis but is generally not applied 186 where RS92 are used. As noted by Ingleby and Edwards (2015), radiation corrections are now often 187 directly applied by the radiosonde manufacturer such as Vaisala, which reduces the need for 188 correction in NWP system. Bias correction and quality controls operationally applied to radiosonde 189 at the Met Office are detailed in the appendix 1 of Ingleby and Edwards (2015).

#### 191 2.3. ECMWF NWP

192 ECMWF data are extracted from the Meteorological Archival and Retrieval System (MARS<sup>4</sup>). Data 193 come from the operational data class atmospheric model long window 4Dvar stream (see MARS 194 documentation for details). The covered area is the same as for the Met Office. Each model data file 195 contains six time steps of three hours starting from T+0 to T+15. The ECMWF analysis/forecast 196 system is documented by ECMWF<sup>5</sup>. A cubic octahedral reduced Gaussian grid is currently used with 197 a resolution of TCo1279 (horizontal grid spacing of about 9 km) and with 137 levels in the vertical. 198 Note that from February 2006 until June 2013, there were 91 vertical levels, and from January 2010 199 until March 2016 a linear reduced Gaussian grid was used with a horizontal spacing of around 16 km. 200 Data assimilation uses incremental 4D-Var (Courtier at al., 1994) with a 12-hour window, the 201 nominal 00:00 UTC analysis uses data from 21:00 UTC to 09:00 UTC. Forecasts and ensembles are 202 run twice daily from early-delivery 6-hour window 4D-Var analyses (Haseler, 2004). Flow-dependent 203 ensemble information from the ECMWF ensemble of data assimilations is incorporated into the 204 modelling of background-error covariances (Bonavita et al., 2016). Satellite radiative transfer 205 calculations use the fast radiative transfer model RTTOV version 11.2 (Hocking et al., 2015) has been 206 used operationally since May 2015 (Lupu and Geer, 2015). Variational bias correction of satellite 207 radiances (and aircraft temperatures) is based on Dee (2004) and Auligné et al (2007).

The treatment of radiosondes in the ECMWF system differs from that of the Met Office in that there
 is no average on model levels and each level is treated as a point value. In addition, the balloon drift
 in space and time was not accounted for in 2016 (i.e. the ascension was assumed instantaneous and
 vertical). The treatment of the radiosonde drift (from BUFR reports) has been introduced in the
 operational system in 2018 (Ingleby et al., 2018). Also in contrast to the Met Office, radiosondes at
 ECMWF are bias corrected for temperature and humidity. The correction, described by Agusti-

Panareda et al (2009), uses monthly statistics of background departure based on night-time RS92.

216

# 217 3. Processor design

The GRUAN Processor, a software based on the NWP Satellite Application Facility (SAF) Radiance Simulator (Smith, 2017), is designed to collocate NWP model fields from the Met Office or ECMWF with radiosondes from the GRUAN network and simulate TOA Tb from those collocated profiles. The simulations are performed at frequencies used by meteorological space-borne instruments and supported by RTTOV. Figure 1 illustrates the Processor top-level design with its main processing steps.

224

225 3.1. Inputs

and is applied as a function of radiosonde type, pressure, and solar elevation angle.

<sup>&</sup>lt;sup>4</sup> <u>https://software.ecmwf.int/wiki/display/UDOC/MARS+user+documentation</u>

<sup>&</sup>lt;sup>5</sup> <u>https://www.ecmwf.int/en/forecasts/documentation-and-support</u>

- 226 The Processor requires as input a GRUAN and a model data file. Supported products are GRUAN
- 227 RS92-GDP, Met Office Unified Model (UM) Fieldfiles (or PP files, see Smith (2017)), and ECMWF GRIB
- files. Both model file types must contain the minimum set of required variables as described by
- 229 Smith (2017) for the Radiance Simulator. Processing options and RTTOV attributes are provided via a
- text file read by the Processor. This file includes the instrument characteristics (e.g. channels) to be
- simulated and output options (output in unit of radiances or Tb for example). Optionally, RTTOV bias
- and root mean square error (rmse) estimated from comparisons between RTTOV and line-by-line
   model calculations, as provided by NWP SAF<sup>6</sup>, can be written to the output files. Finally, an option
- model calculations, as provided by NWP SAF<sup>6</sup>, can be written to the output files. Finally, an option
   allows to opt for a model-radiosonde collocation following the balloon drift (in space and time, see
- section 3.3) or assuming no drift. Note that all collocations presented in this paper account for the
- 236 radiosonde drift.
- 237



239 Figure 1: GRUAN Processor top-level design. Solid arrows show the main processing steps from input

- 240 (blue for NWP model data and green for GRUAN data) to output. Dashed arrows represent the
- 241 internal processing.
- 242

238

# 243 3.2. Conversion

- 244 The conversion step ensures that both model and GRUAN variables (e.g. temperature or humidity)
- are expressed in the same units and that those units are compatible with RTTOV (see section 3.5).
- 246 Two main types of conversion are supported: temperature from potential temperature and specific
- 247 humidity from relative humidity.

- 249 Model data files may sometimes contain potential temperature instead of temperature profiles, as is
- 250 the case for the Met Office. Temperature (*T*) is therefore calculated as a function of potential
- 251 temperature ( $\theta$ ) and pressure (*P*) as follows:

<sup>&</sup>lt;sup>6</sup> <u>https://www.nwpsaf.eu/site/software/rttov/download/coefficients/comparison-with-lbl-simulations/</u>

$$T = \theta \left(\frac{P}{P_0}\right)^{\kappa}$$
(2)

where  $P_0$  is the standard reference pressure equal to 1000hPa and  $\kappa$  the ratio of the gas constant of air to the specific heat capacity at constant pressure.

Similarly, it is worth noting that model data files may not directly contain pressure profiles (e.g. in ECMWF files) or the pressure may be expressed on a different set of levels with respect to other variables (e.g. Met Office files). In both cases however, the pressure on model levels can be

calculated from coefficients provided in the model data files.

259

- 260 The expression of humidity also needs to be harmonised. GRUAN provides profiles of relative
- humidity (*RH*), whereas the humidity from both NWP models is expressed in specific humidity (q), in units kg.kg<sup>-1</sup>. GRUAN *RH* is converted to q as follows:

$$q = \frac{\varepsilon RH e_s}{(P - (1 - \varepsilon) RH e_s)}$$
(3)

263

where  $\varepsilon$  is the ratio of the molecular weight of water vapour to the molecular weight of dry air and e<sub>s</sub> the saturation vapour pressure over liquid. For consistency with GRUAN and Vaisala processing, e<sub>s</sub> is expressed as defined by Hyland and Wexler (1983), such that:

$$\ln(e_s) = \frac{C_1}{T} + C_2 + C_3 T + C_4 T^2 + C_5 T^3 + C_6 \ln(T)$$
(4)

267

268 with:

- 269  $C_1 = -5.8002206 \times 10^3$
- 270  $C_2 = 1.3914993 \times 10^0$
- 271  $C_3 = -4.8640239 \times 10^{-2}$
- 272  $C_4 = 4.1764768 \times 10^{-5}$
- 273  $C_5 = -1.4452093 \times 10^{-8}$
- 274  $C_6 = 6.5459673 \times 10^0$
- 275 for  $e_s$  in Pa and T in K.

276

277 3.3. Interpolations

- 278 The GRUAN Processor generates a set of model profiles (i.e. one profile per variable), on model
- 279 levels, interpolated in space and time along the radiosonde path, which are then vertically
- 280 interpolated on a fixed set of 278 levels as follows.
- 281 First, model fields are linearly interpolated at the radiosonde coordinates (latitude-longitude-time),
- weighted by the distance to the eight closest grid points. Therefore, for an observation at the
- 283 coordinate  $p=[x_p, y_p, z_p]$ , as illustrated on figure 2, in a cube of vertices [(x,y,z), (x+dx,y,z), (x,y+dy,z), (x,y
- 284 (x,y,z+dz), (x+dx,y+dy,z), (x+dx,y,z+dz), (x,y+dy,z+dz), (x+dx,y+dy,z+dz)], where dx and dy represent
- the grid point interval in latitude and longitude, respectively, and *dz* the interval between the time
- 286 T+n and T+(n+13), with associated field values  $F_p$  and  $[F_{000}, F_{100}, F_{010}, F_{001}, F_{110}, F_{101}, F_{111}]$ ,
- 287 respectively,  $F_{\rho}$  is calculated as follows:

$$F_{p} = F_{000}(1 - w_{x})(1 - w_{y})(1 - w_{z}) + F_{100}w_{x}(1 - w_{y})(1 - w_{z}) + F_{010}(1 - w_{x})w_{y}(1 - w_{z}) + F_{001}(1 - w_{x})(1 - w_{y})w_{z} + F_{101}w_{x}(1 - w_{y})w_{z} + F_{011}(1 - w_{x})w_{y}w_{z} + F_{110}w_{x}w_{y}(1 - w_{z}) + F_{111}w_{x}w_{y}w_{z}$$
(5)

289 where  $w_x$ ,  $w_y$ , and  $w_z$  are the weights defined as:

$$w_x = (x_p - x)/dx$$

$$w_y = (y_p - y)/dy$$

$$w_z = (z_p - z)/dz$$
(6)
(7)
(8)

290

- 291 This operation is repeated along the radiosonde path with a time-step of 15 seconds based on the
- radiosonde time profile. A unique model profile (one for each variable) is reconstructed by
- 293 combining the model fields from the pressure levels crossed by the radiosonde between two
- 294 consecutive interpolated model profiles.



Figure 2: illustration of an observation of coordinate  $(x_p, y_p, z_p)$  in a cube that vertices represent the model latitude (*x* axis), longitude (*y* axis), and forecast time (*z* axis).

299

The reconstructed set of profiles is then interpolated on a fixed vertical grid of 278 pressure levels. The fixed grid, referred to as Processor grid (*Pg*), has been designed to have at least one *Pg* level between any two levels of the coarser model (Met Office or ECMWF) grid, referred to as Coarse grid (*Cg*). Therefore, for *Pg* of dimension *n* equal to 278 and *Cg* of dimension *m* (equal to 70 for the Met Office, 91 or 137 for ECMWF), the interpolation is calculated by weighting the fields with respect to the pressure via the interpolation matrix *W* of dimension *n x m*, such as:

$$Pg = W Cg \tag{9}$$

306



$$Pg_j = W_{j1} Cg_1 + W_{j2} Cg_2 + \dots + W_{jm} Cg_m$$
(10)

$$W_{ji} = \frac{P_{i+1} - P_j}{P_{i+1} - P_i} \tag{11}$$

$$W_{ii+1} = 1 - W_{ii} \tag{12}$$

 $W_{jk} = 0 \text{ where } k \neq i, i+1 \tag{13}$ 

- 309 The vertical interpolation of model profiles as well as the subsampling of the radiosonde profiles
- 310 (see section 3.4) to the Processor grid aims to provide a homogenised number of vertical levels on
- 311 which the radiative transfer equation is calculated. Although the coarse model grid and the fine
- radiosonde grid could be directly used as input in RTTOV, it was observed that the lack of
- homogenisation between model and radiosonde profiles causes a bias in radiance space. It was
- therefore decided to interpolate the model profiles and provide a way to estimate the uncertainty
- associated to this interpolation (see section 5).
- 316 Figure 3 illustrates the change from a collocated Met Office temperature profile (LIN 31 December
- 2016, 16:00 UTC) on model levels (70 levels) (a) to a collocated Met Office profile interpolated on
- 318 the Processor grid (278 levels) (b).



319

Figure 3: (a) GRUAN temperature profile (red line) from Lindenberg on 31 December 2016, 16:00 UTC as provided in the RS92-GDP data file with full GRUAN vertical resolution and collocated Met Office temperature profile (blue dotted line) on the model vertical levels. (b) GRUAN temperature profile subsampled at the Processor 278 pressure levels and merged with the Met Office profile

above 9.8 hPa (red line) and collocated Met Office temperature profile interpolated on the Processorvertical levels (blue dotted line).

326

#### 327 3.4. Merging and subsampling

A caveat of processing radiosonde profiles in RTTOV is the lack of information between the top of a profile (bursting point of the balloon) and the TOA. This is addressed by merging the radiosonde profiles with the model profiles above the last available point of the radiosonde. Note that this step occurs after the interpolation of the model profiles so that the upper merged part of the radiosonde and model profiles are strictly identical.

- Similarly, RTTOV requires surfaces information: 2m temperature and humidity, surface pressure and altitude, 10m wind (u and v components, used for microwave simulations over ocean), and skin temperature. While GRUAN provides the surface pressure, temperature, relative humidity, and altitude at launch site in all the data files, the skin temperature ( $T^{G}_{skin}$ ) has to be derived from the difference between the model skin ( $T^{M}_{skin}$ ) and the 2m temperature ( $T^{M}_{2m}$ ) applied to the GRUAN surface temperature ( $T^{G}_{2m}$ ) such as:
- 339

$$T_{skin}^{G} = T_{2m}^{G} + (T_{skin}^{M} - T_{2m}^{M})$$
(14)

Although the 10m wind could be provided by the Vaisala wind profiles (available in GRUAN data
files) or calculated from GRUAN profiles of wind speed and direction, the chaotic rotation of the
radiosonde just after launch results in unreliable wind information near the surface. Therefore, the
model 10m wind (u and v components) is also merged with the GRUAN data. Note that 10m wind is
used to calculate the sea surface emissivity (for microwave simulations) and therefore only concerns
GRUAN sites on small island sites (i.e. La Reunion, Nauru, Manau, Ny-Ålesund, Graciosa, and
Tenerife).

347

348 In the raw RS92 data and GRUAN data, the samplings are provided every second but filtering reduces 349 the effective resolution of temperature to approximately 10s at low levels; the effective resolution 350 of humidity is similar but it is reduced to 40-50s at upper levels (Dirksen et al., 2014). As a result, 351 GRUAN profiles count several thousand levels in the vertical that need to be reduced to the number 352 of levels on the Processor grid. This is achieved with a subsampling of the radiosonde profiles to the 353 nearest levels for each of the 278 Processor pressure levels, at levels where data are available, with 354 the imposed constraint that the ratio radiosonde pressure by Processor pressure must be less than 355 0.1%.

The subsampling of GRUAN profiles has been preferred over layer-averaging or convolution techniques for several reasons. First, we aimed to avoid all unnecessary modification of the GRUAN profiles, used as reference in this study. Second, GRUAN uncertainties are vertically resolved and their processing would have resulted in an information loss. Third, the aim of the Processor is to

360 evaluate uncertainties in radiance space. During the testing phase, we observed that neither the

- 361 choice of averaged layers nor sub-sampled levels significantly affects the calculation of radiative362 transfer and the resulting brightness temperatures.
- Fig. 3 shows a the changes from a GRUAN temperature profile (LIN 31 December 2016, 16:00 UTC) as provided in the RS92-GDP data file (5821 levels, from the surface to 9.88 hPa) (a) to a Processor
- 365 merged and subsampled profile (278 levels, from the surface to 0.008 hPa) (b).
- 366

#### 367 3.5. RTTOV and uncertainties

The radiosonde and model profiles, both on the Processor vertical grid, and their respective surface parameters are passed to RTTOV for the calculation of the TOA Tb. RTTOV version 11.3, currently used by the GRUAN Processor, is documented by Hocking et al. (2015).

371 The surface emissivity depends on the surface type. For land and sea ice, the Processor uses a fixed 372 value, 0.95 and 0.92, respectively. Those estimates are potentially far from the truth, but any bias 373 introduced by fixed emissivity terms is expected to cancel out when the difference in simulated Tb is 374 calculated. Note that RTTOV allows the use of the emissivity atlases over land and sea ice, but this 375 option has not yet been investigated. Over sea, the surface emissivity is calculated by the RTTOV 376 FAST Emissivity Model (FASTEM) version 5 (Kazumori and English, 2015). Although the version 5 is 377 the default version, this can be changed in the input attribute file. It is worth noting here that 378 although the radiosonde may drift from above land to above sea (ice) (or the opposite), the surface 379 type can only be of one kind. The land surface type is typically used as most radiosonde launch sites 380 are well inside land masses. However, for the small island sites of La Reunion, Nauru, Manau, Ny-381 Ålesund, Graciosa, and Tenerife, the radiosonde is expected to rapidly drift over sea and therefore 382 the sea surface type is used instead. The difference between sea and sea ice is controlled by the sea-383 ice mask used by the NWP model.

The viewing angle is set by default to nadir (0°) for all simulations. However, different angles could potentially be used for the purpose of better comparisons with real satellite data, for example.

- 386 All simulations assume clear sky scenes and uses RTTOV direct mode (ignoring the scattering) with 387 the cloud liquid water option off (data not available from GRUAN data file). It is acknowledged that 388 this may introduce discrepancies in the comparison between model and radiosonde in situations 389 where the radiosonde encounters one or several cloud layers. The brightness temperatures 390 calculated from the radiosonde data perturbed by the presence of clouds (e.g. peaks in the humidity 391 profile and to a lesser extent in the temperature profile) will differ from those calculated from the 392 model data that assume clear sky conditions. Because the RS92-GDP does not provide a cloud flag, 393 indirect screening may be required for fine comparisons. To that end, one can use the precipitable 394 water column from the RS92-GDP metadata as a proxy for cloud and or assume the presence of
- 395 cloud when the relative humidity exceeds a threshold value.
- 396 Finally, note that RTTOV interpolation mode (used to interpolate the input levels to the coefficient
- 397 levels for the calculation of the atmospheric optical depth, and then back from the coefficient levels
- to the input levels for the calculation of the radiative transfer equation) uses the log-linear on
- weighting function mode as described by Hocking et al. (2015). This is aimed to avoid a known issue
- 400 causing the oscillation of the temperature Jacobians.

402 It was observed that the interpolation of the model fields at the GRUAN launch site coordinates 403 results in large discrepancies, especially affecting surface parameters (surface pressure and 404 elevation) and the lower part of the profiles, when the local orography presents large variations at 405 scales of the same order as the model grid resolution. The interpolation, using the weighted average 406 of the four neighbouring grid points at a given forecast time may result in the model surface being 407 below or above the actual GRUAN launch site surface. A typical example is the site at La Réunion 408 where the radiosondes are launched from the Maïdo observatory at an altitude of 2200m, compared 409 to which the interpolation of the ECMWF model gives an altitude of 980m and the interpolation of 410 the Met Office model 0m. In Lindenberg by comparison, the radiosondes are launched from the 411 altitude of 103m while both models estimates the altitude to be 57m. To estimate the associated 412 error, a set of dummy model profiles are generated with the surface pressure forced to that 413 provided in the GRUAN metadata. If the model has a surface below that of the observations, the 414 model profiles are linearly interpolated and cut at the observed surface pressure, and the surface 415 parameters become those of the lowest level. If the model has a surface above that of the 416 observations, the model profiles are linearly extrapolated to the observed surface pressure, and the 417 model surface parameters become those of the new lowest level. The difference between the Tb 418 calculated from those modified profiles and the Tb calculated from the original profiles provides an 419 estimation of the associated error. This is referred to as u\_surf\_bt in the Processor output.

420

421 Finally, the GRUAN uncertainties are propagated into radiance space. As described by Calbet et al. 422 (2017), this can be achieved by multiplying the GRUAN profiles of uncertainty by the Jacobians 423 derived by RTTOV from the GRUAN atmospheric profiles, or by applying the radiative transfer to the 424 input atmospheric GRUAN profiles perturbed with their associated uncertainties. The GRUAN 425 Processor is designed to follow the second method although the first one will be further discussed in 426 section 5. In the Processor, two sets of perturbed profiles are created, one containing the GRUAN 427 profiles of temperature, pressure, and humidity, incremented by their respective total uncertainty 428  $(T+u\_temp, P+u\_press, and q+u\_q)$ , and one containing the GRUAN profiles decremented by their 429 total uncertainty ( $T-u\_temp$ ,  $P-u\_press$ , and  $q-u\_q$ ). The resulting brightness temperatures 430 calculated by RTTOV based on those two sets of perturbed profiles, referred to as Tb<sup>+</sup> and Tb<sup>-</sup>, 431 respectively, are compared to Tb, calculated with the unperturbed profiles, to estimate the 432 associated uncertainty in radiance space. The greatest difference between  $|Tb - Tb^+|$  and  $|Tb - Tb^-|$ 433 is given in output as u\_gruan\_bt. Note that the eight combinations of sign that this approach can 434 allow have been tried during the test phase. The resulting uncertainty was not found significantly 435 different from that obtained with Tb<sup>+</sup> and Tb<sup>-</sup>, but the processing time significantly increased. Tb<sup>+</sup> 436 and Tb<sup>-</sup> were therefore retained as the best compromise. 437 It should be noted that the simplified nature of this approach, which applies a perturbation of 438 constant sign in the vertical, ignores the complicated fluctuations that the propagation of 439 uncertainty via a multiplication by the Jacobians would induce (see section 5). Here, we assume that 440 the GRUAN profiles of uncertainty used to perturb the atmospheric profiles are fully correlated at all

442 square of correlated and uncorrelated components (Dirksen et al., 2014). Nevertheless, assuming a

fully correlated perturbation enables the estimation of the total GRUAN uncertainty upper bound in
 radiance space allowed by this approach. The lower bound, not addressed in the GRUAN Processor,
 can be obtained by assuming the uncertainty profiles completely uncorrelated, and lies close to zero
 as demonstrated by Calbet et al. (2017). Note that all eight possible combinations of sign have been
 tried during the test phase. The resulting uncertainty was not found significantly different from that
 obtained with *Tb*<sup>+</sup> or *Tb*<sup>-</sup>, but the processing time significantly increase. *Tb*<sup>+</sup> and *Tb*<sup>-</sup> were therefore

449 retained as the best compromise.

450 This approach assumes that the GRUAN profiles of uncertainty used to perturb the atmospheric

profiles are fully correlated at all levels. This assumption differs from the truth in that GRUAN total
 uncertainty consist of a root sum square of correlated and uncorrelated components (Dirksen et al.,
 2014). Nevertheless, assuming a fully correlated perturbation allows the estimation of the total
 GRUAN uncertainty upper bound in radiance space. The lower bound, not addressed in the GRUAN
 Processor, can be obtained by assuming the uncertainty profiles completely uncorrelated, and lies

456 close to zero as demonstrated by Calbet et al. (2017).

457 Ideally, the correlated and uncorrelated components of GRUAN uncertainty should be treated

458 separately with, for example, the Monte Carlo method described in the Guide to the expression of

459 Uncertainty in Measurement (GUM) (JCGM, 2008<sup>7</sup>). However, those components are not all

independently available and it is currently not possible to differentiate them in the RS92-GDP. Notethat the radiosonde (random and/or systematic) errors are not provided. Instead, GRUAN algorithm

- 462 corrects the systematic errors in the radiosonde measurements, acknowledging that the correction
- is not perfect and introduces an associated residual uncertainty (accounted for in the totaluncertainty).
- For completeness, perturbations to the surface parameters could be added to the total uncertainty
  budget in radiance space, but GRUAN does not provide uncertainties associated with these
  measurements. An alternative is discussed in section 5.

468

# 469 3.6. Outputs

470 For each pair of collocated radiosonde and NWP model fields, the GRUAN Processor generates two

471 outputs files in netcdf format. The first file contains the model-related fields including, but not

472 limited to, the profiles of temperature, humidity, and pressure on the Processor vertical grid, the

473 interpolation matrix W, the simulated brightness temperature, the temperature, humidity, and

- 474 pressure Jacobians, and a quality control flag (qcflags). Note that for successful simulations, qcflags is
- 475 equal to zero. The second file contains the GRUAN-related fields, including e.g. GRUAN atmospheric

476 profiles and associated uncertainties on the Processor vertical grid, the Jacobians, and the Tb and Tb

477 uncertainties estimated from the perturbed GRUAN profiles (u\_gruan\_bt).

Both files also contain metadata documenting the GRUAN Processor version number (here 6.2); the
NWP model, model validity time, and model version number; the simulated satellite name, platform,

<sup>&</sup>lt;sup>7</sup> <u>https://www.bipm.org/en/publications/guides/gum.html</u>

- 480 and channel; the RTTOV version, RTTOV coefficients creation date, and bias and root mean square
- 481 error (when available); and the metadata available from the original RS92-GDP.

483 Note that some GRUAN Processor simulated brightness temperatures have been ingested into the
 484 GAIA-CLIM Virtual Observatory (<u>http://gaia-clim.vo.eumetsat.int/</u>) for the purposes of visualisation,

- 485 manipulation, and extraction of collocated GRUAN-NWP-Satellite data.
- 486

## 487 4. Data analysis illustration

For illustration purposes, one year of collocated profiles and simulated Tb is presented. The dataset
corresponds to 1160 radiosondes launched from Lindenberg, Germany, in 2016, compared to the
Met Office and ECMWF models. Tb values have been simulated at the Advanced Technology
Microwave Sounder (ATMS) 22 channel frequencies, a microwave radiometer with sounding
capability in the oxygen band (53-57GHz), sensitive to tropospheric and lower stratospheric
temperature, and in the water vapour band (around 183GHz), sensitive to mid-to-upper
tropospheric humidity (Bormann et al., 2013).

The dataset is divided into two samples composed of day and night-time profiles, respectively. This is aimed at discriminating the GRUAN profiles affected by solar radiation, the dominant source of uncertainty according to Dirksen et al. (2014). All profiles with a solar zenith angle (calculated as a function of latitude, longitude, and UTC) smaller (greater) than 90° at launch time is considered as day (night) time. Note that for a refined analysis, the whole profile (not just launch time) should be checked and only profiles with the sun below (or above) the horizon throughout should be used. Note that no cloud screening is applied in this study.

- 502 After screening, 573 pairs of GRUAN Processor outputs are available in daytime and 587 in night-
- 503 time for each model. The mean difference *NWP GRUAN* in temperature, humidity, and simulated
- 504 Tb is shown in figures 4 (daytime) and 5 (night-time) together with the number of available
- 505 comparisons as a function of the pressure. Note that at pressures less than 10hPa, the data sampling
- 506 decreases rapidly as less balloons reach those levels. An arithmetic mean is used to average the 507 uncertainty over the sampling according to Immler et al. (2010) Eq. (4). For temperature and
- 508 humidity, the GRUAN total uncertainty as provided in the RS92-GDP is used (the relative humidity
- 509 uncertainty is converted into specific humidity uncertainty in the GRUAN Processor), while the
- 510 uncertainty in Tb shows the GRUAN uncertainties propagated in radiance space via the perturbation
- of the atmospheric profiles. Note that the model uncertainty and the uncertainty associated with
- 512 the vertical interpolation are ignored in this section, but addressed in section 5.
- 513 It is important to note that both Met Office and ECMWF are operationally assimilating the
- radiosonde profiles from the GCOS Upper Air Network (GUAN), which, in Lindenberg, are the same
- as the GRUAN profiles but without the specific GRUAN processing (and without uncertainty
- 516 characterisation). Therefore, unlike the forecasts, the model analyses (T+0) are not completely
- 517 independent from the observations. However, this is not expected to affect significantly the mean
- 518 comparison as only about 5% of the profiles fall in the first time window (i.e. interpolation between
- 519 T+0 and T+3).

- 521 In Fig.s 4 and 5, the main feature for ECMWF is a 0.5K cold bias in the stratosphere (100-10hPa),
- 522 observed both day and night. This bias has also been detected by Shepherd et al. (2018) in the ERA5
- 523 reanalysis that are based on IFS cycle 41r2, the operational model in 2016. It is attributed to an
- 524 <u>excess of moisture transported into the lower stratosphere, which lead to a cold bias by radiative</u>
- 525 <u>cooling. In Fig.s 4 and 5, the main feature for ECMWF is a 0.5K cold bias in the stratosphere (100-</u>
- 526 10hPa), observed both day and night. The model also presents a 50-75% wet bias peaking between
- 527 200 and 100hPa, slightly more pronounced during the day. This is consistent with the results from
- 528 Ingleby (2017) who showed a similar behaviour for several kinds of radiosonde.
- 529 The Met Office model presents a persistent 0.2 to 0.5K cold bias at pressure greater than 300hPa 530 and a 0.25K warm bias between 200 and 100hPa seen at night-time only. This is consistent with 531 Ingleby and Edwards (2015) who showed similar features in the comparison between radiosondes 532 and the Met Office regional model covering the United Kingdom. The Met Office tropospheric 533 humidity fits generally the radiosonde profiles well but presents a 50-60% wet bias with a peculiar 534 double peak at 200 and 100hPa. A wet bias peaking at 300hPa was already observed by Ingleby et al.
- 535 (2013), the coarser vertical resolution used by the authors potentially explaining the different
- 536 pressure level at which the bias is observed. However, the second maximum (at 100hPa) seems to
- be a new feature that appears in 2015 and persists in 2017 (not shown). This remains unexplained to
- 538 date.
- 539 In radiance space, it is important to distinguish between frequencies representative of the difference
- 540 *NWP GRUAN* and those significantly affected by the surface and the mid to upper stratosphere
- 541 where the GRUAN profiles are merged with the model. Hence, ATMS frequencies sensitive to the
- 542 surface (23.8-54.4 and 88.2-165.5GHz, channel 1-7 and 16-17, respectively) and to the upper
- 543 stratosphere (57.29±0.3222±0.022-57.29±0.3222±0.0045GHz, channel 13-15, respectively) should be
- 544 considered with caution and not used for scientific applications. On the contrary, frequencies
- sensitive to the upper tropospheric-lower stratospheric temperature (peaking between 300 and
- 546 20hPa) and to the mid tropospheric humidity (peaking between 650 and 350hPa) cover the same
- 547 vertical domain as the information provided by GRUAN. For those frequencies, ATMS channel
- 548 characteristics and mean Tb difference are provided in Table 1.
- 549
- Table 1: Mean difference NWP GRUAN in simulated Tb for ECMWF ( $\Delta Tb_{ECMWF}$ ) and Met Office
- 551 ( $\Delta Tb_{MetOffice}$ ) and 1 $\sigma$  standard deviation for ATMS channels 8-12 and 18-22 at day and night-time.

Channel	Frequency (GHz)	ΔTb <sub>ECMWF</sub> (1σ) (K)		ΔTb <sub>MetOffice</sub> (1σ) (K)	
		night	day	night	day
8	54.94	-0.08 (0.09)	-0.16 (0.10)	-0.00 (0.11)	-0.04 (0.12)
9	55.5	-0.15 (0.12)	-0.24 (0.13)	0.04 (0.13)	-0.02 (0.14)
10	57.29	-0.32 (0.18)	-0.45 (0.18)	0.01 (0.16)	-0.07 (0.20)
11	57.29±0.217	-0.39 (0.21)	-0.54 (0.22)	-0.04 (0.20)	-0.16 (0.25)
12	57.29±0.3222±0.048	-0.34 (0.25)	-0.53 (0.27)	-0.09 (0.28)	-0.26 (0.31)

18	183.31±7.0	0.35 (0.91)	0.25 (1.09)	0.02 (0.83)	-0.36 (1.02)
19	183.31±7.0	0.37 (1.13)	0.15 (1.24)	-0.09 (1.03)	-0.48 (1.14)
20	183.31±3.0	0.34 (1.31)	-0.01 (1.36)	-0.18 (1.22)	-0.61 (1.27)
21	183.31±1.8	0.22 (1.48)	-0.29 (1.50)	-0.31 (1.42)	-0.81 (1.45)
22	183.31±1.0	0.04 (1.61)	-0.61 (1.64)	-0.46 (1.57)	-1.01 (1.60)

553 At frequencies sensitive to temperature (54-57Ghz, channels 8-12), hereafter referred to as

temperature channels, the mean difference for ECMWF varies from -0.08 to -0.39K at night, mostly

outside GRUAN uncertainty (red shading, Fig. 5), reflecting the cold bias observed in the

stratosphere. Note that a difference greater than GRUAN uncertainty does not mean a statistical

disagreement since the uncertainty related to the model is unaccounted for (i.e. the total

uncertainty of the comparison as expressed in Eq. (1) is larger than the GRUAN uncertainty alone).

559 The difference is slightly larger in daytime (-0.16 to -0.54K). Similarly, the difference at frequencies

sensitive to humidity (around 183GHz, channels 18-22), hereafter referred to as humidity channels,

varies from 0.04 to 0.37K at night (-0.01 to -0.61K during the day), within GRUAN uncertainty.

562 The mean difference in Tb for the Met Office is always found within GRUAN uncertainty and varies

563 from -0.09 to 0.04K during the night (-0.02 to -0.26K in daytime) for the temperature channels and

from -0.46 to 0.02K during the night (-0.36 to -1.01K in daytime) for the humidity channels.

565 The standard deviation of the differences is similar for both centres and does not vary much from 566 day to night.



568

Figure 4: Mean difference ECMWF – GRUAN (blue) and Met Office – GRUAN (green) calculated from
 573 daytime collocation from Lindenberg in 2016. The temperature difference (top left) is expressed
 in K, the humidity difference is expressed in g.kg<sup>-1</sup> (middle left) and in percentage (NWP – GRUAN

572 / GRUAN ) (middle right), and <u>the difference in simulated brightness temperatures for the 22 ATMS</u>

573 <u>channels is expressed in K (bottom)</u> the difference in simulated brightness temperatures for ATMS

574 channels is expressed in K (bottom) with the 1σ standard deviation (vertical bars). The red shading

shows GRUAN uncertainty. The number of observations is shown as a function of the pressure (top

576 right).





579

#### 580 5. Comparison assessment

581 The previous section gives insights into the GRUAN uncertainty propagated in radiance space by the 582 GRUAN Processor. The approach offers a rapid but incomplete evaluation of the *NWP* – *GRUAN* 583 comparison, but several aspects are overlooked in the final budget, that for various reasons are not 584 part of the internal Processor processing. This includes: a) the uncertainty associated with surface parameters, not provided in RS92-GDP and likely to change from station to station, b) the NWP
model uncertainty, often expressed as a covariance matrix and used in the data assimilation process
by the NWP centres, but not available in the input data files, and c) the uncertainty associated with
the vertical interpolation operated by the Processor for which estimation requires information on
the last two points.

590 In this section, a mathematical framework is elaborated to estimate a robust uncertainty budget for 591 the comparison between NWP fields and GRUAN observations, in radiance space, and statistically 592 assess this comparison. This includes uncertainties in the GRUAN observations, in the vertical 593 interpolation of the GRUAN Processor, and in the model fields. Note that, as previously mentioned, any comparison to satellite radiances should also include other sources of uncertainty such as in the 594 595 underlying radiative transfer models and cloud detection. For this study, we focus on the 596 comparison to the Met Office model fields, but the same method could be applied to the 597 comparison with ECMWF fields.

598

599 We define  $x_{rs}$  as the radiosonde profiles and  $x_m$  as the model profiles (temperature, humidity, and 600 pressure, with a pressure coordinate). Note that  $x_{rs}$  and  $x_m$  are on different vertical grids.  $x_{rs}$  is on 601 the GRUAN Processor vertical grid, composed of 278 levels, hereafter referred to as the fine grid (f), 602 subsampled from the original GRUAN profiles (noting that with a ratio radiosonde pressure by 603 Processor pressure less than 0.1%, the subsampling uncertainty is assumed negligible).  $x_m$  is on the 604 model vertical grid, hereafter referred to as the coarse grid (c), as given in input.

605 Given *H*, the observation operator, we can express the simulated Tb as follows:

$$\mathbf{y}_{rs} \equiv H(\mathbf{x}_{rs}) \tag{15}$$

$$\mathbf{y}_m \equiv H(\mathbf{W}\mathbf{x}_m) \tag{16}$$

606 where **W** is the interpolation matrix.

607 Eq.s (15) and (16) can be further expanded as a function of the profiles true value on the fine and 608 coarse grid, hereafter  $x_f^t$  and  $x_c^t$ , respectively, and the errors associated with the radiosonde and the 609 model fields, hereafter  $\varepsilon_{rs}$  and  $\varepsilon_m$ , as follows:

$$\mathbf{y}_{rs} = H(\mathbf{x}_f^t + \boldsymbol{\varepsilon}_{rs}) \tag{17}$$

$$\boldsymbol{y}_m = H(\boldsymbol{W}\boldsymbol{x}_c^t + \boldsymbol{W}\boldsymbol{\varepsilon}_m) \tag{18}$$

610 with  $x_c^t$  defined as  $x_c^t \equiv W^* x_f^t$  where an expression for  $W^*$ , the pseudo-inverse of W, is given in 611 Appendix B.

- 612 The comparison carried out in this study is in radiance space and the observation operator used to
- 613 simulate the brightness temperatures is identical for both radiosonde and model fields simulations.
- 614 For this reasons, we consider the radiance space as our reference and ignore any errors associated
- 615 with observation operator, that would cancel out in the difference anyway since mainly systematic.
- 616 Note that those errors need however to be taken into account if a simulated product is compared to
- 617 real satellite observations.

618 Defining the vertical interpolation error  $\boldsymbol{\varepsilon}_{int}$  as:

$$\boldsymbol{\varepsilon}_{int} \equiv \boldsymbol{W} \boldsymbol{x}_c^t - \boldsymbol{x}_f^t \tag{19}$$

619 Eq. (18) can be written as follows:

$$y_m = H(Wx_c^t - x_f^t + W\varepsilon_m + x_f^t)$$
  
=  $H(W\varepsilon_m + \varepsilon_{int} + x_f^t)$  (20)

- 620 Given *H*, the Jacobian matrix provided by RTTOV and containing the partial derivatives of  $\partial y / \partial x$
- 621 (i.e. the change in radiance,  $\partial y$ , for a change in the state vector,  $\partial x$ ), Eq.s (17) and (20) can be 622 approximated, assuming small errors, as follows:

$$\boldsymbol{y}_{rs} \cong H(\boldsymbol{x}_{f}^{t}) + \boldsymbol{H}_{\boldsymbol{x}_{f}^{t}} \boldsymbol{\varepsilon}_{rs}$$
(21)

$$\mathbf{y}_m \cong H(\mathbf{x}_f^t) + \mathbf{H}_{\mathbf{x}_f^t}(\mathbf{W}\boldsymbol{\varepsilon}_m + \boldsymbol{\varepsilon}_{int})$$
<sup>(22)</sup>

623 Therefore, the *NWP* – *GRUAN* comparison in radiance space is expressed as follows:

$$\delta \mathbf{y} \equiv \mathbf{y}_m - \mathbf{y}_{rs}$$

$$\cong \mathbf{H}_{\mathbf{x}_f^t} (\mathbf{W} \boldsymbol{\varepsilon}_m + \boldsymbol{\varepsilon}_{int} - \boldsymbol{\varepsilon}_{rs})$$
(23)

Assuming a complete uncorrelation between the interpolation error and those of the radiosondeand the model, the covariance of the difference is expressed as follows:

$$\boldsymbol{S}_{\delta \boldsymbol{y}} \equiv E\{(\partial \boldsymbol{y} - E\{\partial \boldsymbol{y}\})^T (\partial \boldsymbol{y} - E\{\partial \boldsymbol{y}\})\}$$
(24)

626 where *E* is the expectation operator. We can approximate Eq. (24) as:

$$S_{\delta v} \cong HR_f^{rs}H^T + HWB_c^m W^T H^T + HS_f^{int}H^T$$
(25)

627 where  $R_f^{rs}$ ,  $B_c^m$ , and  $S_f^{int}$  are the error covariance matrices of GRUAN measurements (on the fine 628 grid), the forecast (on the coarse grid), and the vertical interpolation (on the fine grid), respectively, 629 as described below.

630

631 We first define the GRUAN covariance matrix. GRUAN does not provide a full covariance matrix with 632 the measurements, therefore  $R_f^{rs}$  is built as a diagonal matrix accounting for the different sources of

633 uncertainty such as:

$$HR_{f}^{rs}H^{T} = H_{T}R_{T}H_{T}^{T} + H_{q}R_{q}H_{q}^{T} + H_{P}R_{P}H_{P}^{T}$$

$$+ h_{skinT}u_{skinT}^{2}h_{skinT}^{T} + h_{T2m}u_{T2m}^{2}h_{T2m}^{T}$$

$$+ h_{q2m}u_{q2m}^{2}h_{q2m}^{T} + h_{P2m}u_{P2m}^{2}h_{P2m}^{T}$$
(26)

- 634 where  $\mathbf{R}_T$ ,  $\mathbf{R}_q$ , and  $\mathbf{R}_P$  are diagonal matrices whose diagonals are the square of GRUAN profiles of
- total uncertainty for *T*, *q* (converted from *RH*), and *P*, respectively, on the Processor vertical grid;
- 636  $u_{skinT}$ ,  $u_{T2m}$ ,  $u_{q2m}$ , and  $u_{P2m}$  the uncertainties associated with the surface parameters (i.e. skin
- temperature, 2m temperature, 2m humidity, and 2m pressure) set to 0.3K, 0.3K, 0.04 RH, and
- 638 0.1hPa, respectively (Dr. S. Brickmann, DWD, private communication), estimated for the Lindenberg
- 639 site.  $H_T$ ,  $H_q$ , and  $H_P$  are the Jacobians of the temperature, humidity and pressure profiles,
- 640 respectively, and  $h_{skinT}$ ,  $h_{T2m}$ ,  $h_{q2m}$ , and  $h_{P2m}$  the Jacobians of the surface parameters.
- 641  $\mathbf{R}_T$ ,  $\mathbf{R}_q$ , and  $\mathbf{R}_P$  are diagonal which precludes a proper propagation of the correlation in radiance
- space. In this suboptimal case,  $R_f^{rs}$ , and by extension,  $S_{\delta y}$ , the covariance of the comparison, will not
- 643 capture the most accurate representation of the uncertainty budget.

- 645 Then, we define the forecast error covariance matrix. For the purposes of this study, the forecast
- 646 covariance matrix from the operational Met Office Observation Processing System, a one-
- 647 dimensional variational analysis (1D-Var) performed ahead of the main variational process, is used
- for  $B_c^m$ . Alternatively, the forecast error covariance matrix can be estimated from an ensemble of
- 649 NWP profiles as described in Appendix A.

650

- Finally, we define vertical interpolation covariance matrix. To estimate  $S_f^{int}$ , the interpolation error must be quantified.
- 653 From Eq. (19) we have:

$$\varepsilon_{int} = WW^* x_f^t - x_f^t$$

$$= (WW^* - I) x_f^t$$
(27)

- 654 where the random vector  $x_f^t$ , representing the true state on the fine grid, is assumed to have
- 655 mean  $E\{x_f^t\}$ , the (unknown) mean model forecast profile on the fine grid, and covariance
- 656  $E\left\{\left(\boldsymbol{x}_{f}^{t}-E\left\{\boldsymbol{x}_{f}^{t}\right\}\right)^{T}\left(\boldsymbol{x}_{f}^{t}-E\left\{\boldsymbol{x}_{f}^{t}\right\}\right)\right\}\equiv\boldsymbol{B}_{f}^{m}$ , the covariance of  $\boldsymbol{x}_{f}^{t}$  in model space on the fine grid. It
- 657 follows that we can express the covariance of the interpolation uncertainty as:

$$S_{f}^{int} \equiv E\{(\varepsilon_{int} - E\{\varepsilon_{int}\})^{T}(\varepsilon_{int} - E\{\varepsilon_{int}\})\}$$

$$= (WW^{*} - I)B_{f}^{m}(WW^{*} - I)^{T}$$
(28)

658 Note that when the model grid coincides with the fine grid we have  $W^* = W^{-1}$  and  $S_{int} = 0$  as 659 expected. Replacing  $W^*$  by its form expressed in Appendix B we obtain:

$$S_{f}^{int} = B_{f}^{m} (I - W (W^{T} B_{f}^{m-1} W)^{-1} W^{T} B_{f}^{m-1})$$
<sup>(29)</sup>

660 Note that in practice (i.e. for numerical calculations) it is more convenient to use the form expressed 661 in Eq. (28) to get  $S_f^{int}$  as a symmetric and positive definite matrix.

- This methodology has been applied to the 587 profiles of the night-time dataset described in the
- 664 previous section. The covariances  $S_{\delta y}$  of each comparison as approximated in Eq. (25) have been
- averaged (arithmetic mean, hereafter  $\overline{S_{\delta y}}$ ) and the square root of the diagonal (i.e. the 1 $\sigma$  standard
- deviation of the comparison total uncertainty distribution) is shown in figure 6. In practice, we
- 667 calculate  $S_{\delta y}$  as the sum of the covariance matrices of each variable: the surface measurements
- 668 covariance ( $S_{surf_rs}$ ); the model surface covariance ( $S_{surf_m}$ ); the total humidity covariance
- 669  $(S_{q\_total})$ ; the total temperature covariance  $(S_{T\_total})$ ; and the GRUAN pressure covariance  $(S_{P\_rs})$ .
- 670 The square root of their diagonal is also shown in figure 6. In addition,  $S_{q\_total}$  and  $S_{T\_total}$  can be
- 671 further decomposed into the sum of the covariance matrices of each of their components: the
- 672 GRUAN humidity and temperature covariance ( $S_{q_rs}$  and  $S_{T_rs}$ ); the model humidity and 673 temperature covariance ( $S_{a_m}$  and  $S_{T_m}$ ); and the covariance of the vertical interpolation of the
- temperature covariance ( $S_{q_m}$  and  $S_{T_m}$ ); and the covariance of the vertical interpolation of the model humidity and temperature profiles ( $S_{q_m_int}$  and  $S_{T_m_int}$ ). The square root of their diagonal

675 is also shown in figures 7 and 8.

Note that on some occasions, the Processor fine grid does not capture the lowermost or upper most

677 model levels, which caused missing values in W. The calculation has consequently been done, for

those cases, on the remaining levels of **W**. It is planned to refine the Processor grid in the future

679 version in order to avoid such missing data in the interpolation matrix.

680

681 As expected, the surface components of the total uncertainty are dominant at frequencies where

the radiance is sensitive to the surface (ATMS channels 1-7 and 16-17). Amongst them, the surface

- 683 component from the model is the largest due to the low confidence in surface emission and
- 684 properties. Channels with frequencies sensitive to temperature and humidity are dominated by the
- 685 temperature and humidity total components, respectively.
- The decomposition of the temperature and humidity total uncertainties in the temperature channels
- (fig. 7) and in the humidity channels (fig. 8), respectively, shows that, again, the model components
- are largely dominant. Note that for the highest peaking temperature channel (channel 12) the
- 689 second largest uncertainty is the GRUAN pressure component. Also, the lowest peaking humidity
- 690 channels (channels 18-19) are significantly affected by the surface uncertainty, although this may
- 691 vary with the location and the water vapour burden making those channels peak more or less high in692 the atmosphere and therefore more or less sensitive to surface.
- 693 The total uncertainty ranges from 0.08 to 0.13K for the temperature channels in figure 7, and from
- 1.6 to 2.5K for the humidity channels in figure 8. Compared to the mean difference  $\Delta Tb_{MetOffice}$
- documented in Table 1, the night-time sampling satisfies the consistency requirement of Eq. (1) with
- k=1, noting that the  $\sigma$  term in Eq. (1) that should represent the uncertainty associated with the tri-
- 697 linear horizontal interpolation, is currently unknown, although assumed small, and therefore
- 698 ignored. Future work will be dedicated to the estimation of this σ term using high resolution regional
- 699 model.

- 700 These preliminary results are in line with the uncertainty range provided by Loew et al. (2017). This
- should however be confirmed with the careful evaluation of multiple GRUAN sites over longer time
- periods, beyond the scope of this paper but planned to be addressed in the near future.
- 703
- 704



706 Figure 6: 1σ standard deviation of the total uncertainty distribution expressed as the square root of

- the diagonal of the mean comparison covariance  $\overline{S_{\delta y}}$  (blue dots), and the square root of the
- diagonal of the components forming  $\overline{S_{\delta y}}$ , namely, the GRUAN surface uncertainty (Surf\_rs, orange),
- the model surface uncertainty (Surf\_m, green), the humidity total uncertainty (q\_total, red), the
- temperature total uncertainty (T\_total, purple), and the GRUAN pressure uncertainty (P\_rs, brown).



712 Figure 7: Same as figure 6 but only for ATMS temperature upper tropospheric-lower stratospheric

channels 8-12, with in addition the square root of the diagonal of the components forming  $S_{T_total}$ ,

namely, the GRUAN temperature uncertainty (T\_rs, brownolive), the model temperature uncertainty

715 (T\_m, pink), the model vertical interpolation uncertainty (T\_m\_int, gr $\frac{3}{2}$ ).



Figure 8: Same as figure 6 but only for ATMS humidity tropospheric channels 18-22, with in addition the square root of the diagonal of the components forming  $S_{q\_total}$ , namely, the GRUAN humidity uncertainty (q\_rs, <u>brownolive</u>), the model humidity uncertainty (q\_m, <u>purplepink</u>), the model vertical interpolation uncertainty (q\_m\_int, <u>pinkgrey</u>).

721

722 It is interesting to compare the GRUAN processor upper bound uncertainty, calculated assuming a 723 complete correlation, i.e. u\_gruan\_bt, with the GRUAN contribution to  $\overline{S_{\delta y}}$ . Ignoring the uncertainties associated with the surface parameters, the GRUAN contribution to  $\overline{S_{\delta y}}$  can be 724 725 calculated as the square root of the first three term of Eq. (26). Figure 9 shows that u\_gruan\_bt is 726 consistently four times larger than the 3 $\sigma$  standard deviation of the GRUAN contribution to  $S_{\delta v}$  at 727 the frequencies of interest. It may indicate that the assumption of complete correlation in the 728 uncertainty (i.e. the use of GRUAN total uncertainty as if correlated at all levels), associated with the 729 calculation of the maximal total uncertainty in Tb results in a large overestimation of the uncertainty 730 in radiance space. In addition, it should be remembered that the use of diagonal matrices in Eq. (26) 731 is suboptimal and may not capture the full extent of the uncertainty. The lack of explicit systematic 732 and random errors associated with the radiosonde profiles and the lack of discretisation between 733 correlated and uncorrelated uncertainty components in GRUAN products is also suboptimal. This 734 stresses the need for the GRUAN community to provide proper covariance matrices, better defined 735 error profiles, and better discretisation of correlated and uncorrelated uncertainties. Finally, it is 736 possible, although not likely, that a violation of the assumption of 'small' uncertainties in Eq.s (21737 22) could result in non-linear perturbations potentially causing the GRUAN contribution to  $\overline{S_{\delta y}}$  to be

## vnderestimated.

739



740

Figure 9: 1 $\sigma$  standard deviation of the uncertainty distribution from GRUAN contribution to  $\overline{S_{\delta y}}$  is shown in blue (dotted line). It is calculated as the square root of the first three term of Eq. (26), i.e.  $\sqrt{diag(S_{q_rs} + S_{T_rs} + S_{P_rs})}$ . The 3 $\sigma$  standard deviation of the uncertainty distribution is shown in purple (solid line). u\_gruan\_bt, the GRUAN uncertainty propagated into radiance space by the GRUAN Processor and averaged over the night-time sample is shown in green (solid line).

746

747Next, the overall agreement between the Met Office model and GRUAN, in radiance space, is748assessed via a  $X^2$  test. Here, a reduced  $X^2$ , hereafter  $\tilde{X}^2$ , is estimated for each profile as follows:

$$\tilde{X}^{2} = \frac{1}{c} \left( \delta \boldsymbol{y}_{i} - \overline{\delta \boldsymbol{y}} \right)^{T} \boldsymbol{S}_{\delta \boldsymbol{y}}^{-1} \left( \delta \boldsymbol{y}_{i} - \overline{\delta \boldsymbol{y}} \right)$$
(30)

749

where  $\delta y_i$  is the *NWP* – *GRUAN* difference in Tb for the *i*<sup>th</sup> comparison,  $\overline{\delta y}$  the mean comparison over the sample. The number of degrees of freedom *c*, in this context, is the number of channels regardless any constraints as defined in Rodgers, 2000 (section 12.2).

- Comparing calculated and theoretical  $\tilde{X}^2$  will allow, in theory, the assessment and eventually 754
- 755 revision of the uncertainty estimates used for the NWP model and GRUAN. Figure 10 shows the
- distribution of  $\tilde{X}^2$  calculated for the night-time sampling (blue line) and how it compares to the 756
- theoretical  $\tilde{X}^2$  estimated from random data of similar sampling size (green line). Dashed lines show 757
- the 95-percentile of each distribution.  $\tilde{X}^2$  values beyond the theoretical 95-percentile line reflect the 758
- comparisons where the model and GRUAN are significantly different. For this example, the 95-759
- percentile of the calculated  $\tilde{X}^2$  (blue dashed line) is 5% larger than the theoretical one (green dashed 760
- line): i.e. about 10% of the calculated  $\tilde{X}^2$  are greater than the theoretical 95-percentile threshold. 761
- This relatively good match between calculated and theoretical  $\tilde{X}^2$  rules out the hypothesis of the 762 violation of small uncertainties in Eq.s (21-22). However, it might be that one (or more) component
- 763
- 764 of  $S_{\delta v}$  have been underestimated and could be revised until both 95-percentiles match. It is also possible that unforeseen sources of uncertainty have been unaccounted for in Eq. (25). In both
- 765 cases, the increased total uncertainty will reduce the number of comparisons failing the test and 766
- 767 reduce the difference between the calculated and theoretical 95-percentile threshold.

A refined assessment using a larger sample spanning several years and several GRUAN sites will be 768 addressed as part of future work, but is out of scope of this study. 769







theoretical reduced  $X^2$  estimated from a random sampling of equal size and equal degrees of freedom (blue). Dashed lines show the 95-percentile of each distribution.

775

#### 776 6. Conclusion

777 Numerical weather prediction models have demonstrated ability to act as suitable reference 778 comparators for the calibration and validation of satellite instruments. Model analysis and short-779 range forecast uncertainties are incrementally reduced by progressive improvements in data 780 assimilation techniques and the ingestion of a large and growing number of observations from 781 multiple sources. From the state-of-the-art of NWP output fields, biases as small as a tenth of a 782 Kelvin can be highlighted in some satellite datasets. In addition, NWP models provide global fields, 783 which allow for the evaluation of satellite data across the full dynamic range of the instrument. Yet 784 model uncertainty estimates do not meet international metrological traceability standards as 785 provided by other reference datasets, such as the GRUAN radiosondes.

786

In order to address the missing links in the traceability chain of model uncertainty, a collocation and
 radiance simulation tool (the GRUAN Processor) has been developed in the framework of the GAIA-

789 CLIM project. This allows us to quantify differences between GRUAN radiosonde profiles of well-

790 defined uncertainties and NWP fields, in both observation and radiance space.

791 Based on the radiative transfer core capability of the radiance simulator developed and maintained

by NWP SAF, the Processor collocates model fields to GRUAN radiosonde profiles in space and time,

then simulates top-of-atmosphere brightness temperatures for both datasets at frequencies used by

satellite instruments, and propagates GRUAN uncertainties in radiance space. The details of the

795 GRUAN Processor have been described in this paper and a mathematical methodology aimed at

assessing *NWP* – *GRUAN* comparisons in radiance space has been expounded.

797

For this study, a small sampling of 573 daytime and 587 night-time GRUAN radiosonde profiles from
Lindenberg, Germany, in 2016, and matching NWP fields from the Met Office and ECMWF global
models have been processed and analysed to demonstrate the GRUAN Processor capability.

801 In the geophysical space of the radiosonde observations, the *NWP* – *GRUAN* comparison has

802 highlighted 0.5K cold biases located in the stratosphere of the ECMWF model and in the lower

troposphere of the Met Office model. A wet bias ranging from 50 to 75% of the local specific

humidity is visible in both models at pressure between 200 and 100hPa.

805 In radiance space, the Met Office and ECMWF Tb are found to be within ±0.09K and ±0.39K,

806 respectively, to GRUAN night-time profiles (when GRUAN biases are minimal), at frequencies

807 predominantly sensitive to temperature (54-57GHz) in the vertical domain where GRUAN

radiosonde observations are available. Similarly, the Met Office and ECMWF Tb are found to be

809 within ±0.46K and ±0.37K, respectively, to GRUAN night-time profiles at frequencies predominantly

810 sensitive to humidity (around 183GHz).

- 812 The propagation of GRUAN uncertainties in radiance space is performed in the GRUAN Processor via
- 813 perturbation of the temperature, humidity and pressure profiles by plus and minus their total
- 814 uncertainty as provided in the RS92-GDP data files. This process assumes a complete correlation of
- 815 the uncertainties at all levels. This is a pessimistic assumption and the resulting uncertainty obtained
- 816 in radiance space is therefore representative of a maximum uncertainty of the GRUAN component
- 817 (the model uncertainty is not accounted for). The true GRUAN uncertainty in radiance space is
- smaller than that calculated as only a fraction of GRUAN total uncertainty (in observation space) is
- 819 really correlated over the entire profile.
- 820 Independently from that maximum GRUAN uncertainty estimate, a rigorous estimation of the
- 821 uncertainties in radiance space associated with the *NWP GRUAN* difference is proposed in this
- study as a post-processing application based on the GRUAN Processor outputs. The covariance of
- this difference,  $S_{\delta y}$ , is calculated as the sum of the GRUAN, model, and interpolation uncertainties
- 824 propagated in radiance space.
- 825 Tested with the Met Office background error covariance, the NWP component of  $S_{\delta y}$  is found to be
- the dominant source of uncertainty. The total uncertainty of the difference ranges from 0.08 to
- 827 0.13K at frequencies sensitive to temperature and from 1.6 to 2.5K at frequencies sensitive to
- 828 humidity, satisfying, on average, the consistency check (Eq. 1) for night-time profiles.
- 829 The GRUAN component of  $S_{\delta y}$  is found to be four times smaller (at  $3\sigma$ ) than the maximum GRUAN
- 830 uncertainty estimated in the Processor, demonstrating the large overestimation of the complete
- 831 correlation assumption. However, it is worth stressing that in absence of covariance information,
- 832 error (random and systematic) characterisation, and discretisation between correlated and
- 833 uncorrelated uncertainty components in GRUAN data files, the estimation of  $S_{\delta y}$  remains
- 834 suboptimal.
- 835 The X<sup>2</sup> distribution calculated for the comparisons between model-based (Met Office) and GRUAN-
- based simulated Tb revealed that the number of significantly different comparisons is close although
- slightly larger than that of the corresponding theoretical  $X^2$  distribution. Implications are that either
- 838 one or several components of  $S_{\delta y}$  are underestimated, or that a source of uncertainty has been
- 839 overlooked.
- 840
- 841 The next step will be to process and analyse collocated profiles spanning several years and multiple 842 GRUAN sites. This will provide a better, although incomplete, geographical distribution of model biases as well as their evolution in time. Away from the surface, NWP model biases are to first order 843 a function of latitude and height, and can usefully be studied for polar, mid-latitude and tropical 844 845 bands. For northern latitude bands, the NWP uncertainties can be studied by comparison with GRUAN observations, but for the tropics and southern latitudes, where there are few or no GRUAN 846 847 data, these could to be supplemented with other high quality radiosonde reports. The aim will be to 848 provide a refined set of model uncertainty for selected frequencies spanning both microwave and 849 infrared domains. Ultimately, the contribution from this work will help draw the full model 850 uncertainty budget (composed of uncertainties in radiance space, radiative transfer modelling, scale

- mismatch, and cloud residual) for more robust assessment of satellite observations. Finally, the
- larger sampling will also ensure a more robust  $X^2$  analysis and, if deemed necessary, help revise the model covariance matrices used in operation at the Met Office and ECMWF.

The quantitative estimate of errors and uncertainties in NWP models, both temperature, humidity, and radiance space, could aid in the interpretation of observation minus short-range forecast

- statistics for satellite instruments, for example by helping to identify whether biases in observation-
- 857 minus-model background values could be due to systematic errors in the NWP model short-range
- 858 forecasts. In future work, it is planned to use the GRUAN processor output to evaluate biases in
- 859 observation-minus-model background statistics of satellite data.
- 860 Finally, the GRUAN processor will also evolve with the evolution of RTTOV. For example, a parallel
- 861 version of the Processor is currently being tested with the fast radiative transfer model RTTOV
- 862 Ground-based (RTTOV-gb). RTTOV-gb is a modified version of RTTOV that allow for simulations of
- 863 ground-based upward-looking microwave sensors (De Angelis et al., 2016). Model and GRUAN

simulated Tb and propagated uncertainties are expected to help estimate the uncertainties in the

- 865 microwave radiometer observations for which RTTOV-gb has been developed. It is also planned to
- upgrade the Processor in order to support RTTOV 12 (Hocking et al., 2017). This upgrade will allow
   the better handling of surface emissivity and give the option to output principal components (PC)
- 200 und for the new generation of human star star infrared soundars. Note that other fact redictive
- used for the new generation of hyperspectral infrared sounders. Note that other fast radiative
   transfer models, such as the Community Radiative Transfer Model (CRTM), could potentially be
- 870 tested with the GRUAN Processor, although there is no immediate plan to do so.
- 871

## 872 Appendix A: Forecast error covariance matrix estimation

873If the forecast error covariance matrix from the NWP forecast model used as input to the Processor874is not available, it can be determined from an ensemble of K NWP profiles, with K>N where N is the

875 number of vertical levels, such that:

$$\boldsymbol{B}_{c}^{\boldsymbol{m}} = \frac{\boldsymbol{X}'\boldsymbol{X}'^{T}}{K-1} \tag{A1}$$

where K - 1 gives the best estimate of the covariance of the population from which the sample K is drawn, and with X' such as:

$$X' = (x_c^{m_1} - \overline{x_c^m}, \dots, x_c^{m_j} - \overline{x_c^m}, \dots, x_c^{m_K} - \overline{x_c^m})$$
(A2)

where  $x_c^{m_j}$  is the  $j^{th}$  model profile of the K ensemble, and  $\overline{x_c^m}$  is the mean of the K profiles, both on the coarse model vertical grid.

- 881 Appendix B: Interpolation matrix pseudo inverse
- 882 The interpolation matrix W is not square and therefore its inverse cannot be calculated. Instead, a
- pseudo inverse,  $W^*$ , can be to express using, for example, the weighted least square estimate of  $x_c^t$ (Rodgers, 2000). For that, we need to minimize:

$$\boldsymbol{r} = \frac{1}{2} \left( \boldsymbol{x}_{f}^{t} - \boldsymbol{W} \boldsymbol{x}_{c}^{t} \right)^{T} \boldsymbol{B}_{f}^{m-1} \left( \boldsymbol{x}_{f}^{t} - \boldsymbol{W} \boldsymbol{x}_{c}^{t} \right)$$
(B1)

- where, for the weight, we use the forecast error covariance matrix expressed on the fine grid,  $B_f^m$ , since we interpolate the model profiles on that grid.
- 887 By taking the derivative with respect to  $x_c^t$  and setting it to zero, we find:

$$\boldsymbol{x}_{c}^{t} = \left(\boldsymbol{W}^{T}\boldsymbol{B}_{f}^{m-1}\boldsymbol{W}\right)^{-1}\boldsymbol{W}^{T}\boldsymbol{B}_{f}^{m-1}\boldsymbol{x}_{f}^{t}$$
(B2)

888 where.

$$\boldsymbol{W}^* = \left(\boldsymbol{W}^T \boldsymbol{B}_f^{m-1} \boldsymbol{W}\right)^{-1} \boldsymbol{W}^T \boldsymbol{B}_f^{m-1}$$
(B3)

889 In order to find an expression for  $B_f^m$ , we refer to  $B_c^m$ , the forecast covariance matrix on the coarse

model grid, to calculate the forecast error correlation matrix  $C_c^m$ , on the coarse model grid. The

correlation matrix is then reconditioned on the fine Processor grid, and referred to as  $C_f^{rec}$ , as explained below.

893 Defining  $\Sigma$ , a diagonal matrix representing the square root of  $B_c^m$  variance, such as:

$$\Sigma = \sqrt{diag(\boldsymbol{B}_c^m)} \tag{B4}$$

894  $C_m$  can be expressed as:

$$\boldsymbol{C}_m = \boldsymbol{\Sigma}^{-1} \boldsymbol{B}_c^m \boldsymbol{\Sigma}^{-1} \tag{B5}$$

895 We can then define  $C_f^m$  as:

$$\boldsymbol{C}_{f}^{m} = \boldsymbol{W} \boldsymbol{C}_{c}^{m} \boldsymbol{W}^{T} \tag{B6}$$

However, Eq. (B6) does not guarantee that  $C_f^m$  diagonal elements are equal to one. This constraint needs to be imposed such as:

$$\boldsymbol{C}_{f}^{rec} = \boldsymbol{W}\boldsymbol{C}_{c}^{m}\boldsymbol{W}^{T} - diag(\boldsymbol{W}\boldsymbol{C}_{c}^{m}\boldsymbol{W}^{T}) + \boldsymbol{I}$$
(B7)

898 Given  $\sigma_m$ , a vector composed of the square root of the variance of  $\boldsymbol{\varepsilon}_m$  variance,  $\boldsymbol{B}_f^m$  is expressed as 899 follows:

$$\boldsymbol{B}_{f}^{m} = diag(\boldsymbol{W}\sigma_{m})\boldsymbol{C}_{f}^{rec}diag(\boldsymbol{W}\sigma_{m})$$
(B8)

900

901 Data availability

For further information on the GRUAN Processor source code and/or outputs availability, please
 contact the lead author (<u>fabien.carminati@metoffice.gov.uk</u>).

905	Author contribution
906	FC developed the GRUAN Processor code, analysed the data, and prepared the manuscript with
907	contributions from all co-authors. SM developed the mathematical framework presented in section
908	5. BI and HL provided ECMWF datasets and helped with code design and data analyses. WB and SN
909	helped with code design and data analyses. JH develops and manages RTTOV. AS developed the
910	Radiance Simulator.
911	
912	
913	Competing interests
914	The authors declare that they have no conflict of interest.
915	
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922	
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1080 <u>Tables</u>

# 1082Table 1: Mean difference NWP – GRUAN in simulated Tb for ECMWF (ΔTb<sub>ECMWF</sub>) and Met Office1083(ΔTb<sub>Metoffice</sub>) and 1σ standard deviation for ATMS channels 8-12 and 18-22 at day and night-time.

<u>Channel</u>	Frequency (GHz)	<u>ΔTb<sub>ECMWF</sub> (1σ) (K)</u>		<u>ΔTb<sub>MetOffice</sub> (1σ) (K)</u>	
		<u>night</u>	<u>day</u>	<u>night</u>	<u>day</u>
<u>8</u>	<u>54.94</u>	<u>-0.08 (0.09)</u>	<u>-0.16 (0.10)</u>	<u>-0.00 (0.11)</u>	<u>-0.04 (0.12)</u>
<u>9</u>	<u>55.5</u>	<u>-0.15 (0.12)</u>	<u>-0.24 (0.13)</u>	<u>0.04 (0.13)</u>	<u>-0.02 (0.14)</u>
<u>10</u>	<u>57.29</u>	<u>-0.32 (0.18)</u>	<u>-0.45 (0.18)</u>	<u>0.01 (0.16)</u>	<u>-0.07 (0.20)</u>
<u>11</u>	<u>57.29±0.217</u>	<u>-0.39 (0.21)</u>	<u>-0.54 (0.22)</u>	<u>-0.04 (0.20)</u>	<u>-0.16 (0.25)</u>
<u>12</u>	57.29±0.3222±0.048	<u>-0.34 (0.25)</u>	<u>-0.53 (0.27)</u>	<u>-0.09 (0.28)</u>	<u>-0.26 (0.31)</u>
<u>18</u>	<u>183.31±7.0</u>	<u>0.35 (0.91)</u>	<u>0.25 (1.09)</u>	<u>0.02 (0.83)</u>	<u>-0.36 (1.02)</u>
<u>19</u>	<u>183.31±7.0</u>	<u>0.37 (1.13)</u>	<u>0.15 (1.24)</u>	<u>-0.09 (1.03)</u>	<u>-0.48 (1.14)</u>
<u>20</u>	<u>183.31±3.0</u>	<u>0.34 (1.31)</u>	<u>-0.01 (1.36)</u>	<u>-0.18 (1.22)</u>	<u>-0.61 (1.27)</u>
21	<u>183.31±1.8</u>	<u>0.22 (1.48)</u>	<u>-0.29 (1.50)</u>	<u>-0.31 (1.42)</u>	<u>-0.81 (1.45)</u>
<u>22</u>	<u>183.31±1.0</u>	0.04 (1.61)	<u>-0.61 (1.64)</u>	-0.46 (1.57)	<u>-1.01 (1.60)</u>