# On the information content in linear horizontal delay gradients estimated from space geodesy observations

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**Abstract.** We have studied linear horizontal gradients in the atmospheric propagation delay above ground-based stations receiving signals from the Global Positioning System (GPS). Gradients were estimated from 11 years of observations from five stations in Sweden. Comparing these gradients with the corresponding ones from the European Centre for Medium-Range Weather Forecasts (ECMWF) analyses shows that GPS gradients detect effects over different time scales caused by the hydro-

- 5 static and the wet components. The two GPS stations equipped with microwave absorbing material below the antenna in general show higher correlation coefficients with the ECMWF gradients compared to the other three stations. We also estimated gradients using GPS data from two collocated antenna installations at the Onsala Space Observatory. Correlation coefficients for the east and the north wet gradients estimated with a temporal resolution of 15 minutes from GPS data can for specific months reach up to 0.8 when compared to simultaneously estimated wet gradients from microwave radiometry. The best agreement is
- 10 obtained when an elevation cutoff angle of 3° is applied in the GPS data processing, in spite of the fact that the radiometer does not observe below 20°. Based on the four years of results we note a strong seasonal dependence in the correlation coefficients, from 0.3 during months with smaller gradients to 0.8 during months with larger gradients, typically during the warmer, and more humid, part of the year. Finally, a case study using a 15-day long continuous Very Long Baseline Interferometry (VLBI) campaign was carried out. The comparison of the gradients estimated from VLBI and GPS data indicates that a homogeneous

15 and frequent sampling of the sky is a critical parameter.

# 1 Introduction

Space geodetic techniques, where the fundamental observable is a radio signal's time of arrival at a station on the surface of the Earth, are affected by variations in the propagation velocity in the atmosphere. Because time measurements avoid problems related to accurate calibration, which are common for systems measuring different types of emissions, it is a common view that Global Navigation Satellite Systems (GNSS) have a long term stability and are well suited for climate monitoring, e.g.

20 that Global Navigation Satellite Systems (GNSS) have a long term stability and are well suited for climate monitoring, e.g. in terms of the atmospheric water vapour content. Estimates of the total propagation delay above a GNSS station can be used to determine the integrated amount of water vapour. It is also common practice to estimate two-dimensional horizontal linear gradients for each station in the GNSS data processing, because it improves the reproducibility of estimated geodetic parameters, see e.g. (?).

- 25 We have studied estimated gradients primarily from GPS data from Swedish GNSS stations by comparing these gradients to independent measurements. An important site is the Onsala Space Observatory where a geodetic Very Long Baseline Interferometry (VLBI) telescope and a water vapour radiometer (WVR) are installed and collocated with GNSS receiver stations. The overall goal was to study the usefulness of GPS-derived gradients in atmospheric and climate research. Previous studies have been carried out using GPS/GNSS data from Onsala. Comparing the gradients derived from VLBI, GPS, and a WVR,
- ? found that when varying the constraint for the gradient variability from 0.2 to 5.6 mm/ $\sqrt{h}$  the weighted root-mean-square 30 (RMS) difference compared to the WVR gradients varied between 0.8 and 1.0 mm for both the GPS and the VLBI gradients. Using multi-GNSS observations, ? found a significant increase in the correlation coefficient to about 0.6 when compared to ECMWF gradients, while the one for the GPS only was typically below 0.5. In addition, they found that the RMS difference of the gradient was reduced to about 25-35 % by multi-GNSS processing.
- 35 There are some interesting questions actualised by previous work which we tried to take further. Of specific interest in our study was to investigate if there is any systematic seasonal behaviour in the estimated gradients in Sweden, and if these make sense given the present knowledge about the meteorological conditions. Another issue is that comparisons of estimated GPS gradients with a high temporal resolution are rather sparse, and have to our knowledge so far not covered periods of many years. Here we report on comparisons between GPS and WVR gradients, with a temporal resolution of 15 minutes, over a
- more or less continuous 4-year period. 40

In Section ?? we give a short background on the cause of gradients that are sensed by the space geodetic techniques and the model used to estimate them. In Section ?? instruments, techniques, and their data are described. The results are presented in two sections. First, in Section ??, we compare 11 years of total gradients from five Swedish GNSS stations to gradients originating from the European Centre for Medium-Range Weather Forecasts (ECMWF) analyses. Here we study seasonal dependence

45 as well as estimates of long term trends. In Section ??, we use data from two collocated GNSS stations (with different antenna installations) and one WVR to assess the station performances and differences between different GPS processing variants. We also study the seasonal dependence of the estimated wet gradients over a 4-year period. Finally, within this 4-year period a 15-day long VLBI campaign occurred which we use as a case study. In Section ?? we present our conclusions and suggest possible future studies of gradients.

#### Cause of horizontal gradients and models 50 2

The delay of space geodetic signals propagating through the atmosphere depends of the refractive index. For space geodetic applications it is meaningful to define one hydrostatic and one wet component (?). For a horizontally stratified atmosphere it is then common practise to use equivalent zenith values for these components. Additionally we may define a horizontal linear gradient, that can be inferred from ground-based observations (?), consisting of one east and one north component, which in turn also can be separated, into one hydrostatic and one wet component.

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Hydrostatic gradients are determined by pressure and temperature gradients and exist mainly over regional scales (e.g. persistent high and low pressure systems) and synoptic scales (e.g. weather systems). Using a European and a global GPS network, including three of the GPS stations used in this study, ? have shown that the north gradient has a clear dependence on latitude when averaged over long time scales. For the area of interest in this study we specifically mention the Icelandic

low pressure system that typically evolves in the winter and disappears in the summer (?). This is a component in the North

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Atlantic Oscillation and the Arctic Oscillation (??).

Temperature and especially water vapour can show strong horizontal gradients over small (kilometre) scales and the temporal variability is typically also much higher than that of the hydrostatic gradients, see e.g. ?. Hence, the large local gradients over a station are mainly caused by the variability in water vapour and the wet refractivity. Gradients can be significant during a

- 65 passage of a weather front, e.g. ? report gradient amplitudes of up to 3–4 mm during the passage of an occlusion front over Germany. ? have studied gradients during the passage of mesoscale convective systems in West Africa and ? have shown correlations between gradients and precipitation and moisture fluxes in Morocco. Other specific weather phenomena that can cause horizontal variability in the partial pressure of water vapour, and hence also the wet refractivity, are sea breeze (??), cloud rolls (?) and convection processes in general.
- 70 We note that none of the known processes is expected to be strictly horizontally linear, but the strength in the geometry, the distribution of the observations on the sky, and the GNSS data quality makes it difficult to determine additional atmospheric parameters of higher order.

The atmospheric parameters that are normally estimated when processing space geodesy data are an equivalent zenith wet delay and linear horizontal delay gradients in the east and the north directions. The uncertainties of the estimates depend on the

75 geometry of the observations and the accuracy of the so called mapping functions, used to describe the estimated parameters dependence on the elevation angle, given the specific weather conditions at the site, at the time, see e.g. ? and ?. The common model used to relate the observed delay along the line-of-sight,  $\Delta L(\alpha, \varepsilon)$ , and the estimated parameters (?) is also used in this study, i.e.

$$\Delta L(\alpha,\varepsilon) = m_h(\varepsilon) \Delta L_{hz} + m_w(\varepsilon) \Delta L_{wz} + m_q(\varepsilon) \left[ \Xi_e \sin \alpha + \Xi_n \cos \alpha \right] \tag{1}$$

80 where  $m_h$ ,  $m_w$ , and  $m_g$  are the mapping functions, depending on the elevation angle  $\varepsilon$ , for the hydrostatic and the wet delays, and the gradients, respectively;  $\Delta L_{hz}$  and  $\Delta L_{wz}$  are the equivalent hydrostatic and wet delays in the zenith direction;  $\alpha$  is the azimuth angle, measured clockwise from the north, implying that  $\Xi_e$  and  $\Xi_n$  are the gradients in the east and in the north directions. While total gradients are estimated, they can be interpreted as the sum of hydrostatic and wet components as well. In the following we will subtract the hydrostatic component computed from ECMWF from the total GPS gradient to get the 85 GPS wet gradient.

In addition to the east and the north gradient components we also studied the gradient amplitude, defined as

$$|\Xi| = \sqrt{\Xi_e^2 + \Xi_n^2} \tag{2}$$

The gradient amplitude is defined for the hydrostatic, the wet, and the total gradients.

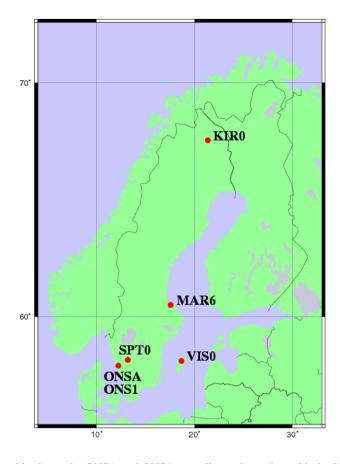


Figure 1. The six GPS stations used in the study. ONSA and ONS1 are collocated together with the VLBI telescope and the WVR at the Onsala Space Observatory.

### 3 Instrumentation and data

90 We compared gradients estimated from GPS observations acquired at five sites and six antenna/receiver installations: Kiruna (KIR0), Mårtsbo (MAR6), Onsala (ONSA and ONS1), Borås (SPT0), and Visby (VIS0), with respect to VLBI, WVR, and ECMWF estimates. These stations are also part of the EUREF network (?). Their geographic locations are shown in Figure ??. In this section we first describe the different datasets. Thereafter, we summarise their use and characterise them in terms of formal errors, advantages, and disadvantages.

### 95 3.1 GPS

We used 11 years of GPS data (2006–2016) from the five Swedish GNSS sites mentioned above. Gradients in the east and the north directions were estimated with a temporal resolution of 5 min. Two GNSS stations are operating continuously at the Onsala Space Observatory, on the west coast of Sweden. The primary station, ONSA, was established already in 1987 and the other station, ONS1, was taken into operation in 2011. The six antenna installations are shown in Figure ??. The antennas of

100 ONSA and ONS1 are located within 100 m from each other and should observe almost identical atmospheric gradients. For the time period 2013–2016 we compared gradients from these two stations with simultaneously estimated gradients using data from a WVR.

The analysis of the GPS data followed the same lines as described by **?** and is summarised in Table **??**. Specifically we mention that each day was analysed independently after adding 3 h of data from the previous day and 3 h from the following day, i.e. in total 30 h. The reason was to avoid discontinuities at midnight in the estimated time series.

Recent work by ? compared estimated gradients with those from a numerical weather model using different gradient mapping functions and elevation cutoff angles. They found the best agreement for an elevation cutoff angle equal to  $3^{\circ}$ . They also showed that the ? gradient mapping function resulted in 17 % smaller gradient amplitudes compared to the ? mapping function. For the 11-year study presented in the next section we used a  $10^{\circ}$  elevation cutoff angle only, whereas we used several different elevation cutoff angles in the comparison with the WVR data from the Onsala site for a 4-year period.

Based on the five-minute gradients we calculated mean values over 15 min, 6 h, 1 day, and 1 month in order to match the temporal resolution of the comparison data and to study the variability of the wet and the hydrostatic gradients over different time scales.

Table 1. Processing of GPS data.

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Parameter	Description / Value
Processing software	GIPSY v6.2 (?)
Strategy	Precise Point Positioning (?) final orbit and clock products
	were provided by JPL obtained from the legacy GIPSY-OASIS software <sup><math>a</math></sup>
Reference frame	IGS08
Mapping functions for $\Delta L_z$	Vienna 1 2006 (VMF1) (?) <sup>b</sup>
Mapping function for $\Xi$	?
Elevation cutoff angle	10° <i>c</i>
Zenith delay	Estimated every 5 min, constraint 10 mm/ $\sqrt{h}$ (?)
Linear horizontal gradient	Estimated every 5 min, constraint 0.3 mm/ $\sqrt{h}$ (?)
Ocean tide model	FES2004 (?)
Antenna phase centre	igs08_1740.atx (?) <sup>d</sup>
Ambiguity resolution	Yes (?)
Ionosphere model	2nd order $(IGRF)^e$ (?)

a For the 11-year dataset, for the 4-year dataset, the products were obtained from a new GipsyX software. We noted that the difference in the products due to the change of software is small (?).

<sup>b</sup> For the 11-year dataset, for the 4-year dataset also the weighted  $(\sin(\varepsilon))$  VMF1 and the NMF (?) were used.

 $^c$  For the 11-year dataset, for the 4-year dataset also 3  $^\circ$  and 20  $^\circ$  were used.

 $^{d}$  For the 11-year dataset, for the 4-year dataset igs08\_1869.atx were used.

 $^{e}$  International Geomagnetic Reference Field



Figure 2. The six antenna installations used to acquire the GPS data. See Figure ?? for their geographical location.

Examples of the sky coverage of the GPS observations are shown in Figure **??** for the Onsala site. At this latitude there is a significant part of the sky that is never sampled, just north of the zenith direction. It is reasonable to assume that this will have a negative impact on the estimated gradients, and especially in the north direction.

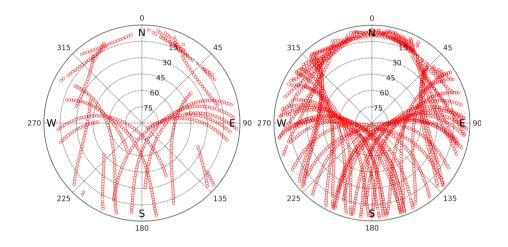


Figure 3. Sky plots of GPS observations at Onsala from 6 to 12 UT (left) and from 0 to 24 UT (right) on May 12, 2014. This particular day was chosen because it is included in the CONT14 campaign presented in Section ??. The sky distribution of observations is very similar, although not identical, for all days.



Figure 4. The water vapour radiometer (WVR) Konrad at the Onsala Space Observatory.

### 3.2 Microwave radiometer

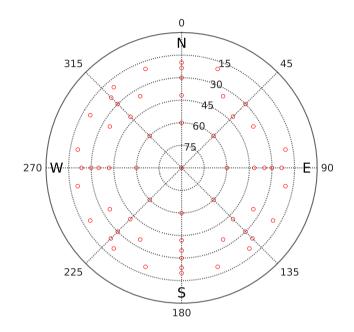
The microwave radiometer, shown in Figure **??**, was designed in order to provide independent estimates of the wet propagation delays for space geodetic applications. It measures the emission from the sky, on and off the water vapour line at 22.2 GHz. Its specifications are summarised in Table **??** and the data processing was carried out as was described for another WVR by **?**.

- 120 specifications are summarised in Table ?? and the data processing was carried out as was described for another WVR by ?. During the time period 2013–2016 the WVR was observing in a sky mapping mode as is illustrated in Figure ??. A disadvantage of a WVR is that the algorithm for calculation of the wet propagation delay fails for data acquired during rain or when large liquid drops are present in the sensed atmosphere. Typically such conditions imply large positive errors in the wet delay, and the water vapour content (?). Therefore, data taken during rain, or when the estimated equivalent amount of liquid water in
- 125 the zenith direction is > 0.7 mm, were discarded from the gradient analysis. In addition there were also time periods when the WVR hardware has failed. The amount of analysed data are shown in Figure ?? as the number of individual observations per day. The first long data gap, in 2014–2015, was caused by a broken mechanical waveguide switch and the second long gap, in 2015–2016, was due to broken cables in the so called cable wrap. The cable wrap was redesigned.
- In order to avoid ground-noise pickup the WVR provided observations of the wet delay in the different directions above 20°.
  130 Therefore a simple sin(ε) mapping function was used to relate these slant wet delays to the equivalent zenith wet delay (ZWD). The WVR gradients were estimated based on all observations carried out during a period of 15 min using the method of least squares and the Bar-Sever gradient mapping function. We used a four-parameter model, fitting a ZWD, a ZWD rate, and an east and a north gradient to the data (?). This means that the estimated gradients are independent of the successive estimates, which is different from the gradients estimated from the space geodetic techniques, where temporal constraints are applied.

 Table 2. Specifications for the Konrad WVR.

Parameter	Value
Frequencies	20.6 GHz and 31.6 GHz
Antenna type (one for each channel)	Conical horn with lens
Antenna beam FWHM <sup>a</sup> , E-plane, ch.1 / ch.2	2.9°/ 2.0°
Antenna beam FWHM <sup>a</sup> , H-plane, ch.1 / ch.2	3.4°/ 2.3°
Reference temperatures (both channels)	313 and 373 K
System noise temperatures, channel 1 / 2	450 / 550 K
RF bandwidth (double sideband)	320 MHz (both channels)
Absolute accuracy (weather dependent due to the quality of tip curves)	1–3 K
Repeatability	0.1 K

 $^a$  FWHM = Full Width Half Maximum



**Figure 5.** A measurement cycle of the WVR begun with two azimuth scans. In order to avoid emission from the ground the lowest elevation angle observed was  $20^{\circ}$ . Starting in the north, first turning at an elevation angle of  $20^{\circ}$  clockwise to the north (excluding the azimuth angles of  $40^{\circ}$  and  $60^{\circ}$  due to a nearby radio telescope), and then turning counterclockwise at an elevation angle of  $35^{\circ}$ . Thereafter four tip curves were made over the zenith direction (implying four observations in the zenith direction during each cycle): from the north to the south, from the southwest to the northeast, from the east to the west, and from the northwest to the southeast. The cycle was about 8 min long and was repeated continuously, implying that almost two complete cycles with a total of  $\approx 100$  observations were used when estimating gradients every 15 min.

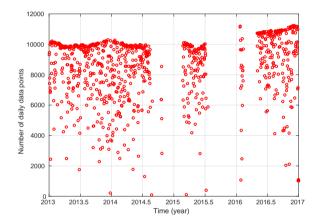


Figure 6. Number of data points per day observed by the WVR. During days without data loss, e.g. due to rain, each estimated gradient was based on  $\approx 100$  observations in the directions illustrated in Figure ??. Observations close to the sun were removed from the raw data before the data analysis was carried out which causes the seasonal variation in the maximum number of observations per day. During the last year the measurement cycle was optimised by reducing some of the time delays inserted between samples but the observational sequence shown in Figure ?? was used during the whole period.

#### 135 3.3 Very long baseline interferometry

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We used the VLBI data from the CONT14 campaign coordinated by the International VLBI Service (?). The IVS organises continuous (CONT) VLBI campaigns every third year in order to acquire state-of-the-art VLBI data over a time period of two weeks and to demonstrate the highest accuracy of which the current VLBI system is capable. The primary goal of these CONT campaigns is to support research concerning high resolution Earth rotation (?) reference frame stability, and daily to sub-daily site motions, but also other aspects. A concise overview of the IVS CONT campaigns is given by ?.

The CONT14 campaign was observed during May 6–20, 2014. The VLBI data were analysed with the calc/solve VLBI data analysis software (?). Station positions, ZWD, atmospheric gradients, relative clock parameters w.r.t. a reference station, as well as earth rotation parameters were estimated. The relative clock parameters were estimated as a piecewise linear functions every hour, with a constraint of  $5 \cdot 10^{-14}$  s/s between clock rate segments. The ZWD and atmospheric gradients were estimated as

145 piecewise linear functions (i.e. not stochastic processes) with a temporal resolution of 30 min and 6 h, respectively. Constraints for the variability of 15 mm/h for the ZWD rate segments, and 2 mm/day for gradient rates were applied. The NMF (?) mapping functions for ZWD and the ? mapping function for gradients were used in the analysis, together with meteorological information recorded at the VLBI stations. An elevation cutoff angle of 5° was used, and no elevation-dependent weighting.

Figure ?? depicts the sampling of the sky for a 6 h period, which is the highest temporal resolution of the gradient estimatesfrom VLBI, as well as all observations scheduled for a 24 h experiment. This schedule was repeated every day with only minor modifications.

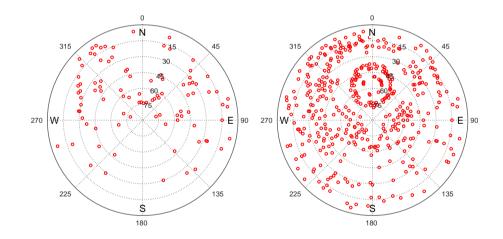
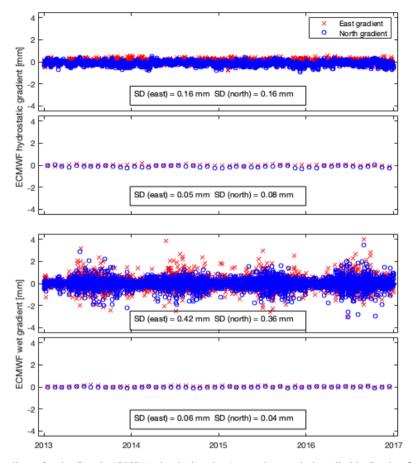


Figure 7. The directions of the VLBI observations for the time period from 6 to 12 UT (left) and from 0 to 24 UT (right), both on May 12, 2014.



**Figure 8.** The ECMWF gradients for the Onsala (ONSA) site during the 4-year time period studied in Section **??**. From the top: hydrostatic gradients every 6 h, their monthly averages, wet gradients every 6 h, and their monthly averages.

# 3.4 ECMWF

The Technical University of Vienna provided hydrostatic and wet gradients based on ECMWF data for many space geodetic sites globally. Figure ?? depicts the five sites used here. Details are given by ?, so we just mention the characteristics that are most relevant for our comparisons. ECMWF provided profiles of hydrostatic and wet refractivity with a temporal resolution of 6 h, and a spatial resolution of  $0.25^{\circ}$  (~30 km). The profile closest to the site were used together with one profile to the east and one profile to the north to calculate the refractivity gradient profiles. These were thereafter integrated to give the delay gradients. The data were available during certain time periods from the mid of 2005 and were more continuous from 2006. We decided to use the data from 2006 to 2016, resulting in a time series of 11 years.

160 As an introduction, examples of the ECMWF hydrostatic and wet gradients are illustrated in Figure **??**. Worth noting is that the wet gradients dominate for the temporal resolution of 6 h and vary with the season, whereas the wet and the hydrostatic gradients show similar standard deviations (SD) for the monthly averages.

#### 3.5 Summary of datasets

The results of comparisons between the gradients from these datasets are presented in the next two sections. The usage is

- 165 defined in Table ??. In Section ?? GPS gradients estimated using the 10° elevation cutoff angle are compared to the ECMWF gradients. The temporal resolution is limited to 6 h in the ECMWF data. On the other hand the time series are 11 years long. The results in Section ?? focus on comparisons of the wet gradients at the Onsala site. These have a temporal resolution of 15 minutes when comparing to WVR data and the ECMWF data are only used to subtract the hydrostatic gradients from the total gradients estimated by the GPS and the VLBI techniques. In Table ?? we summarise the typical formal errors of the remote
- 170 sensing techniques. Worth noting is the larger formal error for the north GPS gradient, compared to the east gradient, using the elevation cutoff angle of 20°. The reason is that we lose many observations of satellites located in the north, see Figure ??. Other important comments are that WVR gradients are not estimated during rain events and are not based on observations below 20° elevation angles, but have a more homogeneous sky coverage compared to the GPS and the VLBI observations. Gradients from GPS and WVR have a superior temporal resolution, 5 and 15 min, respectively, compared to the 6 h of the
  175 VLBI and the ECMWF gradients.

Table 3. Summary of used datasets.

Dataset	Resolution	Time period	ONS1	ONSA	SPT0	VIS0	MAR6	KIR0
GPS <sup>a</sup>	5 min	2006-2016	-	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$
$\mathrm{ECMWF}^{b}$	6 h	2006–2016	-	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$
GPS $^{c}$	5 min	2013-2016	$\checkmark$	$\checkmark$	-	-	-	_
WVR	15 min	2013-2016	$\checkmark$	$\checkmark$	-	-	-	_
VLBI	6 h	6–20 May 2014	$\checkmark$	$\checkmark$	-	-	-	_

 $^a$  The GPS data were processed with elevation cutoff angles equal to  $10^\circ$ .

<sup>b</sup> (?)

 $^{c}$  The GPS data were processed with elevation cutoff angles equal to 3°, 10°, and 20°, different mapping functions, and elevation angle dependent weighting.

Data	Elev.	F	or	
set	cutoff	Grad	ZWD	
	angle	East	North	
	(°)	(mm)	(mm)	(mm)
GPS	3	0.14	0.13	1.7
GPS	10	0.19	0.20	2.3
GPS	20	0.35	0.43	4.0
WVR	20	0.04	0.04	0.2
VLBI	5	0.14	0.13	1.7

Table 4. Formal errors of the remote sensing techniques

#### 4 Comparison of gradients from GPS and ECMWF data for the time period 2006–2016

#### 4.1 Seasonal variations of horizontal gradients

We start by investigating the characteristics of the gradients over the year. In Figure ?? we present the monthly mean gradients for the time period 2006–2016 estimated from ECMWF data and GPS data from the Onsala (ONSA) station. In the top graphs,
comparing ECMWF and GPS gradients, we note that the GPS gradients show a larger variability. There are also differences between the east and the north gradients both in the mean over the year and in the seasonal variations.

We can clearly see negative north gradients in the winter, with a mean value around -0.2 mm, both in the GPS and the ECMWF results. When the ECMWF gradients are separated into the hydrostatic and the wet components this variation appears in the hydrostatic component. We interpret this effect as the influence of the Icelandic low pressure system mentioned in Section **??**. The winter feature is clearly seen in the analyses of the mean sea level pressure in the ERA-40 Atlas

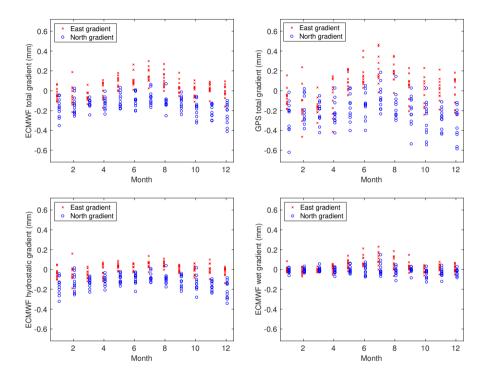
(https://software.ecmwf.int/static/ERA-40\_Atlas/docs/section\_B/parameter\_mslp.html)

The results for the other four stations (KIR0, MAR6, SPT0, and VIS0) show similar systematic features. One exception is KIR0, which is at a higher latitude and has a less humid climate. At KIR0 the average monthly wet gradients are much smaller except during the summer months. Furthermore, the influence of the Icelandic low pressure in the winter is not as large as it

190 is at the other four stations. Another exception is seen in the ECMWF wet gradients for ONSA in Figure ??. They are larger in the summer when the wet refractivity is higher. This is also seen at the other stations, but at ONSA there is a tendency of a positive east gradient in the summer. The ONSA GPS station is located a few hundred metres from the coastline, see Figure ??, suggesting that the air on the average is more humid over land compared to over the sea. One possible cause could be the sea breeze that occurs during the summer (??). The issue of wet gradients is studied further using a higher temporal resolution and

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<sup>195</sup> comparisons with the WVR data in Section ??.



**Figure 9.** Monthly means of estimated gradients at the Onsala station for the period 2006–2016. The top graphs show the total gradients from ECMWF (left) and GPS (right). The graphs at the bottom show the ECMWF gradients when separated into the hydrostatic (left) and the wet gradient (right).

Table 5. Correlation coefficients for the total east and north gradients estimated from GPS data and compared to ECMWF data.

Station	Six hourly		D	aily	Monthly	
	East	North	East	North	East	North
Kiruna (KIR0)	0.55	0.53	0.76	0.75	0.77	0.82
Mårtsbo (MAR6)	0.58	0.51	0.75	0.72	0.83	0.80
Borås (SPT0)	0.58	0.58	0.74	0.74	0.88	0.85
Visby (VIS0)	0.55	0.56	0.71	0.75	0.84	0.81
Onsala (ONSA)	0.60	0.60	0.75	0.78	0.90	0.90

# 4.2 Comparing GPS and ECMWF gradients over different time scales at the five stations

We study the agreement, in terms of correlation coefficients, between the total GPS and ECMWF gradients from 5 GPS stations using data from 2006 to 2016. These are shown in Table **??**.

- The correlations seen in all cases confirm that a consistent atmospheric signal in terms of gradients is detected by the 200 GPS observations and ECMWF analyses. We note that the correlation coefficients increase for longer averaging time periods. Our interpretation is that by long term averaging we compare a larger fraction of the gradient that is caused by large scale temperature and pressure gradients. Unfortunately, the temporal resolution of 6 h in the ECMWF data is not sufficient to resolve neither rapid changes in the pressure related to moving weather systems nor many of the short lived small-scale gradients associated with the variability in the water vapour.
- Another result worth noting is that the two stations with the highest correlation coefficients, especially for the monthly averages, are ONSA and SPT0. The 95 % confidence interval is +0.03/-0.04 for the correlation coefficient of 0.90 obtained at station ONSA, based on 131 data points (12 months over 11 years). These two stations are the only ones that are equipped with microwave absorbing material below the antenna and above the metal plate used for the antenna mounting. This could reduce the impact from unwanted multipath effects. The phenomenon calls for further studies.
- The mean values and the standard deviations of the gradients, for the three different temporal resolutions, are presented in Tables ?? and ?? from GPS and ECMWF data, respectively. For the 6-hour temporal resolution the GPS gradients estimated at the same time epoch as the ECMWF gradients are included in the calculations. The daily and monthly values are averages using these 6-hour data. Comparing the two tables it is clear that the GPS gradients are larger by a factor of  $\approx 1.5$  and this factor is roughly the same for all sites. We note that the standard deviations (SD) obtained for the KIR0 station for 6 h and one
- 215 day are significantly smaller. This is likely a consequence of the lower humidity at the station. For monthly averages, however, all stations have comparable SD, indicating that at this level the hydrostatic gradient and other effects, e.g. signal multipath effects, become important. Variations in the electromagnetic environment that change the impact of the signal multipath at a station may be due to e.g. snow, rain, vegetation, and soil moisture.

Table 6. Mean values and standard deviations (SD) over the 11 years of estimated total gradients from GPS data for different temporal resolutions.

Station	ZW	$^{\prime}\mathrm{D}^{a}$	H			orizontal gradient				
			Mean <sup>b</sup>		Six hourly SD Da		Dail	y SD	Monthly SD	
	Mean	SD	East	North	East	North	East	North	East	North
	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)
Kiruna (KIR0)	62	36	-0.21	-0.14	0.47	0.47	0.32	0.31	0.13	0.13
Mårtsbo (MAR6)	88	46	-0.23	-0.13	0.55	0.58	0.37	0.36	0.14	0.15
Borås (SPT0)	87	45	-0.24	-0.12	0.56	0.49	0.38	0.38	0.16	0.17
Visby (VIS0)	88	47	-0.07	-0.23	0.60	0.56	0.40	0.37	0.16	0.13
Onsala (ONSA)	92	47	0.01	-0.20	0.59	0.55	0.41	0.38	0.18	0.15

<sup>a</sup> The Zenith Wet Delay (ZWD) is included to illustrate the amount of water vapour in the atmosphere above the station and its SD is based on the 6 h gradients.

<sup>b</sup> The mean gradient values are based on the 6 h gradients.

**Table 7.** Mean values and standard deviations (SD) over the 11 years of estimated total gradients from ECMWF data for different temporal resolutions.

Station	Horizontal gradient								
	Mean <sup>a</sup>		Six ho	Six hourly SD Da		y SD	Monthly SD		
	East	North	East	North	East	North	East	North	
	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	
Kiruna (KIR0)	0.00	-0.14	0.28	0.26	0.20	0.19	0.07	0.07	
Mårtsbo (MAR6)	-0.22	-0.13	0.38	0.34	0.25	0.23	0.08	0.09	
Borås (SPT0)	-0.00	-0.13	0.39	0.35	0.25	0.24	0.09	0.09	
Visby (VIS0)	-0.01	-0.14	0.42	0.37	0.26	0.25	0.08	0.08	
Onsala (ONSA)	0.03	-0.14	0.43	0.37	0.27	0.25	0.10	0.09	

<sup>*a*</sup> The mean gradient values are based on the 6 h gradients.

#### 4.3 Search for long term trends

- We expect that any long-term trends would be very small and therefore also difficult to detect because gradients in general are less than 1 mm and large values typically occur over time scales from minutes to a few hours. Examples of time series with a 6-hour and 15-minute temporal resolutions are seen in Figure ?? and in Subsection ??, respectively. An estimated gradient has a direction and from the time series we estimate trends for the east and the north gradients separately. Such trends would correspond to an atmospheric tilt above the station. Combining the east and the north gradients offers the possibility to also
- search for trends in the amplitude of the gradient at the station. A positive trend corresponds to a larger variability and may occur even if there is no trend neither in the east nor in the north components. The amplitude is by definition never negative, see Equation (??). A trend of larger east gradients can be balanced by a similar trend in larger west gradients, resulting in no net trend in the east gradient component, but a trend in the gradient amplitude.

We estimate the total gradient trends from GPS data. Wet gradient trends inferred from GPS can be calculated by subtracting the ECMWF hydrostatic gradients. All the estimated trends are indeed very small, typically well below 10  $\mu$ m/year. The highest value is  $-19 \mu$ m/year for the total gradient in the north direction at the SPT0 station.

For our 11-year long time series of gradients we obtain a typical formal 1-sigma uncertainty of 40  $\mu$ m/year by taking the short term temporal correlation of the deviations into account using the model presented by **?**. Given these circumstances it seems unlikely to detect any trends in gradients caused by the atmosphere unless there is a dramatic local effect of the weather

235 conditions at the site. Nevertheless, to study long time series of estimated gradients is motivated by the monitoring of the quality of the data from a GPS station. An example of hardware problems giving a large impact on the estimated gradients have been reported by **?**.

#### 5 Wet gradients at the Onsala site

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For the Onsala site we study total gradients from the two GPS stations and one VLBI station and wet gradients from the WVR

- 240 for the time period 2013–2016. We use the hydrostatic gradients from ECMWF to calculate wet gradients from GPS and VLBI total gradients. The designs of the two GPS stations are different, see Figure ??, which motivates to include both of them in the comparisons. Three different studies are made using these data: (1) assessment of the impact of using different processing of the GPS data, primarily varying the elevation cutoff angle, by comparison to the WVR gradients; (2) using the GPS gradients from the processing variant showing the best agreement with the WVR gradients, the seasonal variations in the wet gradient
- 245 are characterised; and (3) a 15-day long period with VLBI data is used as a case study for comparisons with GPS and WVR wet gradients and the ZWD.

#### 5.1 Test of GPS processing variants relative to WVR data

Gradients in the east and the north directions are estimated from the GPS data for five different solutions. We use three different elevation cutoff angles for the VMF1 zenith delay mapping functions. One additional solution is carried out with elevation dependent weighting  $(\sin(\varepsilon))$  and in the fifth solution the VMF1 mapping functions are replaced by the NMF. As stated earlier the gradient mapping function presented by **?** is used in all cases.

When we use the independent WVR wet gradients together with the total gradients estimated for ONSA and ONS1, the hydrostatic gradients from ECMWF (see Figure ??), linearly interpolated to match the time epochs of the GPS gradients, are subtracted from the estimated total GPS gradients. Thereafter, we form 15 min averages for the east and the north wet gradients from GPS and compare to the corresponding WVR results.

The results for the different GPS solutions are summarised in Tables ?? and ??. Because of the different gradient amplitudes from the WVR and GPS, we present mean values and SD of the differences as well as correlations coefficients. Table ?? shows the results when the total gradients from the stations ONSA and ONS1 are compared to each other. Table ?? shows the results when the wet gradients from ONSA and ONS1 are compared to the WVR gradients. We note that in both tables the best agreement between the gradients estimated is obtained for an elevation cutoff angle equal to 3°. The 95 % confidence interval

- for correlation coefficients around 0.65 and approximately 80,000 data pairs is ± 0.004. This confirms the results presented by
  ? using a GNSS station network in central Europe. This result was not expected by us, given that the WVR has an elevation cutoff angle of 20° (in order to avoid ground-noise pickup) the GPS solution using the same cutoff angle would show a better agreement. Our interpretation is that for the temporal resolutions of 5–15 min the low elevation observations are important
  in order to distinguish the gradient parameters relative to other estimated parameters in the GPS analysis. A higher elevation
- in order to distinguish the gradient parameters relative to other estimated parameters in the GPS analysis. A higher elevation cutoff angle will remove many observations towards the north, and especially for a cutoff angle of 20°, see Figure ?? and Table ?? with the formal errors.

The solution giving the best agreement, when comparing gradients from ONSA and ONS1 data with each other, is the one with elevation dependent weighting, whereas the comparisons with the WVR, for both ONSA and ONS1, give the best agreement without weighting. The choice of elevation cutoff angle is a compromise between having a good geometry and

Table 8. Assessment of the different GPS solutions comparing total gradients from the two GPS stations ONSA and ONS1.

GPS	Mean		Stan	dard	Correlation		
Solution	Differ	ence <sup>a</sup>	Devi	ation	Coef	Coefficient	
	East North		East	North	East	North	
	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	
VMF 3°	-0.01	0.03	0.22	0.25	0.91	0.87	
VMF $3^{\circ b}$	0.03	0.02	0.15	0.16	0.95	0.92	
NMF $3^{\circ}$	-0.01	0.05	0.23	0.26	0.91	0.86	
VMF $10^{\circ}$	0.02	0.04	0.25	0.27	0.91	0.88	
$VMF 20^{\circ}$	0.33	0.36	0.39	0.47	0.82	0.70	

 $^a$  The mean difference is ONS1–ONSA.

 $^{b}$  Elevation dependent weighting,  $\sin(\varepsilon)$ 

avoiding effects of signal multipath. Our interpretation is that the gradients from ONSA and ONS1 are estimated based on very similar observational directions and have common error sources, such as orbit errors, resulting in correlations around 0.9. In order to increase an already high correlation the observations at the lowest elevation angles are not that important, since multipath effects will be more and more different the closer to the horizon the observations are made. When ONSA and ONS1 gradients are compared to those from the WVR the situation is different, because these gradients are independent and the geometry of the GPS observations becomes more important in order to estimate a more accurate gradient. Although we note that the correlation is here reduced to around 0.6. Since the WVR provides independent gradients, we will in the following focus on the VMF 3° solution without elevation dependent weighting.

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**Table 9.** Assessment of the different GPS solutions for the wet gradients from the two GPS stations ONSA and ONS1 relative to the WVR data.

GPS	Mean $Difference^{a}$		Stan	Standard		Correlation	
Solution			Devi	ation	Coef	ficient	
	East	North	East	North	East	North	
	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	
ONSA							
VMF 3°	0.23	-0.07	0.64	0.57	0.68	0.64	
VMF $3^{\circ b}$	0.21	-0.06	0.71	0.62	0.58	0.55	
NMF 3°	0.22	-0.07	0.64	0.57	0.68	0.64	
VMF $10^{\circ}$	0.20	-0.10	0.65	0.59	0.66	0.62	
$VMF 20^{\circ}$	-0.02	-0.28	0.75	0.73	0.54	0.42	
ONS1							
VMF 3°	0.22	-0.04	0.64	0.58	0.68	0.64	
VMF $3^{\circ b}$	0.24	-0.02	0.71	0.63	0.58	0.55	
NMF $3^{\circ}$	0.21	-0.02	0.64	0.58	0.68	0.63	
VMF $10^{\circ}$	0.22	-0.04	0.66	0.59	0.66	0.62	
VMF $20^{\circ}$	0.36	0.15	0.79	0.73	0.49	0.42	

 $^{a}$  The mean difference is the offset referenced to the corresponding WVR time series.

 $^{b}$  Elevation dependent weighting,  $\sin(\varepsilon)$ 

#### 5.2 Wet gradients from GPS and WVR

larger scatter which implies larger gradient amplitudes.

- 280 An overview of the data in terms of monthly means of the wet gradient amplitude and the ZWD is presented in Figure ??. The GPS solution with a 3° elevation cutoff angle, no weighting, and the VMF1 mapping functions is used. When forming monthly means the correlations are obvious, both between GPS and WVR estimates, and between the variability, in terms of the SD, and the gradient amplitudes and the ZWD. Here we also note that the WVR gives much larger gradients. Factors that can cause a difference in gradient amplitude are:
- (1) The WVR is sensitive to liquid water in the atmosphere. This is a cause for positive systematic errors in the ZWD as well as occasional overestimates of gradient amplitudes. We investigated this possibility by deleting all WVR observations implying a liquid water content larger than 0.3 mm. The impact was however insignificant. The average gradient amplitude decreased by 0.01 mm. The reason being that large liquid contents are rather infrequent, given that already data acquired during rain (which was assumed to occur when liquid water content was larger than 0.7 mm) have been removed.
- (2) The WVR gradients for one 15-minute period do not depend on earlier or later estimates whereas the GPS gradients are estimated using constraints on the variability. A constraint has a similar impact as a low-pass filter. Peaks with a short duration, requiring rapid changes, will be reduced. This is a valid argument for the mean gradient amplitude, but not for the mean values of the individual east and north components, because they are expected to be very close to zero regardless of the value of the constraint.
- (3) The fact that the WVR and the GPS gradients are averaged over different air masses introduce effects that will have an impact on the estimated amplitude. The WVR cannot observe at elevation angles below 20°, due to the risk of picking up emission from the ground, but for the GPS gradients we have the possibility to study the gradient amplitudes for the different elevation cutoff angles presented in Subsection ??. Table ?? summarises these results for ONSA and ONS1 for the 4-year period 2013–2016. We identify two possible reasons for the increase in gradient amplitude with increasing elevation cutoff angle: (i) the larger volume sensed with a 3° cutoff angle will introduce an averaging effect that will reduce the estimated amplitude, similar to averaging over longer time periods, and (ii) the 20° cutoff angle results in larger formal errors and a

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We conclude that the constraints and the sampling of different air masses are the likely explanations for the differences in gradient amplitudes estimated from GPS and WVR data but cannot based on these results determine their relative importance. A correlation plot for the total gradients from ONSA and ONS1 for the VMF1 solution with a 3° elevation cutoff angle is shown in Figure **??**. As in the previous section we see a slightly higher correlation for the east gradients, possibly because of the poorer sampling on the sky north of the zenith direction due to the geometry of the GPS satellite constellation at this latitude (see Figure **??**).

The two GPS stations share several error sources, such as clock and orbit errors of the observed satellites, and the use of 310 the same mapping functions, meaning that the rather high correlation is overoptimistic due to a common mode suppression of errors.

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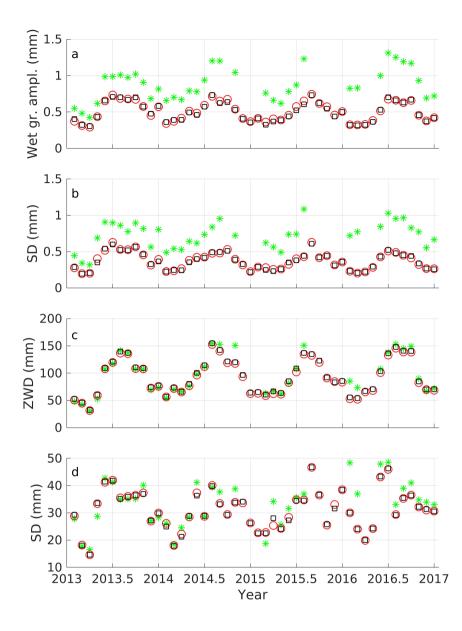
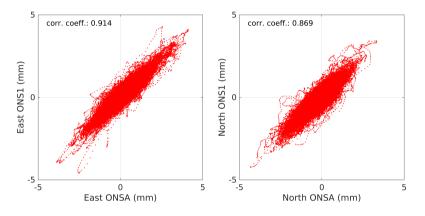


Figure 10. Time series of (a) monthly means of wet gradient amplitudes,  $\sqrt{\Xi_{e,wet}^2 + \Xi_{n,wet}^2}$ , (b) their SD, (c) monthly means of the ZWD, and (d) the ZWD SD from GPS and WVR. The green stars denote WVR data. The ONSA and ONS1 data are denoted by red circles and black squares, respectively.

Elev.	Mean value of gradient amplitudes					
cutoff	ONSA ONS1					
angle	(mm)	(mm)				
3°	0.51	0.50				
$10^{\circ}$	0.58	0.59				
$20^{\circ}$	0.75	0.70				

Table 10. The impact of the elevation cutoff angle on the estimated 15-minute GPS gradient amplitude



**Figure 11.** Correlations between estimated total gradients from the GPS stations ONSA and ONS1 using all data with a 5 min resolution from the period 2013–2016.

Correlation plots for the wet gradients from ONSA, ONS1, and the WVR are presented in Figure ??. As seen previously from total gradients the correlations between the estimated gradients from the two GPS stations are significantly higher compared to when the GPS gradients are correlated with the gradients from the WVR. It is also not surprising that the correlation between

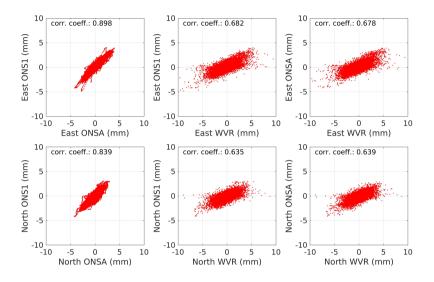
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the wet gradients from ONSA and ONS1 are slightly lower compared to the correlation between the total gradients (Figure ??). When subtracting the hydrostatic gradients, a common signal is removed and the dynamic range is reduced, which affects the correlation coefficients.

The reasons for the lower correlation coefficients between the WVR and the GPS gradients are almost identical with the reasons above why the WVR gradient amplitudes are higher: (1) they do not have common sources of errors; (2) the WVR 320 data suffer both from white noise and algorithm errors, especially when liquid water is present; (3) the WVR data for each 15-minute period are independent of the successive periods, whereas there are temporal constraints on the gradients estimated from the GPS data; (4) the sampling on the sky agrees also much better between the two GPS stations, assuming that in general

the directions of the observations are towards the same satellites, whereas the WVR observations are evenly spread over the sky and above an elevation angle of  $20^{\circ}$ .

325 Concerning the sampling of the atmosphere, the use of a multi-GNSS constellation has been shown to improve the agreement between GNSS gradients with those estimated from a WVR (?). In this context it should be noted that with many more GNSS observations the optimum elevation cutoff angle may not be as low as 3° because of an improved sampling of the atmosphere.



**Figure 12.** Correlations between estimated wet gradients from the WVR, ONSA and ONS1 using all data from the period 2013–2016. The data in the graphs with ONSA and ONS1 (left) have the original 5 min resolution, whereas the GPS data are averaged over 15 min when compared to the WVR data (middle and right). The correlation coefficients obtained when the east gradients from the WVR were correlated with the original total gradients from GPS were 0.633 for ONSA and 0.637 for ONS1. The corresponding values for the north gradients were 0.575 for WVR-ONSA and 0.571 for WVR-ONS1. This supports our assumption that the ECMWF hydrostatic gradients are reasonably accurate when carrying out a linear interpolation between the 6-hour samples.

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We investigated if an average of the wet gradients from both GPS stations, ONSA and ONS1, estimated at the same time epoch, will improve the agreement with the WVR. We see an overall small improvement. For the east gradient the individual correlation coefficients were improved from 0.678 (ONSA) and 0.682 (ONS1) to 0.698. The corresponding values for the north gradient were increased from 0.639 (ONSA) and 0.635 (ONS1) to 0.666. Our interpretation is that by averaging the GPS gradients from ONSA and ONS1 the stochastic noise is reduced.

Correlation plots are shown in Figure **??** for each month of the four years. A clear seasonal dependence is seen, because the variability in the wet refractivity is larger during the warmer time periods, resulting in larger gradients and a larger dynamic range. We note that during October 2014 there were problems with the WVR (see Figure **??**). During most of the days there is a significant data loss, likely due to rain, which could be the reason for the low correlation during this month. The other months

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with low correlations are March 2015 for both the east and the north component, and January and February 2016 for the north component. In all these cases there were no large gradients detected and this has an impact on the correlations. In Figure 8 of ? a correlation coefficient of 0.52 was reported for the months March–May, 2014, between GPS and WVR gradients. Here we

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show that the variability from month to month is large and therefore the choice of the time period for gradient comparison studies is a critical issue.

Comparing the results obtained for ONSA with those from ONS1 they are almost identical (in both Figures ?? and ??) meaning that in this case there is no obvious improvement from the absorbing material below the antenna on ONSA. This is different to the previous finding where ONSA and SPT0, with microwave absorbing material, showed a better agreement with

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ECMWF gradients compared to the KIR0, MAR6, and VIS0 stations. Our assumption is that the lack of a concrete pillar with a metal mounting plate just below the antenna on ONS1, or any other objects affecting the electromagnetic environment at the antenna, eliminates the need for an absorber (see Figure ??).

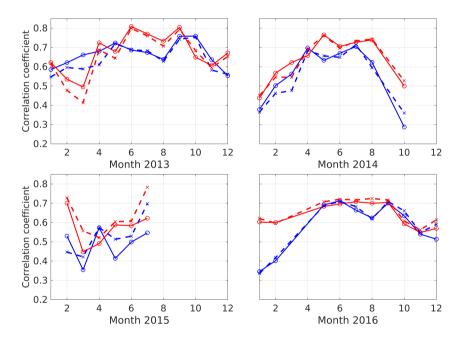


Figure 13. Correlations between estimated wet gradients from the WVR data and the GPS data from ONSA (solid lines) and ONS1 (dotted lines) averaged over 15 min when the hydrostatic gradients are removed from the total GPS gradients for each month of the four years. The east gradients are presented with red lines and the north gradients with blue lines.

#### 5.3 GPS, VLBI, and WVR wet gradients during CONT14

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The wet gradients from the two space geodetic techniques GPS and VLBI are compared to each other and to the WVR during the CONT14 campaign. Observations from several earlier CONT campaigns have been analysed in terms of gradients with different results depending on the station and the time of the campaign (?). We use this campaign as an example study of the short term variability of the wet gradients. The GPS gradients are those obtained from the VMF1 solution, unweighted, with a 3° elevation cutoff angle. The ECMWF data, see Figure ??, is only used to subtract the hydrostatic gradients from the total gradients estimated by VLBI and GPS. The time series are shown in Figure ??.

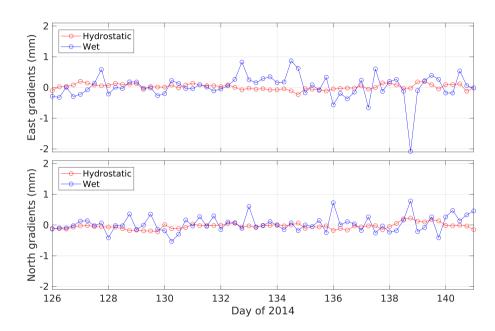
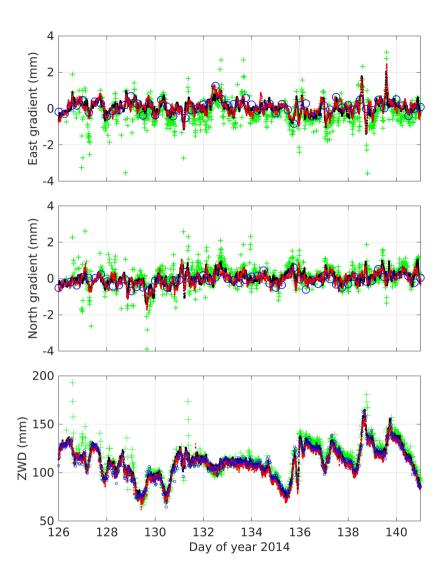


Figure 14. Time series of ECMWF hydrostatic and wet gradients during the CONT14 campaign.

- Again we note that the size of the WVR gradients is larger compared to all other instruments. The VLBI gradients correlate with the gradients from the other instruments but their amplitudes are smaller. Given that the sampling of the atmosphere is much more sparse with the VLBI telescope, a short lived gradient in combination with the assumption of linear functions in 6-hour segments, will probably reduce the variability in the estimated amplitude.
- Table ?? summarises the correlation coefficients for the east and the north VLBI wet gradients compared to those from the two GPS stations, ONSA and ONS1, and the WVR. Here we have correlated averages using data ±3 h around the VLBI gradient value every 6 h. In order to be consistent also the interpolated data from continuous VLBI segments are averaged in this way.

We note that the correlation coefficients are lower for the north component for all three comparisons, whereas the SDs are similar. The reason is that the size of the east gradients are larger compared to the north gradients during this 15-day period. Scatter plots (not shown) confirm what is indicated by the SDs, that the quality of the east and north components is similar.



**Figure 15.** The wet gradients and the ZWD during the VLBI CONT14 campaign 6–20 May (days 126–140). The temporal resolution for the VLBI (blue circles) gradients is 6 h and the ZWD 30 min, 5 min for the GPS gradients for ONSA (red dots) and ONS1 (black dots), and 15 min for the WVR (green plus).

We attribute the lower correlation coefficients obtained between VLBI-GPS and VLBI-WVR using 6 h averages during the CONT14 campaign compared to GPS-WVR 15 min averages for the month of May 2014 in Figure ?? to the sparse sequential

Table 11. Comparison of estimated wet gradients from VLBI relative to GPS and WVR data.

Reference	Mean		Stan	ndard	Correlation		
instrument	difference <sup>a</sup>		devi	deviation		coefficient	
	East	North	East	North	East	North	
	(mm)	(mm)	(mm)	(mm)	(mm)	(mm)	
ONSA	0.01	-0.03	0.22	0.20	0.71	0.57	
ONS1	0.03	-0.08	0.22	0.20	0.71	0.56	
WVR	0.30	-0.17	0.27	0.27	0.65	0.58	

 $^{a}\,$  The mean difference is VLBI- reference instrument.

sampling of the sky by the VLBI observations. On the other hand, averaging the WVR gradients over ±3 h reduces some of the noise seen in the 15 min values. The future use of the twin telescopes with faster slewing speeds at the site is likely to
improve this situation. During CONT14 there were approximately 360 useful observations at Onsala per day. We expect this to increase by a factor of 6–7 when using the new VLBI Geodetic Observing System (VGOS) (?), which means that the use of twin telescopes could result in 200 observations per hour. This in turn makes it possible to improve the temporal resolution of the estimated atmospheric gradients.

Finally, we like to use this 15-day long time series for a discussion on gradient variability. At the end of day 135, see the ZWD plot in Figure ??, more humid air is starting to enter over the site. We note a sudden decrease, followed by a rapid increase. In Figure ?? we zoom in on the gradients and the ZWD during this period. Here we have an example with wet gradients from GPS and WVR gradients when a warm front passage occurs in the evening of day 135. During this passage there is also a smaller drier air mass present causing a decrease followed by an increase in the ZWD. During this dip in ZWD the wind at the ground was from the west increasing from 7 m/s at 18 UT to 11 m/s at 24 UT. During the decrease in ZWD

380 we see a clear positive east gradient and during the following increase in ZWD the east gradient has a negative peak. Also during the first few hours of day 136 a decrease in the ZWD corresponds to positive values for the east gradient, and the wind continued to come from the west. This is as expected, but there are also variations in the north gradient during this period, consistently detected by the WVR and the GPS data, showing that the wind at the ground was not fully representative for all altitudes.

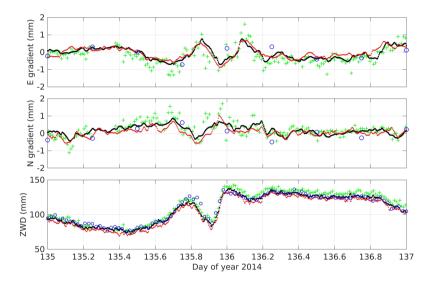


Figure 16. Zoom in on the time series in Figure ??. The symbols are as before: VLBI gradients (blue circles), GPS gradients for ONSA (red dots) and ONS1 (black dots), and WVR (green plus).

#### 385 6 Conclusions and suggestions for future work

We have estimated linear horizontal gradients from GPS data from five sites in Sweden. Averaging gradients in the east and the north direction over one month gives correlation coefficients of up to 0.9 when compared to gradients calculated from meteorological analyses of the ECMWF. Monthly averages of the gradients are dominated by the hydrostatic component.

No significant long-term trends were detected for the GPS gradients. If small gradient trends are detected in the future we 390 recommend to critically assess if they could be caused by station problems or confirmed by a nearby (or even collocated) station.

When studying gradients averaged over shorter time scales, e.g. 15 min, we find the wet component of the gradients to cause most of the variability. We confirm the result from **?**, that an elevation cutoff angle of  $3^{\circ}$  implies a better agreement when comparing GPS gradients with those from a WVR, in spite of the fact that the WVR does not observe the atmosphere below elevation angles of  $20^{\circ}$ . Related to this is that by using a  $3^{\circ}$  elevation cutoff angle in the GPS processing will decrease the amplitude of the GPS gradients by approximately 20 % compared to a  $20^{\circ}$  cutoff angle. We interpret this result as the combined impact of two possible causes: (1) the averaging of a larger air mass results in a similar decrease in gradient amplitudes as the averaging of gradients over longer time periods, and (2) the higher cutoff angle implies larger uncertainties and a larger scatter and thereby also an increase of the mean amplitude of the estimated gradients. The relative importance of these two effects are recommended to be studied further, e.g. by using simulations based on high resolution numerical weather models.

Correlation coefficients between wet gradients estimated from GPS and the WVR data can for specific months reach up to 0.8. Based on the four years of results we note a strong seasonal dependence, from 0.3 during months with smaller gradients to 0.8 during months with larger gradients, typically during the warmer, and more humid, part of the year. Related to this we suggest further studies of large wet gradients estimated from GPS, again in combination with meteorological high-resolution models for verification of the quality of the gradients.

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In general we also note slightly higher correlation coefficients for the GPS derived gradients in the east compared to the north direction. We interpret this difference to be caused by an inhomogeneous spatial sampling on the sky, which is important when we assume that the linear model describing horizontal gradients has deficiencies. The different sampling on the sky is an important issue for any comparison between different techniques. This question remains unresolved and is also recommended for further studies.

Additional issues that deserve attention in future studies, in addition to similar studies in different climates, e.g. the tropics, can include multi-GNSS observations. At latitudes similar to those in this study, the use of GNSS satellites with a higher orbit inclination will reduce the part of the sky not sampled by GPS.

For VLBI the use of VGOS (twin) telescopes will also dramatically improve the sampling of the atmosphere. When WVR
data are used to evaluate gradients from the space geodetic techniques one may consider to also apply different constraints for the temporal variability of these estimates.

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*Data availability.* The input GNSS data, in RINEX format, are available from EUREF, https://igs.bkg.bund.de/dataandproducts/browse. The input VLBI data are available from the IVS, ftp://ivs.bkg.bund.de/pub/vlbi/ivsdata/db/2014/. The ECMWF gradients are accessible from the Technical University of Vienna, http://vmf.geo.tuwien.ac.at/trop\_products/GNSS/LHG/. The estimated gradients from GPS, VLBI, and

420 WVR data have been registered and archived by the Swedish National Data Service (SND): doi:10.5878/nswt-yr39.

Author contributions. Gunnar Elgered coordinated and wrote the major part of the manuscript and together with Tong Ning planned the different GNSS data analyses during the COST Action ES1206. Tong Ning performed the GNSS data analyses, resulting in the estimated gradients. Peter Forkman and Rüdiger Haas carried out the same task for WVR and VLBI data, respectively. All authors contributed in the writing process, in particular to the sections presenting the results produced by each author and approved the entire manuscript before the submission.

Competing interests. The authors declare that they have no conflict of interest.

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