Reviewer 1 major comment: p6 l5, Eq 6: This is not the 2 of an optimal estimate because the constraint term is missing. Without the additional term (^x..xa)T S..1a (^x..xa) I think the expectation value will not be the number of degrees of freedom of the retrieval system (See Rodgers book Eq. 2.43).

Response: Thank you for pointing this out. As the reviewer notes, the (retrieved minus prior) contributes to the chi2 used for the goodness-of-fit in an optimal estimate. For oco-2 fits, there four "bands" contributing to the chi2, the O2A, the weak, the strong, and the state deviation from the prior. However, the purpose of Eq. 6, is to see how well each spectral band is fit for different categories. e.g. see Section 4.2 dP, where the spectral fit is checked for different surface pressure error ranges. This diagnostic was also renamed, "rad_chi^2" so as to avoid confusion with the chi2 used in the retrieval. This section was reworded to explain better the purpose of this diagnostic, "One useful diagnostic is an estimate of how well the modeled radiances match the observed radiances for each of the three OCO-2 spectral bands."

The same terminology was updeated in 2.3 (quality flags) and 4.2 (dP) to be consistent.

p1 l14: what about adding "... larger than predicted by linear error estimation,..."
Response: Updated as suggested.

p1 l25: shouldn't it read "was launched"
Response: Updated as suggested.

p2 l1: either "analysis follows" or "analyses follow"

Response: Wording changed to, "OCO-2 error analysis uses Rodgers (2000)..."

5 p3 l16:"...linearity of the retrieval system in the vicinity of the result..." Actually it is not assumed that the retrieval system is linear but that it is only moderately nonlinear (in Rodgers' language). That is to say, that the system behaves approximately linear in 1 around the result. Response: Thank you for noting this. Updating to "1) Linear estimates of errors, which assumes moderate linearity of the retrieval system"

10

p3 l18: I thought you talk about error estimation but here you talk about the retrieval. Please clarify. Perhaps"Error estimation based on retrievals using a..."?

Response: Updated 2), 3), and 4) as suggested, e.g. "2) Error estimates from non-linear retrievals of simulated radiances using a fast, simplified radiative transfer, called the surrogate

15 model (Hobbs et al., 2017)."

p4 l10 "...the a priori covariance matrix for CO_2 has the dimension..."

Response: Updated the wording as suggested.

20 p4 l12 I might have missed something but it is not clear to me what "aircraft variability" is. I am not sure if the term "error" is adequate in the context of a priori uncertainty.

Response: The variability of the aircraft is outside the scope of this paper. Wording updated to, "The larger variability near the surface allows more variability in the retrieved CO_2 profile near the surface."

25

2

p4 l14 I suggest to add the term "assumed" somewhere. Either"The assumed a priori errors" or, "are all assumed uncorrelated".

Response: Wording updated as suggested, to "The a priori errors for other parameters are all uncorrelated in the a priori covariance... "

p4 l35"Sainv" have you pasted a LaTeX macro into a word document here?

Response: It looks like the word file got mangled in transit between co-authors, and have updated many similar issues in the text.

p5 l 33 and throughout: I suggest to avoid these technical abbreviations like "CO2_grad_delta" in the text as far as possible and to use common language instead. If you do not want to use common language for these terms, then please replace the variable name of the computer code by a variable in mathematical notation.

Response: Updated this to a mathematical notation which I cannot paste into this text box, but first introduced near the end of the abstract.

p6 l1 this should read 2; there are numerous errors of this type. I do not mention each single one.

Response: This notation was updated in response to the major comment, above. The notation was also fixed.

p6 l5 try to avoid computer language type variable names, replace by mathematical notation.

Response: Updated to r, for radiance, in Eq. 6.

p7 l20 "errors due to physics that is perfectly described by the retrieval forward model" not quite clear what is meant. Please reword.

3

Response: This was worded confusingly. Updated wording to, "This error analysis ideally would use the exact same forward model in both the L1b simulations and the L2 retrieval algorithm, as our analysis assumes that Eq. 1 should be valid, without errors from forward model differences."

p11 l17. I do not think that the smoothing error describes the error introduced by the "imperfect sensitievity". Imperfect sensitivity will cause retrieval noise. The cause of the smoothing error is that xtrue != xa.

Response: I see how imperfect sensitivity results in noise which is not smoothing error. Updated wording to, "Smoothing error occurs when the averaging kernel deviates from the identity matrix..." both here and in the abstract.

p8 l19 should this read, "second moment"?

Response: Yes, thank you, updated.

Subsection headers 4.1 and 4.2: please avoid variable names in the subsection headers.

Response: Updated names to "The retrieved profile gradient" and "The retrieved surface pressure".

p14 l13: Not sure if abbreviation "LMT" has been defined. I might have missed the definition but please check.

Response: Yes they were defined earlier, but now are re-referenced Section 2.1 and the paper Kulawik et al. (2017) here.

p15 l9: There is something wrong after "...contribute."

4

5   p15 l22: I thought that the reduced 2 means 2 divided by the degrees of freedom. Isn't normalization with the related inverse covariance matrix inherent in the 2 by definition?

Response: This notation and definition was cleaned up when Eq. 6 was tidied. It is no longer called "reduced" but uses Eq. 6 directly.

10   Thank you to reviewer 2 for the helpful comments. We have responded to all comments (Author responses in blue).

Reviewer 2 responses:

15   1. Page 2, line 8: Typo or possible missing words in "finds that non-linear retrievals this relatively simple simulation".

Response: Added missing word, "However this study finds that non-linear retrievals using this relatively simple simulation..."

20   2. Page 2, line 21: Vague antecedent in "these simulated results", do "these" refer to Connor et al (2016) or the current work?

Response: It refers to the current work. Updated wording, "The linear analysis of Connor et al. (2016) does not explain the higher errors in this work, because the simulations in this work do not include unaccounted errors sources."

25

3. Page 2, lines 26-27, and elsewhere: Suggest making double quotes consistent throughout the document. Currently they're a mixture of "quotes" (preferred), "quotes" and "quotes".
Response: Changed all to "" quotes.

4. Page 3, line 7: Typo, "retrievel"
Response: Updated and did spell check throughout document.

5. Page 3, line 30: The claim that the performance of systems (3) and (4) were comparable is a strong one, since (4) includes a lot of complicating effects not in (3). It seems that the authors compared the two systems to arrive at this conclusion, the "preliminary studies" referred to here. I would like to see some sort of evidence from those studies, i.e., why do they think that the performances are comparable? This is not just idle curiosity; the authors themselves say that their error estimates are larger than earlier estimates by Hobbs et al (2017) using a surrogate model, which raises the question of whether choice (3) indeed is sufficient to capture most of the error sources.
Response: The initial runs using the more complicated system have been lost, and the statement that (3) and (4) are comparable is not supported by any analysis in this paper. This statement was made weaker, "...because preliminary studies seemed to find that the performance of systems (3) and (4) were comparable (results not shown)" Regardless of whether (3) and (4) are comparable, this paper uses system (3). This paper, using system (3) finds comparable errors to those found with the actual OCO-2 system, and a similar ratio of 2 between actual and predicted errors. We think that the fact that our errors are larger than Hobbs et al (2017) (which uses the surrogate model, indicates that the simplified radiative transfer used in Hobbs et al (2017) does not result in realistic errors.

6. Page 4, line 35: Typo, Sainv ! S..1a

Response: Updated this notation. Also, checked other equations for similar errors.

7. Page 5, equation (5), and page 12, equation (8): Typo, hxCOT 2 ! hT XCO2 or something like that, right now it looks like CO2 is the vector that's being transposed

Response: Agree this was mangled. Updated this here and one other location.

8. Page 6, lines 26-30: It was not clear to me whether the current work used the newer scheme (which picks the two most likely aerosol types per scene) or the older one.

Response: This work uses the scheme where the same 4 aerosols are always selected. Updated wording, "In the older L2 algorithm versions (pre B3.5), also used in this work... "

9. Page 7, lines 1-5: The authors downsample from 24 soundings per second to 1 sounding per second. While I understand this choice from the point of computational convenience, this has the potential for changing inter-sounding correlations, and whether errors average down over multiple soundings (e.g., the top part of page 11). Can the authors comment? Would the conclusions in the top half of page 11 still hold for real OCO2 retrievals?

Response: The measurement error, with this dataset, was random and reduced as 1/sqrt(N) in this study. The question as to whether it would average for denser data, likely it would. The caveat was weakened to "The simulated data does not have the data density of actual OCO-2 data so while averaging in close proximity would likely behave similarly, there is some uncertainty."

10. Page 7, lines 16-17: Why is a realistic cloud screener necessary for this work, given that coverage is not the focus of this investigation? Interfering errors from clouds are important, of course, but cloud screening to throw out soundings prior to retrieval should not affect the conclusions of this work, right?

Response: This work processes pre-generated simulated radiances consistently to how real data is processed. Part of the process is cloud screening, which is never 100% accurate, sometimes letting through cloudy cases and sometimes screening out clear cases. After retrievals, quality flags are applied, and can result in some true cloudy cases being flagged as good cases without clouds. So, it is important to test the end-to-end system, and not only give the system non-cloudy cases. Added text to better explain this to the reader. "It is important to test the system from end-to-end with radiances containing a variety of cloud conditions, because the cloud screening is never 100% accurate, sometimes letting through cloudy cases, and because quality flags can sometimes flag cloudy cases being as good quality without clouds. "

11. Page 7, line 26: Define "true" retrieval errors before this sentence. Currently it's defined on line 33.

Response: Updated wording to define exactly what we are comparing, "Our goal in this work is to compare linearly predicted vs. actual errors in XCO2..."

12. Page 8, lines 18-19: Do the biases in table 5 average down with the number of soundings? Or are they true biases that are independent of the number of sounding used to calculate them (with variations due to finite sample size)?

Response: Table 5 column heading was updated to "Mean bias". This is the bias over all the data and does not average away. A paragraph and figure were added to Section 2.4 to look at the spatial distribution of biases. The new paragraph is:

"Correlated biased errors are seen in real OCO-2 data, with correlations in time, e.g. ~60 days (Kulawik et al., 2019), at small spatial scales, e.g. < 1 degree (Worden et al., 2016), and at medium spatial scales, e.g. 5-10 degrees (Kulawik et al., 2019). Although this dataset cannot probe a seasonally dependent bias, as it covers only 1 day of observations, it can be used to

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probe spatial patterns of the biases. However, note that probing very small spatial patterns will be difficult to see because of the small amount of data processed in comparison to real OCO-2. A plot showing the spatial pattern of retrieved minus true is shown in Fig. 2 panel (a), which shows a high bias near the equator and a low bias near the poles. Panel (b) of Fig. 2 shows the difference between true XCO2 and XCO2 with the OCO-2 averaging kernel. The overall spatial pattern in panel (a) is not affected by the application of the averaging kernel, which makes sense because the averaging kernel effect is ~0.2 ppm whereas the differences are on the order of 0.9 ppm. An analysis of the correlation scale length of (retrieved minus true) XCO2 finds a correlated error of 0.3 ppm and full-width half-maximum in the bias of ~3 degrees, which is similar to the correlated error of 0.4 ppm and scale length of ~5-10 degrees found in Kulawik et al., 2019. The simulated data has accurate meteorology (temperature, winds, etc.) that drive the simulated true states, but the cloud and aerosol spatial structures are not very accurate, so that the spatial scales are not expected to be identical between this simulated dataset and real OCO-2 data. This analysis shows that correlated biases exist in simulated data, and that simulated data is useful for exploring the characteristics and even more importantly, the cause of regional biases."

13. Page 9: Define the linear estimate and how it's calculated before discussing it. For calculating the linear estimate from equation (1), are the Jacobians/averaging kernels evaluated at the prior state vector values or the posterior values from the nonlinear solution?

Response: The linear estimate was previously introduced in Section 2.1 but not referred back in the text on page 9. Text added in Section 2.1 to better introduce the linear estimate, "The linear estimate describes the response of the retrieval system to instrument errors and incorrect a priori inputs, based on the strengths of the Jacobians (representing sensitivity of the radiances to the retrieval state) and constraints (how much pressure is applied to parameters to stay near the a priori inputs). The linear estimate in Eq. 1 is used to estimate the errors, and for

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simulations, where we know all the inputs, it is useful to test each component of Eq 1." Page 9 now has the updated text, "To test the system linearity the linear estimate, using Eq. 1, and discussed in Section 2.1 is compared to the non-linear retrieval result. The inputs to Eq. 1 include the instrument noise (if on), a priori covariance, and Jacobians at the final retrieved state."

14. Page 9, line 9: Are the 1.3 and 1.0 ppm figures biases or standard deviations (random errors)?

Response: These are the single-observation errors. I updated to v8 error estimates from Kulawik et al., 2019 (in prep). The text was updated to, "For real OCO-2 v8 data, comparisons to TCCON for single-observation land nadir and ocean glint show errors (including both random and systematic errors) of 1.0 and 0.8 ppm, respectively (Kulawik et al., 2019), meaning that the real errors are comparable to these simulated data errors. Real OCO-2 data has location-dependent biases on the order of 0.5-0.6 ppm (Wunch et al., 2017; Kulawik et al., 2019)..."

15. Page 11, line 27: I'm surprised by the 0.0 ppm bias, is this because there are no clouds in the true state for this exercise?

Response: The 0.0 ppm is the mean bias. There is still a spatial pattern to the bias, listed as the standard deviation. The spatial pattern of true_ak minus true is also now shown in Fig. 2 and a discussion was added about the spatial distribution of biases in Section 2.4.

16. Page 12, lines 1-4: Seasonality of the effect of the averaging kernel is one reason for applying it to models, another is the possibility of spatial patterns. The data in this study do not span multiple seasons, but it does span multiple surface types, albedos, aerosol loading, etc., all of which influence the averaging kernel. Does the impact of applying the averaging kernel and prior have a spatial pattern? C3

Response: Yes, the analysis of the spatial pattern of the bias was previously lacking in the paper. The spatial pattern of the difference between the retrieved and true or retrieved and true with the averaging kernel applied were very similar. The application of the averaging kernel did not affect the spatial pattern. This makes sense because the AK application is a 0.2 ppm effect, and the systematic error is ~0.6 ppm (Kulawik et al., 2019). The analysis of the spatial pattern of the differences between retrieved and true, or true_ak and true was added to Section 2.4 as described above in the answer to #12.

17. Page 12, line 25: What does it mean that there is no predicted relationship but a strong correlation? Does it mean that the correlation is arising because both variables are impacted by some common element in the state vector?
Response: We have found that the CO_2 Jacobian strength varies with the retrieved water. If the retrieved water is not the true water it will result in the wrong strength CO_2 Jacobian. This will affect the retrieved CO_2 value but will not be predicted to have an effect. A sentence was added to this section, "This could be explained by the results from Section 3.1, showing that the XCO_2 Jacobian strength varies with the retrieved albedo or retrieved water, whereas the error analysis assumes that the Jacobian strength does not vary."

18. Page 13, line 1: Unresolved reference to "Eq xx".
Response: Fixed this, refers to Eq. 5.

19. Page 14, line 4: "gradient", not "curvature"
Response: Updated wording to gradient.

20. Page 16, paragraph 2: Here and elsewhere, it is not clear to me how a bias correction is done in this OSSE setup. For real OCO2 retrievals, the retrieved XCO_2 are compared to any of

a set of truth metrics, and linear relationships derived between the errors and co-retrived parameters. In the OSSE, what supplies the truth metric? Just the "true" state that is already known (because this is an OSSE)? In that case, is the bias correction formula applied derived specifically for this OSSE, or is the formula for real v7 retrievals used? It would seem to be more appropriate to use the former, but lines 8-9 here suggest that the latter was used. Why is that valid?

Response: This was not worded well. We calculated the bias correction for this simulated dataset. We compare the bias correction on this simulated dataset to the bias correction found in v7. We don't expect the exactly same relationships, but we would expect similarities, assuming that the biases are caused by the effects studied in this simulated dataset. Added wording in Section 4, "The bias correction is determined using this simulated dataset, and then applied to the same dataset, which is somewhat circular, since the true is both used to determine the bias correction and to check the bias correction, but it is important to know whether the relationships exist. For example, what causes the spatial patterns seen in the bias in Fig. 2. " Clarified the wording in section 4.2, "The bias found in this work for this simulated dataset for the XCO2 bias versus dP is -0.23 for land and 0.15 for ocean. We can compare these to the OCO-2 v7 biases of -0.3 for land and -0.08 for ocean. "

21. Page 16, lines 12-13: I did not know that the ACOS algorithm kept the number of O2 molecules fixed. How is this done, is it computed from the surface pressure and explicitly kept fixed? In that case, how does the surface pressure change during the retrieval? Purely due to water? And if so, is this change in water (which leads to dP 6= 0) consistent with the water column in the retrieval?

Response: This was not worded well. The ACOS algorithm keeps the O2 volume mixing ratio fixed not the number of O2 molecules. The retrieved surface pressure then affects the number

of molecules. Updated wording to, "Also note that the O2 volume mixing ratio (VMR) is fixed and not retrieved."

Validation of OCO-2 error analysis using simulated retrievals

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Abstract. Characterization of errors and sensitivity in remotely sensed observations of greenhouse gases is necessary for their use in estimating regional-scale fluxes. We analyze 15 orbits of simulated OCO-2 with the Atmospheric Carbon Observations from Space (ACOS) retrieval, which utilizes an optimal estimation approach, to compare predicted versus actual errors in the retrieved CO_2 state. We find that the non-linearity in the retrieval system results in XCO_2 errors of ~0.9 ppm. The predicted measurement error (resulting from radiance measurement error), about 0.2 ppm, is accurate, and an upper bound on the smoothing error (resulting when the averaging kernel deviates from the identity matrix~~from imperfect sensitivity~~) is not more than 0.3 ppm greater than predicted. However, the predicted XCO_2 interferent error (resulting from jointly retrieved parameters) is a factor of 4 larger than predicted. This results from some interferent parameter errors larger than predicted, as well as some interferent parameter errors more strongly correlated with XCO_2 error than predicted~~.~~ by linear error estimation. Variations in the magnitude of CO_2 Jacobians at different retrieved states, which vary similarly for the upper and lower partial columns, could explain the higher interferent errors. A related finding is that the error correlation within the CO_2 profiles is less negative than predicted, and that reducing the magnitude of the negative correlation between the upper and lower partial columns from -0.9 to -0.5 results in agreement between the predicted and actual XCO_2 error. We additionally study how the post-processing bias correction affects errors. The bias corrected results found in the operational OCO-2 Lite product consists of linear modification of XCO_2 based on specific retrieved values, such as the CO_2 grad ~~delta (del ($\delta\nabla_{CO2}$),~~ a measure of the change in the profile shape versus the prior~~;)~~ and dP~~.~~ ~~(~~the retrieved surface pressure minus the prior~~)~~. We find similar linear relationships between XCO_2 error and dP or ~~CO2_grad_delta,~~ $\delta\nabla_{CO2}$, but see a very complex pattern of errors throughout the entire state vector. Possibilities for mitigating biases are proposed, though additional study is needed.

1 Introduction

OCO-2 was launched in July 2014 and began providing science data in September, 2014, with the goal of estimating CO_2 with the "precision, resolution, and coverage needed to characterize sources and sinks of this important green-house gas." (Crisp et al., 2004). Validation of the ACOS/OCO-2 Build 7 (referred to hereafter as v7) data set (Eldering et al., 2017) versus measurements from the Total Carbon Column Network (TCCON) (Wunch et al., 2011) shows regional biases of about 0.5 ppm and standard deviations of 1.5 ppm (Wunch et al., 2017), though these errors are not entirely due to OCO-2 (TCCON and colocation errors also contribute). Biases are particularly concerning due to propagation of CO_2 biases into flux biases (Basu

et al., 2013; Chevallier et al., 2014; Feng et al., 2016). OCO-2 error analysis ~~follow~~uses Rodgers (2000) which gives a statistical estimate of errors using first-order analysis that assumes that the forward model is linear and estimates errors due to smoothing, radiance measurement error, and interferent species. The predicted XCO_2 errors for v7 OCO-2 are typically 0.4 ppm for ocean glint and 0.5 ppm for nadir land, which underestimate the actual errors by at least a factor of 2 (Wunch et al.,

5 2017). The cause of regional biases is thought to be underestimated interferent error or missing components of error analysis but is not well understood. Connor et al. (2016) found that missing physics in the forward model (e.g. more aerosol types; spectroscopy error; instrument error) leads to significantly larger posterior uncertainties than predicted by the current ACOS error analysis, using a purely linear error estimation framework. However, this study finds that non-linear retrievals using this relatively simple simulation system (e.g. no spectroscopic errors, no instrument noise, consistent aerosol types between the

10 true and retrieved states) also shows a similar relationship between predicted and actual errors, with the actual error about twice the predicted.

Cressie et al. (2016) estimates the size of second-order terms of the error analysis. The second order terms contain derivatives of the averaging kernel, gain matrix, and Jacobians with respect to state parameters. Cressie et al. (2016) estimates the errors

15 resulting from second-order error analysis are on the order of 0.2 ppm, but this analysis was dependent on the states and sizes of deviations used to calculate the second-order derivatives. Cressie et al. (2016) found that second order terms can cause both larger errors and biased results.

This paper explores the errors in the ~~""~~"full physics~~""~~" retrieval system using a simulated system with no mismatches in the

20 retrieval versus true state vector, and no spectroscopy or instrument errors. The actual errors covariance of (retrieved minus true) for this retrieval system are about twice the predicted errors. The linear analysis of Connor et al. (2016) does not explain the higher errors in this work, because ~~these simulated results~~the simulations in this work do not include unaccounted errors sources. Cressie et al. (2016) also does not explain the higher actual errors, because Cressie et al. (2016) estimates the second-order error as about 0.2 ppm, whereas the unaccounted error is about 0.8 ppm in this paper. In order to identify the source of

25 the unaccounted error, actual errors are ~~ompared~~compared to the predicted linear errors for a series of setups.

The ACOS Level 2 (L2) ~~""~~"full physics~~""~~" retrieval algorithm used to estimate XCO_2 from OCO-2 employs optimal estimation using 3 near infrared bands: (1) 0.76 μm containing significant O2 absorption ("O2 A-band"), (2) around 1.6 μm containing weak CO_2 absorption ("weak CO_2 band"), and (3) near 2.1 μm containing strong CO_2 absorption ("strong CO_2 band"). Prior

30 to the main retrieval, a series of fast pre-processing steps are performed for quality analysis (primarily to screen out clouds) and to provide estimates of chlorophyll fluorescence (Frankenberg, 2014). Only soundings that are deemed sufficiently clear are selected to be processed by the computationally expensive L2 retrieval. In the optimal estimation L2 retrieval used in this simulation, 45-46 retrieval parameters are ~~simulateously~~simultaneously estimated, including CO_2 volume mixing ratios

(VMR) at 20 pressures, albedos in 3 bands, 4 types of aerosols, meteorological parameters (temperature, water vapor, surface pressure), dispersion (frequency offset), wind speed (ocean only), and fluorescence (land only).

The retrieved CO_2 profile is then collapsed into a column, XCO_2. Recent work has alternatively partitioned the information into two partial columns (Kulawik et al., 2017). Post-processing quality screening and linear bias corrections based on various L2 retrieved parameters are then performed on XCO_2. The corrections are based on the slope of XCO_2 error versus different retrieved values, where the XCO_2 error is estimated from retrieved XCO_2 minus either (a) a constant value, in the southern hemisphere, "The Southern Hemisphere Approximation", (b) values from surface-based observations from TCCON stations, (c) the mean of small areas (less than 1 degree), or (d) a multi-model mean (Mandrake et al., 2015). We study the effects of the post-process bias correction in Section 4.3. The simulations in this paper differ from the operational ~~retrieval~~retrieval in that the fluorescence true state is set to zero, although fluorescence is still retrieved; and amplitudes of spectral residual patterns are not retrieved; except for these minor differences, these simulated retrievals are identical to the operational v7 retrievals. We refer the interested reader to O'Dell et al (2018) for a full description of the operational retrieval, including retrieved variables and bias correction.

Simulation studies can be used to understand and probe retrieval results. There are many different ways to assess errors, listed here in order of increasing complexity and non-linearity:

1) Linear estimates of errors, which assumes moderate linearity of the retrieval system (Connor et al., 2008; Connor et al., 2016), useful for surveying impacts of different errors with linear assumptions

2) ~~Retrievals~~Error estimates from non-linear retrievals of simulated radiances using a fast, simplified radiative transfer, called the surrogate model (Hobbs et al., 2017~~, which incorporates non-linearity, is very fast, but~~). This system does not result in the discrepancy of larger actual versus predicted error

3) ~~Retrievals~~Error estimates from non-linear retrievals of simulated ~~data~~radiances generated using the operational L2 forward model, called the "simplified true state", which has the advantage that the true state is within the span of the retrieval vector and the linear estimate should be valid

4) ~~Studies~~Error estimates from non-linear retrievals of simulated radiances using a more complex and accurate radiative transfer model to generate the observed radiances (e.g. Raman scattering, polarization handling, surface BRDF effects) and discrepancies between the true and retrieved state vectors (e.g. aerosol type mismatches between the true and retrieval state vector, albedo shape variations) (e.g. O'Dell et al., 2012).

This paper uses system (3), which makes it easier to interpret the actual versus expected performance of the retrieval system. System (3) was used because preliminary studies ~~found~~seemed to find that the performance of systems (3) and (4) were comparable~~.~~ (results not shown). Note that the observed radiance is generated with slightly different code than the retrieval system but they are matched as closely as possible.

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2 Retrieval system

2.1 Description of the OCO-2 L2 retrieval algorithm and error diagnostics

The ACOS optimal estimation approach is described in O'Dell et al. (2012, 2018) and Crisp et al. (2010). In this section we review the parameters in the retrieval vector and the equations for error estimates. The retrieved parameters for this simulation
5 study are shown in Table 1.

All non-CO_2 parameters are called interferents, and the propagation of errors from these parameters into CO_2 is called "interferent error".

10 The a priori ~~error~~covariance matrix for CO_2 ~~is a~~has the dimensions 20x20 ~~matrix~~, and has strong correlations as shown in Fig. 2 of O'Dell et al. (2012). The CO_2 a priori error ~~specifie~~is 48 ppm error at the surface, 12 ppm in the mid-Troposphere, and 1.4 ppm error in the stratosphere. ~~This is consistent with aircraft~~The larger variability~~, but biased towards~~ near the surface allows more variability~~;~~ in the retrieved CO_2 profile near the surface. However, in the ACOS retrieval, about 8% of the true mid-Tropospheric CO_2 variations are incorrectly attributed to surface variations based on the bias correction of
15 ~~CO2_grad_delta~~$\delta\nabla_{CO2}$ (Kulawik et al., 2017). The a priori errors for other parameters are all uncorrelated in the a priori covariance, and can be found in the L2 Product file.

The predicted errors, found in the OCO-2 L2 product as "~~xCO₂~~XCO$_2$_error_components", are based on the assumption that the non-linear, iterative retrievals can be represented as a linear estimate (Connor et al., 2008; Rodgers, 2000), and shown in
20 Eq. 1~~;~~.

$$\hat{\mathbf{v}} = \mathbf{v}_a + \mathbf{A}_{vv}(\mathbf{v}_{true} - \mathbf{v}_a) + \mathbf{A}_{ve}(\mathbf{e}_{true} - \mathbf{e}_a) + \mathbf{G}_v\boldsymbol{\varepsilon} \qquad\qquad (1)$$

where

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- $\hat{\mathbf{v}}$ is the retrieved CO_2 profile, size nCO_2 (20 for OCO-2). This variable is called "$\mathbf{u}$" in Connor et al., 2008, called "$\mathbf{v}$" here so as not to be confused with a different U variable introduced later.
- $\mathbf{v}_a$ is the a priori CO_2 profile, size nCO_2
- $\mathbf{v}_{true}$ is the true CO_2 profile, size nCO_2
- $\mathbf{A}_{vv}$ is the nCO_2 x nCO_2 CO_2 profile averaging kernel
30
- $\mathbf{A}_{ve}(\mathbf{e}_{true} - \mathbf{e}_a)$ is the cross-state error representing the propagation of error from non-CO_2 retrieved parameters, $\mathbf{e}$ (aerosols, albedo, etc.), into retrieved CO_2.
- $\mathbf{e}_a$ is the a priori interferent value, size n_{interf}. For this work, n_{interf} is 26(27) for ocean (land)
- $\mathbf{e}_{true}$ is the true interferent value, size n_{interf}
- $\mathbf{A}_{ve}$ is size nCO_2 x n_{interf}
35
- $\mathbf{G}_v$ is the gain matrix for CO_2, size nCO_2 x n_f, where n_f is the number of spectral points, and
- $\boldsymbol{\varepsilon}$ is the spectral error, also called measurement error, size n_f

The full gain matrix, $\mathbf{G}$, maps from spectral signals to retrieval parameter changes, and is:

$$\mathbf{G} = \cancel{(\mathbf{K^T S_\varepsilon^{-1} K + Sainv})^{-1}}(\mathbf{K^T} S_\varepsilon^{-1} \mathbf{K} + S_a^{-1})^{-1}\mathbf{K^T} S_\varepsilon^{-1}$$

(2)

5   where $\mathbf{K}$ is the Jacobian (or Kernel) matrix, and $\mathbf{S_\varepsilon}$ is the error covariance of the spectral error, ε. Note that $\mathbf{G}$ is size n x n_f, where $n = nCO_2 + n_{interf}$ is the total number of retrieved parameters. $\mathbf{K}$ is a matrix of derivatives giving the sensitivity of the radiance at each frequency to each retrieved parameter; e.g. for the CO_2 parameter at 800 hPa,

$$\mathbf{K} = \frac{dRadiance}{d(CO2\ @\ 800\ hPa)}$$

(3)

10

An assumption of the ACOS retrieval system is that the Jacobians are fairly invariant during the retrieval process, as is the ~~case in~~assumption for nearly all optimal estimation retrievals (see e.g. Rodgers, 2000).

The averaging kernel, $\mathbf{A}$, is one of the most fundamental and useful quantities in Bayesian inversion theory. It describes the
15   predicted linear dependence of the retrieved state on the true state and prior. The diagonal of the averaging kernel gives the degrees of freedom for signal for each retrieval parameter. The averaging kernel is calculated as:

$$\mathbf{A} = \mathbf{GK}$$

(4)

20   As will be shown in Section 3.1, we find that $\mathbf{K_{CO2}}$ varies depending on the retrieved state (indicating non-linearity), which would result in error in retrieved CO_2 that is not captured in the predicted errors.

The linear estimate describes the response of the retrieval system to instrument errors and incorrect a priori inputs, based on the strengths of the Jacobians (representing sensitivity of the radiances to the retrieval state) and constraints (how much
25   pressure is applied to parameters to stay near the a priori inputs). The linear estimate in Eq. 1 is used to estimate the errors, and for simulations, where we know all the inputs, it is useful to test each component of Eq 1.

After an inversion is complete, the pressure weighting function $\mathbf{h}$ (size nCO_2) is used to convert the retrieved CO_2 profile to XCO_2 by tracking the contribution from each level to the column quantity;

30

$$XCO_2 = \cancel{\mathbf{h_x CO_2^T}}\underline{\mathbf{h}_{XCO2}^T}\ \hat{\mathbf{v}}$$

(5)

The predicted errors on the estimated XCO_2 arise from 3 separate terms in Eq. 1;

18

1. $\mathbf{G_x}\boldsymbol{\varepsilon}$ results from the errors on the measured radiances (measurement error),
2. $\mathbf{A_{vv}}(\mathbf{v_{true}} - \mathbf{v_a})$ results from both imperfect sensitivity and constraint choices (smoothing error)
3. $\mathbf{A_{ve}}(\mathbf{e_{true}} - \mathbf{e_a})$ results from jointly retrieved species propagated into CO_2 (interferent error)

The CO_2 profile can also be partitioned into a lower and upper partial column (Kulawik et al., 2017). These can be calculated using equations similar to Eq. 5, with h set for the lower partial column air mass (LMT) by zeroing out the upper 15 levels, and h set for the upper partial column (U) by zeroing out the lower 5 levels. In this work, the lower and upper partial columns are explored to try to understand the reasons behind the underpredicted XCO_2 errors, and the effect of the ~~CO2_grad_delta~~$\delta\nabla_{CO2}$ component of the bias correction.

One ~~important~~useful diagnostic ~~to assess retrieval quality is the chi-squared statistic, χ^2,~~is an estimate of how well the modeled radiances match the observed radiances~~, defined~~ for each of the three OCO-2 spectral bands;

$$\chi^2 = \frac{1}{n_f}\sum_f((\text{rad\_fit}_f - \text{rad\_obs}_f)/\varepsilon_f)^2. \tag{6}$$

$$\chi_{rad}^2[band] = \frac{1}{n_f}\sum_f((\text{r}_{fit\ f} - \text{r}_{obs\ f})/\varepsilon_f)^2. \tag{6}$$

Where ~~rad_fit~~r_{fit} is the fit radiance, ~~rad_obs~~r_{obs} is the observed radiance, ε is the radiance error. ~~For OCO-2, χ^2 is calculated separately for each of the three OCO-2 spectral bands.~~

In reality, Eq. 1 would contain many additional error terms that are not considered in these simulations, e.g. spectroscopy, instrument characteristics, aerosol mismatch errors (i.e. picking the wrong aerosol type to retrieve). These are discussed in detail in Connor et al. (2016) as linear error estimates. The results reported here only address errors in the full non-linear retrieval system for the actual retrieved variables; it does not include errors from unincluded physics or other error sources (such as spectroscopy error). In the analysis presented in Section 3, each of the diagnostics given in Equations 1 through 5 will be used to examine the error estimates on the simulations and compared to previously published results on real OCO-2 data.

2.2 Description of the simulated dataset

The simulated data set analyzed in this study is comprised of a set of realistic retrievals using the ACOS b3.4 version of the retrieval algorithm. It is a slightly modified version of that described in detail in O'Dell et al. (2012) (which discussed b2.9), described more fully in O'Dell et al. (2018). Table 2 shows the most important changes to the L2 retrieval algorithm between b2.9 and b3.4.

Although newer versions of the OCO-2 L2 algorithm exist (currently b8 as of time of writing), the work presented here was initially begun prior to the launch of OCO-2 in July 2014. In addition, certain tests, where the L2 true state is directly related

to the retrieval vector, were simplified by using the older version of the retrieval algorithm which contains a less complicated aerosol scheme. In the older L2 algorithm versions (pre B3.5), also used in this work, the state vector for all soundings always included the same four aerosol types; cloud water, cloud ice, Kahn 1 (a mixture of course and fine mode dust aerosols) and Kahn 2 (carbonaceous mode aerosols) (described more in Nelson et al. (2016)). Both Kahn 1 and 2 types contain some sulfate

5 and sea salt aerosols as well. Newer versions of the OCO-2 L2 retrieval include a more complicated scheme in which each sounding includes water and ice, and picks the two most likely aerosol types based on a MERRA monthly climatology for the particular sounding location. The aerosol fits use a Gaussian-shaped vertical profile for each of the four types, as described in O'Dell et al. (2018).

10 Inputs to the b3.4 L2 retrieval algorithm include simulated L1b radiances and meteorology (taken from ECMWF) that were generated using the CSU/CIRA simulator (O'Brien et al., 2009). The simulator is driven by satellite two-line-elements which are used to provide the satellite time and position. The code calculates relevant solar and viewing geometry and polarization, and takes surface properties from MODIS. Only a single day's worth of orbits (15 orbits on 17 June 2012) at reduced temporal sampling (1Hz instead of the operational 3Hz) and with only 1 footprint per frame (instead of the operational 8) are presented

15 in this work. This yields approximately 2700 soundings per orbit, totaling about 40,000 soundings. Unlike real OCO-2 viewing modes (see Crisp et al. (2017)), the simulations were generated with nadir viewing over land and glint viewing over water. Therefore, no nadir-water, glint-land or target mode simulations exist as are found in real OCO-2 data. The spectral error for these simulations assumes Gaussian random noise, following the OCO-2 noise parameterization as described in Rosenberg et al. (2017).

20

Although the simulations do include realistic clouds and aerosols from a CALIPSO/CALIOP (Winker et al., 2010) monthly climatology, the radiative transfer portion of the simulator code allows clouds and aerosols to be switched off, making it easy to generate clear-sky radiances used in this research. The OCO-2 instrument model, described in detail in (Connor et al., 2009), was used to add realistic instrument noise to the radiances prior to running the L2 retrieval for the noise-less simulations. The

25 operational OCO-2 dispersion and ILS values, as well as its polarization sensitivity, were used to sample the top of atmosphere radiances. The same solar model as used in the operational retrieval was used in the L1b simulations. In addition, the A-Band Preprocessor code described in Taylor et al. (2016) was run on the cloudy-sky L1b simulations to provide realistic cloud screening prior to running the L2 retrieval. It is important to test the system from end-to-end with radiances containing a variety of cloud conditions, because the cloud screening is never 100% accurate, sometimes letting through cloudy cases, and

30 because quality flags can sometimes flag cloudy cases being as good quality without clouds.

This error analysis study ideally would use the exact same forward model in both the L1b simulations and the L2 retrieval algorithm, as our goal is not to studyanalysis assumes that Eq. 1 should be valid, without errors from imperfect forward model physics, but rather errors due to physics that is perfectly described by the retrieval forward model.differences. However, in

20

reality these two code bases are very similar but not identical. For example, the number of vertical levels within the two code bases differ. Reasonable attempts were made to put the L1b simulations on the same footing with the L2 forward model, but minor model mismatches may remain. We do not believe these minor differences affect our primary results.

5   Our goal in this work is to compare linearly predicted vs. ~~true retrieval~~actual errors in XCO$_2$, specifically in terms of three primary contributions to retrieval error discussed above: measurement, smoothing, and interferent error. Several different configurations were used to allow the estimation of the true error for each of these error components, as shown in Table 3. The "clear results" have no clouds or aerosols in the true state, however the retrieval is free to insert clouds into the retrieved state (and given that aerosols are retrieved as ln (AOD~.~), the retrieved states is never fully aerosol-free).

10

Results from different configurations are intercompared to validate the individual measurement, smoothing, and retrieval errors. These predicted errors are compared to the "true" errors resulting from nonlinear retrievals, which are the retrieved minus true values.

2.3 Post-processing quality screening

15   Similar to retrievals from real observations, the simulated retrieval results need screening to remove cloudy scenes (e.g. see O Brien, 2016; Polonsky et al., 2014). Because pre-screening is not perfect, the XCO$_2$ estimates from some soundings are of low quality, even if they converge. Post-processing screening is handled through calculation of quality flags, taken from Table 5 of Polonsky et al. (2014). These flags are (a) ~~χ^2~~χ_{rad}^2 (defined in Eq. 6) <2 for cases with measurement error, or ~~χ^2~~ ~~<~~$\chi_{rad}^2 \leq 1$ for cases with no measurement error, (b) retrieved aerosol optical depth <0.2, and (c) degrees of freedom > 1.6

20   (degrees of freedom are defined near Eq. 4). The 3 bands are averaged to calculate the ~~χ^2~~χ_{rad}^2 for the scene.

Table 4 shows the effects of applying post-processing quality screening for the different configurations from Table 3. The results are separated into land and ocean scenes; approximately 1/3 pass post-processing quality screening for cloudy cases; about 80% pass post-processing quality screening for cloud-free cases. For cloudy cases, 11% and 28% of cases passing pre-

25   screening for ocean and land, respectively, and 25% and 43% of cases passing post-screening for ocean and land, respectively. These are low compared to OCO-3 simulation studies (Eldering et al., 2018), where 25-30% of cases passed pre-screening, and 50-70% of cases passed post-screening. Some of the quality flags used for the OCO-3 studies (particularly the pre-processing flags) are not available in our study so it is hard to directly compare throughput. The lower throughput suggests that the cloud cases or other aspects of this study were harder than the OCO-3 simulation studies.

30   **2.4 Comparisons of retrieved values to true**

Table 5 shows XCO$_2$ biases and errors for the different configurations from Table 3. The quantities calculated for Table 5 are the bias (the mean retrieved minus true values) and standard deviation (the square root of the second moment of the retrieved

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minus true difference). These quantities indicate the overall quality of the results for each configuration. The results in Table 5 are sorted by standard deviation. The worst result by far is the cloudy case with no post-processing screening. This has ~10 ppb error for land and ~3 ppm error for ocean. Ocean generally does better than land; post-processing screening generally does better than no screening; and clear cases do better than cloudy cases. The addition of measurement error has a negligible
5 effect on standard deviation for this testing. The bold entry in Table 5 represents the most realistic "real-life" case (+measurement error, +clouds, +post-processing screening). This has 0.8 ppm standard deviation for land and 0.7 ppm standard deviation for ocean.

In the ~~post-processing~~ screened data, the main concern is the -0.5 ppm bias in the clear land retrieval. We have seen this in
10 other sets of simulations and it is an unresolved issue at this time. Recently we did find a minor bug in the simulator code that caused a small mismatch between the water vapor profile used to calculate the L1b radiances and that written to the meteorology file that is then used in the L2 retrieval. It is possible that other minor bugs of this nature are driving the clear-sky bias, with errors mitigated by clouds in the cloudy cases.

15 Figure 1 shows a scatter plot of the retrieved versus true XCO$_2$ (both with the ~~apriori~~a priori subtracted). The lower panels in Figure 1 show the histogram of differences, which range from about -1.25 to +1.5 ppm for land and -1.5 to +2 ppm for water soundings. Bias correction, discussed in Section 4.3, further improves the land results by 0.1 ppm in the bias and standard deviation as seen in Table 5, but does not improve ocean results. The standard deviation of (retrieved – true) (green dashed line) and (retrieved – linear estimate) (blue dashed line) are very similar; the linear estimate does not estimate the results any
20 better than 0.7 to 0.9 ppm, and gives an estimate of the nonlinearity.

For real OCO-2 ~~v7~~v8 data, comparisons to TCCON for single-observation land nadir and ocean glint ~~show~~have errors of 1.~~3~~0 and ~~1.~~0.8 ppm, respectively (Kulawik et al., ~~2017~~2019), meaning that the real errors are ~~0.3-0.4 ppm larger than in~~ comparable to these simulated data~~, i.e., approximately 30 to 40% larger.~~. Real OCO-2 data has ~~location-dependent biases~~systematic error
25 on the order of 0.5~~-~~0.6 ppm (Wunch et al., ~~2017), compared to the much lower overall bias of 0.1-0.2 ppm~~2017; Kulawik et al., 2019). Correlated biased errors are seen in real OCO-2 data, with correlations in time, e.g. ~60 days (Kulawik et al., 2019), at small spatial scales, e.g. < 1 degree (Worden et al., 2016), and at medium spatial scales, e.g. 5-10 degrees (Kulawik et al., 2019). Although this ~~simulated~~ dataset~~. However, a location-dependent or~~ cannot probe a seasonally dependent bias ~~would be hard to probe with this simulated dataset, which~~, as it covers only 1 day of observations, it can be used to probe spatial patterns
30 of the biases. However, note that probing very small spatial patterns will be difficult to see because of the small amount of data processed in comparison to real OCO-2. A plot showing the spatial pattern of retrieved minus true is shown in Fig. 2 panel (a), which shows a high bias near the equator and a low bias near the poles. Panel (b) of Fig. 2 shows the difference between true XCO2 and XCO2 with the OCO-2 averaging kernel. The overall spatial pattern in panel (a) is not affected by the application of the averaging kernel, which makes sense because the averaging kernel effect is ~0.2 ppm whereas the

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differences are on the order of 0.9 ppm. An analysis of the correlation scale length of (retrieved minus true) XCO2 finds a correlated error of 0.3 ppm and full-width half-maximum in the bias of ~3 degrees, which is similar to the correlated error of 0.4 ppm and scale length of ~5-10 degrees found in Kulawik et al., 2019. The simulated data has accurate meteorology (temperature, winds, etc.) that drive the simulated true states, but the cloud and aerosol spatial structures are not very accurate, so that the spatial scales are not expected to be identical between this simulated dataset and real OCO-2 data. This analysis shows that correlated biases exist in simulated data, and that simulated data is useful for exploring the characteristics and even more importantly, the cause of regional biases.

3 Validation of errors and non-linearity

In this section the different error components that were introduced in Section 2.1 are isolated as much as possible to evaluate each one separately. The Averaging Kernel and Jacobians, introduced in Section 2.1 are used as diagnostics. In addition, the linearity, or lack thereof, of the system is explored.

3.1 System linearity

To test the system linearity, Eq. 1, the linear estimate, using Eq. 1, and discussed in Section 2.1 is compared to the non-linear retrieval result. The inputs to Eq. 1 include the instrument noise (if on), a priori covariance, and Jacobians at the final retrieved state. Table 6 shows the results for cases passing post-processing quality screening, clouds, and no measurement error (Table 3, case d) using 1) the first two terms on the right side of Eq. 1 (i.e. only the CO_2 part of the Averaging Kernel) or 2) all of Eq. 1 (i.e. utilizing the interferent terms). The last term of Eq. 1 is not used for the noise-free case. The bottom entry in Table 6, showing retrieved vs. true XCO_2 (without averaging kernel applied). The comparison of retrieved XCO_2 versus the linear estimate have biases between 0.2 ppm and 0.9 ppm and standard deviation between 0.6 and 0.9 ppm. The bias is worse if the full averaging kernel is used. Looking through parameter by parameter, the band 3 albedo average causes most of the large bias for the full averaging kernel for ocean. The difference between the linear estimate and the non-linear retrieval is an estimate of the non-linear error in the retrieval system.

Another way to test of the system linearity is to look at the consistency of the sensitivity of the system to changes in XCO_2, i.e., how constant are the XCO_2 Jacobians (defined in Eq. 3)? For example, consider if the XCO_2 Jacobian weakens when an interferent, e.g. call it interferent #1, increases. If interferent #1 is larger than its true value, the XCO_2 Jacobian will be weaker than the true XCO_2 Jacobian. If the XCO_2 Jacobian is weaker than the true Jacobian, then more XCO_2 is needed to account for the radiance differences observed, resulting in a positive bias in XCO_2. This would result in a positive correlation in the errors of interferent #1 and XCO_2. This error correlation would not be predicted by the linear error analysis because the linear error analysis assumes that the Jacobians do not vary. This could explain the stronger error correlations seen

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To calculate an error resulting from varying Jacobians requires calculating second order terms, like dJacobian[XCO_2]/d[H2O scaling]. Cressie et al. (2016) calculated non-linear errors, using second order error analysis, and found errors on the order of 0.2 ppm, which would not fully explain the discrepancy between the predicted and true errors either in the simulation studies or real data.

5

Figure 23 shows the Jacobian magnitude (the XCO_2 Jacobian averaged over all frequencies) for XCO_2 versus retrieved "Band 2 albedo slope". The Jacobian for the lower (LMT) and upper (U) partial columns (described in Kulawik et al., 2017 and Section 2.1) are also plotted, and both partial columns vary the same way, e.g. same slope signs, i.e. the nonlinear interferent error would be positively correlated between the two partial columns.

10

The right panel of Figure 23 compares the Jacobian magnitude between matched results from configuration (c) and (d), in Table 3 for land cases with post-processing screening. The CO_2 Jacobian magnitude difference is up to -4% different for case (c) minus (d), and is correlated with the difference in retrieved "H2O Scaling" with correlation -0.75. Other parameters that had strong correlations (> 0.4) are: aerosol water pressure (0.55), aerosol ice pressure (0.43), surface pressure (0.41). Mapping
15 this correlation to an error in retrieved XCO_2 would require the calculation of second order Jacobians as in Cressie et al. (2016), and then mapping this into an error in XCO_2. A crude way to estimate the XCO_2 error resulting from these Jacobian differences is to consider the completely linear case, where radiance = K multiplied by XCO_2. In this case, a +1% error in the Jacobian would result in a -1% error in XCO_2, to fit the radiance. So, the variations in the XCO_2 Jacobians that are seen could explain the 0.8 ppm XCO_2 differences from the linear estimate.

20 **3.2 Measurement error**

To validate the measurement error, results from runs with and without noise (cases (c) and (b) from Table 3) are analyzed. The standard deviation of the XCO_2 difference between the runs ("true error") was compared to the predicted measurement error. The two runs, which both have clouds and other interferents, as well as smoothing errors, are assumed to be identical other than one having measurement error added. The runs are compared after quality screening, which was described in Section 2.4.

25

Figure 34 shows the baseline and predicted measurement error. For land nadir, the average error is 0.35 ppm and the average predicted is 0.29 ppm. For ocean glint, the average error is 0.14 ppm and the average predicted error is 0.21 ppm. The bias difference between the runs with and without noise was 0.01 ppm for ocean and 0.03 ppm for land nadir.

30 The predicted error ranged from 0.14 to 0.70 ppm for land and 0.12 to 0.35 ppm for ocean. The correlation between the predicted error and the absolute value of the error is 0.27 for land and 0.08 for ocean, so the scene-to-scene variations in the predicted error are not very useful.

24

~~The errors for averaged~~Adjacent observations are averaged, and then the error of this averaged quantity is calculated ~~using averaged adjacent observations.~~. If the error ~~for averaged observations~~ reduces with the square root of the number of observations averaged, then the error is a random, not correlated, error. Random error is highly desirable for assimilation and other uses. For land nadir the error is shown in Table 7

If the error is random, then the n = 9 result should be one third the error for the n = 1 result, and this is what is found. Similarly for ocean, the error for n=9 is 1/3 of the n=1 error. The simulated data does not have the data density of actual OCO-2 data so ~~that it is hard to say whether~~while averaging in close proximity would likely behave similarly, there is some uncertainty.

In summary, for these simulated cases, the measurement error is overpredicted for land by 0.06 ppm, and overpredicted for ocean by 0.07 ppm, but the measurement error appears to average randomly and does not introduce a bias.

3.3 Smoothing error

Smoothing error ~~represents the error introduced by imperfect sensitivity~~occurs when the averaging kernel deviates from the identity matrix, and is calculated using the averaging kernel, the true state and the prior state. The smoothing error terms from Eq. 1 are:

$$\mathbf{v}_{true\_ak} = \mathbf{v}_a + \mathbf{A}_{xx}(\mathbf{v}_{true} - \mathbf{v}_a) \qquad (7)$$

Here, $\mathbf{v}$ represents the CO_2 profile, which is converted to XCO_2 using Eq. 5. To validate the smoothing error, the non-linear ~~retrieval~~retrieved XCO_2 is compared to the linear estimate, ~~called v_(true_ak),~~$(XCO_2)_{true\_ak} = \mathbf{h}_{XCO_2}^T \mathbf{v}_{true\_ak}$, from Eq. 7, and to ~~the true.~~$XCO_2{}_{true} = \mathbf{h}_{XCO_2}^T \mathbf{v}_{true}$. The linear estimate should compare better to the non-linear retrieval. Run (a) from Table 3 is used, which does not contain clouds in the true state (i.e., limited interferent error), and does not have measurement error in the observed radiances.

The predicted smoothing error is 0.12 ppm for ocean glint and 0.16 ppm for land nadir. Comparison between retrieved XCO_2 and true has a mean bias of 0.0 ppm ~~bias~~ for ocean and a mean bias of 0.46 ~~bias~~ for land (retrieved XCO_2 is 0.46 ppm lower than true). The standard deviation is 0.33 ppm for land and 0.35 ppm for ocean.

Comparison of the retrieved XCO_2 versus ~~[XCO₂] true~~$(XCO_2)_{true\_ak}$ or ~~[XCO₂] (true_ak) (true state with OCO-2 averaging kernel applied)~~$(XCO_2)_{true}$ yielded the same biases and standard deviations (within 0.02 ppm). Therefore, the use of the OCO-2 averaging kernel and prior for comparisons, using Eq. 7, does not improve the comparison quality versus OCO-2. This analysis suggests modelers would do similarly to directly compare to OCO-2 versus applying the OCO-2 averaging kernel

25

and prior to the model before comparing to OCO-2. However, a previous study by Wunch et al. (2011) found that for comparisons to TCCON, if the averaging kernel is not applied, it leads to 0.2 ppm seasonal biases. The current analysis shows that it does not do harm to apply Eq. 7, but that it does not help either, with the caveat that the simulated data does not cover different seasons.

3.4 Interferent error

Previous studies by Merrelli et al. (2015), and O'Brien et al., (2016) have found that clouds and aerosols can contribute errors larger than predicted. We look at the relationship between errors in retrieved interferents versus errors in XCO_2 and the prediction of the relationship as characterized by the averaging kernel.

The error in XCO_2 from the interferent term of Eq. 1, multiplied by the pressure weighting function, $\mathbf{h}$, estimates the propagation of interferent error into XCO_2, shown in Eq. 8.

$$XCO_2 \text{ interferent error} = \mathbf{h}_{XCO2}^{\mathrm{T}} \mathbf{A}_{xv}(\mathbf{v}_a - \mathbf{v}_{true}) \tag{8}$$

This equation predicts that the interferent will only have an impact if the prior is different than the true, and that the impact will be proportional to the prior minus true difference, with the constant of proportionality provided by the off-diagonal averaging kernel, ~~A_xv.~~ $\mathbf{A}_{xv}$. Many of the interferents, e.g. H2O Scaling, ~~parameters~~ start at their true values for this simulation, and are predicted to have no impact on XCO_2. Yet, large correlations in errors are seen, when comparing XCO_2 error versus interferent error. Taking the expected standard deviation of XCO_2 interferent error from Eq. 8 gives the predicted interferent error, which averages 0.2 ppm for case (b) from Table 3.

We look at (retrieved minus true XCO_2) versus (prior minus true interferent) or (retrieved minus true interferent) in Fig. 4~~5~~, using run (b) from Table 3, which has clouds but no measurement error. The red line shows ~~$\mathbf{h}_{XCO2}^{\mathrm{T}}$ A xv (v a v true)~~, $\mathbf{A}_{xv}(\mathbf{v}_a - \mathbf{v}_{true})$, the predicted relationship between the XCO_2 error and the prior minus true difference. For both "band 2 albedo slope", left, and "H2O scaling", right, there is no predicted relationship but a strong correlation is seen. This could be explained by the results from Section 3.1, showing that the XCO_2 Jacobian strength varies with the retrieved albedo or retrieved water, whereas the error analysis assumes that the Jacobian strength does not vary.

Figure 5~~6~~ shows the predicted versus true errors, including correlations. The true error is calculated from ~~Eij =mean((retrieved minus true)i * (retrieved minus true)j)~~ $\text{Error}_{ij} = mean((retrieved - true)_i (retrieved - true)_j)$ for all cases ~~that pass post-processing~~with good quality. The true errors are much larger and show more correlations than predicted. Both matrices are normalized using the equation ~~Eij = Eij / sqrt(E0ii*E0jj),~~ $\text{Error}_{ij} = \text{Error}_{ij}/\sqrt{\text{Error0}_{ii} * \text{Error0}_{jj}}$, where ~~E~~$\text{Error}$ is

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the error covariance of interest and ~~E0~~Error0 is the predicted error covariance. To further analyze the interferent error, we looked at the diagonal terms of the error covariance and the correlations to XCO_2 in Table 8. In order for the error correlations between XCO_2 and interferents to be assessed, the CO_2 profile is mapped to XCO_2 using ~~the pressure weighting function as given in Eq xx.~~ Eq 5. Table 8 shows the predicted and true errors for all interferents, for all good quality land cases. The error factor (EF) is calculated as:

$$EF = \sqrt{(\sigma_{true}{}^2 + \text{bias}_{true}{}^2)/\sigma_{predicted}{}^2} \qquad (9)$$

where the predicted standard deviations come from the predicted errors and the ~~"~~"true~~"~~" standard deviation and bias come from the true errors. The error factor is found to be greater than 1 for almost all parameters.

Another useful diagnostic of interferent error is the predicted error correlation between each interferent and XCO_2, calculated by:

$$Correlation_{ij} = \sim error_{ij}/\sqrt{error_{ii} * error_{jj}} Error_{ij}/\sqrt{Error_{ii} * Error_{jj}}$$

$$(10)$$

which can be compared to the actual error correlation. Table 8 shows that for most interferents both the errors and the correlations are underpredicted. The parameters that are both underpredicted and significantly correlated (>0.25) to XCO_2 errors are shown in bold.

The true effect of interferent error on XCO_2 can be crudely estimated by the actual slope of XCO_2 error (not shown in Table 8, but, the actual slope shown in Fig. ~~4~~5) multiplied by the interferent error. This estimate cannot distinguish between correlation and causation. The standard deviation of this estimate is shown as the last column of Table 8. "Impact on XCO_2". The interferent error estimated with a more simplified "surrogate" model was much smaller in Hobbs et al. (2017)

4 Post processing bias corrections

Post-processing analysis of real ACOS OCO-2 retrieval results has uncovered linear relationships between XCO_2 error and various parameters such as the retrieved surface pressure, liquid water optical depth, and ~~$CO_2\_grad\_del$~~$\delta\nabla_{CO2}$ (an estimate of the profile curvature) (Wunch et al., 2011). Similar correlations have been found between the above parameters and the lower partial column (Kulawik et al., 2017). The standard operational procedure that has been adopted by the ACOS algorithm team for both OCO-2 and GOSAT data is to perform a bias correction of the estimated XCO_2 based on the linear correlations of the difference in XCO_2 compared to various truth metrics with certain retrieved parameters. In this section, we look specifically

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at the behavior of ~~CO₂_grad_del~~ $\delta\nabla_{CO}$ (defined in Section 4.1) and dP (defined in Section 4.2) bias correction in the simulated system. The purpose of the analysis of this section is to answer the following questions:

(1)   Do the bias correction for dP and ~~CO₂_grad_del~~$\delta\nabla_{CO2}$ behave similarly in the simulation system as in real OCO-2 retrievals?

5   (2)   What is the effect of bias correction on CO_2 errors?

~~4.1 CO2_grad_delta~~

~~CO₂_grad_del~~The bias correction is determined using this simulated dataset, and then applied to the same dataset, which is somewhat circular, since the true is both used to determine the bias correction and to check the bias correction, but it is
10   important to know whether the relationships exist. For example, what causes the spatial patterns seen in the bias in Fig. 2.

4.1 The retrieved profile gradient

$\delta\nabla_{CO2}$ is defined as delta[20] – delta[13] where delta is the retrieved CO_2 profile minus the prior CO_2 profile, [20] is the surface level, and [13] is 7 levels above the surface, i.e., 0.63*(surface pressure). ~~CO2_grad_delta~~ $\delta\nabla_{CO2}$ represents ~~curvature~~gradient of the retrieved CO_2 profile that differs from the prior. It has been found that the slope of XCO₂ error versus ~~CO2_grad_delta~~
15   $\delta\nabla_{CO2}$ varies depending on the a priori covariance that is used in the retrieval system, with a more evenly varying covariance having less dependency of XCO₂ error versus ~~CO2_grad_delta~~$\delta\nabla_{CO2}$ (O'Dell, unpublished result). The standard OCO-2 constraint is very loose at the surface (e.g. with 50 ppm a priori variability) and tighter in the mid-Troposphere (with ~10 ppm a priori variability). Most CO_2 variability does occur near the surface near the primary sources and sinks, but the apriori constraint used in the retrieval algorithm would favor variations at the surface even in cases when the variations occur at a
20   higher level due to the weighting due to the prior covariance.

Figure ~~6~~7 shows errors in XCO₂, LMT~~,~~ (the lower tropospheric column, approximately up through 2.5 km), and U (the upper partial ~~columns~~column, approximately from 2.5 km through the top of the atmosphere) (LMT and U are described in Kulawik et al., 2017 and Section 2.1) versus ~~CO2_grad_delta~~$\delta\nabla_{CO2}$ for configuration (b). In the simulated retrievals, the values of the
25   slope of delta xCO₂ versus ~~CO2_grad_delta~~$\delta\nabla_{CO2}$ is -0.001 and -0.008 for land and ocean, respectively. It is clear that there are significant errors in the partitioning between the lower (LMT) and upper (U) partial columns that are correlated to ~~CO2_grad_delta.~~$\delta\nabla_{CO}$. The slope of LMT versus ~~CO2_grad_delta~~ $\delta\nabla_{CO2}$ is 0.23 and 0.22 for land and ocean, respectively and -0.07 and -0.08 for for U land and ocean, respectively. For real ACOS-GOSAT (b3.5) data, Kulawik et al. (2017) found a slope of 0.39 for land and 0.31 for ocean for LMT and -0.11 and -0.09 for U land and ocean, respectively, which are similar
30   values as seen in this simulated data.

These results naturally lead to the question; what is the effect of placing CO_2 at the wrong pressure level? The mean Jacobian for the U partial column (upper 15 layers) is only about 60% (0.62) of the mean value for the lowermost 4 layers. Therefore a molecule in the LMT partial column is equivalent to about 1.6 molecules in the upper partial column. Therefore, a molecule mistakenly placed in the lower 4 layers and moved to the upper layers in the post-processing step needs to be exchanged for

5   1.6 molecules in the upper partial column to have the same impact on the radiances at the new level. At ~~CO2_grad_delta~~$\delta\nabla_{CO2}$ of 35, for land, LMT is high by ~8.4 ppm. For an even exchange, moving 8.4 ppm from the LMT partial column to the U partial column results in +2.5 ppm in the U partial column ONLY from the effects of air mass (because the U partial column has more air mass; = 8.4 ppm *.23 LMT airmass / 0.77 U airmass). Considering the difference in sensitivity, and multiplying by 1.6, this corresponds to +4.0 ppm in the U partial column. The net effect on XCO_2 of this bias correction is the sum of the

10   partial columns times the air mass, -8.4*.23 + 4.0*.77 = 1.1 ppm. This is at ~~CO2_grad_delta~~$\delta\nabla_{CO2}$ of 35, so that would mean that the slope for XCO_2 error versus ~~CO2_grad_delta~~$\delta\nabla_{CO}$ is 0.031. For real OCO-2 v7 data, the slope of XCO_2 error versus ~~CO2_grad_delta~~$\delta\nabla_{CO2}$ is +0.0280 and -0.077 for land, ocean, respectively (Mandrake et al., 2017). This analysis explains a positive slope in XCO_2 versus ~~CO2_grad_delta;~~$\delta\nabla_{CO2};$ but would not explain a negative slope. The negative slope would result from additional correlations or errors acting in addition to this effect.

15   ~~4.2 dP~~

4.2 The retrieved surface pressure

The quantity dP is the difference between retrieved and prior surface pressure and is used as a post-processing bias correction for OCO-2. In this section, we explore results from dP in the simulated dataset to try to understand why bias correction based on this parameter is useful.

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Although it is typically assumed that the surface pressure is determined solely from the O2A band, the strong and weak CO_2 bands also contribute~~,~~ information. For land nadir, averaged over cases passing post-processing quality screening, the band-averaged Jacobian strengths in the weak and strong CO_2 bands relative to the O2A band are 0.2 and 0.4, respectively. Based on the surface pressure Jacobian and the spectral error, a value of -2 hPa will create a spectral bias 0.2 times the size of the

25   spectral error in the O2A band, which, because it is a correlated error, will be an additive error over the band.

Figure ~~7~~8 shows the actual error covariances and biases for 3 different subsets of run (d): dP < -2 hPa, -1<dP<1hPa ("nominal cases"), and dP>1.5hPa. The errors shown are normalized by the predicted error, using the equation Eij = Eij / sqrt(E0ii*E0jj), where E is the error covariance of interest and E0 is the predicted error covariance. A diagonal value of 1 means that the actual

30   error is the same as predicted, and a diagonal value of 4 represents an actual error that is twice (sqrt(4)) as large as predicted. The errors and error correlations are much larger than predicted for many parameters. In addition, the CO_2 parameters show

less correlation with other parameters for the nominal case. Also note that the nominal case has less saturation, meaning less errors and correlations.

Next we looked at the possibility of screening incorrect surface pressure results using ~~the reduced χ^2 (χ^2 normalized by the~~ ~~expected noise).~~χ_{rad}^2 (defined in Eq. 6). To do this we used the ~~χ^2~~χ_{rad}^2 for land, cloudy cases with dP<-2 vs. -1<dP<0. The cases with dP<-2 had 0.04, 0.01, and 0.06 higher reduced ~~χ^2~~χ_{rad}^2 in the 3 bands, respectively. Although the dP<-2 case fit the spectra worse there was too much overlap to distinguish between these cases solely from ~~the reduced χ^2.~~χ_{rad}^2.

The albedo errors and correlations (purple box) particularly stand out, with correlations with many retrieved parameters. The albedo terms are, in order: O2A mean, O2A slope, weak mean, weak slope, strong mean, strong slope. Based on the O2A mean albedo and the surface pressure Jacobians, a change in retrieved surface pressure of -2 hPa can be compensated by a change in the albedo on the order of -0.001, with this analysis based on band averages, and not necessarily implying a good fit. However, this analysis indicates that very minute changes in the surface albedo (on the order of 0.1%) can compensate for moderate sized errors in the retrieved surface pressure. The exact relationship can be better studied by examining the radiative transfer, and looking at how the final transmission of sunlight relates to both the total amount of atmospheric absorption and the surface albedo.

Error in the retrieved XCO$_2$, lower partial column (~~lmt~~LMT) and upper partial columns (~~u~~U) are plotted versus the error in surface pressure in Fig. ~~8~~9, which all show moderate (R=0.63) to strong (R=-0.98) correlations. ~~For ocean soundings, the~~ ~~OCO-2 v7 dP correction factor is -0.08, while the simulated data has a slope of +0.15. For land scenes the OCO-2 v7 dp~~ ~~correction factor is -0.3, and the correction factor~~The bias found in this work for this simulated ~~data~~dataset for the XCO$_2$ bias versus dP ~~i~~s -0.23 for land and 0.15 for ocean. We can compare these to the OCO-2 v7 biases of -0.3 for land and -0.08 for ocean. Note that for the simulated data, the prior surface pressure is set to the true, so (surface pressure – prior) is the same as (surface pressure – true). The bias correction factors are found in Table 4 of the v7 bias correction documentation.

The retrieval system must match the mean photon path length for the O2A channel using retrieved parameters like surface pressure, albedo, water, temperature, aerosol pressure heights, and aerosol optical depths. Also note that the ~~number of~~ O2 ~~molecules~~volume mixing ratio (VMR) is fixed and not retrieved. Mean photon path length increases with higher albedo and aerosol optical depth (Palmer et al., 2001). Additionally, moving aerosols lower in the atmosphere increases mean photon path length, because light scattered by the aerosol travels farther, and a larger surface pressure will increase mean photon path length because the path length to the surface is longer. The retrieval system varies these parameters to match the observed radiances. Ideally, the 3 bands would have the same albedo and aerosol properties, so that getting the O2A band mean photon path length right will also get the mean photon path length in the CO$_2$ bands. Real aerosol optical depths tend to be higher in the O2A band then in the CO$_2$ bands. However, the aerosol optical depth versus frequency is fixed for OCO-2. Therefore, as

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an example, using a too-thick aerosol in the O2A band to compensate for a too-small surface pressure will not balance in the CO_2 bands because the same too-small surface pressure will be offset by less aerosol. The relative strengths of the Jacobians for the four aerosol optical depths in the O2A versus CO_2 bands are 1.5x, 3.3x, 7.2x, and 2.1x, respectively, indicating the dominance of the O2A-band concerning aerosol information.

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As seen in Fig. 7b8b, for dp < -2 hPa, there is a negative bias in surface pressure (because we selected for this), negative biases in 3 of the 4 aerosol optical depths (green box, parameters 1, 4, and 10), positive bias in retrieved aerosol pressure (green box, parameters 2, 5, 8), and negative biases in the retrieved albedo (purple box, parameters 1, 3, 5). The error covariances show that within this subset of observations, there are also strong negative correlations between retrieved surface pressure error and
10 errors in albedo and errors in aerosol optical depth and positive correlations between error in aerosol optical depth and errors in albedo.

To trace the interferent errors to an error for XCO_2 the effect of each bias on mean photon path length for the O2A, weak and strong bands needs to be calculated and then the mean photon path length error of the CO_2 bands versus the O2A band will
15 give the error for XCO_2. For example if the O2A mean photon path length is perfect and the CO_2 mean photon path length is 0.5% too large relative to true, then the CO_2 retrieved VMR will be 0.5% too small. Since aerosols are compensating for errors in surface pressure, it is not ideal to fix their relationship versus frequency.

Figure 7d8d-f shows the bias patterns for these different groups. Comparing 7d,e, and f, reveals patterns that could be used
20 for screening: e.g. low bias in Kahn1 aerosol optical depth and a low biases in all albedo means and high biases in all albedo slope indicates a negative surface pressure error; whereas a high bias in Kahn1 aerosol pressure and width and a high bias in the strong band albedo slope indicates a positive surface pressure error. In real retrievals, since true is not known; e.g. an albedo high bias versus an actual high albedo cannot be distinguished; however a particular pattern of biases versus the priors would be suspicious.

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It is interesting to note that the system appears to be able to compensate and pass post-processing quality screening, using albedo and aerosols, for low surface pressure biases down to -4 hPa, but high surface pressure biases only up to +2 hPa.

4.3 Error correlation and effect of bias correction on errors

Another important question is; how does bias correction within the CO_2 column affect errors, particularly the error correlations
30 in XCO_2 and the partial columns? Kulawik et al. (2017) found that the predicted error correlation between the LMT and U partial columns was -0.7 for land and -0.8 for ocean; whereas the actual error correlation versus aircraft was found to be +0.6 (with uncertainty in the correlation due to the fact that aircraft do not cover the full U partial column and effects of co-location error). Additionally, Kulawik et al. (2017) found that whereas the XCO_2 predicted errors were underestimated by about a

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factor of 2, the LMT and U errors were overestimated by about a factor of 2. Weakening the LMT and U correlations would result in higher and more accurate error estimates for XCO_2.

The errors for XCO_2, LMT, and U for land and ocean for configuration (b) are summarized in Table 9. The bias correction for XCO_2 (using only ~~CO_2_grad_del~~$\delta\nabla_{CO}$ and dP) lowers the XCO_2 bias from 0.2 to 0.1 ppm and the error from 0.8 ppm to 0.7 ppm for land, but has no impact on the ocean error or bias. The XCO_2 error is underestimated by a factor of 2 for these simulation results, similarly to what was found with real data.

Similar to findings with real data, the XCO_2 error in these simulations is underestimated, whereas the LMT and U errors are overestimated. However, the overestimate of the partial column errors are not as large as seen with real GOSAT data. The predicted error correlation is -0.91 for the LMT and U errors, whereas the actual error correlation is -0.5. Using eq. 10c from Kulawik et al. (2017), and the LMT and U errors in Table 9, we note two key results. First, the XCO_2 predicted error is 0.37 ppm when the error correlation is -0.91. Second, the predicted XCO_2 error is 0.64 (0.71) ppm for ocean (land) when the actual correlation is -0.57 (-0.46) for ocean (land). The second result is close to the actual error of 0.7 ppm. The estimate of +0.6 correlation from Kulawik et al. (2017) is probably wrong, and could be due to unaccounted effects of co-location error on correlation estimates.

As seen in Section 3.1, non-linearities from interferents affect both partial columns similarly. This would result in positive error correlation (since the correlation is strongly negative and results in a less negative correlation than predicted) and explain the larger actual versus predicted XCO_2 error. A high negative correlation is desirable for XCO_2 because it asserts that, although there is uncertainty in the partitioning of LMT and U, the sum of the two has a smaller uncertainty.

6 Discussion and conclusions

The 15 orbits of simulated retrievals result in ~10,000 land and ocean scenes for cloud-free runs, and 870 and 680 land and ocean cases for runs with clouds, after post-processing quality screening. Prior to application of quality flags, described in Section 2.3, the errors are ~10 ppm for land and ~2 ppm for ocean. After quality flags, and bias correction are applied, the errors are 0.7 ppm, with mean bias errors of 0.1 ppm for both land and ocean. There is a spatial pattern to the bias, which has similar characteristics to the spatial pattern of real OCO-2 biases, with a correlation length of ~3 degrees, similar to the correlation length of 5-10 degrees for OCO-2 (Kulawik et al., 2019).

Comparing runs with and without measurement noise added to the radiances showed that the predicted measurement error is accurate. Comparing the retrieved results to the linear estimate using only the CO_2 parameters ("smoothing error") shows that the smoothing error is not greater than 0.5 ppm, but due to interferent error and non-linearity this could not be validated more

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accurately with the tests used. A more accurate way to validate this would be to run tests with different priors (e.g. Kulawik et al., 2008), which was previously done (unpublished) finding that the smoothing errors are smaller than 0.2 ppm.

The linear estimate does not predict the non-linear retrievals to better than 0.9 ppm (much worse when quality flags are not
5   used), indicating this level of non-linearity in the retrieval system. The interferent error is underpredicted by a factor of 4, based on the relationship of XCO_2 error versus error for each retrieved interferent. The retrieved interferent error is twice as large as predicted for some parameters, and the correlation between the retrieved interferent error and XCO_2 error is twice as large as predicted for some parameters. The larger correlation is likely due to the fact that CO_2 Jacobian strength is correlated with many retrieved interferent values; a wrong interferent value will result in the wrong CO_2 Jacobian strength, resulting in
10   an error in CO_2.

Two bias correction terms are explored: ~~CO2_grad_delta,~~$\delta\nabla_{CO_2}$, the gradient of the retrieved CO_2 profile relative to the priori; and dP, the retrieved surface pressure minus the prior. The ~~CO2_grad_delta~~ $\delta\nabla_{CO}$ bias correction could be explained by 1) a loose CO_2 constraint near the surface prefers changes near the surface versus changes elsewhere. 2) Since the CO_2 Jacobian
15   strength near the surface is stronger versus the Jacobian elsewhere in the profile, molecules incorrectly placed near surface are underestimated, because each molecule has "too much" effect on the observed radiance, 3) this results in an XCO_2 column that is too low. This explanation would explain the positive bias correction factor seen in OCO-2 v7 land and v8 land and ocean, but would not explain the negative correction factor seen in v7 ocean.

20   The theoretical basis for dP is complicated because so many other retrieval parameter errors are correlated to errors in dP. This makes sense from a fundamental radiative transfer perspective which ties together the surface and scattering properties with the amount of atmospheric column for any particular sounding. The retrieval system appears to use albedo and aerosols to compensate for errors in dP. In these simulated results the dP bias correction has a similar slope as seen in real OCO-2 data for land, but not for ocean. The results with dP errors had marginally higher radiance residuals but not high enough to easily
25   screen.

Similar to the findings in Kulawik et al. (2017), the XCO_2 column error is much higher than predicted, whereas the lower and upper partial CO_2 column errors, LMT and U, respectively, have errors lower than predicted. The underprediction of XCO_2 error results because the retrieval system thinks the LMT and U partial column error correlation is -0.91. The actual correlation
30   is -0.5 to -0.6 after bias correction, with the uncorrected results having both higher error and higher correlations in the partial columns. When the actual correlation is used to estimate XCO_2 error, the predicted XCO_2 error matches the actual error within 0.1 ppm. The reason why this correlation is off may be due to the fact that both partial column Jacobian strengths vary similarly with interferent errors, which are underpredicted in the linear estimates of errors, and would result in less negative correlation between the partial columns.

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These results suggest a few possible strategies (a) isolating the primary interferent parameters via pre-retrievals of aerosols with surface pressure, CO_2, and albedo fixed, followed by a full joint retrieval. This would allow clouds and aerosols to be approximately set without throwing the other retrieved parameters off. A similar technique was employed in the thermal

5   infrared to mitigate cloud contamination (e.g. Eldering et al., 2008). A second tactic would be to perform retrievals beginning at many different initial states, selecting the result with the lowest radiance residual. This solution however is computationally expensive.

In summary, the simulated retrievals have many of the same attributes of real data, with the advantage of knowledge of the

10   true state and ability to see what is going on under the hood. These simulation studies suggest attention should be given to non-linearity, because the ability to estimate errors and make incremental improvements depends on the accuracy of the linear estimate, which has accuracy of only about 0.9 ppm in these simulation studies.

Author contributions:

15   Susan Kulawik set the direction of the research and did the analysis, figures, and was the primary manuscript writer. Rob Nelson and Tommy Taylor generated simulated OCO-2 true states, radiances, and retrievals. Chris O'Dell guided the work of the simulation system and advised on the analysis. All authors participated in the manuscript writing and editing.

Competing interests:

20   The authors declare that they have no conflict of interest.

Data availability:

Data is available here: https://drive.google.com/file/d/1F_VfJOCfjlqVFLD3sY2zBjYbqPsrOVSW/view?usp=sharing

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Table 1. Retrieved parameters in this simulation study

Index	Parameter
1-20	20 CO_2 volume mixing ratios (VMR) at 20 pressure levels from the surface to top of the atmosphere (20)
21	Water vapor scaling factor
22	Surface pressure
23	Temperature profile offset
24, 27, 30, 33	Aerosol optical depth for 4 types
25, 28, 31, 34	Aerosol pressure height for 4 types
26, 29, 32, 35	Aerosol width for 4 types (prior uncertainty is very tight)
36, 38, 40	Albedo mean for 3 bands
37, 39, 41	Albedo slope for 3 bands
42, 43, 44	Dispersion offset for 3 bands (frequency offset).
45	Wind speed (ocean). In the original files this is index 36, but was moved to index 45 so that the albedo indices are consistent between land and ocean.
45, 46	Fluorescence (Land). The true fluorescence is set to zero for these simulations.

Table 2. Updates in the simulated retrieval system since O'Dell et al. (2012)

B2.10 changes	B3.3 changes	B3.4 changes
1) Gaussian aerosol profiles	1) Residual fitting	1) Ocean surface parameterization
2) Sigma pressure levels	2) Reduced p_surf prior uncertainty	2) Update weak CO_2 spectral range
3) Update to prior CO_2 profile	3) Prior AOD=0.05	3) Spectroscopy update
4) Spectroscopy updates	4) Spectroscopy update	
5) Correction to XCO_2 AK	5) Fluorescence fit land gain H (GOSAT)	

Table 3. Configurations used in this work.

Case	Measurement Error	Clouds+Aerosols	Comment
(a)	No	No	Smoothing only
(b)	No	Yes	Smoothing + interferent
(c)	Yes	Yes	Smoothing + interferent + measurement error
(d)	No	Yes	Different water prior/initial

Table 4. Number of cases for each configuration. The "clouds in true==yes" cases contain many fewer soundings than "no clouds" because of pre-screening. The #good is from post-processing screening

	Clouds in true	#	# good (post-screening)	configuration (from Table 3)
Land (nadir)	No	12,097	10,229	a
Ocean (glint)	No	14,265	11,468	a
Land (nadir)	Yes	3,445	868/869/768	c/b/d
Ocean (glint)	Yes	1,560	679/674/620	c/b/d

Table 5. Mean bias and standard deviation between retrieved and true, sorted by standard deviation. The bold entries are the nominal cases most closely simulating actual OCO-2 retrievals.

Case from Table 3	Land/Ocean	Clouds in true	Post-processing screening	Meas. error	~~Bias~~ Mean bias	Standard deviation
(a)	Ocean	No	Yes	No	-0.1	0.4
(a)	Land	No	Yes	No	-0.5	0.4
(a)	Ocean	No	No	No	-0.3	0.6
(a)	Land	No	No	No	-0.5	0.7
(b)	Ocean	Yes	Yes	No	0.1	0.7
(c)	**Ocean**	**Yes**	**Yes**	**Yes**	**0.1**	**0.7**
(b)	Land	Yes	Yes	No	0.2	0.8
(c)	**Land**	**Yes**	**Yes**	**Yes**	**0.2**	**0.8**
(b)	Ocean	Yes	No	No	-0.6	2.7
(b)	Land	Yes	No	No	-2.3	10.3

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Table 6. Difference of linear estimate versus non-linear retrieval, noise-free, cloud, quality-screened cases

	Land bias	Land std	Ocean bias	Ocean std
Predicted	0	0.3	0	0.2
Retrieved vs. CO_2 AK	-0.2	0.8	-0.2	0.6
Retrieved vs. full AK	-0.4	0.8	-0.9	0.8
Retrieved vs true	0.2	0.9	0.1	0.7

Table 7. Error versus averaging for measurement error

n (number averaged)	Error land (ppm)	Error ocean (ppm)
1	0.35	0.14
2	0.25	0.10
3	0.20	0.08
9	0.12	0.05

Table 8. Predicted and actual errors for interferents and correlations between interferents and XCO$_2$ for simulated land retrievals for case (b) from Table 3. Bold values are those parameters with interferent errors larger than predicted and large actual correlations to XCO$_2$ error (absolute value larger than 0.25).

		Pred error	Actual error	Error factor	Pred corr	Actual corr	Impact on XCO$_2$ (ppm)
Met	**H2O scaling**	**0.003**	**0.005 ± 0.004**	**5**	**0.35**	**0.93**	**1.2**
Met	Surface pressure	0.5	-0.67 ± 1.02	3	-0.38	-0.02	0.0
Met	**Temperature offset**	**0.04**	**0.25 ± 0.22**	**9**	**0.17**	**0.44**	**0.6**
Aerosol	**Aerosol ice OD**	**0.002**	**-0.02 ± 0.21**	**101**	**0.03**	**0.81**	**1.1**
Aerosol	Aerosol Ice Pressure	0.09	0.03 ± 0.28	3	-0.01	0.22	0.3
Aerosol	Aerosol Ice Width	0.01	0.01 ± 0.01	2	-0.00	0.13	0.2
Aerosol	**Aerosol Kahn1 OD**	**0.01**	**-5.0 ± 0.8**	**4**	**-0.36**	**-0.39**	**0.5**
Aerosol	Aerosol Kahn1 Pressure	0.3	0.3 ± 0.4	1	0.08	-0.10	0.1
Aerosol	Aerosol Kahn1 Width	0.01	0.04 ± 0.08	9	-0.00	-0.19	0.3
Aerosol	Aerosol Kahn2 OD	0.01	-5.0 ± 0.8	2	0.32	-0.02	0.0
Aerosol	**Aerosol Kahn2 Pressure**	**0.4**	**0.7 ± 0.5**	**2**	**-0.02**	**0.26**	**0.3**
Aerosol	Aerosol Kahn2 Width	0.01	0.1 ± 0.09	17	0.00	0.18	0.2
Aerosol	Aerosol Water OD	0.008	-5.9 ± 1.0	7	-0.06	-0.15	0.2
Aerosol	Aerosol Water Pressure	0.4	0.7 ± 0.5	3	-0.01	-0.06	0.1
Aerosol	Aerosol Water Width	0.01	0.09 ± 0.03	9	0.00	-0.13	0.2
Albedo	**Band 1 Albedo ave**	**0.0008**	**-0.0002 ± 0.003**	**3**	**0.19**	**-0.50**	**0.7**
Albedo	Band 1 Albedo slope	1e-6	1e-6 ± 1e-6	3	-0.26	-0.10	0.1
Albedo	**Band 2 Albedo ave**	**0.0006**	**-0.002 ± 0.004**	**7**	**0.19**	**-0.54**	**0.7**
Albedo	Band 2 Albedo slope	1e-7	2e-6 ± 2e-6	8	0.10	0.20	0.3
Albedo	Band 3 Albedo ave	0.0007	-0.001 ± 0.005	7	0.04	-0.22	0.3

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Albedo	Band 3 Albedo slope	1e-6	0e-6 ± 2e-6	3	0.14	-0.36	0.5

Table 9. Predicted and actual errors and biases in raw and bias-corrected simulated data run with configuration (b) from Table 3. Similar to operational retrievals, bias-corrected XCO_2 error is underestimated, whereas the CO_2 partial column errors are overestimated. The XCO_2 error underprediction results from overestimated error correlations of the partial columns.

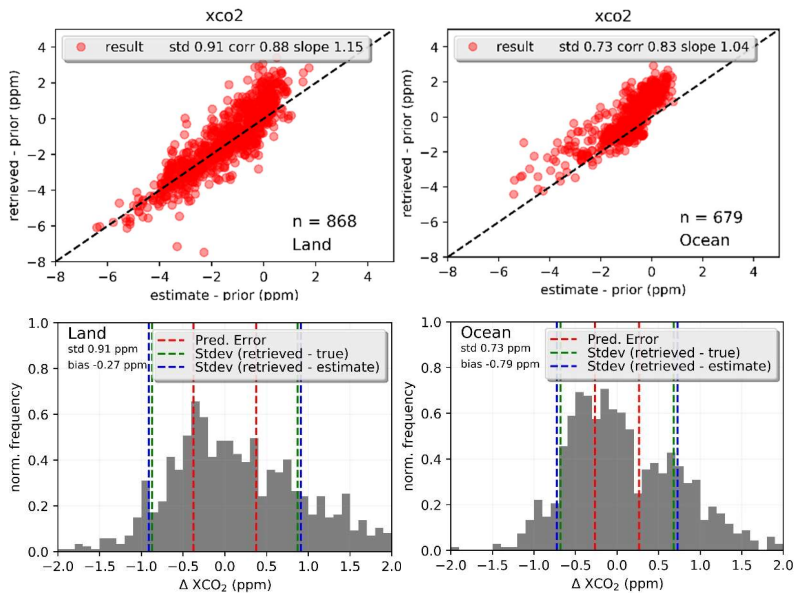|	Ocean pred. (ppm)	Ocean actual (ppm)	Ocean actual corrected (ppm)	Land pred. (ppm)	Land actual (ppm)	Land actual corrected (ppm)
LMT	2.6	2.6 ± 2.9	0.1 ± 2.3	3.3	2.9 ± 4.2	-0.6 ± 2.6
U	0.9	-0.6 ± 1.1	0.2 ± 1.0	1.2	-0.6 ± 1.4	0.3 ± 0.9
XCO_2	0.3	0.1 ± 0.7	0.1 ± 0.7	0.4	0.2 ± 0.8	0.1 ± 0.7
LMT and U correlation	-0.91	-0.67	-0.57	-0.90	-0.68	-0.46

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Figure captions:

Figure 1. Scatter plots of XCO_2 difference from the prior for retrieved versus true on the simulated data. This corresponds to dataset (c) with clouds and measurement error, and post-processing screening applied for land (left) and ocean (right), with 1:1 plots shown on the top panels, and histogram of the differences on the lower panels.
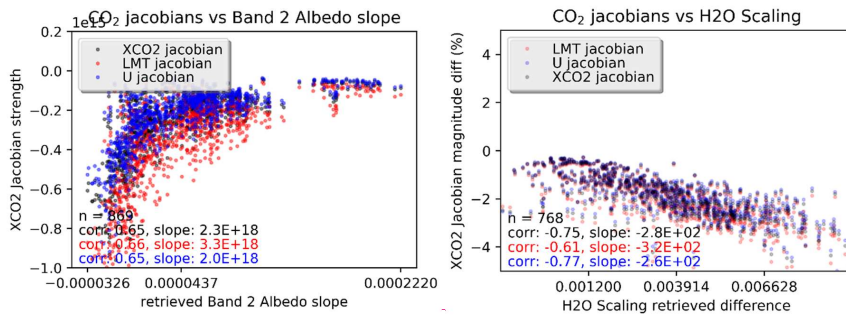
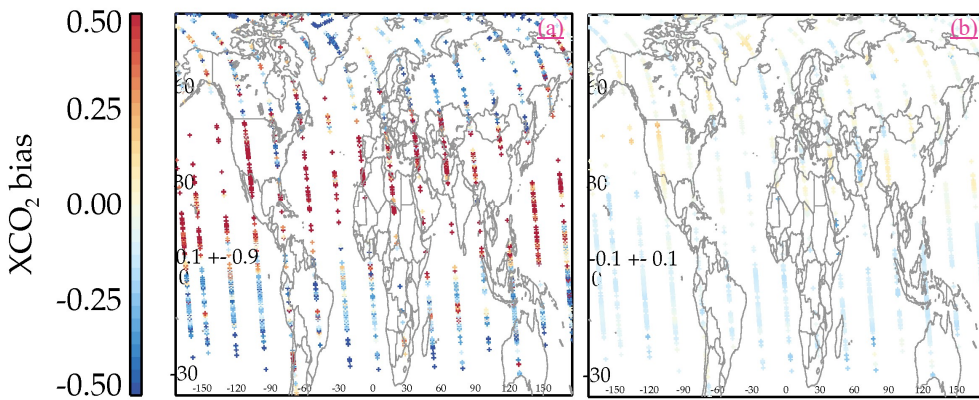Figure 2. (a) Spatial pattern of XCO_2 retrieved minus true for case (b) from Table 3 (cloudy but no measurement error), with quality screening. Panel (b) shows the difference between true XCO_2 with the OCO-2 averaging kernel applied minus true XCO_2.
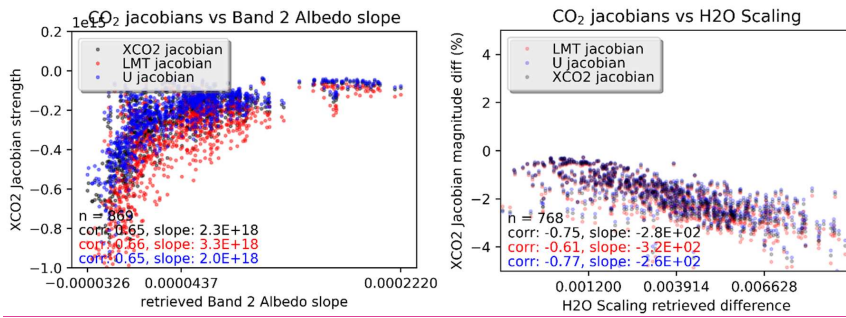
Figure 3. XCO_2 (black), lower CO_2 partial column (red), and upper CO_2 partial column (blue) Jacobian band-averaged magnitude versus interferent parameters. Left shows CO_2 magnitude versus retrieved "Band 2 Albedo slope", using configuration (b) from Table 3; right shows the CO_2 Jacobian magnitude difference (in percent) for matched cases from run (b) and (d) versus differences in retrieved "H_2O scaling".
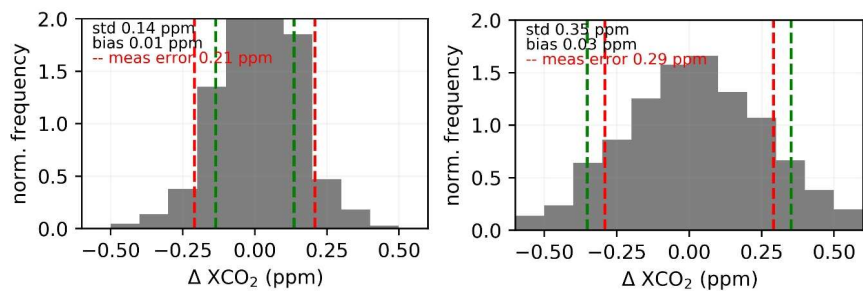
Figure 34. Histogram of difference between XCO_2 with noise on and noise off for ocean(left) and land(right), cases (b) and (c) from Table 3.
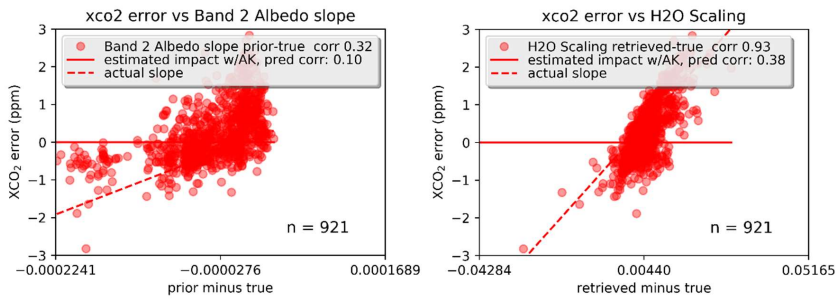
Figure 45. Predicted (red line) and true error (red dots) for two interferents, "Band 2 albedo slope", left, and "H2O Scaling", right.

Figure 56. Predicted and true errors. Left shows the predicted error covariance matrix, for the retrieval parameters listed in Table 1, with the CO_2 profile collapsed into 2 parameters [LMT and U partial columns]. The blue, orange, green, and purple boxes contain CO_2, metrological, aerosol, and albedo parameters, respectively. Both matrices are normalized by the diagonal of the predicted errors.

Figure 67. Error in retrieved CO_2 for XCO_2 (black), upper partial column, U (blue) and lower partial column LMT (red) versus ~~CO2_grad_delta~~$\delta \nabla_{CO}$ for ocean (left) and land (right)

Figure 78. Normalized actual error covariances and biases of retrieved parameters for dp<-2 hPa (a, d), -1<dp<1 hPa (b, e), and dp > 1.5 hPa (c, f) using configuration from Table 3 (d) for land/cloudy. The purple box surrounds the albedo parameters, the green box surrounds aerosol parameters, the red box surrounds metrological parameters, and the blue box surrounds the CO_2 fields, which have been collapsed into lower and upper partial columns. The errors are normalized by the predicted errors

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(which are shown in Fig. 5). The arrow in panel (a) shows correlation between LMT and surface Pressure, which is negative (also see Fig. 8b below)

Figure 89. Error in the lower partial column (LMT), upper partial column (U) and total column (XCO_2) versus error in surface
pressure (with 0.2 hPa bins) for ocean (left) and land (right). ~~The~~Fhe OCO-2 v7 XCO_2 bias versus dP is -0.3 for land and -0.08 for ocean.

Figure 1. Scatter plots of XCO$_2$ difference from the prior for retrieved versus true on the simulated data. This corresponds to dataset (c) with clouds and measurement error, and post-processing screening applied for land (left) and ocean (right), with 1:1 plots shown on the top panels, and histogram of the differences on the lower panels.

CO_2 jacobians vs Band 2 Albedo slope

XCO2 jacobian strength

- XCO2 jacobian
- LMT jacobian
- U jacobian

n = 869
corr: 0.65, slope: 2.3E+18
corr: 0.56, slope: 3.3E+18
corr: 0.65, slope: 2.0E+18

retrieved Band 2 Albedo slope

CO_2 jacobians vs H2O Scaling

XCO2 Jacobian magnitude diff (%)

- LMT jacobian
- U jacobian
- XCO2 jacobian

n = 768
corr: -0.75, slope: -2.8E+02
corr: -0.61, slope: -3.2E+02
corr: -0.77, slope: -2.6E+02

H2O Scaling retrieved difference

Figure 2.

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XCO_2 bias

Figure 2. (a) Spatial pattern of XCO_2 retrieved minus true for case (b) from Table 3 (cloudy but no measurement error), with quality screening applied. Panel (b) shows the difference between true XCO_2 with the OCO-2 averaging kernel applied minus true XCO_2.

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Figure 3. XCO$_2$ (black), lower CO$_2$ partial column (red), and upper CO$_2$ partial column (blue) Jacobian band-averaged magnitude versus interferent parameters. Left shows CO$_2$ magnitude versus retrieved "Band 2 Albedo slope", using configuration (b) from Table 3; right shows the CO$_2$ Jacobian magnitude difference (in percent) for matched cases from run 5 (b) and (d) versus differences in retrieved "H$_2$O scaling".

Figure 34. Histogram of difference between XCO_2 with noise on and noise off for ocean(left) and land(right), cases (b) and (c) from Table 3.

Figure 45. Predicted (red line) and true error (red dots) for two interferents, "Band 2 albedo slope", left, and "H2O Scaling", right.

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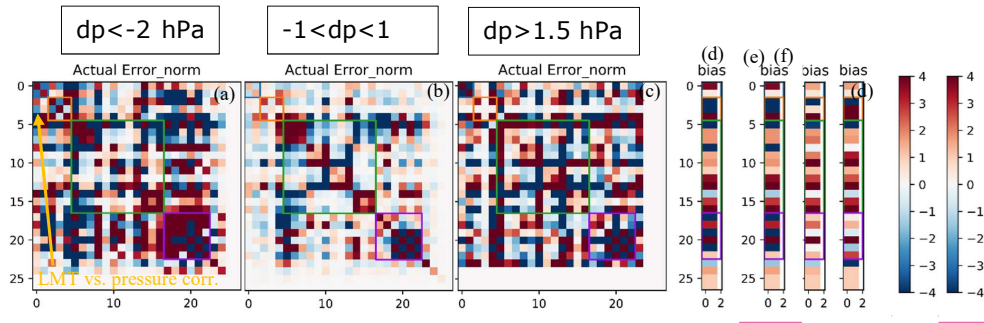
Figure 78. Normalized actual error covariances and biases of retrieved parameters for dp<-2 hPa (a, d), -1<dp<1 hPa (b, e), and dp > 1.5 hPa (c, f) using configuration from Table 3 (d) for land/cloudy. The purple box surrounds the albedo parameters, the green box surrounds aerosol parameters, the red box surrounds metrological parameters, and the blue box surrounds the CO_2 fields, which have been collapsed into lower and upper partial columns. The errors are normalized by the predicted errors (which are shown in Fig. 5). The arrow in panel (a) shows correlation between LMT and surface Pressure, which is negative (also see Fig. 8b below)
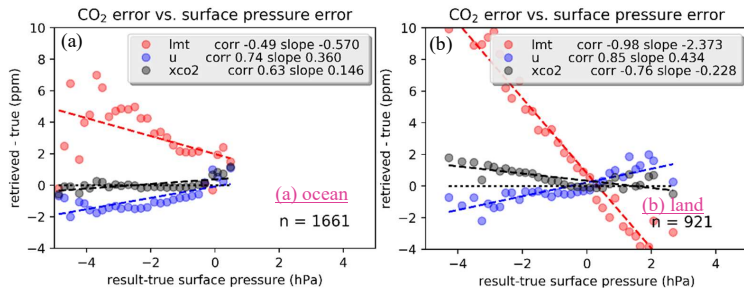
Figure 89. Error in the lower partial column (LMT), upper partial column (U) and total column (XCO₂) versus error in surface pressure (with 0.2 hPa bins) for ocean (left) and land (right). The ~~OCO-2 v7~~ XCO₂ bias versus dP is -0.~~3~~23 for land and -0.~~08~~15 for ocean.

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