Method to measure the size-resolved real part of aerosol refractive index using differential mobility analyzer in tandem with single particle soot photometer

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Abstract

Knowledge on the refractive index of ambient aerosol can help reduce the uncertainties in estimating aerosol radiative forcing. A new method is proposed to retrieve the size-resolved real part of refractive index (RRI). Main principle of deriving the RRI is measuring the scattering intensity by single particle soot photometer of size-selected aerosol. This method is validated by a series of calibration experiments using the components of known RRI. The retrieved size-resolved RRI cover a wide range from 200 nm to 450 nm with uncertainty less than 0.02. Measurements of the size resolved RRI can improve the understanding of the aerosol radiative effects.

1 Introduction

Aerosols exert significant influence on the earth energy budget by scattering and absorbing radiation (Ramanathan and Carmichael, 2008). There still remain great uncertainties when estimating the aerosol effective radiative forcing (RF) (Ghan and Schwartz, 2007) and an accurate estimation of the aerosol optical properties can help reduce the RF variations. The optical properties of the ambient aerosol particles are determined by their particle size and complex refractive index (RI, $m=n+ki$) (Bohren and Huffman, 2007;Levoni et al., 1997). Despite that the ambient aerosol particle size distribution can be measured with high accuracy (Wiedensohler et al., 2012), an accurate measurement of the ambient aerosol RI remains challenging. The RI is also widely used in remote sensing (Redemann et al., 2000;Dubovik, 2002;Zhao et al., 2017) and atmospheric modelling (Ghan and Schwartz, 2007;Kuang et al., 2015) because the aerosol single scattering albedo (SSA) and aerosol scattering phase function are highly related with the RI. At the same time, a small uncertainty in the real part of the RI (RRI) can lead to great uncertainties when estimating the aerosol RF. Zarzana et al. (2014) found that a variation of 0.003 in RRI can lead to uncertainties of 1% in RF for non-absorbing ammonium sulfate particles. Moise et al. (2015) estimated that the RF would increase 12% when the

30   RRI varied from 1.4 to 1.5. Valenzuela et al. (2018) reported that the uncertainties in RF is estimated

31   to be 7% when the aerosol RRI varied by 0.1. Therefore, it is pressing that the uncertainties of the RI

32   be reduced when estimating the RF.

33   Many methods were proposed to derive the RRI. The RRI can be estimated by linear volume

34   average of the known aerosol chemical components by

35 $$\text{n} = \sum_i f_i \, n_i \qquad (1)$$

36   where f_i and n_i is the volume fraction and known partial refractive index of ith component (Wex et

37   al., 2002;Hand and Kreidenweis, 2002;Hänel, 1968;Liu and Daum, 2008). The aerosol RRI can also

38   be calculated by partial molar refraction approach (Stelson, 1990;Hu et al., 2012) which is essentially

39   consistent with the linear volume method (Liu and Daum, 2008). The ambient aerosol RRI can be

40   derived by synthetically using the radiative transfer calculations and the ground-based solar extinction

41   and scattering measurements (Wendisch and Hoyningen-Huene, 1994, 1992). Sorooshian et al. (2008)

42   developed a method to measure the aerosol RRI based on the differential mobility analyzer (DMA)

43   and an optical particle counters. The RRI could be retrieved from the known particle size from the

44   DMA and the aerosol scattering intensity from the Optical Particle Counter (OPC) for aerosol particles

45   larger than 500 nm. The Scanning Mobility Particle Sizer (SMPS) and OPC was used in combination

46   to derive the RRI by aligning the particle size distributions in the instrument overlap regions (Hand

47   and Kreidenweis, 2002;Vratolis et al., 2018). The aerosol effective RRI was also retrieved by applying

48   Mie scattering theory to the aerosol particle number size distribution, aerosol bulk scattering

49   coefficient and aerosol absorbing coefficient data (Cai et al., 2011;Liu and Daum, 2000). Spindler et

50   al. (2007) retrieved the aerosol RRI value by using the cavity ring-down spectroscopy to measuring

51   the scattering and absorbing properties of bulk aerosols. Eidhammer et al. (2008)) measured the light

52   scattering at different angles and retrieved the RRI. Similarly, the aerosol RRI was retrieved by

53   measuring the aerosol phase function (Barkey et al., 2007). Recently, a method by using the single

54   particle mass spectrometry was proposed to measure the aerosol RRI (Zhang et al., 2015). At the same

55   time, aerosol time-of-flight mass spectrometer was proved to be capable of measuring the aerosol RRI

56   (Moffet et al., 2008). The aerosol RRI can also be retrieved from the Mie spectroscopy by using the

57   optical tweezers in the laboratory (Shepherd et al., 2018).

58   Many studies show that aerosol of different diameters share different properties such as shape

59   (Zhang et al., 2016;Peng et al., 2016), density (Qiao et al., 2018), aerosol hygroscopicity (Wang et al.,

2017) and most importantly, the chemical components (Liu et al., 2014;Hu et al., 2012). Thus, there might be significant variations in the aerosol RRI for aerosols of different diameters because the aerosol RRI is highly related to the aerosol density (Liu and Daum, 2008) and chemical components (Stelson, 1990). On the other way round, information of the size-resolved aerosol RRI can help to study the chemical information and the aging process of aerosols among different diameters. Therefore, measurement of the size-resolved aerosol RRI is necessary.

Up to now, there are few information in the literature of the size-resolved ambient aerosol RRI (Ebert et al., 2004;Kandler et al., 2007;Ebert et al., 2002). Traditionally, the size-resolved ambient aerosols RRI are estimated by measuring the molar fraction or volume fraction of main aerosol chemical compositions. However, the influence of organic component on the aerosol RRI is ignored. The organic component contributes more than 20% of the total aerosol component in the North China Plain (Hu et al., 2012;Liu et al., 2014). At the same time, RRI of the organic aerosol changes significantly between 1.36 and 1.66 (Moise et al., 2015). Ignoring the organic component may lead to significantly uncertainties when estimating the aerosol RRI. There were no technique, to our knowledge, that directly measures the size-resolved aerosol optical properties and derives the size-resolved aerosol RRI.

In this study, a novel method is proposed to measure the size-resolved ambient aerosol RRI by using a DMA in tandem with a single particle soot photometer (SP2). The principle of the system is using the SP2 to measure the scattering properties of size-selected aerosols. Knowing the aerosol diameter and corresponding scattering intensity, the size-resolved aerosol RRI can be retrieved based on the Mie scattering theory. This proposed method can measure the ambient aerosol RRI over a wide size range with high accuracy. The measurement system is employed in a field campaign in the North China Plain and the corresponding results are further discussed.

The structure of this manuscript is as follows: section 2 provides the instruments setup and details of the instrument. The method to retrieve the size-resolved aerosol RRI is given in section 3. Section 4 shows the discussions about the uncertainties of the proposed method and field measurements results of the size-resolved aerosol RRI. Conclusions come at the last part.

2 Instrument

2.1 Instrument Setup

89   The instrument setup is schematically shown in fig. 1(a). Firstly, the dried sample aerosols are

90   guided to a X-ray soft diffusion charger and then lead to a DMA (Model 3081, TSI, USA). The quasi-

91   monodisperse aerosols that pass though the DMA at a given diameter are then drawn into a SP2 to

92   measure the aerosol scattering properties with a flow ratio of 0.12 lpm and a condensation particle

93   counter (CPC, Model 3776, TSI, USA) to count the aerosol number concentration with a flow ratio of

94   0.28 lpm respectively. Thus, the sample flow (Q_a) of the DMA is 0.4 lpm. Accordingly, the sheath

95   flow (Q_{sh}) of the DMA is 4 lpm. The DMA is set to scan the aerosols diameter from 12.3 to 697 nm

96   over a period of 285s and repeats after a pause of 15 s. The combination of DMA, CPC and SP2 can

97   provide information of aerosol particle number size distribution (PNSD) and size resolved RRI.

98   On 8th, June, 2018, the measurement system was employed at the filed measurement of

99   AERONET station of BEIJING_PKU (N39°59′, E116°18′) to test the reliability of retrieving the

100   ambient size-resolved RRI. This measurement site locates on the north west of the city of Beijing,

101   China and is about 1.8 km north of the Zhongguancun, Haidian District, which is one of the busiest

102   areas in Beijing. It is surrounded by two main streets: Zhongguancun North Street to the west and

103   Chengfu Road to the south. This site can provide representative information of the urban roadside

104   aerosols (Zhao et al., 2018).

105   **2.2 DMA**

106   When a voltage (*V*) is applied to the DMA, only a narrow size range of aerosol particles, with the

107   same electrical mobility (Z_p) can pass through the DMA (Knutson and Whitby, 1975). The Z_p is

108   expressed as:

109   $$Z_P = \frac{Q_{sh}}{2\pi VL} ln(\frac{r_1}{r_2}) \qquad (2)$$

110   where Q_{sh} is the sheath flow rate; *L* is the length of the DMA; r_1 is the outer radius of annular space

111   and r_2 is the inner radius of the annular space. The transfer function refers to the probability that a

112   particle with a certain electrical mobility can pass through the DMA. For a given *V*, the transfer

113   function is triangular-shaped, with the peaking value of 100% and a half width (HW) of

114   $$\Delta Z_p = Z_P \frac{Q_a}{Q_{sh}} \qquad (3)$$

115   The aerosol $Z_{p,}$ which is highly related to the aerosols diameter (D_p) and the number of elementary

116   charges on the particle (*n*), is defined as:

117
$$Z_p = \frac{neC(D_p)}{3\pi\mu D_p} \qquad (4)$$

118 where e is the elementary charge; μ is the gas viscosity coefficient, $C(D_p)$ is the Cunningham slip

119 correction that is defined by:

120
$$C = 1 + \frac{2\tau}{D_p}(1.142 + 0.558e^{-\frac{0.999D_p}{2\tau}}) \qquad (5)$$

121 where τ is the gas mean free path.

122   Based on the discussion above, the aerosols that pass through the DMA with the same Z_p, can

123 have different D_p and different elementary charges.

124 **2.3 SP2**

125   The SP2 is a widely used instrument that can measure the optical properties of every single particle.

126 The measurement principle and instrumental setup of the SP2 have been discussed in detail previously

127 (Stephens et al., 2003;Schwarz et al., 2006) and will be briefly described here. When the sample

128 aerosol particles pass through the continuous Nd:YAG laser beam at 1064 nm with the circulating

129 power about 1 mW/cm^2 in the cavity, eight sensors distributed at four directions are synchronously

130 detecting the emitted or scattered light by using avalanche photo-detector (APD) at different angles

131 (45° and 135°). For each direction, the two APDs sample the same signal with different sensitivities to

132 get a wider measurement range. The low gain channels are less sensitive to the measured signal and

133 can be used to measure the stronger signal of larger particles. In accordance, the high gain channels

134 are more sensitive to the measured signal, and can be used to measure the weaker signal of smaller

135 particles. The optical head of the SP2 is shown schematically in fig. 1(b).

136   In this study, we utilize signals from four channels of the SP2: two of them measure the scattering

137 signals and another two measure the incandescent light between 350 nm and 800 nm. The peak height

138 (*H*) of the incandescence signals is used to infer whether the sampled aerosol contains the black carbon

139 (BC). If the *H* of the incandescence signal is larger than 500, the sample aerosol contains the BC and

140 the scattering signals should deviate from the signals of pure scattering aerosol. Those sample aerosols

141 are not considered when dealing with the aerosol scattering signals. This is achieved by just studying

142 the signals when the particle are recognized as pure scattering particle.

143   Despite that some aerosol particles are internally mixed with a small BC core, whose

144 incandescence signal is below the detection threshold of SP2, we will demonstrate that these particles

145 have little influence on the retrieved aerosol RRI. At the same time, there are some weakly absorbing

146 organic components that absorb light intensity in the near infrared range, which were termed as brown

147 carbon (BrC). These BrC components have ignorable influence on the retrieving of aerosol RRI, which

148 will be discussed in detail in section 4.2. Thus, the imaginary part of complex refractive index is set to

149 be zero in the following discussion.

150 **3 Methodology**

151 **3.1 Scattering intensity measured by the SP2**

152 From fig. 1(b), the APDs of the SP2 receive signals that were scattered by the sampled aerosols in

153 a certain small range at 45° and 135°. Thus, the scattering intensity (S) measured by the APD can be

154 expressed as:

$$S = C_0 \cdot I_0 \cdot \sigma \cdot (PF_{45^o} + PF_{135^o}) \qquad (6)$$

156 where I_0 is the laser's intensity; σ is the scattering coefficient of the sampled aerosol, PF_{45^o} and

157 PF_{135^o} are scattering phase function at 45° and 135° respectively of the sampled aerosols; and C_0 is

158 a constant that is determined by the distance from the aerosol to the APD and the area of the APD. The

159 scattering intensity of the aerosol is recorded as the H of the scattering signals in SP2. The following

160 calibration studies show that the scattering intensity S is highly related the H measured by SP2.

161 Therefore, the SP2 can be used as a powerful tool to measure the scattering signals of the sampled

162 aerosols, thus determining the corresponding scattering intensity.

163 Based on the Mie scattering theory, the scattering coefficient σ can be calculated by integrating

164 the square of scattering intensity function $Q(\theta, x, RRI)$ from 0° to 180°. Angle θ is defined as the

165 angle between the light incident direction and scattering light direction. The size parameter x is defined

166 as $x = \frac{\pi D_p}{\lambda}$, where λ is the light incident wavelength. The scattering phase function can be directly

167 derived from $S(\theta, x, m)$, too. Therefor, the σ, PF_{45^o} and PF_{135^o} in equation 6 are determined by

168 the Dp and RRI of the aerosol. The amount of scattering signals from the sample aerosol varies with

169 the aerosol Dp and RRI (Bohren and Huffman, 2007). The scattering intensity at different aerosol

170 diameters and RRI is calculated based on equation 6 and shown in fig. 2. The C_0 is assumed to be 1

171 here. From fig. 2, we can see that the aerosol scattering intensity increases monotonously with the

172 increasing aerosol RRI at a given Dp, which makes it possible to retrieve the aerosol RRI with given

173 Dp and the scattering intensity.

174   Bridging the scattering H values measured by the SP2 scattering channel and the scattering

175   intensity S defined by equation 6 is achieved by calibrating the SP2 with ammonium sulfate. The

176   instrument setup of the calibration procedure is the same as that described in section 2.1. The diameters

177   of the aerosols passing through the DMA are manually changed from 100 to 450 nm with a step of 10

178   nm. For each diameter, the scattering H value and incandescence signal of every particle are analyzed.

179   When calibrating, there is no aerosol whose incandescence signal exceeds 1000 (This value depends

180   on the stability of the instrument and working conditions. It can be different for different instrument),

181   which means that the SP2 works stably and the incandescence signal channel can well distinguish the

182   BC containing aerosols. With the calibration, the relationship between the measured H and

183   theoretically calculated S can be determined.

184   The procedure of retrieving the RRI are summarized as follows: (1) measuring the scattering H

185   values at a given Dp; (2) transferring the H into to S by the established relationship from calibration;

186   (3) calculating the refractive index with the given Dp and S by using equation 6.

187   **3.2 Multiple Charging**

188   Fig. S1 gives the aerosols scattering H probability distribution under different aerosol diameters.

189   For each diameter, the distributions of the scattering H may have more than one mode for both the high

190   gain and low gain channels. The following discussions would give explanation about the multiple

191   mode distributions of H.

192   For each mode, the number of recorded aerosol particles at a given H is fit by the log-normal

193   distribution function:

194
$$N(H) = \frac{N_0}{\sqrt{2\pi}\log(\sigma_g)} \cdot exp\left[-\frac{\log(H)-\log(H_0)}{2log^2(\sigma_g)}\right] \qquad (7)$$

195   Where σ_g is the geometric standard deviation; H_0 is the geometric mean value of H and N_0 is the

196   number concentrations for a peak mode. The geometric standard deviation is highly related to the half

197   width of the transfer function (equation 3). The H_0 is further used for discussion in the following part.

198   The H_0 values of corresponding to different elementary charges are labeled with different markers

199   in fig. 3. The σ_g is fitted to be a small range at 1.182 ± 0.02 for different modes and different aerosol

200   diameters. In the following discussion, we conclude that the different H_0 values in fig. 3 represent that

201   the aerosols are charged with different number of elementary charges. Based on the Mie scattering

202   theory (Bohren and Huffman, 2007), the scattering intensity increases with increasing Dp, which imply

203   that the H_0 of the singly charged aerosol should increase with the increment of Dp. Thus, the black

204   square markers in fig. 3 represent the aerosols that are singly charged. At the same time, the

205   relationships between the H_0 and Dp can be interpolated.

206   Other colored markers represent that the aerosols have more than one charge. We calculated the

207   corresponding diameter ($\widetilde{Dp}$) of the aerosols that share the same Z_p but different charges with those

208   particles that have diameter of Dp with one charge. Then the corresponding $\widetilde{H_0}$ at $\widetilde{Dp}$ are calculated.

209   Then the relationship between $\widetilde{H_0}$ and Dp is shown in dashed line in fig. 3(a). From fig. 3(a), the

210   calculated H_0 shows good consistence with the measured H_0.

211   From the discussion above, we conclude that the SP2 can only detect those ammonium sulfate

212   aerosols with the diameter larger than 160 nm. However, the ambient aerosol RRI is always lower than

213   that of ammonium sulfate (Liu and Daum, 2008), thus the lower detecting limit of the ambient

214   scattering aerosols should be larger than 160 nm. The measured H_0 of the SP2 scattering low gain

215   channel signals are shown in fig. 3(b). From fig. 3(b), the same results can be deduced as those of the

216   high gain channel signals.

217   Fig. 4(a) gives the relationships between the calculated scattering intensity and the SP2 aerosol

218   scattering H_0 at different diameters. When calculating the scattering intensity, the RRI value of

219   ammonium sulfate is set to be 1.521 (Flores et al., 2009), and the C_0 in equation 6 is set to be unity.

220   The aerosol scattering intensity shows good consistence with the peak height (R^2=0.9992), which to

221   some extent reflect the high accuracy of our proposed method. When regressing the scattering intensity

222   on the measured peak height, the value 0.36 were obtained for the slope, which means that the

223   scattering intensity can be calculated by multiplying the peak height with a factor of 0.36.

224   **3.3 Validation of the calibration**

225   Ammonium chloride is used to validate the method of deriving the RRI from SP2. The RRI value

226   of ammonium chloride is 1.642 (Lide, 2006). The scattering H of the ammonium chloride under

227   different diameters are measured and analyzed. Fig. 4(b) shows the comparison between the measured

228   scattering high gain peak heights and the theoretical peak heights at different aerosols diameters.

229   Results show that the measured peak heights and the calculated ones are well correlated with

230   R^2=0.9994, which means that the DMA and SP2 can be used to derived the aerosol RRI with high

231   accuracy.

232   Fig. S2 gives the corresponding results of the scattering low gain channel. In fig. S2, the

233   relationship between the aerosol scattering peak height of the low gain channel and the scattering

234   intensity is determined. At the same time, the comparison between the measured peak height and the

235   calculated peak height shows good consistence too.

4 Results and Discussion

4.1 Field Measurements

238   Figure 5 shows the measured average probability distribution of the ambient size-resolved RRI

239   and the measured mean PNSD over two hours during the measurement. From fig. 5, we can see that

240   the derived RRI is 1.46 ± 0.02 and doesn't vary significantly with diameter between 199 nm and 436

241   nm. The aerosol chemical component may not vary significantly for different diameters during the

242   measurement. Another field measurement shows that the measured RRI varies significantly from 1.47

243   at 198 nm to 1.54 at 450 nm as shown in Fig. S4 in supplementary part.

244   The measured aerosol PNSD during the measurement has a maximum of 26400 #/cm^3 at 107 nm.

245   The mass concentration of the BC measured by the SP2 is 6.31 μg/m^3. Based on the measured PNSD

246   and the measured RRI, the size distribution of the scattering coefficient is calculated based on the Mie

247   scattering theory. The results in fig. 5 show that the measured RRI diameter range covers most of the

248   aerosol that contributes a fraction of 0.63 to the aerosol scattering properties with integrated scattering

249   coefficient at 385 Mm^{-1}. Thus, the derived size-resolved RRI of this range is representative of the

250   ambient aerosols scattering properties.

4.2 Uncertainty analysis

4.2.1 Uncertainties from SP2

253   The factors that influence the accuracy of retrieving RRI include the aerosols scattering *H*

254   measured by SP2 and the aerosol diameter selected by DMA.

255   The uncertainties of the selected diameter by DMA are well characterized based on equation 2 and

256   3. The uncertainties from the DMA transfer function can be avoided by fitting the scattering *H* using

257   the log-normal distribution function. However, the uncertainties of the measured H from the SP2

258   remain unknown. The half width $(\Delta Z_p/Z_p)$ of the transfer function is 0.1 times the scanning diameter,

259   which means that the geometric standard deviation of the aerosol PNSD selected by the DMA is

260   estimated to be 1.102. At the same time, the measured geometric standard deviation of the measured

261   *H* mode by SP2 is 1.182. Thus, the additional broadening by the H distribution is 1.073, which implies

262   that the geometric standard deviation of the measured *H* from the SP2 is estimated to be 1.073, whose

263   corresponding uncertainties is 6.8%.

264   The uncertainties of the retrieved RRI to the variations in the measured *H* are analyzed. Firstly,

265   we calculated the theoretical scattering intensity that can be measured by the SP2 for a given aerosol

266   diameter and RRI. The scattering intensity are changed by $\pm 6.8\%$ and the corresponding RRI can be

267   derived using the given aerosol diameter and changed scattering intensity. Finally, the derived RRI are

268   compared with the given aerosol RRI. The uncertainties are analyzed for different aerosol diameter

269   and different RRI. The corresponding results are shown in fig. 6. The variations in RRI increase with

270   the increment of RRI but decrease with the increment of the *Dp*. For most ambient aerosols, the RRI

271   ranges from 1.4 to 1.5 and corresponds to a variation in RRI of 0.015.

272   Table 1 lists the retrieved ammonium chloride RRI under different diameters. The absolute

273   difference between the retrieved RRI and theoretical values is always smaller than 0.02 regardless of

274   the particle diameter, which means that the measured RRI is in line with the theoretical one. Thus, we

275   conclude that the uncertainty of the retrieved RRI is within 0.02 due to the uncertainties of SP2

276   measurement.

277   **4.2.2 Uncertainties due to BC exists**

278   There are some particles with a small soot core and the incandescence signal is below the detection

279   threshold of SP2. The derived aerosol RRI should be influenced by small soot core. Uncertainties

280   might be resulted when deriving the RRI for these BC-contained aerosols. With the calibration of the

281   SP2 with Aquadag soot particles, we concluded that the SP2 can't detect the soot particles lower than

282   80 nm, which is shown in detail in supplementary material in section S3.

283   We derived the aerosol equivalent refractive index when the aerosol have BC cores lower than 80

284   nm with two steps. The scattering strength of the BC-containing aerosols are first calculated based on

285   Mie scattering theory. Then the scattering strength are used to deriving the equivalent refractive index

286   with assuming that the BC-containing aerosols are pure scattering aerosols.

287   Monte Carlo simulations were applied to investigate the influence of the BC core on the retrieved

288   ambient aerosol RRI. Firstly, aerosol with diameter between 200 nm and 500 nm was chosen. Then

289   the core diameter are random determined lower than 80 nm. The core diameters flow the log-normal

distribution with the mean core diameter of 120 nm (Raatikainen et al., 2017). When calculating the scattering strength, the complex refractive index of the core 1.8+0.54i (Zhao et al., 2018) is used. The complex refractive of the shell adopts the measured mean values (1.46+0i) during the field measurements. The scattering strength can be calculated with the above information. With the calculated scattering strength, the equivalent real part of the refractive index (RRI) can be derived with assuming that the aerosols are pure scattering aerosols. If the core diameter is 0, then the derived aerosol equivalent aerosol RRI should be 1.46.

For each aerosol diameter, the Monte Carlo simulations were conducted for 10000 times. Fig. 7(a) gives the retrieved aerosol equivalent RRI at different diameters. Results show that the retrieved aerosol equivalent RRI are larger than 1.46 for all of the given aerosol diameters. When the aerosols have BC core, the scattering strength are larger than that of pure scattering aerosols with the same aerosol diameter. The derived mean equivalent RRI tend to be closer to 1.46 when the aerosol diameter are larger, where the BC core contributes less and the influence of the BC core are be smaller. The derived mean aerosol equivalent RRI is 1.47 and 1.462 at 200 nm and 500 nm respectively. At the same time, the uncertainties associated with the equivalent RRI are larger when the aerosol diameter are smaller. We conclude that the uncertainties associated with BC core are smaller than 0.01 when the aerosol diameter are larger than 250 nm. The maximum of the difference of the derived RRI is 0.02.

4.2.3 Uncertainties from BrC

There are some BrCs that absorb the light intensity in the near infrared range. The imaginary part of the refractive index at a given wavelength λ (k_λ) of the BrC can be calculated as:

$$k_{\lambda 1} = k_{\lambda 2} \times (\frac{\lambda 2}{\lambda 1})^w \qquad (8)$$

Where w is defined by mass of BC to organic aerosol ratio (R) (Saleh et al., 2015)with:

$$w = \frac{0.21}{R+0.07} \qquad (9)$$

Based on the work of Saleh et al. (2015), the k_{550} can be expressed as:

$$k_{550} = 0.016 \times log_{10}(R) + 0.04 \qquad (10)$$

The values R ranges between 0.09 and 0.35 for different types of aerosols (Saleh et al., 2015). Based on equation (8), (9) and (10), the k_{1024} ranges between 0.01 and 0.024. The maximum value 0.024 is used for further analysis.

The uncertainties of the retrieved RRI when ignoring the effect of BrC are analyzed. Firstly, The scattering light intensity at a given diameter with a refractive index of $1.46 + 0.024i$ is calculated using the Mie model. Then the corresponding RRI are retrieved using given diameter and the calculated light intensity with assumption that these are pure scattering aerosols. The retrieved aerosol RRI values for different aerosol diameter are shown in fig. 7(b). For the light absorbing particles, their scattering light intensity is smaller than that of the pure scattering particles with the same diameter and RRI. Therefore, the retrieved aerosol RRI is underestimated for most of the conditions. The differences between the given RRI value (1.46) and retrieved RRI value are lower than 0.006 for all of the diameters as shown in fig. 7(b). The BrC component has little influence on the retrieved aerosol RRI.

4.2.4 Overall of the uncertainties

Monte Carlo simulations were conducted to study the influence of the above three uncertainty sources. Four steps are involved in the Monte Carlo simulations. First, the core diameter of an aerosol particle at a given diameter are randomly given with the core diameter flowing the log-normal distribution with the mean core diameter of 120 nm (Raatikainen et al., 2017). The refractive index of the core is set to be the same as that in section 4.2.2. The RRI of the shell uses the measured mean value 1.46. The imaginary part of the shell is determined randomly with a mean value of 0.023. Second, the light scattering intensity can be calculated using the Mie model and the information in step one. Then the light scattering intensity was randomly changed with uncertainties of 6.8%. Finally, the changed light scattering intensity are used to derive the aerosol RRI with the given diameter and assumption that the particles are pure scattering particles.

The aerosol diameters were changed from 200 nm to 500 nm, and the simulations were conducted for 10000 times for each diameter. The overall uncertainties are shown in fig. 7(c). The uncertainties from SP2 instrument measurement don't lead to bias of the retrieved aerosol RRI. When the aerosol diameter is lower than 300 nm, the influence of the BC core is more important than the influence of BrC. The retrieved RRI tend to be overestimated when the aerosol is lower than 300 nm. When the aerosol diameter is larger than 300 nm, the influence of BrC domains and the retrieved aerosol RRI are underestimated. However, the bias caused by BC and BrC are all the way lower than 0.01. For most of the conditions, the retrieved aerosol RRI are within the range of 1.46 ± 0.02. Thus, we conclude that the uncertainty of the retrieved RRI is 0.02 with considering all of the factors.

5 Conclusions

Knowledge on the microphysical properties of ambient aerosol is import for better evaluating their radiative forcing. The aerosol RRI is a key factor that determines the aerosol scattering properties. In this study, a new method to measure the ambient aerosol RRI is developed by synthetically using a DMA in tandem with a SP2. This method can continuously measure the size-resolved RRI over a wide range between 198 nm and 426 nm. At the same time, it is free from the influence of the BC containing aerosols.

The basic principle of measuring the size-resolved RRI is to select the aerosols at a certain diameter by the DMA and measure the corresponding scattering intensity by the SP2. The relationship between the aerosols scattering intensity and the peak height of the scattering signal channels are determined by calibrating the SP2 using ammonium sulfate (RRI=1.521).

The method is validated by measuring the size-resolved RRI of the ammonium chloride with the RRI value of 1.642 as sample aerosol and the corresponding derived value is 1.642 ± 0.02. There are three factors that influence the accuracy of derived aerosol RRI. The measured scattering intensity by SP2 has an uncertainty of 0.68%, which can lead to the uncertainties of the derived RRI values less than 0.15. There are some particles with a small soot core and the incandescence signal is below the detection threshold of SP2. The light scattering intensity of these particles increases compared with that of the pure scattering particles with the same aerosol diameters. The retrieved aerosol RRI values can be overestimated by up to 0.02. Some BrCs absorb the light intensity in the near infrared range. The corresponding scattering intensity is weaker than that of pure scatter particles for the same diameter and the retrieved aerosol RRI value can be underestimated by up to 0.006. Based on Monte Carlo simulations, the uncertainty of the retrieved RRI is 0.02 with considering all of the factors.

This instrument is employed at a field measurement at the AERONET PKU stating, the size-resolved RRI of the ambient aerosols is 1.46 and doesn't show significant variation among the diameter. The corresponding aerosol diameter range, which can be detected by SP2 to derive the RRI, covers most of the aerosol scattering. Thus, the derived size-resolved RRI of this range can be used as a good representative of the ambient aerosols scattering properties.

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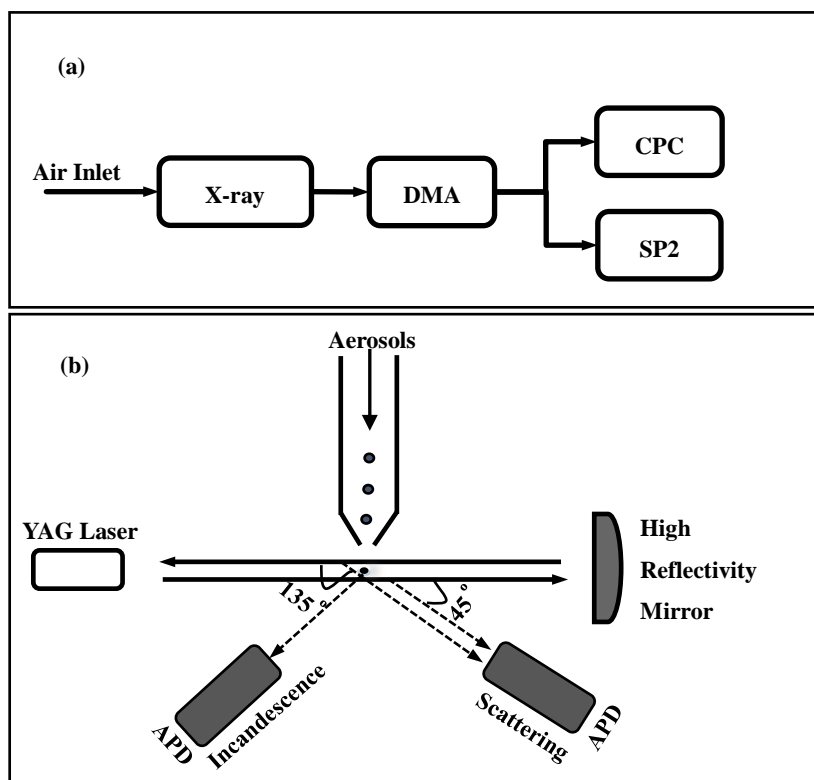536 10.1007/s11430-015-5146-y, 2015.

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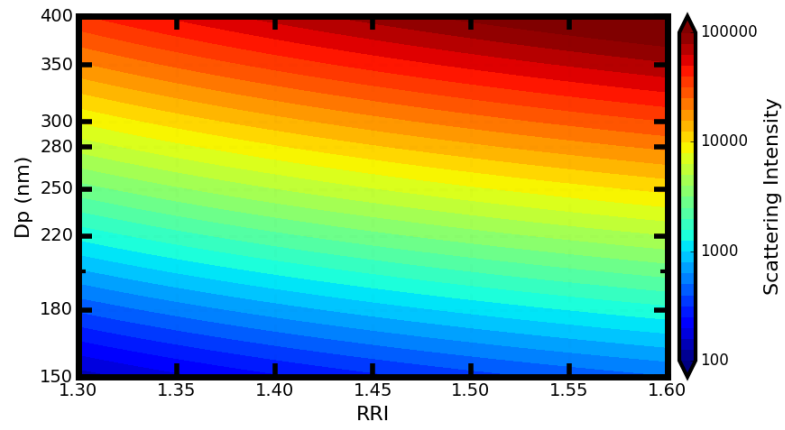
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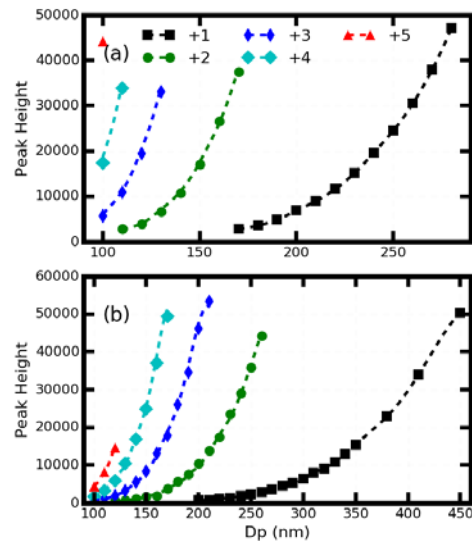546 Chemistry and Physics, 18, 9049-9060, 10.5194/acp-18-9049-2018, 2018.

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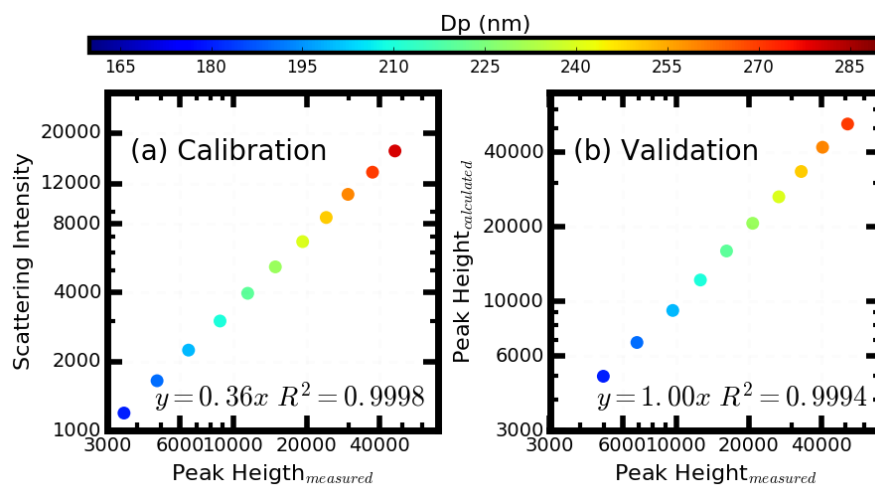**Figure 1.** (a) Schematic of the measurement system. (b) Diagram of SP2 Chamber.

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Figure 2. The distribution of the aerosols scattering intensity at different Dp and different RRI.

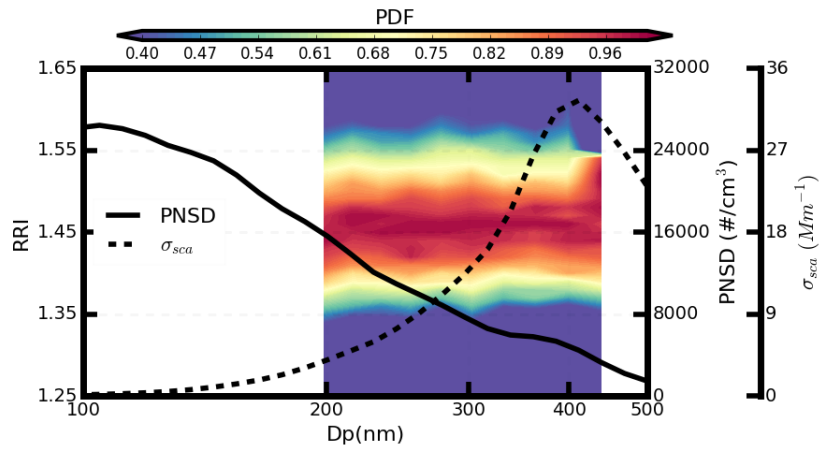**Figure 3.** The geometric mean peak height for different diameters of the high gain channel. The markers gives the measured values and the dotted line shows the theoretically calculated value. Different colors represent the different number of elementary charges.
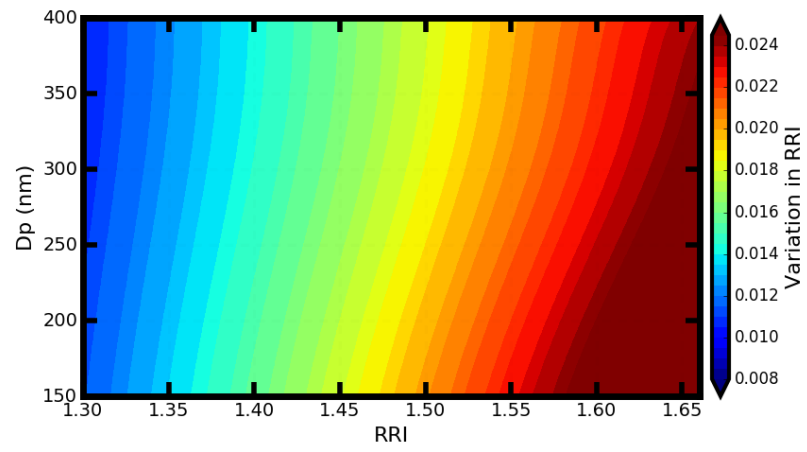
Dp (nm)

(a) Calibration

$y = 0.36x \ R^2 = 0.9998$

Scattering Intensity

Peak Heigth$_{measured}$

(b) Validation

$y = 1.00x \ R^2 = 0.9994$

Peak Height$_{calculated}$

Peak Heigth$_{measured}$

Figure 4. (a) the relationship between the scattering peak height from the SP2 high gain scattering channel when calibrating by using the ammonia sulfate and (b) the comparison between the measured scattering peak height from SP2 high gain scattering channel using the ammonia chloride and the calculated scattering peak height using the Mie scattering theory. Different colors represents the results at different diameters.
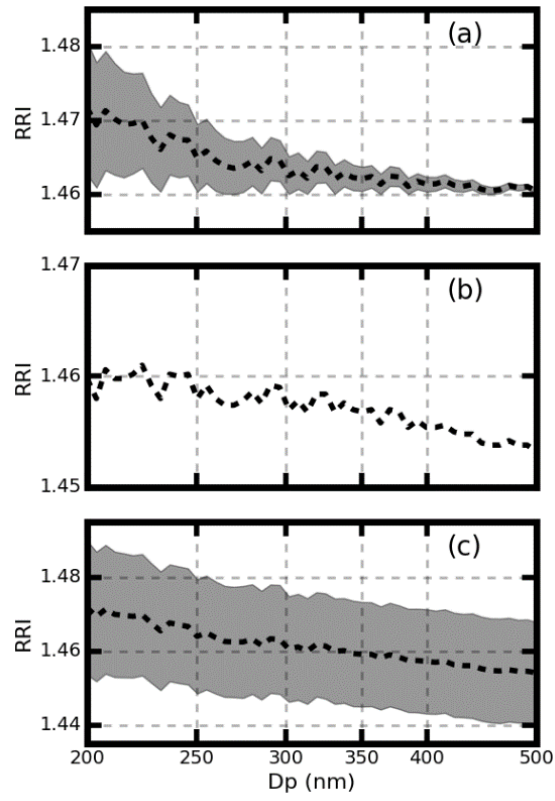
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Figure 5. The measured probability of the size-resolved RRI (the filled color), the measured mean PNSD (the full line) and the mean scattering size distribution (the dotted line).

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Figure 6. The variation in RRI for different kinds of aerosols that have different diameters and different RRI.

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574   **Figure 7.** The retrieved aerosol RRI at different aerosol diameter. The filled color represents the 5th

575   and 95th percentiles.

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577

578

Tabel 1. The retrieved RRI and the absolute difference between the retrieved RRI and the theoretical
RRI for different ammonia chloride diameters.

Dp(nm)	160	170	180	190	200	210	220	230	240	250	260	270
RRI	1.654	1.650	1.651	1.643	1.656	1.645	1.633	1.626	1.634	1.626	1.624	1.625
Difference	0.012	0.008	0.009	0.001	0.012	0.003	0.009	0.016	0.008	0.016	0.018	0.017

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