**Assimilation of GNSS tomography products into WRF using radio occultation data assimilation operator**

Natalia Hanna1, Estera Trzcina2, Gregor Möller1, Witold Rohm2, Robert Weber1

1Department of Geodesy and Geoinformation, TU Wien, Vienna, 1040, Austria

5 2Institute of Geodesy and Geoinformatics, Wroclaw University of Environmental and Life Sciences, Wroclaw, 50-357, Poland

*Correspondence to*: Natalia Hanna (natalia.dymarska@geo.tuwien.ac.at)

**Abstract**. From Global Navigation Satellite Systems (GNSS) signals, accurate and high-frequency atmospheric parameters can be determined in all-weather conditions. GNSS tomography is a novel technique that takes advantage of these

10 parameters, especially of slant troposphere observations between GNSS receivers and satellites, traces these signals through a 3D grid of voxels and estimates by an inversion process the refractivity of the water vapour content within each voxel. In the last years, the GNSS tomography development focused on numerical methods to stabilize the solution, which has been achieved to a great extent. Currently, we are facing new challenges and possibilities in the application of GNSS tomography in numerical weather forecasting, the main research objective of this paper. In the first instance, refractivity fields were

15 estimated using two different GNSS tomography models (TUW, WUELS), which cover the area of Central Europe during the period of 29 May - 14 June 2013, when heavy precipitation events were observed. For both models, Slant Wet Delays (SWD) were calculated based on estimates of Zenith Total Delay (ZTD) and horizontal gradients, provided for 72 GNSS sites by Geodetic Observatory Pecny (GOP). In total, three sets of SWD observations were tested (set0 without compensation for hydrostatic anisotropic effects, set1 with compensation of this effect, set2 cleaned by wet delays outside

20 the inner voxel model). The GNSS tomography outputs have been assimilated into the nested (12- and 36-km horizontal resolution) Weather Research and Forecasting (WRF) model, using its three-dimensional variational data assimilation (WRFDA 3DVar) system, in particular its radio occultation observations operator (GPSREF). As only total refractivity is assimilated in GPSREF, it was calculated as the sum of the hydrostatic part derived from the ALADIN-CZ model and the wet part from the GNSS tomography. We compared the results of the GNSS tomography data assimilation to the radiosonde

25 (RS) observations. The validation shows the improvement in the weather forecasting of relative humidity (bias, standard deviation) and temperature (standard deviation) during heavy precipitation events. Future improvements to the assimilation method are also discussed.

**1 Introduction**

Global Navigation Satellite Systems (GNSS) measurements of the microwave signals transmitted between the

bent, attenuated and delayed in two atmospheric layers, namely the ionosphere and the troposphere (Böhm and Schuh,

2013). As the effects caused by both of them can be distinguished, the latter is referred to as the tropospheric delay and stands for the signal delay integrated over the whole ray path (Bevis et al., 1992; Kleijer, 2004; Mendes, 1999). In t he case of a dense network of ground-based receivers, the tropospheric delay can be estimated precisely from differenced GNSS

5 measurements. Therefore, it is usually modelled in a vertical column above each station as Zenith Total Delay (ZTD) – i.e. the observed delay is mapped to the zenith direction and integrated over a certain period of time (Dach et al., 2007). The tropospheric delay is related to the weather conditions in the vicinity of the GNSS station (pressure, temperature, and humidity), therefore it carries valuable meteorological information (Guerova et al., 2016).

In the last years, a huge effort was made to utilize GNSS measurements for operational weather forecasting; as a

10 result, several projects have been conducted to establish processing centres for a continuous estimation of the tropospheric state using GNSS products (Elgered, 2001; Haase et al., 2001; de Haan et al., 2009; Dousa, 2010 ; Karabatić et al., 2011). Besides from ZTD, another tropospheric parameter, namely an Integrated Water Vapour (IWV) has been derived and assimilated into the Numerical Weather Prediction (NWP) models (Falvey and Beavan, 2002; Gutman et al., 20014). This parameter is calculated based on the wet part of ZTD (i.e. Zenith Wet Delay, ZWD), and is strictly related to the amount of water

15 vapour in the troposphere, thus it is beneficial for meteorological systems since a precise knowledge about humidity in the neural atmosphere is crucial for accurate weather forecasting (Andersson, 2016). Studies have shown that assimilation of GNSS products, either ZWDs or IWVs, into operational NWP models has always a positive, at least a neutral impact on the forecast of humidity, rain location, and accumulated rain amount (Inness and Dorling, 2012; Poli et al., 2007; Bennitt and Jupp, 2012). Cucurull et al., 2004; Nakamura et al., 2004; Boniface et al., 2009; Tilev-Tanriover and Kahraman, 2014

20 demonstrated that the positive impact is most significant during heavy precipitation or storms events.

However, as the tropospheric parameters integrated into a zenith direction reflect horizontal changes in meteorological parameters, they do not provide information about a vertical structure. In order to make better use of information that is contained in the raw GPS measurements, ZTD can be mapped back into the direction of the satellites, using mapping functions and additional information about azimuthal asymmetry (horizontal gradients of the troposphere)

25 (Niell, 1996; Böhm and Schuh, 2004; Böhm et al., 2006). This process leads to the calculation of a Slant Total Delays (STD) for each GNSS satellite-receiver pair (along the individual signal path). GNSS slant delays represent better the state of the troposphere, especially in case of strong horizontal humidity gradients during severe weather phenomena in frontal regions (Koch et al., 1997). Operational assimilation of STDs into the MM5 system has shown a positive impact on the representation of water vapour field and precipitation; also a reduction of the spin-up time of the model was noticed (Bauer

30 et al., 2011). An assimilation experiment carried out during a local heavy rainfall event indicated that GPS -STD assimilation improved rainfall forecast significantly in terms of timing and intensity, when compared to a GPS-ZTD and GPS-IWV assimilation only (Kawabata et al., 2013).

Fostered by the increasing number of GNSS satellites and the build-up of densified ground-based GNSS networks

from GNSS tropospheric parameters – also known as GNSS tropospheric tomography. This technique is one of the most promising since it uses Slant Wet Delay (SWD) observations together with the principles of tomography to obtain not only the amount of water vapour, but also its distribution in space and time. For the inversion of the equation system, Flores et al. (2000) were using Singular Value Decomposition (SVD) methods together with constraints imposed on the system of

5 equations (smoothing, boundary, and vertical constraints). In the following years, a number of refinements in the technique have been implemented. Inclusion of supplementary wet refractivity data from external data sources into a functional model (Bender et al., 2011; Rohm et al., 2014; Benevides et al., 2015; Möller, 2017) resulted in stabilization of the solution without need of smoothing constraints, which is especially important during severe weather phenomena with high variability of water vapour in the troposphere. A new approach of parametrization of the domain, using trilinear and spline functions

10 instead of constant values inside each volume element (voxel) showed the substantially smaller maximum error of the solution (Perler et al., 2011; Ding et al., 2018). Another approach, using the Kalman Filter instead of Least Squares (Rohm et al., 2014), led to better responsiveness to the severe weather. A number of experiments have been carried out showing positive results for detecting heavy precipitation events (Troller et al., 2006; Rohm and Bosy, 2009; Perler et al., 2011; Rohm et al., 2014; Adavi and Mashhadi-Hossainali, 2015; Chen et al., 2017). Besides the development of technical aspects,

15 which was widely performed in the last years, GNSS tomography should be also tested on its ability to fulfil the requirements of up-to-date weather prediction methods, i.e. on its suitability for assimilation into the NWP models (Innes and Dorling, 2012). The first research on this topic was carried out by Möller et al. (2015). Its aim was to trans form wet refractivities derived by GNSS tomography into humidity and temperature profiles, and then assimilate them into the AROME NWP model for a selected test period. Verification was made using surface station measurements, radio sounding

20 data, and precipitation analysis. Tomography data assimilation results compared with the results of ZTD data assimilation, indicated a significantly larger impact of the new technique, especially within the first 6 to 12 hours of the forecast (a drying effect in the AROME forecast field). As the results clearly showed the potential of 3D refractivity observations, another case study has been performed by Trzcina and Rohm (2018), concerning assimilation of a Near Real-Time (NRT) tomographic solution into WRF model using an operator dedicated to radio occultation (RO) observations of total refractivity.

25 Comparison with several external observations has shown the positive impact within the 6 to 12 hours of the forecast of humidity in autumn, but not in summer. Such assimilation-oriented tomography data analyses are essential for further research on the utilization of GNSS troposphere tomography output as a valuable data source for NWP forecasts.

In this work, we present the assimilation of a 3D wet refractivity field derived by GNSS tomography technique, into the WRF model using the GPSREF observation operator. The experiment was performed during a heavy precipitation event

30 in Central Europe in order to investigate the impact on the weather forecast. Since two tomographic models (TU Wien, WUELS) and three different approaches of SWD data calculation were used, the results of several tomographic approaches were discussed in terms of assimilation impact. The structure of the paper is as follows: Section 2 describes the derivation of slant wet delays from GNSS measurements. Section 3 is dedicated to the methodology of GNSS troposphere tomography and provides a detailed description of the models used for tomography processing. Section 4 introduces the methodology of

tomographic data assimilation into the WRF model; followed by a description of the meteorological situation under study in Section 5. In section 6 and 7, the results of tomography and of the assimilation experiments are analysed. The main conclusions are presented in section 8.

**2 GNSS slant wet delays**

5 GNSS tropospheric estimates (1h ZTDs and 6h horizontal gradients), as provided by Geodetic Observatory Pecny (GOP) for 72 GNSS sites in Central Europe (see Fig. 3), were utilised for the computation of Slant Wet Delays (SWDs). For more details about the GNSS processing strategy at GOP, the reader is referred to (Dousa et al., 2016, Section 5.1).

In a first step, the tropospheric parameters were linearly interpolated over time to 0, 6, 12, 18 UTC. Afterwards, for each epoch the Zenith Hydrostatic Delay (ZHD) was computed by means of Saastamoinen model (Saastamoinen, 1972) and

10 removed from the ZTD estimates. The required air pressure values have been derived from meso-scale ALADIN-CZ 6 hour forecast data, as provided by the Czech Hydrometeorological Institute (CHMI), and spatially interpolated to each GNSS reference site.

��𝐷 = ��𝐷 − ����. (1)

The Zenith Wet Delays (ZWDs) and the horizontal gradients (GN, GE) were mapped into direction of the GPS and

15 GLONASS satellites in view above 3° elevation angles. Therefore and for highest consistency with GNSS data processing,

the VMF1 mapping function (Böhm et al., 2006) was used for mapping (𝑚�� ) of the ZWDs and the (Chen and Herring,

1997) gradient mapping function (����� ) was applied for mapping of the horizontal gradient parameters as follows:

��𝐷 = ��𝐷 ∙ 𝑚�� (��) + �𝑁 ∙ ����� (��) ∙ cos(��) + �� ∙ ����� (��) ∙ sin(��) (2)

The elevation (��) and azimuth angles (��) of each satellite in view have been computed from broadcast ephemerides. The

20 resulting dataset of SWDs is hereafter referred to as ‘set0’.

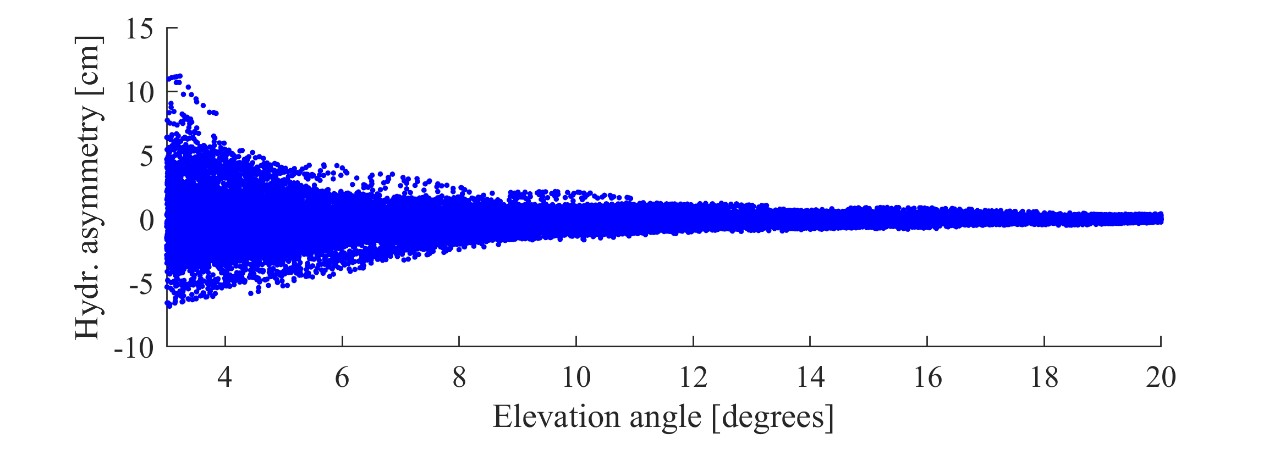
Based on set0 two additional, more refined datasets were derived, whereby ‘set1’ compensates for hydrostatic anisotropic effects, and ‘set2’ was cleaned by wet delays ‘outside’ the inner voxel model (see Table 3 for further details about the voxel model). In both cases, 2D ray-tracing through ALADIN-CZ model level data (6 hour forecast data) was carried for the determination of the delay corrections. For more details about the applied ray-tracer, the reader is referred to (Möller,

25 2017).

For set1, i.e. for compensation of hydrostatic asymmetric effects, ray-traced delays were determined for each GNSS satellite in view, and for equidistant azimuth angles (separated by 30°). From the obtained set of ray-traced hydrostatic delays, the mean hydrostatic delay was computed and removed from the ray-traced hydrostatic delay in direction of the satellite in view. Figure 1 shows the resulting hydrostatic asymmetric delay, obtained for all observations within the study period (29 May –

14 June, 2013). In a final step, the hydrostatic asymmetric delays were removed from set0. Assuming that the ALADIN-CZ

model pressure error is small, the obtained SWDs (set1) are widely free from hydrostatic effects.



**Figure 1: Hydrostatic component of azimuthal asymmetry, derived from the ALADIN-CZ model level data by ray-tracing.**

5 Furthermore, for set2 the ray-tracer was applied for determining intersection points between the GNSS signal paths and the inner voxel model boundaries. In case, the signal enters the inner voxel model not through the top layer but through any lateral surface, the outer tropospheric wet delay (between intersection point and the upper rim of the troposphere at about

13.5 km height above mean sea level) is determined by ray-tracing and removed from its equivalent in set0.

**3 GNSS tomography**

10 For conversion of precise integral measurements (like SWDs) into three-dimensional structures, a technique called tomography has been invented. According to Iyer & Hirahara (1993) the general principle of tomography is described as follows:

�� = ∫�

�(�) ∙ ��

(3)

where �� is the projection function, �(�) is the object property function and �� is a small element of the ray path � along

15 which the integration takes place. In order to adapt the tomography principle for GNSS tropospheric delay parameters and to

find a solution for Eq. (3), first the troposphere is discretised in volume elements, named voxels, in which the index of

refraction is assumed as constant and the ray path is assumed as straight line. Further, by replacing �� with ��𝐷 and �(�) by wet refractivity (��� ), the basic function of GNSS tomography reads:

��𝐷 = ∑𝑚

��=1

���, ∙ �𝑘

(4)

20 whereby ���, is the constant wet refractivity and �𝑘 is the ray length in volume element k. In matrix notation Eq. (4) reads:

where ��𝐷 is the observation vector of size (l, 1), 𝑁� is the vector of unknowns of size (m, 1) and � is a matrix of size

(l,m) which contains the partial derivatives of the slant wet delays with respect to the unknowns. Since Eq. (5) is linear, the

partial derivatives of SWD are the ray lengths (�𝑘 ) in each voxel k. A solution for � is obtained by inversion of matrix � .

𝑁� = �−1 ∙ ��𝐷 (6)

5 Unfortunately in GNSS tomography, matrix � is usually not of full rank (i.e. has zero singular value). In consequence Eq.

(6) is ill-posed, i.e. not uniquely solvable. In order to find a solution for Eq. (6), truncated singular value decomposition

(TSVD) methods are applied (Xu, 1998). Therefore, matrix � is split into three components:

� = � ∙ � ∙ � � (7)

where � and � are orthogonal matrices and matrix � (l, m) is a diagonal matrix. The first m diagonal elements of � are the

10 singular values (���, ), all other elements are zero. The ratio between largest and smallest singular value defines the condition

number ��(�) of matrix � .

��( � ) =

|����|

|��𝑖� |

(8)

A condition number near ‘1’ indicates a well-conditioned matrix, a larger condition number indicates an ill-conditioned problem. As consequence the tomography solution is sensitive to observation errors, changes in the observation geometry

15 but also to the solving strategy and its parameters defined within the analysis. In the following, the two processing strategies as used for parameter estimation are described more in detail. The general, underlying tomography settings and input data are summarised in Table 3.

**3.1 Least-squares solution (TUW)**

The TU Wien tomography solution was calculated using the ATom software package (Möller, 2017). It is based on a

20 least-squares adjustment, whereby each observation type is processed individually as partial solution (see Möller, 2017 Eq.

7.46 ff.). This approach allows for proper Truncated Singular Value Decomposition (TSVD), whereby an eigenvalue threshold of 0.006 km², found by l-curve technique, was set for singular value selection.

Weighting of the GNSS slant observations was based on the elevation angle (sin⁡2 ��), with a standard deviation of 2.8

mm for the zenithal observations (ZTD). A height-dependent weighting model was applied to the a priori wet refractivity

25 information, whereby the height-dependent standard deviations were computed by comparison of the a priori data with radiosonde data and interpolated to the 15 height levels of the voxel model (see Table 1).

The first two TU Wien solutions are based on SWD set0 and set1. Therefore, the voxel model boundaries were defined according to Table 3 and wet refractivity was estimated in both, the inner and outer domain. In consequence, all available SWDs could be used for estimation of the wet refractivity fields (sol0 and sol1). The third TU Wien solution is based on the

in preparation of set2. In consequence, all available SWDs could be used and wet refractivity was estimated for the inner

voxel model (sol2). Quality control was based on analysis of the SWD residuals (�).

� = ����𝑖 − �𝑖 ∙ ��� (9)

Those residuals larger than 120 times the RMS of the residuals were discarded. The processing stopped after 10

5 iterations or before, if the change in RMS was lower than 3 percent or if the RMS was lower than 0.5 mm.

**3.2 Kalman filter solution (WUELS)**

Estimation of the wet refractivity distribution in the WUELS solution was performed using TOMO2 software

(Rohm and Bosy, 2009, 2011; Rohm, 2012, 2013; Rohm et al., 2014; Zhang et al., 2015 ), based on a Kalman filter

application. In a first step, the state vector of wet refractivity ��� and its covariance matrix � for epoch 𝑘 were updated,

10 based on the outputs form a previous epoch (𝑘 − 1):

���

(−) = Φ 𝑘 ���

𝑘

��−1

(+) (10)

�

�𝑘 (−) = Φ 𝑘 ���−1 (+) Φ 𝑘 + � ��−1 (11)

where Φ denotes a state transition matrix, indicating predicted changes of the wet refractivity between consecutive epochs; �

is a dynamic disturbance noise matrix. The state transition matrix is a diagonal matrix, set based on a priori information for

15 both epochs where:

Φ𝑘

(����𝑝𝑟 )

= ��,1

𝑘

. (12)

��,

(���

)

�𝑝��𝑘−1 ��,1

The dynamic disturbance noise matrix was set based on mean wet refractivity changes between epochs, calculated from ALADIN-CZ model data for the whole period. The noise was calculated separately for each height level of the tomographic domain (see Table 3). After the prediction step, corrections to the state vector and its covariance matrix were computed

20 from the observations. Hereby, the Kalman gain matrix K was defined as follows:

� � −1

� = �𝑘 (−)�𝑘 ( � 𝑘 �𝑘 (−) � 𝑘 + � 𝑘 )

(13)

���

(+) = ���

𝑘

(−) + �𝑘 ( ����𝑘 − � 𝑘 ���

𝑘

(−)) (14)

𝑘

�𝑘 (+) = �𝑘 (−) − �𝑘 � 𝑘 �𝑘 (−) (15)

where ��𝐷 stands for a vector of observations and � for its covariance matrix. The vector of observations consists of two

25 parts, the SWD observations and the a priori information derived from ALADIN-CZ model data. Errors of the slant delays

������ are dependent on the elevation angle 𝜀 and were calculated using the following mapping function:

𝑚 = �����𝐷 (16)

�𝑊�

sin⁡(��)

whereby ���𝑊� = 10𝑚�� is the assumed ZWD error (Kacmarík et al., 2017). Errors of the a priori information were

computed as for the TUW solution by comparison with radiosonde observations (stations 10548 and 10771), separately for

each height of tomographic domain (Table 1).

For tomography processing, all available SWD observations above 3° elevation angle were taken into account and

5 the signal paths were assumed as straight-lines. The WUELS tomography solutions (sol0 and sol1) are based on the SWD observations from set0 and set1, respectively. The voxel model boundaries were defined according to Table 3 (both inner and outer voxel model taken into account). A main quality indicator in the WUELS model was based on a comparison of the

SWD residuals (see Eq. 9). Observations with residual values �𝑖 larger than three times the standard deviation were

removed from the solution. The filter process was stopped after five iterations. Thereby, stations with a number of removed

10 observations higher than 150 (for the whole period) were rejected.

**Table 1: A priori model error (**��**) and dynamic disturbance noise values (**Q**) as obtained by comparison of the a priori model data**

**with radiosonde data for each level of the TUW and WUELS tomography model.**

height

[m]

𝑚

TUW

[ppm]

225 675 1170 1715 2313 2972 3697 4494 5371 6336 7397 8564 9848 11260 12814

4.95 4.54 5.04 5.25 4.15 5.08 3.55 2.89 2.33 1.03 0.59 0.29 0.10 0.02 0.01

𝑚

WUELS

[ppm]

10.57 5.56 5.40 5.95 5.48 4.55 4.29 3.25 2.41 1.65 1.12 0.57 0.23 0.06 0.02

�

[ppm]

8.62 5.49 5.54 5.17 4.62 4.39 3.68 2.65 1.97 1.32 0.71 0.27 0.07 0.02 0.01

**4 WRF Assimilation operator and settings**

**4.1 WRF model**

15 The Weather Research and Forecasting (WRF) model is a mesoscale numerical weather prediction system designed for both, atmospheric research and operational forecasting needs. It provides 1) two different numerical cores (the Non- hydrostatic Mesoscale Model core (NMM) for operational use and the Advanced Research WRF core (ARW) for research studies), 2) a data assimilation system, 3) a software architecture enabling parallel computation and system extensibility (Schwitalla et al., 2011).

20 In the WRF model, a nest simulation can be performed. The nest is a finer-resolution model run, which can be embedded simultaneously within a coarser-resolution (parent) model run, or run independently as a separate model forecast. The nested solution allows for the low-resolution model run within the parent domain and the high-resolution model run in the nested domain, what helps enhance the efficiency of the model and reduces the time of calculation of the high-resolution

part of the model. Nesting enables also to run the model in a high-resolution very small domain, avoiding a mismatch time and spatial lateral boundary conditions (Skamarock et al., 2008). A coarse grid and the fine grid can interact, depending on the chosen feedback option. Nested grid simulations can be produced using either 1-way nesting or 2-way nesting. In both, the 1-way and 2-way simulation modes, the fine grid boundary conditions (i.e., the lateral boundaries) are interpolated from

5 the coarse grid forecast. In a 1-way nest, the only information exchange between the grids comes from the coarse grid to the fine grid. In the 2-way nest integration, the fine grid solution replaces the coarse grid solution for coarse grid points that lie inside the fine grid. This information exchange between the grids in both directions (Skamarock et al., 2008).

In this research, the WRF model includes two domains (see Fig. 2): a parent domain (d01), which spans the area of almost the whole

Europe, with 36 km horizontal spacing, and a nested domain (d02) within the area of Central Europe, with 12 km horizontal

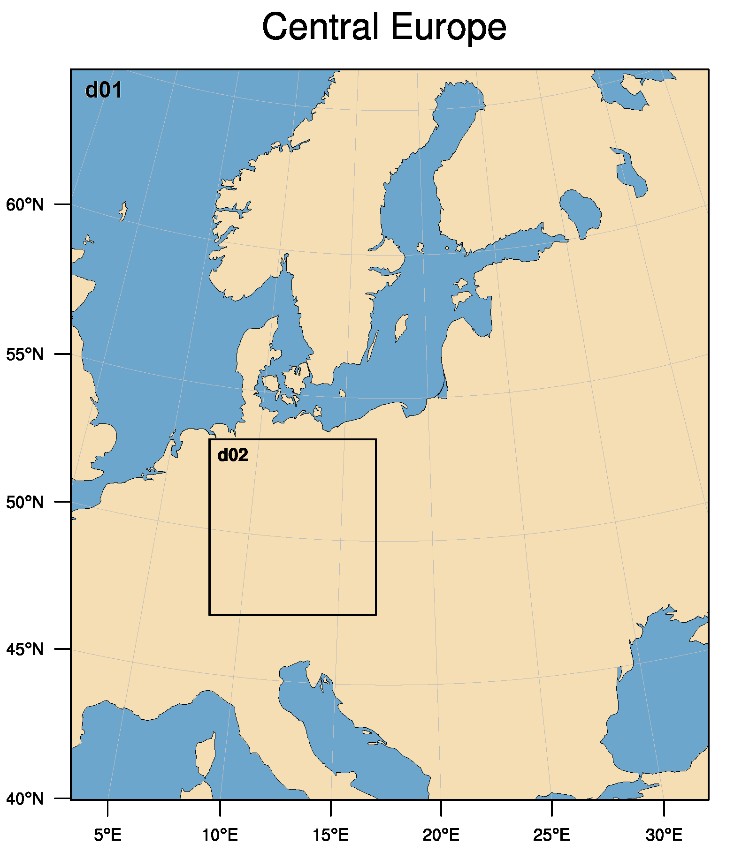
10 spacing (Fig. 3). The information between the domains flow in both directions (2-way nested run). The vertical resolution of the model in both includes 35 pressure levels, whereby the model top is defined at 50 hPa air pressure. The model background (initial

and boundary conditions) is provided by the National Centers for Environmental Prediction (NCEP) FNL (Final) operational global analysis data with 1° x 1° horizontal

resolution and 26 vertical layers from the NCEP. These data are available

on [http://rda.ucar.edu/datasets/ds083.2/.](http://rda.ucar.edu/datasets/ds083.2/)

15



**Figure 2: The geographical extensions of the WRF domains using in this research (d01 = coarse grid with 36 km horizontal spacing, d02 = fine grid with 12 km horizontal spacing).**

WRF offers multiple user-selectable physic options to represent convection, cloud microphysics, boundary-layer properties and land-surface interactions. The options typically range from simple and efficient, to sophisticated and more computationally costly, and from newly developed schemes, to well-tried schemes. In this study, the Atmospheric Boundary Layer (ABL) is parametrized with the Yonsei University (YSU) Scheme (Hong et al., 2006), which is the default scheme in

5 WRF. We use also the revised MM5 scheme for surface layer (Jimenez et al., 2012), unified Noah land surface model (Tewari et al., 2004), Dudhia scheme for shortwave radiation (Dudhia, 1989), and Kain-Fritch scheme for the cumulus parametrization (Kain, 2004).

**4.2 Assimilation operator**

Data assimilation is the technique by which observations are combined with an NWP product (the first guess or

10 background forecast) and their respective error statistics to provide an improved estimate (the anal ysis) of the atmospheric (or oceanic, Jovian, etc.) state. Variational (Var) data assimilation achieves this through the iterative minimization of a prescribed cost (or penalty) function. The aim of a variational data assimilation scheme is to find the best least-square fit

between an analysis field � and observations �(�) with an iterative minimization of a cost function �(�):

�

15 �(�) = 1 (� − � )� �−1 (� − � ) + 1 (� − �(�)) �−1 (� − �(�)). (17)

2 � � 2

In Eq. 17, � is a vector of analysis, �� is the forecast or background vector (first guess), � is an observation vector, � is the background error covariance matrix, � is an observation operator, and � is the observation covariance matrix. The observation operator �, which can be non-linear, converts model variables to observation space. Differences between the

analysis and observations/first guess are penalized (damped) according to their perceived error.

20 In order to assimilate observations into the WRF data assimilation system, a special function, i.e. data assimilation

operator (�), should be used. Although the WRF DA system does not provide a direct assimilation operator for the GNSS

tomography wet refractivity fields, it is possible to apply a radio occultation operator (GPSREF) for the GNSS tomography

output data. The GPSREF assimilation operator is used to map model variables to refractivity space (Cucurull et al., 2007):

𝑃 5

���

25 𝑁 = ��ℎ + ����� = 77.6 (� ) + 3.73 × 10

( ), (18)

� 2

where � is the total atmospheric pressure (hPa), � is the atmospheric temperature (K), and �� is the partial pressure of water vapor (hPa). The GPSREF operator enables assimilation of total refractivity (��)⁡at each observation height. Since GNSS tomography provides ����� only, the hydrostatic (dry) component of refractivity (��ℎ ) has to be modeled. Therefore we use

meteorological parameters (total atmospheric pressure and atmospheric temperature) provided by ALADIN-CZ model.

30 The ALADIN-CZ model is a local area, hydrostatic model provided by Czech Hydrometeorological Institute (CHMI).

Model simulations run at 4.7 km x 4.7 km horizontal resolution and 87 hybrid-model levels. NWM 3D analysis fields are provided in GRIB format for 00, 06, 12 and 18 UTC together with 6 hours forecast fields with one hour resolution

(Kacmarik et al, 2017). In this study, the analysis data of the ALADIN-CZ model is used to: 1) Compute pressure values at the height of GNSS station to reduce the hydrostatic part from the Slant Total Delays (STDs); 2) Compute temperature and

pressure at the height of each ����� observation in order to model the hydrostatic part of refractivity. In order to calculate the

hydrostatic component of refractivity, the meteorological parameters provided by ALADIN-CZ are interpolated to each

5 observation height. Finally, total refractivity field, i.e. the sum of ��ℎ and ����� , is assimilated.

**4.3 Assimilation settings**

The 3DVar assimilation of five sets of tomography data (TUW0, TUW1, TUW2, WUELS0, WUELS1) and the control run of the base weather forecast (without assimilation) has been performed. In order to allow the NWP model to approach its own climatology after being started from the initial conditions (NCEP final data), the assimilation was

10 performed six hours after model run (spin-up time). The analysis has been performed at 00, 06, 12 and 18 UTC. Each analysis includes 18 hours forecast with one hour resolution. Table 2 shows the data assimilation settings. In the process of assimilation, only the data from the voxels crossed by the GNSS signal were used.

**Table 2: Applied data assimilation settings.**

**Horizontal resolution**

parent domain: 36 km x 36 km nested domain: 12 km x 12 km

**Vertical layers** 35

3DVar

**Method**

**Initial and boundary conditions**

radio occultation observation operator GPSREF

NCEP FNL 1° x 1°

**Assimilation window** 1 h

00, 06, 12, 18 UTC

**Model run**

6 hours of model integration + 18 hours of forecast lead time

**5 Case study**

15 Our studies are based on the complex dataset collected within the European COST Action ES1206, as described in details by Dousa et al. (2016). The study area comprises central parts of Europe (Fig. 2). The study period (29 May to 14

June, 2013) covers the events of heavy precipitation, which finally led to severe river flooding in all catchments on the Alpine north-side (Switzerland, Austria, and southern Germany) and of the mountain ranges in Southern and Eastern Germany as well as in the Czech Republic.

20 As reported by Grams et al. (2014), the core period of the heavy precipitation occurred from 31 May 2013, 00:00

UTC to 3 June 2013, 00:00 UTC. Within these 72 hours, accumulated precipitation of 50 mm was reported in regions of

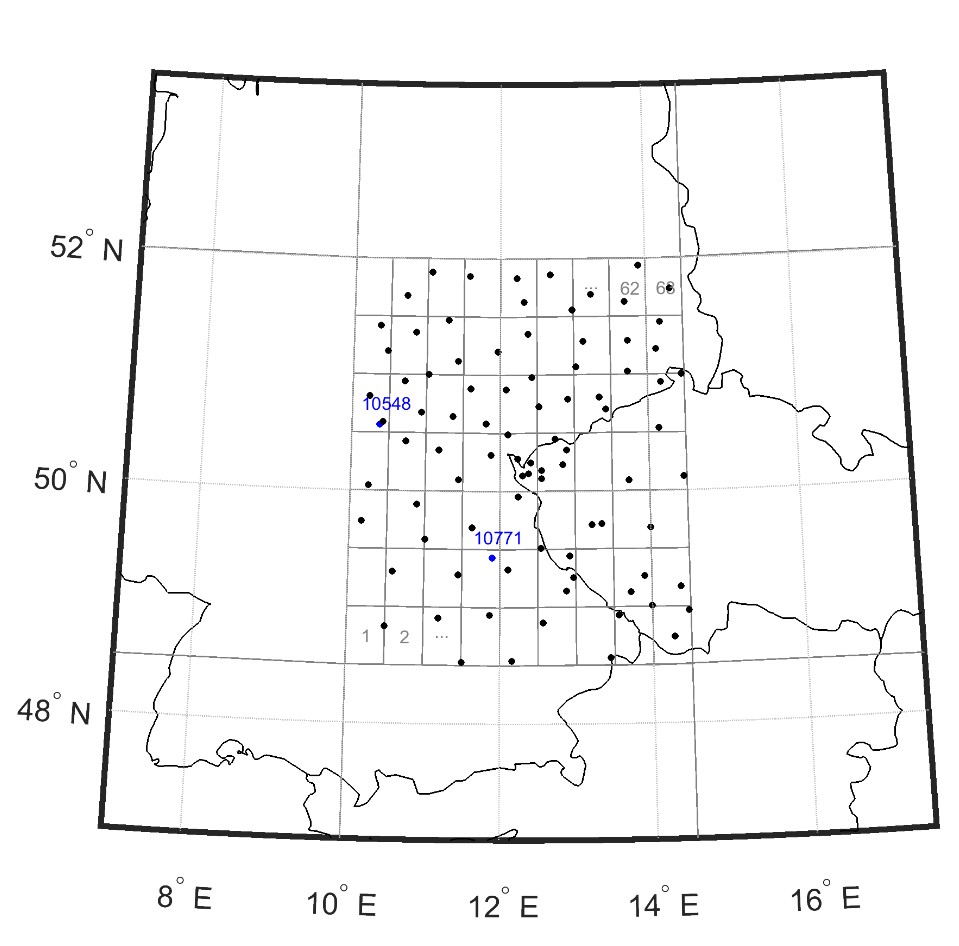
Eastern Switzerland, the Austrian Alps and Czech Republic, and exceeded even 100 mm in several regions of the Northern

Alps. The events of heavy precipitation are connected to the presence of three cyclones: “Dominik”, “Frederik”, and “Günther”. These cyclones formed over (South-) Eastern Europe as a “cluster” with very similar tracks, and were rather shallow systems with relatively high values of minimum sea level pressure. These systems unusually track westward, maintaining a northerly flow against the west-east oriented mountain ranges in Central Europe. However, within this period

5 their movement was blocked by an anticyclone located over the North Atlantic, which forced the cyclones to form an equatorward conveyor belt.

The GNSS tomography solutions covers the region of East Germany and western parts of Czech Republic, including the Erzgebirge (see Fig. 2). Within this area, the equatorward flowing warm air masses started to lift up, which goes along with a local maximum of precipitation of more than 75 mm within the core period of heavy precipitation. For

10 tomography processing, the study area was divided into an inner and an outer voxel model. The parameters of the tomography model and model settings are summarized in Table 3. From the benchmark dataset, 72 GNSS sites could be identified within the inner model, with an average distance of 48 km and altitude ranging from 70 m to 885 m.



**Figure 3: Study area (inner voxel domain) including GNSS sites (black) and radiosonde launch sites (blue).**

15

**Table 3: Applied tomography model settings.**

**Period** 29th of May – 14th of June 2013 number of GNSS sites: 72

**GNSS stations network**

**Tomography domain**

average distance: 48 km

altitude of stations: 70 m – 885 m latitude: 48.5° – 52.0° (0.5° resolution) longitude: 10.0°– 14.5° (0.5° resolution) height: 225 – 12814 m

outer voxel model: latitude +/- 3°, longitude +/-2°

**A priori data** ALADIN-CZ 6 hour forecast

set 0: SWDs (GPS + GLONASS, ZHD from ALADIN-CZ)

**SWD observations**

set 1: SWDs (GPS + GLONASS, ZHD from ALADIN-CZ, hydrostatic gradients removed)

set 2: SWDs (GPS + GLONASS, ZHD from ALADIN-CZ, outer delay removed)

**Cut-off angle** 3° elevation angle

**Time settings** every 6 hours (00, 06, 12, 18 UTC)

TUW: outlier tests based on the post-fit residual RMS

**Quality indicators**

WUELS: filtration of dSWD based on synthetic data for detecting outlier observations

**6 Tomography results**

In the following, the TUW and WUELS tomography solutions are compared with each other and validated against

5 GNSS ZWDs and radiosonde measurements.

**6.1 Intra-technique comparison**

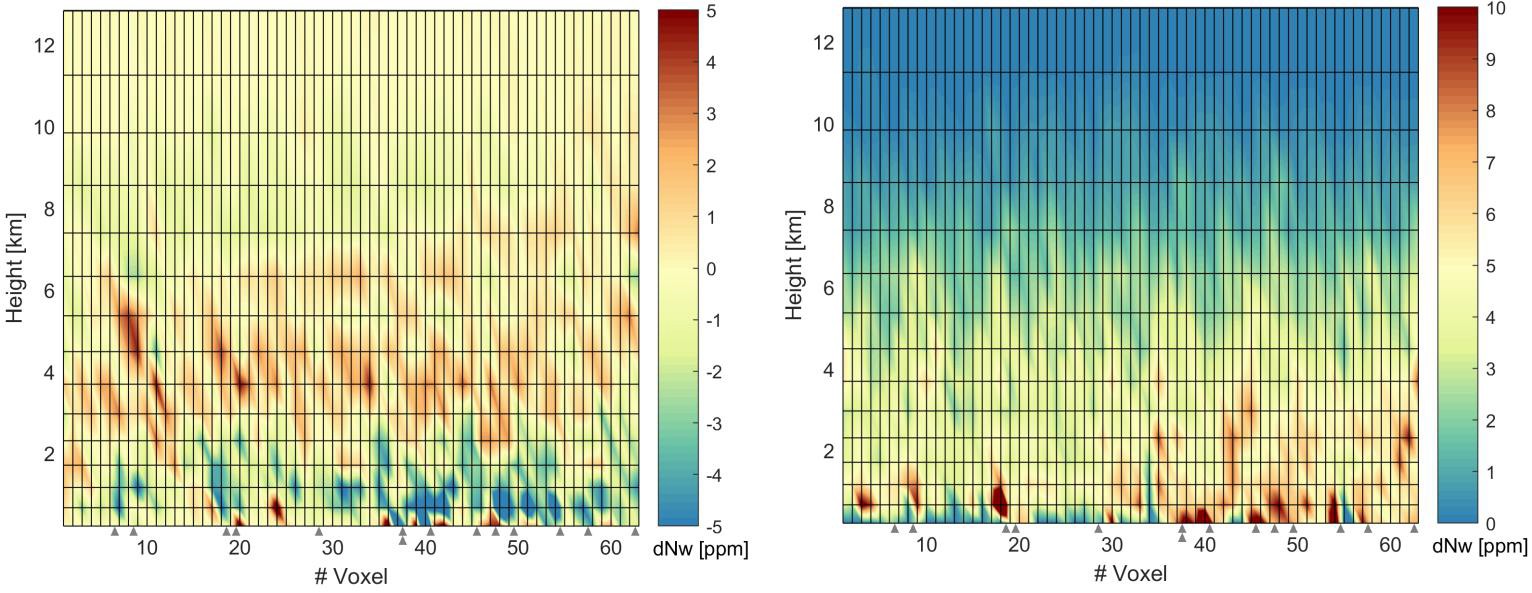
Over the study period of 17 days, in total 68 tomography epochs (four solutions per day) have been processed. Based on the wet refractivity differences (TUW minus WUELS) for each voxel, bias and standard deviation were computed. Figure 4 shows the results for the 63 (horizontal) x 15 (vertical) voxels of the inner voxel model, whereby voxel number 1 indicates the lower

10 South-West corner and the voxel number 63 the North-East corner of the domain. Since both tomography solutions (TUW and WUELS) are based on same input data (set 1), similar wet refractivity fields are obtained. The largest discrepancies are visible within the boundary layer, i.e. the lowest 1-2 km of the atmosphere, and for the layer of 3-6 km height. The TUW solution tends to produce larger wet refractivity fields in specific voxels near surface (#19, 20, 24, 25, 35, 38, 41, 48, 50,…), in return slightly lower values in the 2-3 layers above, and then slightly higher values for the heights of 3-6 km (up to 5

15 ppm). Above the 6 km altitude, the absolute bias and the standard deviation between TUW and WUELS solutions decrease significantly (below 3 ppm). The discrepancies between both models are caused by different approaches of the tomography settings. The tomography models differ in application of quality indicators. In the WUELS approach, the GNSS stations that

frequently failed quality-check, are removed from the solution; whereas in the TUW solution all GNSS stations are taken into account in every epoch. As a result, 14 GNSS stations were rejected from the WUELS model but not from the TUW model. Locations of these stations within the voxel domain are presented in Fig. 4 (grey triangles). In most cases, the locations of the rejected stations correspond with the largest discrepancies between the models, e.g. voxels number 19, 37-

5 40, 45-49. Also, different weightings of the a priori data were applied in both solutions which results in noticeable discrepancies between the outputs of the models.



**Figure 4: Bias (left) and standard deviation (right) of the differences in wet refractivity [ppm] between TUW and WUELS solution**

**1. Analysed period: 29 May – 14 June 2013 (68 epochs). Grey triangles denote GNSS stations removed from the specific voxels of**

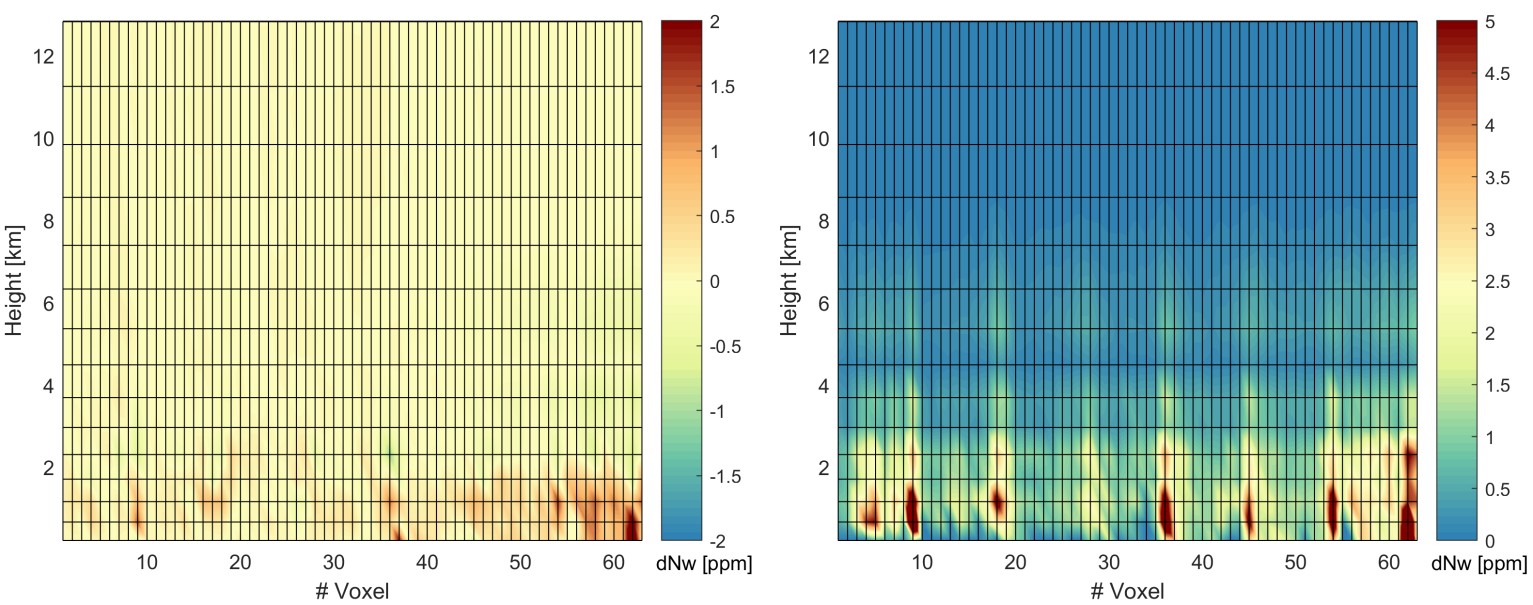
10 **the WUELS solution (one triangle stands for one rejected GNSS station).**

A similar analysis has been carried out for TUW1 and TUW2 (Fig. 5). The major differences between both solutions are caused by the different approaches for compensation of the outer voxel delay. While in solution 1 the tropospheric delay in the outer voxel model was estimated, in solution 2 the outer delay was removed beforehand by ray- tracing through ALADIN-CZ six hour forecast data. Largest offsets between both TUW solutions appear in Northern parts of

15 the study area (voxels columns #55-63). In this part, the tropospheric delay is systematically overestimated (compared to ray-traced delays) in the outer voxel model and in consequence, underestimated in the inner voxel model. This leads to the positive bias as visible in Fig. 5. In all other parts of the voxel model, the differences are widely averaged out over the study period of 17 days. However, the standard deviation shows that variations over time cannot be avoided. Especially between the 31st of May 18 UTC and the 4th of June 18 UTC, larger standard deviations were detected (not shown). These variations

20 are caused by changes in the observation geometry but also by changes in atmospheric conditions not described by the

forecast data (error source in set2).



**Figure 5: Bias (left) and standard deviation (right) of the differences in wet refractivity [ppm] between TUW solution 1 and 2. Analysed period: 29.05. – 14.06.2015 (68 epochs).**

...

**6.2 Time series of integrated zenith wet delays**

5 From the obtained wet refractivity fields, time series of ZWDs were computed for the 72 GNSS sites within the

study area by vertical integration using Eq. 19,

��𝐷 = 10−6 ∑��𝑡

𝐻

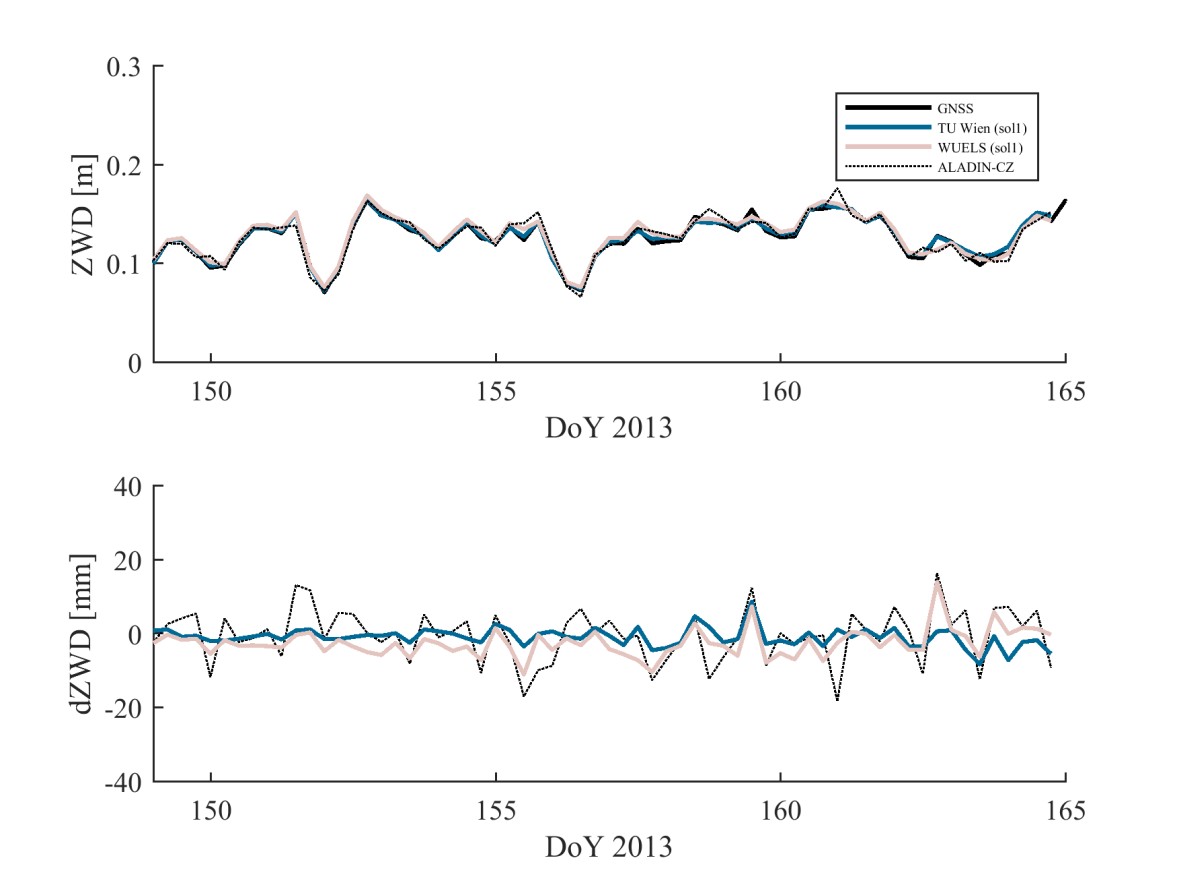
0

��� ∙ �ℎ

(19)

where �0 is the height of the GNSS site and �� is the height of the voxel top (at about 13.5 km height above mean sea level). Beforehand, ��� was horizontally interpolated from adjacent voxel centre points to GNSS site and the vertical resolution was

10 further increased to 20 m. Figure 6 shows the derived ZWD time series for the entire study period of 17 days with 6 h temporal resolution, exemplary for GNSS site WTZR.



**Figure 6: GNSS-derived (black) and tomography-derived (blue and red) ZWD time series at GNSS site WTZR (Wettzell, germany). The dashed line shows the ZWD values derived from the ALADIn-CZ model. The top plot shows the absolute values and the bottom plot highlights the ZWD differences with respect to the GNSS-derived ZWDs.**

Both tomography solutions are more consistent with the GNSS-derived ZWDs than the ALADIN-CZ data. The ZWDs

5 derived from the ALADIN-CZ 6-hour forecasts are occasionally biased, a few hours ‘ahead’ or ‘behind’ the GNSS-derived ZWDs. The WUELS solution is negatively biased, while discrepancies between GNSS and TUW are smaller and equally distributed in positive and negative values. Table 4 shows the statistic of the ZWD differences for GNSS site WTZR but also the mean values over all 72 GNSS sites within the study domain.

**Table 4: Statistics of the differences in ZWD for GNSS site WTZR and all 72 GNSS sites within the study domain. The reference**

10 **solution (GNSS) was obtained by parameter estimation using GNSS phase measurements. The ALADIN-CZ, the TU Wien and**

**WUELS solutions were computed by vertical integration through the wet refractivity fields: Analysed period: 29th of May until**

**14th of June 2013.**

**GNSS minus ALADIN-CZ GNSS minus TU Wien GNSS minus WUELS**

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
|  | bias(dZWD) | stddev(dZWD) | bias(dZWD) | stddev(dZWD) | bias(dZWD) | stddev(dZWD) |
| WTZR | -0.5 mm | 7.2 mm | -0.9 mm | 2.6 mm | -2.5 mm | 3.9 mm |

ALL (72) 0.1 mm 9.1 mm 0.6 mm 2.8 mm -1.8 mm 5.0 mm

With respect to ZWD, both tomography solutions are closer to the GNSS solution than the a priori ALADIN-CZ 6-hour forecast. Especially the standard deviation of the ZWD differences can be reduced if GNSS tomography is applied. However, significant differences are visible between both tomography solutions. The WUELS solution tends to overdetermine the water vapour content in the atmosphere slightly, this goes along with a higher variability of the ZWD

5 differences (about 2 times larger standard deviation than for the TUW solution). This shows that weighting of a priori data and applied quality control methods have a great impact on the results of tomography solutions.

**6.3 Validation of tomography results with radiosonde data**

Radiosonde measurements of temperature ( � ) and dew point temperature ( �� ) were downloaded from

(https://ruc.noaa.gov/raobs/) for station 10548 near Meiningen, Germany (Lat: 50.57°, Lon: 10.37°, H=450m within voxel

10 column #37) and 10771 near Kümmersbruck, Germany (Lat: 49.43°, Lon: 11.90°, H=420m within voxel column #13). The temporal resolution of the measurements is 12 hours (10548) and 6 hours (10771), respectively. Dew point temperature and

temperature were converted into water vapour � (Sonntag, 1990)

17.62∙𝑇𝑑

� = 6.112 ∙ � 243.12+𝑇𝑑 (20)

and wet refractivity

′ � �

15 ��� = 𝑘2 ∙ � + 𝑘3 ∙ � 2 (21)

with ��′ = 22.9744⁡�/ℎ�� and 𝑘 = 375463�

2 3

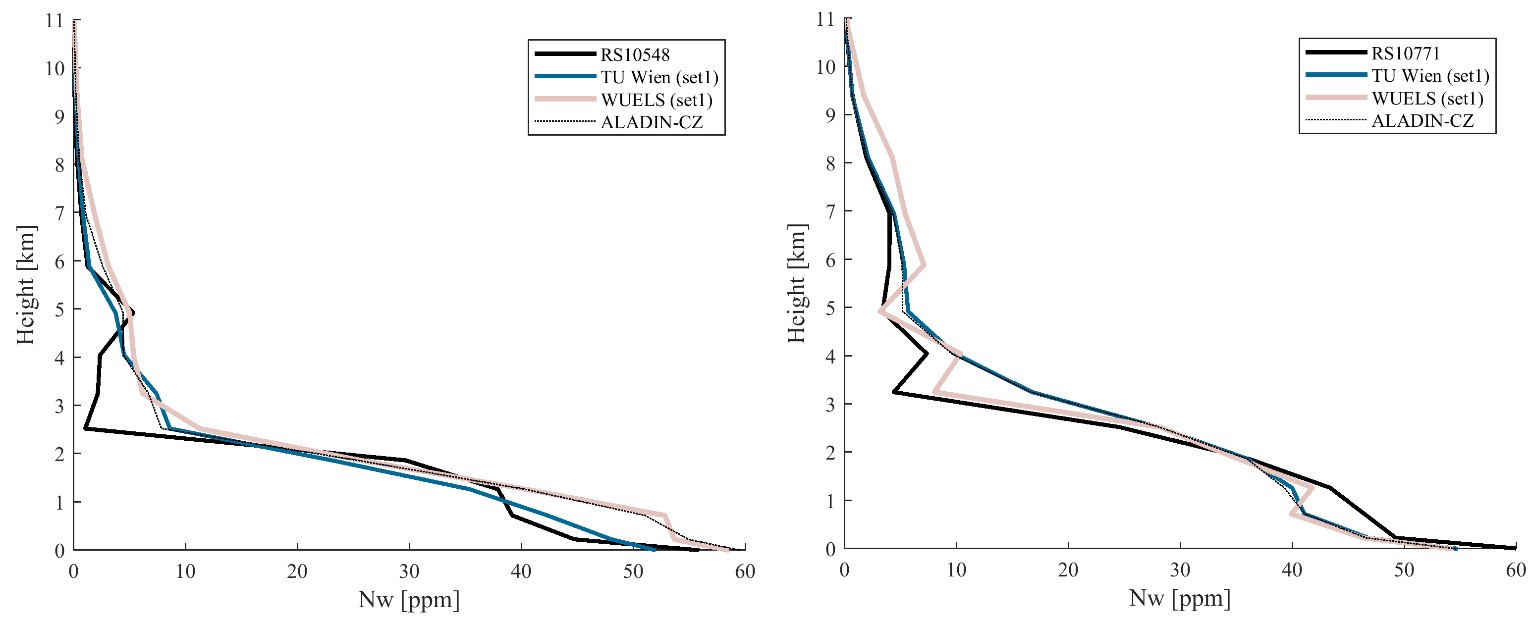
2 /ℎ�� , see Rüeger, 2002, best average. For comparison, the obtained

profiles of wet refractivity (��� ) were linearly interpolated to the voxel centre heights (see Table 1).

Figure 7 shows wet refractivity profiles as obtained at radiosonde site RS10548 on the 6th of June 2013, 00 UTC

and radiosonde site RS10771 on the 13th of June 2013, 00 UTC. Both plots were selected to highlight typical characteristics

20 of the tomography solution. Due to proper weighting, the tomography solution can correct deficits in the a priori model (see the lower 2 km of TUW solution 1 in Fig. 7 left and the WUELS solution between 2 and 5 km height in Fig. 7 right). Sharp changes in wet refractivity can be recovered from TUW tomography solution in the boundary layers and from the WUELS solution in the mid-troposphere (related to weighting model). The tomography solutions are still affected by reconstruction errors (artefacts in the Nw profiles as visible in Fig. 7 left between 2 and 5 km height).



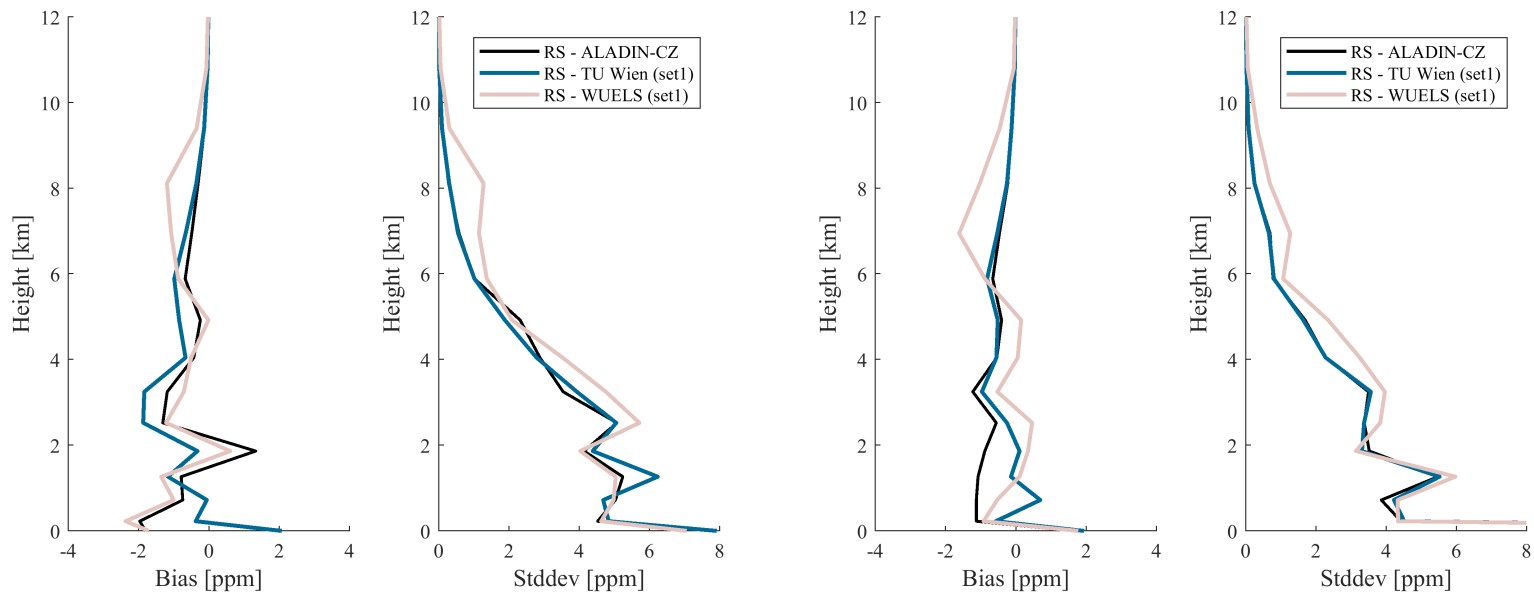
**Figure 7: Wet refractivity profiles derived from radiosonde launches, ALADIN-CZ 6 hour forecast data, TUW and WUELS**

**tomography solution 1 for the 6th of June 2013, 12 UTC (left) and the 13th of June 2013, 00 UTC (right), respectively.**

Fig. 8 shows the corresponding bias and standard deviation over all analysed epochs (34 for RS10548 and 68 for

5 RS10771), separately for each radiosonde site. While RS10548 is located nearby a GNSS site, RS10771 lies within a voxel in which no GNSS site is located. Nonetheless, the quality of the tomography solution does not vary signi ficantly according to the locations of RS stations. Up to 2 km height, the statistics for both tomographic models are on the same level. In the upper parts of the troposphere, the RS - TUW comparison shows similar accuracy as the RS - ALADIN-CZ data, whereas the standard deviation of the WUELS model is noticeably higher.

10

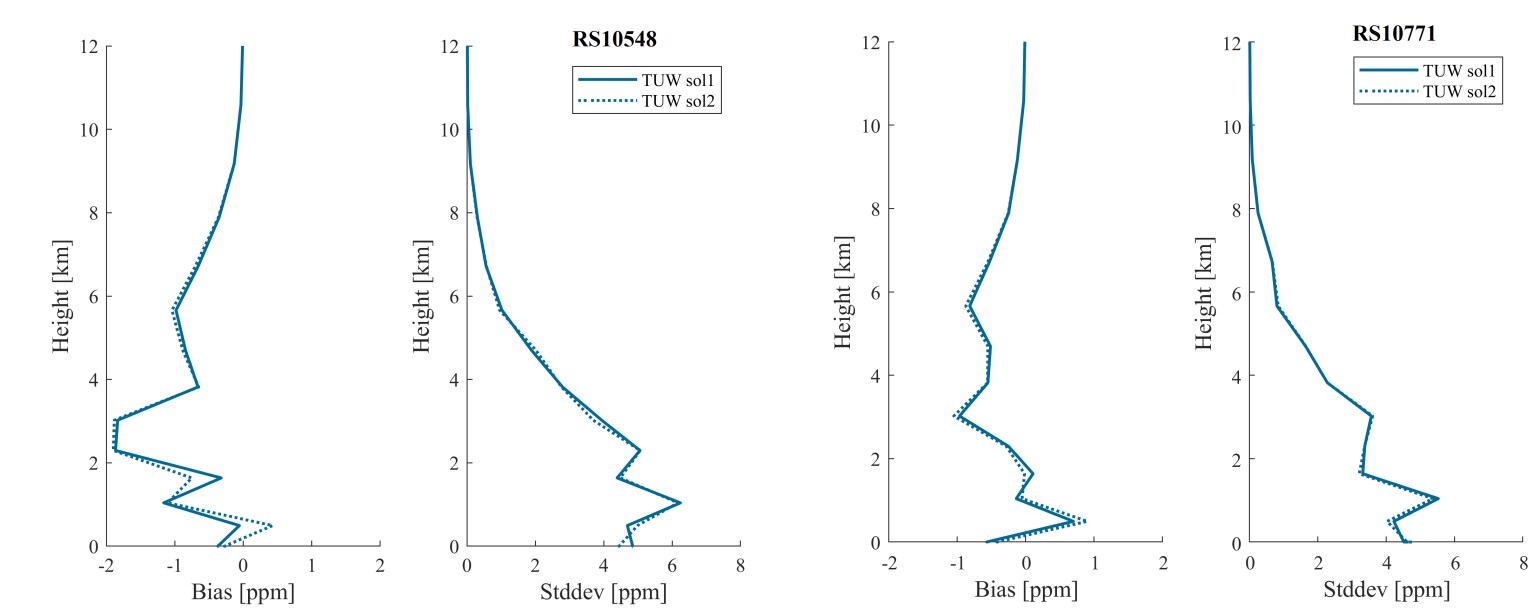


**Figure 8. Statistics of the differences in wet refractivity at radiosonde site RS10548 (left) and RS10771 (right).**

Figure 9 shows the differences between TUW1 and TUW2, separately for each radiosonde site. In fact, the strategy for compensation of the outer delay has only a small impact on the tomography solution. Thereby, the impact is independent from the location of the radiosonde site within the inner voxel model but mostly related to the tomography settings. The largest differences are visible in the lower 2 km of the atmosphere. However, the overall

5 impression is that solution 1 (estimation of the tropospheric delay in the outer voxel model) provides slightly better results than solution 2 (compensation of the outer delay by ray-tracing through ALADIN-CZ 6 hour forecast data). This is most likely related to the quality of the weather model forecast data during the period of extreme precipitation. Nevertheless, since both solutions are rather close to each other, especially with respect to standard deviation, only small improvements are expected by ray-tracing through more reliable weather forecast data.

10



**Figure 9: Statistics of the differences in wet refractivity between radiosonde data and various tomography solutions. Differences between solution 1 and 2 are related to the strategy for compensation of the outer tropospheric delay.**

**7 Assimilation results**

15 **7.1. Diagnosis output**

The WRFDA system and the GPSREF operator are equipped with a quality control diagnostic tool, which allow for verification of all input data before assimilation. As a result, not all of the refractivity observations are actually assimilated into the model. Figure 10 presents a percentage of successfully assimilated observations for each tomography set, as a function of height. The height range with the largest number of assimilated observations is between 4 and 10 km. For these

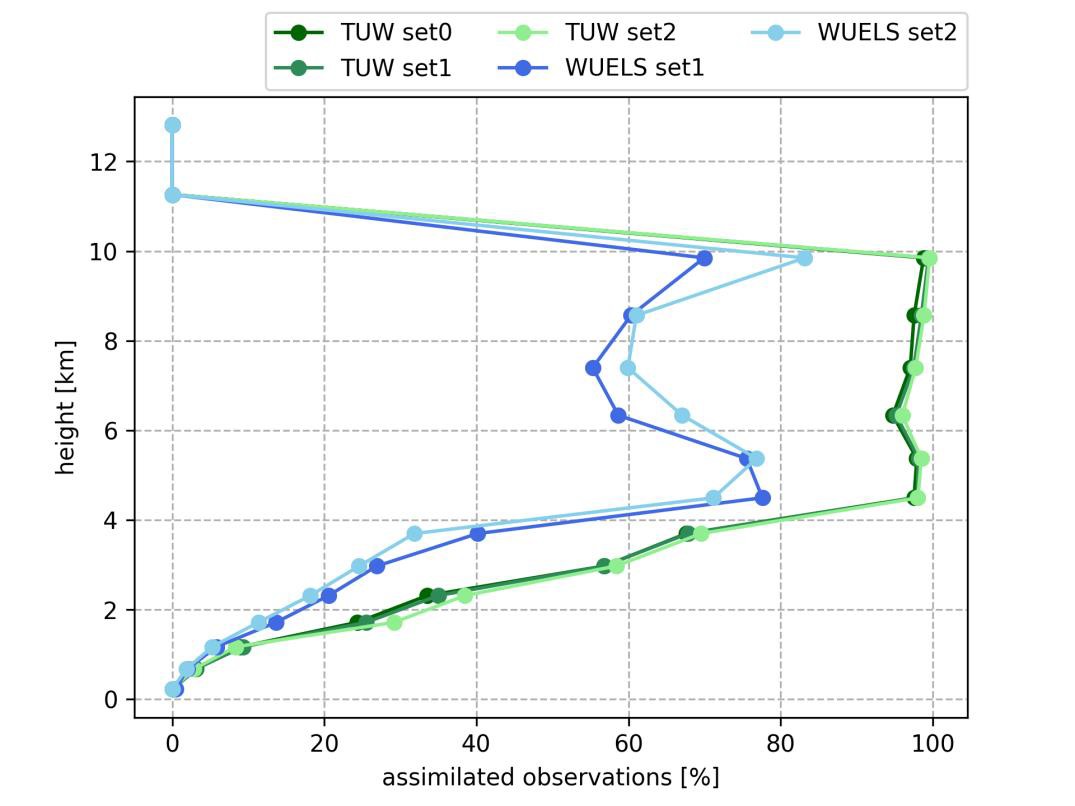
20 heights, more than 90% observations of the TUW solutions and about 50-80% of those form the WUELS solution were assimilated. Below 4 km, the percentage of assimilated observations grows systematically with height, from 0% at surface to

70% for TUW and 40% for WUELS. Above 10 km, no observations were assimilated.

There is a noticeable difference between the numbers of assimilated observations for the two models. At all heights, about 5%-40% more observations were assimilated by the TUW compared to the WUELS model. Since the comparison of tomographic observations with radiosonde data showed that in general the TUW solutions have smaller errors than the

WUELS solutions, the number of observations that passed the quality control is connected to the quality of the tomographic data.

5



**Figure 10: Percentage of successfully assimilated observations for TUW (green) and WUELS (blue) models in a function of height.**

Apart from the number of successfully assimilated observations, the reason of the rejection was also studied. In the quality control diagnostics of the GPSREF operator, each observation is assigned to one group, based on the information of acceptance or rejection (and its cause). Figure 11 presents the results of the quality control check, separately for each group

10 and for each tomography solution as function of height in colour lines. For both tomography solutions, a large number of observations is assigned to a group 0 (orange line) that denotes successfully assimilated data. The number of observations from this group corresponds well with the one already presented in Fig. 10. The quality flags with numbers -88, -77, and -3 are the general flags of the WRFDA system, whereas the numbers from -31 to -36 are the flags assigned by the GPSREF operator.

15 The general flags with numbers -88, -77, and -3 denote respectively: missing data, data laying outside of horizontal domain, data failing maximum error check. Observations assigned to the first group (blue line) occur in the surface layer only, in number of about 2000 observations for the TUW model and 1200 for the WUELS. The second group (yellow line) includes observations from the two highest layers (11.260 km and 12.814 km). The number of observations assigned to the third group (green line) is about 0 at all heights, only for the WUELS model at heights 4 – 8 km the number slightly grows

20 up to about 50 observations.

The quality flags assigned by the GPSREF operator (from -31 to -36) are connected with the values of assimilated refractivity data. The first type of diagnostics is based on the comparison between the assimilated observations and the background values of refractivity (Cucurull et al. 2007). The discrepancies between the two refractivity values should not be larger than 5% (below 7 km) or 4% (7 – 25 km) of the mean value. Observations that do not meet this requirement are

5 assigned to the group -31 (below 7 km, red line) or -32 (above 7 km, purple line). Additionally, if an observation gets the flag -31, all observations in the same vertical profile (same latitude and longitude) below that observation, are also assigned to the flag -31 and they are not assimilated into the model. For the TUW model, the largest number of observations with flag

-31 is at height of 0.675 km (about 3000 observations); this number systematically decreases with height, to about 0 observations at 4 km. For the WUELS model, the largest discrepancies between the observations and the background occur

10 between the heights of 0.675 km and 2.972 km (2000 – 3000 observations); no significant discrepancies are noticed above 6 km. The second type of quality check inside the GPSREF operator is based on a refractivity lapse rate (Poli et al., 2009). The

-34 flag (brown line) is assigned to the observations where �𝑁 is smaller than -50 km-1, whereas the -35 flag (pink line)

�𝑧

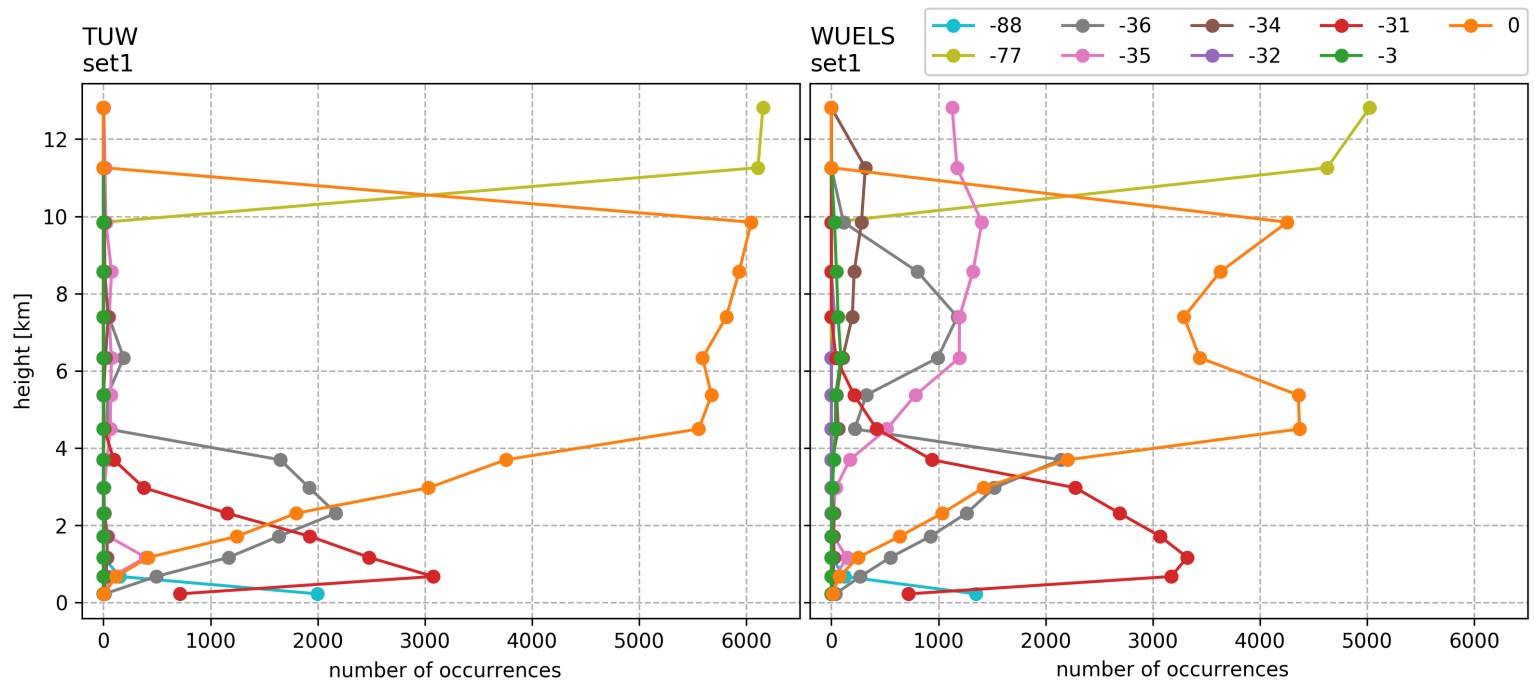
indicates observations where an absolute value of � 𝑁 is larger than 100 km-2. For the TUW model there are no observations

2

�𝑧 2

rejected from the assimilation based on the lapse rate of refractivity. It indicates internal coherency of the model’s output. In

15 the WUELS model, for each layer above 6 km, more than 1000 observations were rejected from the assimilation process based on the refractivity lapse rate. The last type of quality check (flag -36, grey line) is based on the discrepancies between observations and background, as proposed by Cucurull (2010). In the TUW model, these flags occur mainly in the bottom parts of the troposphere (2 km), whereas in the WUELS model inconsistency between model and background is noticed al so for the higher parts (5 – 8 km).



**Figure 11: Number of flagged observations as function of height (flags explanation in the text) - separately for TUW1 (left) and**

**WUELS1 (right).**

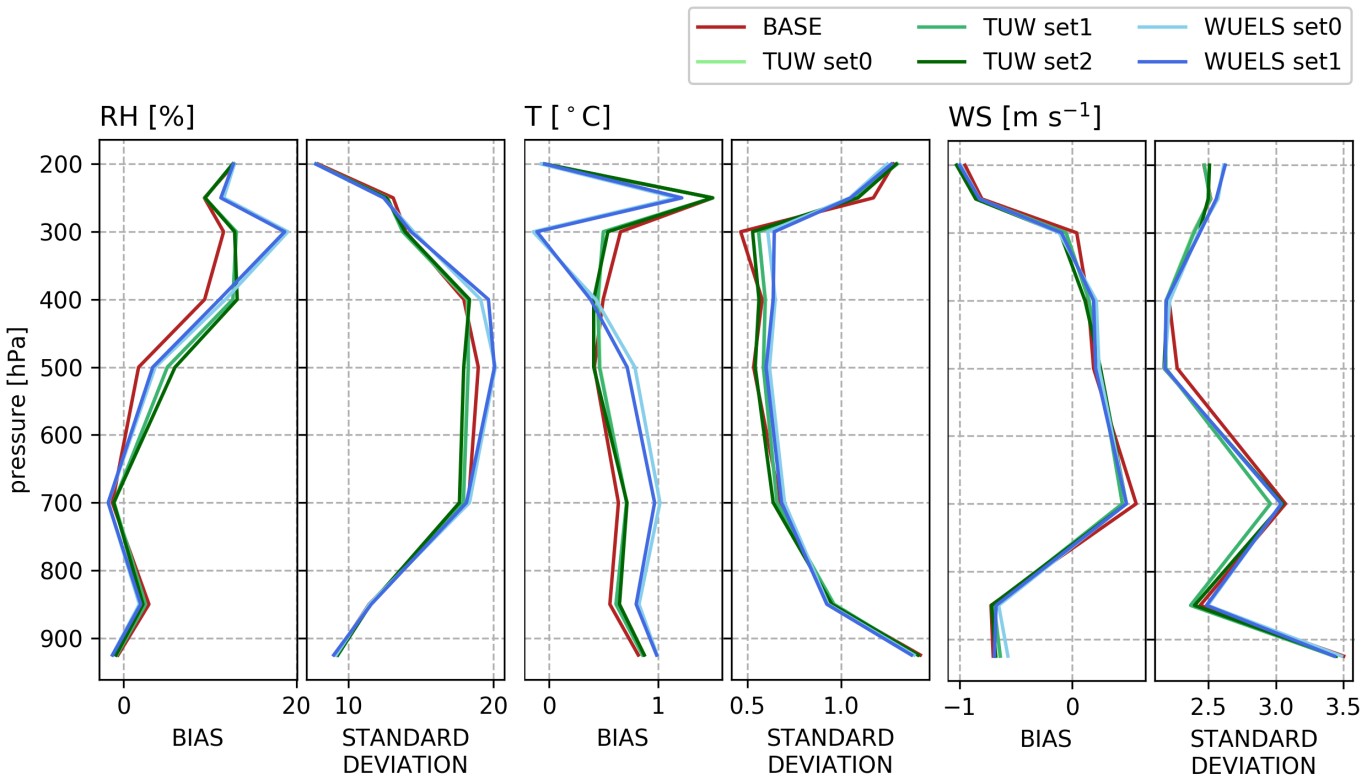
**7.2. Assimilation results at analysis time**

5 The WRF model outputs with assimilated tomographic data were compared to the radiosonde measurements of relative humidity, temperature, and wind speed (Fig. 12). Systematic errors and standard deviations are presented as a function of pressure. Relative humidity slightly improved in terms of systematic error in the boundary layer (900 – 700 hPa) by 1% – 2%. In higher layers, bias of relative humidity increased (by 1% – 5%) but standard deviation decreased (by 1% –

2%) in the case of assimilation of the TUW data (especially within the pressure range of 700 to 400 hPa). Bias of

10 temperature is growing after assimilation in the pressure range of 900 – 400 hPa, especially for the WUELS data assimilation (by 0.2 – 0.5°C) but also for the TUW model (by 0.1°C). In the higher troposphere, the bias is decreased when compared with the base run, by 0.5°C for WUELS and 0.2°C for TUW. Impact of assimilation on the standard deviation of temperature is neutral in the lower troposphere and negative for the higher parts (600 – 250 hPa for WUELS and 400 – 250 hPa for TUW). For the wind speed, there is a small impact of data assimilation on the values of bias, but in terms of standard

15 deviation there is a noticeable improvement for pressure range of 600 – 400 hPa (0.2 m s-1). In the lower troposphere, standard deviation of wind speed decreases after assimilation of the TUW data (by 0.1 m s-1) but increases after assimilation of the WUELS output (by 0.2 m s-1).



**Figure 12: From left to right, statistics (bias, standard deviation) for Relative Humidity (RH), Temperature (T), and Wind Speed (WS) base forecast and model fed with TUW (set0, set1, set2) and WUELS (set0, set1) data when compared with radiosonde measurement; comparison at assimilation time (6 hours since model start).**

5

**7.3. Assimilation output results at simulation time**

Based on the radiosonde observations (10548, 10771), we calculated the bias and standard deviation between the radiosonde data and the model run. The results of the statistics for the weather forecast with assimi lated tomographic output data have been compared to the statistics for the base run (raw run) of the model. This comparison has been conducted 6

10 hours after assimilation (i.e., 12 hours since model start) for the whole tested period (29 May 2013 00:00 UTC – 13 June

2013 18:00 UTC), in the location of radiosonde stations (10548, 10771). We analysed three meteorological parameters:

Relative Humidity (RH), Temperature (T), and Wind Speed (WS, Fig. 13).

In order to assess the impact of the assimilation of the GNSS tomography outputs on the weather forecast, we subtracted the absolute values of statistics for the case of assimilation and the base model run. If the difference between t he

15 statistics is negative, it means that the assimilation of the GNSS tomography output decreases the value of bias and/or standard deviations between the model and radiosonde observation. It implies that the model after assimilation becomes closer to the real observations.

In the beginning of the tested period, i.e., during the first two days, the weather in the Central Europe area was rather calm, thus for all assimilation cases the differences between the statistics for the weather forecast after tomography

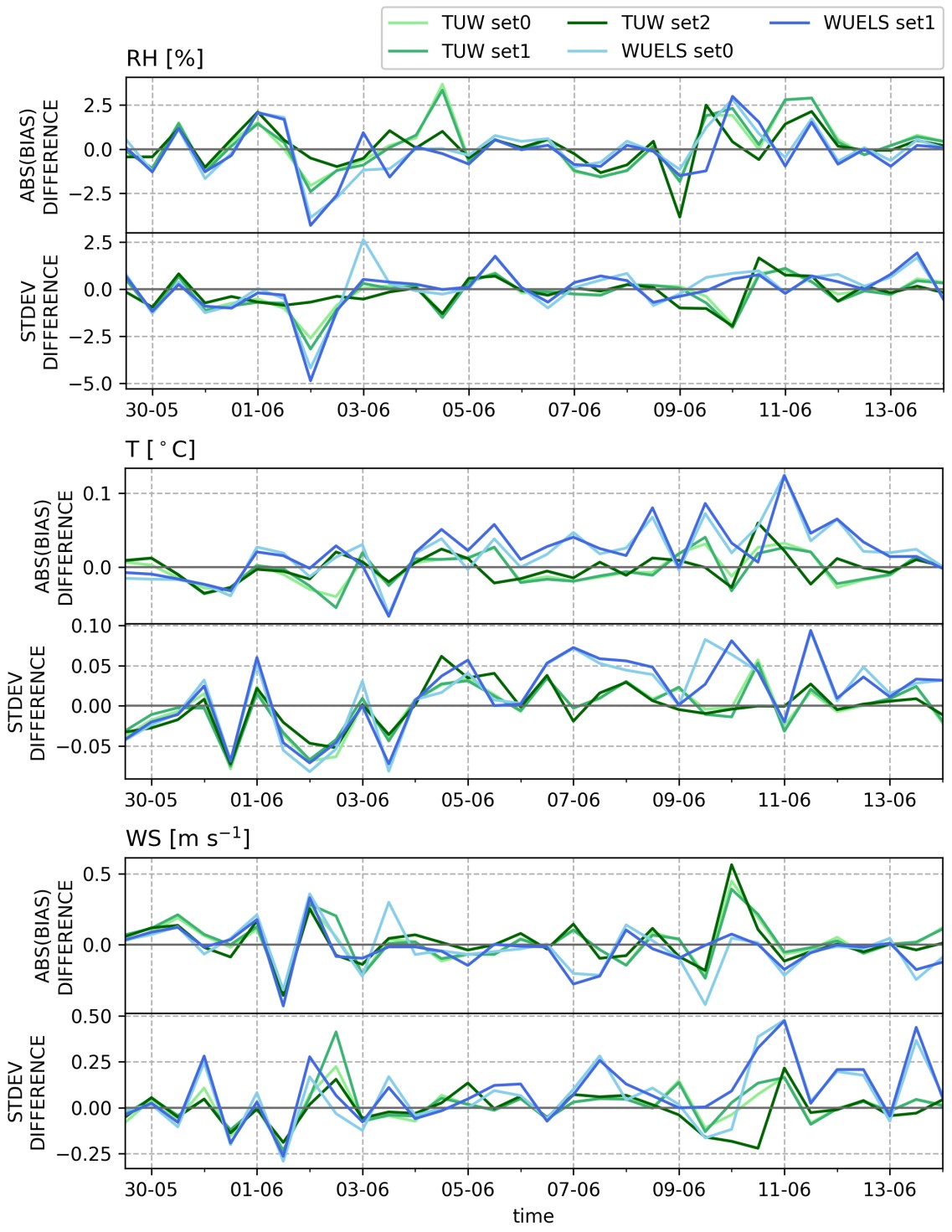
20 data assimilation and the base run are on similar level. In case of a relative humidity assimilation, in time of the heavy

precipitation events (01-03 June 2013), the absolute differences of bias between the models after assimilation of the tomography data and the base run have negative values. The highest positive impact (i.e., decrease of the value of bias) occurs in case of assimilation of the WUELS tomography outputs and exceeds -4.5 % for both bias and the standard deviation differences. In case of the TUW GNSS tomography data assimilation, the differences in the statistical numbers

5 reach around -1 % for set2 and around -2.5 % for set0 and set1.

We observe that the assimilation of the tomography outputs does not have any significant influence on the other examined meteorological parameters. In case of the temperature, the differences hold the level up to 0.1 ℃ for both bias and standard deviations. Since 04 June 2013, the tomography wet refractivity assimilation gives mainly a positive effect for the differences in case of WUELS data (set0, set1), whereas the differences for the TUW data (set0, set1, set2) are close to zero.

10 The statistics for the wind speed look very similar; the assimilation of the tomography data modifies barely the difference between results of statistics, up to 0.5 m/s for both bias and standard deviation differences.



**Figure 13: The differences between statistics of model fed with tomographic data (TUW (set0, set1, set2) and WUELS (set0, set1))**

**and base forecast for Relative Humidity (RH), Temperature (T), and Wind Speed (WS) 6 hours after assimilation (12 hours since model start).**

5

**8 Conclusions**

The GNSS tomography wet refractivity fields can play a key role in the evolution of the weather forecast quality. Although nowadays it is possible to perform GNSS tomography only on regional scale, the outputs provide the crucial information about a local water vapour horizontal and vertical distribution. In this study, GNSS tomography was performed

5 by two models (TUW, WUELS), which are based on the different tomography solutions. We analysed the data for the area of Central Europe in the period of 29 May – 14 June 2013, when heavy precipitation events were observed. The SWDs were calculated based on estimates of the ZTDs and horizontal gradients, provided for 72 GNSS sites by Geodetic Observa tory Pecny (GOP). For the TUW model, three sets of SWD observations were tested (set0 without compensation for hydrostatic anisotropic effects, set1 with compensation of this effect, set2 cleaned by wet delays outside the inner voxel model), wherea s

10 for the WUELS model the set0 and set1 were analysed.

The validation of the tomography results with radiosonde data shows that due to proper weighting the tomography solution can correct deficits in the a priori model. Two different approaches of elimination of the outer parts of SWD observations, which do not pass through the model domain, were examined. The use of the outer model domain led to similar results as a removal of the outer SWD parts using the raytracing technique. Thus applying the raytracing techni que

15 for the tested case did not improve the tomography solution; it can be caused by the low accuracy of the NWP model because of the severe weather events.

In order to assess the benefits of the GNSS tomography outputs for the weather forecasting, we arranged five assimilation tests. This process is enabled by the use of the WRF GPSREF operator. However, in this case, the hydrostatic part of refractivity, using the ALADIN-CZ data, had to be calculated. The assimilation of the tomography products is

20 complex as this procedure requires a proper characterisation of the observation errors. During the assimilation process a lot of observations, depending on the observation level, were rejected. The differences between the GNSS tomography observations from both models (TUW, WUELS) and the background data in the lower part of the troposphere were significant. Therefore most of the observations were assigned as incorrect during the quality check procedure and they do not have any impact on the assimilation results. In the higher part of the troposphere, in case of the TUW model, most of the

25 observations have been successfully assimilated, whereas in case of the WUELS data about 1000 observations at every height layer above 6 km have been omitted in the solution. The accuracy of the tomography model outputs was determined by the comparison of wet refractivity from tomography data with RS observations. The validation indicated large standard deviation values of the WUELS data in the upper part of the troposphere. Hence, the verification process in the assimilation is consistent with the quality of the data. Based on this we assess, that the quality check system dedicated to radio occulta tion

30 data can be applied for the assimilation of tomography outputs.

The assimilation was performed in the diverse weather conditions. The heaviest precipitation occurred in the period of 01-03 June 2013. During this period the most significant positive effect after the assimilation of the tomography data was noticed. The weather forecast after the assimilation was improved in terms of relative humidity (bias and standard deviation)

and temperature (standard deviations), whereas the impact on the wind speed is not visible. However, the long -term impact of the assimilation of the GNSS tomography outputs should be investigated.

The advantage of using the GNSS tomography data in the weather forecasting could be also verified against the assimilation of other GNSS tropospheric parameters, e.g., ZTD or IWV. Additionally, the hydrostatic part of r efractivity

5 might be calculated from the background model (at time of assimilation) in order to avoid the influence of differences between two models (ALARO-CZ and WRF) on the results. Future research will cover the development of the observation operator dedicated to the assimilation of the GNSS tomography wet refractivity, in order to eliminate the need of an external data source to derive the hydrostatic part of the refractivity.

**Author contribution**

10 Natalia Hanna as a first and corresponding author administered the project, formulated the methodology of assimilation process, investigated the assimilation experiments, and validated the results. Estera Trzcina, Gregor Moeller, and Witold Rohm prepared the methodology of GNSS tomography process. Estera Trzcina contributed by investigation of GNSS tomography for WUELS model, and conducted the formal analyses in the GNSS tomography and data assimilation part, and validated the results. Gregor Moeller contributed by investigation of GNSS tomography for TUW model, conducted the

15 formal analyses in the GNSS tomography part, and validated the results. Witold Rohm and Robert Weber initiated the research idea, supervised the project, and reviewed the manuscript. Natalia Hanna and Estera Trzcina prepared the manuscript with contributions from all co-authors.

**Acknowledgements**

This study has been organized within the EU COST action ES1206 (GNSS4SWEC). The research has been supported by

20 the Polish National Science Centre (project no UMO-2015/17/B/ST10/03827) and the Wroclaw Center of Networking and Supercomputing (<http://www.wcss.wroc.pl/)>computational grant using MATLAB Software License No: 101979. The authors thank all the institutions that provided data for the campaign: GNSS data from the Geodetic Observatory Pecny (GOP; [http://www.pecny.cz/),](http://www.pecny.cz/)) NWM data from the local area model ALADIN-CZ provided by the Czech Hydrometeorological Institute (CHMI; http://portal.chmi.cz), and radiosonde observations from the Deutscher Wetterdienst

25 (DWD Germany, https://www.dwd.de).

**Competing interests**

The authors declare that they have no conflict of interest.

**References**

1. Adavi, Z. and Mashhadi-Hossainali, M.: 4D-tomographic reconstruction of water vapor using the hybrid regularization technique with application to the North West of Iran, Advances in Space Research, 55(7), 1845-1854, doi:10.1016/j.asr.2015.01.025, 2015.

5 2. Andersson, E.: Statement of Guidance for Global Numerical Weather Prediction (NWP), World Meteorological

Organisation, 2018.

3. Bauer, H. S., Wulfmeyer, V., Schwitalla, T., Zus, F., and Grzeschik, M.: Operational assimilation of GPS slant path delay measurements into the MM5 4DVAR system, Tellus A: Dynamic Meteorology and Oceanography, 63(2), 263-

282, doi:10.1111/j.1600-0870.2010.00489.x, 2011.

10 4. Bender, M., Dick, G., Ge, M., Deng, Z., Wickert, J., Kahle, H. G., Raabe, A., and Tetzlaff, G.: Development of a GNSS

water vapour tomography system using algebraic reconstruction techniques, Advances in Space Research, 47(10), 1704-

1720, doi:10.1016/j.asr.2010.05.034, 2011.

5. Benevides, P., Catalao, J., Nico, G., & Miranda, P. M.: Inclusion of high resolution MODIS maps on a 3D tropospheric water vapor GPS tomography model, Remote Sensing of Clouds and the Atmosphere XX (Vol. 9640, p. 96400R),

15 International Society for Optics and Photonics, doi:10.1117/12.2194857, 2015.

6. Bennitt, G. V. and Jupp, A.: Operational assimilation of GPS zenith total delay observations into the Met Office numerical weather prediction models, Monthly Weather Review, 140(8), 2706-2719, doi:10.1175/MWR-D-11-00156.1

2012.

7. Bevis, M., Businger, S., Chiswell, S., Herring, T. A., Anthes, R. A., Rocken, C., and Ware, R. H.: GPS meteorology:

20 Mapping zenith wet delays onto precipitable water, Journal of applied meteorology, 33(3), 379-386, doi:10.1175/1520-

0450(1994)033<0379:GMMZWD>2.0.CO;2, 1994.

8. Böhm, J. and Schuh, H.: Vienna mapping functions in VLBI analyses, Geophysical Research Letters, 31(1), doi:10.1029/2003GL018984, 2004.

9. Böhm, J. and Schuh, H. (Eds.): Atmospheric effects in space geodesy (Vol. 5), Berlin, Springer, 2013.

25 10. Böhm, J., Werl, B., & Schuh, H.: Troposphere mapping functions for GPS and very long baseline interferometry from European Centre for Medium‐Range Weather Forecasts operational analysis data, Journal of Geophysical Research: Solid Earth, 111(B2), doi:10.1029/2005JB003629, 2006.

11. Boniface, K., Ducrocq, V., Jaubert, G., Yan, X., Brousseau, P., Masson, F., Champollion, C., Chery, J., and Doerflinger, E.: Impact of high-resolution data assimilation of GPS zenith delay on Mediterranean heavy rainfall forecasting,

30 Annales Geophysicae (Vol. 27, pp. 2739-2753), doi:10.5194/angeo-27-2739-2009, 2009.

12. Chen, B., Liu, Z., Wong, W. K., and Woo, W. C.: Detecting water vapor variability during heavy precipitation events in Hong Kong using the GPS tomographic technique, Journal of Atmospheric and Oceanic Technology, 34(5), 1001-1019, doi:10.1175/JTECH-D-16-0115.1, 2017.

13. Chen, G. and Herring, T.: Effects of atmospheric azimuthal asymmetry on the analysis of space geodetic data, Journal of

Geophysical Research: Solid Earth, 102(B9), 20489-20502, doi:10.1029/97JB01739, 1997.

14. Cucurull, L.: Improvement in the use of an operational constellation of GPS radio occultation receivers in weather forecasting, Weather and Forecasting, 25(2), 749-767, doi:10.1175/2009WAF2222302.1, 2010.

5 15. Cucurull, L., Vandenberghe, F., Barker, D., Vilaclara, E., and Rius, A.: Three-dimensional variational data assimilation of ground-based GPS ZTD and meteorological observations during the 14 December 2001 storm event over the western Mediterranean Sea, Monthly Weather Review, 132(3), 749-763, doi:10.1175/1520-

0493(2004)132<0749:TVDAOG>2.0.CO;2, 2004.

16. Cucurull, L., Derber, J. C., Treadon, R., & Purser, R. J.: Assimilation of global positioning system radio occultation

10 observations into NCEP’s global data assimilation system, Monthly Weather Review, 135(9), 3174-3193, doi:10.1175/MWR3461.1, 2007.

17. Dach, R., Hugentobler, U., Fridez, P., and Meindl, M.: Bernese GPS software version 5.0, Astronomical Institute, University of Bern, 640, 114, 2007.

18. Ding, N., Zhang, S. B., Wu, S. Q., Wang, X. M., and Zhang, K. F.: Adaptive node parameterization for dynamic

15 determination of boundaries and nodes of GNSS tomographic models, Journal of Geophysical Research: Atmospheres,

123(4), 1990-2003, doi:10.1002/2017JD027748, 2018.

19. de Haan, S., Holleman, I., and Holtslag, A. A.: Real-time water vapor maps from a GPS surface network: Construction, validation, and applications, Journal of applied meteorology and climatology, 48(7), 1302-1316, doi:10.1175/2008JAMC2024.1, 2009.

20 20. Dousa, J.: Precise near real-time GNSS analyses at Geodetic Observatory Pecny-precise orbit determination and water vapour monitoring, Acta Geodynamica et Geromaterialia, 7(1), 7-18, 2010.

21. Douša, J., Dick, G., Kačmařík, M., Brožková, R., Zus, F., Brenot, H., Stoycheva, A., Möller, G., and Kaplon, J.: Benchmark campaign and case study episode in central Europe for development and assessment of advanced GNSS tropospheric models and products, Atmospheric Measurement Techniques, 9, 2989-3008, https://doi.org/10.5194/amt-9-

25 2989-2016, 2016.

22. Dudhia, J.: Numerical study of convection observed during the Winter Monsoon Experiment using a mesoscale two–

dimensional model, Journal of the atmospheric sciences, 46(20), 3077-3107, doi:10.1175/1520-

0469(1989)046<3077:NSOCOD>2.0.CO;2, 1989.

23. Elgered, G.: An overview of COST Action 716: Exploitation of ground-based GPS for climate and numerical weather

30 prediction analysis, Proceedings COST-716/IGS Workshop, Oslo 2000, 2001.

24. Falvey, M. and Beavan, J.: The impact of GPS precipitable water assimilation on mesoscale model retrievals of orographic rainfall during SALPEX'96, Monthly weather review, 130(12), 2874-2888, 10.1175/1520-

0493(2002)130<2874:TIOGPW>2.0.CO;2, 2002.

25. Flores, A., Ruffini, G., and Rius, A.: 4D tropospheric tomography using GPS slant wet delays, Annales Geophysicae

(Vol. 18, No. 2, pp. 223-234), Springer-Verlag, doi:10.1007/s00585-000-0223-7, 2000.

26. Guerova, G., Jones, J., Douša, J., Dick, G., Haan, S. D., Pottiaux, E., Bock, O., Pacione, R., Elgered, G., Vedel, H., and

Bender, M.: Review of the state of the art and future prospects of the ground-based GNSS meteorology in Europe,

5 Atmospheric Measurement Techniques, 9(11), 5385-5406, doi:10.5194/amt-9-5385-2016, 2016.

27. Gutman, S. I., Sahm, S. R., Benjamin, S. G., Schwartz, B. E., Holub, K. L., Stewart, J. Q., and Smith, T. L.: Rapid retrieval and assimilation of ground based GPS precipitable water observations at the NOAA Forecast Systems Laboratory: Impact on weather forecasts, *Journal of the Meteorological Society of Japan. Ser. II*, *82*(1B), 351-360, doi:10.2151/jmsj.2004.351, 2004.

10 28. Haase, J., Calais, E., Talaya, J., Rius, A., Vespe, F., Santangelo, R., Huang, X.-Y., Davila, J.M., Cucurull, L., Flores, A, Sciarretta, C., Pacione, R., Boccolari, M., Pugnanghi, S., Vedel, H., Mogensen, K., Yang, X., and Garate, J..: The contributions of the MAGIC project to the COST 716 objectives of assessing the operational potential of ground -based GPS meteorology on an international scale, Physics and Chemistry of the Earth, Part A: Solid Earth and Geodesy, 26(6-

8), 433-437, doi:10.1016/S1464-1895(01)00079-5, 2001.

15 29. Hirahara, K.: Local GPS tropospheric tomography, Earth, planets and space, 52(11), 935-939, doi:10.1186/BF03352308, 2000.

30. Hofmann-Wellenhof, B., Lichtenegger, H., and Wasle, E.: GNSS–global navigation satellite systems: GPS, GLONASS, Galileo, and more, Springer Science & Business Media, 2007.

31. Hong, S. Y., Yign, N., and Dudhia, J.: A new vertical diffusion package with an explicit treatment of entrainment

20 processes, Monthly weather review, 134(9), 2318-2341, doi:10.1175/MWR3199.1, 2006.

32. Inness, P.M. and Dorling, S.: Operational weather forecasting, Wiley, 2012.

33. Iyer, H. M. and Hirahara, K. (Eds.).: Seismic tomography: Theory and practice, Springer Science & Business Media,

1993.

34. Jimenez, P. A., Dudhia, J., Gonzalez–Rouco, J. F., Navarro, J.,Montavez, J. P., and Garcia–Bustamante, E.: A revised

25 scheme for the WRF surface layer formulation. Monthly Weather Review, 140(3), 898-918, doi:10.1175/MWR-D-11-

00056.1, 2012.

35. Kacmarík, M., Douša, J., Dick, G., Zus, F., Brenot, H., Möller, G., Pottiaux E., Kaplon J., Hordyniec P., Václavovic P. and Morel, L.: Inter-technique validation of tropospheric slant total delays, Atmospheric Measurement Techniques,

10(6), doi:10.5194/amt-10-2183-2017, 2017.

30 36. Kain, J. S.: The Kain–Fritsch convective parameterization: an update, Journal of applied meteorology, 43(1), 170-181, doi:10.1175/1520-0450(2004)043<0170:TKCPAU>2.0.CO;2, 2004.

37. Karabatić, A., Weber, R., and Haiden, T.: Near real-time estimation of tropospheric water vapour content from ground based GNSS data and its potential contribution to weather now-casting in Austria, Advances in Space Research, 47(10),

16911703, doi:10.1016/j.asr.2010.10.028, 2011.

38. Kawabata, T., Shoji, Y., Seko, H., and Saito, K.: A numerical study on a mesoscale convective system over a subtropical island with 4D-Var assimilation of GPS slant total delays, Journal of the Meteorological Society of Japan, Ser. II, 91(5), 705-721, doi:10.2151/jmsj.2013-510 2013.

39. Kleijer, F.: Troposphere modeling and filtering for precise GPS levelling, Diss., TU Delft, Delft University of

5 Technology, doi:10.26491/mhwm/65146, 2004.

40. Koch, S. E., Aksakal, A., and McQueen, J. T.: The influence of mesoscale humidity and evapotranspiration fields on a model forecast of a cold-frontal squall line, Monthly Weather Review, 125(3), 384-409, doi:10.1175/1520-

0493(1997)125<0384:TIOMHA>2.0.CO;2, 1997.

41. Mendes, V. B.: Modeling the neutral-atmospheric propagation delay in radiometric space techniques, UNB geodesy and

10 geomatics engineering technical report (199), 1999.

42. Möller, G.: Reconstruction of 3D Wet Refractivity Fields in the Lower Atmosphere: Along Bended GNSS Signal Paths, Südwestdeutscher Verlag für Hochschulschriften, 2017.

43. Möller, G.,Wittmann, C., Yan, X., Umnig, E., Joldzic, N., and Weber, R.: 3D ground based GNSS atmospheric tomography, Final report GNSS-ATom, Austrian Research Promotion Agency (FFG), project 840098, 2015.

15 44. Nakamura, H., Koizumi, K., and Mannoji, N.: Data assimilation of GPS precipitable water vapor into the JMA mesoscale numerical weather prediction model and its impact on rainfall forecasts, Journal of the Meteorological Society of Japan. Ser. II, 82(1B), 441-452, doi:10.2151/jmsj.2004.441, 2004.

45. Niell, A. E.: Global mapping functions for the atmosphere delay at radio wavelengths, Journal of Geophysical Research: Solid Earth, 101(B2), 3227-3246, doi:10.1029/95JB03048, 1996.

20 46. Perler, D., Geiger, A., and Hurter, F.: 4D GPS water vapor tomography: new parameterized approaches, Journal of

Geodesy, 85(8), 539-550, doi:10.1007/s00190-011-0454-2, 2011.

47. Poli, P., Moll, P., Puech, D., Rabier, F., and Healy, S. B.: Quality control, error analysis, and impact assessment of FORMOSAT-3/COSMIC in numerical weather prediction, Terrestrial, Atmospheric & Oceanic Sciences, 20(1), doi:10.3319/TAO.2008.01.21.02(F3C), 2009.

25 48. Poli, P., Moll, P., Rabier, F., Desroziers, G., Chapnik, B., Berre, L., Healy, S. B., Andersson, E., and El Guelai, F. Z.: Forecast impact studies of zenith total delay data from European near real‐time GPS stations in Météo France 4DVAR, Journal of Geophysical Research: Atmospheres, doi:10.1029/2006JD007430, 112(D6), 2007.

49. Rohm, W.: The precision of humidity in GNSS tomography, Atmospheric research, 107, 69-75, doi:10.1016/j.atmosres.2011.12.008, 2012.

30 50. Rohm, W.: The ground GNSS tomography–unconstrained approach, *Advances in Space Research*, *51*(3), 501-513, doi:10.1016/j.asr.2012.09.021, 2013.

51. Rohm, W. and Bosy, J.: Local tomography troposphere model over mountains area, Atmospheric Research, 93(4), 777-

783, doi:10.1016/j.atmosres.2009.03.013, 2009.

52. Rohm, W. and Bosy, J.: The verification of GNSS tropospheric tomography model in a mountainous area, Advances in

Space Research, 47(10), 1721-1730, doi:10.1016/j.asr.2010.04.017, 2011.

53. Rohm, W., Zhang, K., and Bosy, J.: Limited constraint, robust Kalman filtering for GNSS troposphere tomography.

Atmospheric Measurement Techniques, 7(5), 1475-1486, doi:10.5194/amt-7-1475-2014, 2014.

5 54. Saastamoinen, J.: Atmospheric correction for the troposphere and stratosphere in radio ranging satellites, The use of artificial satellites for geodesy, 15, 247-251, doi:10.1029/GM015p0247, 1972.

55. Schwitalla, T. , Bauer, H. , Wulfmeyer, V., and Aoshima, F.: High‐resolution simulation over central Europe:

assimilation experiments during COPS IOP 9c, Quarterly Journal of the Royal Meteorological Society, 137(S1), 156-

175, doi:10.1002/qj.721, 2011.

10 56. Skamarock, W. C., J. B. Klemp, J. Dudhia, D. O. Gill, D. M. Barker, M. G Duda, X.-Y. Huang, W. Wang, and J. G.

Powers.: A description of the advanced research WRF version 3, *NCAR Tech. Note NCAR/TN-475+STR,* 113 pp., doi:10.5065/D68S4MVH, 2008.

57. Tewari, M., F. Chen, Wang, W., Dudhia, J, LeMone, M. A. K., Mitchell, M. A., Gayno, M. Ek, G., Wegiel, J., and

Cuenca, R. H.: Implementation and verification of the unified NOAH land surface model in the WRF model, 20th

15 conference on weather analysis and forecasting/16th conference on numerical weather prediction, Vol. 1115, 2004.

58. Tilev‐Tanriover, S. and Kahraman, A.: Impact of Turkish ground‐based GPS‐PW data assimilation on regional forecast:

8–9 March 2011 heavy snow case, Atmospheric Science Letters, 15(3), 159-165, doi:10.1002/asl2.482, 2014.

59. Troller, M., Geiger, A., Brockmann, E., Bettems, J. M., Bürki, B., and Kahle, H. G.: Tomographic determination of the spatial distribution of water vapor using GPS observations, Advances in Space Research, 37(12), 2211-2217, doi:

20 10.1016/j.asr.2005.07.002, 2006.

60. Trzcina, E. and Rohm, W.: Estimation of 3D wet refractivity by tomography, combining GNSS and NWP data. First results from assimilation of wet refractivity into NWP, Manuscript submitted for publication, 2018.

61. Xu, P.: Truncated SVD methods for discrete linear ill-posed problems, Geophysical Journal International, 135(2), 505-

514, doi:10.1046/j.1365-246X.1998.00652.x, 1998.

25 62. Zhang, K., Manning, T., Wu, S., Rohm, W., Silcock, D., and Choy, S.: Capturing the signature of severe weather events in Australia using GPS measurements, IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing, 8(4), 1839-1847, doi:10.1109/JSTARS.2015.2406313, 2015.