# Development of time-varying global gridded Ts-Tm model for precise GPS-PWV retrieval

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**Abstract:** Water-vapor-weighted mean temperature,  $T_m$ , is the key variable for estimating the mapping factor between GPS zenith wet delay (ZWD) and precipitable water vapor (PWV). For the near real-time GPS-PWV retrieving, estimating  $T_m$  from surface air temperature  $T_s$  is a widely used method because of its high temporal resolution and a fair degree of accuracy. Based on the estimations of  $T_m$  and  $T_s$  at each reanalysis grid node of the ERA-Interim data, we analyzed the relationship between  $T_m$ and  $T_s$  without data smoothing. The analyses demonstrate that the  $T_{s-}T_{m}$  relationship has significant spatial and temporal variations. Static and time-varying global gridded  $T_s$ - $T_m$  models were established and evaluated by comparisons with the radiosonde data at 723 radiosonde stations in the Integrated Global Radiosonde Archive (IGRA). Results show that our global gridded  $T_s - T_m$  equations have prominent advantages over the other globally applied models. At a considerable number of stations, the gridded  $T_s$ - $T_m$  models can remove the large biases in Bevis equation and in the latitude-related linear model. Multiple statistical tests at the 5 % significance levels show that the time-varying global gridded model is superior to the other models at 60.03 % of the radiosonde sites. The second-best model is the  $1^{\circ} \times 1^{\circ}$  GPT2w model, which is superior at only 12.86 % of the sites. The contribution of the  $T_m$ 's uncertainty to the total uncertainty of GPS PWV also dropped significantly. GPS-PWV retrievals using different  $T_m$  estimates were compared at 74 IGS stations. At most of the sites, the relative differences of GPS-PWV are within 1 % by applying time-varying global gridded  $T_s$ - $T_m$  equations. This performance is superior to the other  $T_m$  estimation models. The differences between GPS-PWV and radiosonde PWV are influenced by multiple factors instead of a single  $T_m$  parameter. However, evident improvements still exist at particular sites by using more precise  $T_s - T_m$  equations. PWV errors could decrease 1~2 mm during the wetter months.

#### 1. Introduction

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Water vapor is an important trace gas and one of the most variable components in the troposphere. The transport, concentration, and phase transition of water vapor are directly involved in the atmospheric radiation and hydrological cycle. It plays a key role in many climate changes and weather processes (Adler et al., 2016; Mahoney et al., 2016; Song et al., 2016). However, water vapor has high spatial-temporal variability, and its content is often small within the atmosphere. It is a challenge to measure water vapor content accurately and timely. For decades, several methods have been studied, such as radiosondes and water vapor radiometers, sun photometers, and GPS (Campmany et al., 2010; Ciesielski et al., 2010; Liu et al., 2013; Perez-Ramirez et al., 2014; Li et al., 2016). Compared with the traditional water vapor observations, ground-based GPS water vapor measurement has the advantages of high accuracy, high spatial-temporal resolution, all-weather availability, and low-cost (Haase et al., 2003; Pacione and Vespe, 2008; Lee et al., 2010; Means, 2013; Lu et al., 2015). Ground-based GPS water vapor products, mainly including precipitable water vapor (PWV), are widely used in many fields such as real-time vapor monitoring, weather and climate research, and numerical weather prediction (NWP) (Van Baelen and Penide, 2009; Karabatic et al., 2011; Rohm et al., 2014; Adams et al., 2017).

GPS observations require some kinds of meteorological elements to estimate PWV. Zenith hydrostatic delay (ZHD) can be calculated using surface pressure  $P_s$  by equation (Ning et al., 2013):

$$ZHD = (2.2767 \pm 0.0015) \frac{P_s}{f(\varphi, H)}$$
 (1)

where  $\varphi$  is the latitude, H is the geoid height in meters, and

$$f(\lambda, H) = (1 - 2.66 \times 10^{-3} \cos \varphi - 2.8 \times 10^{-7} H)$$
 (2)

Then, zenith wet delay (ZWD) is generated by deducting ZHD from zenith total delay (ZTD). ZTD can be directly estimated from precise GPS data processing. Finally, a conversion factor Q, which is used to map ZWD onto PWV, is determined by the water-vapor-weighted mean temperature  $T_m$  over a GPS station. The mapping function from ZWD to PWV is expressed as (Bevis et al., 1992):

$$PWV = \frac{ZWD}{O} = \frac{ZTD - ZHD}{O} \tag{3}$$

and *Q* is computed using following formula:

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$$Q = 10^{-6} \rho_{\scriptscriptstyle W} R_{\scriptscriptstyle V} \left[ \left( k_3 / T_{\scriptscriptstyle m} \right) + k_2' \right] \tag{4}$$

where  $\rho_w$  is the density of liquid water,  $R_v$  is the specific gas constant for water vapor,  $k_2' = (22.1 \pm 2.2) \text{K} \cdot \text{mbar}^{-1}$  and  $k_3 = (3.739 \pm 0.012) \times 10^5 \text{K}^2 \cdot \text{mbar}^{-1}$  are physical constants (Ning et al., 2016).

There are three main approaches to estimate  $T_m$ . They have respective advantages and disadvantages when they are applied for different purposes:

- (1) The integration of vertical temperature and humidity profiles are believed to be the most accurate method. The profile data can be extracted from radio soundings or NWP datasets (Wang et al., 2016). However, some inconveniences have to be endured. It usually takes considerable amounts time to acquire the NWP data, which is normally released with large volumes every 6 hours. This limits the use of NWP data in the near real-time GPS-PWV retrieving. Radiosonde data is another profile data source, but it has low spatial and temporal resolution. At most of the radiosonde sites, sounding balloons are daily cast at 00:00 UTC and 12:00 UTC. Furthermore, a large amount of GPS stations are not located close enough to the radio sounding sites. Therefore, such methods are appropriate for the climate research or the study of long-term PWV trends, but do not meet the real-time requirements.
- (2) Several global empirical models of  $T_m$  are established based on the analyses of  $T_m$  time series from NWP datasets or other sources (Yao et al., 2012; Chen et al., 2014; Bohm et al., 2015).  $T_m$  at any time and any location can be estimated from these models. They are often independent of the current meteorological observations which are required to be observed together with the GPS data. However, some important real variations, which may be dramatic during some extreme weather events, can be lost without the constraints of current real data (Jiang et al., 2016). Therefore, these modeled estimates are not accurate enough for high-precision meteorological applications, such as providing GPS-PWV estimates for weather prediction.
  - (3) Many studies indicated that  $T_m$  parameter has relationship with some surface meteorological elements, such as surface

air temperature or surface air humidity (Bevis et al., 1992; Yao et al., 2014a). These surface meteorological parameters can be measured accurately and rapidly.  $T_m$  is then estimated using these surface measurements. However, these studies also revealed that the relationships are often weak, except the  $T_s$ - $T_m$  relationship. For example, Bevis introduced the Bevis  $T_s$ - $T_m$  equation,  $T_m$ =0.72  $T_s$ +70.2 [K], according to analyzing 8712 radiosonde profiles collected at 13 sites in the U.S. over two years (Bevis et al., 1992). This equation has been widely used in many other studies.

According to Rohm's research (Rohm et al., 2014), GPS-ZTD can be estimated very precisely by real-time GPS data processing. This means that  $T_m$  is one of the key parameters in the near real-time GPS-PWV estimation. On the other hand, method (3) is the most suitable method for estimating  $T_m$  in near real-time because of its balance between timeliness and accuracy. The  $T_s$ - $T_m$  relationship has spatial-temporal variations. Several regional  $T_s$ - $T_m$  equations were established using the profile data over corresponding fields (Wang et al., 2012). However, it is not precise enough to apply the same  $T_s$ - $T_m$  model over a vast field, e.g., in the Indian region (Singh et al., 2014). Aside from this, some vast areas have no specific high-precision  $T_s$ - $T_m$  model, for example over the oceans. In general, significant differences exist between oceanic and terrestrial atmospheric properties, especially near the surface layer and within the boundary layer. The change of  $T_s$  from land to ocean may be very different from that of  $T_m$ . Therefore it is necessary to model the  $T_s$ - $T_m$  relationship over oceanic regions, since several ocean-based GPS meteorology experiments demonstrated the potential of such technique to retrieve PWV over the broad ocean (Rocken et al., 2005; Kealy et al., 2012). A global gridded  $T_s$ - $T_m$  model has been established in Lan's study (Lan et al., 2016). In Lan's model, the  $2.0^{\circ} \times 2.5^{\circ}$   $T_m$  data from "GGOS Atmosphere" and the  $0.75^{\circ} \times 0.75^{\circ}$   $T_s$  data from the European Centre for Medium-Range Weather Forecasts (ECMWF) reanalysis data are both smoothed to the resolution of  $4^{\circ} \times 5^{\circ}$ . Actually the  $T_s$ - $T_m$  relationship has time variation (Yao et al., 2014a). However, Lan's model is static and does not consider the time variation.

The objective of this study is mainly to (1) develop global gridded  $T_s$ - $T_m$  models without any smoothing of the data, then assess their precision, and (2) study the performances of GPS-PWV retrievals using our  $T_s$ - $T_m$  models. Table (1) lists the main differences between the  $T_s$ - $T_m$  model developed in this study and the other global used  $T_m$  models. In section 2, the data sources and determining methods of  $T_m$  are introduced in detail. Then, in section 3 we analyze the  $T_s$ - $T_m$  relationships and their variations on a global scale. Global-gridded  $T_s$ - $T_m$  estimating models in different forms are established and evaluated in section 4. Section 5 compares different PWV retrievals and section 6 presents conclusions based on our experiments.

**Table 1.** Main differences between  $T_s$ - $T_m$  models developed in this study and other global used  $T_m$  estimation models

Strategies \ T <sub>s</sub> -T <sub>m</sub> Models	Bevis model (Bevis et al., 1992)	Latitude-related linear model (Yao et al., 2014b)	Global-gridded model (Lan et al., 2016)	Time-varying global gridded model (our study)	GPT2w model (Bohm et al., 2015)
Applicable Regions	Regional/Global	Global	Global	Global	Global
Data Sources	Radiosonde	$T_s$ from the 0.75° $\times$ 0.75° ERA-Interim, and $T_m$ from the 2° $\times$ 2.5° "GGOS Atmosphere"	$T_s$ from the 0.75° $ imes$ 0.75° ERA-Interim, and $T_m$ from the 2° $ imes$ 2.5° "GGOS Atmosphere"	$T_s$ and $T_m$ both from the 0.75° $\times$ 0.75° ERA-Interim	$T_m$ from the $1^{\circ} \times 1^{\circ}$ ERA-Interim monthly mean data
Data Processing	Integrate radiosonde profiles	4° × 5° Sliding window smooth	4° × 5° Sliding window smooth	Integrate ERA- Interim profiles	Integrate ERA- Interim profiles
Variations in model	Static without any variations	Spatial variations depend on only latitude(15° latitude interval), but no temporal variations	4° × 5° global gridded, but no temporal variations	0.75° × 0.75° global gridded and considering time variations	1° × 1° global gridded, considering time variations, but independent of current surface observations

### 2. Data Sources and Methodology

#### 2.1 $T_m$ Definition

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 $T_m$  is defined as a function related to the temperature and water vapor pressure. It can be approximated as the following formula (Bevis et al., 1992):

$$T_{m} = \frac{\int \frac{e}{T} dz}{\int \frac{e}{T^{2}} dz} \approx \frac{\sum_{i=1}^{n} \frac{e_{i}}{T_{i}} \Delta z_{i}}{\sum_{i=1}^{n} \frac{e_{i}}{T_{i}^{2}} \Delta z_{i}}$$

$$(5)$$

where e and T respectively represent vapor pressure in hPa and temperature in Kelvin, i denotes the ith pressure level and  $\Delta z_i$  is the height difference of ith levels. Vapor pressure e is calculated using equation  $e=e_s\times RH$ ; RH is the relative humidity, and the saturation vapor pressure  $e_s$  can be estimated from the temperature observations using Goff-Gratch formula (Sheng et

al., 2013). For the ith level,  $e_i$  parameter at the middle height is calculated by vertically exponential interpolation of its two neighbor measurement points' water vapor pressure. The temperature is estimated by linear interpolation of the two neighbor temperatures. The integral intervals are from the earth's surface to the top level of the profile data. The height of the top level depends on the data sources we employed, which will be shown in section 2.2.

#### 2.2 Data sources and Methodology of $T_m$ Determination

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Equation (5) needs temperature, height and relative humidity values through the entire atmospheric column. The essential profile data can be obtained from the radiosondes or NWP datasets.

We employed radiosonde data from the Integrated Global Radiosonde Archive (IGRA. ftp://ftp.ncdc.noaa.gov/pub/data/igra) to calculate  $T_m$ . Version 2.0 of the IGRA-derived sounding parameters provides pressure, geopotential height, temperature, saturation vapor pressure, and relative humidity observations at the observed levels. Bias may be introduced if the integrals were terminated at lower levels (Wang et al., 2005), thus the integrations were performed up to the topmost valid radiosonde data. According to our quality control processes, some radiosonde profile data were rejected. In each profile, the surface observations must be available and the top profile level should not be lower than 300 hPa standard level. Furthermore, the level number between the surface and the top level should be greater than 10 to avoid too sparse vertical profile. At most of the radio sounding stations, sounding balloons are launched every 12 hours, and their ascending paths are assumed to be vertical.

Profile data are usually provided by NWP products at certain vertical levels. The ERA-Interim product from ECMWF provides data on a regular 512 longitude by 256 latitude N128 Gaussian grid after the grid transforming performed by the NCAR's Data Support Section (DSS). On each grid node of ERA-Interim, temperature, relative humidity and geopotential at 37 isobaric levels from 1000 hPa to 1 hPa can be obtained. Dividing the geopotential by constant gravitational acceleration value ( $g \approx 9.80655 \text{ m/s}^2$ ), we can determine the geopotential heights of the surface and levels. Datasets are available at 00:00, 06:00, 12:00 and 18:00 UTC every day and have been covering a period from 1979.01 to present.

In theory, the computation of equation (5) should be integrated through the entire atmospheric column, and the geopotential height should be converted to the geometric height. However, water vapor is solely concentrated in the

troposphere, and most of it is specifically located within the first 3 kilometers above sea-level. Moreover, in the two selected datasets, the geopotential heights of top pressure levels are approximately 30~40 km. Geopotential height is very close to geometric height in such height ranges. According to our computation, the relative difference between them is only between 0.1 %~0.9 %. In fact, the height difference  $\Delta z$  can be replaced by the geopotential height difference  $\Delta h$  in equation (5), since the division operation can almost eliminate the difference between the two different height types. The  $T_m$  value nearly has no change after such height replacement. For the convenience of calculations, we directly employed the geopotential height variable. In this paper, we denoted the  $T_m$  derived from ERA-Interim as  $T_{m ERAI}$ .

At each reanalysis grid node, the computation of equation (5) always starts from the surface height to the top pressure level. The pressure levels below surface height were rejected in the calculation.  $T_s$  is defined as the variable of "temperature at 2 meters above ground", and surface water vapor pressure can be derived from the "2 meter dewpoint temperature" variable in ERA-Interim. These  $T_s$  were also used in the regression analyses between  $T_m$  and  $T_s$ .

#### 3. Correlation between Ts and Tm

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Many studies have indicated the close relationship between  $T_s$  and  $T_m$ . However,  $T_m$  is also found to not be closely related to  $T_s$  in some regions, e.g., in the Indian zone (Raju et al., 2007). Using the  $T_m$  and  $T_s$  generated from the global gridded reanalysis data, we are able to study the  $T_s$ - $T_m$  relationship in detail.

We first carried out a linear regression analysis on the four years long  $T_s$  and  $T_m$  data generated from the point radiosonde data and the global gridded ERA-Interim datasets. The data cover the period from 2009.01 to 2012.12. The analysis results are shown in figure (1). Although the two datasets have different temporal resolutions (12 hours for the radiosonde data and 6 hours for the ERA-Interim data) and spatial resolutions, both analyses agree with each other. This is expected because the radiosonde data have been assimilated into the ERA-Interim products. Our analyses also indicate that the  $T_s$ - $T_m$  correlation coefficient is generally related to the latitude. The same conclusion has been drawn in other studies (Yao et al., 2014b). Significant positive correlation coefficients can be found in the mid- and high- latitudes and reaches the maximum in the Polar Regions. Then, the correlation coefficients drop dramatically in the low latitudes. We further analyzed the main reason for

these changes.  $T_m$  variable in the low latitudes is stable, thus it shows independence of the other parameters. To study the variations of  $T_s$  and  $T_m$ , we illustrated the denary logarithm values of their standard deviations in figure (2). It is evident that  $T_m$  varies to a lesser degree in the low latitudes. Aside from the latitude-related features, there are obvious differences of the  $T_s$ - $T_m$  correlation coefficient between land and ocean. Analyses even demonstrate negative correlation coefficients over certain oceans, e.g., low-latitude Western Pacific, Bay of Bengal or Arabian Sea. Unreliable regression analysis results may be derived when the  $T_s$  and  $T_m$  data both have small variations. In figure (3), scatter plots of  $T_s$  and  $T_m$  from ERA-Interim at two locations N 0.35° E 180.00° and N 70.53° E 180.00° are given. As the blue dots show, the  $T_s$ - $T_m$  relationship is weak in the areas near the equator. It is because that the entire variation ranges of  $T_s$  and  $T_m$  are both below 10 K. As the magenta line shows, the linear regression result also makes less sense. The  $T_s$ - $T_m$  correlation coefficient is only -0.0893. Other than the large spatial variations, studies have revealed that  $T_s$ - $T_m$  relationships also have temporal variations (Wang et al., 2005). Therefore, a good  $T_s$ - $T_m$  model should take both the spatial and temporal variations into consideration, and this is the main aim in the following sections.

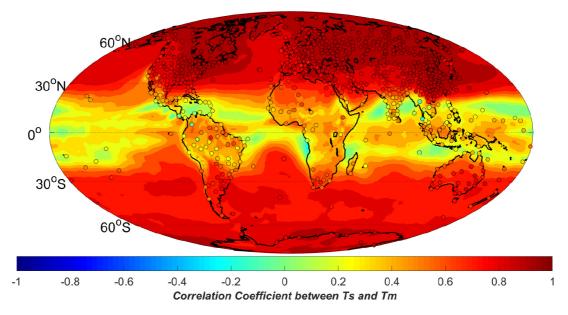


Figure 1: Correlation coefficients between  $T_s$  and  $T_m$  generated from radiosonde data (dots) and ERA-Interim reanalysis datasets (color-filled contours) over a period of 4 years from 2009 to 2012.

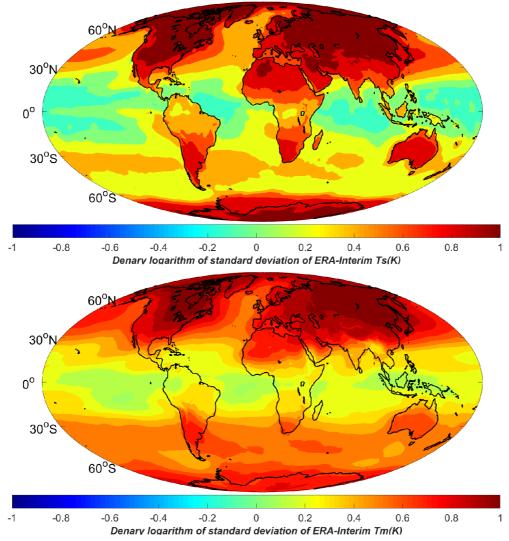
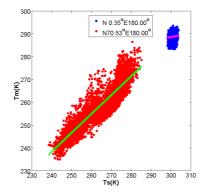


Figure 2: Denary logarithm of the standard deviation of (top)  $T_s$  and (bottom)  $T_m$  generated from the ERA-Interim over a period of 4 years from 2009 to 2012. Temperature unit is Kelvin.



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Figure 3:  $T_s$ - $T_m$  scatter plots at two locations: (blue dots) N 0.35° E 180.00° and (red dots) N 70.53° E 180.00°, the magenta and green lines are their linear fitting curves. Temperature unit is Kelvin.

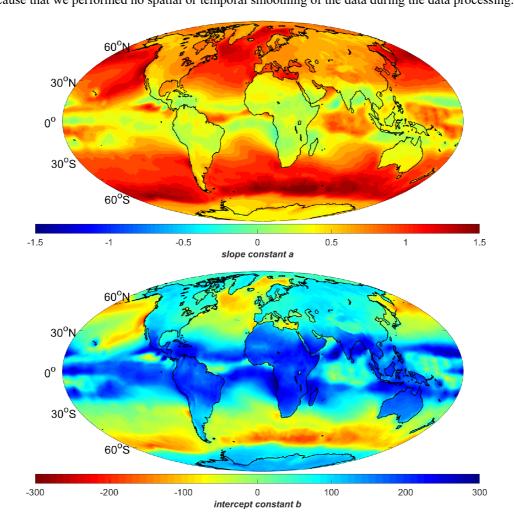
#### 4. Developments of Global-gridded $T_s$ - $T_m$ models

Since the  $T_s$ - $T_m$  relationship has large spatial variations, it is necessary to establish detailed global gridded  $T_s$ - $T_m$  estimating equations for precise GPS-PWV estimations. In this section, a static global gridded model and a time-varying global gridded model are established and assessed.

#### 4.1 Static global-gridded T<sub>s</sub>-T<sub>m</sub> model

Linear formula expressed as  $T_m = aT_s + b$  has been adopted in many studies. Based on the  $T_s$  and  $T_m$  products from ERA-Interim, we performed linear fittings of  $T_s$  versus  $T_m$  on each grid point. Then, the slope constant (a), the intercept constant (b) and the fitting root mean square error (RMSE) of each linear expression were calculated and contoured in figure (4). The a and b values are related to the latitude as well as the underlying surface. In the mid-high latitudes over the northern hemisphere, constant a value varies from 0.6 to 0.8, and constant b is approximately  $100\sim50$  over most of the continents. The constants in the Bevis equation are within these value ranges. Constant a is smaller (approximately  $0.5\sim0.7$ ) over the lands in the mid-high latitudes over the southern hemisphere. Especially, there are acute value changes of constant a and a from land to ocean in the mid-high latitudes. The reason for this is the different variation features of a0 and a1, which can be seen in figure (2). In the low latitudes, a1 value is smaller than the other regions. This is because of the low variations of a1 and a2. The fitting RMSE are within a2-4 K over the mid-high latitude lands, and relatively lower values over the oceans or the low latitudes. The reason

for the low RMSE around the equator is the smaller fluctuations of  $T_m$ . Meanwhile, there is no RMSE larger than 4.5 K in the results of our model. The precision and the resolution of our static model is clearly better than previous models (Lan et al., 2016). It is because that we performed no spatial or temporal smoothing of the data during the data processing.



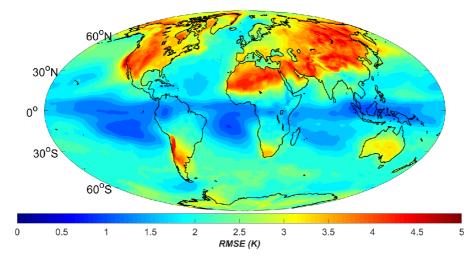


Figure 4: Distribution of the (top) slope constant a, (middle) intercept constant b, and (bottom) RMSE of static linear  $T_s$ - $T_m$  equations at ERA-Interim grid nodes. Temperature unit is Kelvin.

# 4.2 Time-varying global-gridded $T_s$ - $T_m$ model

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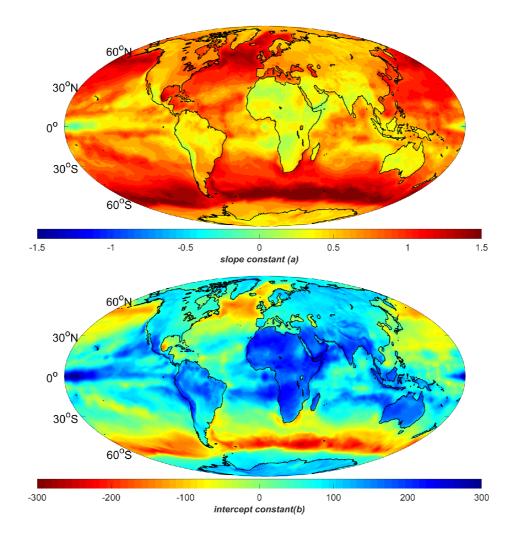
The  $T_s$ - $T_m$  relationship has time variations which should also be considered in the precise  $T_s$ - $T_m$  model. Therefore, a time-varying equation is applied for  $T_s$ - $T_m$  regression at each grid node:

$$T_{m} = aT_{s} + b + m_{1}\cos\left(\frac{doy}{365.25}2\pi\right) + m_{2}\sin\left(\frac{doy}{365.25}2\pi\right) + n_{1}\cos\left(\frac{doy}{365.25}4\pi\right) + n_{2}\sin\left(\frac{doy}{365.25}4\pi\right) + p_{1}\cos\left(\frac{hr}{12}\pi\right) + p_{2}\sin\left(\frac{hr}{12}\pi\right)$$
(6)

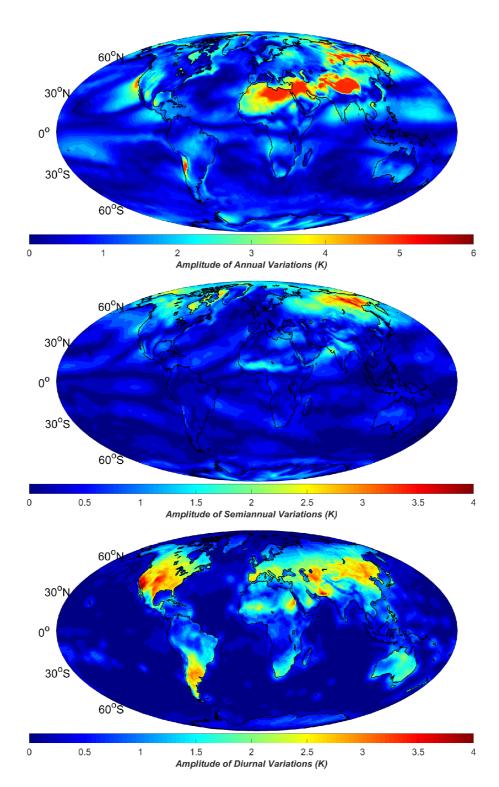
where *doy* represents the observed day of year and hr is the observed hour in UTC time;  $(m_1, m_2)$ ,  $(n_1, n_2)$  and  $(p_1, p_2)$  are the fitting coefficients of corresponding formula items. These formula items can reflect the amplitudes of annual, semiannual and diurnal variations in our  $T_s$ - $T_m$  models.

Our regression indicate that the static terms in equation (6), which are determined by the coefficients a and b, are similar to the static models in section 4.1 except some differences over the oceans. Other than a and b, we also illustrated the amplitudes of annual, semiannual, and diurnal terms. We can see that there are large annual variations (amplitude > 5 K) in the vast regions from Tibet to North Africa, and in some places of the Siberia and Chile. Large diurnal variations (amplitude > 3 K) mainly occur in the mid-latitude lands such as Northeast Asia or North America. Semiannual variations, however, are small in most

of areas except some high-latitudes (amplitude > 3 K). All variations are smaller over the oceans due to the slower temperature changes over the waters than the lands. The estimated  $T_m$ 's RMSE is also contoured in figure (5), and we can see that the RMSE dropped significantly in the regions with large annual or diurnal variations.







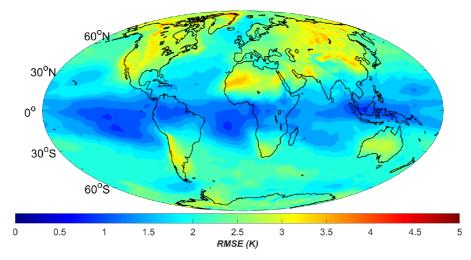


Figure 5: (top) The slope constant a, (second) intercept constant b, amplitudes of  $T_m$  (third) annual, (forth) semiannual and (fifth) diurnal terms in our time-varying global gridded  $T_s$  - $T_m$  model, and (bottom) the model estimated  $T_m$  's RMSE distribution. Temperature unit is Kelvin.

#### 4.3 Assessments of $T_s$ - $T_m$ models

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To assess the precision of the  $T_s$ - $T_m$  models further using other independent data sources, we generated  $T_m$  and  $T_s$  from the radiosonde data at 723 radiosonde stations in the year 2016. These data are not assimilated into the 2009~2012 ERA-Interim datasets. As a result, we can regard them as independent data to our model. At each radiosonde site, different  $T_s$ - $T_m$  models were employed to calculate  $T_m$ . In addition, we also estimated  $T_m$  using the 1° × 1° GPT2w model (Bohm et al., 2015), which is a global gridded  $T_m$  empirical model independent of the surface meteorological observation data. Then, these calculated  $T_m$  will be evaluated by comparing them with the radiosonde's integrated  $T_m$  (denoted as  $T_{m_m}$ Rs) twice a day.

The model estimations of  $T_m$  are denoted as  $T_{m\_Bevis}$ ,  $T_{m\_LatR}$ ,  $T_{m\_static}$ ,  $T_{m\_varying}$ , and  $T_{m\_GPT2w}$  from the Bevis equation, Yao's latitude-related model, our static global gridded model, time-varying global gridded model, and the GPT2w model. When the global gridded models are employed, there is a problem that a radiosonde station may not be located at a grid node. Therefore, the coefficients in  $T_s$ - $T_m$  equations should be horizontally interpolated from the neighboring grids to the radiosonde sites. The interpolation formula is expressed as (Jade and Vijayan, 2008):

$$C_{site} = \sum_{i=1}^{4} w^i C_{grid}^i \tag{7}$$

 $C_{site}$  and  $C_{site}^i$  represent the coefficients in  $T_s$ - $T_m$  equations at the radiosonde site location and its neighboring grids, respectively.  $w^i$  is the interpolation coefficients, which is determined using equation:

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$$w^{i} = \frac{\left(R\psi^{i}\right)^{-\lambda}}{\sum_{j=1}^{4} \left(R\psi^{j}\right)^{-\lambda}} \tag{8}$$

where R=6378.17 km is the mean radius of the earth,  $\lambda$  is the scale factor which equals one in our study, and  $\psi^i$  is the angular distance between the *i*th grid node and the station's position.  $\psi^i$  is computed using following formula related to latitude  $\varphi$  and longitude  $\theta$ :

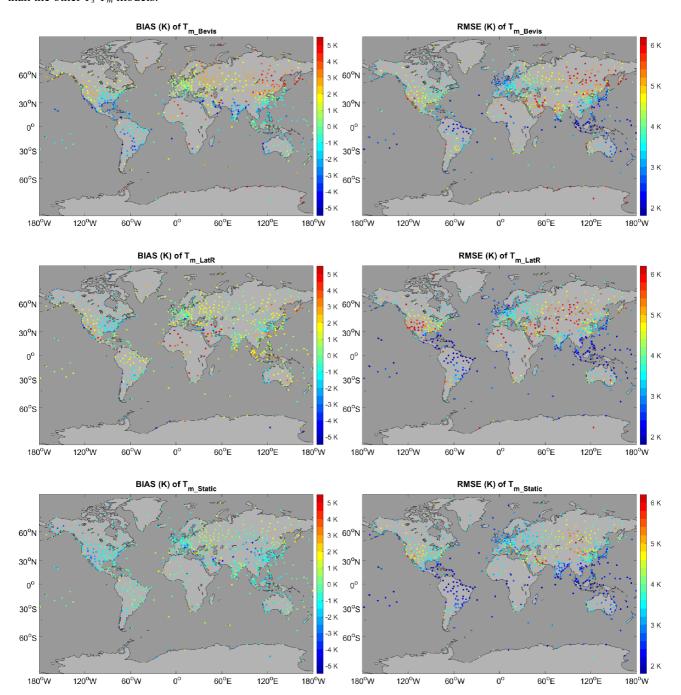
$$\cos \psi_i = \sin \varphi_i \sin \varphi + \cos \varphi_i \cos (\theta_i - \theta) \cos \varphi \tag{9}$$

Considering the reanalysis grids are definite, and every radiosonde site is in situ; we can compute the interpolation coefficients in equation (5) for all of the radiosonde stations. Then, these coefficients are stored as constants to avoid reduplicating the calculation.

Taking  $T_{m\_RS}$  as the reference values, we calculated the bias and RMSE of  $T_{m\_Bevis}$ ,  $T_{m\_LatR}$ ,  $T_{m\_static}$ ,  $T_{m\_varying}$ , and  $T_{m\_GPT2w}$  at each radiosonde site. The results are illustrated in figure (6). Obviously in many regions, Bevis equation has bad precision with the absolute bias and RMSE are both larger than 5 K.  $T_{m\_LatR}$  can reduce the estimated biases in many areas, but the RMSE remain large. Large biases still exist at quite a few radiosonde stations, e.g. in Africa or West Asia.  $T_{m\_static}$  and  $T_{m\_GPT2w}$  remove the large  $T_m$  biases at most of the radiosonde stations.  $T_{m\_varying}$  performs significantly better over the world, especially in the Middle East, North America, Siberia region, etc.

Detailed statistics of the bias's and RMSE's distributions of different models are shown in figure (7) and table (2). At over 97.37 % of the radiosonde stations, the biases of  $T_{m\_varying}$  are within -3~3 K. Large positive biases (> 3 K) nearly disappear in  $T_{m\_varying}$ . In contrast, there are significant large biases in  $T_{m\_Bevis}$  and  $T_{m\_LatR}$ . Improvements in RMSE are more evident.  $T_{m\_varying}$ 's RMSE are smaller than 4 K at over 91 % of the radiosonde sites, while few sites (<1 %) have RMSE larger than 5 K. This is clearly better than the other models. In  $T_{m\_Bevis}$  and  $T_{m\_LatR}$ , there are more than 17 % of the radiosonde sites have

RMSE larger than 5 K. The overall performance of  $T_{m\_GPT2w}$  is very close to  $T_{m\_Bevis}$ , except that its absolute bias is smaller than the other  $T_s$ - $T_m$  models.



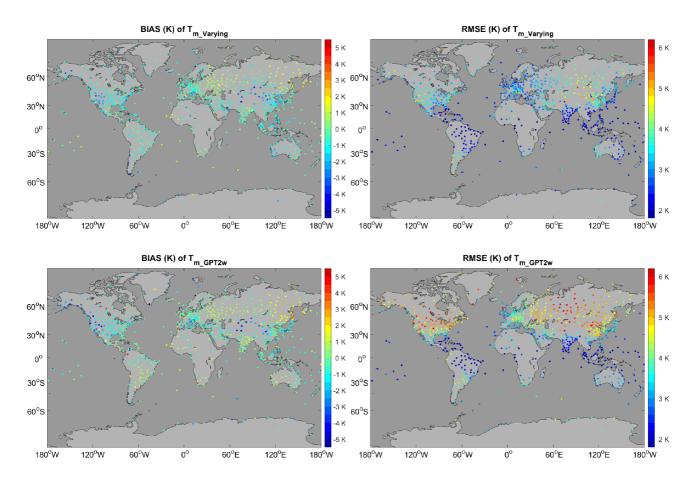
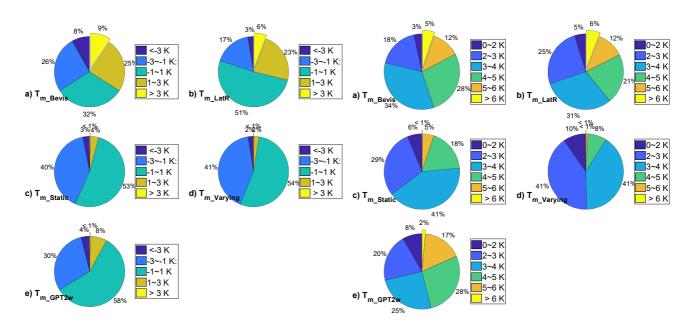


Figure 6: (left) The bias and (right) RMSE of the estimated  $T_m$  from (top) Bevis equation, (second) Yao's latitude-related model, (third) static global gridded model, (forth) time-varying global gridded model and (bottom) GPT2w model at each radiosonde station. Reference data are the radiosonde data of the year 2016. Temperature unit is Kelvin.



1) Bias distribution 2) RMSE distribution Figure 7: (left) The bias's and (right) RMSE's distributions of  $T_{m\_Bevis}$ ,  $T_{m\_LatR}$ ,  $T_{m\_static}$ ,  $T_{m\_varying}$  and  $T_{m\_GPT2w}$  compared with the

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Table 2: Statistics of  $T_m$  estimates from different models. Reference data are the radiosonde  $T_m$  derivations

radiosonde data at 723 stations in the year 2016. Temperature unit is Kelvin.

Statistics	$T_{m\_Bevis}$	$T_{m\_LatR}$	$T_{m\_static}$	$T_{m\_varying}$	$T_{m\_GPT2w}$
Average value of absolute $T_m$ bias (K)	1.88	1.30	1.13	1.08	1.06
Average value of $T_m$ RMSE (K)	3.95	3.81	3.36	3.01	3.80
Average relative RMSE of $T_m$ (%)	1.44	1.39	1.22	1.09	1.39
Max Relative RMSE of mean $T_m$ (%)	3.69	4.26	2.40	2.19	4.31
% of sites with $T_m$ RMSE < 4 K	55.19	61.00	76.49	91.01	53.94
% of sites with $T_m$ Relative RMSE less than 1.5 %	59.47	64.73	78.01	89.76	56.43

To identify the superior  $T_m$  estimation model at each radiosonde site, we employed the following statistical tests under the assumption of normal distribution of the estimated  $T_m$ 's error:

(1) First, Brown-Forsythe's tests (Brown and Forsythe, 1974) of equality of variances were carried out at each site for estimating the  $T_m$  errors from two different models, e.g., model A and B. The purpose of this step is to determine whether there is significant variance difference between the  $T_m$  results. If the test rejects the null hypothesis at a 5 % significance level that the errors of model A and B have the same variance, the model with the smaller sample variance is regarded as the better one.

However, if the test does not reject the homogeneity of variances, analysis of variance (ANOVA) is performed in the next step.

(2) ANOVA is a technique used to analyze the differences among group means (Hogg, 1987). It evaluates the null hypothesis that the samples all have the same mean against the alternative that the means are not the same. If the null hypothesis is rejected at a 5 % significance level, the  $T_m$  sample with smaller absolute mean value is believed to be better. Otherwise, we think that two models perform almost the same at this radiosonde site.

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(3) After multiple tests and comparisons, the best model at each radiosonde stations may be identified. However, at some sites no superior model can be confirmed. All the models are believed to have the equivalent performances.

Finally, we counted the number of sites at which each  $T_m$  model respectively performed the best. The results are given in table (3). The time-varying global gridded model is superior to the others at 434 radiosonde stations (60.03 % of all sites), while the second-best estimation,  $T_m$   $_{GPT2w}$ , is superior at only 12.86 % of the sites.

Table 3: Number of radiosonde sites at which the five global applied  $T_m$  estimation models respectively perform superiorly

Superior model	None	Tm_Bevis	$T_{m\_LatR}$	$T_{m\_static}$	T <sub>m_varying</sub>	$T_{m\_GPT2w}$
Number of sites	50	46	61	39	434	93

A comprehensive research on the uncertainty of GPS-PWV can be found in Ning's work (Ning et al., 2016). The uncertainties of the ZTD, ZHD and conversion factor *Q* have been studied in detail. The total uncertainty of GPS-derived PWV is:

$$\sigma_{PWV} = \frac{1}{Q} \sqrt{\sigma_{ZTD}^2 + \left(\frac{2.2767\sigma_{Ps}}{f(\varphi, H)}\right)^2 + \left(\frac{P_s\sigma_c}{f(\varphi, H)}\right)^2 + \left(PWV \cdot \sigma_{Q}\right)^2}$$
(10)

where  $\sigma_{PWV}$ ,  $\sigma_{ZTD}$ ,  $\sigma_{Ps}$ , and  $\sigma_{Q}$  are the uncertainty of the GPS-PWV, ZTD estimates,  $P_s$  observations and conversion factor Q, respectively.  $\sigma_c = 0.0015$  denotes the uncertainty of the constant C = 2.2767 in equation (1), PWV is the GPS-PWV value and

$$\sigma_{Q} = 10^{-6} \rho_{W} R_{v} \sqrt{\left(\frac{\sigma_{k_{3}}}{T_{m}}\right)^{2} + \sigma_{k_{2}}^{2} + \left(k_{3} \frac{\sigma_{T_{m}}}{T_{m}^{2}}\right)^{2}}$$
(11)

where  $\sigma_{k_3}$ ,  $\sigma_{k'_2}$ , and  $\sigma_{T_m}$  denote the uncertainty of the  $k_3$ ,  $k'_2$  and  $T_m$  in equation (4).

Table 4: List of the uncertainty values for the error sources in GPS-PWV

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Variables	$\sigma_{_{ZTD}}$ [mm]	$\sigma_{\!\scriptscriptstyle Ps}$ [hPa]	$\sigma_{\scriptscriptstyle C}$	$\sigma_{_{\!k_{\!2}^{'}}}$ [K hPa $^{ ext{-}1}$ ]	$\sigma_{k_3} [10^5 \times \text{K}^2 \text{ hPa}^{-1}]$
Uncertainty value	4	0.5	0.0015	2.2	0.012

However, Ning's study assumed the  $T_m$  were obtained from NWP models so the  $T_m$ 's uncertainty was set to be small  $(\sigma_{T_m}=1.1 \text{ K})$ . At each site, we replaced the  $\sigma_{T_m}$  by the  $T_m$ 's RMSE shown in figure (6) to re-evaluate the  $\sigma_Q$ , while the other uncertainties are assumed to be the corresponding values listed in table (4) based on Ning's summaries. The  $\sigma_{P_S}$  equals 0.2 hPa in Ning's paper, however we enlarged it to 0.5 hPa in consideration of the possible worse performance of the surface barometers. The  $\sigma_Q$  in equation (11) was estimated using  $T_{m\_Bevis}$ ,  $T_{m\_LatR}$ ,  $T_{m\_Static}$ ,  $T_{m\_varying}$ , and  $T_{m\_GPT2w}$ , respectively. We also calculated the mean PWV and  $T_m$  values in equation (10) and (11). Then  $\sigma_{PWV}$  results were generated from the different  $\sigma_Q$  estimates using equation (10). Considering  $T_m$ 's errors is propagated to Q, we calculated the percentage of  $\sigma_{PWV}$  caused by the uncertainty of Q (denoted as PQ). Larger PQ means more contribution of  $T_m$ 's errors to the uncertainty of GPS-PWV. Comparisons between the  $PQ_{Varying}$  (PQ estimated from  $T_{m\_varying}$ ) and the other PQ estimates are illustrated in figure (8). Significantly  $PQ_{Varying}$  is smaller than the PQ estimates from other  $T_m$  models at most of the sites. The PQ value grows with the PWV's increase, which can also be derived from equation (10). At some sites PQ drops more than 20 % from  $PQ_{Bevis}$  to  $PQ_{Varying}$ . It is evident that more precise  $T_m$  estimation model is effective to reduce the contribution of  $T_m$  error to the uncertainty of GPS-PWV.

It is worth mentioning that the uncertainty of ZHD may be underestimated in some situations. There are two reasons for this. Firstly, the calculation of ZHD assumes that the water vapor is not contributed to the mass of the atmosphere. The ZHD error introduced by this assumption is often negligible. But in some very wet regions, the mass of water vapor could produce significant errors to the ZHD calculation. Secondly and more importantly, the error of  $P_s$  in equation (1) can be very large sometime. From table (4) we can see that the  $\sigma_{P_s}$  is small, which is reasonable when the surface barometer is calibrated routinely and equipped together with the GPS antenna. However, if there were significant height difference between the GPS antenna and the barometer, the error of ZHD would increase significantly. Snajdrova (Snajdrova et al., 2006) found that 10 m of height difference approximately causes a difference of 3 mm in the ZHD. On the other hand,  $P_s$  can be generated from NWP data if there were no nearby barometer to GPS site. The error of  $P_s$  could be very large using this method (Means and Cayan, 2013; Jiang et al., 2016). In these cases, the GPS-PWV's error reduction due to the more precise  $T_m$  estimation will be very limited. When the  $\sigma_{P_s}$  is larger than 5 hPa, most of the pQ values are smaller than 10 %, while the error associated with the calculation of ZHD can contribute more than 80 % of the GPS-PWV's error.

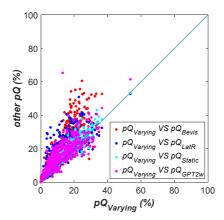


Figure 8: Comparisons between  $pQ_{Varying}$  and the other pQs, where pQ represents the percentage of the uncertainty cause by conversion factor Q in total GPS PWV uncertainty.

In figure (9), the  $T_m$  series at IGRA station NO.62378 (N 29.8628° E 31.3492°) are given. We can see that large negative biases (< -5 K) between  $T_{m\_Bevis}$  (or  $T_{m\_LatR}$ ) and  $T_{m\_RS}$  exist.  $T_{m\_static}$  performs only slightly better from July to October. However,  $T_{m\_varying}$  and  $T_{m\_GPT2w}$  can eliminate most of the seasonal errors. Different properties of  $T_m$  series appear at another IGRA station NO.40841 (N 30.2500° E 56.9667°). Some observation data are missing, but we can still see that there are large positive

differences (> 5 K) between  $T_{m\_Bevis}$  (or  $T_{m\_LatR}$ ) and  $T_{m\_RS}$  throughout the year. The biases of  $T_{m\_static}$  are much smaller, but some large errors still appear in many months. The  $T_{m\_varying}$ , however, performs as well as at the NO.62378 IGRA station, with small biases and good capturing of  $T_m$ 's variations. The time series of  $T_{m\_GPT2w}$  are smooth so they cannot capture the large fluctuations of  $T_m$  time series, which causes its worse accuracy than  $T_{m\_varying}$ .

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On the other hand, even  $T_{m\_varying}$  have large differences from  $T_{m\_RS}$  at a few IGRA stations. It is because that our fitting analyses were based on the  $T_m$  values derived from ERA-Interim profiles. The quality of ERA-Interim data can be very poor in the regions with sparse observation data (Itterly et al., 2018). Improvements on the reanalysis data should be performed in future.

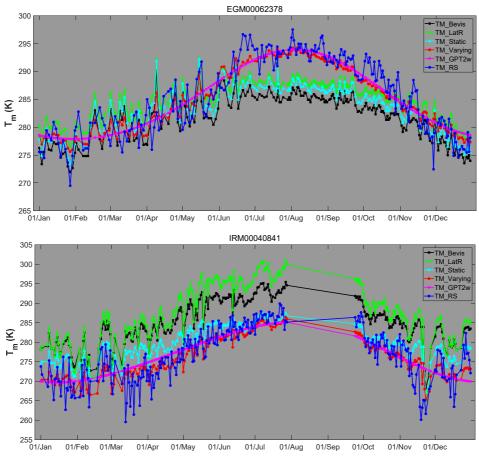


Figure 9:  $T_m$  series of  $T_{m\_Bevis}$ ,  $T_{m\_LatR}$ ,  $T_{m\_static}$ ,  $T_{m\_varying}$ ,  $T_{m\_GPT2w}$  and  $T_{m\_RS}$  at (top) EGM00062378 and (bottom) IRM00040841 IGRA sites. Temperature unit is Kelvin.

#### 5. GPS-PWV retrieving experiments

GPS-PWV has different error sources with different properties as described in section 4.3. It is complicated to evaluate GPS-PWV uncertainty due to the lack of collaborated additional independent techniques to monitor water vapor at the GPS site. Therefore, several experiments were carried out to investigate the GPS-PWV precision carefully.

#### 5.1 Impact of $T_m$ estimation

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To study the impacts of  $T_m$  on the GPS-PWV retrievals, we first downloaded GPS ZTD products (Byun and Bar-Sever, 2009) several **IGS** sites 2016 from the **CDDIS** FTP address the year (ftp://cddis.gsfc.nasa.gov/pub/gps/products/troposphere/zpd). These selected GPS sites were equipped with meteorological sensors so the surface pressure and temperature measurements could also be obtained. ZHD was calculated using equation (1). It is deducted from ZTD to obtain ZWD. Then,  $T_m$  was generated through six approaches: the first five  $T_m$  series were  $T_m$  Bevis,  $T_{m \ LatR}$ ,  $T_{m \ static}$ ,  $T_{m \ varying}$ , and  $T_{m \ GPT2w}$ . The sixth  $T_{m \ was}$  integrated from the ERA-Interim profiles and interpolated to each GPS site (Jiang et al., 2016; Wang et al., 2016). Finally, the GPS-PWV was generated from the ZWD and the six different  $T_m$ estimates. We denoted these GPS-PWV sets as  $PWV_{BTm}$ ,  $PWV_{LTm}$ ,  $PWV_{STm}$ ,  $PWV_{VTm}$ ,  $PWV_{GTm}$ , and  $PWV_{ETm}$ . The only difference between these GPS-PWV estimations is the  $T_m$  estimation model; therefore, the impacts of other errors are excluded.

The  $T_m$  from ERA-Interim is believed to be the most accurate among our  $T_m$  estimates at the selected GPS sites. We regarded the PWV<sub>ETm</sub> as reference values to assess the other PWV. Finally, the GPS-PWV at 74 IGS sites were obtained. Each GPS-PWV series have over one hundred compared points. The relative RMSE of PWV<sub>BTm</sub>, PWV<sub>LTm</sub>, PWV<sub>STm</sub>, PWV<sub>VTm</sub> and PWV<sub>GTm</sub> at these selected stations were calculated and illustrated in figure (10). The detailed statistics are given in table (5). The mean relative error of all sites drops from 1.18 % of PWV<sub>BTm</sub> to 0.91 % of PWV<sub>VTm</sub>. At most of the sites, PWV<sub>VTm</sub> has the minimum relative errors and is superior to the other PWV retrievals. PWV<sub>STm</sub> and PWV<sub>VTm</sub> obtain relative RMSE smaller than 1.0 % at 55 sites, while only 28 sites of PWV<sub>BTm</sub>, 31 sites of PWV<sub>LTm</sub> and 22 sites of PWV<sub>GTm</sub> perform similarly. For example, at ALIC site which is located in Australia with mean PWV of approximately 23 mm, the relative RMSE dropped from 1.97 % of PWV<sub>BTm</sub> to 1.10 % of PWV<sub>VTm</sub>. The time series of the relative differences of PWV<sub>BTm</sub>, PWV<sub>LTm</sub>, PWV<sub>STm</sub>, PWV<sub>STm</sub>, PWV<sub>VTm</sub>, and PWV<sub>GTm</sub> are given in figure (11). We found that some relative RMSE could reduce more than 2 % from PWV<sub>BTm</sub>

to  $PWV_{VTm}$ . Obviously,  $PWV_{BTm}$  and  $PWV_{LTm}$  have larger relative errors throughout the year while the PWV differences are significantly larger only in the summer season. It is because that the  $T_m$ 's variations in summer are not modeled well by both Bevis model and the latitude-related model. Furthermore, the higher PWV values in summer enlarge the PWV differences.  $PWV_{STm}$  eliminate those large differences but still retain some residual errors. These residuals are removed more than 1.0 mm in  $PWV_{VTm}$  further.  $PWV_{GTm}$  has some large errors during the period from May to July. All of these results demonstrate that our time-varying model has precision advantages.

Table 5: Statistics about the relative errors of different PWV retrievals

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Statistics	PWV <sub>BTm</sub>	PWV <sub>LTm</sub>	PWV <sub>STm</sub>	PWV <sub>VTm</sub>	PWV <sub>GPT2w</sub>
Mean relative RMSE of all sites	1.18 %	1.12 %	0.93 %	0.91 %	1.32 %
Number of sites with relative errors $< 1.0 \%$	28	31	55	55	22

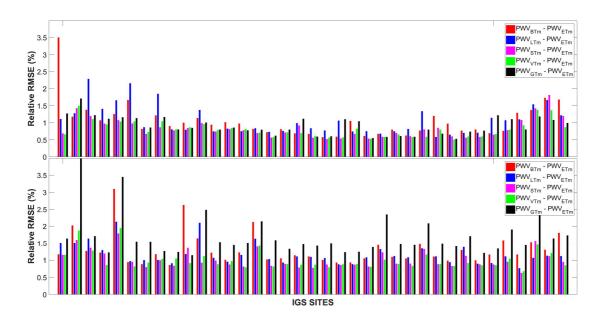


Figure 10: Relative RMSEs of  $PWV_{BTm}$ ,  $PWV_{STm}$ ,  $PWV_{VTm}$  and  $PWV_{GTm}$  compared with  $PWV_{ETm}$  at 74 IGS stations in the year 2016

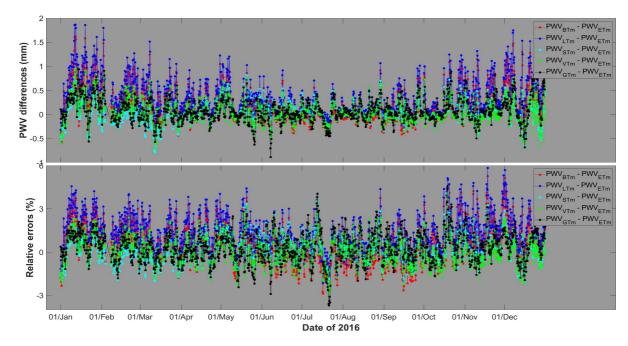


Figure 11: (top) PWV differences and (bottom) relative differences of PWV<sub>BTm</sub>, PWV<sub>LTm</sub>, PWV<sub>VTM</sub> and PWV<sub>GTm</sub> compared with PWV<sub>ETm</sub> at the ALIC station in the year 2016. PWV unit is mm.

# 5.2 Comparisons between GPS-PWV and radiosonde PWV

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Among our selected 74 IGS sites, there are only 11 sites located within 5 km to the nearby IGRA radiosonde stations. At these common stations, we generated PWV from the radiosonde data (PWV<sub>RS</sub>) by adjusting the sounding profiles to the heights of IGS sites. It worth noting that geoid undulation corrections should be carried out on each IGS site's geoid height (Jiang et al., 2016). Then, we compared PWV<sub>BTm</sub>, PWV<sub>LTm</sub>, PWV<sub>STm</sub>, PWV<sub>VTm</sub>, PWV<sub>GTm</sub>, and PWV<sub>ETm</sub> with PWV<sub>RS</sub>. Figure (12) shows the statistics. The RMSE of GPS-PWV are approximately 1~5 mm. Comparisons indicate that the RMSE of different GPS-PWV retrievals are very close (differences < 0.2 mm) regardless of the applied  $T_m$  sources at most of the selected sites. This means that other errors (e.g. ZTD estimation errors or sounding sensors errors) instead of  $T_m$  occupied the differences between the GPS-PWV and the radiosonde PWV. Actually, each sounding does not represent the vertical sounding centered at the radiosonde site because of the complex path of the balloon. And GPS-PWV represents the averaged value of the water vapor zenithal projection from all the slant signal paths during the observation period. Such differences can introduce significant uncertainty to our comparisons. However, we still found obvious gaps between PWV at NRIL (N 88.3598° E 69.3618°, 4.1

km away from the NO.23078 radiosonde site). The RMSE decreases from 2.29 mm of PWV<sub>BTm</sub> to 1.84mm of PWV<sub>VTm</sub> and 1.42 mm of PWV<sub>ETm</sub>. As shown in figure (13), the large PWV differences appear mainly from May to September. During those five months, mean GPS-PWV differences to PWV<sub>RS</sub> decrease by over 30 % from 2.52 mm of PWV<sub>BTm</sub> to 1.67 mm of PWV<sub>VTm</sub>. Some differences can reduce  $1\sim2$  mm during the wetter months. The accuracy of PWV<sub>GTm</sub> is close to PWV<sub>VTm</sub> at this site, which indicates that the spatiotemporal variations of  $T_m$  are also modeled very well by GPT2w model.

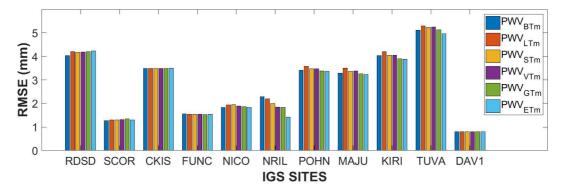


Figure 12: RMSE of PWV<sub>BTm</sub>, PWV<sub>STm</sub>, PWV<sub>VTm</sub>, PWV<sub>GTm</sub> and PWV<sub>ETm</sub> compared with PWV<sub>RS</sub> at 11 IGS stations in 2016. PWV unit is mm.

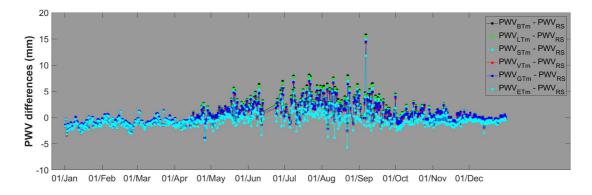


Figure 13: PWV differences of PWV $_{BTm}$ , PWV $_{LTm}$ , PWV $_{STm}$ , PWV $_{CTm}$  and PWV $_{ETm}$  compared with PWV $_{RS}$  at NIRL station in the year 2016. PWV unit is mm.

# 405 6. Summary and conclusion

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In this study, we estimated  $T_m$  using the temperature and humidity profile data from the IGRA radiosonde data and the

ERA-Interim reanalysis datasets over the year 2009~2012.  $T_s$  was also extracted from the two data sets. Then, we analyzed the  $T_s$ - $T_m$  relationship at each reanalysis grid node and radiosonde station. Analyses indicated that (1) The  $T_s$ - $T_m$  relationship is stronger in the mid-high latitudes than in the low latitudes, (2) The  $T_s$ - $T_m$  correlation coefficients are higher over the lands than over the oceans in the low latitudes, (3) the variation properties of  $T_s$ - $T_m$  relationship are much more complicated rather than only dependence on the latitude, and (4) the  $T_s$ - $T_m$  relationship has strong annual, semiannual, and diurnal variations in many areas.

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Using the  $0.75^{\circ} \times 0.75^{\circ}$  ERA-Interim datasets over the year 2009~2012, we developed two global gridded  $T_s$ - $T_m$  models. The difference is that one model is static and another has time variations. The annual, semiannual, and diurnal variations in  $T_s$ - $T_m$  relationship are considered in the time-varying model. Then, by comparing with the radiosonde data in 2016, we evaluated the  $T_m$  results from the different  $T_s$ - $T_m$  models and the  $1^{\circ} \times 1^{\circ}$  GPT2w model. Results demonstrate that our time-varying global gridded  $T_s$ - $T_m$  model has a significant global precision advantage over the other global applied models. Average RMSE of  $T_m$  reduces by approximately 1 K. The proportion of the sites with small biases and RMSE increases significantly. At over 90 % of the radiosonde sites, the time-varying global gridded model has RMSE smaller than 4 K, while the RMSE more than 5 K nearly disappear. On the other hand, in the Bevis model or the latitude-related model, there are more than 17 % of the radiosonde sites having RMSE larger than 5 K. Multiple statistical tests at the 5 % significance level identified the significant superiority of the time-varying model at more than 60 % of the radiosonde sites. Analyses at the specific stations also demonstrate that the time-varying model can eliminate large errors in the estimated  $T_m$  series.

More precise  $T_s$ - $T_m$  models also have positive impacts on the GPS-PWV retrievals. Regarding the GPS-PWV using ERA-Interim  $T_m$  estimates as the references, the relative errors of GPS-PWV using the time-varying global gridded  $T_s$ - $T_m$  models are within 1.0 % at more than 74 % of our selected IGS sites. This result is clearly better than the other models. The differences between the GPS-PWV and the radiosonde PWV are approximately 1~5 mm. Some differences decrease 1~2 mm in the wetter conditions by using more precise  $T_m$  models. However, the error reductions of GPS-PWV due to the  $T_m$  models are very limited overall. This means that the other error sources, as we described in section 4.3, occupied the errors of GPS-PWV.

According to our experiments, we are confident that the time-varying global gridded  $T_s$ - $T_m$  models presented here will help us to retrieve GPS PWV more precisely and to study the precise PWV variations in high temporal resolution as well as

the  $T_s$  observations. Matlab array file consisting of the global gridded coefficients in our model, as well as codes to interpolate coefficients at any given location, are provided as the supplement of this study. It could be useful for researchers and applicants in relevant fields.

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#### Data sets

Radiosonde data: ftp://ftp.ncdc.noaa.gov/pub/data/igra

ERA-Interim Project: <a href="https://doi.org/10.5065/D6CR5RD9">https://doi.org/10.5065/D6CR5RD9</a>

GPS-ZTD Product: ftp://cddis.gsfc.nasa.gov/pub/gps/products/troposphere/zpd

Our model Supplement: https://www.atmos-meas-tech-discuss.net/amt-2018-67/amt-2018-67-supplement.zip

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# Competing interests

The authors declare that they have no conflict of interest.

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