



# Caution with Spectroscopic NO<sub>2</sub> Reference Cells (Cuvettes)

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**Abstract:** Spectroscopic measurements of atmospheric trace gases, e.g. by Differential Optical Absorption Spectroscopy (DOAS) are frequently supported by recording the trace gas column density (CD) in absorption cells (cuvettes), which are temporarily inserted into the light-path.

- 15 The idea is to verify the proper working of the instruments, to check the spectral registration (wavelength calibration and spectral resolution), and to perform some kind of calibration (absolute determination of trace gas CDs). In principle DOAS applications do not require absorption cell calibration, however in practice measurements with absorption cells in the spectrometer's light path are frequently performed. In addition, trace gas absorption cells are used as a central component in gas correlation spectroscopy instruments.
- Here we show at the example of  $NO_2$  absorption cells that the effective CD seen by the instrument can deviate greatly from expected values (by orders of magnitude). Analytical calculations and kinetic model studies show the dominating influence of photolysis and dimerisation of  $NO_2$ . In particular, this means that the partial pressure of  $NO_2$  in the cell matters.
- 25 However, problems can be particular severe at high  $NO_2$  pressures (around  $10^5$  Pa) as well as low  $NO_2$  partial pressures (of the order of a few 100 Pa). Also, it can be of importance whether the cell contains pure  $NO_2$  or is topped up with air or oxygen ( $O_2$ ). Some suggestions to improve the situation are discussed.

# 30 1. INTRODUCTION

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There are a number of reasons to use absorption cells in conjunction with instruments measuring trace gas column densities (CDs) by absorption spectroscopy, e.g. by Differential Optical Absorption Spectroscopy (DOAS). These include the verification of the overall working of the instrument, stray-light determination, or even a check of the instrument's absolute calibration (reliable barrent in DOAS and there are not needed on a Platt and State 2008).

35 (which, however is inherent in DOAS and thus not needed, see e.g. Platt and Stutz, 2008). In addition, gas correlation spectroscopy measurements (e.g. Ward and Zwick, 1975; Sandsten et al., 1996, 2004; Kebabian et al., 2000) require absorption cells containing the gas to be measured at CDs leading to optical densities around unity.

In general, there are a number of issues with using gas cells for these purposes including:

- Stability of the gas in the cell due to photolysis and/or chemical reactions
  - Temperature dependence of chemical equilibria within the cell
  - Temperature dependence of the optical density
  - Optical problems with the cell
- In the following we discuss the above problems for the case of NO<sub>2</sub> absorption cells, however
- 45 some of the discussed issues will also apply to cells with other gases.





#### 2. OPTICS OF CELLS

In principle the introduction of an absorption cell into the optical path of a remote sensing instrument (e.g. a spectrometer) is straightforward. The cell is mounted in front of the entrance optics and in first approximation the absorption due to the trace gas in the cell (i.e. due to the trace gas CD) is added to the trace gas absorption seen without the cell. While this view is correct in some approximation, in detail there are a number of problems that need investigation.

#### 2.1. Path length in an isolated cell

In a realistic cell partial reflection (reflectance R) occurs at the cell windows. For simplicity we assume an index of refraction of n=1.5 for the cell window material and accordingly

$$R = \left(\frac{n-1}{n+1}\right)^2 \approx 0.04 \tag{1}$$

i.e. about 4% reflection per surface for near-normal incidence (see Fig. 1). While the reduction of the incoming intensity by  $(1-R)^4$  or about 15% is probably of minor importance a fraction of about  $(1-R)^2 \cdot (R+R)^2 \approx 0.59\%$  of the incoming radiation and 0.69% of the transmitted radiation

- 15 passes the cell three times. Due to this multiple reflected light the total absorption of the cell (and thus the trace gas slant column density, SCD,  $S_C$ ) will be enhanced by about 2%. We note the case of nearly normal incidence is quite realistic in many cases, for instance MAX-DOAS instruments (e.g. Hönninger and Platt, 2002, Platt and Stutz, 2008) have total aperture angles of the order of 1°, i.e. incidence angles of -0.5° to +0.5°. A typical use of a cell would be to just
- 20 mount it in front of the telescope. In this arrangement the enhancement of the light path inside the cell (and thus the trace gas column density  $S_C$ ) due to the finite aperture angle of the radiation passing the cell will vary according to  $S_C = S_0/cos(\vartheta)$  with  $S_0$  denoting the trace gas CD for rays parallel to the cell axis. An angle of  $\vartheta = 0.5^\circ$  would lead to an enhancement in  $S_C/S_0$  of  $\approx 1.000038$  or 0.004%.



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Fig. 1: Sketch of the optics of a gas absorption cell, parallel rays are assumed, the (small) tilt of the incoming ray with respect to the cell axis is introduced to distinguish the rays. The described effect will also be there at strictly normal incidence. We assume an index of refraction of n=1.5 for the cell window material and accordingly 4% reflection per surface (for near-normal incidence). Note that a fraction of about 0.69% of the transmitted

radiation passes the cell three times thus adding  $\approx 2\%$  to the total absorption.

Thus a slight (few degrees) tilt of the cell will not lead to noticeable light path extension in the cell, but already a 1° tilt, leading to 0.015% light path extension would be sufficient to reflect the multiple reflected light outside the field of view of the telescope. Thus, the additional 2% cell absorption would disappear. On the other hand, larger tilts of the cell, e.g. 10° would increase the cell absorption again by 1.5% and should therefore be avoided. This could be accomplished by a





rigid mount which fixes the (removable) cell at a defined angle with respect to the cell optical axis (normal of the windows), e.g. at  $2^{\circ}$ .

As will be discussed below, the acceptance angle off the cell to ambient (sun)light can play a significant role. Therefore, this small aperture angle allows for shielding the cell from sunlight, since solar radiation does only need to enter from a small solid angle (of the order of 10<sup>-3</sup> sr). This could be accomplished by mounting the cell inside a relatively long tube made of nontransparent material.

# 10 **2.2. Path length in a cell as part of an optical system**

In section 2.1 we discussed the behaviour of an isolated cell, however the idea is to incorporate an absorption cell into an optical system, i.e. to just hold it in front of a MAX-DOAS instrument. In this case there can be interaction between the cell and the entrance optics of the instrument (for instance due to reflection of light at the surface of the telescope lens). As described by

- 15 Lübcke et al., (2013) this can further enhance the trace gas CD in the cell as seen by the instrument looking through it. In the case of using gas cells gas in imaging instruments, for instance imaging spectrometers (e.g. Lohberger et al., 2004) or gas correlation instruments (e.g. Ward and Zwick, 1975) a larger aperture angle is required, which causes two potential problems: First, the aperture angle of the
- cell has to be much larger than in the case of a one pixel (narrow field of view) instrument, for instance typically  $30^{\circ}$  total angle, thus the acceptance angle for solar radiation becomes considerably larger (e.g. 0.22 sr instead of  $10^{-3}$  sr) and consequently the photolysis frequencies for the gases inside the cell (see below). Second, the trace gas CD of the cell becomes dependent on the observation angle  $\vartheta$  (angle between the optical axis and the actual viewing direction
- 25 within the field of view), as described above. For a total aperture angle of  $30^{\circ}$  this would amount to an enhancement of the  $S_{C}(15^{\circ})$  over  $S_{0}=S_{C}(0^{\circ})$  of about 3.5%.

# 3. CHEMISTRY IN NO<sub>2</sub>-ABSORPTION CELLS

Nitrogen dioxide (NO<sub>2</sub>) is a quite reactive gas, therefore a series of chemical processes in an absorption cell can occur. Since they can alter the NO<sub>2</sub> concentration - and thus the NO<sub>2</sub> CD in the cell - considerably they have to be watched. In the following subsections we discuss the relevant chemical processes, starting with important reactions and then proceeding to further reactions, which are only relevant under certain conditions or if high precision is required.

# 3.1. The (initial) NO<sub>2</sub>-only Chemistry – simple case

- 35 In a cell (initially) filled only with NO<sub>2</sub> we can expect the following reactions (bi-molecular rate constants are given in cm<sup>3</sup>molec<sup>-1</sup>s<sup>-1</sup>, termolecular rate constants are given in cm<sup>6</sup>molec<sup>-2</sup>s<sup>-1</sup> for 25°C and 1000 hPa, details on temperature and pressure dependence as well as literature references can be found in Table 1):
- 40 Usually cells are exposed to sun light or radiation needed for the measurement, thus NO<sub>2</sub> in the cell can be photolyzed:

$$NO_2 + hv \rightarrow NO + O(^{3}P) \quad J_1 \approx 8 \cdot 10^{-3} \text{ s}^{-1}$$
 (R1)

In the following ground state oxygen atoms  $O({}^{3}P)$  will be denoted by O. The threshold wavelength for reaction 1 is about 400 nm (e.g. Johnston and Graham, 1974, Burkholder et al., 2015), however, due to vibrational excitation of the ground state melawle there is noticeable

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photolysis up to about 425 nm. If the cell is only illuminated with radiation of wavelength longer than 425 nm, NO<sub>2</sub> will not photolyze and  $J_1$  will be essentially zero.

Although it is only a small effect it is worth noting that the photolysis frequency inside a cell is not different from the value in the air surrounding the cell as, despite reflectance of the cell walls as described by e.g. Bahe et al., 1979

The oxygen atoms produced in Reaction 1 can (1) recombine

$$O + O + M \rightarrow O_2 + M$$
 (R2)

However, this is a slow process.

10 Alternatively, (2), O-atoms may react with the wall where they predominantly recombine (see e.g. Cartry et al., 2000):

$$O + O \rightarrow Wall \rightarrow O_2$$
 (R3)

Also, (3) O-atoms can react with NO<sub>2</sub> to form NO:

$$O + NO_2 \rightarrow NO + O_2 \quad k_4(298K) \approx 2.52 \cdot 10^{-12} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$
 (R4)

15 Further, (4), oxygen atoms also may react with NO to form NO<sub>2</sub>:

$$O + NO + M \rightarrow NO_2 + M = k_5(298K) \approx 2.2 \cdot 10^{-12} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$
 (R5)

The final possibility (5) formation of  $NO_3$  - as well as further reactions - will be treated in section 3.4, below.

20 In addition there is the termolecular reaction of the O<sub>2</sub> formed in reaction 4 (or added to the cell filling) oxidises NO to NO<sub>2</sub>:

$$2 \operatorname{NO} + \operatorname{O}_2 \rightarrow 2 \operatorname{NO}_2 \qquad k_6 \approx 1.95 \cdot 10^{-38}$$
 (R6)

In an attempt to obtain a first order quantitative understanding of the processes in the cell we just consider a pure NO<sub>2</sub> initial filling and Reactions 1 (NO<sub>2</sub> photolysis), 4 (O+NO<sub>2</sub>) and 6 (2NO+O<sub>2</sub>):

From the combination of reactions 1 and 4 we derive the rates of NO and  $O_2$  formation under illumination:

$$P(NO) = \frac{d}{dt} [NO] \approx 2 \cdot P(O_2) \approx 2 \cdot [NO_2] \cdot J_1$$
(2)

Which ultimately (i.e. in the stationary state) must equal the rate of NO destruction, D(NO) and NO<sub>2</sub> formation,  $P(NO_2)$  due to reaction 6:

$$D(NO) = -\frac{d}{dt} [NO] \approx P(NO_2) \approx 2 \cdot [NO]_s^2 \cdot [O_2] \cdot k_6$$
(3)

Since  $P(O_2) \approx 0.5 \cdot P(NO)$  and the concentration of both species are zero initially we have  $[NO] \approx 2 \cdot [O_2]$ . Substituting this relationship

$$D(NO) = -\frac{d}{dt} [NO] \approx [NO]^3 \cdot k_6$$
(4)

35 and equating P(NO) with D(NO) we obtain:

$$2[NO_2] \cdot J_1 \approx [NO]_S^3 \cdot k_6$$
<sup>(5)</sup>

Further substituting  $[NO_2] \approx [NO_2]_0$ - $[NO]_S$ :





$$\left[\mathrm{NO}_{2}\right]_{0} - \left[\mathrm{NO}\right]_{\mathrm{s}} \approx \left[\mathrm{NO}\right]_{\mathrm{s}}^{3} \cdot \frac{\mathbf{k}_{6}}{2J_{1}}$$
(6)

or

$$\left[\mathrm{NO}_{2}\right]_{0} \approx \left[\mathrm{NO}\right]_{\mathrm{S}}^{3} \cdot \frac{\mathrm{k}_{6}}{\mathrm{2}\mathrm{J}_{1}} + \left[\mathrm{NO}\right]_{\mathrm{S}} \tag{7}$$

This cubic equation can be solved for the stationary state NO concentration  $[NO]_S$  as function of the initial  $[NO_2]_0$  as given in Appendix 1.

Examples:

As an example and to obtain a first idea of what might be happening in the cell we assume about 1 atmosphere (1000 hPa) of pure NO<sub>2</sub> (initially) i.e. the initial NO<sub>2</sub> concentrations in the cell will be [NO<sub>2</sub>]<sub>0</sub> ≈ 2.4·10<sup>19</sup> cm<sup>-3</sup> and the very simple chemical system just comprising reactions 1, 4, and 6. As we shall show below the simplified reaction system - with the exception of the NO<sub>2</sub> dimer (N<sub>2</sub>O<sub>4</sub>) formation (see section 3.2) - is quite adequate. Also, such a cell would have a peak optical density (at around 440 nm) of about 14 at 1 cm length but much lower at other wavelengths.

15 In the dark  $(J_1 = 0)$  nothing will happen while in sun light  $(J_1 = 8 \cdot 10^{-3})$ : NO + O – formation will take place followed by reaction (4) of NO<sub>2</sub> with O. Thus the (initial) rate of NO formation P(NO) will be:

$$P(NO) \approx 2[NO_2]_0 \cdot J_1 \approx 3.8 \cdot 10^{17} \text{ cm}^{-3} \text{s}^{-1}$$
 (8)

This will lead to an initial decay time  $\tau_{NO2} = [NO_2]_0/P(NO)=1/(2J_1) \approx 63$  s. The stationary state

20 NO concentration can be calculated according to Equation 7 and the solution given in Appendix 1 to be  $[NO]_S \approx 2.57 \cdot 10^{18}$  molec/cm<sup>3</sup> or about 10.7 % of the initial NO<sub>2</sub> level. In other words, the NO<sub>2</sub> concentration will be reduced to 89.3 % of its initial value  $[NO_2]_0$ . The corresponding NO rate of destruction will be:

$$D(NO) \approx [NO]^3 \cdot k_6 \approx 3.32 \cdot 10^{17} \text{ molec.} \cdot \text{cm}^{-3} \text{s}^{-1}$$

25 matching  $P(NO) \approx 2[NO_2]_S \cdot J_1$  from NO<sub>2</sub> photolysis.

2) We like to give a further example using about 1 hPa of pure NO<sub>2</sub> (initially) corresponding to  $[NO_2]_0 \approx 2.4 \cdot 10^{16} \text{ cm}^{-3}$ , and the same simple chemical system just comprising reactions 1, 4, and 6 as above. Such a cell would have an initial differential optical density in the vicinity of 450 nm of about  $2.4 \cdot 10^{-3}$  and would thus appear ideal to test the sensitivity of a NO<sub>2</sub> spectrometer.

- of about 2.4 · 10<sup>-3</sup> and would thus appear ideal to test the sensitivity of a NO<sub>2</sub> spectrometer. In sunlight we have D(NO<sub>2</sub>) ≈ 1.92·10<sup>14</sup> cm<sup>-3</sup>s<sup>-1</sup>. In this case (using the same calculation as given in appendix 1) the resulting stationary state NO level becomes [NO]<sub>S</sub> ≈ 2.4·10<sup>16</sup> or about 100% of the initial NO<sub>2</sub>. In other words after illumination the remaining NO<sub>2</sub> concentration and thus the NO<sub>2</sub> CD of the cell will only be a very small fraction of the expected value ([NO<sub>2</sub>]<sub>S</sub>·J<sub>1</sub> = D(NO) or [NO<sub>2</sub>]<sub>S</sub> = D(NO)/ J<sub>1</sub> ≈ 1.7·10<sup>13</sup> cm<sup>-3</sup> i.e. <0.1% of the initial [NO<sub>2</sub>]). In
- 35 ( $[NO_2]_{s}$ ·J<sub>1</sub> = D(NO) or  $[NO_2]_{s}$  = D(NO)/ J<sub>1</sub> ≈ 1./·10<sup>-4</sup> cm<sup>-4</sup> i.e. <0.1% of the initial  $[NO_2]_{s}$ . In other words, after a short (of the order of one minute) exposure to sunlight the NO<sub>2</sub> in the cell will practically vanish.

On the other hand, the NO re-conversion, D(NO), to  $NO_2$  will be much slower than the initial photolysis:

$$D(NO) \approx 0.5 \cdot [NO]^3 \cdot k_6 \approx 1.35 \cdot 10^{11} \text{ molec.} \cdot \text{cm}^{-3} \text{s}^{-1}$$

## **Recovery from illumination:**

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A further interesting question concerns the time for the chemical system to recover from a period of photolysis. Equation 4, gives the rate of NO destruction as function of [NO]. In the case of





example 1), above NO would decay with an initial rate of  $D(NO)/[NO]\approx 0.11/s$  (ca. 11% per second suggesting a 9 seconds time constant for recovery). However, D(NO) varies with the third power of [NO]. When e.g. 90% the NO is consumed (i.e. still 1.4% of [NO] is left) the time constant would increase by a factor of 1000 to around three hours.

5 In the case of example 2) the initial re-conversion rate would only be  $5.6 \cdot 10^{-6}$ /s (or  $\approx 49$  % per day), which would seem to imply a recovery time of somewhat more than 2 days. But again the dependence on the cube of the NO concentration means that the recovery time becomes much longer later on. For some model results see Figure 7.

#### 3.2. The NO<sub>2</sub> $\leftrightarrow$ N<sub>2</sub>O<sub>4</sub> Equilibrium.

An additional problem in  $NO_2$  cells - in particular if high  $NO_2$  concentrations approaching 1000 hPa are used - is the formation of the dimer  $N_2O_4$  (see also Roscoe et al. 1993):

$$2 \text{ NO}_2 + M \rightarrow \text{N}_2\text{O}_4 + M \qquad k(298\text{K})\cdot[\text{M}] \approx 3.3 \cdot 10^{-14} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$
 (R7)

There is a thermal decay of the dimer:

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$$N_2O_4 + M \rightarrow 2 NO_2 + M \quad k_8(298K) \cdot [M] \approx 1.47 \cdot 10^5 s^{-1}$$
 (R8)

Leading to an equilibrium with the equilibrium constant (298K, from Atkinson et al. 2014):

$$K_{Eq} = \frac{k_{\rightarrow}}{k_{\leftarrow}} = \frac{[N_2 O_4]}{[NO_2]^2} \approx 2.29 \cdot 10^{-19} \text{ cm}^3 \text{ molec}^{-1}$$
(9)

Note that the time to attain the equilibrium is shorter than  $1/k_8 \approx 7 \ \mu s$  (at 298 K and 1000 hPa) thus one can assume that there is always equilibrium between NO<sub>2</sub> and N<sub>2</sub>O<sub>4</sub>. From this follows for the [NO<sub>2</sub>]/[N<sub>2</sub>O<sub>4</sub>] ratio:

$$\frac{1}{K_{Eq}[NO_2]} = \frac{[NO_2]}{[N_2O_4]} \text{ or } [N_2O_4] = K_{Eq} \cdot [NO_2]^2$$
(10)

What is usually most interesting is the fraction of NO<sub>2</sub> of the total amount of NO<sub>2</sub>+N<sub>2</sub>O<sub>4</sub> (i.e. pressure during filling) in the cell. The latter is given by  $[NO]_Z = [NO_2]+[N_2O_4]$  and thus:

$$\frac{[NO_2]}{[NO_2]_Z} = \frac{[NO_2]}{[N_2O_4] + [NO_2]} = \frac{[NO_2]}{K_{Eq} \cdot [NO_2]^2 + [NO_2]} = \frac{1}{K_{Eq} \cdot [NO_2] + 1}$$
(11)

25 Which can be transformed to:

$$\mathbf{K}_{\mathrm{Eq}} \cdot \left[\mathrm{NO}_{2}\right] + 1 = \frac{\left[\mathrm{NO}_{2}\right]_{Z}}{\left[\mathrm{NO}_{2}\right]} \Longrightarrow \left[\mathrm{NO}_{2}\right]_{Z} = \mathbf{K}_{\mathrm{Eq}} \cdot \left[\mathrm{NO}_{2}\right]^{2} + \left[\mathrm{NO}_{2}\right]$$
(12)

And solved for [NO<sub>2</sub>]:

$$\left[NO_{2}\right]^{2} + \frac{\left[NO_{2}\right]}{K_{Eq}} - \frac{\left[NO_{2}\right]_{Z}}{K_{Eq}} = 0$$
(13)

With the only positive solution:

$$[NO_{2}]_{I} = -\frac{1}{2K_{Eq}} + \sqrt{\frac{1}{4K_{Eq}^{2}} + \frac{[NO_{2}]_{Z}}{K_{Eq}}}$$
(14)

or





$$\left[NO_{2}\right]_{I} = \frac{1}{K_{Eq}} \left( -\frac{1}{2} + \sqrt{\frac{1}{4} + \left[NO_{2}\right]_{Z} \cdot K_{Eq}} \right)$$
(15)

The relationship between NO<sub>2</sub> and  $[NO_2]/[NO_Z]$  in the cell as a function of total  $[NO]_Z = [NO_2] + [N_2O_4]$  is shown in Figure 2.

- 5 Examples:  $[M]=2.4 \cdot 10^{19}$  (1000 hPa or ca. 1 atmosphere of total pressure, at 298 K) resulting in  $[NO_2]_1 \approx 8.29 \cdot 10^{18}$  molec/cm<sup>3</sup> and  $[NO_2]_1/[NO]_Z \approx 0.344$ . Thus, filling a cell from an NO<sub>2</sub> reservoir (e.g. an NO<sub>2</sub> tank) to one atmosphere of total pressure will lead to only 32% of this pressure being present as NO<sub>2</sub> (see also Figure 2).
- At 100, 10, 1 hPa (ca. 0.1, 0.01, and 0.001 atmospheres) of NO<sub>2</sub>+N<sub>2</sub>O<sub>4</sub> the corresponding figures
  for [NO<sub>2</sub>]<sub>1</sub>/[NO]<sub>Z</sub> would be 0.717, 0.95, and 0.99.5, respectively. These figures are independent of an additional topping with air or oxygen to a full atmosphere of total pressure, as will be described below. In other words unless the NO<sub>2</sub> partial pressure is around 100 Pa the actual NO<sub>2</sub> partial pressure (and thus concentration of NO<sub>2</sub>) will be below expected levels by two-digit percentages.

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A further problem associated with the  $NO_2 - N_2O_4$  equilibrium is the marked temperature dependence of the equilibrium constant. In the usual Arrhenius expression it is given as:

$$K_{Eq}(T) = A \cdot e^{\frac{B}{T}}$$
(16)

With  $A = 1.07 \cdot 10^{-28} \text{ cm}^3/\text{molec}$  and B = 6400 K (see Table 1). The (relative) temperature dependence of  $K_{Eq}$  is given by:

$$\frac{1}{K_{Eq}(T)}\frac{d}{dT}\left(K_{Eq}(T)\right) = \frac{1}{K_{Eq}(T)}A \cdot e^{\frac{B}{T}}\frac{d}{dT}\left(\frac{B}{T}\right) = \frac{1}{K_{Eq}(T)} \cdot -\frac{AB}{T^2} \cdot e^{\frac{B}{T}} = -\frac{B}{T^2}$$
(17)

With the above values for A and B we obtain for the relative change in the equilibrium constant:

$$\frac{1}{K_{Eq}(T)}\frac{d}{dT}(K_{Eq}(T)) = -\frac{B}{T^2} \approx -0.072\frac{1}{K}$$
(18)

In other words the equilibrium constant is reduced by more than 7%/K of heating. Fortunately the effect on NO<sub>2</sub> is somewhat smaller, ranging from near zero change at very small NO<sub>2</sub> levels to about 3% increase per degree of heating at 1000 hPa (see section 4).





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Fig. 2:  $NO_2$ -concentration (black line in units of  $10^{19}$  molec/cm<sup>2</sup>, left axis) and fraction of  $NO_2$ (red line, right axis) of the total  $[NO_2]_Z = [NO_2] + [N_2O_4]$  as a function of  $[NO_2]_Z$  (given in pressure units for 25°C). At atmospheric pressure (1000 hPa) in the cell only about 34% of the total  $NO_{2Z}$  (or  $\approx 344$  hPa partial pressure) exist as  $NO_2$ .

#### 3.3. NO<sub>2</sub>+O<sub>2</sub> chemistry

10 The addition of O<sub>2</sub> (or air) to the NO<sub>2</sub> filling has two effects that can greatly help stabilising the NO<sub>2</sub> concentration in a cell under certain conditions, as explained below:
1) In the presence of molecular oxygen following the photolysis of NO<sub>2</sub> ozone is formed in the cell:

 $O + O_2 + M \rightarrow O_3 + M = k_9(298K) \approx 1.46 \cdot 10^{-14} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$  (R9)

15 Which in turn can react with NO to form NO<sub>2</sub>:

$$O_3 + NO \rightarrow NO_2 + O_2 \quad k_{10}(298K) \approx 1.9 \cdot 10^{-14} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$
 (R10)

The reaction scheme encompassing the pertinent reaction pathways discussed above is sketched in Figure 3.







*Fig. 3: Simplified scheme of the chemical reactions in an illuminated NO*<sub>2</sub>*-cell. The reactions in the 'NO*<sub>2</sub> *only' system are indicated by fat arrows. Formation of OH is not shown.* 

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#### Here we can distinguish two regimes:

a) Comparable concentrations of O<sub>2</sub> and NO<sub>2</sub> i.e. [O<sub>2</sub>]/[NO<sub>2</sub>] around unity. In this case the termolecular oxidation of NO by O<sub>2</sub> dominates, this is similar to the situation discussed in section 3.1, however we can take the O<sub>2</sub> concentration [O<sub>2</sub>] to be essentially constant. This reduces the third order kinetics of Equation 7 to (pseudo) second order kinetics and we obtain:

$$[NO] = \sqrt{\frac{P_{NO}}{2[O_2]k_{NO}}} \underset{P_{NO} \text{ substituded}}{\approx} \sqrt{\frac{[NO_2] \cdot J}{[O_2]k_{NO}}}$$

$$\frac{[NO]}{[NO_2]} \approx \sqrt{\frac{J}{[O_2][NO_2]k_{NO}}}$$
(19)

For example we may assume 0.5 atmospheres (500 hPa), each of pure NO<sub>2</sub> and O<sub>2</sub> (initially) i.e. the initial concentrations of either species in the cell will be [O<sub>2</sub>]<sub>0</sub> = [NO<sub>2</sub>]<sub>0</sub> ≈ 1.2·10<sup>19</sup> cm<sup>-3</sup>. In sunlight we have NO<sub>2</sub> photolysis (reaction 1) followed by O+NO<sub>2</sub> (reaction 4) plus oxidation of NO by O<sub>2</sub>.

 $D(NO) \approx 2[NO]^2 \cdot [O_2]k_{NO} = P(NO)$ 

From this stationary state assumption we can calculate [NO]<sub>s</sub>:

$$[\text{NO}]_{\text{s}} \approx \sqrt{\frac{\text{P}_{\text{NO}}}{2[\text{O}_2] \text{k}_{\text{NO}}}} \approx 0.054 \cdot [\text{NO}_2]$$

20 Thus the NO<sub>2</sub> concentration would be reduced by only 5.4% from its initial value once the cell is subjected to sunlight.





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b) High  $[O_2]/[NO_2]$  ratio (for instance larger than  $10^4$ ), so that the reaction of O-atoms formed in NO<sub>2</sub> photolysis are much more likely to react with O<sub>2</sub> than with NO<sub>2</sub>. In this case for each molecule of NO<sub>2</sub> photolyzed nearly one molecule of O<sub>3</sub> is formed, which will react with the NO molecule produced in the NO<sub>2</sub> photolysis. The O<sub>3</sub> concentration will rise until its reaction with NO balances the rate of NO<sub>2</sub> photolysis:

$$[NO][O_3]k_{10} = [NO_2] \cdot J_1$$
(20)

Since [NO]  $\approx$  [O<sub>3</sub>] we obtain:

$$[NO]^{2} k_{10} \approx [NO_{2}] \cdot J \Longrightarrow [NO] \approx \sqrt{\frac{[NO_{2}] \cdot J}{k_{10}}}$$
(21)

For instance at  $[NO_2] = 2.4 \cdot 10^{15} \text{ cm}^{-3}$  and about one atmosphere (1000 hPa) of O<sub>2</sub> the stationary state NO level would be  $[NO] \approx 4.4 \cdot 10^{13} \text{ cm}^{-3}$  or about 1.8% of the initial NO<sub>2</sub> concentration. Note that a small fraction (about  $10^{-4}$  in this example) of the O-atoms produced in the NO<sub>2</sub>photolysis would still react with NO<sub>2</sub> and form NO without a corresponding O<sub>3</sub> production (rate about  $2 \cdot 10^9 \text{ cm}^{-3} \text{s}^{-1}$ ), thus the NO-fraction in the cell would slowly grow until reaction 6 balances this process. At the above NO level the rate of NO<sub>2</sub> formation would be around  $10^9 \text{ cm}^{-3} \text{s}^{-1}$ , thus

15 the NO level would slightly grow (by about 50%) during several days of continuous illumination of the cell.

#### 3.4. The (initial) NO<sub>2</sub>-only Chemistry – some complications

In addition to the three reactions described above, O-atoms can recombine with  $NO_2$  to form nitrate radicals,  $NO_3$ :

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$$O + NO_2 + M \rightarrow NO_3 + Mk_{11}(298K, 1 \text{ atm}) \approx 2.5 \cdot 10^{-11} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$
 (R11)

The thus formed NO<sub>3</sub> radicals can be photolyzed:

$$NO_3 + hv \rightarrow NO_2 + O \qquad J_{12a} \approx 0.19 \text{ s}^{-1}$$
 (R12a)

$$NO_3 + hv \rightarrow NO + O_2 \qquad J_{12b} \approx 0.016 \text{ s}^{-1}$$
 (R12b)

The threshold wavelength is much longer than in the case of  $NO_2$  (J<sub>1</sub>) and the photolysis is much faster. Alternatively, NO<sub>3</sub> may react with NO (from R1) to re-form NO<sub>2</sub>:

NO<sub>3</sub> + NO → 2 NO<sub>2</sub> 
$$k_{13}(298K) \approx 2.6 \cdot 10^{-11} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$
 (R13)

Or undergo self reaction:

NO<sub>3</sub> + NO<sub>3</sub> → 2 NO<sub>2</sub>+ O<sub>2</sub> 
$$k_{14}(298K) \approx 2.3 \cdot 10^{-16} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$
 (R14)

Finally, and typically most likely, NO3 will react with NO2 to form dinitrogen pentoxide, N2O5:

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$$NO_3 + NO_2 + M \rightarrow N_2O_5 + M \qquad k_{15}(298K) \approx 1.34 \cdot 10^{-12} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$
 (R15)

Dinitrogen pentoxide is thermally unstable and decays:

$$N_2O_5 + M \rightarrow NO_3 + NO_2 + M \quad k_{16}(298K) \approx 2.98 \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$
 (R16)

In the absence of water (dry system)  $N_2O_5$  will just be another reservoir potentially sequestering some of the NO<sub>2</sub>. On the other hand,  $N_2O_5$  is the anhydride of nitric acid and may react with water to form HNO<sub>3</sub>. While the  $N_2O_5$  plus water vapour reaction appears to be exceedingly slow it may react with a layer at the cell surface, details are given in section 3.5.

Analyzing the above system of reactions one notices that loss of O-atoms other than by reactions 4 or 11 are of minor importance. This is underlined by the results of the model calculations using the full chemical system (see Table 1) presented in section 4.





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Therefore, we can summarize that each photolysis reaction (R1) is followed by a conversion of NO<sub>2</sub> to NO (R4) or to NO<sub>3</sub> (R11). However, NO<sub>3</sub> is largely converted back to NO<sub>2</sub> by reactions 12a, 13, and (to a minor extent) 14, thus, in effect each photolysis act of NO<sub>2</sub> leads to the loss of approximately two NO<sub>2</sub> molecules. Essentially NO<sub>2</sub> would be converted to NO + O<sub>2</sub>. In bright sunshine with  $J_1 \approx 8 \cdot 10^{-3} \text{ s}^{-1}$  this would lead to a NO<sub>2</sub> – lifetime in the cell of  $\tau(NO_2) \approx 1/(2 \cdot J_1) \approx 63$  s or roughly one minute. Even if the cell is kept in the shade or is only exposed to indoor illumination where  $J_1$  could be estimated to be 10-times (shade) to 100-times (indoor) smaller than in bright sunshine the conversion could be expected to proceed within around 10 (shade) to 100 (indoor) minutes.

## 10 **3.5.** $NO_2 + O_2 + (trace) H_2O$ chemistry

It may be possible that traces of water enter the cell when it is filled, then a series of additional reactions may play a role:

$$O_3 + h\nu \rightarrow O(^1D) + O_2 \quad J \approx 3 \cdot 10^{-5} \text{ s}^{-1}$$
 (R17)

Followed by quenching of  $O(^{1}D)$  to  $O(^{3}P)$  or the formation of hydroxyl (OH) radicals:

 $O(^{1}D) + H_{2}O \rightarrow 2 OH \qquad k_{18}(298K) \approx 2.0 \cdot 10^{-10} \text{ cm}^{3} \text{ molec}^{-1} \text{ s}^{-1}$  (R18)

In an NO<sub>2</sub> cell OH radicals are most likely to react with NO<sub>2</sub> to form nitric acid:

$$OH + NO_2 + M \rightarrow HNO_3 + M = k_{19}(298K) \approx 1.05 \cdot 10^{-11} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$
 (R19)

Nitric acid is photolyzed very slowly, also its reaction with OH (to form  $NO_3$ ) is slow, thus it will constitute a final sink of  $NO_2$  (and water) in the cell. Alternatively OH may react with NO to form nitrous acid:

OH + NO + M → HNO<sub>2</sub> + M 
$$k_{20}(298K) \approx ?? \cdot 10^{-11} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$
 (R20)

Which - in turn - is lost by photolysis:

HNO<sub>2</sub> + hv → OH + NO 
$$j_{21}$$
 (298K) ≈ 1.34 · 10<sup>-3</sup> s<sup>-1</sup> (R21)

In addition  $N_2O_5$ , formed in reaction 15, can react with (liquid) water adsorbed at the wall of the cell, also forming HNO<sub>3</sub>:

$$N_2O_5 + (H_2O)_{liq} \rightarrow 2 (HNO_3)_{liq}$$
 (R22)

Finally N<sub>2</sub>O<sub>4</sub> is also known to heterogeneously react with water:

$$N_2O_4 + (H_2O)_{liq} \rightarrow HNO_2 + (HNO_3)_{liq}$$
 (R23)

HNO<sub>2</sub> will relatively quickly photolyze to form OH + NO (with OH in most cases reacting according to R19), and HNO<sub>3</sub> from the above two reactions will remain. One can actually assume that all H<sub>2</sub>O is ultimately converted to HNO<sub>3</sub>, sequestering equivalent amounts of NO<sub>2</sub> and water.

For example a cell having been filled with a small amount of NO<sub>2</sub> (e.g. 10 hPa or 2.4 · 10<sup>17</sup> molec cm<sup>-3</sup>) is topped with laboratory air at 25°C and 70% relative humidity. Thus the approximate amount of water admitted is 70% of the saturation vapour pressure of H<sub>2</sub>O at that temperature (70% of 31.6 hPa = 22.1 hPa or 5.3 · 10<sup>17</sup> molec cm<sup>-3</sup>). Some of this water will form a film at the inside of the cell and allow heterogeneous reactions 22 and 23 converting NO<sub>2</sub> into HNO<sub>3</sub>, although it is hard to judge how fast this process will provide (relatively slow) gas-phase conversion of NO<sub>2</sub> to HNO<sub>3</sub>. Since the amount of H<sub>2</sub>O in this example exceeds the amount of NO<sub>2</sub> it is likely that ultimately all NO<sub>2</sub> is converted to HNO<sub>3</sub>.





Table 1: Summary of reaction rate constants (<sup>1</sup>: data from Burkholder et al., 2015 (JPL Publication 15-10; <sup>2</sup>: data from Atkinson et al., 2004; <sup>3</sup>: data from Tsang and Hampson, 1986; <sup>4</sup>: data from Trebs et al., 2009, <sup>5</sup>: data from Bahe and Schurath, 1978, <sup>6</sup>: data from Alicke et al., 2002). The reactions marked with \* are included in the kinetic model, see Section 4.

No.	Reaction	k(T), j, or k <sub>0</sub> (T)	k∞	k(298 K, 1
		cm <sup>3</sup> molec <sup>-1</sup> s <sup>-1</sup> if not given otherwise		$cm^3molec^{-1}s^{-1}$
				if not given otherwise
1* <sup>,4</sup>	$NO_2 + hv \rightarrow NO + O$	$8 \cdot 10^{-3} \text{ s}^{-1}$		$8 \cdot 10^{-3} \text{ s}^{-1}$
2* <sup>,3</sup>	$O + O + M \rightarrow O_2 + M$	5.21.10 <sup>-35</sup> e <sup>(900/T)</sup> cm <sup>6</sup> molec <sup>-2</sup> s <sup>-1</sup>		2.51·10 <sup>-14</sup>
3	$O + O \rightarrow Wall \rightarrow O_2$	neglected		
4* <sup>,1</sup>	$O + NO_2 \rightarrow NO + O_2$	$5.1 \cdot 10^{-12} \cdot e^{(-210/T)}$		$2.52 \cdot 10^{-12}$
5* <sup>,1</sup>	$O + NO + M \rightarrow NO_2 + M$	$9.10^{-32}(T/300)^{-1.5}$ cm <sup>6</sup> molec <sup>-2</sup> s <sup>-1</sup>	3.0.10 <sup>-11</sup>	$2.2 \cdot 10^{-12}$
6* <sup>,2</sup>	$2 \text{ NO} + \text{O}_2 \rightarrow 2 \text{ NO}_2$	$3.3 \cdot 10^{39} \exp(530/T)$ cm <sup>6</sup> molec <sup>-2</sup> s <sup>-1</sup>		$1.95 \cdot 10^{-38}$ cm <sup>6</sup> /(molec <sup>2</sup> s)
7* <sup>,2</sup>	$2 \operatorname{NO}_2 + M \rightarrow \operatorname{N}_2\operatorname{O}_4 + M$	1.4·10 <sup>-33</sup> (T/300) <sup>-3.8</sup> cm <sup>6</sup> molec <sup>-2</sup> s <sup>-1</sup>	1.0·10 <sup>-12</sup>	3.3.10 <sup>-14</sup>
8* <sup>,2</sup>	$N_2O_4 + M \rightarrow 2 NO_2 + M$	$1.3 \cdot 10^{-5} (T/300)^{-3.8}$ e <sup>-(6400/T)</sup>	$\frac{1.15 \cdot 10^{16} e^{(-6460/T)}}{s^{-1}}$	$1.47 \cdot 10^5 \text{ s}^{-1}$
9* <sup>,1</sup>	$O + O_2 + M \rightarrow O_3 + M$	6.0·10 <sup>-34</sup> (T/300) <sup>-2.4</sup> cm <sup>6</sup> molec <sup>-2</sup> s <sup>-1</sup>	$\begin{array}{ll} k_0[M] <\!\!< & k_\infty & at \\ 1000 \ hPa & \end{array}$	$1.46 \cdot 10^{-14}$
10* <sup>,1</sup>	$O_3 + NO \rightarrow NO_2 + O_2$	$3.0 \cdot 10^{-12} \cdot e^{(1500/T)}$		$1.9 \cdot 10^{-14}$
11* <sup>,1</sup>	$O + NO_2 + M \rightarrow NO_3 + M$	2.5·10 <sup>-31</sup> (T/300) <sup>-1.8</sup>	2.2·10 <sup>-11</sup> (T/300) <sup>-0.7</sup>	6.1.10 <sup>-12</sup>
12a* <sup>,2</sup>	$NO_3 + hv \rightarrow NO_2 + O$	0.19 s <sup>-1</sup>		0.19 s <sup>-1</sup>
12b* <sup>,2</sup>	$NO_3 + hv \rightarrow NO + O_2$	$0.016 \text{ s}^{-1}$		0.016 s <sup>-1</sup>
13* <sup>,1</sup>	$NO_3 + NO \rightarrow 2 NO_2$	$1.5 \cdot 10^{-11} e^{(170/T)}$		$2.6 \cdot 10^{-11}$
14* <sup>,1</sup>	$NO_3 + NO_3 \rightarrow 2 NO_2 + O_2$	$8.5 \cdot 10^{-13} e^{(-2450/T)}$		$2.3 \cdot 10^{-16}$
15*,1	$NO_3+NO_2+M \rightarrow N_2O_5+M$	$2.4 \cdot 10^{-30} (T/300)^{-3.0}$ cm <sup>6</sup> molec <sup>-2</sup> s <sup>-1</sup>	$\frac{1.6 \cdot 10^{-12}}{(T/300)^{0.1}}$	$1.34 \cdot 10^{-12}$
16* <sup>,2</sup>	$N_2O_5+M \rightarrow NO_3+NO_2+M$	$\frac{1.3 \cdot 10^{-3} (T/300)^{-3.5}}{e^{(-11000/T)} s^{-1}}$	$9.7 \cdot 10^{14} (T/300)^{0.1}$ e <sup>(-11080/T)</sup> s <sup>-1</sup>	2.98 s <sup>-1</sup>
17 <sup>5</sup>	$O_3 + hv \rightarrow O(^1D) + O_2$	$3 \cdot 10^{-5} \text{ s}^{-1}$		$3 \cdot 10^{-5} \text{ s}^{-1}$
18 <sup>1</sup>	$O(^{1}D) + H_{2}O \rightarrow 2 OH$	$1.63 \cdot 10^{-10} \cdot e^{(60/T)}$		$2.0 \cdot 10^{-10}$
19 <sup>1</sup>	$OH+NO_2+M \rightarrow HNO_3+M$	$1.8 \cdot 10^{-30} (T/300)^{-3}$	$2.8 \cdot 10^{-11}$	$1.05 \cdot 10^{-11}$
20	$OH+NO+M \rightarrow HNO_2+M$	$7 \cdot 10^{-31} (T/300)^{-2.6}$	$3.6 \cdot 10^{-11} (T/300)^{-0.1}$	$9.7 \cdot 10^{-12}$
216	$HNO_2+h\nu \rightarrow OH+NO$	$1.34 \cdot 10^{-3}$		
22	$N_2O_5+(H_2O)_{liq}\rightarrow 2(HNO_3)_{liq}$	neglected		
23	$N_2O_4+H_2O \rightarrow HNO_2+HNO_3$	neglected		





# 4. GAS KINETIC SIMULATIONS

A series of gas kinetic simulation calculations were performed in order to check on the simplified analytical calculations in the previous section.

- 5 In a one-box model, the system of coupled ordinary differential equations resulting from the above reactions was solved numerically. This allows to follow the temporal evolution of the concentration of the individual gases in the cell under given conditions. Our full model includes Reaction 1 to Reaction 16 of Table 1 (marked with an asterisk in column 1) and neglects possible wall losses (reaction 3). Also some runs with a subset of the reactions were performed as described below.
  - The first reaction kinetic model calculations show the temporal evolution of  $[NO_2]$ , [NO],  $[O_2]$ , according to the simple reaction system (reactions 1, 4, and 6) in an illuminated NO<sub>2</sub>-cell. In particular we initially neglect the NO<sub>2</sub> dimer formation. These calculations merely serve to demonstrate that the analytical solution as derived in section 3.1 matches the model calculations.
- 15 Figure 4 shows some results of this (over)simplified model assuming (as above) initial NO<sub>2</sub> levels  $[NO_2]_0$  of 1, 10, 100, 1000 hPa (2.4·10<sup>16</sup>, 2.4·10<sup>17</sup>, 2.4·10<sup>18</sup>, 2.4·10<sup>19</sup> molec/cm<sup>3</sup>), respectively. As expected the initial NO<sub>2</sub> concentration drops within the first few seconds (at high initial NO<sub>2</sub>) to minutes (at low NO<sub>2</sub>) until the back-reaction kicks in and leads to stationary state levels of all species after this initial period. At 1 hPa initial NO<sub>2</sub> its concentration drops to
- 20 very small levels (< 0.1 %) as shown in section 3.1 while at 1000 hPa we still see about 10.7 % loss of initial NO<sub>2</sub> These figures are exactly the same as found from the steady state calculations (see Appendix 1).
- Figure 5 shows some results of the simplified model (reactions 1, 4, and 6) but including the NO<sub>2</sub> - N<sub>2</sub>O<sub>4</sub> equilibrium (reactions 7 and 8) for initial NO<sub>2</sub> levels,  $[NO_2]_0$  of 1, 10, 71, 344 hPa (2.4·10<sup>16</sup>, 2.4·10<sup>17</sup>, 1.7·10<sup>18</sup>, 0.84·10<sup>19</sup> molec/cm<sup>3</sup>, due to filling the cell with NO<sub>2</sub> levels of 1, 10, 100, 1000 hPa, which then immediately undergo N<sub>2</sub>O<sub>4</sub> equilibration), respectively. For the lower initial NO<sub>2</sub> levels (1, 10 hPa) there is little difference to Figure 4: The initial NO<sub>2</sub> concentration drops within the first few seconds to minutes to small fractions of the initial [NO<sub>2</sub>]<sub>0</sub>. As
- 30 discussed above (Sect. 3.3), the situation can be improved by adding initial O<sub>2</sub> (topped up to 1000 hPa). The thin blue line in the plots for [NO<sub>2</sub>]<sub>0</sub> = 1, 10, 71 hPa indicates the results for the corresponding NO<sub>2</sub> profiles. In particular at higher initial NO<sub>2</sub> levels (e.g. 71 hPa) the ultimate NO<sub>2</sub> levels are considerably enhanced by O<sub>2</sub> addition. However at higher initial NO<sub>2</sub> levels (see plots for 71 and 344 hPa initial NO<sub>2</sub>) there is a large reduction in NO<sub>2</sub> due to the NO<sub>2</sub>-dimer formation inducing stronger temperature dependence.
- In order to get a feeling for the influence of temperature changes in the model run for  $[NO_2]_0 = 344$  hPa the temperature was raised by 5 K (298 K to 303 K) after 100s, the corresponding plot (bottom right in Fig. 5) shows an increase in NO<sub>2</sub> (thin blue line) of about 16% due to this temperature rise.







Fig. 4: Model calculations of the temporal evolution of  $[NO_2]$  (thick drawn black line), [NO] (dashed black line),  $[O_2]$  (drawn brown line) according to the simple reaction system (reactions 1, 4, and 6 only, at 298 K) in an illuminated  $NO_2$ -cell. Here the  $NO_2 - N_2O_4$  chemical equilibrium is neglected, which makes in particular the plots for initial  $[NO_2]_0 = 1000$  hPa unrealistic. All time series are for calculation with no added initial  $O_2$ . Initial  $[NO_2]_0 = 1, 10, 100, 1000$  hPa ( $2.4 \cdot 10^{16}, 2.4 \cdot 10^{17}, 2.4 \cdot 10^{18}, 2.4 \cdot 10^{19}$  molec/cm<sup>3</sup>), respectively.







Fig. 5: Same Model calculations as shown in Fig 4 but including  $N_2O_4$ . Initial  $[NO_2]_0 = 1, 10, 71, 344$  hPa  $(2.4 \cdot 10^{16}, 2.4 \cdot 10^{17}, 1.7 \cdot 10^{18}, 0.8 \cdot 10^{19}$  molec/cm<sup>3</sup>), respectively, see text. Temporal evolution of  $[NO_2]$  (thick drawn black line), [NO] (dashed black line),  $[O_2]$ 

(drawn brown line), and  $[N_2O_4]$  (thin dashed-dotted line) according to the simple reaction system (reactions 1, 4, 6, 7, and 8 only, at 298 K) in an illuminated NO<sub>2</sub>-cell. All time series with the exception of the thin blue line (in the plots for  $[NO_2]_0 = 1$ , 10, 71 hPa) are for calculation with no added initial O<sub>2</sub>. The thin blue line (in the plots for  $[NO_2]_0 = 1$ , 10, 71 hPa) indicates the evolution of NO<sub>2</sub> for a calculation with initial O<sub>2</sub> topped up to 1000 hPa. The plot for  $[NO_2]_0 = 344$  hPa additionally shows the increase in NO<sub>2</sub> (thin blue line) at a temperature rise of 5 K (298 K to 303 K).

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Fig. 6: Results of calculations with the full model (reaction 1 to 16, see Table 1). Shown are the temporal evolutions of  $[NO_2]$  (thick drawn line), [NO] (dashed line), [O] (dotted line)  $[O_2]$  (drawn brown line),  $[N_2O_4]$  (dashed-dotted line),  $[NO_3]$  (fine dotted line),  $O_3$  (fine dashed line), and  $[N_2O_5]$  (thin dashed-dotted line) in an illuminated  $NO_2$ -cell. Initial  $[NO_2]_0 = 1, 1, 10, 71, 344$  hPa (2.4·10<sup>16</sup>, 2.4·10<sup>17</sup>, 1.7·10<sup>18</sup>, 0.84·10<sup>19</sup> molec/cm<sup>3</sup>). Except for the top panel

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initial O2 was assumed. Left panel: logarithmic scale, right panel: linear scale.



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Fig. 7: Recovery of NO<sub>2</sub> in the dark after initial illumination: Model calculations of the temporal evolution of [NO<sub>2</sub>] (thick drawn black line), [NO] (dashed black line), [O<sub>2</sub>] (drawn brown line) calculated with the full model (reaction 1 to 16, see Table 1, at 298 K). The NO<sub>2</sub>-cell is initially illuminated for 1500 s and then left in the dark afterwards. Initial [NO<sub>2</sub>]<sub>0</sub> = 1, 1, 10, 71, 344 hPa (2.4·10<sup>16</sup>, 2.4·10<sup>17</sup>, 1.7·10<sup>18</sup>, 0.84·10<sup>19</sup> molec/cm<sup>3</sup>). The blue thin line in the plots for 1, 10, 71 hPa show [NO<sub>2</sub>] for O<sub>2</sub>-topped-up cell.

Further calculations encompass the full range of Reaction 1 to Reaction 16 (except wall losses) as given in Table 1, where an analytical solution is not practical or probably even impossible.
Figure 6 shows the results of these model runs for NO<sub>2</sub>, NO, O-atoms, O<sub>2</sub>, N<sub>2</sub>O<sub>4</sub>, NO<sub>3</sub>, O<sub>3</sub>, and N<sub>2</sub>O<sub>5</sub> in an illuminated NO<sub>2</sub>-cell for initial, N<sub>2</sub>O<sub>4</sub>-equilibrated [NO<sub>2</sub>]<sub>0</sub> = 1, 10, 71, 344 hPa (2.4·10<sup>16</sup>, 2.4·10<sup>17</sup>, 1.7·10<sup>18</sup>, 0.84·10<sup>19</sup> molec/cm<sup>3</sup>). In the top panel no initial O<sub>2</sub> was assumed, the





remaining panels show time series with initial  $O_2$ . The left and right panels have logarithmic and linear concentration scales, respectively. Comparison of the result with the data in Figure 5 shows that there are no fundamental differences in the  $NO_2$  time series between the simple model and the full model.

- 5 As discussed in section 3.1 the recovery of NO<sub>2</sub> in the dark after initial illumination (e.g. due to a use of the cell in a measurement) is an important question. Figure 7 shows model calculations of the temporal evolution of NO<sub>2</sub>, NO, and O<sub>2</sub> according to the full model (reaction 1 to 16, see Table 1, at 298 K). The NO<sub>2</sub>-cell is initially illuminated for 1500 s and then left in the dark afterwards for initial, N<sub>2</sub>O<sub>4</sub>-equilibrated [NO<sub>2</sub>]<sub>0</sub> = 1, 10, 71, 344 hPa ( $2.4 \cdot 10^{16}$ ,  $2.4 \cdot 10^{17}$ ,  $1.7 \cdot 10^{18}$ ,
- 10  $0.84 \cdot 10^{19}$  molec/cm<sup>3</sup>), respectively. At the two highest [NO<sub>2</sub>]<sub>0</sub> levels the initial NO<sub>2</sub> was chosen such that total pressures of 100 hPa and 1000 hPa, respectively, were reached. It can be seen that the NO<sub>2</sub> recovery at low NO<sub>2</sub> levels can take days to hours. Adding O<sub>2</sub> to the cell again has a strong impact on the [NO<sub>2</sub>] evolution (see thin blue lines in Fig. 7), reducing the recovery time to a fraction of the NO<sub>2</sub>-only case. For larger initial NO<sub>2</sub> concentrations (e.g. 71 hPa) and added O<sub>2</sub>
- 15 a hysteresis between initial  $[NO_2]$  and equilibrium  $[NO_2]$  in the dark can be observed, i.e. the  $NO_2$  level does not return to its initial value after illumination. This is due to the formation of  $N_2O_5$  in the illuminated period.

## 5. SUMMARY AND CONCLUSIONS

- 20 We conclude that the use of  $NO_2$  cells requires careful consideration, in particular when quantitative measurements of the  $NO_2$  CD in the cell are desired. If unfortunate parameters are chosen (e.g. rather low  $NO_2$  pressures, no  $O_2$  or air added) practically no  $NO_2$  might be found in the cell at all. Also, one can not say that particularly high or low  $NO_2$  concentrations in the cell are the superior choice. At high  $NO_2$  concentrations (approaching atmospheric pressure) a large
- 25 fraction of the NO<sub>2</sub> is converted to the dimer N<sub>2</sub>O<sub>4</sub>, which not only reduces the NO<sub>2</sub> CD way below expected values but also introduces a large temperature dependence (up to 3% per degree) of the NO<sub>2</sub> CD in the cell (also, there might be some uncertainty due to uncertainty of the equilibrium constant as pointed out by Roscoe and Hind, 1993). On the other hand, at low NO<sub>2</sub> levels (e.g. 1 hPa) photolysis may convert much (if not virtually all) of the NO<sub>2</sub> to NO. Although
- 30 NO<sub>2</sub> eventually recovers, this process may take long (days) to complete. Thus the actual NO<sub>2</sub> CD of the cell may become dependent on the illumination and recovery history of the cell and may be rather unpredictable for a particular cell.

Unfortunately, the two described effects are not even the full story, therefore the potential problems are listed below. Fortunately, there are ways to minimize the problems, like oxygen addition to the cell and choosing the right  $NO_2$  concentration, which may help to reduce the uncertainty of the  $NO_2$  CD of a given cell to the single digit percent range.

#### 5.1. Summary of Problems

As discussed above the  $NO_2$  concentration in a cell - and thus the  $NO_2$  CD of the cell – can deviate from expectations due to a number of reasons:

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- 1) Optical effects: multiple reflection in the cell and tilt of the cell with respect to the optical axis can enhance the light path and thus the apparent NO<sub>2</sub> CD
- 2) Photolysis of NO<sub>2</sub> can reduce the NO<sub>2</sub>-CD in the cell
- 3) Sequestration of NO<sub>2</sub> as N<sub>2</sub>O<sub>4</sub> due to the thermodynamic equilibrium between the two species can reduce NO<sub>2</sub> in the cell and cause temperature dependence of the NO<sub>2</sub> CD
- 4) (re-)formation of NO<sub>2</sub> from NO in the cell leads to slow recovery of NO<sub>2</sub>
- 5) (Irreversible) Conversion of NO2 to HNO3 can lead to long-term loss of NO2
- 6) Wall loss of  $NO_X$ -species like  $N_2O_4$  or  $N_2O_5$  can lead to long-term loss of  $NO_2$





## 5.2. Some ideas to remedy the situation

One approach to minimize loss of  $NO_2$  in the cell is certainly to reduce the photolysis of  $NO_2$  (R1), this can be achieved by a series of measures:

- 1) Only expose the cell to measurement radiation by e.g. putting it in an nontransparent tube.
- 2) Minimizing exposure time by e.g. putting the cell in a light-tight box when not in use
  - 3) Use filter in front of the cell which only admits radiation at wavelengths >450 nm, this, however, may interfere with the measurements.

Also, it may be good to avoid ozone photolysis in the cell to minimize OH-formation by using a

10 UV-nontransparent cell material, e.g. glass instead of quartz. In addition it is a good idea to keep the gas in the cell as dry as possible to avoid formation of HNO<sub>3</sub> or HNO<sub>2</sub> and to further minimize OH formation.

A further important measure is to add  $O_2$  to the cell in order to enhance re-conversion of any NO formed to  $NO_2$ .

- 15 The problems associated with excessive  $N_2O_4$  formation in the cell (reduction of the NO<sub>2</sub> CD, temperature dependence of the NO<sub>2</sub> CD, HNO<sub>3</sub> formation) can be reduced by using lower NO<sub>2</sub> concentrations in the cell. The length of the cell may need to be extended to still achieve a desired NO<sub>2</sub> CD. In principle the cell may also be heated to lower the amount of steady state  $N_2O_4$ .
- 20 Problems with the optics of the cell are also difficult to avoid, fortunately they usually lead to changes in the NO<sub>2</sub> CD of <10%. In principle anti-reflective coatings could be used on the cell windows to minimize the problems described in section 2. Another approach would be to tilt the cell with respect to the optical axis thus reflected radiation would not reach the entrance optics of the spectrometer.

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# 6. LITERATURE

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#### Appendix 1: Solution of the cubic equation for the stationary state NO concentration:

40 The above Equation 7 is a cubic equation which we recognize as Cardano's formula after substituting z = [NO]:

$$z^{3} + pz + q = 0 (22)$$

For which the solution is well known as (e.g. Bronstein and Semendjajew, 1980):

$$z = u + v \tag{23}$$

45 With:

$$u = \sqrt[3]{-\frac{q}{2} + \sqrt{\Delta}}, \quad v = \sqrt[3]{-\frac{q}{2} - \sqrt{\Delta}}$$
(24)

And:





$$\Delta = \left(\frac{q}{2}\right)^2 + \left(\frac{p}{3}\right)^3 \tag{25}$$

Equation 7 for z=[NO] thus becomes:

$$[NO]^{3} \cdot \frac{k_{6}}{2J_{1}} + [NO] - [NO_{2}]_{0} = 0$$
(26)

It is transformed with  $a = 2J_1/k_6 \approx 4 \cdot 8 \cdot 10^{-3}/1.95 \cdot 10^{-38} \approx 8.205 \cdot 10^{35} \text{ molec}^{2}/\text{cm}^{6}$  to:

$$\left[\mathrm{NO}\right]^{3} + a\left[\mathrm{NO}\right] - a\left[\mathrm{NO}_{2}\right]_{0} = 0$$
<sup>(27)</sup>

Sample solutions:

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1) 1000 hPa of initial NO<sub>2</sub>, i.e.  $[NO_2]_0 = 2.4 \cdot 10^{19}$ : With p = a and q =  $-a[NO_2]_0 \approx -2.4 \cdot 10^{19} \cdot 8.205 \cdot 10^{35} \approx -1.969 \cdot 10^{55}$  and:

$$\Delta = \left(\frac{q}{2}\right)^2 + \left(\frac{p}{3}\right)^3 = \frac{a^2 \left[NO_2\right]_0^2}{4} + \frac{a^3}{27} \approx 9.694 \cdot 10^{109} + 2.046 \cdot 10^{106} \approx 9.696 \cdot 10^{109}$$
(28)

we obtain the only positive and real solution: 10

$$[NO] = u + v = \sqrt[3]{-\frac{a[NO_2]_0}{2} + \sqrt{\Delta} + \sqrt[3]{-\frac{a[NO_2]_0}{2} - \sqrt{\Delta}}}{\approx \sqrt[3]{1.969 \cdot 10^{55}} + \sqrt[3]{-2 \cdot 10^{51}} \approx 2.700 \cdot 10^{18} - 1.26 \cdot 10^{17} \approx 2.574 \cdot 10^{18}}$$
(29)

This means  $[NO]/[NO_2]_0$  is about  $2.574 \cdot 10^{18}/2.4 \cdot 10^{19} \approx 10.7\%$  of the initial NO<sub>2</sub>.

2) At 100 hPa of initial NO<sub>2</sub> ( $[NO_2]_0 = 2.4 \cdot 10^{18}$ ) we obtain  $[NO]/[NO_2]_0 \approx 2.4 \cdot 10^{18} \approx 42.9\%$  of the 15 initial NO<sub>2</sub>.

3) At 10 hPa of initial NO<sub>2</sub> ([NO<sub>2</sub>]<sub>0</sub>=  $2.4 \cdot 10^{17}$ ) we obtain [NO]/[NO<sub>2</sub>]<sub>0</sub>  $\approx 2.4 \cdot 10^{17} \approx 94.0\%$  of the initial NO<sub>2</sub>.

4) At 1 hPa of initial NO<sub>2</sub>, ([NO<sub>2</sub>]<sub>0</sub>= 
$$2.4 \cdot 10^{16}$$
) we obtain [NO]/[NO<sub>2</sub>]<sub>0</sub>  $\approx 100\%$  of the initial NO<sub>2</sub>.