

1 Dear editor,

2 We really appreciated the reviewers for their patience and nice suggestions. The manuscript is
3 revised according to their suggestions. Please see the following responses.

4 Yours,

5 Authors

6

7 **Reply to Anonymous Referee #1**

8

9 I am satisfied by the authors' responses to my review and I recommend this paper be accepted for
10 publication in AMT.

11 I do have one additional minor correction regarding the caption in Fig. 4. In the last sentence please
12 change "showed" to "shown".

13 **Response:**

14 Revised.

15

16 **Reply to Anonymous Referee #2**

17

18 The manuscript is greatly improved. However, it is still not easy to read and one has to be an expert
19 in the field to understand the approach. All in all, it is a very complex and complicated paper.

20 Some recommendations:

21 One should discuss the two recently published CCN-lidar approaches (Lv et al., JGR 2018,
22 Mamouri and Ansmann, ACP 2016) in more detail in the introduction. What is the idea in these two
23 foregoing papers? How do the ideas presented here differ from the foregoing methods.

24 The paper of Mamouri and Ansmann is based on single-wavelength polarization lidar (and not on
25 multiwavelength lidar), and applicable to marine, dust, and pollution aerosol types.

26 **Response:**

27 Additional discussions about the two recent papers were added to the introduction (page 2, line 15-
28 23; page 2, line 29-34 for the marked-up version).

29 *Mamouri and Ansmann (2016) investigate the potential of single-wavelength polarization lidar to*
30 *retrieval CCN for three aerosol types (desert, non-desert continental, and marine). The polarization*
31 *lidar can separate desert and non-desert by means of the particle linear depolarization ratio. Based*
32 *on datasets from multiyear Aerosol Robotic Network (AERONET) observations, valid relationships*
33 *are found between particle extinction coefficients and number concentrations of particles with dry*
34 *radius larger than 50 nm (for non-desert and marine) and 100 nm (for desert). CCN concentrations*
35 *at different supersaturations are parameterized with the particle number concentration derived from*
36 *extinction profiles according to aerosol types. The consideration of the hygroscopicity of ambient*
37 *particles is empirical. Besides, single-wavelength lidar also lacks of sufficient information to*
38 *quantify particle number concentration, which will bring large uncertainty on CCN retrieval.*

39 *Lv et al. (2018) build a look-up table based on AERONET datasets to retrieve particle number size*
40 *distributions from backscatter and extinction profiles. Then assumed activation critical diameters*
41 *according to aerosol type classification together with the retrieved optical-equivalent particle size*
42 *distributions are utilized to calculate CCN concentrations. It is worth noting that most of the*
43 *foregoing methods implement crude particle type classification to determent particle hygroscopicity.*

44 The statement of the difference of our method is also added (page 3, line 21-28 for the marked-up

45 version).
46 *Different from the foregoing approaches which use AERONET datasets, we use in situ measured*
47 *microphysical and chemical data in this study. Theoretical simulations based on in situ*
48 *measurements are carried out to seek the relationship between CCN number concentrations and*
49 *lidar-derived optical properties. The simulation implements κ -Köhler theory (Petters and*
50 *Kreidenweis, 2007) to describe particle hygroscopic growth and activation process. Mie theory*
51 *(Bohren and Huffman, 2007) is utilized to calculate particle backscatter and extinction coefficients*
52 *from in situ measured aerosol microphysical and chemical properties. The enhancements of*
53 *backscatter and extinction with RH are implemented to quantify particle hygroscopicity instead of*
54 *using empirical estimation according to aerosol type classification.*

55
56 One should also clearly state right in the beginning and thus in the introduction: The new method
57 is only applicable to well mixed aerosol layers with large changes in the relative humidity, and thus
58 only in the case of the planetary boundary layer. Furthermore, the method works only in the absence
59 of dust (non spherical particles).

60 **Response:**

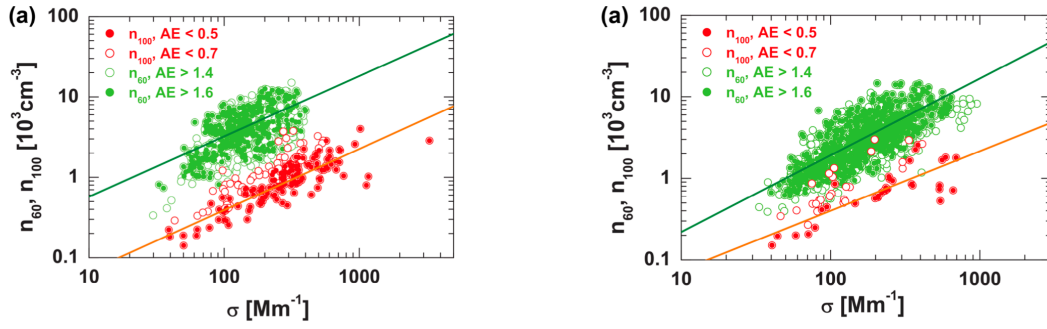
61 The statement was added to the introduction. The method is not limited to the cases with large
62 changes in RH, because the RH range is flexible. For different cases with different RH ranges,
63 researchers only need to change the input data (parameters fitted from different RH ranges) for the
64 random forest model. The RH range in the paper is just an example. Also, well-mixed layers are
65 commonly found in the planetary boundary layer (PBL), but they can appear in the free troposphere,
66 especially for cumulus above the PBL. The following statement was added (page 3, line 28-31 for
67 the marked-up version):

68 *The new method is applicable to well-mixed aerosol layers. We take datasets in the North China*
69 *Plain (NCP) as an example of this method. The NCP is influenced by heavy and complex pollution*
70 *which shows strong characteristics of continental aerosols. Mineral dust and marine particles are*
71 *not considered in this study.*

72
73 You could compare your AR values with published ones in Mamouri and Ansmann 2016 and
74 Shinozuka, Y., et al. : The relationship between cloud condensation nuclei (CCN) concentration and
75 light extinction of dried particles: indications of underlying aerosol processes and implications for
76 satellite-based CCN estimates, Atmos. Chem. Phys., 15, 7585-7604, [https://doi.org/10.5194/acp-](https://doi.org/10.5194/acp-15-7585-2015)
77 [15-7585-2015](https://doi.org/10.5194/acp-15-7585-2015), 2015.

78 **Response:**

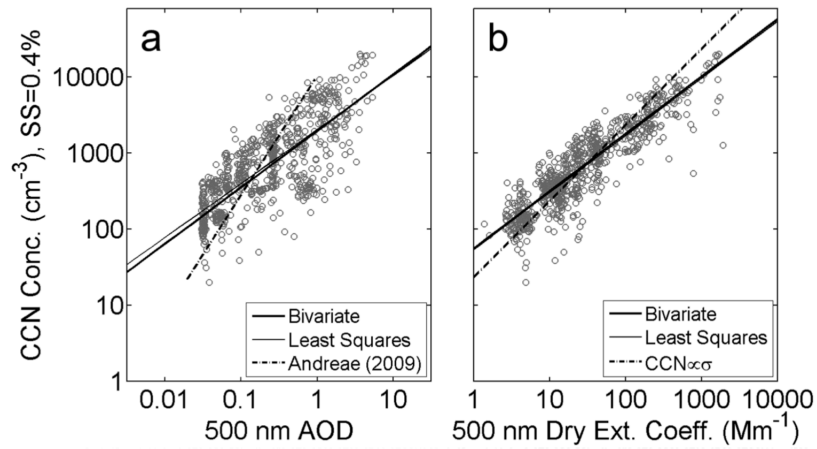
79 Mamouri and Ansmann (2016) describe the relationship between extinction coefficient at 532 nm
80 and number concentrations of particle with radius larger than 60 (n₆₀) and 100 nm (n₁₀₀) (see Figure
81 R1). The extinction and number concentrations are all in ambient condition. According to Mamouri
82 and Ansmann (2016), n₆₀ represents n₅₀ at dry condition and n₁₀₀ is for desert dust which do not take
83 up water. From Fig. 3(a) in our paper, n₆₀ can be compared with CCN concentrations at
84 supersaturation of 0.20%, and n₁₀₀ can be compared with CCN concentrations at supersaturation of
85 0.10%. Shinozuka et al. (2015) describe the relationship between dry extinction coefficient at 532
86 nm and CCN number concentrations at supersaturation of 0.40% (see Figure R2). Figure R3 gives
87 the results using our simulated data. As there are so many data points, 1000 pairs of data are selected
88 randomly to plot in Fig. R2. The result agrees well with their results in magnitude.



89

90 **Figure R1.** Figure 4(a) (left) and Figure 5(a) (right) in the paper of Mamouri and Ansmann (2016).

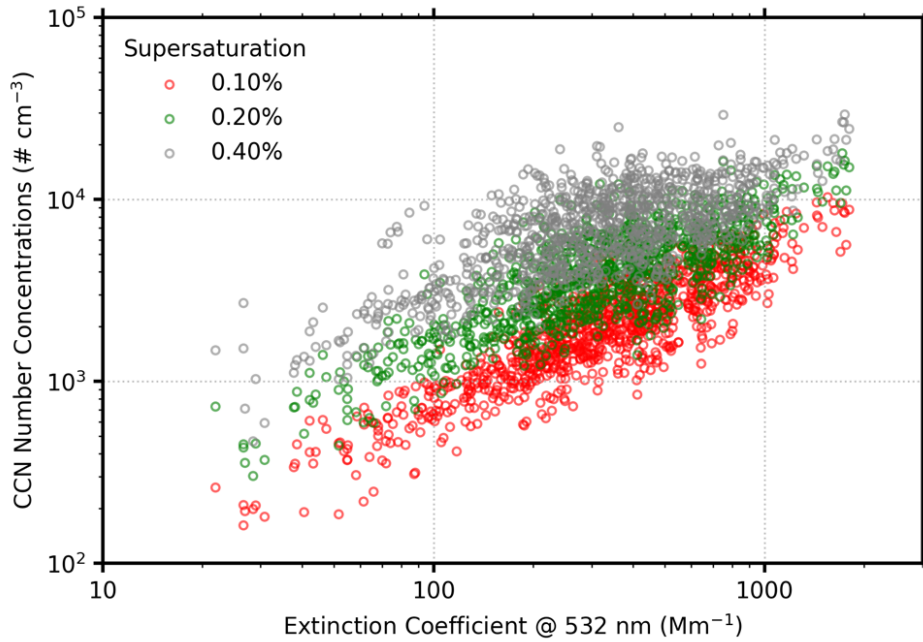
91



92

93 **Figure R2.** Figure 1 in the paper of Shinozuka et al. (2015)

94



95

96 **Figure R3.** Relationship between dry extinction coefficient at 532 nm and CCN number
 97 concentrations at supersaturations of 0.10% (red), 0.20% (green), and 0.40% (grey).

98

99 If your RH is retrieved by using microwave radiometer (no water vapour Raman lidar) then relative
 100 uncertainties in the range of 10-20% are much more realistic as your 5% (in all your simulations).

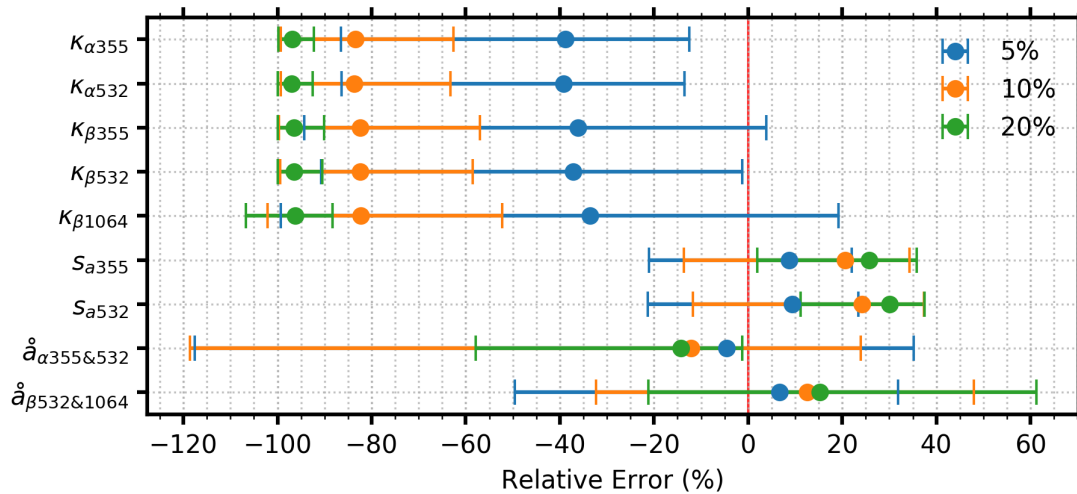
101 **Response:**

102 We added additional two tests of random error considering RH uncertainty of 10% and 20%. Table
 103 6 (Table R1) and Figure 8 (Figure R4) are accordingly updated. Description and discussion in the
 104 manuscript are also renewed.

105 **Table R1.** Mean and one standard deviation (std) values (mean \pm std) of relative errors in retrieved
 106 CCN number concentrations at different supersaturations with different random error conditions.
 107 The uncertainty of backscatter and extinction coefficients of all the tests is 10%, and the
 108 uncertainties of relative humidity are 5%, 10%, and 20%, respectively.

Supersaturation ratio	Random error (10% for backscatter and extinction)		
	Error of relative humidity		
	5%	10%	20%
0.07%	-4.1% \pm 21.8%	0.2% \pm 23.4%	0.7% \pm 22.6%
0.10%	-1.5% \pm 23.4%	-2.8% \pm 24.0%	-2.5% \pm 21.2%
0.20%	-1.2% \pm 27.8%	-9.1% \pm 26.3%	-5.2% \pm 18.0%

109



110

111 **Figure R4.** Relative errors in fitted and calculated parameters with 10% random errors for
 112 backscatter and extinction and 5% (blue), 10% (orange), and 20% (green) random error for relative
 113 humidity. The dots are the median values, and the error bars denote the 5th and 95th percentiles.
 114 The dashed red line marks the position of zero.

115

116 Figure4: very confusing y-axis and x-axis parameters:

117 For ‘model-predicted extinction-related CCN activation ratio...’

118 may be simply use ‘AR applied in the retrieval’ or simply ‘retrieval AR’

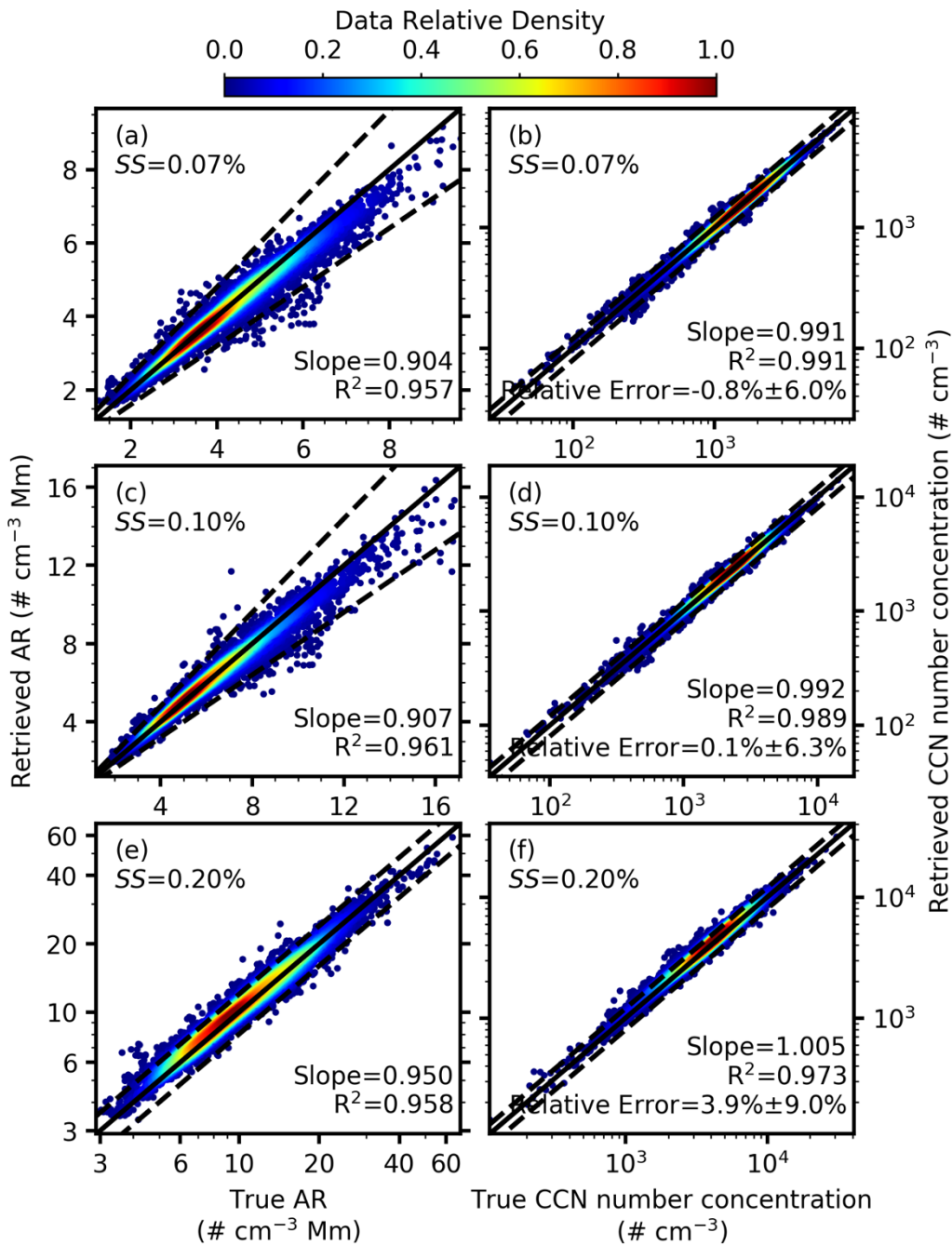
119 and for

120 ‘theoretical calculated extinction-related CCN activation ratio...’

121 take ‘true AR’ or ‘modelled AR’

122

Response:



124

125 **Figure R5.** Comparison of the theoretical calculated extinction-related CCN activation ratio at 532
 126 nm (true AR) and the model predicted extinction-related CCN activation ratios at 532 nm (retrieved
 127 AR) at supersaturations of (a) 0.07%, (c) 0.10%, and (e) 0.20%, and of the theoretical calculated
 128 CCN number concentrations (true CCN number concentration) and the retrieved CCN number
 129 concentrations at supersaturations of (b) 0.07%, (d) 0.10%, and (f) 0.20%. A total of 80575 pairs of
 130 data calculated from campaign C5 are used. The solid line is 1:1 line, and the dashed lines are 20%
 131 relative difference lines. Colors represent the relative density of the data points normalized by the
 132 maximum data density of each panel. The relative error shown in the figure is mean value \pm one
 133 standard deviation.

134

135 **Reference**

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139 Retrieval of Cloud Condensation Nuclei Number Concentration Profiles From Lidar Extinction and
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147 1961-2007, 2007.
- 148 Shinozuka, Y., Clarke, A. D., Nenes, A., Jefferson, A., Wood, R., McNaughton, C. S., Ström, J., Tunved,
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150 between cloud condensation nuclei (CCN) concentration and light extinction of dried particles:
151 indications of underlying aerosol processes and implications for satellite-based CCN estimates,
152 *Atmospheric Chemistry and Physics*, 15, 7585-7604, 10.5194/acp-15-7585-2015, 2015.
- 153

Method to retrieve cloud condensation nuclei number concentrations using lidar measurements

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- 10 *Correspondence to:* Chengcai Li (ccli@pku.edu.cn)

Abstract. Determination of cloud condensation nuclei (CCN) number concentrations at cloud base is important to constrain aerosol-cloud interactions. A new method to retrieve CCN number concentrations using backscatter and extinction profiles from multiwavelength Raman lidars is proposed. The method implements hygroscopic enhancements of backscatter and extinction with relative humidity to derive dry backscatter and extinction and humidogram parameters. Humidogram parameters, Ångström exponents, and lidar extinction-to-backscatter ratios are then linked to the ratio of CCN number concentration to dry backscatter and extinction coefficient (AR_{ξ}). This linkage is established based on the datasets simulated by Mie theory and κ -Köhler theory with in situ measured particle size distributions and chemical compositions. CCN number concentration can thus be calculated with AR_{ξ} and dry backscatter and extinction. An independent theoretical simulated dataset is used to validate this new method and results show that the retrieved CCN number concentrations at supersaturations of 0.07%, 0.10%, and 0.20% are in good agreement with theoretical calculated values. Sensitivity tests indicate that retrieval error in CCN arise mostly from uncertainties in extinction coefficients and RH profiles. The proposed method improves CCN retrieval from lidar measurements and has great potential in deriving scarce long-term CCN data at cloud base which benefits aerosol-cloud interaction studies.

15
20

1 Introduction

- 25 Anthropogenic activities have caused an increase in atmospheric aerosols, and some of the aerosol particles affect the climate by serving as cloud condensation nuclei (CCN). CCN in clouds can modify cloud forming processes and cloud microphysical properties (Rosenfeld et al., 2014). Although numerous impacts of aerosol-cloud interactions on radiative forcing (McCoy et al., 2017; Zhou et al., 2017), precipitation (Xu et al., 2017; Fan et al., 2018), cloud electrification (Wang et al., 2018), and severe weathers or hazards (Fu et al., 2017) have been discovered, constraining the relationships between aerosols and clouds is still

a big challenge (Seinfeld et al., 2016). Lacking the knowledge of aerosol-cloud interactions limits our ability to estimate climate forcing caused by aerosols (Boucher et al., 2013).

Aerosol CCN supersaturation activation spectrum is one of the most critical parameters to quantify aerosol-cloud interactions (Schmale et al., 2018). Despite that a large amount of CCN number concentrations near ground have been measured worldwide (Tao et al., 2017), ground-measured CCN may not represent CCN at cloud base that alter clouds directly. Obtaining CCN near cloud base becomes a crucial issue. Cloud base CCN can be measured in situ on aircraft platforms, but airborne measurements have the limitations of huge costs and discontinuity. Satellites are difficult to observe CCN at cloud base, because clouds can obscure aerosol signals beneath them. Rosenfeld et al. (2016) have proposed an alternative approach for satellites to retrieve CCN concentrations using clouds as CCN chambers, however, employing CCN concentrations derived with this strategy limits our exploration of the relationship between CCN concentrations and cloud droplet concentrations in the natural environment. So far, CCN concentrations at cloud base are scarce for aerosol-cloud interaction studies.

Ground-based lidars can continuously provide optical properties of aerosol particles from ground up to cloud base (Mattis et al., 2016; Li et al., 2019), suggesting great potential in deriving CCN concentrations near cloud base. Ghan and Collins (2004) propose a simple method to infer CCN profiles with the combination of surface in situ CCN and aerosol optical measurements.

The method is only applicable when boundary layer is well mixed from surface to cloud base (Ghan et al., 2006). Mamouri and Ansmann (2016) investigate the potential of single-wavelength polarization lidar to retrieval CCN for three aerosol types (desert, non-desert continental, and marine). The polarization lidar can separate desert and non-desert by means of the particle linear depolarization ratio. Based on datasets from multiyear Aerosol Robotic Network (AERONET) observations, valid relationships are found between particle extinction coefficients and number concentrations of particles with dry radius larger than 50 nm (for non-desert and marine) and 100 nm (for desert). CCN concentrations at different supersaturations are parameterized with the particle number concentration derived from extinction profiles according to aerosol types. The consideration of the hygroscopicity of ambient particles is empirical. Besides, single-wavelength lidar also lacks of sufficient information to quantify particle number concentration, which will bring large uncertainty on CCN retrieval.

Multiwavelength Raman lidars (MWRLs) are increasingly used to detect aerosol vertical distributions in recent years. The principle of MWRLs allows independent retrieval of particle backscatter (β) and extinction coefficients (α), which provides more information about particle microphysical properties (Müller et al., 2016). The $3\beta+2\alpha$ MWRL systems (backscatter coefficients at 355, 532, and 1064 nm and extinction coefficients at 355 and 532 nm) have been widely recommended to derive particle microphysical properties (Burton et al., 2016). Existing approaches to retrieve CCN using MWRLs are based on microphysical inversion techniques ~~Mamouri and Ansmann (2016)~~. Lv et al. (2018) build a look-up table based on AERONET datasets to retrieve particle number size distributions from backscatter and extinction profiles. Then assumed activation critical diameters according to aerosol type classification together with the Retrieved-retrieved optical-equivalent particle size distributions together with assumed activation critical diameters are utilized to calculate CCN concentrations Lv et al. (2018). It is worth noting that most of the foregoing methods implement crude particle type classification to determent particle hygroscopicity.

There are three major challenges in CCN concentration retrieval with lidars. The first is the conversion of lidar-derived optical properties into particle number concentrations. High uncertainties of retrieved particle number concentrations could be an important source of CCN retrieval error. The second one is the determination of particle hygroscopicity in order to evaluate the ability of particles to participate as CCN. Particle hygroscopicity, which is highly related to chemical composition and aging/coating effect, is found to cause nonnegligible variations in cloud droplet activation (Hudson, 2007;Zhang et al., 2017). The last is the influence of high relative humidity (RH) near clouds. Aerosol particles are likely to be humidified in the ambient environment, and the consequent changes in optical properties make CCN retrieval more challenging. Most studies working on CCN retrieval with MWRLs mainly focus on deriving particle number concentrations, but seldom commence to solve the issue of hygroscopicity.

10 In recent years, several aerosol hygroscopic studies based on lidar measurements have been carried out (Fernández et al., 2017;Lv et al., 2017;Bedoya-Velásquez et al., 2018). Backscatter and extinction enhancement factors can be derived with lidar measurements and RH profiles. The enhancement factor, which is associated with both particle size and hygroscopicity (Kuang et al., 2017), is defined as:

$$f_{\xi}(\text{RH}, \lambda) = \frac{\xi(\text{RH}, \lambda)}{\xi(\text{RH}_{\text{ref}}, \lambda)}, \quad (1)$$

15 where f_{ξ} is the enhancement factor of the optical property ξ (backscatter or extinction) at a specific light wavelength λ and RH, and RH_{ref} is the reference RH value. Many studies manifest that lidar-derived enhancement factors are in good agreement with in situ measurements (Wulfmeyer and Feingold, 2000;Pahlow et al., 2006;Fernández et al., 2015;Rosati et al., 2016). Feingold and Morley (2003) demonstrate that the extent of backscatter and extinction enhancements hints at the ability of particles to serve as CCN. Tao et al. (2018) use in situ measured light scattering enhancement factors to predict N_{CCN} at 0.07% supersaturation, and the result shows strong consistency with CCN counter.

20 In this paper, a new method to retrieve CCN number concentrations for $3\beta+2\alpha$ MWRL systems is proposed. Different from the foregoing approaches which use AERONET datasets, we use in situ measured microphysical and chemical data in this study. Theoretical simulations based on in situ measurements are carried out to seek the relationship between CCN number concentrations and lidar-derived optical properties. The simulation implements κ -Köhler theory (Petters and Kreidenweis, 2007) to describe particle hygroscopic growth and activation process. Mie theory (Bohren and Huffman, 2007) is utilized to calculate particle backscatter and extinction coefficients from in situ measured aerosol microphysical and chemical properties. The enhancements of backscatter and extinction with RH are introduced to quantify particle hygroscopicity instead of using empirical estimation according to aerosol type classification. The new method is applicable to well-mixed aerosol layers. We take datasets in the North China Plain (NCP) as an example of this method. The NCP is influenced by heavy and complex pollution which shows strong characteristics of continental aerosols. Mineral dust and marine particles are not considered in this study.

The paper is structured as follows. ~~The field campaign and in situ measurements are introduced in Sect. 2.1. Section 2.2 briefly introduce the simulations to calculate CCN number concentrations, backscatter, and extinction coefficients from in situ measured microphysical and chemical data. Section 2 introduces the measured and simulated datasets used in this paper.~~ The new CCN retrieval method for MWRLs ~~is described in Sect. 3.1 in detail. Sensitivity of the method to the systematic and random errors of backscatter, extinction, and RH is tested in Sect. 3.2, and the sensitivity tests are respectively described in Sect. 3.1 and Sect. 3.2. Sensitivity tests are carried out in Sect. 3.2.~~ Results and discussions are given in Sect. 4. Section 5 summarizes the paper.

2 Data

Since it is not easy to accumulate large datasets of simultaneous measurements of lidars and aircrafts, ground-measured aerosol microphysical and chemical data are used to simulate lidar-derived backscatter and extinction coefficients and corresponding CCN number concentrations. The simulations are based on κ -Köhler theory and Mie theory. The required datasets include: particle number size distribution (PNSD), black carbon (BC) mass concentrations (m_{BC}), mixing state of BC containing particles, and size-resolved hygroscopicity. The simulation results are used to establish and validate the new retrieval method.

2.1 Datasets of aerosol microphysical and chemical properties

In situ measured aerosol properties were collected from five field campaigns at three different measurement sites in the ~~North China Plain~~ (NCP). The measurement sites are located at Wuqing (39°23' N, 117°01' E, 7.4 m a.s.l) in Tianjin, Xianghe (39°45' N, 116°58' E, 36 m a.s.l) and Wangdu (38°40' N, 115°08' E, 51 m a.s.l) in Hebei province. The specific locations, topographical information, and pollution status of these measurement sites are shown in Fig. S1 in the Supplement. These three sites all lie inside the polluted NCP region and are highly representative of the polluted background (Xu et al., 2011; Bian et al., 2018; Sun et al., 2018). Time periods, measured parameters, and corresponding instruments of individual campaign are listed in Table 1. During these field campaigns, except measurement for size-resolved chemical compositions, ambient particles were drawn in through a PM10 inlet (16.67 L/min), passed through a silica gel diffusion drier, and then were split into different instruments. All instruments were operated at RH less than 30%.

The particle number size distributions (PNSDs) were measured with the combination of a twin differential mobility particle sizer (TDMPS, IfT, Leipzig, Germany) or a scanning mobility particle size spectrometer (SMPS) and an aerodynamic particle sizer (APS, TSI, Inc., Shoreview, MN USA, Model 3320 or Model 3321). The statistical information about the measured PNSDs is shown in Fig. 1a. The peaks of the PNSDs are at about 100 nm (diameter in log-scale), which shows strong characteristics of continental aerosols.

The black carbon (BC) mass concentrations (m_{BC}) were measured by a multi-angle absorption photometer (MAAP, Thermo, Inc., Waltham, MA USA, Model 5012). As for mixing states of BC, BC and other non-absorbing compositions were found to

be both externally mixed and core-shell mixed during the campaigns (Ma et al., 2012). The mass fraction of externally-mixed BC (r_{ext}) is defined to quantify the mixing states of BC:

$$r_{\text{ext}} = \frac{m_{\text{ext_BC}}}{m_{\text{BC}}}, \quad (2)$$

where $m_{\text{ext_BC}}$ is the mass concentration of externally mixed BC. According to Ma et al. (2012), r_{ext} can be retrieved from
 5 hemispheric backscattering fractions (HBFs) measured by an integrating nephelometer (TSI, Inc., Shoreview, MN USA, Model 3563).

Size-resolved chemical compositions all come from campaign C2. The size-resolved aerosol sampling was carried out with a
 ten-stage Berner low pressure impactor (BLPI). Chemical species including inorganic ions (NH_4^+ , Na^+ , K^+ , Mg^{2+} , Ca^{2+} , NO_3^- ,
 SO_4^{2-} , Cl^-), elemental carbon, organic carbon, water-soluble organic carbon and some other species such as dicarboxylic acids
 10 were analyzed from sample substrates. After transforming the ambient wet aerodynamic diameters into dry volume-equivalent
 diameters, size-resolved κ distributions were derived from measured size-resolved chemical compositions. The chemical
 compositions are found to be size dependent during the campaign C2, especially the mass fraction of organic matter (Liu et
 al., 2014). Twenty-five typical size-resolved κ distributions in the NCP are given in Fig. 1b. The measured size-resolved κ
 distributions vary a lot and cover a wide range of aerosol hygroscopicity (Kuang et al., 2018). More details about the
 15 measurements can be found in Liu et al. (2014).

2.2 Datasets of CCN number concentrations and lidar-derived optical properties

In situ measured aerosol properties mentioned above are utilized to calculate CCN number concentrations and particle
 backscatter and extinction coefficients base on κ -Köhler theory and Mie theory. For each simultaneously measured PNSD,
 m_{BC} , and r_{ext} (16183 sets of data), simulations are carried out with every one of the twenty-five size-resolved κ distributions.
 20 CCN number concentrations can be calculated with PNSD and size-resolved κ distributions based on κ -Köhler equation. Petters
 and Kreidenweis (2007) introduce the κ -Köhler equation to describe the relationship between particle or droplet diameter D
 and critical supersaturation ratio (SS) or RH with a single hygroscopic parameter κ :

$$\text{RH}(D) = 1 + \text{SS}(D) = \frac{D^3 - D_{\text{dry}}^3}{D^3 - D_{\text{dry}}^3(1 - \kappa)} \exp\left(\frac{4\sigma_{\text{s/a}}M_{\text{w}}}{RT\rho_{\text{w}}D}\right), \quad (3)$$

where D_{dry} is particle dry diameter, $\sigma_{\text{s/a}}$ is the surface tension of the solution-air interface, M_{w} is the molecular weight of
 25 water, R is the universal gas constant, T is temperature, and ρ_{w} is the density of water. For a specific supersaturation, critical
 activation diameter can be derived with κ -Köhler equation using size-resolved κ distributions. CCN number concentrations
 thereby can be calculated by integrating number concentrations of particles larger than the critical diameter. CCN number
 concentrations at the supersaturations of 0.07%, 0.10%, 0.20%, 0.40%, and 0.80% are accordingly simulated. The selected
 supersaturation ratios are widely used in CCN measurements.

30 Particle backscatter and extinction can be calculated with PNSD, m_{BC} , and r_{ext} using Mie models. Mie theory can solve light
 scattering problems of homogeneous and coated spherical particles. Without the consideration of mineral dust, using Mie

model is quite reasonable because particles are likely to be spherical near clouds where the RH could be relatively high. When simulating particle backscatter and coefficients, PNSD, m_{BC} , r_{ext} , and complex refractive index are needed. PNSD at different RH can be calculated with κ -Köhler equation as well. The refractive indices of BC, non-absorbing component, and pure water are set to be $1.8+0.54i$ (Ma et al., 2012), $1.53+10^{-7}i$ (Wex et al., 2002), and $1.33+10^{-7}i$ respectively. Backscatter coefficients (355, 532, and 1064 nm) and extinction coefficients (355 and 532 nm) at dry condition and RH from 60-90% are simulated with an interval of 1%.

The simulations are introduced in detail in Sect. S3 in the Supplement. The new method and all the analyses in this paper are based on the Mie model simulated datasets, and all the simulations mentioned above are implemented.

3 Methodology

10 3.1 Method to retrieve CCN number concentrations using MWRL

3.1.1 Overview

An optical-related CCN activation ratio, AR_{ξ} , is introduced to bridge the gap between CCN and lidar-derived optical properties. AR_{ξ} is the ratio between CCN number concentration and backscatter or extinction coefficient, which can be expressed as:

$$15 \quad AR_{\xi}(SS, \lambda) = \frac{N_{CCN}(SS)}{\xi_{dry}(\lambda)} = \frac{N_{CCN}(SS)}{N_{aerosol}} \cdot \frac{N_{aerosol}}{\xi_{dry}(\lambda)}, \quad (4)$$

where N_{CCN} is the CCN number concentration, and $N_{aerosol}$ is the total number concentration of aerosol particles. AR_{ξ} can be divided into two parts: one is the ratio of CCN to the total particles, which is the origin definition of CCN activation ratio; the other is the ratio of total number concentration to backscatter or extinction at dry condition. Bulk CCN activation ratio is related with particle size distribution and hygroscopicity, and the relationship between particle number concentration and optical properties is mainly controlled by size distribution. Therefore, AR_{ξ} could be quantified with size and hygroscopicity information. The key point of our method is to seek parameters that can indicate size and hygroscopicity of particles from lidar measurement and use these parameters to estimate AR_{ξ} . Besides, deriving backscatter and extinction coefficients at dry condition is also important.

A schematic diagram of the method to retrieve CCN number concentration is shown in Fig. 2.

25 Firstly, enhancement of backscatter and extinction coefficients with RH (also called humidogram) is derived from lidar measurements and additional ancillary data (i.e. pressure, temperature, RH profiles). Humidogram parameter which can indicate particle hygroscopicity can be fitted from humidograms with parameterization equation. Particle dry backscatter and extinction can also be inferred from the humidograms. This step is applied to all the $3\beta+2\alpha$ parameters. The approaches to select appropriate hygroscopic layers and fit humidogram parameters, dry backscatter, and dry extinction are described in Sect.

30 3.1.2.

Then, Ångström exponent (\hat{a}) and lidar extinction-to-backscatter ratio (lidar ratio, s_a) are calculated from inferred dry backscatter and extinction coefficients. Extinction-related Ångström exponent (\hat{a}_α) is the most commonly used parameter to reveal information about the predominant size of aerosols. Generally speaking, a smaller \hat{a}_α represents there are more large particles. Similarly, backscatter-related Ångström exponent (\hat{a}_β) are often employed in lidar analysis (Fernández et al., 2015), and particle backscatter coefficients of different wavelengths also have been proved to have a valid Ångström exponent relationship (Komppula et al., 2012). Ångström exponent of dry backscatter and extinction coefficients (\hat{a}_ξ) between two wavelengths can be derived using Eq. (5):

$$\hat{a}_\xi(\lambda_1, \lambda_2) = -\frac{\log(\xi_1/\xi_2)}{\log(\lambda_1/\lambda_2)}, \quad (5)$$

where the subscript 1 and 2 represents different wavelengths. Another widely used parameter to express aerosol characteristics in lidar studies is the particle lidar extinction-to-backscatter ratio (lidar ratio, s_a), which is defined as the ratio of extinction coefficient to backscatter coefficient at a specific light wavelength:

$$s_a(\lambda) = \frac{\alpha(\lambda)}{\beta(\lambda)} = \frac{4\pi}{P(\pi)\omega}. \quad (6)$$

As is shown in Eq. (6), lidar ratio is determined by the scattering phase function at 180° $P(\pi)$ and the single scattering albedo ω . $P(\pi)$ is mainly influenced by particle size and ω indicates the content and mixing state of light absorbing components. Lidar ratio is often utilized in aerosol type classification and is proved to be very sensitive to particle sizes (Zhao et al., 2017). The lidar ratio can provide information on particle type and also serve as a proxy for particle hygroscopicity. Therefore, lidar ratio of dry particles could be a reliable parameter to estimate AR_ξ .

Next, \hat{a}_ξ , s_a , and humidogram parameters are utilized to estimate AR_ξ . AR_ξ of all the $3\beta+2\alpha$ parameters is calculated. Statistical relationship among humidogram parameters, \hat{a}_ξ , s_a , and AR_ξ are used in our new method. The estimation of AR_ξ is introduced in Sect. 3.1.3 in detail. The implement of \hat{a}_ξ and s_a is quite similar to the microphysical inversion process for particle size distribution retrieval. Microphysical inversion is a physics-based approach but will bring large uncertainties in retrieving particle number concentrations. Constraining AR_ξ directly with statistical relationship is a much more simple and straightforward way.

Finally, after AR_ξ of backscatter and extinction at different wavelengths are derived, CCN number concentration can be calculated by multiplying AR_ξ by the corresponding ξ_{dry} . The average value of CCN concentrations calculated by different ξ_{dry} is the final retrieval result.

3.1.2 Derivation of humidogram parameters, dry backscatter, and dry extinction from lidar measurement

A constraint needs to be satisfied when quantifying the enhancements of backscatter and extinction coefficients with lidar measurements. The selected vertical layers must be well-mixed, so we can guarantee that the variations of particle backscatter and extinction coefficients are caused by different RH and not by various aerosol types or loads. Atmospheric vertical homogeneity is fulfilled if the layer has little variability of virtual potential temperature profile and water vapor mixing ratio

profile (Lv et al., 2017). Additional analyses can also be considered to evaluate vertical mixing of air masses, such as backward trajectory, horizontal wind velocities at different altitude, or the third moment of the frequency distribution of vertical wind velocities (Bedoya-Velásquez et al., 2018).

Once vertical homogeneity is ensured, physical and chemical properties at dry condition can be assumed to be uniform in the selected layer, and the number concentrations are proportional to air molecule number density. Accordingly, the relative variations of particle backscatter and extinction coefficients against different RH can be achieved after normalizing the backscatter and extinction coefficients with air molecule number density.

Humidogram parameterization is needed to find a representative parameter for the relationship between enhancement factor and RH. Unlike in situ controlled-RH measurements, there is no such a generic reference RH as dry condition for lidar measurements to derive enhancement factor. Inferring backscatter and extinction coefficients at dry condition (ξ_{dry}) is also an important issue in CCN retrieval. Therefore, humidogram parameterization of lidar-derived optical properties should combine ξ_{dry} and $f_{\xi}(\text{RH}, \lambda)$ together.

Many equations to parameterize enhancement factors have been proposed by previous studies (Titos et al., 2016). Two one-parameter equations are selected to test their performance on estimating ξ_{dry} and representing particle hygroscopic growth characteristics. The first equation is the most commonly used one initially introduced by Kasten (1969):

$$\xi(\text{RH}, \lambda) = \xi_{\text{dry}}(\lambda) \cdot f_{\xi}(\text{RH}, \lambda) = \xi_{\text{dry}}(\lambda) \cdot (1 - \text{RH})^{-\gamma_{\xi}(\lambda)}, \quad (7)$$

where the exponent γ_{ξ} is the fitting parameter and describes the hygroscopic behavior of the particles; the other equation is proposed based on physical understanding by Brock et al. (2016), which has been reported to have better performance in describing light scattering enhancement factor than Eq. (7) (Shin et al., 2018):

$$\xi(\text{RH}, \lambda) = \xi_{\text{dry}}(\lambda) \cdot f_{\xi}(\text{RH}, \lambda) = \xi_{\text{dry}}(\lambda) \cdot \left[1 + \kappa_{\xi}(\lambda) \frac{\text{RH}}{1 - \text{RH}} \right], \quad (8)$$

where κ_{ξ} is the fitting parameter and shows significant correlation with bulk hygroscopic parameter κ (Kuang et al., 2017). Here, Eq. (7) and Eq. (8) are denoted as γ -equation and κ -equation respectively. With given backscatter and extinction at different RH, ξ_{dry} and γ_{ξ} or κ_{ξ} can be fitted simultaneously by means of least squares.

Comparisons between the performances of γ -equation and κ -equation on inferring backscatter and extinction at dry condition are carried out to select a better parameterization. Four RH ranges (60%-90%, 60%-70%, 70%-80%, and 80%-90%) are selected. The fitted ξ_{dry} are compared with the ξ_{dry} calculated by Mie model. The slopes of linear regressions, determination coefficients (R^2), and relative errors are listed in Table 2. Apparently, κ -equation has a better performance than γ -equation for all RH ranges. Inferring ξ_{dry} with γ -equation will underestimate about 10%-30%. It is consistent with the finding of Haarig et al. (2017) that γ -equation does not hold for RH lower than 40%. The bias of backscatter is found to be larger than the bias of extinction.

The RH range of humidogram equations also influences the fitting results. Table 2 shows the fitted ξ_{dry} have larger bias when the value of RH increase. The fitted humidogram parameters γ_{ξ} and κ_{ξ} from different RH ranges are compared to each other,

and the results are displayed in Table 3. Parameterization equations are not always perfect for the whole RH ranges, so humidogram parameters fitted with various RH ranges can be different. If γ_ξ and κ_ξ are used to represent hygroscopic behavior of particles, more careful attention should be paid to the RH ranges.

Based on the comparisons above, Eq. (8) (κ -equation) is selected as our humidogram equation to derive ξ_{dry} and κ_ξ . The RH range for parameter fitting used is fixed to 60%-90% in the following method.

3.1.3 Estimation of AR_ξ

Ångström exponents, lidar ratios, and optical humidogram parameters κ_ξ are used to estimate optical-related activation ratio AR_ξ . Concerning the Ångström exponents and lidar ratios are not independent to each other (any parameter can be calculated from other parameters), we reduce the number of parameters to a sufficient number to represent all the information. The selected nine parameters are listed in Table 4. One possible way to seek the relationship between the nine parameters and AR_ξ is to build a lookup table, but too many input parameters would make the lookup table so large to build and operate.

In the past few decades, machine learning has been a field that has developed rapidly, which experiences a very wide range of applications (Grange et al., 2018). Compared to traditional statistical methods, many machine learning techniques are nonparametric and do not need to fulfill many assumptions required for statistical methods (Immitzer et al., 2012). Random forest (RF) is an ensemble decision tree machine learning method that can be used for regression. (Breiman, 2001; Tong et al., 2003). Beside the free restraints on input parameters and assumptions, RF also has the advantage of being able to explain and investigate the learning process (Kotsiantis, 2013). The Python module *RandomForestRegressor* from the Python Scikit-Learn library (<http://scikit-learn.org/stable/modules/generated/sklearn.ensemble.RandomForestRegressor.html>, last access: 18 December 2018) are utilized as the RF model. The nine parameters in Table 4 are the input parameters for the RF model, and the AR_ξ of the $3\beta+2\alpha$ are the output parameters.

Some tuning parameters required by RF model need to be specified by users. Experiments are made to determine the optimal values of the tuning parameters. Experiment results are showed in Fig. S7 in the Supplement and the detailed settings of the RF model are listed in Table S2 in the Supplement. In this case, the results are rather insensitive to the tuning parameters. Data simulated with datasets measured from campaign C1-C4 are utilized as the training data, and those from C5 are used as test data.

3.2 Sensitivity test

Both systematic and random errors exist in lidar-retrieved backscatter and extinction coefficients (Mattis et al., 2016). Systematic errors in backscatter and extinction can come from instrumentation setup, data processing method, and retrieval algorithm. Sensitivity test is carried out to test the impact of systematic errors of backscatter and extinction on CCN retrieval. Errors in backscatter or extinction influence the value of Ångström exponents and lidar ratios. The errors of individual backscatter or extinction are considered to be independent, though systematic errors of different parameters are related. The

systematic errors are given in the range of -20% to 20% with an interval of 2%. In each test, the error is only applied to one parameter, and other parameters are error-free.

RH is another crucial factor in this new method to retrieve CCN. Profiles of RH derived by remote sensing techniques are also influenced by errors. At present, RH profiles are usually obtained with the combination of temperature from microwave radiometer and water vapor mixing ratio from MWRL. Both measurements can cause systematic and random errors in RH (Bedoya-Velásquez et al., 2018). Errors in RH will influence the values of ξ_{dry} and κ_{ξ} , which in turn influence all the nine input parameters. Systematic errors ranging from -10% to 10% in intervals of 1% are considered for RH.

Random errors in observations can be reduced by temporal averaging but cannot be eliminated. The influence of random errors in backscatter, extinction, and RH on CCN retrieval are investigated with Monte Carlo method. Three sets of sensitivity tests for random errors are conducted. Errors obeying Gaussian distribution are generated randomly with the mean value of zero. The standard deviation of Gaussian distribution is fixed at 10% for backscatter and extinction, and the standard deviation of RH is set to be 5%, 10%, and 20% for each test. The procedure is repeated for 2000 times. All the 80575 sets of data from campaign C5 are used for sensitivity test.

4 Results and discussions

4.1 Supersaturations for lidar CCN retrieval

CCN number concentrations are related with supersaturations. Critical diameters of each supersaturations calculated with twenty-five size-resolved κ distributions are shown in Fig. 3a. Most of the critical diameters at supersaturation of 0.07% are larger than 200 nm, while critical diameters at supersaturation of 0.80% are around 50 nm. Suitable supersaturations for lidar CCN retrieval depend on the ability of lidar optical properties to provide information about number and hygroscopicity of CCN-related sizes.

Size cumulative contributions of particle number of all measured particle size distribution and corresponding calculated backscatter and extinction at dry condition are also displayed in Fig. 3a. As the cumulative contributions of particle number suggest, particles with diameter less than 100 nm dominate particle number concentrations (over 65%). However, most backscatter and extinction come from particles larger than 200 nm (around 90%) and almost 100% come from particles larger than 100 nm. If critical diameter is small, dry backscatter and extinction are insensitive to particles diameters that contribute to most CCN concentrations.

Size-resolved enhancement contributions of backscatter and extinction are calculated to discuss hygroscopicity sensitive size of optical enhancement factor measurement. The enhancement contribution is defined as the difference between optical cross-sections of RH at 90% and 60%, and represents the proportion of each size to the enhancement in backscatter or extinction.

As is shown in Fig. 3b, the contributions of the extinction enhancements are concentrated in the diameters within 200 nm to 700 nm, and extinction enhancement at 355 nm is related to smaller particles than that at 532 nm. Similar to particle number, particles with diameters smaller than 100nm contributes little to the enhancements of both backscatter and extinction.

Figure 3b also shows that different κ_{ξ} is sensitive to the hygroscopicity of different size. Size-dependent hygroscopicity is important to estimate CCN rather than a bulk hygroscopicity information, especially for different supersaturation conditions. One humidogram may indicate the bulk hygroscopicity, but it is the hygroscopicity of small particles that influences CCN number concentrations most. Using κ_{ξ} of all the $3\beta+2\alpha$ can provide some information about the hygroscopicity of small particles.

Comparing sensitive size of optical properties and critical diameters at different supersaturations. $3\beta+2\alpha$ MWRL systems have potential to retrieve CCN number concentrations at supersaturations smaller than 0.20%. It is not recommended to estimate CCN concentrations using lidar data at superstations larger than 0.40%.

4.2 CCN number concentrations retrieved with error-free data

With error-free data as input, the model predicted extinction-related activation ratio at 532 nm ($AR_{\alpha 532}$) and the retrieved CCN number concentrations at supersaturations of 0.07%, 0.10%, and 0.20% are compared to the theoretical calculated values. A total of 80575 pairs of data calculated from campaign C5 are used for verification. The retrieval results are displayed in Fig. 4. The values $AR_{\alpha 532}$ at a specific supersaturation are distributed in a wide range and can span over an order of magnitude, indicating that the relationship between CCN and optical parameters is very complex. According to Fig. 4, all data points are distributed almost evenly on both sides of the 1:1 line and the relative errors of most points are within 20%. The determination coefficients (R^2) of CCN concentrations are all larger than 0.97, and the results do not show obvious systematic deviations. The retrieval errors are found to grow with supersaturation. Retrieval results for higher supersaturations (i.e. 0.40% and 0.80%) is displayed in Fig. S8 in the Supplement. There are larger errors for supersaturations of 0.40% and 0.80%. Only 47.76% of the retrieved CCN number concentration at supersaturation of 0.80% have relative errors less than 20%. The results demonstrate again that lidars may not be sufficient enough to retrieve CCN number concentrations at supersaturations larger than 0.40%.

4.3 Importance of size-related and hygroscopicity-related parameters

RF models can evaluate the importance of features (input parameters) by calculating the mean decrease impurity (MDI) for each feature among all the trees in the forest. The MDIs and corresponding standard deviations of each parameter at different supersaturations are shown in Fig. 5. Importance of the nine input parameters varies with supersaturations. For 0.07% and 0.10%, $\kappa_{\alpha 355}$ and $\kappa_{\beta 1064}$ are the two most important parameters, showing the impact of hygroscopicity on the relationship between CCN and optical properties. For 0.20%, $\hat{a}_{\alpha 355\&532}$ becomes much more important. Among the nine input parameters, κ_{ξ} are denoted as hygroscopicity-related parameters, and \hat{a}_{ξ} are denoted as size-related parameters. Particularly, s_a can be regarded as both size- and hygroscopicity-related parameter. As is shown in Fig. 5, hygroscopicity-related parameters, especially $\kappa_{\alpha 355}$, $\kappa_{\beta 1064}$, and $s_{\alpha 532}$, play crucial roles in retrieving CCN. Size-related parameters have already been proved to be vital in retrieving CCN, however, humidogram parameters κ_{ξ} have not been implemented in previous methods. CCN

concentrations retrieved with and without κ_{ξ} are compared to show the importance of κ_{ξ} . When retrieving CCN without κ_{ξ} , the RF model is also trained with datasets from campaign C1-C4, but the input data only contains Ångström exponents and lidar ratios. The retrieved CCN concentrations are all compared with datasets from campaign C5, and the results are listed in Table 5. R^2 of retrieved CCN decreases from 0.991 to 0.887 for supersaturations of 0.07%, from 0.992 to 0.857 for 0.10%, and from 0.973 to 0.785 for 0.20%. Retrieval errors also increase overwhelmingly, and there are significant positive systematic biases. Parameters which are derived from backscatter and extinction enhancements, κ_{ξ} , are indispensable parameters in CCN retrieval.

4.4 Impact of systematic and random error on CCN retrieval

Figure 6 shows the relative errors of CCN retrieved with systematic errors in backscatter and extinction. Errors of retrieved CCN increase as errors of backscatter and extinction increase, and higher supersaturations are more affected by errors of optical parameters. Errors in extinction coefficients at 355 nm (α_{355}) influence the retrieval results most. On average, a positive relative error of 20% in α_{355} will cause about 20% overestimate in CCN number concentrations for supersaturation of 0.07%, about 40% overestimate for 0.10%, and about 60% overestimate for 0.20%. A negative error of 20% in α_{355} will underestimate CCN concentrations, and the degree of impact is slightly smaller than positive error. Errors in extinction coefficient at 532 nm (α_{532}) and at 355nm have opposite effect on retrieval error. Errors in α_{532} do not show significant impact at supersaturations of 0.07% and 0.10%, but an overwhelming effect is found at supersaturations of 0.20%. It is interesting to note that the errors in backscatter coefficients do not affect the results much. However, in practical applications of MWRLs, the errors in extinction are always much larger than the errors of backscatter. If the error of retrieved CCN concentrations needs to be limited to 20% at supersaturation of 0.20%, the errors of retrieved extinction coefficients should to be controlled within 5%.

The test result of systematic error in RH is shown in Fig. 7. When RH has a negative systematic error, CCN concentrations are overestimated, and the extent of overestimation increases as the error increase. A negative error of 10% in RH will overestimate CCN at supersaturations at 0.20% by about 60% in average, and the standard deviation is over 60%. Effects of positive errors in RH is much smaller than negative errors but more complex. The standard deviations of retrieval relative error increase with RH error, and the extreme value of the mean retrieval error appears at the RH error of 5%. Underestimating RH will cause much more errors than overestimation. Great care should be paid to RH profiles if enhancements of backscatter and extinction with RH are utilized.

The relative error of retrieved CCN with random errors are presented in Table 6. The retrieval error does not change significantly as the random error of RH increases. For all the conditions that are tested, the mean values of relative error are below or near zero, and the standard deviations are within 18%-28%. The mean values of relative error are 2.8%, 1.3%, and 1.3% for CCN at supersaturations of 0.07%, 0.10%, and 0.20%, respectively, and the corresponding standard deviations are 29.7%, 31.5%, and 42.9%. The impact of random errors on the nine input parameters is also evaluated and is shown in Fig. 8. Random errors will (10% for backscatter and extinction, and 5% RH) underestimate κ_{ξ} by 30%-35% in average for 5% RH

~~error, 80-85% for 10% RH error, and 90-95% for 20% RH error, and the standard deviations are about 40% or more. s_{a355} , s_{a532} , and $\hat{a}_{\beta532\&1064}$ are likely to be overestimated by 5%–10%. As the random error of RH grows, the absolute relative error of input parameters will become larger.~~

5 Summary

5 CCN number concentration at cloud base is a crucial and scarce parameter to constrain the relationship between aerosols and clouds. A new method to retrieve CCN number concentrations using backscatter and extinction coefficients from MWRL measurements is proposed. Enhancements of backscatter and extinction coefficients with RH are implemented to derive dry backscatter and extinction ξ_{dry} and humidogram parameter κ_{ξ} . The ratio of CCN number concentration to dry backscatter or extinction coefficient AR_{ξ} , which is estimated by κ_{ξ} , Ångström exponents, and lidar ratios, is introduced to retrieve CCN
10 number concentrations.

The method is established and verified by theoretical simulations using Mie theory and κ -Köhler theory with in situ measured particle size distributions, mixing states, and chemical compositions. The values of AR_{ξ} are found to have large variations due to different size distributions and hygroscopicity. Theoretical analyses show that optical properties provided by current $3\beta+2\alpha$ MWRL systems basically contains size distribution and hygroscopicity information of particles with diameters larger than 100
15 nm, which only fits the critical diameters for supersaturations lower than 0.20%. Accordingly, CCN number concentrations at supersaturations of 0.07%, 0.10%, and 0.20% are retrieved. The performance of the new method is evaluated with error-free data, and CCN number concentrations at all three supersaturations are in good agreements with theoretical calculated values. Sensitivity tests are carried out to show the influence of systematic and random errors of lidar-derived optical properties and auxiliary RH profiles on CCN retrieval. Systematic errors in extinction coefficients and RH are found to have large impact on
20 error in retrieved CCN. Parameters fitted from backscatter and extinction enhancements (i.e. ξ_{dry} and κ_{ξ}) is significantly influenced by RH. The uncertainty of RH profiles derived by remote sensing techniques is a major problem in CCN retrieval. Optical properties near cloud base from lidar measurements always influenced by high RH. Thus, transforming backscatter and extinction coefficients at ambient RH to dry conditions is a must for CCN retrieval, and accurate RH profiles are highly demanded.

25 The importance of humidogram parameters κ_{ξ} is demonstrated by comparing the error of CCN concentration retrieved with and without κ_{ξ} . Neglecting hygroscopicity information contained in backscatter and extinction enhancements will bring huge errors to CCN retrieval by lidars. The performance of two parameterization schemes for backscatter and extinction humidograms are evaluated. The κ -equation shows better performance on inferring dry backscatter and extinction than γ -equation. The κ -equation, therefore, is recommended to describe the hygroscopic behaviors of the backscatter and extinction
30 coefficients from lidar measurements. The fitted hygroscopic parameter are found to be sensitive to fitting RH range when the RH range is limited and relatively high (between 60%-90%). This is an extreme essential problem for current research for

aerosol hygroscopicity with lidar measurements. Great care should be paid to the RH range when evaluating the hygroscopic growth of the lidar-related optical properties.

It should be noted that the theoretical analyses in this paper are based on datasets of continental aerosols, and the implement of Mie theory also limits the scope of the results. The results can be applied in the North China Plain but are not fit for sea salts and mineral dust. Studies with datasets of other aerosol types should be carried out in the future. Although the applicability of this new method is limited by large uncertainties in RH profiles, comparison between real measured MWRL data and airborne in situ measurement should also be conducted.

This work furthers our understanding of the relationship between CCN and aerosol optical properties and providing an optional way to retrieve CCN number concentration profiles from lidar measurements. The newly proposed method has potential to provide long-term CCN at cloud base for aerosol-cloud-interaction studies.

Author contribution. C. Zhao and C. Li determined the main goal of this study. W. Tan and G. Zhao designed the methods. W. Tan carried them out and prepared the manuscript with contributions from all co-authors.

Competing interests. The authors declare that they have no conflict of interest.

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Table 1. Locations, time periods, parameters, and instruments of five field campaigns

Location	Wuqing	Wuqing	Xianghe	Xianghe	Wangdu
Campaign name	C1	C2	C3	C4	C5
Time period	7 March to 4 April, 2009	12 July to 14 August, 2009	22 July to 30 August, 2012	9 July to 30 August, 2013	4 June to 14 July, 2014
PNSD	TSMPS+APS	TSMPS+APS	SMPS+APS	TSMPS+APS	TSMPS+APS
m_{BC}	MAAP	MAAP	MAAP	MAAP	MAAP
HBF	TSI 3563	TSI 3563	TSI 3563	TSI 3563	TSI 3563
Size-resolved chemical composition	–	Substrates sampled by BLPI	–	–	–

Table 2. Slopes of linear regressions, determination coefficients (R^2), and relative errors (RE) between Mie model simulated particle dry backscatter or extinction coefficients and those inferred from humidogram functions. 404575 pairs of the simulations from in situ dataset are used. The RE are given in the form of mean value \pm one standard deviation (std).

RH (%)	ξ	γ -equation			κ -equation		
		slope	R^2	RE(%)	slope	R^2	RE(%)
60-90	$\alpha_{355,\text{dry}}$	0.850	0.998	-16.2 \pm 2.1	1.045	0.998	3.4 \pm 2.4
	$\alpha_{532,\text{dry}}$	0.820	0.998	-19.2 \pm 2.0	1.017	0.999	0.5 \pm 1.8
	$\beta_{355,\text{dry}}$	0.784	0.960	-20.8 \pm 7.2	0.817	0.971	-9.6 \pm 7.5
	$\beta_{532,\text{dry}}$	0.812	0.972	-22.7 \pm 7.6	0.874	0.988	-11.7 \pm 5.6
	$\beta_{1064,\text{dry}}$	0.878	0.986	-12.9 \pm 5.7	0.935	0.994	-5.4 \pm 4.4
60-70	$\alpha_{355,\text{dry}}$	0.913	1.000	-9.2 \pm 1.1	1.016	1.000	1.1 \pm 0.9
	$\alpha_{532,\text{dry}}$	0.900	0.999	-10.4 \pm 1.3	1.005	1.000	0.0 \pm 0.7
	$\beta_{355,\text{dry}}$	0.939	0.989	-9.1 \pm 6.0	0.906	0.991	-5.6 \pm 4.9
	$\beta_{532,\text{dry}}$	0.939	0.990	-9.9 \pm 5.6	0.939	0.996	-6.4 \pm 3.9
	$\beta_{1064,\text{dry}}$	0.966	0.997	-3.9 \pm 2.9	0.974	0.999	-1.9 \pm 2.0
70-80	$\alpha_{355,\text{dry}}$	0.852	0.999	-15.8 \pm 1.9	1.037	0.999	2.7 \pm 2.1
	$\alpha_{532,\text{dry}}$	0.827	0.998	-18.3 \pm 1.9	1.012	0.999	0.3 \pm 1.5
	$\beta_{355,\text{dry}}$	0.799	0.950	-20.5 \pm 8.9	0.818	0.968	-10.5 \pm 8.1
	$\beta_{532,\text{dry}}$	0.833	0.966	-21.4 \pm 9.0	0.880	0.986	-11.7 \pm 6.6
	$\beta_{1064,\text{dry}}$	0.898	0.987	-10.8 \pm 5.7	0.942	0.995	-4.6 \pm 4.1
80-90	$\alpha_{355,\text{dry}}$	0.756	0.922	-26.5 \pm 3.8	1.110	0.991	8.5 \pm 5.5
	$\alpha_{532,\text{dry}}$	0.702	0.994	-31.9 \pm 3.1	1.047	0.995	1.9 \pm 4.2
	$\beta_{355,\text{dry}}$	0.547	0.848	-37.0 \pm 11.1	0.695	0.892	-13.4 \pm 14.1
	$\beta_{532,\text{dry}}$	0.593	0.925	-42.1 \pm 8.7	0.775	0.961	-19.2 \pm 8.7
	$\beta_{1064,\text{dry}}$	0.702	0.934	-30.4 \pm 10.3	0.867	0.971	-11.5 \pm 8.8

Table 3. Slopes of linear regressions and determination coefficients (R^2) between γ_ξ or κ_ξ fitted from RH range 60%-90% and those fitted from limited RH ranges (60%-70%, 70%-80%, and 80%-90%).

RH (%)	ξ	γ_ξ		κ_ξ	
		slope	R^2	slope	R^2
60-70	α_{355}	0.992	0.958	1.113	0.955
	α_{532}	0.969	0.978	1.007	0.977
	β_{355}	1.019	0.814	1.213	0.819
	β_{532}	0.790	0.797	0.891	0.799
	β_{1064}	0.806	0.834	1.011	0.812
70-80	α_{355}	1.021	0.996	1.045	0.995
	α_{532}	1.015	0.997	1.014	0.997
	β_{355}	1.115	0.968	1.195	0.958
	β_{532}	1.078	0.973	1.128	0.969
	β_{1064}	0.999	0.979	1.034	0.972
80-90	α_{355}	0.941	0.939	0.847	0.934
	α_{532}	0.957	0.969	0.969	0.967
	β_{355}	0.741	0.679	0.684	0.626
	β_{532}	0.970	0.851	1.002	0.827
	β_{1064}	1.090	0.816	1.036	0.818

Table 4. Lidar derived parameters for predicting optical-related CCN activation ratio AR_{ξ}

Parameter	Description
$\kappa_{\alpha 355}$	Fitted parameter of extinction humidogram at 355 nm in κ -equation form
$\kappa_{\alpha 532}$	Fitted parameter of extinction humidogram at 532 nm in κ -equation form
$\kappa_{\beta 355}$	Fitted parameter of backscatter humidogram at 355 nm in κ -equation form
$\kappa_{\beta 532}$	Fitted parameter of backscatter humidogram at 532 nm in κ -equation form
$\kappa_{\beta 1064}$	Fitted parameter of backscatter humidogram at 1064 nm in κ -equation form
$s_{a 355}$	Particle dry lidar extinction-to-backscatter ratio at 355 nm
$s_{a 532}$	Particle dry lidar extinction-to-backscatter ratio at 532 nm
$\dot{a}_{\alpha 355\&532}$	Ångström exponent of particle dry extinction coefficients between 355 and 532 nm
$\dot{a}_{\beta 532\&1064}$	Ångström exponent of particle dry backscatter coefficients between 532 and 1064 nm

Table 5. Slopes of linear regressions, determination coefficients (R^2), and relative errors (RE) between theoretical calculated CCN number concentrations and CCN number concentrations retrieved with/without κ_ξ as input parameter. The relative errors are given in the form of mean value \pm one standard deviation (std).

Supersaturation Ratio	With κ_ξ			Without κ_ξ		
	slope	R^2	RE(%)	slope	R^2	RE(%)
0.07%	0.991	0.991	-0.8 ± 6.0	0.877	0.866	4.6 ± 26.1
0.10%	0.992	0.989	0.1 ± 6.3	0.857	0.837	5.9 ± 26.7
0.20%	1.005	0.973	3.9 ± 9.0	0.860	0.785	11.9 ± 28.1

Table 6. Mean and one standard deviation (std) values (mean \pm std) of relative errors in retrieved CCN number concentrations at different supersaturations with error-free and different random error (10% for backscatter and extinction and 5% for relative humidity) conditions. The uncertainty of backscatter and extinction coefficients of all the tests is 10%, and the uncertainties of relative humidity are 5%, 10%, and 20%, respectively.

<u>Supersaturation ratio</u>	<u>Random error (10% for backscatter and extinction)</u>		
	<u>Error of relative humidity</u>		
	<u>5%</u>	<u>10%</u>	<u>20%</u>
<u>0.07%</u>	<u>-4.1% \pm 21.8%</u>	<u>0.2% \pm 23.4%</u>	<u>0.7% \pm 22.6%</u>
<u>0.10%</u>	<u>-1.5% \pm 23.4%</u>	<u>-2.8% \pm 24.0%</u>	<u>-2.5% \pm 21.2%</u>
<u>0.20%</u>	<u>-1.2% \pm 27.8%</u>	<u>-9.1% \pm 26.3%</u>	<u>-5.2% \pm 18.0%</u>

5

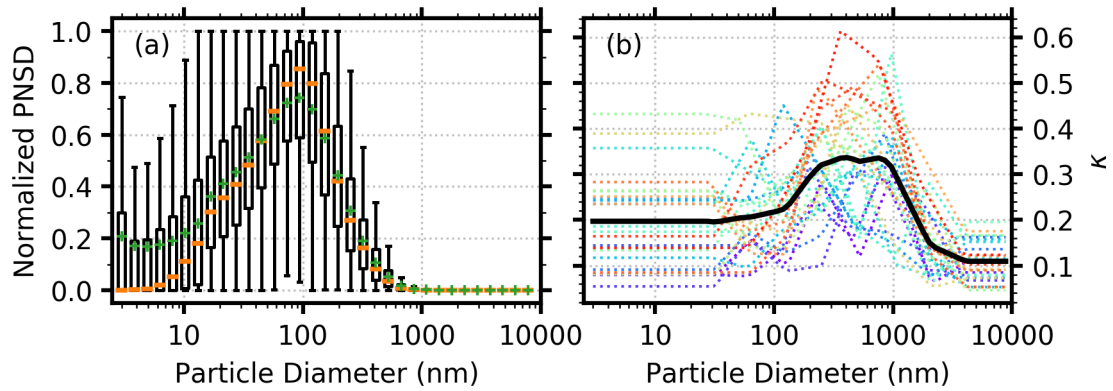


Figure 1. (a) Boxplot of particle number size distributions (PNSDs) in the datasets from five field campaigns. Each PNSD is normalized by its maximum value at the peak diameter. Green markers “+” represent the mean value of each diameter. The boxes extend from the lower to upper quartile values, with orange lines at the median. The whiskers extend from the box to the minimum/maximum values or extend from the box by 1.5 times of interquartile range. The flyers are not shown in the plot. **(b)** Twenty-five typical size-resolved κ distributions. Each dotted line with color represents one size-resolved κ distribution. The solid black line represents the mean value of the size-resolved κ distributions.

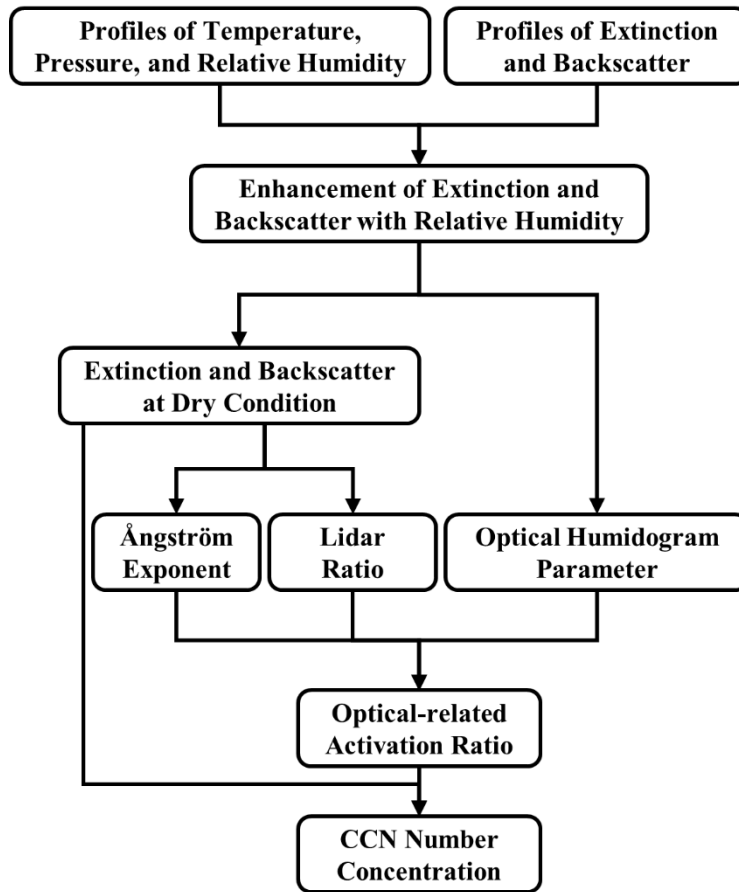


Figure 2. Schematic diagram of newly proposed method to retrieve cloud condensation nuclei number concentrations using multiwavelength Raman lidar.

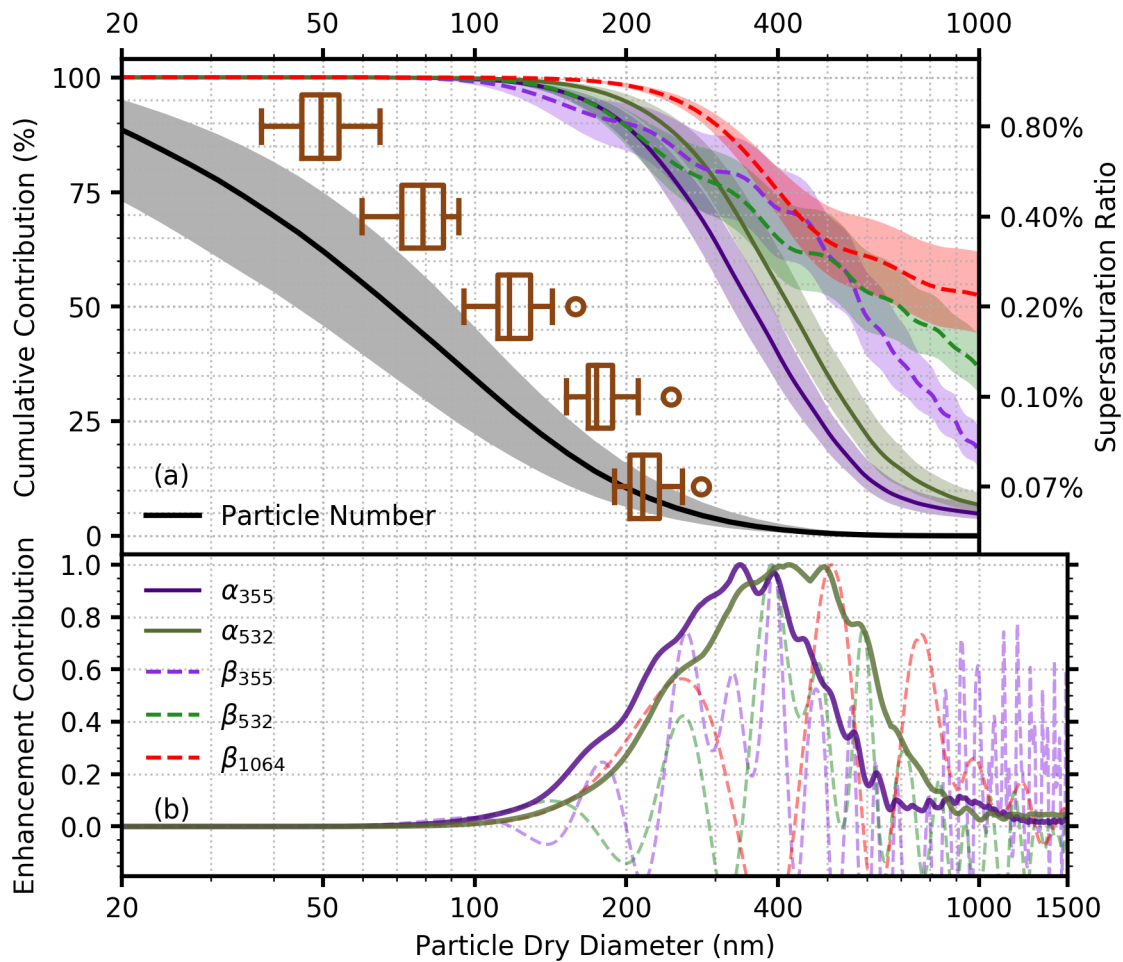
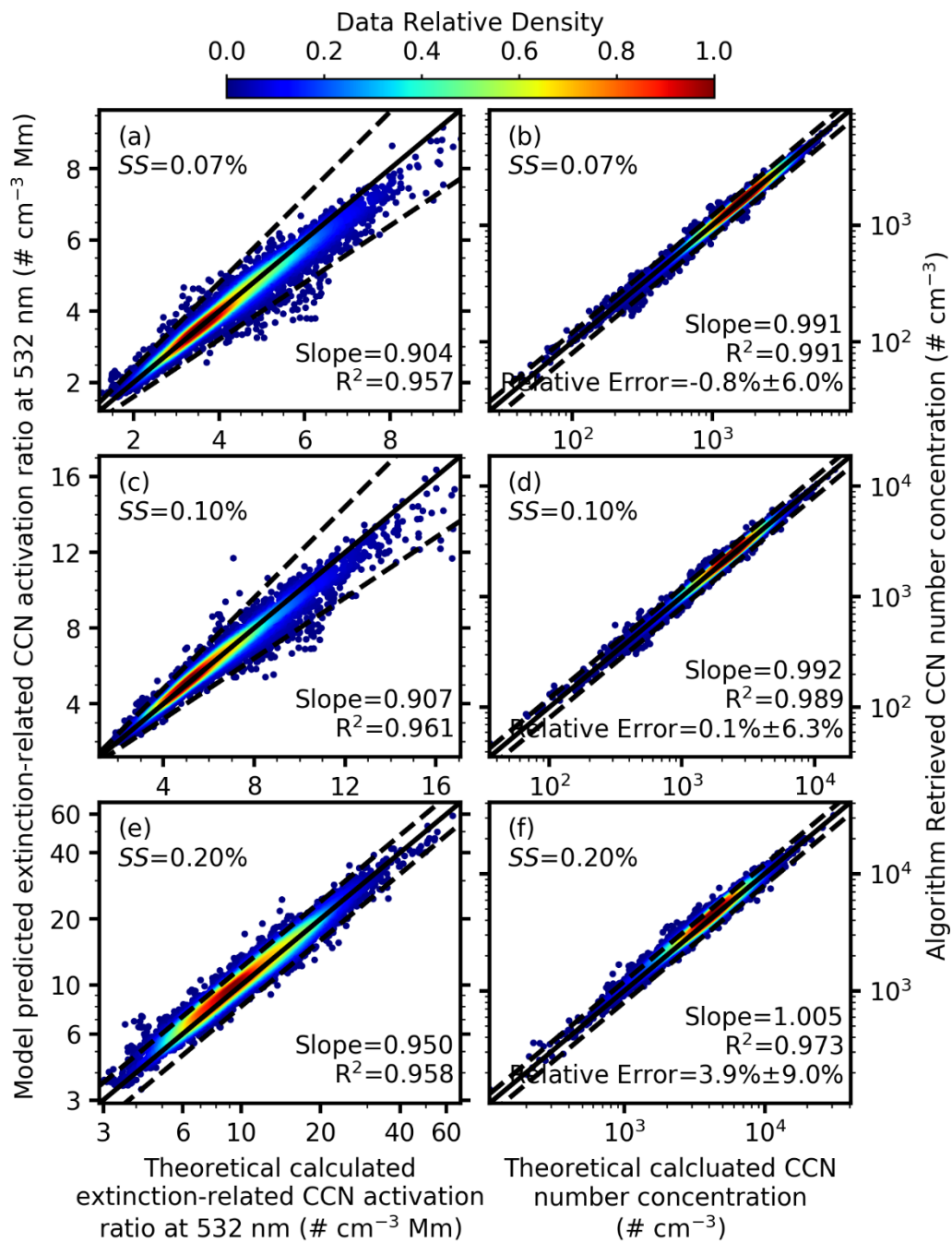


Figure 3. (a) Cumulative contributions (accumulate from large particle size to small particle size) of particle number concentrations (measured), dry particle backscatter coefficients (simulated), and dry particle extinction coefficients (simulated). The solid and dashed lines represent the median values of five field campaigns, and the shadows cover from the lower to upper quartile values. The box plots in brown contain statistical information about critical diameter of each supersaturation condition (right y-axis). The boxes extend from the lower to upper quartile values, with lines at the median. The whiskers extend from the box to the minimum/maximum values or extend from the box by 1.5 times of interquartile range. The markers “o” are the flyers. **(b)** Normalized size-resolved enhancement contributions when relative humidity increases from 60% to 90%, which are theoretically calculated by the mean particle number size distribution, the mean black carbon mass concentration ($4.717 \mu\text{g m}^{-3}$), the mean mass ratio of externally mixed black carbon (0.664%), and the mean size-resolved κ distribution.



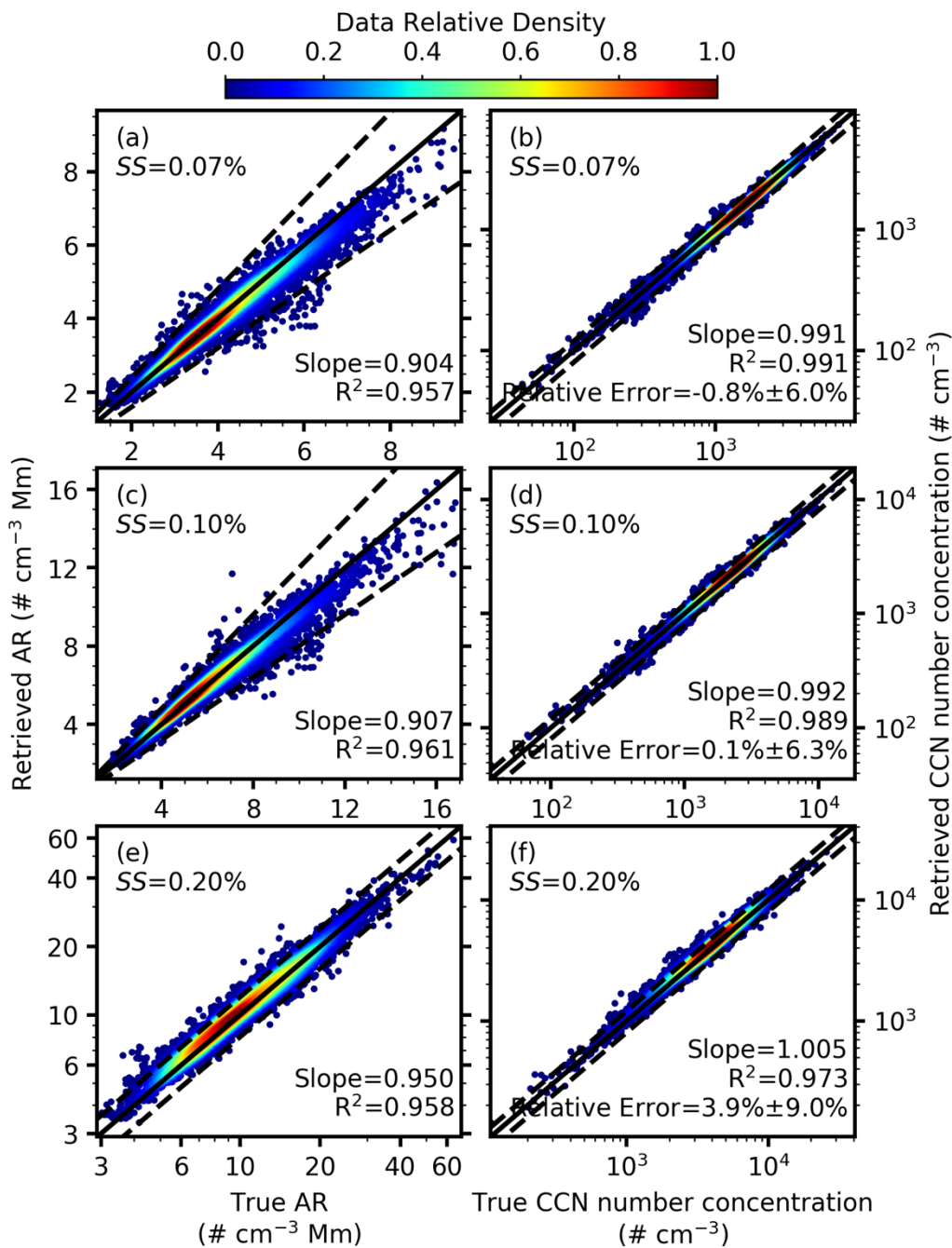


Figure 4. Comparison of the theoretical calculated extinction-related CCN activation ratio at 532 nm (true AR) and the model predicted extinction-related CCN activation ratios at 532 nm (retrieved AR) at supersaturations of (a) 0.07%, (c) 0.10%, and (e) 0.20%, and of the theoretical calculated CCN number concentrations (true CCN number concentration) and the retrieved

CCN number concentrations at supersaturations of **(b)** 0.07%, **(d)** 0.10%, and **(f)** 0.20%. A total of 80575 pairs of data calculated from campaign C5 are used. The solid line is 1:1 line, and the dashed lines are 20% relative difference lines. Colors represent the relative density of the data points normalized by the maximum data density of each panel. The relative error ~~showed~~shown in the figure is mean value \pm one standard deviation.

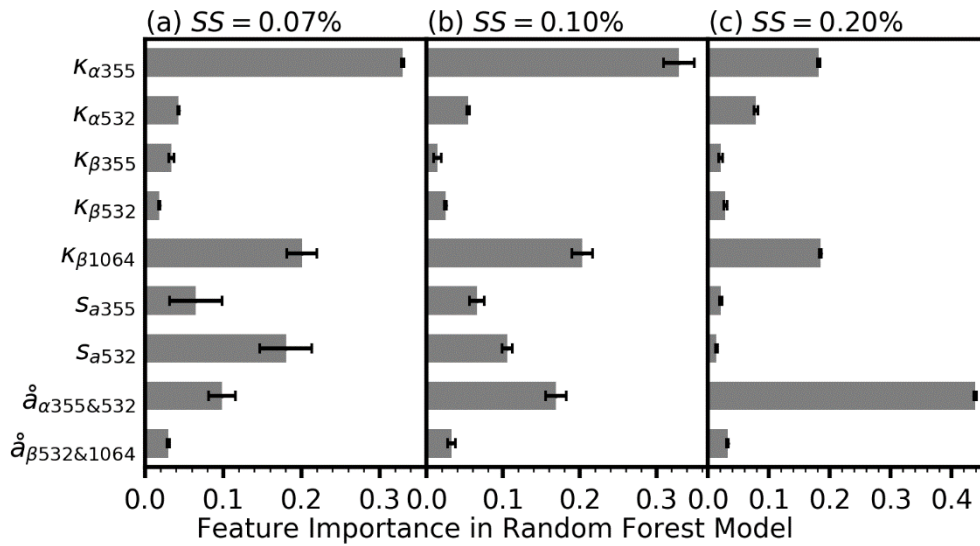


Figure 5. Importance of each feature (input parameter) output by the Random Forest model for predicting optical-related CCN activation ratios at supersaturations of **(a)** 0.07%, **(b)** 0.10%, and **(c)** 0.20%. The values of feature importance indicate the decrease in impurity for each feature. The length of the bar represents the mean values among all trees and the error bars give the standard deviations.

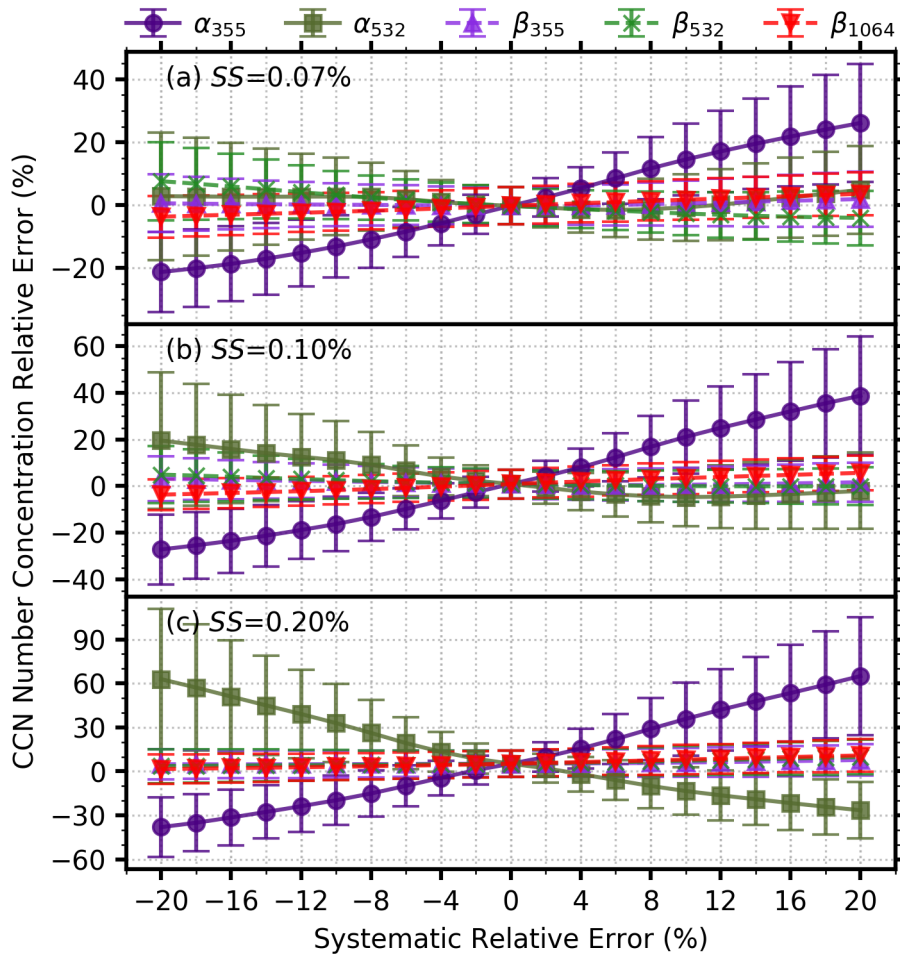


Figure 6. Relative errors in retrieved CCN number concentrations at supersaturations of **(a)** 0.07%, **(b)** 0.10%, and **(c)** 0.20% as a function of systematic errors in backscatter or extinction. The markers are the mean values, and the error bars denote the standard deviations.

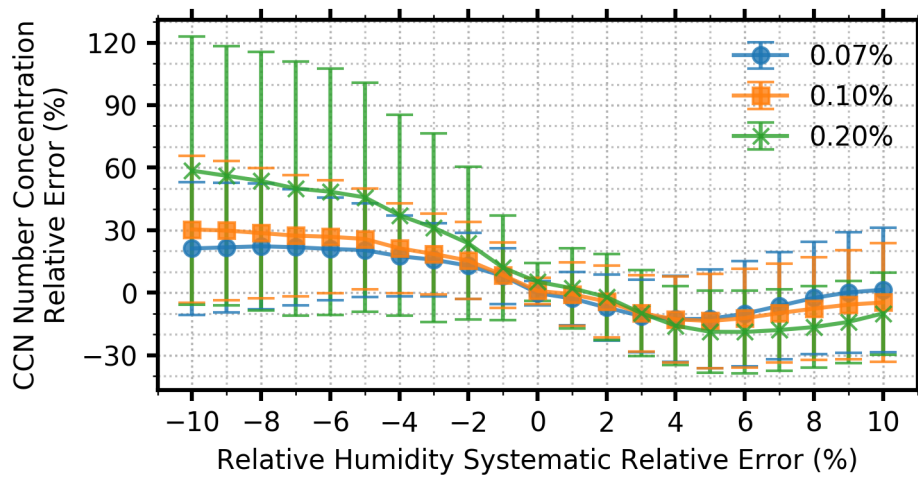


Figure 7. Relative errors in retrieved CCN number concentrations at supersaturations of 0.07%, 0.10%, and 0.20% as a function of systematic errors in relative humidity. The markers are the mean values, and the error bars denote the standard deviations.

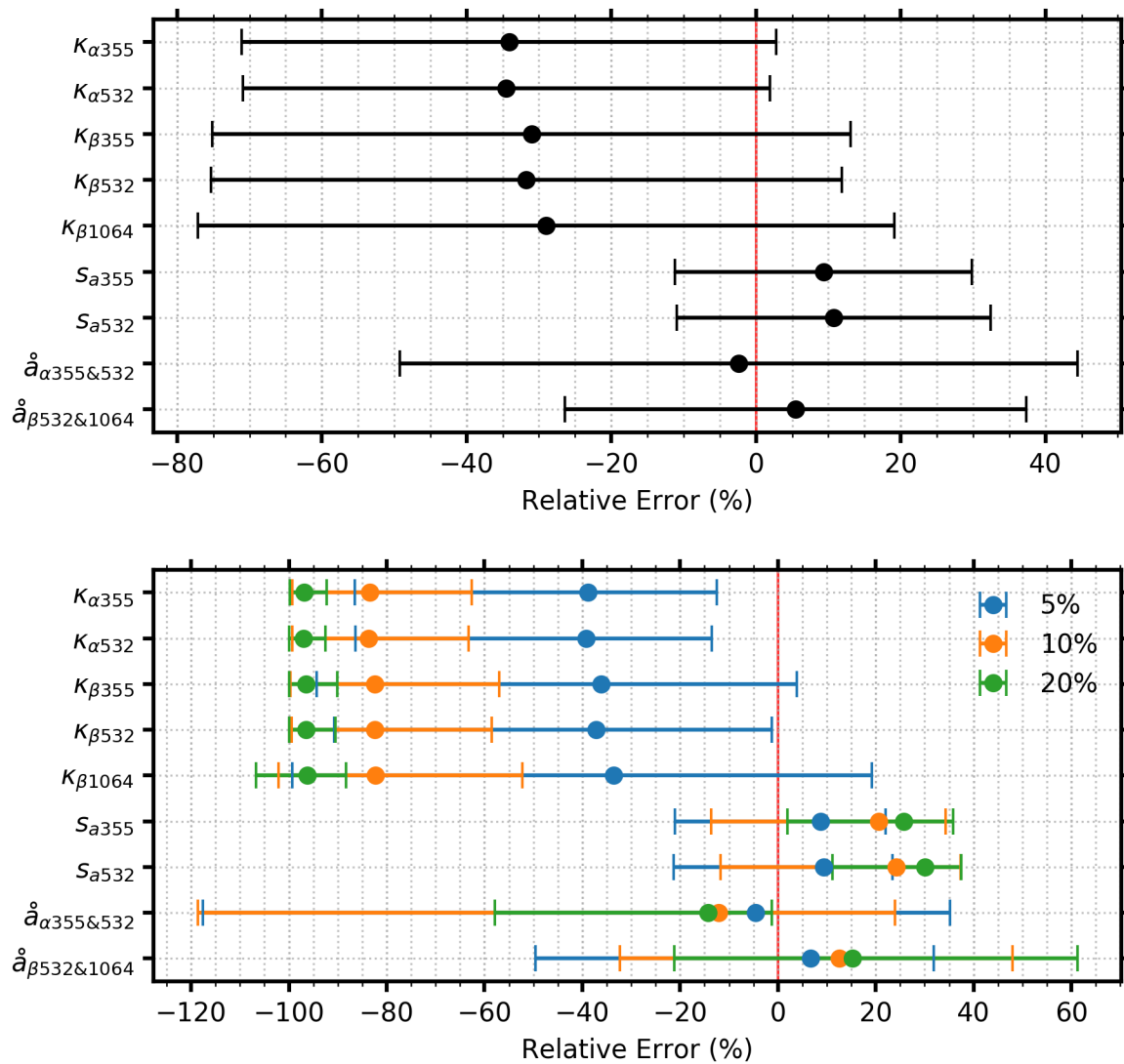


Figure 8. Relative errors in fitted and calculated parameters with 10% random errors for backscatter and extinction and 5% (blue), 10% (orange), and 20% (green) random error for relative humidity. The dots are the mean median values, and the error bars denote the 5th and 95th percentiles standard deviations. The dashed red line marks the position of zero.