

Improved Water Vapour retrieval from AMSU-B/MHS in polar regions

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Abstract.

Exact monitoring of water vapour in the Arctic on long time scales is essential for predicting Arctic weather and understanding climate trends, as well as addressing its influence in the positive feedback loop contributing to Arctic Amplification. However, this is challenged by the sparseness of in-situ measurements and the problems that standard remote-sensing retrieval methods for water vapour have in Arctic conditions. Here, we present advances in a retrieval algorithm for vertically integrated water vapour (total water vapour, TWV) in polar regions from data of satellite-based microwave humidity sounders: (1) In addition to AMSU-B (Advanced Microwave Sounding Unit-B), we can now also use data from the successor instrument MHS (Microwave Humidity Sounder); (2) artefacts caused by high cloud ice content in convective clouds are filtered out. Comparison to in-situ measurements using GPS and radiosondes during 2008 and 2009 as well as radiosondes during the N-ICE2015 campaign show overall good performance of the updated algorithm. Combining TWV data from the present algorithm with those retrieved from microwave imagers like AMSR-E and AMSR2 makes a continuous record of TWV since the year 2000 possible, with nearly complete and year-round coverage of the Arctic.

1 Introduction

Water vapour is a key element of the hydrological cycle (Chahine, 1992; Serreze et al., 2006; Jones et al., 2007; Hanesiak et al., 2010), with shifts in it affecting atmospheric transport processes, creating and intensifying droughts and flooding (Trenberth et al., 2013). Additionally, as the most important greenhouse gas in the atmosphere, it has a dominant effect on climate and radiative forcing (Soden et al., 2002; Dessler et al., 2008; Kiehl and Trenberth, 1997; Trenberth et al., 2007; Ruckstuhl et al., 2007). Hence, it is essential to monitor its variability considering the anthropogenic increase of other greenhouse gases (Solomon et al., 2010), with the water vapour positive feedback loop highlighted as part of other feedbacks responsible for Arctic Amplification (Francis and Hunter, 2007; Miller et al., 2007; Screen and Simmonds, 2010; Ghatak and Miller, 2013). In summary, understanding the water vapour cycle has high value, yet our comprehension is incomplete (Stevens and Bony, 2013). Throughout this paper, when mentioning atmospheric water content, we refer to the vertically integrated mass in a

column of air with a base of 1 m^2 , and call it total water vapour (TWV, sometimes also called column water vapour, integrated water vapour or total precipitable water).

Balloon-borne radiosondes are a standard method for retrieving the water vapour profile. Additionally, ground-based retrievals by microwave radiometers as well as GPS-based retrievals – while having a lower vertical resolution – are good for monitoring purposes in regions where ground stations can be installed. However, in the Arctic, neither radiosondes measurements nor ground-based retrievals are sufficient for this purpose because weather stations are too scarce. Only satellite measurements fulfill the global coverage requirements. An additional challenge is to construct a consistent long-term climate record, due to the changes in measuring instruments, and degradation of the existing ones. Because of the strong absorption properties of water vapour in the infrared and microwave range, suitable space-borne instruments can in principle ensure a complete global coverage of water vapour retrievals (Miao et al., 2001; L. P. Bobylev and Mitnik, 2010). In polar regions, however, satellite retrieval of water vapour faces a number of obstacles such as cloud cover which restricts infrared measurements, or incomplete understanding of the high and highly variable sea-ice emissivity which challenges microwave measurements. Some studies – like the one by Weaver et al. (2017) – have been done for TWV in the Arctic atmosphere, but none of them have been able to provide a long-term Arctic-wide data set.

An important step for Arctic water vapour retrieval comes from the work of Miao et al. (2001). They used data from the SSM/T2 (Special Sensor Microwave/Temperature 2) humidity sounder to develop an algorithm which was designed to work in the Antarctic. The key concept of this method is the use of several microwave channels with similar surface emissivity but different water vapour absorption. These are the three channels near the 183.31 GHz water absorption line (183.31 ± 1 , ± 3 and ± 7 GHz), which, together with the channel at the 150 GHz window frequency, allows retrieval of TWV values up to about 7 kg/m^2 . Above this value, two of the 183.31 GHz band channels become saturated and the sensor is not able to "see" through the whole atmospheric column anymore. This limited range is enough for Antarctica, and suffices for the Arctic in winter conditions (in the polar winter atmosphere, the water vapour column is typically around 3 kg/m^2 according to Serreze et al. (1995)), as well as for the central Arctic (above 70° N) most of the year. However, because of the upper limit, this method cannot ensure monitoring of the complete yearly cycle. The algorithm developed by Melsheimer and Heygster (2008) extends the TWV retrieval range over sea ice by including the 89 GHz channel into the retrieval. Using the triplet of the 183.31 ± 7 , 150 and the 89 GHz channels allows the retrieval to function up the saturation limit of the 183.31 ± 7 GHz channel. This method has been compared with other datasets: In Rinke et al. (2009) a comparison with the HIRHAM model showed realistic patterns and maximum root-mean-square errors for monthly data in summer of 1-2.5 kg/m^2 . For the comparison with Ny Ålesund radiosondes in Palm et al. (2010), the correlation coefficient was 0.86 and the slope $0.8 \pm 0.04 \text{ kg/m}^2$. And lastly, in Buehler et al. (2012) AMSU-B TWV are compared to GPS data from Kiruna, with standard deviations of 1 kg/m^2 and a correlation coefficient of 0.86. However, the AMSU-B algorithm is not without problem: while the frequency range allows it to bypass most clouds, the AMSU-B sensor is still sensitive to convective clouds with high ice content. Here we provide an approach for filtering out problematic data caused by the effect of such ice clouds. This is intended as groundwork for the planned merging with TWV retrieved over open ocean based on passive microwave imagers (product described by Wentz and Meissner, 2006).

In Section 2, we describe the algorithm in a more detailed way. In Section 3 we evaluate the application of the algorithm to MHS instead of AMSU-B data, which is necessary for extending the data set to cover recent years, performing a comparison with different in-situ data sources in Section 3.2. Then, we evaluate the new ice cloud filtering developed for the algorithm in Section 4, and finally give some conclusions in Section 5.

5 2 Retrieval algorithm

2.1 Data sources

The algorithm uses microwave radiometer satellite measurements from humidity sounders such as AMSU-B or MHS on board the NOAA (National Oceanic and Atmospheric Administration) 15 to 19 satellites and Eumetsat (European Organisation for the Exploitation of Meteorological Satellites) Metop-A, Metop-B and Metop-C satellites. The characteristics of each sensor can be found in Table 1, and the launch dates of each satellite in Table 2. Through this paper, when we refer to AMSU-B TWV, the brightness temperature data used for the retrieval is always from the sensor on NOAA-17, with the version from the Fundamental Climate Data Record (Ferraro and Meng, 2016), which provides an inter-satellite calibrated set of brightness temperatures as described in Ferraro (2016). When we refer to MHS TWV, the brightness temperature data are from NOAA-18, similarly sourced.

15 2.2 Radiative transfer equation

The algorithm starts from the formulation of the radiative transfer equation in the contracted form by Guissard and Sobiesky (1994) which describes the brightness temperature (T_B) measured by a space-borne radiometer as:

$$T_B(\theta) = m_p T_s - (T_0 - T_c)(1 - \epsilon_s)e^{-2\tau \sec \theta}, \quad (1)$$

where θ is the zenith angle, T_s and T_0 are the surface and air temperatures, respectively, T_c is the cosmic background emission, ϵ_s the surface emissivity, τ_0 the total opacity of the atmosphere in the vertical direction, and m_p a correction to take into account a non-isothermal atmosphere ($m_p = 1$ would be the isothermal case). The approach by Melsheimer and Heygster (2008), summarized in the following, assumes the ground to be approximated as a specular reflector, which should be good enough for remote sensing in the frequency range we are dealing with, according to Hewison and English (1999).

2.3 Retrieval for equal emissivity assumption

25 Note that the entire derivation of the final total water vapour retrieval equation from the radiative transfer equation is described in detail in the initial paper for the Antarctic by Miao et al. (2001) and the subsequent Arctic extension by Melsheimer and Heygster (2008). We summarize it here because the basic mechanism is necessary to understand the changes performed.

We start from microwave radiometer satellite measurements in three different channels i, j, k , such as mentioned in Section 2.1. We assume none of these three channels are saturated, i.e., the sensor is still sensitive to the whole atmospheric

column and ground. Additionally, we take the ground emissivity as equal in all three channels (as they see the same footprint, and the emissivity does not vary between the channels), while the water vapour absorption (mass absorption coefficient k) is different, with $k_i < k_j < k_k$. Then, the brightness temperature difference of two channels i, j can be expressed as:

$$\Delta T_{ij} \equiv T_{Bi} - T_{Bj} = (T_0 - T_c)(1 - \epsilon_s)(e^{-2\tau_i \sec \theta} - e^{-2\tau_j \sec \theta}) + b_{ij}, \quad (2)$$

5 where τ_i is the nadir opacity of the atmosphere at the frequency of channel i , and b_{ij} is a bias related to the term m_p for the channels i and j :

$$b_{ij} = T_s(m_{pi} - m_{pj}), \quad (3)$$

As shown in Melsheimer and Heygster (2008) – Appendix II, the bias can here be approximated as:

$$b_{ij} \approx \int_0^\infty \left[e^{-2\tau_i(z, \infty) \sec \theta} - e^{-2\tau_j(z, \infty) \sec \theta} \right] \frac{dT(z)}{dz} dz, \quad (4)$$

10 where $T(z)$ is the atmospheric temperature profile. Then we take the ratio of what we call compensated brightness temperature differences:

$$\eta_c \equiv \frac{\Delta T_{0ij}}{\Delta T_{0jk}} = \frac{\Delta T_{ij} - b_{ij}}{\Delta T_{jk} - b_{jk}} = \frac{e^{-2\tau_i \sec \theta} - e^{-2\tau_j \sec \theta}}{e^{-2\tau_j \sec \theta} - e^{-2\tau_k \sec \theta}}. \quad (5)$$

We can express the opacities τ_i as a sum of the atmospheric constituent contributions to them: water vapour (τ_i^w) and oxygen (τ_i^{oxygen}). The latter is negligible for AMSU-B channels near the water vapour line, so if we take water vapour mass absorption

15 coefficients k_i and TWV W :

$$\tau_i = \tau_i^w + \tau_i^{oxygen} \approx k_i W, \quad (6)$$

If we approximate the differences of exponentials by products in (5) and take logarithms, we get:

$$\ln(\eta_c) = B_0 + B_1 W \sec \theta + B_2 (W \sec \theta)^2 \quad (7)$$

The three constants B_0 , B_1 , and B_2 depend on the mass absorption coefficients for the different channels. The term quadratic in W can be neglected (Selbach, 2003; Miao et al., 2001) which leaves us with an equation linear in W that can then be solved to yield our retrieval equation:

$$W \sec \theta = C_0 + C_1 \ln(\eta_c) \quad (8)$$

where $C_0 = \frac{B_0}{B_1}$ and $C_1 = \frac{1}{B_1}$. They are determined empirically as calibration parameters from simulated brightness temperatures based on radiosonde profiles by a regression analysis, described in more detail below (section 2.6).

2.4 Extension of the retrieval

Normally, for TWV values above 7 kg/m^2 , saturation occurs at Channel 19 ($183.3 \pm 3 \text{ GHz}$). To extend the retrieval range above this threshold, another channel is required that is less sensitive to water vapour to take its place in the triplet. This means that a new set of assumptions has to be made about the surface emissivity influence. For AMSU-B, the next channel "in line" is the one at 89 GHz (Channel 16). Thus, the three channels i, j, k are now the AMSU-B Channels 16, 17 and 20 (89, 150 and $183.31 \pm 7 \text{ GHz}$). Because Channel 16 is so far from the other two, we can no longer assume that it has the same surface emissivity as the others. Therefore the retrieval equation needs to be re-derived with the changed premise: $\epsilon_i \neq \epsilon_j = \epsilon_k$. This leaves us with a similar looking retrieval equation:

$$W \sec \theta = C_0 + C_1 \ln(\eta'_c) \quad (9)$$

where η'_c is a modified ratio of compensated brightness temperatures:

$$\eta'_c \equiv \frac{r_j}{r_i} (\eta_c + C(\tau_j, \tau_k)) - C(\tau_j, \tau_k), \quad (10)$$

and $C(\tau_j, \tau_k)$ is defined as

$$C(\tau_j, \tau_k) = \frac{e^{-2\tau_j \sec \theta}}{e^{-2\tau_j \sec \theta} - e^{-2\tau_k \sec \theta}}, \quad (11)$$

Since now there is a dependence on emissivities ϵ_i , or, equivalently, on reflectivities $r_i = 1 - \epsilon_i$, the surface emissivity at 89 GHz needs to be examined. Ideally, the ratio of corresponding reflectivities would be taken for each footprint. However, that is not possible without knowing atmospheric conditions and surface temperature. As an approximation, the emissivity is parametrized, and fixed reflectivity ratios depending on surface types are obtained. This was done for sea ice in Melsheimer and Heygster (2008) and for open water surfaces in Scarlet et al. (2018). The upper limit of this extended retrieval is about 15 kg/m^2 . Here, we will use this extended retrieval only over sea ice.

2.5 The "sub-algorithms": regime selection

As described through Sections 2.3 and 2.4, three different channel triplets are used for the retrieval, depending on the water vapour amount and the saturation of channels; hence, there are three "sub-algorithms" or retrieval regimes. Each sub-algorithm reaches its upper retrieval limit when the channel which is most sensitive to water-vapour becomes saturated. In the original algorithm formulation by Melsheimer and Heygster (2008), the switch from one sub-algorithm to the next (always starting with the most sensitive one) is done only when the saturation condition,

$$T_{bj} - T_{bk} > 0 \quad (12)$$

is fulfilled. This means that for each satellite footprint, only one of the three sub-algorithms is finally used. As the sub-algorithms have been calibrated independently, the switch from one to the next can cause a jump in the retrieved value. A method avoiding this discontinuity in the retrieval values will be discussed further in the follow-on paper. Additionally, as the switch between regimes is done in the brightness temperature space, this does not correspond to a strict cut-off point in water vapour. In Table 3 we summarize the characteristics of each regime.

2.6 Bias and calibration parameters

Since we ordered the channels by the water vapour sensitivity ($\tau_i < \tau_j < \tau_k$), the difference of exponentials in ΔT_{0ij} and ΔT_{0jk} is negative. Therefore, the first term of the temperature difference increases with increased emissivity from negative values to 0 (reached when $\epsilon = 1$). η_c doesn't depend on ϵ , which cancels on the ratioing. In a plot with ΔT_{jk} as abscissa and ΔT_{ij} as ordinate, for constant W and varying ϵ , this is a straight line with slope $\eta_c(W)$, running through the bias points (b_{jk}, b_{ij}) . Since the biases depend only weakly on W and ϵ , all straight lines for different W run through almost the same point $F = (F_{jk}, F_{ij})$, which is called focal point by Miao et al. (2001) and Melsheimer and Heygster (2008). The focal point F is found by simulating brightness temperatures for a set of different ϵ , with different input atmospheric profiles (including W) from radiosonde data, and surface temperature taken as ground-level atmospheric temperature (which makes the small emissivity dependence of the biases vanish; see Melsheimer and Heygster (2008) - Appendix II). Having determined the focal point, the simulated brightness temperature differences and corresponding TWV values from the radiosonde profiles can be used to get the calibration parameters C_0 and C_1 . Thus, together with the two focal point coordinates F_{jk} and F_{ij} , there is a total of four calibration parameters in the retrieval equation which are derived by this regression. The specific values for each viewing angle and regime of AMSU-B sensor are found in Melsheimer and Heygster (2008) – Appendix III. For MHS, all these calibration parameters were recalculated and are shown in Appendix A.

2.7 Filtering ice cloud artefacts

The effect of ice clouds at the AMSU-B frequencies as studied in Sreerexha (2005) is known, and has been used for detecting tropical deep convection (Hong et al., 2005) and for an automated method for finding polar mesocyclones (Melsheimer et al., 2016). The latter method uses the sensitivity of retrieved TWV to convective clouds with high ice content as one of the main signatures of polar lows. In these cases, since cloud ice particles are strong scatterers in the used microwave range, the radiation from below the clouds is scattered strongly and hardly reaches the sensor, so that the AMSU-B retrieval is only sensitive to atmospheric water vapour above such clouds and retrieves erroneously low TWV. A procedure to recognize and screen such cases for the AMSU-B/MHS algorithm has been developed. Our approach for eliminating the affected TWV is to find connected areas – minimum of two pixels – of low TWV ($< 4 \text{ kg/m}^2$) smaller than 50 pixels which are surrounded by higher or non-retrieved values and remove them with a succession of morphology operations (Gonzalez and Woods, 2007), using the tools for Python described in van der Walt et al. (2014): First a dilation with a 7×7 square structural element, and then a closing with the same size structural element.

3 Evaluation of retrieval with MHS data

3.1 Comparison between MHS and AMSU-B based retrieval

As shown in Table 1, there are some frequency and polarization differences between AMSU-B and MHS sensors. According to the analysis in John et al. (2012), there are some non-negligible discrepancies between the brightness temperatures of AMSU-B

and MHS for the second and fifth channels (17 – 150 GHz – and 20 – 183.31 ± 7 GHz – for AMSU-B, respectively), due to the differences in frequency, while the differences in polarization seem not to be relevant. That raises the question of whether the TWV algorithm will perform equally when using MHS data as input, and, if that is not the case, which adaptation would be needed to ensure consistency of the retrieval results. First, we evaluate the performance for the retrieval as a whole by comparing the retrieved data of both algorithms in the overlap period of both sensors (2008-2009). Figure 1 shows two density plots for the overlap months of January (top) and July (bottom) of 2008-2009. The results of a least squares regression are shown in the figure as well. Both data sets show good agreement, with most of the points along the one-to-one line. However, we can observe some outliers with high MHS TWV and low, almost constant, AMSU-B TWV, and vice versa, specially striking during the month of July. They are likely caused by time differences of the satellite overpasses, and amount to only about 0.27% of the data, so they are not significant in the overall picture.

In Table 4, the fit statistics for all months are shown. The correlation ranges from 0.87 in June to 0.94 in September. The lowest slope (0.82 kg/m^2) is found in December, which may be related to the smaller than expected amount of data for this month compared to the coincidences in the other winter months. On the other hand, the slope is closest to 1.0 in May (0.91 kg/m^2). The intercept increases for the summer months (June, July, August) but is relatively small for the other months. The RMSD has a similar behaviour: we find higher values for the central months of the year, with a maximum of 2.25 kg/m^2 in August, coinciding with the increased number of outliers. Minimum is of 0.73 kg/m^2 in March. The bias is generally small (minimum of 0.04 kg/m^2 in March, maximum of 0.49 kg/m^2 in September), and positive except for May and June. In general, all parameters show lowest agreement in the summer months when the atmospheric variability is highest. However, we presume the strongest contribution to the low agreement in summer is due to the higher uncertainty and variability in the surface emission due to melt process and occurrence of melt ponds.

To check any possible influence from the surface type in the consistency of our retrievals, we have studied the TWV time series during 2008-2009 for MHS and AMSU-B over different surfaces: ice, land and open water. The location chosen for each study point is shown in Figure 2, with the surface classification used in the TWV retrieval for a day in early March 2008 (maximum ice extent) as background. Using the ice concentration provided by the ASI-algorithm (Spren et al., 2008), pixels with ice concentrations below 15% will be open water, while the ones with more than 80% will be considered ice. We show the monthly and yearly means of this time series for the four different locations in Figure 3. Note the lack of data for summer months over open water and ocean because of the limitations of the algorithm. All four time series show good agreement which confirms the consistency between our retrievals. The bias and RMSD are small for all four surface types (ice: $0.1 \pm 0.4 \text{ kg/m}^2$, open water: $0.03 \pm 0.15 \text{ kg/m}^2$, marginal ice zone: $0.2 \pm 0.7 \text{ kg/m}^2$, land: $0.12 \pm 0.19 \text{ kg/m}^2$), but slightly higher in two cases with ice surfaces, which agrees with the higher error of our method for higher water vapour values (extended regime).

3.2 Comparison with in-situ data sources

While TWV retrieved from AMSU-B has been validated with different data sources (Rinke et al., 2009; Palm et al., 2010; Buehler et al., 2012), the same cannot be said about the retrieval with MHS data. Therefore, we performe a comparison with TWV derived from radiosondes taken during the N-ICE21015 campaign from January to June 2015 onboard research vessel

Lance north of Svalbard (Hudson et al., 2017; Cohen et al., 2017). We select the MHS data as the mean of all the values in a 50 km radius around the location of each radiosonde. The resulting time series is shown in Figure 4. The first thing to note is that the MHS series ends at the start of June because, afterward, the water vapour values are too high for the retrieval. However, both data sets show good visual agreement, except that MHS is not able to capture some of the quasi periodic peaks in TWV from N-ICE2015 data set (seen roughly every two weeks in February and March). We have eliminated these nine outliers from the following analysis. The scatter plot of all overlapping points of both data sets – with the colour scale representing the month of the campaign – shown in Figure 5, confirms the good agreement.

Additionally, we used Global Positioning System (GPS) and radiosounding (RS) TWV observations during the common 2008-2009 period between the AMSU-B and MHS sensors to evaluate the satellite TWV retrieval. GPS and radiosonde TWV have been measured at the five coastal Arctic stations Alert, Eureka, Ny Ålesund, Resolute and Scorebysund, as shown in Figure 6. These datasets are part of a homogenized year time series. From the GPS data, 1-h average values of local integrated TWV have been computed each 6 hours. The radiosoundings have been performed once or twice per day at the selected sites (00:00 and 12:00 UTC). Further details about processing can be found in Negusini et al. (2016). As for the AMSU-B and MHS TWV values, we selected points fulfilling the data conditions of ± 1 h from the integrated GPS measurements (00:00, 06:00, 12:00, 18:00UTC) and found in a 50 km radius around the GPS/RS stations. The resulting AMSU-B, MHS, GPS and radiosonde time series in Figure 7 present generally consistent patterns and reasonable seasonal evolution, with drier winters and wetter summers. Overall, the datasets have worse agreement during the summer months, mainly due to “spikier” data, i.e. more extreme water vapour values. Due to this pronounced seasonal cycle, we separate the results between summer (April to September) and winter (October to March) in the following analysis. There seems to be a slight wet bias in summer for both satellite-derived TWV with respect to the other datasets.

Scatter plots comparing each satellite dataset with both radiosondes and GPS have been prepared for each season and station. As an example, Figure 8 shows the results for Alert. The correlation coefficients vary between 0.55 to 0.82, and the correlations in winter seems to be generally lower. We presume this is just a numerical effect because of the narrower data distribution. The RMSD, in contrast, is higher in summer (as seen in Figure 9). The only difference between both satellite-based retrievals seems to be a smaller number of coincident points between the MHS TWV and the radiosondes TWV (approximately half of the data points).

Figure 9 shows all fit parameters for the five stations, with separated results between summer and winter. There seems to be only little difference between the results from the two satellite-based retrievals, which corroborates our confidence in the MHS-based retrieval. Over the three quality indicating parameters RMSD, bias and correlation coefficient there is even a slight, but consistent advantage for the MHS based retrieval. The bias values are almost all negative, and smaller than the RMSD. In other words, the variability of our data is bigger than the systematic difference between the compared datasets. Additionally, RMSD is along usual values for TWV studies at high latitudes (as seen in Palm et al. (2010) for Ny Ålesund and in Buehler et al. (2012) for Kiruna), which reassures us on the quality of satellite-based PW retrievals. The higher RMSD values in the Arctic summer correlate with the higher disagreement seen at high PW values over 7 kg/m^2 for all methods in Figure 8 (left, top and bottom). Such disagreement can be explained by the change in sub-algorithms as explained in Section 2.5.

4 Evaluation of changes/improvements in the retrieval: Filtering ice cloud artefacts

Figure 10 shows daily averaged TWV maps – with the cloud mask (Section 2.7) already applied – for the AMSU-B/MHS algorithm (top and centre), as well as from a different data product based on AMSR-E observations (Wentz and Meissner, 2006) over open ocean (bottom) in winter (left) and summer (right). The days chosen to represent each season (6 January and 6 July, 2008, respectively) show how a typical retrieval looks like for the respective season. The first thing to notice is the difference in spatial coverage of AMSU-B TWV between winter and summer. In summer, AMSU-B/MHS retrieval is restricted to the drier regions, mostly over sea ice and Greenland (the upper limit of the retrieval is usually about 15 kg/m^2 for sea ice surfaces). In winter, the retrieval is possible over most of the land, open water areas and sea ice. Meanwhile, there is no significant coverage variation between seasons for the AMSR-E retrieval: most open water areas are covered. In consequence, the area covered by both methods is smaller in summer, as we can note in the map illustrating the regional coverage – for the same days – of both algorithms in Figure 11 (orange area shows joint coverage). Still, TWV is retrieved in most of the Arctic in both seasons. Another consequence is that in summer the overlap area is small. In this particular example of Figure 11, there is no overlap between both datasets.

To visualize the areas affected by the ice cloud mask, Figure 12 shows different areas of interest before (left) and after (right) masking, for different days spaced evenly throughout 2008 (each three months approximately: 6th of January, 2nd of April, 6th of July and 14th of October). These areas have been chosen as representative cases for the season. Most features are removed, but there are still some small areas of low values of TWV (such as the retrieved regions in the land around 70°W , 62°N Figure 12 (October, bottom right)). Note that these incorrectly retrieved areas are surrounded by grey values which represent water vapour too high to be retrieved with the AMSU-B method (about $>7 \text{ kg/m}^2$ over ocean or land surfaces).

To show the overall effectiveness of the ice cloud mask, we have compiled all the overlapping retrieved TWV from AMSU-B and AMSR-E for the complete months of January (top) and July (bottom) from 2006 to 2008, shown in Figure 13. Before filtering for ice cloud artifacts (left), there is a big cluster of data with high AMSR-E values for relatively low AMSU-B values. Those correspond to the values affected by convective clouds with high ice content. Note that the overlap area between AMSR-E and AMSU-B is small (Figure 11) and therefore cloud artifacts make up a large fraction of the overlap data points, particularly in summer. After filtering (right) the AMSU-B retrieval, they are gone. Additionally, the fit performed improves significantly, with the correlation reaching 0.6 in summer and the slope getting much closer to one in winter (0.95, as compared to 0.3). Note also the jump in density of the retrieved TWV values caused by switching between sub-algorithms mentioned above (Section 2.5), most notably near 6 kg/m^2 (Figure 13).

5 Conclusions

We provide an updated version of the TWV retrieval algorithm that originally uses as input microwave humidity sounder data from AMSU-B. The updated algorithm, can now also use data from MHS, the successor instrument of AMSU-B, and contains a filter for artifacts caused by convective clouds with high cloud ice content. The improved retrieval performs better when compared to another satellite product and to in situ data.

We have investigated the impact of differences between AMSU-B and MHS on the retrieved TWV and have found the differences to be negligible. This means that a consistent continuous data set for the years 1999 until now can be generated from combining AMSU-B and MHS data. Additionally, the MHS-based TWV data have been compared with radiosonde data from the N-ICE2015 campaign, and the results show good performance for MHS TWV. Both satellite-derived TWV have
5 been compared against GPS and radiosonde data for five Arctic coastal stations during 2008 and 2009, and the results are satisfactory.

The filter for ice cloud artifacts performs well as shown by comparison with data from the AMSR-E based algorithm that works over open water. A remaining issue are the jumps of retrieved TWV values between the different retrieval regimes. This can, however, in principle be mitigated by comparing root mean square differences and bias for adjacent TWV regimes,
10 and choosing an optimal regime, i.e., channel combination, for the range of the water vapour column. Where regimes overlap, weighted averages can smooth the transition.

The algorithm described here has an upper TWV limit that restricts retrieval in summer to the central Arctic and Greenland. However, when combining the TWV data retrieved by the algorithm described here with TWV retrieved over open ocean from AMSR-E and AMSR2 – the product by Remote Sensing Systems (RSS) (Wentz and Meissner, 2006) – a nearly complete
15 coverage of the whole Arctic year-round is possible, starting in 2000, which is the overall goal of future work.

Appendix A

The following tables list the calibration parameters C_0 , C_1 , F_{jk} , and F_{ij} for the TWV retrieval algorithm for the Arctic and – for the sake of completeness – the Antarctic, for 15 viewing angles that span the range of the viewing angles of MHS, calculated in the same way as the parameters for AMSU-B-based retrieval by Melsheimer and Heygster (2008). The retrieval equation is,
20 from (5) and (8):

$$W \sec \theta = C_0 + C_1 \ln \left[\frac{\Delta T_{ij} - F_{ij}}{\Delta T_{jk} - F_{jk}} \right], \quad (\text{A1})$$

where $\Delta T_{ij} = T_{b,i} - T_{b,j}$, the MHS channels i, j, k are

– 5 (190.31 GHz), 4 (183.31 ± 3 GHz), 3 (183.31 ± 1 GHz) for the low-TWV algorithm,

– 2 (157 GHz), 5 (190.31 GHz), 4 (183.31 ± 3 GHz) for the mid-TWV algorithm,

25 and, from equations (10) and (9),

$$W \sec \theta = C_0 + C_1 \ln \left[\frac{r_j}{r_i} \left(\frac{\Delta T_{ij} - F_{ij}}{\Delta T_{jk} - F_{jk}} + 1.1 \right) - 1.1 \right] \quad (\text{A2})$$

where i, j, k are 1 (89.9 GHz), 2 (157 GHz), 5 (190.31 GHz) for the extended algorithm.

The calibration parameters for the Arctic (Tables A1–A3) were derived using radiosonde data from those World Meteorological Organization (WMO) stations in the Arctic that are located on the coast or on islands (29 stations), from the years 1996
30 to 2002, which amounts to about 27000 radiosonde profiles.

Competing interests. No competing interests are present

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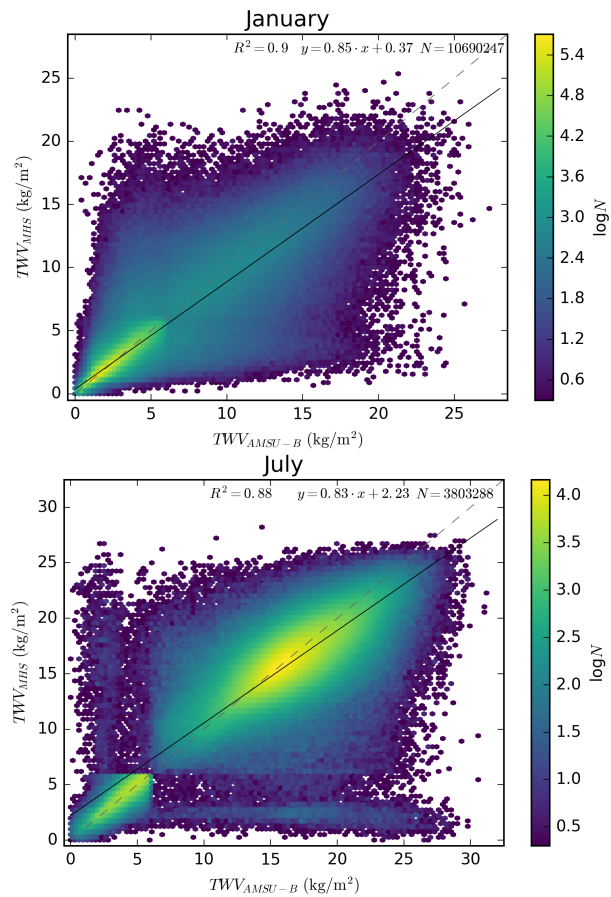


Figure 1. Density plot and fit for MHS TWV versus AMSU-B TWV retrievals for all the coincident points in January (top) and July (bottom), 2008-2010. The dashed line is the one-to-one line, and the black line corresponds to the linear fit of the data.

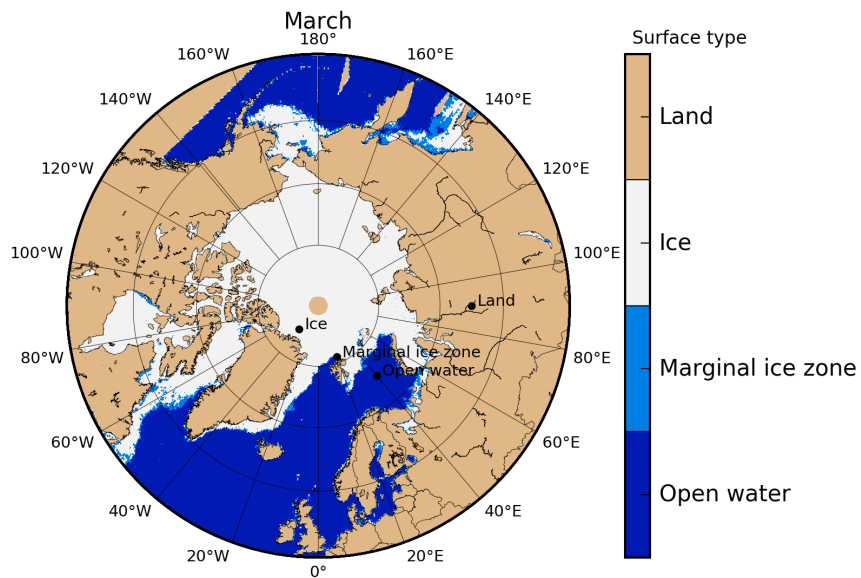


Figure 2. In black, location of the points chosen for the surface characterisation study for TWV. As background, the surface classification used in the TWV algorithm, obtained from ASI algorithm ice concentration (Spreen et al., 2008) for a typical day in March (6.03.2008).

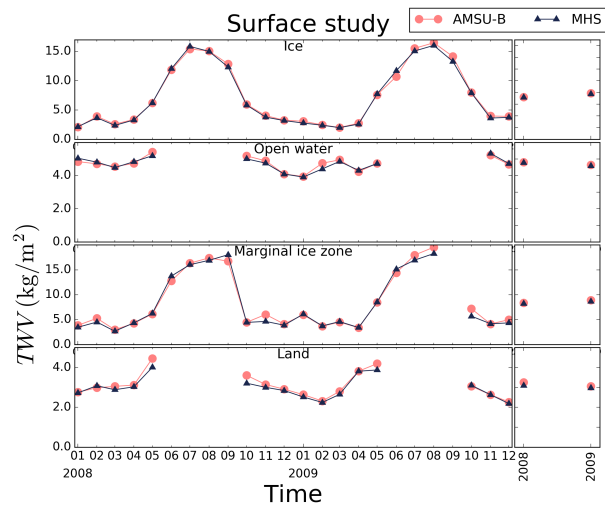


Figure 3. Monthly and yearly means for 2008 and 2009 of the AMSU-B (pink circles) and MHS (blue triangles). TWV retrieval over the locations shown in Figure 2.

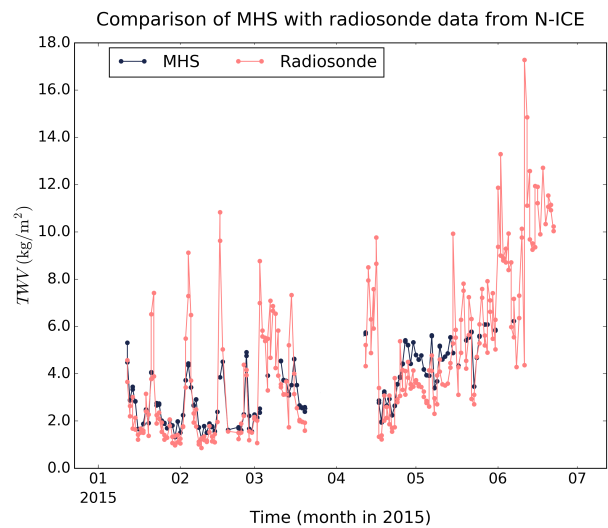


Figure 4. Time series of coincident MHS TWV data (blue symbols) and TWV from radiosondes (red symbols) during the N-ICE campaign.

Comparison of MHS with radiosonde data from N-ICE

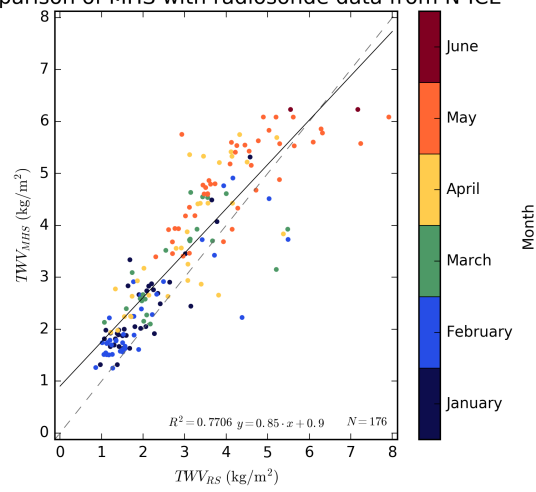


Figure 5. Scatter plot and fit for MHS TWV versus radiosonde TWV retrievals for all coincident points during the N-ICE campaign. The colour scale shows the month where the data point comes from; dashed line: one-to-one lines, solid line: linear regression.

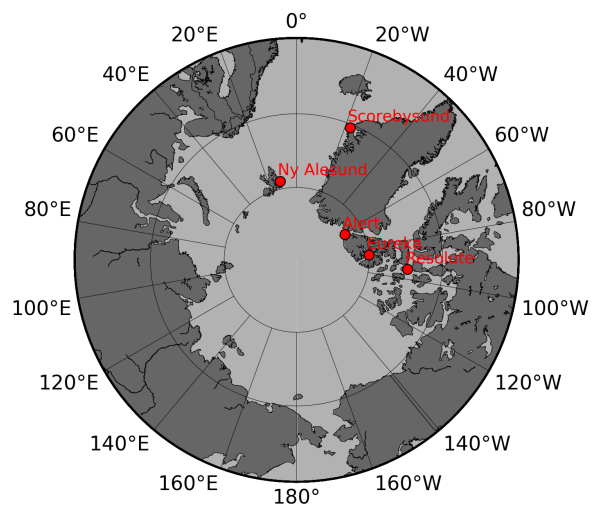


Figure 6. Location of the radiosonde and GPS stations.

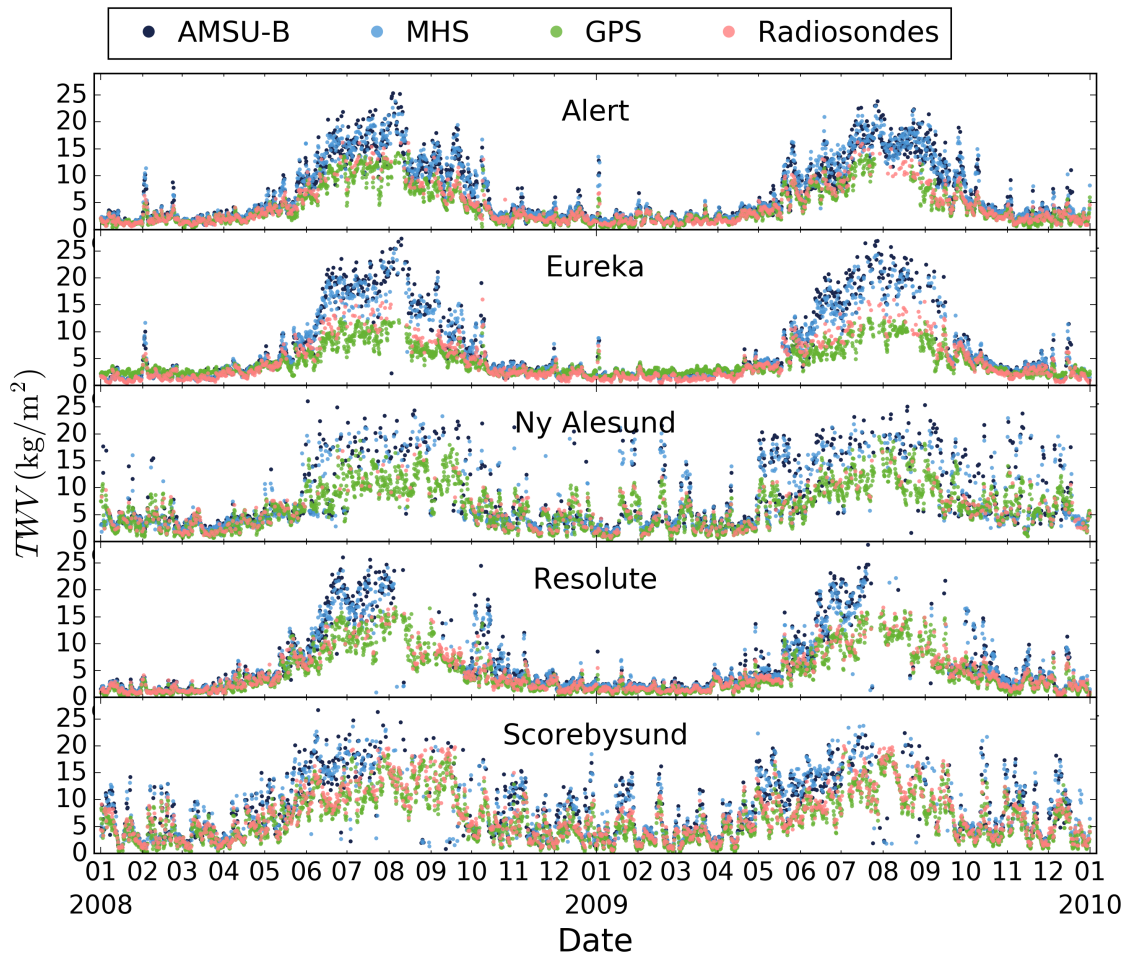


Figure 7. Time series of AMSU-B (dark blue), MHS (light blue), GPS (green) and radiosonde (salmon) TWV retrievals during 2008 and 2009.

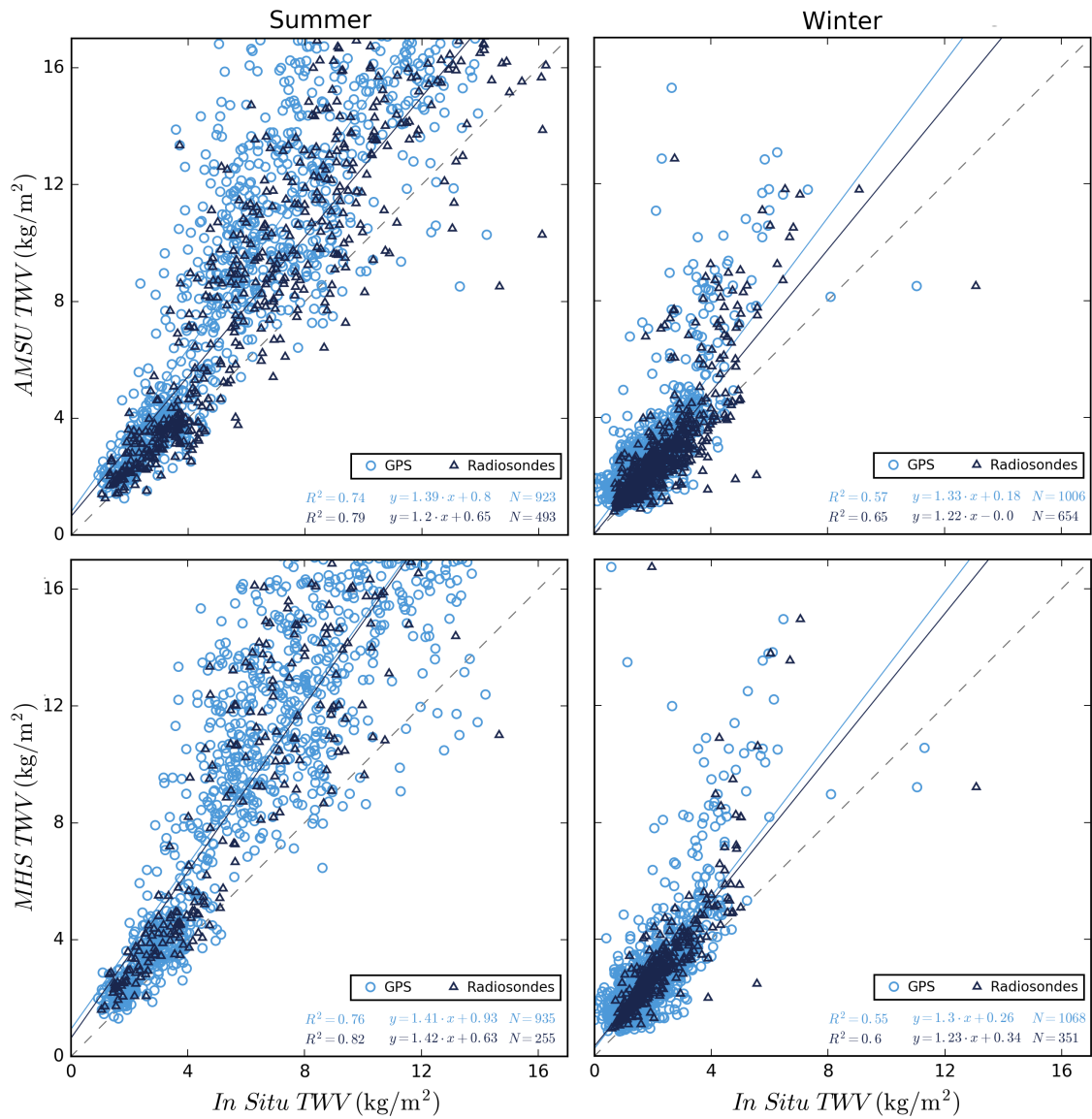


Figure 8. Scatter plots and fits for AMSU-B (top) and MHS (bottom) TWV retrievals versus GPS (light blue) and radiosondes (dark blue) TWV retrievals for all coincident points during summer (left) and winter (right) of 2008 and 2009 in the Alert station. The solid lines in light and dark blue show the linear regressions for GPS and radiosondes in each case, while the dashed lines are the identity line

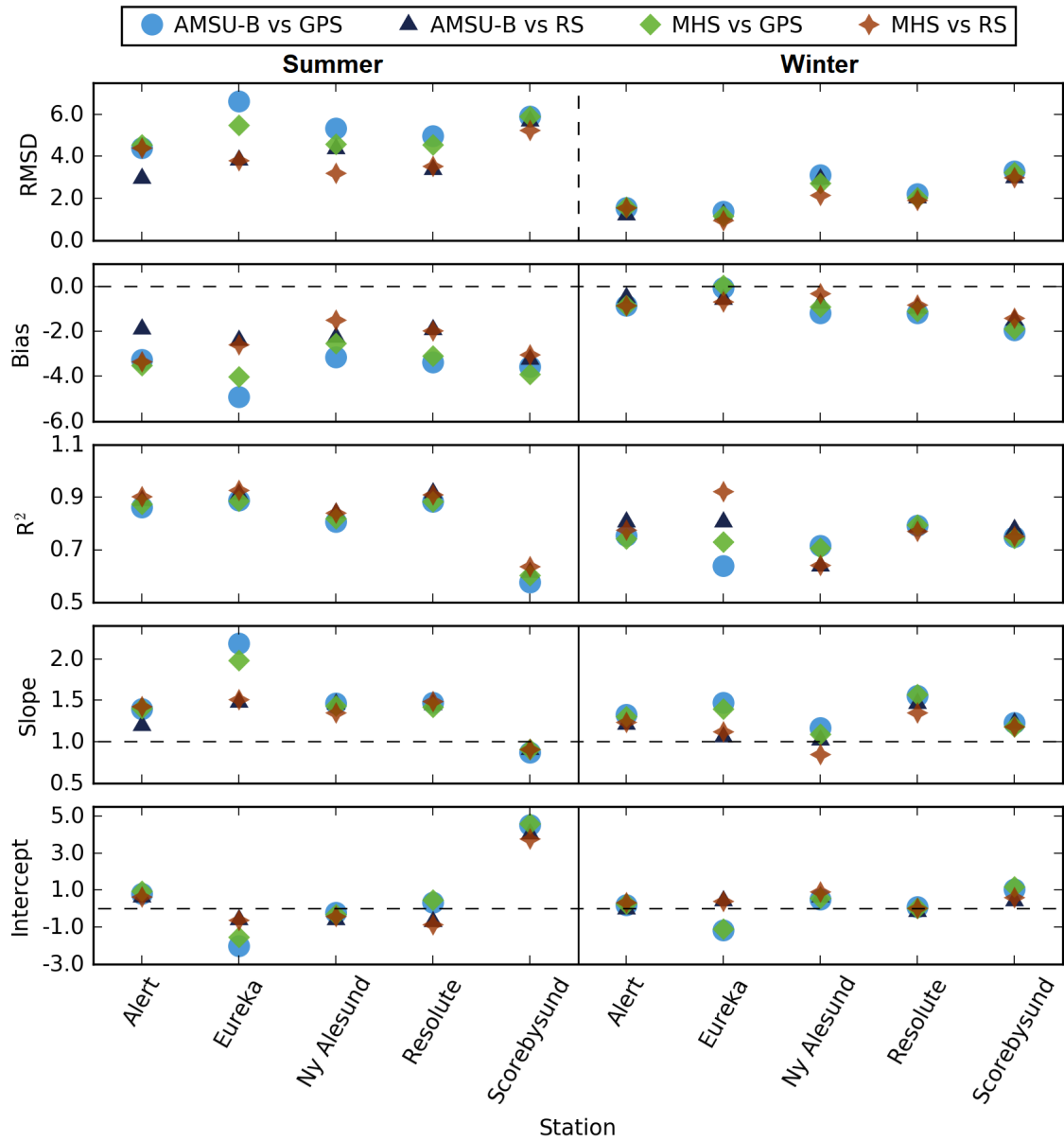


Figure 9. Values of fit parameters for summer (left) and winter (right): RMSD, bias, correlation coefficient R^2 , slope and intercept of regression line for MHS and AMSU-B TWV retrievals versus radiosonde and GPS TWV retrievals. RMSD, bias and intercept are in kg/m^2 , slope and R^2 are absolute numbers.

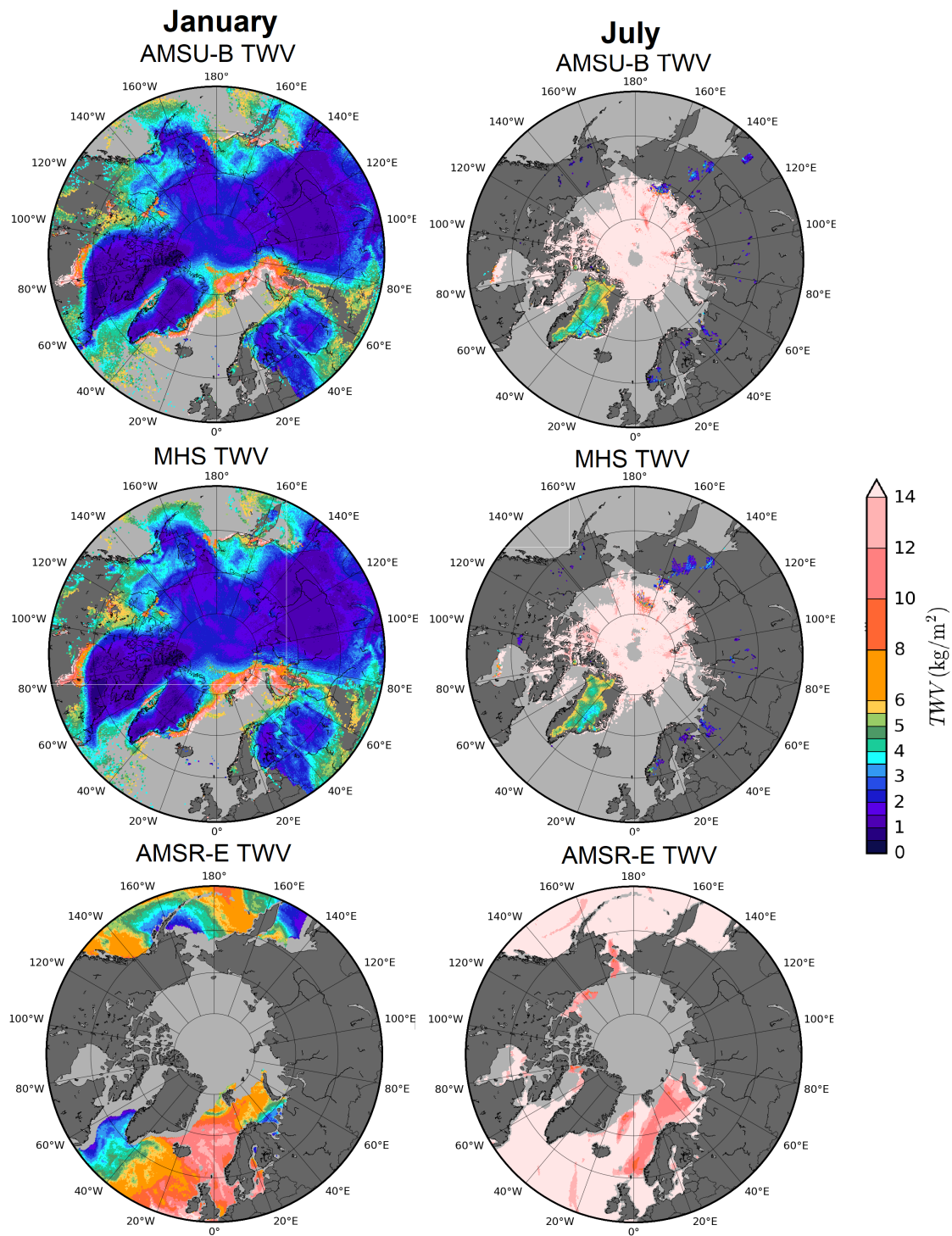


Figure 10. AMSU-B (top), MHS (centre) and AMSR-E (bottom) TWV retrievals for (left) winter (6 January, 2008), and (right) summer (6 July 2008)

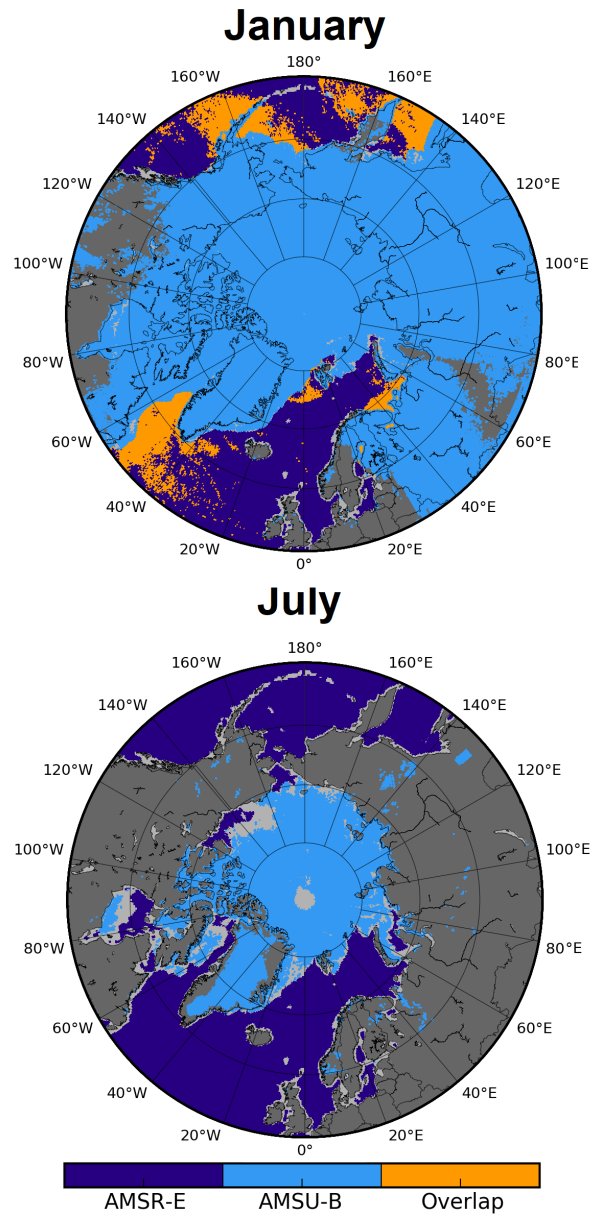


Figure 11. Coverage and overlap area of the merged AMSU-B and AMSR-E retrieval for (top) winter (6 January, 2008), and (bottom) summer (6 July, 2008). Note that there is no overlap between retrievals (orange) for the summer case presented.

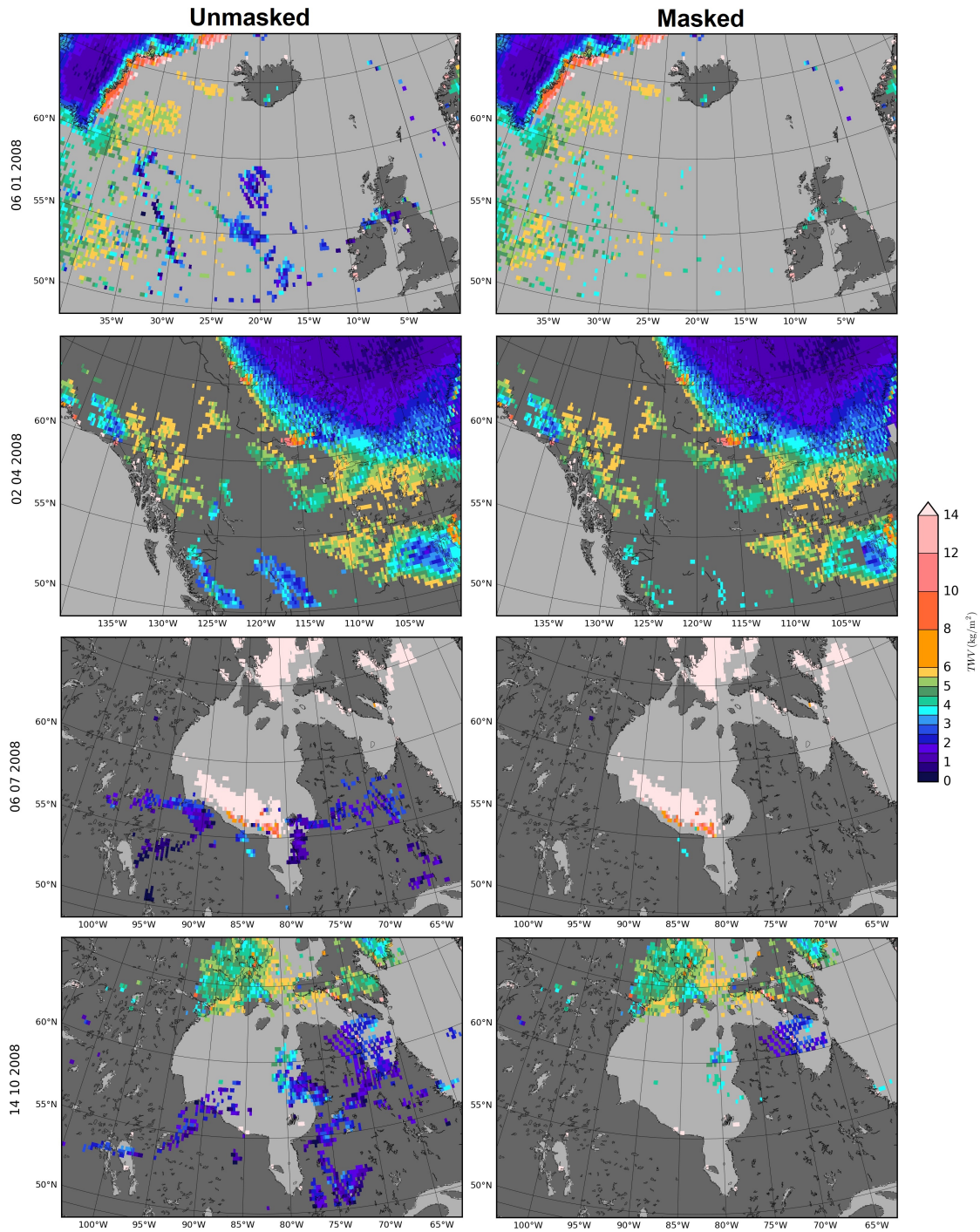


Figure 12. Unmasked (left) and masked (right) AMSU-B TWV retrieval for different showcased areas of four days through 2008: 6 January (top), 2 April (middle up), 6 July (middle down) and 14 October (bottom). Please note the different location in each case.

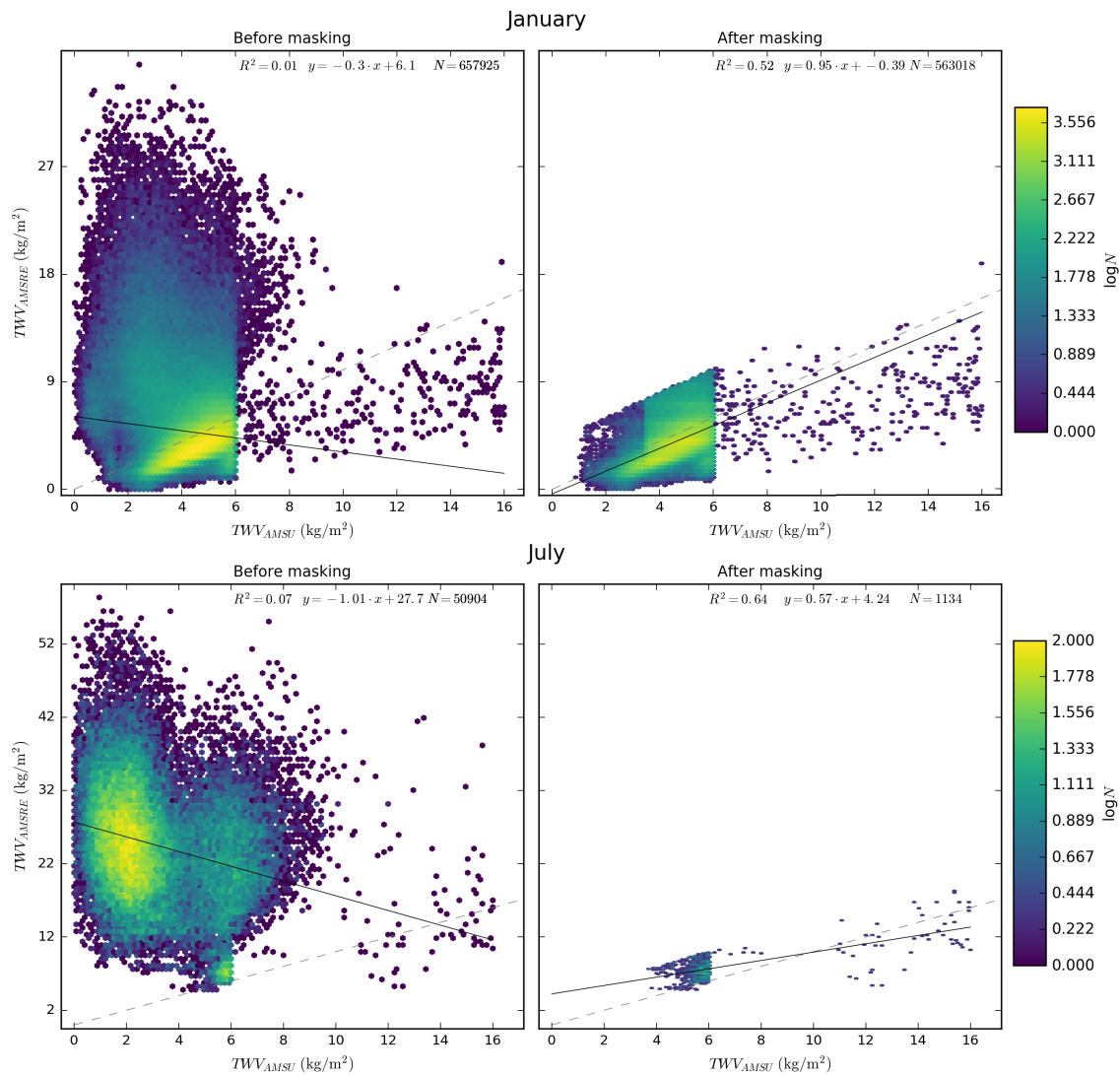


Figure 13. Density plot and fit for AMSR-E TWV versus AMSU-B TWV retrievals for all the coincident points in January (top) and July (bottom) from 2006 to 2008, before (left) and after (right) filtering AMSU-B retrieval for ice cloud artifacts, with a fit (black solid line) for the data clusters over the 1-1 line (dashed grey).

Table 1. Frequency and polarization details for each channel of AMSU-B and MHS sensor

AMSU-B			MHS		
Channel	Frequency (GHz)	Polarisation	Channel	Frequency (GHz)	Polarisation
16	89.9 ± 0.9	Vertical	1	89.9	Vertical
17	150.0 ± 0.9	Vertical	2	157.0	Vertical
18	183.31 ± 1	Vertical	3	183.31 ± 1	Horizontal
19	183.31 ± 3	Vertical	4	183.31 ± 3	Horizontal
20	183.31 ± 7	Vertical	5	190.311	Vertical

Table 2. Humidity Sounders in orbit with platforms, launch year and approximate equator crossing times (ECT) [NOAA]

Platform	Sensor	Launch year	ECT
NOAA15	AMSU-B	1999	07:00
NOAA16	AMSU-B	2000	21:00
NOAA17	AMSU-B	2002	07:00
NOAA18	MHS	2005	20:00
NOAA19	MHS	2009	20:00
MetOp-A	MHS	2006	9:30
MetOp-B	MHS	2012	9:30
MetOp-C	MHS	2018	9:30

Table 3. Characteristics of the different sub-algorithms of the AMSU-B/MHS TWV retrieval. The channel combination is described with AMSU-B frequencies, the MHS retrieval uses the corresponding ones

Sub-algorithm	Chanel combination			Operating surface	Approximate limit TWV (kg/m²)
Low	183.31 ± 7	183.31 ± 3	183.31 ± 1	Sea ice, ocean, land	1.5
Middle	183.31 ± 7	183.31 ± 3	150	Sea ice, ocean, land	7
Extended	183.31 ± 7	150	89	Sea ice	15

Table 4. Parameters for linear regression for monthly MHS and AMSU-B intercomparison

Month	R^2	Slope	Intercept	RMSD	Bias	Number of points
January	0.90	0.85	0.37	0.97	0.06	10691385
February	0.89	0.84	0.38	0.87	0.05	9858305
March	0.90	0.87	0.31	0.73	0.04	10389349
April	0.90	0.88	0.40	1.02	0.06	8592621
May	0.91	0.91	0.61	1.59	-0.02	6087842
June	0.87	0.84	2.33	2.25	-0.38	4741678
July	0.88	0.83	2.23	2.18	0.38	3803287
August	0.92	0.88	1.43	2.07	0.35	3272951
September	0.94	0.89	0.83	1.77	0.49	3630497
October	0.93	0.86	0.67	1.55	0.19	6000153
November	0.90	0.85	0.53	1.20	0.06	8610697
December	0.88	0.82	0.50	1.24	0.12	7723324

Table A1. Calibration parameters, Arctic, low-TWV algorithm

θ	C_0 [kg/m ²]	C_1 [kg/m ²]	$F_{4,3}^L$ [K]	$F_{5,4}^L$ [K]
1.667°	0.619	1.05	4.86	4.43
5.000°	0.619	1.05	4.87	4.45
8.333°	0.618	1.05	4.90	4.50
11.667°	0.617	1.05	4.94	4.58
15.000°	0.615	1.05	4.99	4.68
18.333°	0.613	1.05	5.06	4.81
21.667°	0.609	1.05	5.14	4.97
25.000°	0.606	1.04	5.23	5.16
28.333°	0.601	1.04	5.32	5.36
31.667°	0.598	1.02	5.31	5.41
35.000°	0.597	1.00	5.25	5.36
38.333°	0.602	0.96	5.01	4.96
41.667°	0.603	0.92	4.76	4.50
45.000°	0.607	0.87	4.43	3.85
48.333°	0.607	0.80	4.12	3.27

Table A2. Calibration parameters, Arctic, mid-TWV algorithm

θ	C_0 [kg/m ²]	C_1 [kg/m ²]	$F_{5,4}^M$ [K]	$F_{2,5}^M$ [K]
1.667°	1.63	2.64	6.56	5.74
5.000°	1.63	2.64	6.55	5.75
8.333°	1.62	2.64	6.54	5.75
11.667°	1.61	2.63	6.52	5.75
15.000°	1.60	2.62	6.50	5.77
18.333°	1.59	2.61	6.46	5.77
21.667°	1.57	2.59	6.43	5.79
25.000°	1.55	2.57	6.38	5.82
28.333°	1.53	2.54	6.34	5.86
31.667°	1.50	2.50	6.25	5.86
35.000°	1.46	2.46	6.18	5.90
38.333°	1.42	2.40	6.09	5.95
41.667°	1.37	2.33	5.99	6.01
45.000°	1.30	2.24	5.83	6.03
48.333°	1.22	2.11	5.65	6.08

Table A3. Calibration parameters, Arctic, extended algorithm

θ	C_0 [kg/m ²]	C_1 [kg/m ²]	$F_{2,5}^E$ [K]	$F_{1,2}^E$ [K]
1.667°	14.4	7.45	6.52	0.74
5.000°	14.4	7.47	6.55	0.74
8.333°	14.4	7.50	6.61	0.75
11.667°	14.4	7.56	6.71	0.77
15.000°	14.4	7.63	6.84	0.80
18.333°	14.4	7.73	7.00	0.83
21.667°	14.5	7.83	7.20	0.87
25.000°	14.5	7.97	7.44	0.93
28.333°	14.5	8.11	7.72	1.00
31.667°	14.5	8.26	8.04	1.08
35.000°	14.5	8.43	8.41	1.19
38.333°	14.4	8.60	8.83	1.33
41.667°	14.2	8.76	9.30	1.50
45.000°	13.9	8.90	9.83	1.74
48.333°	13.4	8.99	10.4	2.04