

# Response to comments

Synergistic radar and radiometer retrievals of ice hydrometeors

# 1 Comments from referee 1

## 1.1 General comments

### Reviewer comment 1

The revised manuscript is vastly improved and my concerns have mostly been satisfied in these revisions. I agree that recasting the measurements as airborne is an appropriate way to simplify the radiative transfer assumptions and demonstrate the concept. My second comment, about the inclusion of forward model error, is not directly addressed though changes in the methods but I do agree with the author response that such an error would be scene-dependent and therefore not trivial. However, I think the appropriate caveats have been mentioned in the interpretation of results so as to not interpret the combined or radiometer-only methods as being poor compared to the radar due to the higher chi-squared(y) - in fact, it is noted that the radar is instead overfitting the measurements.

I only found a few instances of inconsistent nomenclature (e.g., capitalization of GEM on line 252) that should be corrected prior to publication.

### Author response

We would like to thank the auto for pointing out the inconsistencies in nomenclature, which we will correct in the revised version of the manuscript.

### Changes in manuscript

Changes starting in line 230:

GEM Graupel, ~~Gem~~GEM Hail and GEM Cloud Ice are more efficient.

## 2 Comments from referee 2

### 2.1 General comments

#### Reviewer comment 1

L 106: that cloud ice particles are small and abundant while snow particles are large and much rare is nature not the model. So I would recommend to change the sentence: " An important characteristic can be identified here.."

#### Author response

The proposed change will be adopted in the revised manuscript.

#### Changes in manuscript

##### Changes starting in line 106:

An important characteristic ~~of the model~~ can be identified here, which will help to better understand the retrieval results presented later: Cloud ice ~~in the model~~ is characterized by high particle number concentrations and small particle sizes, whereas snow has lower number concentrations and larger particles.

#### Reviewer comment 2

L222-223: The two sentences are a bit contradictory: Just say M1 results will be shown for certain aspects only

#### Author response

The proposed changes will be adopted in the revised manuscript.

#### Changes in manuscript

##### Changes starting in line 220:

In addition to a two-moment radar-only retrieval, also a one-moment version (M1), in which only the  $D_m$  parameter is retrieved has been tested. ~~For completeness, retrieval results for IWC will be reported also for the M1 version. However, to allow for better comparison with the combined and passive-only retrieval, for the~~

~~remaining results only the two-moment version is considered~~ However, results of this version will be shown only for the comparison of IWC retrieval errors.

### Reviewer comment 3

L247 WC is used as abbreviation before being defined

### Author response

The corresponding paragraph will be rewritten taking into account the referees comment.

### Changes in manuscript

#### Changes starting in line 247:

Mass backscattering ~~efficiency and attenuation coefficient~~ and attenuation coefficients are defined as the ratio of the corresponding ~~cross-section~~ backscattering or attenuation coefficient  $\sigma$  and the bulk water content  $\div$  WC:

$$Q = \frac{\sigma}{WC}. \quad (2.1)$$

### Reviewer comment 4

Figure 5 caption: say that this is an ice cloud

### Author response

The caption of Fig. 5 will be changed in the revised manuscript as shown below.

### Changes in manuscript

#### Changes starting in line 284:

Simulated observations of a homogeneous, 5 km thick ice cloud ~~layer~~ centered at 10 km with varying water content  $m$  and mass-weighted mean diameter  $D_m$ . The panels display the maximum radar reflectivity ( $\text{dBZ}_{\text{max}}$ ) overlaid onto the cloud signal ( $\Delta T_B$ ) measured by selected radiometer channels of the MWI (first row) and ICI radiometers (second row).

### Reviewer comment 5

I really like Fig. 12 It shows the clear contribution in DOF from the different parameters. Just as a quick idea which does not necessaryl need to be implemented but might strengthen the discussion on LCWC: Could you look at the ratio of the the combined DOF and the sum of the the single retrievals. This could help to explain that the



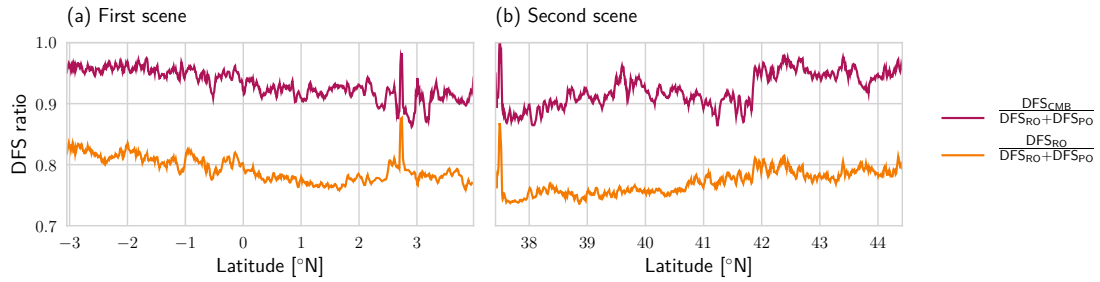


Figure 2.1: Ratios of the DFS of the combined retrieval ( $DFS_{CMB}$ ) and the sum of the DFS or the single-instrument retrievals ( $DFS_{RO} + DFS_{PO}$ ) for the two test scenes.

ice information is in both radar and passiv and therefore in the combined retrieval the microwave information content for ice is not needed (ice contribution is determined) and therefore the information content is transfered to LCWC is transfer. This argumention in 4.2.3 is currently not too strong.

### Author response

As suggested by the referee, we have produced a plot of the ratio of the DFS of the combined retrieval and the sum of DFS of the single-instrument retrievals. Since this plot indeed strengthens our arguments on the combined information content on LCWC, we have extended the discussion in Sect. 4.2.3 as shown below.

### Changes in manuscript

#### Changes starting in line 398:

In order to allow a more detailed analysis of the complementarity of the information in the passive and active observations, Fig. 2.1 displays the ratio of the DFS of the combined retrieval and the sum of the DFS in the radar- and passive-only retrievals. Comparison with the information content provided by the radar-only observations confirms that the active and passive observations consistently provide a fairly high amount of complementary information across both scenes.

#### Changes starting in line 527:

This conclusion is supported by the information content analysis in Fig. 12 ~~which shows that the passive observations provide some information on LCWC and that this is increased slightly for the combined retrieval.~~ and Fig. 13. In particular, the DFS ratio of the combined retrieval shows a distinct increase around 42 ° N, where the scene contains non-precipitating mixed-phase clouds.

This coincides with a slight increase in information content on LCWC in the combined compared to the passive-only retrieval show in Fig. 12.

#### **Reviewer comment 6**

L548: "..was able TO reproduce..

#### **Author response**

The missing word will be added to the revised manuscript.

#### **Changes in manuscript**

##### **Changes starting in line 548:**

Moreover, the combined retrieval showed clear sensitivity to particle number concentrations and was able to reproduce their vertical structure in regions where the cloud composition ...

#### **Reviewer comment 6**

Table 3 caption - give symbol  $l_q$  for correlation length

#### **Author response**

The caption of Table 3 will be corrected in the revised manuscript, as shown below.

#### **Changes in manuscript**

##### **Changes starting in line 218:**

A priori uncertainties  $\sigma_a$  and correlation lengths  $l_q$  used in the retrieval.

## 3 Comments from referee 3

We thank the referee for, again, identifying a number of mistakes in the manuscript. In some cases we misunderstood the comments in the previous review, but we also simply failed to implement a correction in one case. That said, co-authors (including the senior ones) read the complete revised manuscript but apparently all focused on the textual changes and the remaining problems went unnoticed. This is a good lesson for the future, that the co-authors should focus on checking different aspects of the manuscript. However, we stress that the mistakes only affect the presentation, in no case we have found any problems in the actual results.

The referee requires a major revision, but exactly why is not obvious. Our impression is that the referee would like that the study addressed different questions, and this is the main reason for his overall judgement. We would like to point out that it is our scientific freedom to decide on the focus of the study (note point three of "General obligations for referees", AMT (2020)).

In any case, the recommendation of a major revision stands in strong contrast to the opinion of the other two referees ( who mark excellent or good for all three judgement categories). We also note that the referee, both in the earlier review and this one, only give marginal credit to the original contributions of the study. To mention only the most obvious, the synergy between a cloud radar and a sub-millimetre radiometer is largely uncharted territory. The only similar journal articles on the subject we have found are the ones of Evans et al. (2005) and Jiang et al. (2019). The scope of our study is most similar to one of Jiang et al. (2019) and our study clearly provides both more quantitative results and a more direct analysis of the nature of the synergy.

### 3.1 General comments

#### Reviewer comment 1

The abstract from line 13 onwards is way too generic. There is not a single statement there that the reader can remember as specific for this work.

#### Author response

In an effort to improve the abstract we will introduce the following changes in the revised manuscript.

#### Changes in manuscript

### Changes starting in line 12:

retrieval results is assessed for all retrieval implementations. Although they show greater sensitivity to the assumed particle shape, the synergistic ~~retrieval shows~~ observations can better constrain the microphysics of the cloud, which decreases uncertainties in retrieved ice water content and improves the retrieval of particle number concentrations. Our results also indicate improved sensitivity to liquid ~~water in both warm and supercooled clouds~~ cloud water content for the synergistic configuration compared to a passive-only setup. The results of this study ~~clearly demonstrate the potential of the combined observations to constrain the microphysical properties of ice hydrometeors, which can help to reduce errors in retrieved profiles of mass and number densities~~ synergistic sensor configuration to improve retrievals of frozen hydrometeors. The developed synergistic retrieval algorithm can be applied with only minor modifications to suitable airborne observations from sub-millimeter radiometers such as the International Sub-Millimetre Airborne Radiometer.

### Reviewer comment 2

“Microwave sensors employ wavelengths ranging down to about 1 mm. ... At the same time, they provide the advantage of penetrating even thick clouds.” Well if this may be true for wavelength in the cm-region is certainly not true for frequency in the G-band for instance. What are “thick ice clouds”?

### Author response

We agree with the reviewer here that some of the terminology applied here can be improved. We remain convinced, however, that the general statement made in this paragraph, i.e. that microwave sensors can sense only comparably large ice particles while optical and IR sensors can sense also small ice particles, is true and relevant to put the study in context. We therefore propose to reformulate the paragraph as presented below.

### Changes in manuscript

#### Changes starting in line 29:

Current operational observation systems used to study clouds can be divided into two groups by virtue of their observing frequency and ~~their~~ corresponding capabilities and limitations. Microwave sensors employ comparably long wavelengths ranging down to about 1 mm. ~~Compared to the~~ Since these wavelengths are large compared to the typical sizes of ice particles, ~~the wavelengths are very long and therefore sensitive only to very large ice particles. At the same time, they provide in a cloud,~~ microwave sensors are most sensitive to the ~~advantage of penetrating even thick clouds~~ largest particles and do not provide any sensitivity to the small particles in the cloud. Optical and infrared sensors use radiation with wavelengths from around

15  $\mu\text{m}$  down to several hundred nano meters. ~~Although these~~ These relatively short wavelengths make them sensitive ~~to also to the~~ small ice particles, ~~their signal saturates for thick clouds, which makes them insensitive to the ice mass further down the line of sight.~~ ~~Although radars and lidars allow detection of lower ice water contents in the cloud.~~ The comparably low sensitivity of microwave sensors to small ice particles allows them to sense the larger, potentially precipitating, particles typically located at the center and base of a cloud, which cannot be sensed at infrared and optical wave lengths due to saturation of the signal.

### Reviewer comment 3

“Compared to the sizes of ice particles, the wavelengths are very long and therefore sensitive only to very large ice particles.”, again this is way too generic (what is very large?), it seems to give the idea that radars (even cloud radars) are not sensitive to 100-200 micron size particles, which is erroneous (see your Fig.5!)

### Author response

See answer to General comment 2.

### Reviewer comment 4

“Although radars and lidars allow detection of lower ice water contents than their passive counterparts, they are ultimately limited by the same principles.”

I am not sure what the authors are alluding to here. Radars in the G-band are now a reality (e.g. see recent work by Roy et al.) and the technology for active systems for even higher frequencies (>300 GHz) has already been demonstrated. Anyhow if a radar cannot penetrate a certain cloud the radiometer at the same frequency will suffer from the same issue; actually the radar via PIA technique can provide estimates of optical thicknesses up to 10 and more (where the radiometers are already saturated).

### Author response

It seems the referee has misunderstood what we wanted to express with this sentence. Although our original statement is in agreement with the point put forward by the referee, we will reformulate the sentence to avoid such misinterpretation.

### Changes in manuscript

#### Changes starting in line 38:

Active sensors have the advantage of providing high vertical resolution and generally higher sensitivity than their passive counterparts, ~~they are ultimately limited by the same principles.~~ This, however, typically comes at the expense of lower spectral and spatial coverage of the observations.

## Reviewer comment 5

“Prominent examples of satellite missions that exploit both of these synergies....”

Again I do not see how the

“non-local synergy which uses the vertically resolved radar observations to support passive-only retrievals across the wide swath of the passive sensor“.

What GPM does is use synergistic radar-radiometer retrievals to build a database for a Bayesian inversion, which is a different thing.

## Author response

Since passive-only observations provide only limited information on the vertical distribution of hydrometeors in the atmosphere, realistic a priori assumptions are necessary in order to produce accurate retrievals of hydrometeor profiles from the passive observations of the GPM constellation. The accuracy of these retrievals directly depends on the realism of the a priori database, which is ensured by deriving it from the combined observations provided by the radar and radiometer suite on the GPM Core Observatory. Because of this, we consider the accuracy of the a priori assumptions used for the GPM passive-only retrievals a synergy between the radiometers and the radar of the constellation. However, since the observations from the Core Observatory and the other radiometers do not need to be co-located to exploit this synergy, we refer to it as the non-local synergy.

To hopefully make our reasoning more clear, we will introduce the following changes in the manuscript.

## Changes in manuscript

### Changes starting in line 46:

Two types of synergies can be distinguished for such an observation scenario: A local synergy, which consists of using the co-located radar and radiometer observations to obtain more accurate hydrometeor retrievals, and ~~the a~~ non-local synergy, which uses the vertically ~~resolved radar~~ well-resolved results from the radar-only or combined observations to support passive-only retrievals across the wide swath of the passive sensor, for example by providing realistic a priori constraints.

## Reviewer comment 6

“and hence provide only limited sensitivity to frozen hydrometeors” but later on you say that MWi “will provide additional sensitivity to liquid and frozen precipitation”. Again very generic statements.

## Author response

We agree with the referee that the terminology can be made more precise. To do so, we will introduce the following changes in the revised manuscript.

## Changes in manuscript

### Changes starting in line 53:

Since the principal target of these missions ~~are retrievals of liquid hydrometeors~~ is the retrieval of precipitation, they make use of ~~sensors at~~ comparably low microwave frequencies and hence provide only ~~limited sensitivity to frozen hydrometeors~~ little sensitivity to non-precipitating hydrometeors (Greenwald and Christopher, 2002).

## Reviewer comment 7

Fig.2: I do not see any change to the figure (despite what the authors say). Units are still the same and wrong.

## Author response

We have unfortunately missed to correct unit of the PSDs in the plot, however we will ensure that this will be corrected in the revised manuscript.

## Changes in manuscript

Fig. 2 now looks as show in Fig. 3.1.

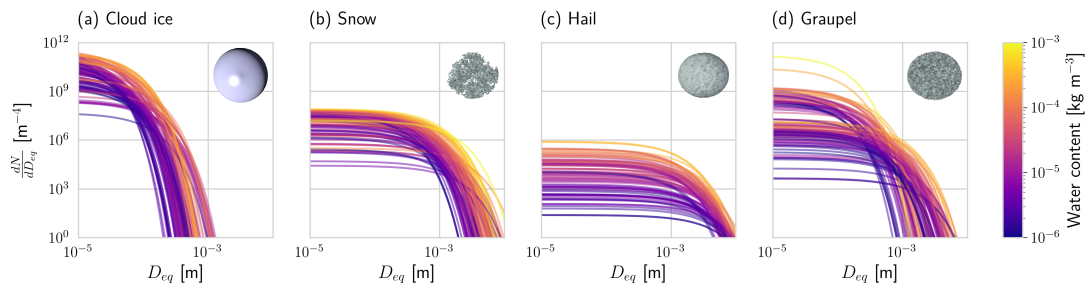


Figure 3.1: Realizations of particle size distributions from the test scenes used in this study. The particle number concentration is plotted with respect to the volume-equivalent diameter  $D_{eq}$ . Shown are the PSDs corresponding to 100 randomly chosen grid points with a water content higher than  $10^{-6}$   $\text{kg m}^{-3}$ . Line color encodes the corresponding water content. Insets display visualizations of the particle shape assumed for each hydrometeor species.

### Reviewer comment 8

Units of standard deviation of  $Z$ . The authors are reiterating common mistakes/typos present in literature, even when errors are highlighted. dBZ-dBZ is dB, that's the nature of logarithmic units!

### Author response

We would like to thank the reviewer for pointing and will correct this in the revised manuscript.

### Changes in manuscript

#### Changes starting in line 138:

The minimum sensitivity is set to be  $-30$  dBZ and the noise at each range gate is modeled to be independent with standard deviation ~~0.5 dBZ~~0.5 dB.

### Reviewer comment 9

Eq.3 : another wrong equation. Not sure what the authors are doing here but it is simple algebra, the equation is clearly wrong because there is no factor  $\pi$  involved (see <https://agupubs.onlinelibrary.wiley.com/doi/epdf/10.1029/2018JD028603>).

### Author response

The work referenced by the referee does in fact employ a similar transform. The transform in the referenced study, however, uses the inverse tangens, while we employ the inverse *hyperbolic* tangens. A factor of  $\pi$  is therefore not required in our case.

The plot given in Fig. 3.2 shows the relation between the quantities  $x$  and  $RH$  in the equation and proves that the transformation does what it is expected to do: Map any arbitrary value of  $x$  to the range  $[0.0, 1.2]$ .

### Reviewer comment 10

Eq.6 is another example of very confused terminology (the numerator is not a cross section!! efficiency is usually used for other scattering quantities)

### Author response

We thank the referee for pointing out the inaccurate terminology that we have applied here. The quantity  $\sigma$  is indeed not a cross section and a more consistent term for the quantity denoted as "mass backscattering efficiency" is probably "mass backscattering coefficient". This will be corrected in the revised manuscript.



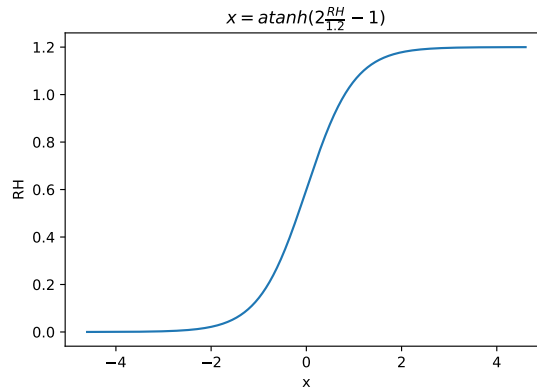


Figure 3.2: Plot of the relation between relative humidity values and the transformed quantity  $x$ .

### Changes in manuscript

#### Changes starting in line 242:

~~Fig-Figure 4 provides an overview of the bulk mass backscattering efficiencies and mass and attenuation coefficients of the selected particles computed for three different values of the  $N_0^*$  parameter of the PSD at the frequency of the cloud radar and three selected frequencies of the passive radiometers. Mass backscattering efficiency and attenuation coefficient and attenuation coefficients are defined as the ratio of the corresponding cross-section backscattering or attenuation coefficient  $\sigma$  and the bulk water content  $\div$ WC:~~

$$Q = \frac{\sigma}{WC}. \quad (3.1)$$

~~For high values of each particle shape and frequency,  $Q$  has been computed for three different values of the  $N_0^*$  parameter of the PSD. For a fixed bulk-mass, the value of the  $N_0^*$  parameter of the PSD is related to the size of the bulk particles: For high  $N_0^*$  values the number of large particles is decreased while it is increased for low  $N_0^*$  values. The variation of the mass backscattering and attenuation coefficients with mass show the non-linear relationship between bulk mass and the particles' radiometric properties. For high values of  $N_0^*$ , which are typical for cloud ice, the radiometric properties of particle shapes differ only for large masses at the two highest frequencies considered. For low  $N_0^*$  values, which are more typical for snow, the particles' properties differ considerably at all masses and frequencies.~~

### Reviewer comment 11

Fig.4 also does not make much sense to me (if you are normalising by IWC you should not plot it in the x-axis).

### **Author response**

We do not think that what the referee claims here is true. As the plots show, there is a non-linear dependency between water content and scattering properties. Normalization therefore does not cancel the dependency of the mass backscattering coefficient on the water content. Moreover, normalization is required to make the differences between different particles discernable in the plot, which would otherwise be dominated by the strong increase of the backscattering coefficient with bulk mass.

### **Reviewer comment 12**

Fig.7 y-label panel b) That is not IWP but a ratio of  $IWP_{\text{ret}}/IWP_{\text{true}}$ . Re-label.

### **Author response**

We will relabel the figure according to the referee's suggestions.

### **Changes in manuscript**

Figure 7 from the manuscript now looks as shown in Fig. 3.3.

### **Reviewer comment 13**

Units of IWC in Fig.14 are wrong.

### **Author response**

We thank the referee for pointing out this inconsistency and will correct it in the revised manuscript.

### **Changes in manuscript**

Fig. 14 now looks as shown in Fig. 3.4.

## **3.2 Scientific comments**

### **Reviewer comment 1**

I am still convinced about some major issues related to the selection of the scene. The key strength of the combination should be in ice clouds and mixed-phase but no clear message are coming out of this study on this (i.e. what kind of cloud-LWP can we retrieve with confidence? how important is to know the location of the SLWC layer?). Profiles with high density ice and rain underneath are much more complicated and certainly should not be the target of such a suite of instruments (but they occupy a large fraction of your scene). The only semi-quantitative statements is indeed present in the conclusions "While observations at currently available microwave frequencies provide information

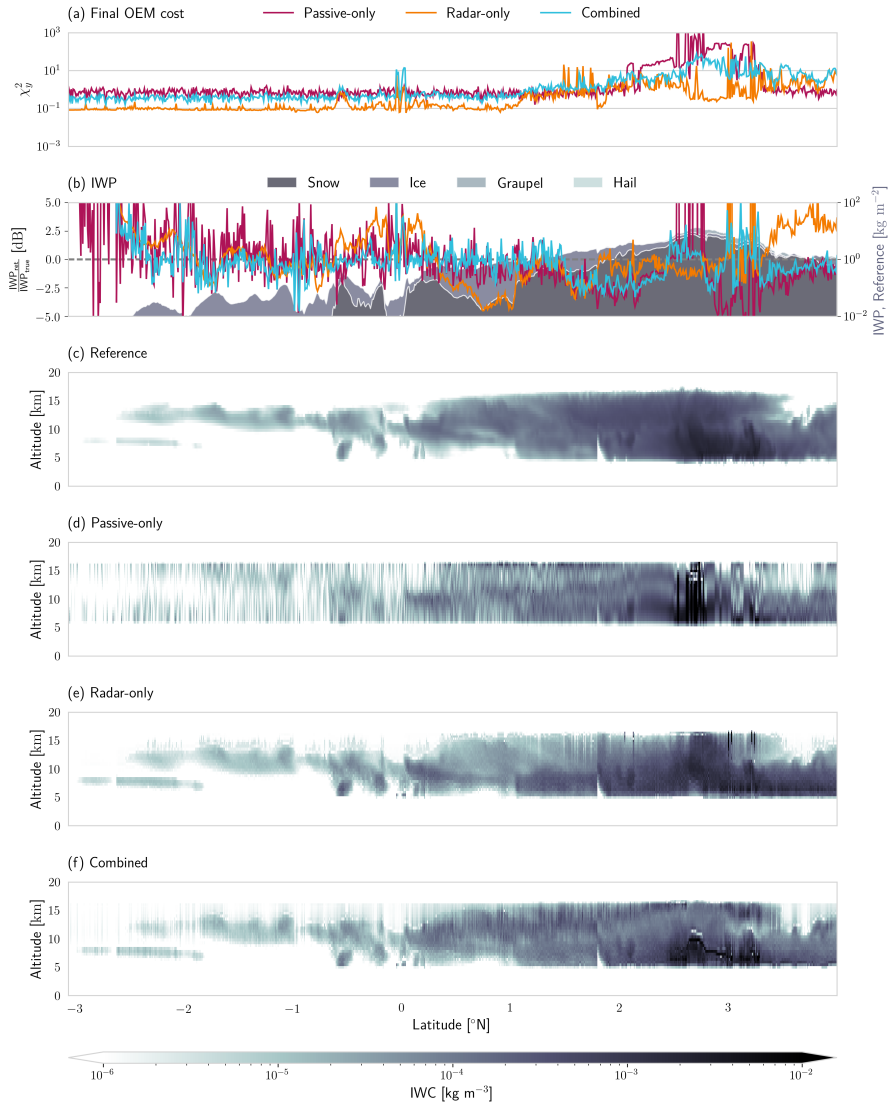


Figure 3.3: Results of the ice hydrometeor retrieval for the first test scene using the Large Plaque Aggregate particle model. Panel (a) displays the value of the  $\chi_y^2$  diagnostic normalized by the dimension of the measurement space of the corresponding retrieval. Panel (b) displays retrieved IWP in dB relative to the reference IWP. Reference IWP and the contributions from different hydrometeor classes are displayed by the filled areas in the background. Panel (c) shows the reference IWC from the model scene. Panel (d), (e) and (f) display the retrieval results for the passive-only, radar-only and combined retrieval, respectively.

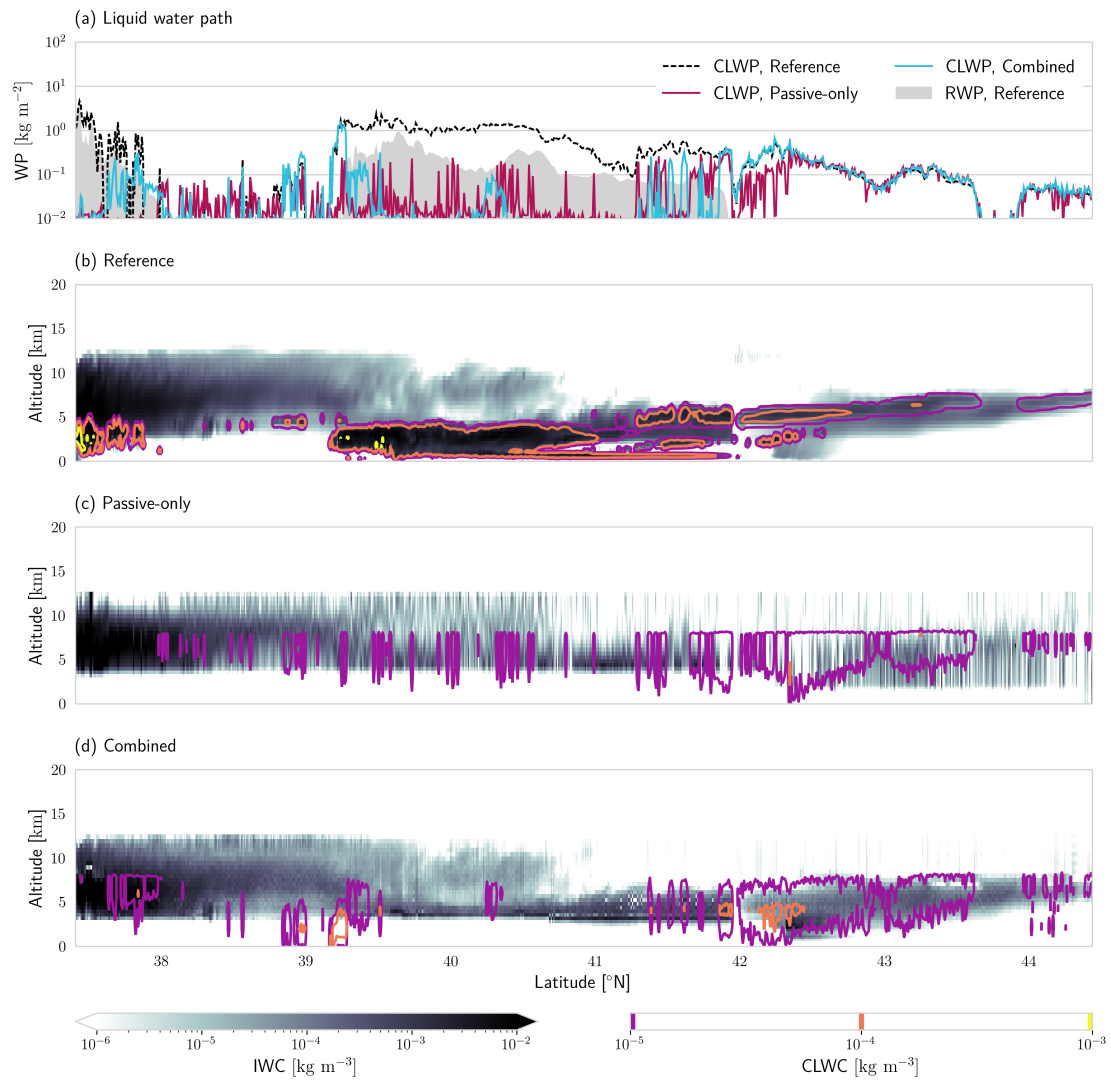


Figure 3.4: Reference and retrieved CLWC and IWC. Panel (a) shows the reference and retrieved LWP for each profile. Panel (b) displays reference LWC contours drawn on top of the total hydrometeor content. Retrieval results for passive-only and combined retrieval are given in Panel (c) and (d).

complementary to that from a radar only for thick clouds with very large particles ...” and is actually based on your Fig.5 (no retrieval involved).

## Author response

We have justified the selection of the test scenes in our previous response: The presented scenes contain a wide range of different cloud formations, which we chose over cherry picking specific scenes where the combined retrieval would work well. We did this in order to provide a more balanced view on the potential and limitations of the combined retrieval.

The referee goes on to request a more accurate assessment of the performance of the LWC retrieval, although we mention clearly that the main focus of our article is the retrieval of ice hydrometeors. We therefore consider the assessment of these specific cases to be out the scope of this article.

Furthermore, it is true that we refrain from making absolute statements on the performance of the combined retrieval. This is because our intention was never to develop a production-ready retrieval and give accurate performance estimates. Since this study is based purely on simulations the reliability of such an analysis would anyways be questionable. Although we already state this in the paragraph on the limitations of the study, we will reformulate the paragraph in an effort to make this point clearer.

## Changes in manuscript

### Changes starting in line 543:

Moreover, this study is purely based on simulations ~~and restricted to two selected model test scenes. The validity of~~ from two selected CRM scenes. These two scenes are certainly insufficient to accurately represent the variability of clouds in the atmosphere. Furthermore, the accuracy of the estimated retrieval performance will depend on the ~~presented results thus depends on how well cloud microphysics are represented in the GEM model. While this may affect interpretation of the results realism of the test scenes. Because of this, this study does not aim to provide an accurate assessment of the performance of the combined retrieval in absolute terms, the main findings of this work, which are based on a relative comparison of the retrieval results, should be less dependent on the realism of the test scenes~~ but instead a qualitative assessment of the potential of a combined retrieval based on the comparison of its results to the single instrument retrievals.

## Reviewer comment 2

Fig.3 and retrieval grid: the definition of the retrieval grid must be different if you consider a radiometer only or a retrieval including the radar. The advantage of a radar is indeed to produce a cloud mask first (actually with the sensitivity you have used all clouds are practically detected by the radar). So I really do not understand how it is possible to

see IWC in Fig.,7 panel e) and f) where there are no clouds (this magically disappear in Fig.10??). On the other hand I am also curious to know how with a radiometer-only retrieval you can constrain the cloud top like you are doing.

### Author response

As explained in the manuscript, performing the passive-only retrieval on the same grids as the combined retrieval is made possible by including spatial correlation in the a priori assumptions. Although limited, the passive observations contain some information on the vertical distribution of hydrometeors, which allows us to constrain the cloud top in the passive-only retrieval to a certain degree. Although it would have been possible to use the radar-only retrieval to produce a cloud mask, this is something we have not pursued in our implementation. All of these points are described in the section covering the retrieval implementation.

The contradicting data that the reviewer points out in Fig. 10, is due to an error in the reported masking threshold applied, which was chosen at  $5 \cdot 10^{-6} \text{kg m}^{-3}$  and not  $1 \cdot 10^{-6} \text{kg m}^{-3}$ . We will correct this in the revised manuscript.

#### 3.2.1 Change in manuscript

The following changes will be introduced in the revised manuscript:

**Changes starting in line 355:**

To simplify the comparison, number concentrations are displayed only where the corresponding reference or retrieved IWC is larger than  ~~$10^{-6} \text{kg m}^{-3}$~~   $5 \cdot 10^{-6} \text{kg m}^{-3}$ .

**Changes starting in line 351:**

Only values for which the corresponding reference or retrieved IWC was larger than  ~~$10^{-6} \text{kg m}^{-3}$~~   $5 \cdot 10^{-6} \text{kg m}^{-3}$  are shown here.

## 4 Marked-up differences

# Synergistic radar and radiometer retrievals of ice hydrometeors

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**Abstract.** Remote sensing observations at sub-millimeter wavelengths provide higher sensitivity to small hydrometeors and low water content than observations at millimeter wavelengths, which are traditionally used to observe clouds and precipitation. ~~Hence they~~ They are employed increasingly in field campaigns to study cloud microphysics and will be integrated into the global meteorological observing system to measure the global distribution of ice in the atmosphere. ~~A milestone in this development is with~~ the launch of the Ice Cloud Imager (ICI) radiometer on board the second generation of European operational meteorological satellites (Metop-SG), ~~which will make sub-millimeter observations of ice clouds available operationally~~. Observations at these novel wavelengths provide valuable information not only on their own but also in combination with complementary observations at other wavelengths. This study investigates the potential ~~benefits~~ of combining passive sub-millimeter radiometer observations with a hypothetical W-band cloud radar for the retrieval of frozen hydrometeors. ~~Using a simplified~~ An idealized cloud-model ~~is used to investigate~~ the information content of the combined observations ~~is investigated and the capacity of the observations and establish their capacity~~ to constrain the microphysical properties of ice hydrometeors ~~is established~~. A synergistic retrieval algorithm for airborne observations is proposed and applied to simulated observations from a cloud-resolving model. Results from the synergistic retrieval are compared to equivalent radar- and passive-only implementations in order to assess the benefits of the synergistic sensor ~~configurations~~ configuration. The impact of the assumed ice particle shape on the retrieval results is assessed for all retrieval implementations. ~~Although they show greater sensitivity to the assumed particle shape, the synergistic observations can~~ We find that the combined observations better constrain the ~~microphysics of the cloud, which decreases microphysical properties of ice hydrometeors which reduces~~ uncertainties in retrieved ice water content and ~~improves the retrieval of~~ particle number concentrations. ~~Our results also indicate improved sensitivity to liquid cloud water content for~~ for suitable choices of the ice particle model. Analysis of the ~~synergistic configuration compared to a passive-only setup. The results of this study demonstrate the potential of the synergistic sensor configuration to improve retrievals of frozen hydrometeors. The developed synergistic retrieval algorithm can be applied with only minor modifications to suitable airborne observations from sub-millimeter radiometers such as the International Sub-Millimetre Airborne Radiometer~~ retrieval information content shows that, although the radar contributes the largest part of information in the combined retrieval, the radiometer observations provide complementary information over a



25 wide range of atmospheric states. Furthermore, the combined retrieval yields slightly improved retrievals of liquid cloud water in mixed-phase clouds, pointing towards another potential application of combined radar-radiometer observations.

## 1 Introduction

Ice hydrometeors play an important role for both weather and climate. They influence the Earth's energy budget through their interaction with incoming and outgoing radiation, constitute a part of the global hydrological cycle and are coupled to the dynamics of the atmosphere in multiple ways (Bony et al., 2015). Because of this, observations of ice clouds are required for understanding the role of clouds in a changing climate (Boucher et al., 2013), to provide information on the dynamical state of the atmosphere in numerical weather prediction (NWP) models (Geer et al., 2017) and to validate climate models (Waliser et al., 2009). Despite this ~~importance~~, today's global observing system cannot provide accurate information on the global distribution of ice in the atmosphere (Eliasson et al., 2011; Duncan and Eriksson, 2018). A major difficulty of measuring atmospheric ice using remote sensing lies in the large variability of ice particle sizes, concentrations and shapes ~~in which ice particles occur in the atmosphere. The wide spectrum of ice crystal sizes, which ranges from micro- to millimeter scales,~~ which can only be partially resolved by available space-borne sensors.

Current operational observation systems used to study clouds can be divided into two groups by virtue of their observing frequency and ~~their~~ corresponding capabilities and limitations. Microwave sensors employ comparably long wavelengths ranging down to about 1 mm. ~~Compared to the~~ Since these wavelengths are large compared to the typical sizes of ice particles ~~, the wavelengths are very long and therefore sensitive only to very large ice particles. At the same time, they provide in a cloud,~~ microwave sensors are most sensitive to the ~~advantage of penetrating even thick clouds~~ largest particles and do not provide any sensitivity to the small particles in the cloud. Optical and infrared sensors use radiation with wavelengths from around 15  $\mu\text{m}$  down to several hundred nano meters. ~~Although these~~ These relatively short wavelengths make them sensitive ~~to also to the~~ small ice particles ~~, their signal saturates for thick clouds, which makes them insensitive to the ice mass further down the line of sight. Although radars and lidars allow detection of lower ice water contents in the cloud. The comparably low sensitivity of microwave sensors to small ice particles allows them to sense the larger, potentially precipitating, particles typically located at the center and base of a cloud, which cannot be sensed at infrared and optical wave lengths due to saturation of the signal.~~

Active sensors have the advantage of providing high vertical resolution and generally higher sensitivity than their passive counterparts ~~, they are ultimately limited by the same principles. This, however, typically comes at the expense of lower spectral and spatial coverage of the observations.~~

The ~~currently most accurate~~ most accurate current information on the global distribution of ice water content (IWC) is provided by the CloudSat radar. A main strength of these observations is their vertical resolution, in the order of 500 m. However, the radar lacks scanning capability and the swath width is just 1.5 km wide, to be contrasted with the swath width of passive imagers which is on the order of 1000 km. ~~A potentially less obvious limitation is that~~ CloudSat performs a single-frequency measurement ~~. Since this,~~ which limits the information per range bin to one degree of freedom ~~, a priori information~~

~~is required as additional constraint on.~~ Retrieving bulk properties like water content or particle number densities thus requires making a priori assumptions that constrain cloud microphysical properties such as particle size, concentration and shape.

A way to overcome the limitations of single-frequency radars is to combine them with observations from passive sensors, which typically provide measurements at multiple frequencies and a significantly wider swath. Two types of synergies can be distinguished for such an observation scenario: A local synergy, which consists of using the co-located radar and radiometer observations to obtain more accurate hydrometeor retrievals, and ~~the a~~ non-local synergy, which uses the vertically ~~resolved radar well-resolved results from the radar-only or combined~~ observations to support passive-only retrievals across the wide swath of the passive sensor, for example by providing realistic a priori constraints. Prominent examples of satellite missions that exploit both ~~of~~ these synergies are the the Tropical Rainfall Measuring Mission (TRMM, Kummerow et al. (1998); Grecu et al. (2004); Munchak and Kummerow (2011)) and the Global Precipitation Measurement (GPM, ~~Hou et al. (2014); Grecu et al. (2016); Kummerow et al. (2015)) mission~~) mission (Hou et al., 2014; Grecu et al., 2016; Kummerow et al., ). Since the principal target of these missions ~~are retrievals of liquid hydrometeors~~ is the retrieval of precipitation, they make use of ~~sensors at~~ comparably low microwave frequencies and hence provide only ~~limited sensitivity to frozen hydrometeors~~ little sensitivity to non-precipitating hydrometeors (Greenwald and Christopher, 2002).

With the upcoming launch of the Ice Cloud Imager (ICI) a new passive microwave sensor will become operational, which is dedicated to observing ice hydrometeors from space. ICI will extend the range of currently available microwave frequencies with channels at 243, 325, 448 and 664 GHz (Eriksson et al., 2020). This will narrow the size-sensitivity gap between the infrared and traditional microwave sensors by extending the smallest currently available microwave wavelength from 1.6 mm at 183 GHz down to the sub-millimeter domain (0.45 mm at 664 GHz) and significantly improve the size-sensitivity of spaceborne microwave observations of clouds. Together with ICI, the newly developed Microwave Imager (MWI) will be flown on the satellites of the Metop-SG program. MWI will complement ICI's observations with measurements at traditional millimeter wavelengths as well as a spectral band around the 118 GHz oxygen line. The observations of MWI, which cover the frequency range from 19 GHz up to 183 GHz, will provide additional sensitivity to liquid and frozen precipitation as well as water vapor.

~~With ICI sub-millimeter radiometry of clouds will reach operational status. This has of course sparked interest in its potential~~ A number of studies have investigated the potential of ICI for studying ice in the atmosphere. The information content and retrieval performance of radiometer observations alone has been studied in detail for column-integrated ice water content (Jiménez et al., 2007; Wang et al., 2017; Brath et al., 2018; Eriksson et al., 2020) as well as for the vertical distribution of ice in the atmosphere (Birman et al., 2017; Grützun et al., 2018; Aires et al., 2019). Although not directly related to ICI, the combination of millimeter and sub-millimeter radiometer observations with active observations from a cloud radar has been investigated by Evans et al. (2005) and Jiang et al. (2019).

In this study, we are interested in the local synergies of co-located MWI/ICI-type radiometer observations combined with observations from a W-band radar. In particular, we aim to answer the question what additional information can be gained from combined observations compared to observations from ~~the a~~ radar or MWI and ICI alone. For this, a combined, variational retrieval is developed and applied to simulated observations of scenes from a cloud-resolving model (CRM). An airborne viewing geometry is assumed for the simulations with all sensors pointing at nadir and close-to overlapping antenna beams.

Our work extends the previous work by Evans et al. (2005) and Jiang et al. (2019) by comparing the performance of the combined retrieval to that of equivalent radar- and passive-only retrievals, which allows us to quantify the value added by the synergistic observations. In addition to that, the impact of the assumed scattering properties of ice hydrometeors on the retrieval is investigated.

This study consists of two principal parts: In the first part, simulated observations from a simplified cloud model are used to perform a preliminary study of the complementary information content of radar and passive radiometer observations. In the second part, the developed synergistic retrieval algorithm is applied to simulated observations from a CRM to investigate the performance benefits of the combined observations compared to radar- and passive-only configurations. Following this introduction, Section 2 introduces the test data, sensor configuration and the developed retrieval algorithm on which the study is based. This is followed by the experimental results on the information content of the combined observations and the simulated retrieval results in Section 3. The article closes with a discussion of the results in Section 4 and conclusions in Section 5.

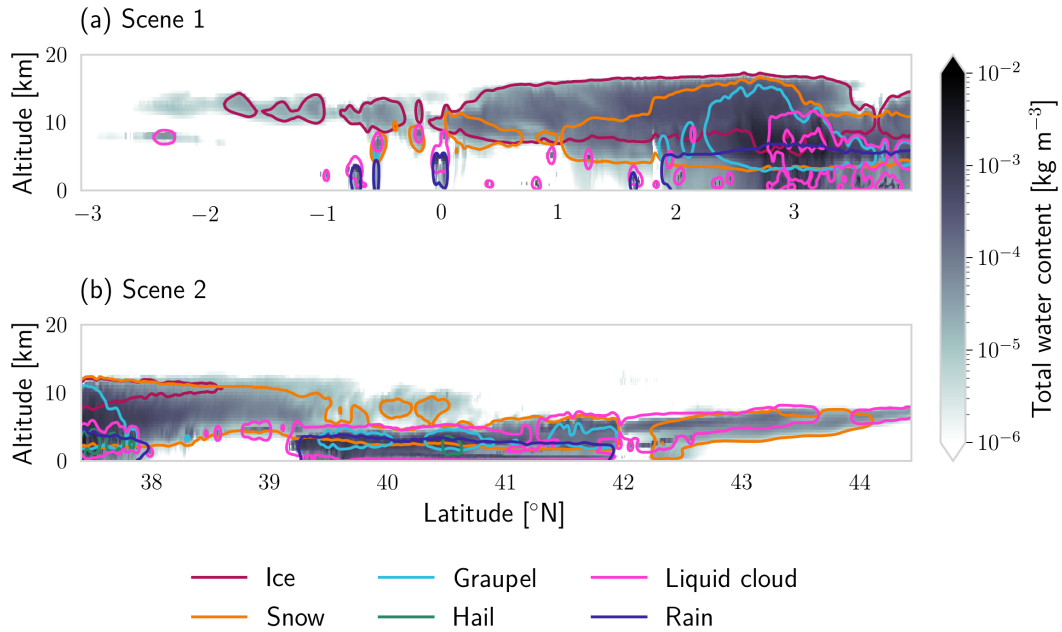
## 2 Methods and data

### 2.1 Reference cloud scenes

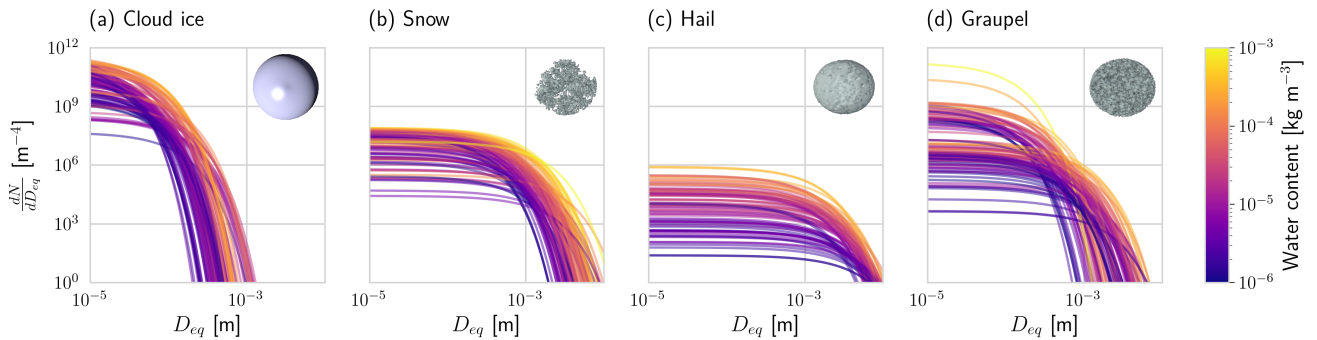
The cloud scenes which are used for the testing of the retrieval were produced by Environment and Climate Change Canada using a high-resolution NWP configuration of the Global Environmental Multiscale (GEM) Model (Côté et al. (1998)). Two test scenes with a horizontal resolution of 1 km and an extent of 800 km were selected. The vertical resolution of the model scenes varies between 250 and 500 m below an altitude of 18 km and decreases steadily above that. The scenes, displayed in Fig. 1, were chosen with the aim of covering a large range of cloud structures and compositions so as to ensure a realistic-broad assessment of the retrieval. The first test scene, shown in panel (a), is located in the tropical Pacific and contains a mesoscale convective system in the northern half of the scene and its anvil which extends into the southern half. The second scene, shown in panel (b), is located in the North Atlantic and contains an ice cloud in the southern part and a low-level, mixed-phase cloud in the northern part.

The GEM model uses a two-moment scheme with six types-classes of hydrometeors to represent clouds and precipitation (Milbrandt and Yau, 2005): Two classes of liquid hydrometeors (rain and liquid cloud) and four of frozen hydrometeors (cloud ice, snow, hail and graupel). The particle size distribution (PSD) of each hydrometeor class is described by a three-parameter gamma distribution. The prognostic parameters of the model are the slope and intercept parameters of the PSD, which are derived from the predicted mixing ratios and number concentrations. The third parameter, which defines the shape of the PSD, is set to a fixed, species-specific value. For each hydrometeor species a specific mass-size relationship is assumed.

Examples of particle size distributions of frozen hydrometeors are displayed in Fig. 2. The assumed particle size distributions across different ice species vary mostly in their scaling with respect to size and concentration, whereas the normalized-shape shows less variability. An important characteristic of-the-model can be identified here, which will help to better understand the retrieval results presented later: Cloud ice in-the-model is characterized by high particle number concentrations and small particle sizes, whereas snow has lower number concentrations and larger particles.



**Figure 1.** The distribution of total water content including all hydrometeor classes in the two cloud scenes used to test the retrieval. Colored lines show the  $10^{-5} \text{ kg m}^{-3}$  contour of the water content of each hydrometeor class.



**Figure 2.** Realizations of particle size distributions from the test scenes used in this study. The particle number concentration is plotted with respect to the volume-equivalent diameter  $D_{eq}$ . Shown are the PSDs corresponding to 100 randomly chosen grid points with a water content higher than  $10^{-6} \text{ kg m}^{-3}$ . Line color encodes the corresponding water content. Insets display visualizations of the particle shape assumed for each hydrometeor species.

125 In order to simulate observations from the GEM model scenes, the hydrometeor classes of [the GEM-its](#) microphysics scheme must be associated with particle shapes to define their radiometric properties. The ARTS single-scattering database, described in more detail below, contains particle models which were designed to be consistent with the mass-size relationships assumed

**Table 1.** Particle shapes used to represent the hydrometeor species of the GEM model scenes. The mass size relationship is given in terms of the parameters of a fitted power law of the form  $m = \alpha \cdot D_{\max}^{\beta}$  with  $D_{\max}$  the maximum diameter in  $\mu\text{m}$  and  $m$  in  $\text{kg}\cdot\text{m}^{-3}\cdot\text{kg}$ .

GEM hydrometeor class	Associated particle shape Name (ID)	Size range		Mass size relationship	
		$D_{\text{eq, min}}$ [ $\mu\text{m}$ ]	$D_{\text{eq, max}}$ [ $\mu\text{m}$ ]	$\alpha$	$\beta$
Liquid cloud	LiquidSphere (25)	1	$5 \cdot 10^4$	480	3
Rain	LiquidSphere (25)	1	$5 \cdot 10^4$	480	3
Ice cloud	GEM Cloud Ice (31)	10	$3 \cdot 10^3$	440	3
Snow	GEM Snow (32)	94	$5 \cdot 10^3$	24	2.86
Graupel	GEM Graupel (33)	94	$5 \cdot 10^3$	170	2.96
Hail	GEM Hail (34)	94	$5 \cdot 10^3$	540	3.02

in the GEM model. The particle shapes used to represent the GEM model’s different hydrometeor types are listed together with their properties in Tab. 1.

## 130 2.2 Simulated cloud observations

An airborne sensor configuration is simulated to test the retrieval. The beams of all three sensors are assumed to point at nadir and to be perfectly coincident pencil beams. Multiple scattering effects in the radar observations as well as the effects of particle orientation are neglected. Although these assumptions may be justified for an airborne configuration, this will not be the case for space-borne observations from ICI and MWI. Moreover, the incidence angles of the beams of ICI and MWI will be around  
135  $53^\circ$  at the Earth’s surface. This further complicates the radiative transfer modeling since it requires treating a more complex co-location geometry of for the nadir-pointing radar and the passive instruments. At off-nadir viewing angles, polarization also needs to be taken into account, the effects of which can be several Kelvin at the typical viewing angles of microwave imagers (Xie et al., 2015).

### 2.2.1 Sensor configuration

140 The sensor configuration assumed for the simulated observations includes the 11 highest-frequency channels of the MWI radiometer and all ICI channels. For the radar, a nadir-pointing W-band cloud radar with similar characteristics as the CloudSat Cloud Profiling Radar (CPR, Stephens et al. (2002); Tanelli et al. (2008)) is assumed.

Observations from the ICI radiometer are simulated by performing a single, non-polarized radiative transfer simulation located at the centers of the pass bands of each double-sideband channel and averaging the resulting brightness temperatures.  
145 For channels with multiple polarizations, only a single simulation is performed. To compensate for this, the noise of the corresponding channel is reduced by a factor of  $\sqrt{2}$ . The simulated ICI channels and assumed noise levels are presented in Tab. 2.

Observations from the MWI radiometer are simulated in a similar manner to those of ICI except that for MWI only channels with frequencies larger than or equal to 89 GHz are used. The reason for this is that the footprints of the channels with

150 frequencies lower than 89 GHz will have full-width at half maximum of 50 km compared to only 10 km for the MWI's higher-frequency channels and 16 km for ICI's channels. For a spaceborne configuration, these channels were deemed unlikely to be beneficial for a synergistic retrieval due to the very small overlap of the footprints of these channels with that of the radar. The included MWI channels are listed in Tab. 2.

**Table 2.** Channels of the MWI and ICI radiometers used in the retrieval.

MWI			ICI		
Channel	Freq. [GHz]	Noise [K]	Channel	Freq. [GHz]	Noise [K]
MWI-8	89	1.1	ICI-1	$183.31 \pm 7.0$	0.8
MWI-9	$118.75 \pm 3.2$	1.3	ICI-2	$\pm 3.4$	0.8
MWI-10	$\pm 2.1$	1.3	ICI-3	$\pm 2.0$	0.8
MWI-11	$\pm 1.4$	1.3	ICI-4	$243 \pm 2.5$	$\frac{1}{\sqrt{2}} \cdot 0.7$
MWI-12	$\pm 1.2$	1.3	ICI-5	$325.15 \pm 9.5$	1.2
MWI-13	$165.5 \pm 0.75$	<del>1.3</del> <u>1.2</u>	ICI-6	$\pm 3.5$	1.3
MWI-14	$183.31 \pm 7.0$	<del>1.2</del> <u>1.3</u>	ICI-7	$\pm 1.5$	1.5
MWI-15	$\pm 6.1$	1.2	ICI-8	$448 \pm 7.2$	1.4
MWI-16	$\pm 4.9$	1.2	ICI-9	$\pm 3.0$	1.6
MWI-17	$\pm 3.4$	1.2	ICI-10	$\pm 1.4$	2.0
MWI-18	$\pm 2.0$	1.3	ICI-11	$664 \pm 4.2$	$\frac{1}{\sqrt{2}} \cdot 1.6$

The frequency of the the cloud radar is chosen to be 94 GHz similar to the CloudSat CPR. The vertical resolution of the nadir-pointing radar observations is assumed to be 500 m ranging from 0.5 to 20 km in altitude. The minimum sensitivity is set to be  $-30$  dBZ and the noise at each range gate is modeled to be independent with standard deviation  $0.5$  dBZ  $0.5$  dB.

### 2.2.2 Radiative transfer simulations

All simulations presented in this study were performed using Version 2.3.1279 of the Atmospheric Radiative Transfer Simulator (ARTS, Buehler et al. (2018)). Radar reflectivities are computed using ARTS' built-in single-scattering radar solver, which provides analytic Jacobians. For the simulation of passive radiances, a hybrid solver is used which combines the DISORT (Stamnes et al., 2000) scattering solver with the ARTS standard scheme for pencil beam radiative transfer. The hybrid solver has been added to ARTS specifically for this study and provides approximate, analytical Jacobians, which are required for variational retrievals of hydrometeors. All simulations are performed assuming an ocean surface with emissivities calculated using the Tool to Estimate Sea-Surface Emissivity from Microwaves to sub-Millimeter waves (TESSEM, Prigent et al. (2017)). Polarization is neglected in all simulations performed in this study. Gaseous absorption is modeled using the absorption models from Rosenkranz (1993) for  $N_2$ ,  $O_2$  and from Rosenkranz (1998) for  $H_2O$ .

Single scattering data for hydrometeors are taken from ARTS single scattering data base (ARTS SSDB, Eriksson et al. (2018)). The database provides scattering data for a wide range of hydrometeor shapes including particles designed specifically

to be consistent with assumptions of the GEM microphysics scheme. It also provides a number of predefined habit mixes, referred to as standard habits, ~~designed to~~ which cover the full range of particle sizes relevant for microwave observations of ice hydrometeors.

### 2.3 Retrieval algorithm

A one-dimensional, variational cloud retrieval algorithm is proposed which uses the optimal estimation method (OEM, Rodgers (2000)) to fit an atmospheric state to given observations. The quality of a retrieved state  $\hat{\mathbf{x}}$  and corresponding simulated observations  $\hat{\mathbf{y}} = \mathbf{F}(\hat{\mathbf{x}})$  is assessed using the following diagnostic quantity:

$$\chi_y^2 = \Delta \mathbf{y}^T \mathbf{S}_e^{-1} \Delta \mathbf{y} \quad (1)$$

Here,  $\Delta \mathbf{y} = \mathbf{y} - \hat{\mathbf{y}}$  is the difference between the ~~fitted and true~~ true and fitted observations and  $\mathbf{S}_e$  is the covariance matrix describing the measurement errors. The quantity  $\chi_y^2$  corresponds to the sum of squared errors in the fitted observations weighted by the ~~uncertainties in precision of~~ each channel or range bin. It should be noted that the quantity has no meaningful interpretation in terms of  $\chi^2$ -statistic for the errors in the fitted observations since they will neither be independent (c.f. Chapter 12 in Rodgers (2000)) nor Gaussian due to the presence of forward model error. The value is therefore used here solely as a heuristic to quantify the goodness of the fit to the true observations.

#### 2.3.1 Measurement space

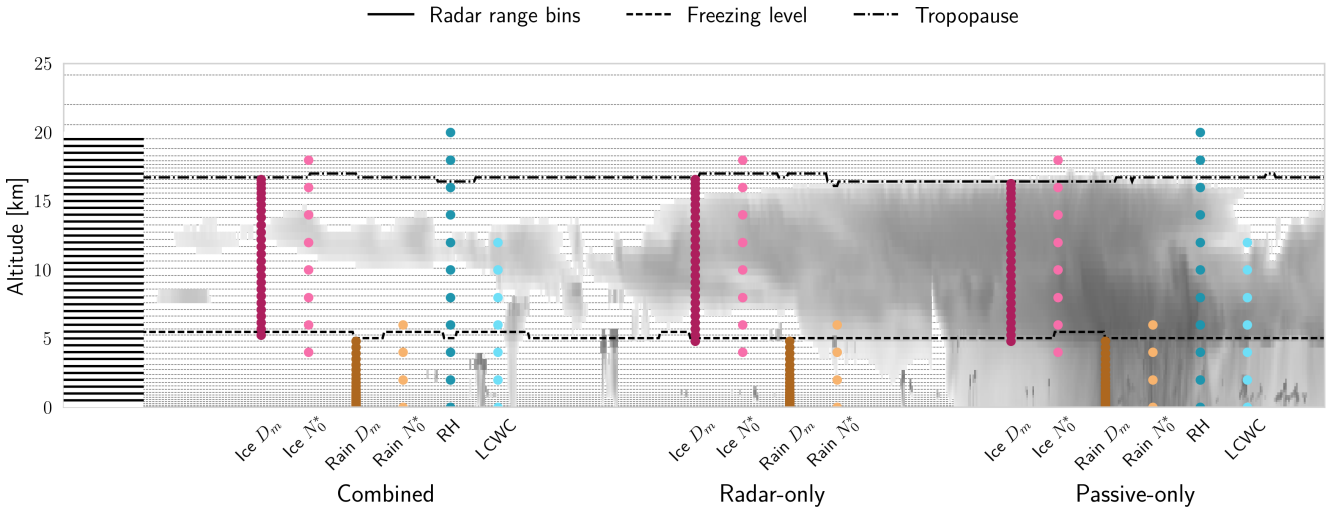
The input for the synergistic retrieval is the combined observation vector  $\mathbf{y}$  consisting of the concatenated single-instrument observations from the cloud radar and the two radiometers. Measurement errors are assumed to be independent and Gaussian distributed with standard deviations according to the noise characteristics given in Section 2.2.1. For the single-instrument retrievals the measurement vector consists only of observations from either the radar or the radiometers.

#### 2.3.2 State space

The proposed retrieval solves for profiles of two degrees of freedom of the PSDs of frozen hydrometeors and rain along with profiles of relative humidity (RH) and liquid-cloud water content (LCWC). An illustration of the retrieved quantities and their respective retrieval grids for the combined and single-instrument configurations of the retrieval are given in Fig. 3.

The PSDs of frozen hydrometeors and rain are represented using the normalized particle size distribution formalism proposed by Delanoë et al. (2005). The PSD of a hydrometeor species at a given altitude is modeled using a generalized gamma distribution function with four parameters. The mass-weighted mean diameter  $D_m$ , which scales the PSD along the size dimension, and the normalized number density  $N_0^*$ , which scales the particle concentration, are the two retrieved degrees of freedom of the PSD. The other two parameters describe the shape of the normalized PSD. The same shape parameters as in version 3 of the DARDAR-CLOUD product (Cazenave et al., 2019) are chosen for frozen hydrometeors. For rain, they are chosen to match the shape used in the GEM model for rain drops.





**Figure 3.** Illustration of retrieval quantities and their respective retrieval grids. Grey, dashed lines in the background display the vertical grid of the GEM model. Black, solid lines on the left side display the range bins of the radar observations. Filled markers represent the retrieval grids of each retrieval quantity for the combined, radar-only and passive-only configurations of the retrieval algorithm.

The temperature-dependent a priori profile for  $N_0^*$  for frozen hydrometeors is determined using the relation from Delanoë et al. (2014)

$$N_0^* = \exp(-0.076586 \cdot (T - 273.15) + 17.948), \quad (2)$$

where  $T$  is in K. The a priori profile of  $D_m$  for frozen hydrometeors is chosen so that the a priori IWC is equal to  $10^{-6} \text{ kg m}^{-3}$ . For rain, a fixed value for  $N_0^*$  of  $10^6 \text{ m}^{-4}$  is assumed and the a priori profile for  $D_m$  is determined similarly as for frozen hydrometeors.

Since the  $N_0^*$  parameters vary over several orders of magnitude they are retrieved in  $\log_{10}$ -space for both frozen hydrometeors and rain. The  $D_m$  parameters, in contrast, are retrieved in linear space. Alternative parametrizations using water content and  $D_m$  or the water content and  $N_0^*$  have been tested but no considerable effect on retrieval performance has been observed. As additional constraints, the retrieval of frozen hydrometeors is restricted to the region between the freezing level, here defined simply as the 273.15 K-isotherm, and the approximate altitude of the tropopause. The altitude of the tropopause is approximated as the first grid point at which the lapse rate is negative and temperature below 220 K. The retrieval of rain hydrometeors is restricted to below the freezing level. The retrieval of the  $N_0^*$  parameters is further regularized by retrieving them at reduced vertical resolution of 2 km. This was found necessary to keep the retrieval from getting stuck in spurious local minima. **This resembles the approach** [A similar approach is](#) taken in the GPM combined precipitation retrievals (Greco et al., 2016), where the PSD parameter scaling the particle concentration is also retrieved at reduced resolution.



215 Relative humidity is retrieved at a vertical resolution of 2 km. However, the values are not retrieved directly but instead an inverse hyperbolic tangent transformation is applied to the relative humidity profile:

$$x = \operatorname{arctanh}\left(\frac{2\text{RH}}{1.2} - 1.0\right) \quad (3)$$

The transformation restricts the retrieved relative humidity values to the range between 0 and 120%. The a priori profile for relative humidity is set to

$$220 \text{ RH}(t) = \begin{cases} 0.7 & , 270 \text{ K} < t \\ 0.7 - 0.01 \cdot (270 - t) & , 220 < t \leq 270 \text{ K} \cdot \\ 0.2 & , t < 220\text{K} \end{cases} \quad (4)$$

LCWC is retrieved at a resolution of 2 km but is restricted to the region between the surface and the 230 K isotherm. In contrast to frozen hydrometeors and rain, the PSD of liquid cloud droplets is not explicitly resolved in the retrieval forward model. Instead, liquid cloud droplets are modeled as purely absorbing quantity using the model by Liebe et al. (1993) for suspended liquid cloud droplets. Note that this is the case only for the retrieval. For the simulated observations, liquid cloud droplets are handled as any other hydrometeor species in the GEM model. LCWC is retrieved in  $\log_{10}$ -space and the a priori profile is set to a fixed value of  $10^{-6} \text{ kg m}^{-3}$  in the permitted region of the atmosphere.

The a priori distributions of the 6 retrieval quantities ( $N_0^*$  and  $D_m$  for frozen and liquid hydrometeors, RH, CLWC) are assumed to be independent so that the overall a priori covariance matrix  $\mathbf{S}_a$  has block-diagonal structure. Within each block, vertical correlations between the values of a given retrieval quantity at different altitudes are assumed to be exponentially decaying. The covariance of the values of retrieval quantity  $q$  at points  $i$  and  $j$  of the retrieval grid is computed as

$$(\mathbf{S}_{a,q})_{i,j} = \sigma_{q,i} \sigma_{q,j} \cdot \exp\left(-\frac{d(i,j)}{l_q}\right), \quad (5)$$

where  $\sigma_{q,i}$  is the a priori uncertainty assumed for retrieval quantity  $q$  at grid point  $i$ ,  $d(i,j)$  the vertical distance between the grid points and  $l_q$  the quantity-specific correlation length. The assumed a priori uncertainties and correlation lengths for the retrieval quantities are summarized in Tab. 3.

235 The radar-only version of the retrieval is similar to the combined version except that RH and LCWC are not retrieved. Instead, perfect knowledge of the true RH profile is assumed while LCWC is neglected. In addition to a two-moment radar-only retrieval, also a one-moment version (M1), in which only the  $D_m$  parameter is retrieved has been tested. ~~For completeness, retrieval results for IWC will be reported also for the M1 version. However, to allow for better comparison with the combined and passive-only retrieval, for the remaining results only the two-moment version is considered~~ However, results of this version will be shown only for the comparison of IWC retrieval errors. For the passive-only retrieval, the retrieval quantities and grids are the same as for the combined retrieval. However, higher correlations lengths are assumed, which are shown in Tab. 3

### 2.3.3 Representation of ice particle shape

A major difficulty for cloud retrievals is that the observations may not provide sufficient information to distinguish different ~~hydrometeor species~~ species of hydrometeors. Due to this ambiguity, frozen hydrometeors in the proposed retrieval algorithm

**Table 3.** A priori uncertainties  $\sigma_q$  and correlation lengths  $l_q$  used in the retrieval.

Retrieval target		Combined / Radar-only		Passive-only	
Name	Retrieved quantity	$\sigma_q$	$l_q$ [km]	$\sigma_q$	$l_q$ [km]
Ice, $N_0^*$	$\log_{10}(N_{0,\text{Ice}}^*)$	2	2	2	5
Ice, $D_m$	Ice $D_{m,\text{Ice}}$	300 $\mu\text{m}$	2	300 $\mu\text{m}$	5
Rain, $N_0^*$	$\log_{10}(\text{Rain } N_0^*)$	2	2	2	5
Rain, $D_m$	$D_{m,\text{Rain}}$	300 $\mu\text{m}$	2	300 $\mu\text{m}$	5
Relative humidity (RH)	$\text{arctanh}(\frac{2 \cdot \text{RH}}{1.2} - 1.0)$	0.5*	2*	0.5	2
Cloud liquid water content (CLWC)	$\log_{10}(\text{CLWC})$	1*	2*	1	2

\*: Not retrieved in radar-only retrieval

245 are represented using only a single hydrometeor species. It is therefore necessary to find a suitable representation for frozen hydrometeors, which can capture the variability of the four frozen hydrometeor species in the GEM model and ideally also that of real ice hydrometeors.

The ~~differences between hydrometeor species in the test scenes are due to their different~~ four species of frozen hydrometeors in the GEM model have different characteristic particle concentrations, sizes and shapes (c.f. Fig. 2). Since ~~two parameters of the retrieval can adapt two degrees of freedom of the PSD of frozen~~ hydrometeor species are retrieved, the retrieval is able to represent the characteristic hydrometeors, it can represent the variations in particle number concentrations and particle sizes of the different hydrometeor species. ~~Variations in particle shape which~~ By using a habit mix for the ice hydrometeor shape used in the retrieval, variations in particle shape that correlate with particle size ~~can be represented using a habit mix combining crystal shapes at small sizes with~~, such as differences between pristine crystals and aggregates or rimed particles ~~at larger sizes.~~ This provides the retrieval with some flexibility to represent the different shapes present in the test scenes, can be represented in the retrieval.

Even with this configuration ~~the simplified retrieval forward model will not~~, the single hydrometeor species used in the retrieval is unlikely to be able to represent ~~every possible configuration of mixes of the four ice hydrometeor species the variability present~~ in the GEM model. ~~It thus remains unclear or the real world. To shed some light on the question~~ which particle shape should be ~~used to best represent this mixture. We therefore~~ assumed in the retrieval to minimize the resulting representation error, we choose a set ~~consisting~~ of multiple particle shapes and habit mixes for which we investigate the impact of the particle choice on the retrieval results.

The selected particles are listed in Tab. 4. Three of them, GEM Cloud Ice, GEM Snow, and GEM Graupel, correspond to the shapes present in the GEM model scenes. The GEM Snow and Graupel habits were mixed with crystal shapes to ensure that they cover sizes down to around 10  $\mu\text{m}$ . In addition to this, two of the habit mixes distributed with the ARTS SSDB, the Large Plate Aggregate and Large Column Aggregate standard habits, are included in the selection to increase the range of scattering properties it covers. ~~Fig.~~

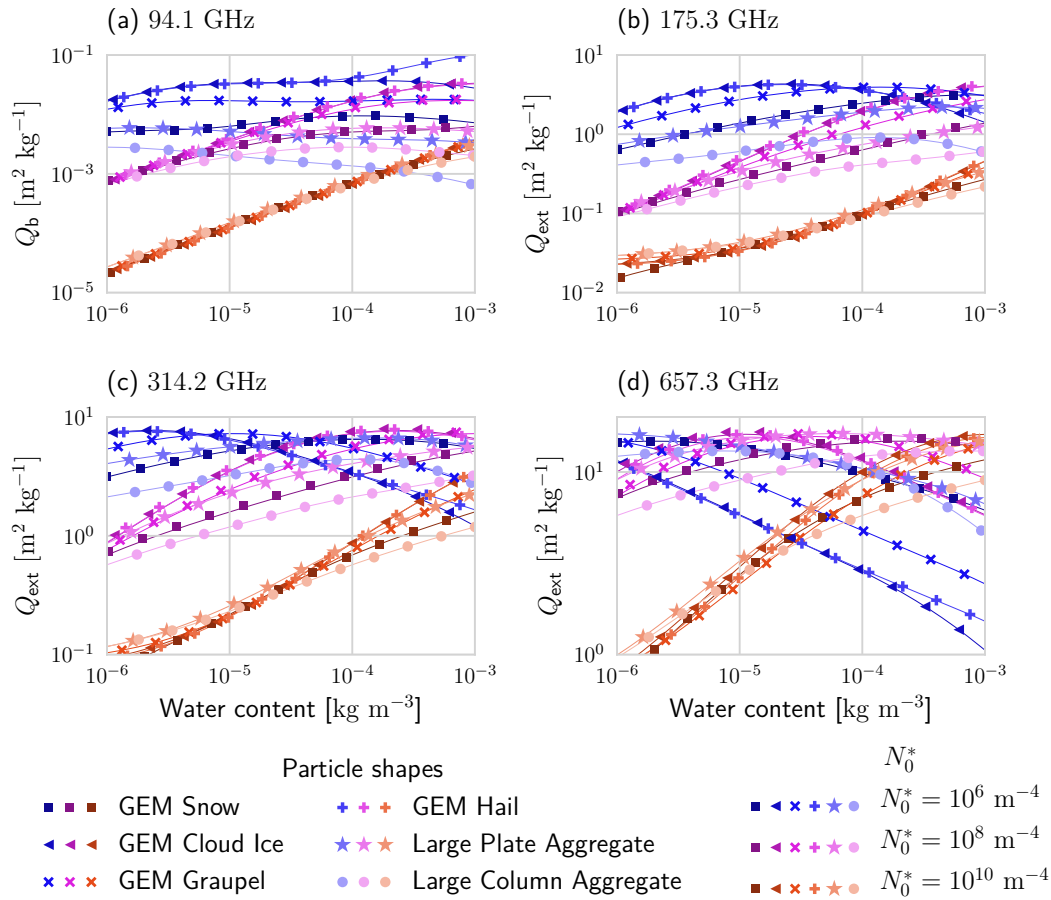
**Table 4.** Particle models used to represent ice hydrometeors used in the retrieval. The mass size relationship is given in terms of the parameters of a fitted power law of the form  $m = \alpha \cdot D_{\max}^{\beta}$  with  $D_{\max}$  the maximum diameter in  $\mu\text{m}$  and  $m$  in  $\text{kg}\cdot\text{m}^{-3}\cdot\text{kg}$ .

Name	Shapes used Name (ID)	Size range		Mass size relationship	
		$D_{\text{eq, min}}$ [ $\mu\text{m}$ ]	$D_{\text{eq, max}}$ [ $\mu\text{m}$ ]	$\alpha$	$\beta$
<del>CloudIce</del> -GEM Cloud Ice	GEM <del>CloudIce</del> ( <del>H</del> Cloud Ice (31))	10	3000	440	3
GEM Snow	8-Column Aggregate (8)	10	127	65	3
	GEM Snow (32)	107	5000	24	2.86
GEM Graupel	8-Column Aggregate (8)	10	179	65	3
	GEM Graupel (33)	107	5000	170	2.96
Large Plate Aggregate	Thick Plate (15)	16	200	110	3
	Large Plate Aggregate (33)	160	3021	0.21	2.26
Large Column Aggregate	Block Column (12)	10	200	<del>110</del> 210	3
	Large Column Aggregate (2218)	160	3021	0.25	2.43

Figure 4 provides an overview of the bulk mass backscattering efficiencies and mass and attenuation coefficients of the selected particles computed for three different values of the  $N_0^*$  parameter of the PSD at the frequency of the cloud radar and three selected frequencies of the passive radiometers. Mass backscattering efficiency and attenuation coefficient and attenuation coefficients are defined as the ratio of the corresponding cross-section backscattering or attenuation coefficient  $\sigma$  and the bulk water content  $\div\text{WC}$ :

$$Q = \frac{\sigma}{\text{WC}}. \quad (6)$$

For high values of each particle shape and frequency,  $Q$  has been computed for three different values of the  $N_0^*$  parameter of the PSD. For a fixed bulk-mass, the value of the  $N_0^*$  parameter of the PSD is related to the size of the bulk particles: For high  $N_0^*$  values the number of large particles is decreased while it is increased for low  $N_0^*$  values. The variation of the mass backscattering and attenuation coefficients with mass show the non-linear relationship between bulk mass and the particles' radiometric properties. For high values of  $N_0^*$ , which are typical for cloud ice, the radiometric properties of particle shapes differ only for large masses at the two highest frequencies considered. For low  $N_0^*$  values, which are more typical for snow, the particles' properties differ considerably at all masses and frequencies. At the two lowest frequencies, the Large Column Aggregate, Large Plate Aggregate and GEM Snow are the least efficient scatterers or absorbers of in scattering or absorbing radiation whereas GEM Graupel, Gem-GEM Hail and GEM Cloud Ice are more efficient. This behavior is also observed at the two higher frequencies, except for the lowest  $N_0^*$  value for which a reversal of the ordering occurs as the bulk mass increases. The mass backscattering efficiency at 94 GHz shows the greatest relative variability across different bulk water contents and  $N_0^*$  values, spanning six orders of magnitudes, while for the mass attenuation coefficients at the other frequencies the variability spans at most three orders of magnitude.



**Figure 4.** Bulk mass backscattering efficiency coefficient  $Q_b$  at 94.1 GHz (a) and mass attenuation coefficients  $Q_e$  at frequencies 175.3 GHz (b), 314.2 GHz (c) and 657.3 GHz (d) for the particle models used in the simulated observations and the retrieval. Different colors show the bulk properties for different values of the  $N_0^*$  parameter of the PSD.

### 3 Results

The first part of this section presents results from a numerical experiment which investigates the complementary information content of the active and passive microwave observations. Results of the combined and the single-instrument retrievals applied to the reference cloud scenes are presented in the second part.

#### 3.1 Complementary information content

A fundamental question regarding the benefit of combining two remote sensing observations in a retrieval is to what extent the observations contain non-redundant information. The degree of non-redundancy in the combined observations is what we

refer to here as complementary information content. We are thus interested in the information that cannot be provided by  
 295 either of the instruments alone. ~~The higher~~ As an example, we do not consider the high vertical resolution achieved by adding  
~~radar observations to passive ones is therefore not considered~~ combining passive with radar observations as complementary  
 information since the ~~radar alone can provide the increased resolution~~ same vertical resolution would be provided by radar-only  
observations.

In order to explore the complementary information content in the radar and radiometer observations, an idealized, homoge-  
 300 neous cloud layer with a thickness of 5 km centered at an altitude of 10 km in a tropical atmosphere is considered. The cloud  
 is assumed to consist of a single species of frozen hydrometeors represented using the PSD parametrization which is also used  
 in the retrieval and described in Sec. 2.3.2. As particle model, the 8-Column Aggregate (ID 8) from the ARTS SSDB is used.

The question that ~~is addressed~~ we aim to address here is whether the combination of active and passive observations is able  
 to constrain both the size and concentration of the ice particles in the cloud. To investigate this, the  $N_0^*$  and  $D_m$  parameters  
 305 of the homogeneous cloud layer are varied and observations of the cloud are simulated. The cloud signal in the radiometer  
 observations is the difference between the cloudy- and clear-sky brightness temperatures ( $\Delta T_B$ ). The signal in the active  
 observations is here defined as the maximum of the measured profile of radar reflectivity  $\text{dBZ}_{\text{max}}$ . Figure 5 displays the contours  
 of  $\Delta T_B$  and  $\text{dBZ}_{\text{max}}$  with respect to  $D_m$  and the cloud's water content, which is proportional to  $N_0^*$ :

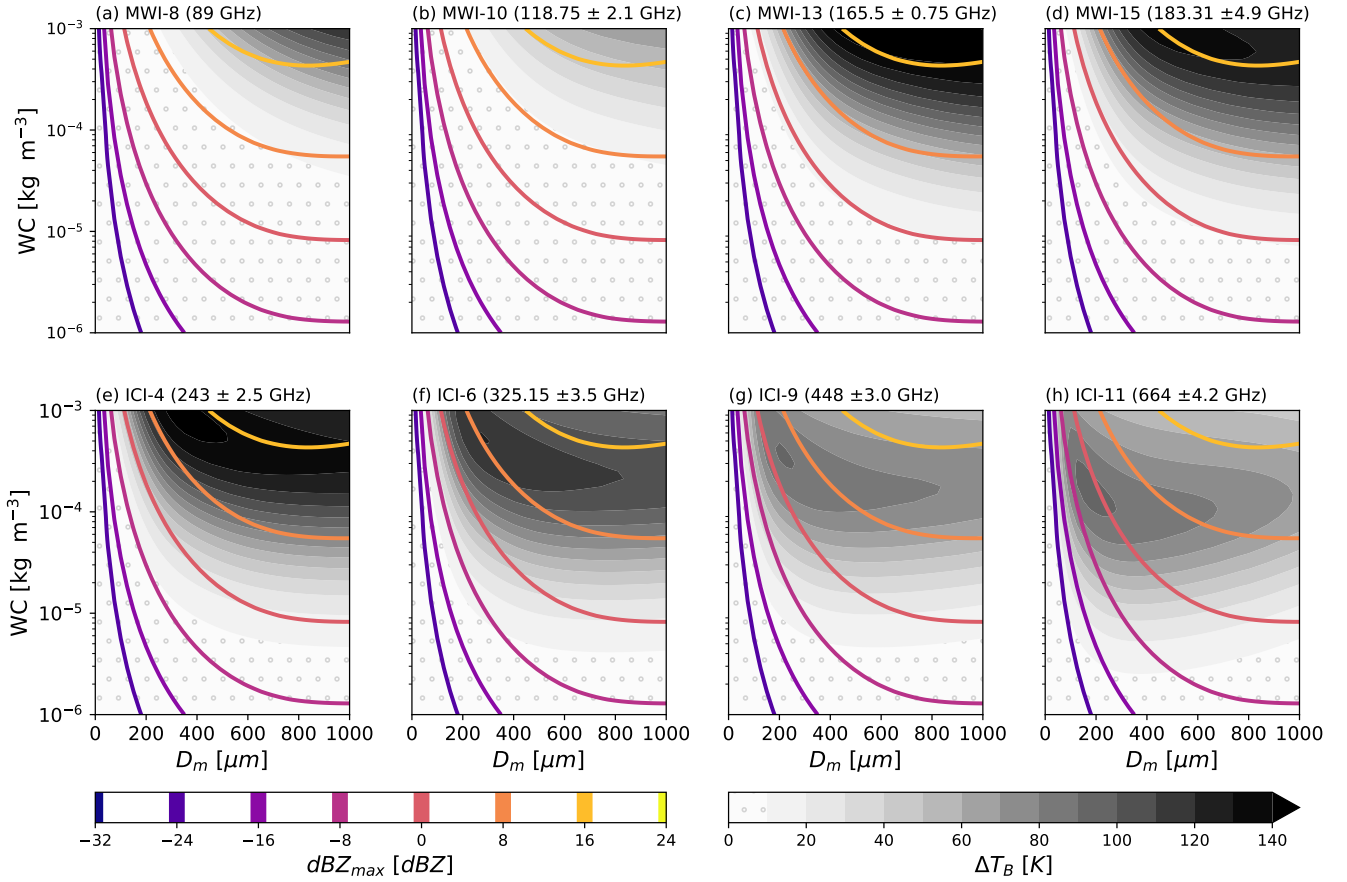
$$\text{WC} = \frac{\pi \rho}{4^4} N_0^* D_m^4, \quad (7)$$

310 with  $\rho$  the density of ice.

Along the  $\text{dBZ}_{\text{max}}$ -contours the cloud composition changes but the observed signal stays the same. This shows the ambiguity  
 of the radar observations with respect to the cloud composition. A necessary condition for a passive observation at a given  
 frequency to be able to resolve this ambiguity is that the contours of the active and passive signals cross each other. The panels  
 in Fig. 5 thus provide an indication to what extent the information in the radar measurement and the corresponding passive  
 315 radiometer channel provide complementary information on the two degrees of freedom of the PSD. The results show that  
 the MWI channels provide complementary information only for very dense clouds consisting of large particles. In contrast to  
 that, the ICI observations exhibit crossing contours already at lower water content and  $D_m$  values, indicating complementary  
 information for less dense clouds and smaller particles.

### 3.2 Retrieval results

320 To assess the performance of the combined cloud retrieval, the developed algorithm has been applied to the two designated  
 cloud scenes. The same retrievals have been performed with a radar-only and a passive-only version of the algorithm to serve  
 as baselines for the evaluation of the combined retrieval. Each retrieval was performed multiple times using the different ice  
 particle models listed in Tab. 4. Since the results for both test scenes are qualitatively similar, results from the second scene are  
 provided in App. A. Complete results for all retrieval quantities, ~~both scenes and all tested~~ test scenes and particle shapes are  
 325 provided as digital supplement to this article.

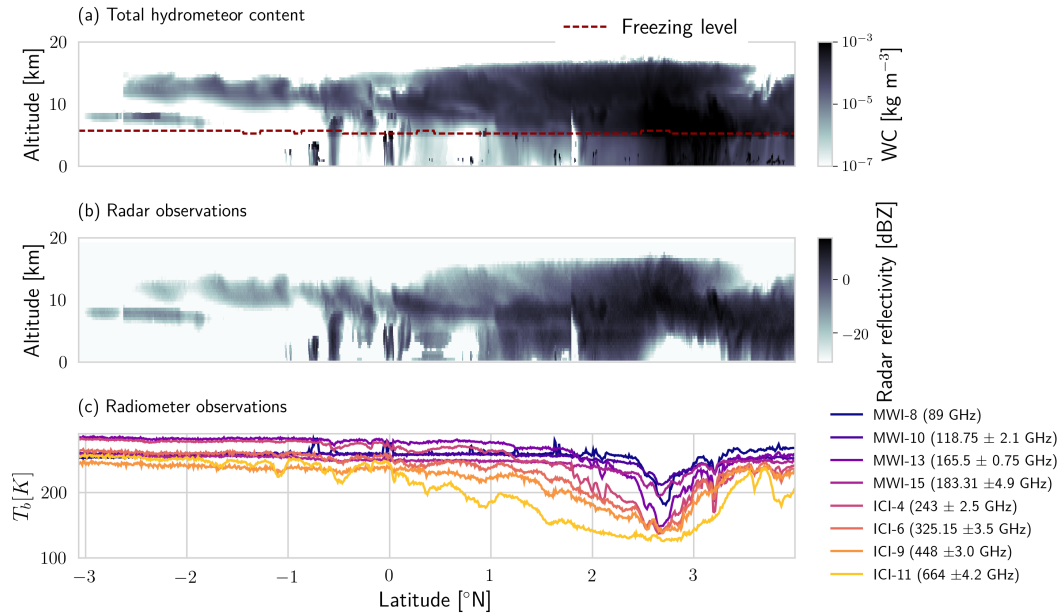


**Figure 5.** Simulated observations of a homogeneous, 5 km thick ice cloud layer centered at 10 km with varying water content  $m$  and mass-weighted mean diameter  $D_m$ . The panels display the maximum radar reflectivity in dBZ ( $\text{dBZ}_{\max}$ ) overlaid onto the cloud signal ( $\Delta T_B$ ) measured by selected radiometer channels of the MWI (first row) and ICI radiometers (second row).

The simulated observations which were generated to test the retrievals are shown for the first test scene in Fig. 6. Independent Gaussian noise with standard deviations according to sensor specifications has been added to the simulated observations to account for sensor noise. It is important to note that the simulated observations used to test the retrieval assume different microphysics than what is assumed in the retrieval. The synthetic observations are computed using the six hydrometeor classes from the GEM model, while the retrieval forward model assumes only two classes of hydrometeors.

### 3.2.1 Water content

Retrieved IWC obtained using the Large Plate Aggregate particle model for the first test scene is displayed together with the reference IWC field in Fig. 7. The reference IWC is defined here as the sum of the masses of the four frozen hydrometeor species in the GEM model scenes.



**Figure 6.** Total water content (WC) and simulated observations for the first test scene. Panel (a) displays the total water content *in the scene*, i.e. the sum of the water content of all hydrometeor species of the GEM model. Panel (b) shows the simulated radar reflectivities. Panel (c) displays the simulated brightness temperatures for a selection of channels of the MWI and ICI radiometers.

335 The normalized  $\chi_y^2$  values of the three retrieval configurations, displayed in Panel (a), give an indication of how well the retrievals are able to fit the observations. For the radar-only retrieval, the values are much smaller than 1 for most parts of the scene, while for the passive-only and combined retrieval they are around the expected value of 1. This indicates that the radar-only retrieval overfits the observations, while the passive-only and combined retrievals achieve the expected fit. The exception is the region around  $3^\circ N$  to  $3^\circ N$ , where the cloud is particularly thick and consists of a mix of different hydrometeor types. Here, especially the passive-only retrieval has problems fitting the observations.

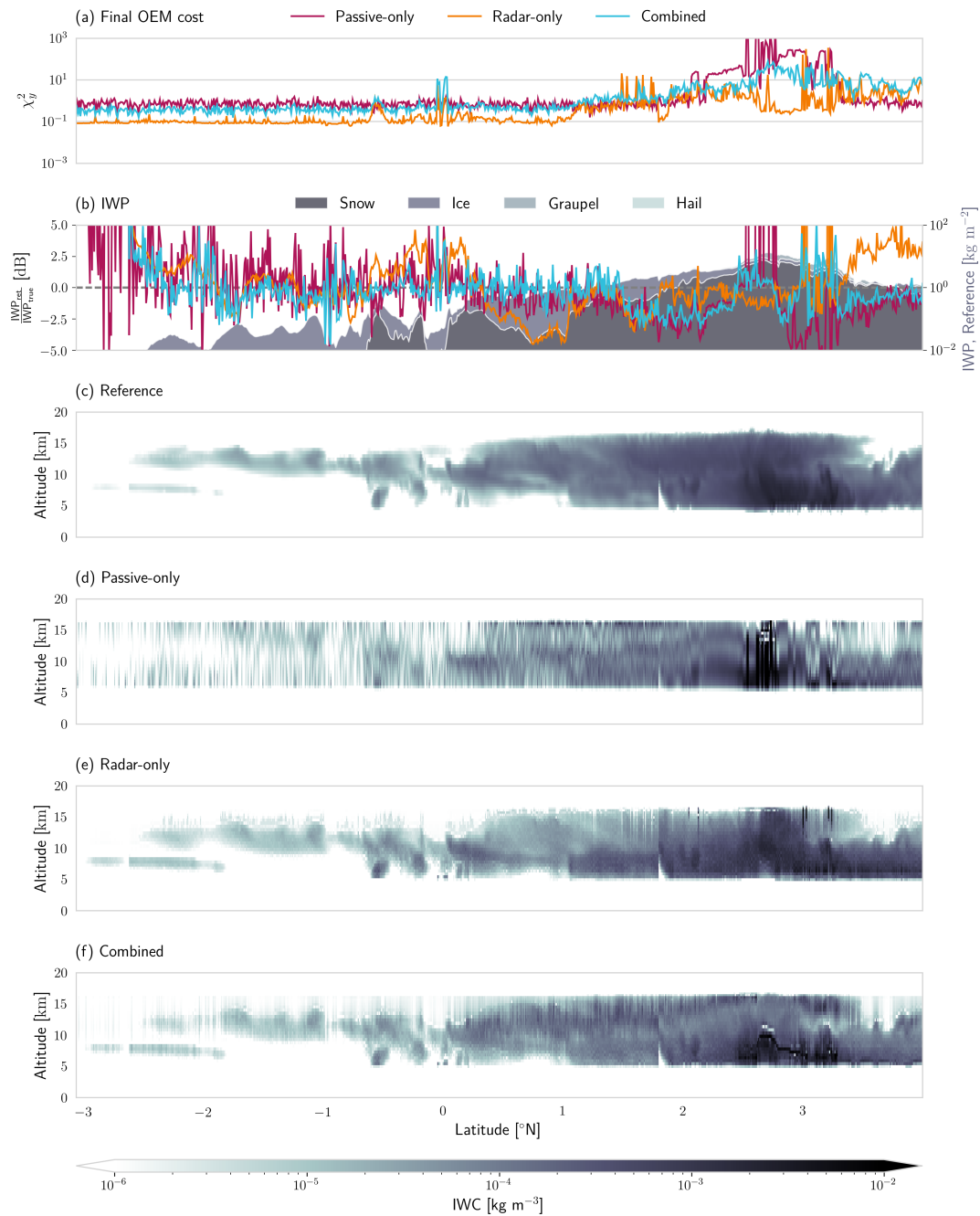
340

In terms of IWP, all methods provide fairly good estimates of the reference values with the combined retrieval consistently yielding the smallest deviations. Larger differences between the methods are observed when comparing the retrieval results in terms of IWC. While the vertical structure of the cloud is captured only very roughly by the passive retrieval, it is better resolved by the radar-only and the combined retrieval. On closer inspection, however, it becomes evident that the radar-only retrieval deviates systematically from the reference IWC in specific regions of the cloud, such as for example the upper part of the cloud between  $0^\circ N$  and  $2^\circ N$  and  $0^\circ N$  and  $2^\circ N$ . These deviations are corrected in the results from the combined retrieval, however certain retrieval artifacts remain visible.

345

For a more quantitative assessment of the retrieval performance, retrieved water content is plotted against the reference water content in Fig. 8. In terms of precision, the passive-only retrieval performs worst while both the radar-only and combined retrieval yield much smaller spread in the retrieved values. This is not surprising considering that the passive observations

350



**Figure 7.** Results of the ice hydrometeor retrieval for the first test scene using the Large Plage Aggregate particle model. Panel (a) displays the value of the  $\chi^2_y$  diagnostic normalized by the dimension of the measurement space of the corresponding retrieval. Panel (b) displays retrieved IWP in dB relative to the reference IWP. Reference IWP and the contributions from different hydrometeor classes are displayed by the filled areas in the background. Panel (c) shows the reference IWC from the model scene. Panel (d), (e) and (f) display the retrieval results for the passive-only, radar-only and combined retrieval, respectively.



do not contain sufficient information on the vertical distribution of IWC to yield accurate results at the resolution of the model scenes. In terms of overall accuracy, i.e. systematic deviations from the diagonal, no clear differences between the three configurations are visible. However, the color-coding with respect to hydrometeor species reveals that the radar-only retrieval is biased for specific hydrometeor classes. In the combined and even the passive-only results, this effect is weaker and the clusters are generally moved towards the diagonal. For graupel, all retrievals perform badly but this is likely due to it being present only in the core of the convective system where the signals from all sensors can be expected to be saturated.

Comparing the results for different particle models, a clear dependency is evident-visible in the passive-only and the combined results while the radar-only retrieval is affected the least. For the combined and passive-only retrieval, the effect is consistent across the methods, with the GEM Cloud Ice and Large Column Aggregate yielding the largest deviations and the Large Plate Aggregate yielding the most accurate results.

To summarize retrieval performance for all tested retrieval methods and particle shapes, the distributions of the logarithmic error

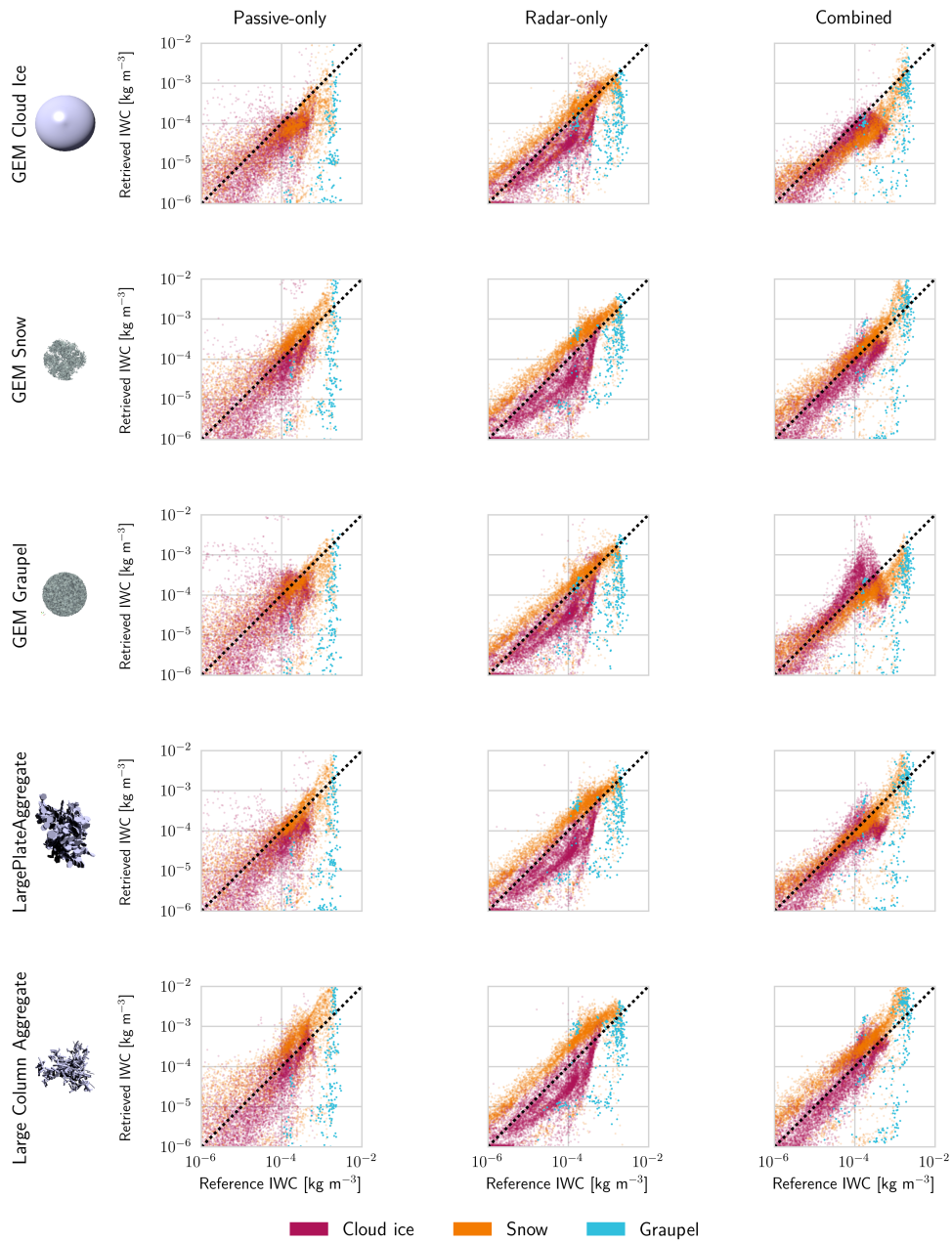
$$E_{\log_{10}} = \log_{10} \left( \frac{x_{\text{retrieved}}}{x_{\text{reference}}} \right) \quad (8)$$

for the retrieved IWC and IWP are displayed in Fig. 9. In addition to the two-moment version of the radar-only retrieval, this figure also displays results of the single-moment version of the retrieval, which was actually found to yield better IWC retrievals for the second test scene.

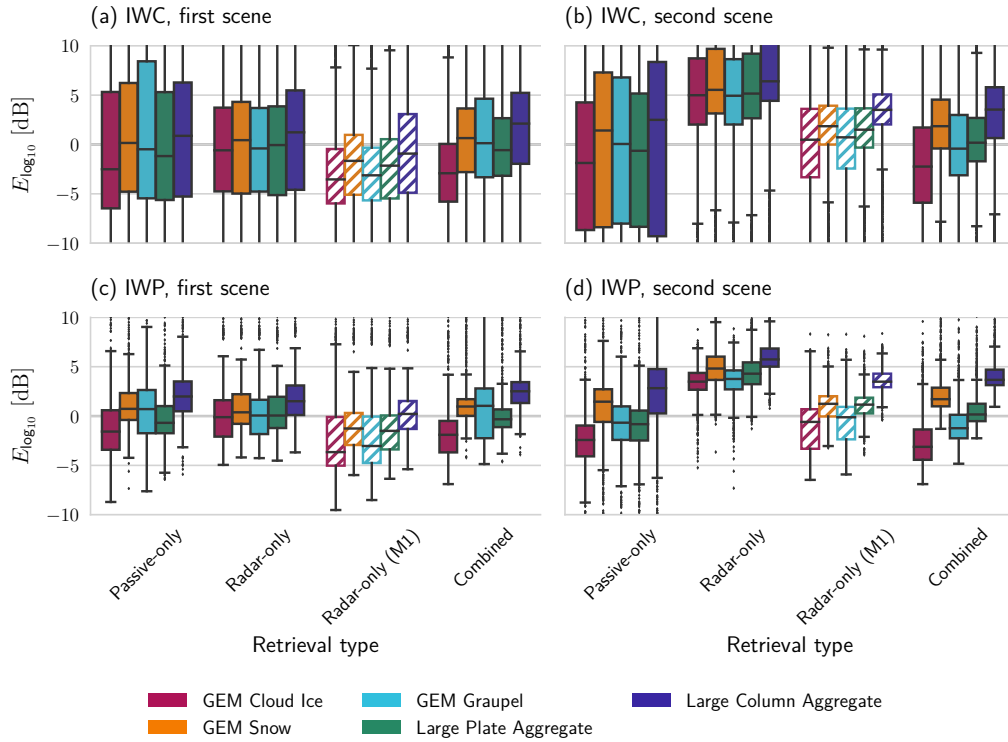
The error for IWC has been computed considering only grid points where either reference or retrieved IWC is larger than  $10^{-6} \text{ kg m}^{-3}$ . Similar to the results presented above, the combined retrieval yields the smallest retrieval errors for suitable choices of the particle model. Although the two-moment radar-only retrieval performs similar to the combined retrieval in terms of precision, it yields significant systematic errors for the second scene. The reason for this can be understood considering the cloud composition displayed in Fig. 1. Since the clouds in the second test scene consist mostly of snow, the bias of the radar-only retrieval with respect to this specific hydrometeor species (c.f. Fig. 8 and also Fig. A2) leads to the large observed systematic errors for the second scene. The single-moment radar-only retrieval does not produce the same large systematic errors for the second scene, but instead produces systematic errors for the first scene. The passive-only retrieval yields the largest errors in terms of retrieved IWC due its low vertical resolution.

In terms of IWP, however, the errors of the passive-only retrieval are decreased making the retrieval comparable to the other methods. For the radar-only and combined retrievals, the precision is generally increased but the systematic deviations observed for IWC persist. This leads, particularly for the second test scene, to significant systematic errors in the IWP retrieved by the two-moment radar-only retrieval.

Also in these results, a strong dependence on the applied particle model is observed for the passive-only and combined retrievals. The errors are particularly large for the GEM Cloud Ice and the Large Column Aggregate. Although the impact is stronger for the M1 version, the particle shape has less impact on the retrieval performance of the radar-only retrieval and does not affect the large systematic errors observed for the second test scene.



**Figure 8.** Retrieved IWC plotted against reference IWC for the tested retrieval configurations. Each row shows the retrieval results for the particle shape shown in the first panel. The following panels show the retrieval results for the passive-only (first column), the radar-only (second column) and the combined retrieval (third column). Markers are colored according to the prevailing hydrometeor type at the corresponding grid point in the test scene. Due to their sparsity, markers corresponding to graupel are drawn at twice the size of the other markers.



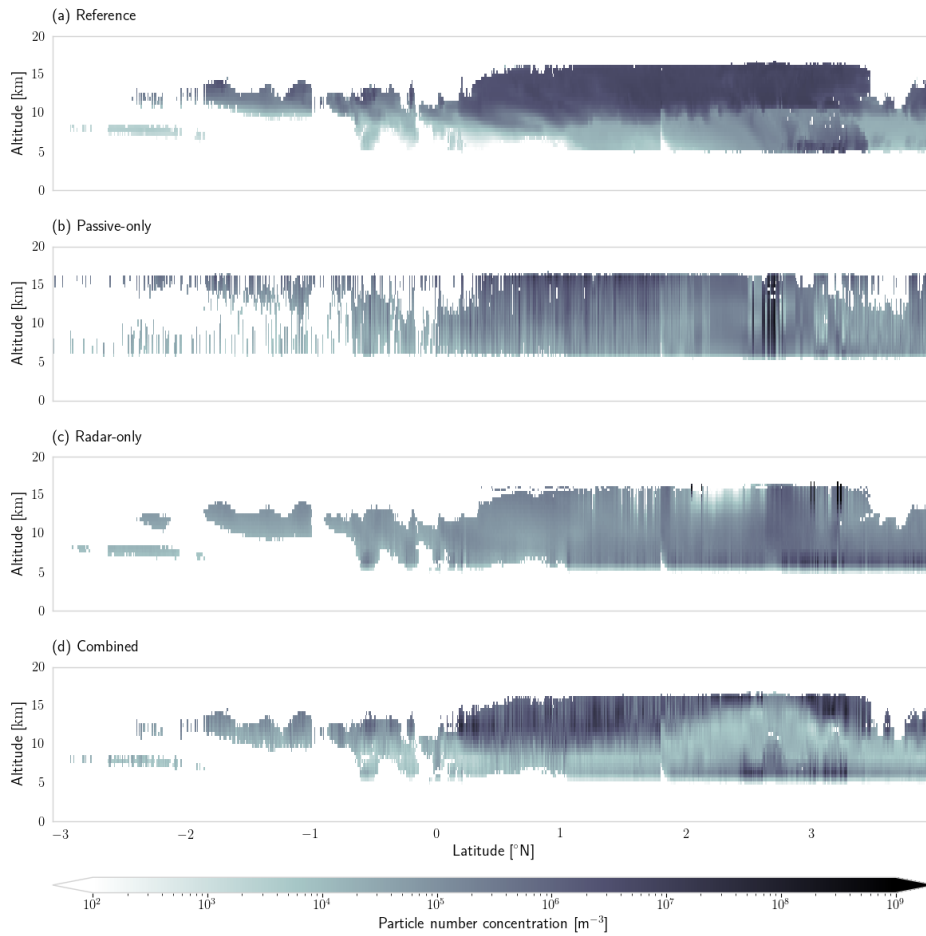
**Figure 9.** Distributions of the logarithmic retrieval error in IWC and IWP for all tested retrieval methods and particle shapes displayed as box plots. Colored boxes display the interquartile range (IQR) while whiskers show the full range of all points not considered outliers. Points whose distance to the IQR is larger than 1.5 times the width of the IQR are considered outliers and drawn as markers. Two results are shown for the radar-only retrieval, one for the standard version retrieving both PSD moments (solid boxes) and one for the single-moment (M1) version (diagonal hatches).

### 3.2.2 Particle number concentrations

385 Particle number concentrations of frozen hydrometeors have been derived from the retrieved  $N_0^*$  and  $D_m$  parameters by  
 390 computing the zeroth moment of the corresponding PSD. The resulting particle number concentration fields are displayed  
 together with the reference field in Fig. 10. To simplify the comparison, number concentrations are displayed only where the  
 corresponding reference or retrieved IWC is larger than  $10^{-6} \text{ kg m}^{-3}$   $5 \cdot 10^{-6} \text{ kg m}^{-3}$ .

Comparing the passive-only and the radar-only retrieval to the reference fields shows that both methods have little to no  
 skill in predicting number concentrations. Although the passive-only retrieval partly captures the gradient between very high  
 concentrations at the top of the cloud and the low concentrations at the bottom, it is not at all resolved in the radar-only retrieval.

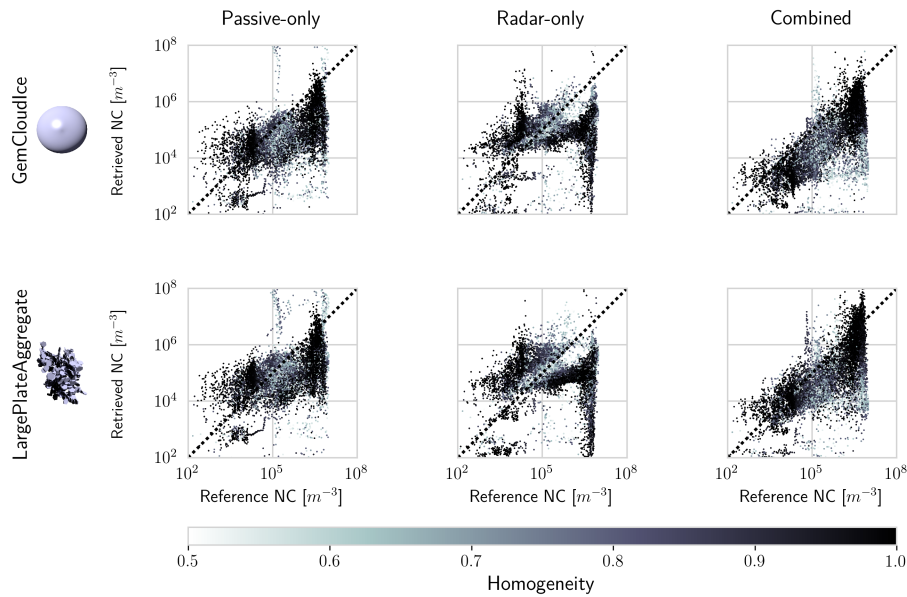
In contrast to this, the combined retrieval manages to reproduce this gradient in most parts of the scene. The strongest  
 deviations of the combined results from the reference field are observed between  $2^\circ \text{N}$  and  $3^\circ \text{N}$   $2^\circ \text{N}$  and  $3^\circ \text{N}$  latitude. Here,



**Figure 10.** Reference and retrieved particle number concentrations of frozen hydrometeors for the first test scene obtained with the ~~LargePlateAggregate~~ Large Plate Aggregate particle model. Panel (a) displays the reference ~~water content~~ number concentrations from the model scene. Panel (b), (c) and (d) display the retrieval results for the passive-only, radar-only and combined retrieval. Only values for which the corresponding reference or retrieved IWC was larger than  $10^{-6} \text{ kg m}^{-3}$   $5 \cdot 10^{-6} \text{ kg m}^{-3}$  are shown here.

the results strongly underestimate the true number concentrations. Comparison with the cloud composition displayed in Panel 395 (a) of Fig. 1 shows that this region contains large amounts of both cloud ice and snow. The retrieval uses only a single hydrometeor species to represent ice in the atmosphere and is therefore not able to represent such heterogeneous conditions. Since snow will have a stronger impact on the observations, the retrieval in these regions will likely tend to represent snow rather than ice, which leads to the low retrieved number concentrations.

Fig.Figure 11 displays scatter plots of the reference and retrieved particle number concentrations for all three methods and 400 two particle models from the first test scene. Markers in the plot are color coded according to their homogeneity in the reference scene, here defined as the ratio of the maximum water content of any of the frozen hydrometeor species and the total water



**Figure 11.** Scatter plots of the retrieved particle number concentration (NC) at grid points with reference IWC larger than  $10^{-5} \text{ kg m}^{-3}$  for [two different particle models](#). Rows show the results for the different particle models used in the retrieval while columns display results for different retrieval methods. The marker color encodes the homogeneity of the corresponding ice mass, which is computed as the ratio of the maximum water content of any of the frozen hydrometeor species and total IWC.

content. These results confirm that the passive-only retrieval possesses some sensitivity to the particle number concentrations since the cluster at low concentrations corresponding to snow is placed correctly on the diagonal, which is not the case for the radar-only retrieval. The radar-only retrieval does not exhibit any retrieval skill, hardly reproducing any of the variation of the reference values. Contrary to this, the combined retrieval moves both clusters, the one corresponding to snow and the one at high number concentrations corresponding to cloud ice, towards the diagonal. This indicates that it is capable of distinguishing the microphysical properties of cloud ice and snow. Furthermore, the color coding shows that the strongest deviations between retrieved and reference number concentrations occur for grid points where the cloud composition is heterogeneous.

The general effect of particle shape on the retrieval results is similar to what has been observed for IWC, which is why only results for two particle shapes are shown. For the passive-only and combined retrieval, the GEM Cloud Ice and Large Column Aggregate models yield the worst retrieval results, while the Large Plate Aggregate performs best. For the radar-only retrieval no noticeable differences are observed between different particle models.

### 3.2.3 Information content

To quantify the information content of the single-instrument and the combined observations, the degrees of freedom for signal (DFS) have been computed following Rodgers (2000) by calculating the trace of the averaging kernel matrix

$$\mathbf{A} = (\mathbf{K}^T \mathbf{S}_e^{-1} \mathbf{K} + \mathbf{S}_a^{-1})^{-1} \mathbf{K}^T \mathbf{S}_e^{-1} \mathbf{K}, \quad (9)$$

where  $\mathbf{K} = \frac{d\mathbf{F}(\mathbf{x})}{d\mathbf{x}}$  is the Jacobian of the forward model. The information content and its decomposition into contributions from different retrieval quantities are displayed in Fig. 12.

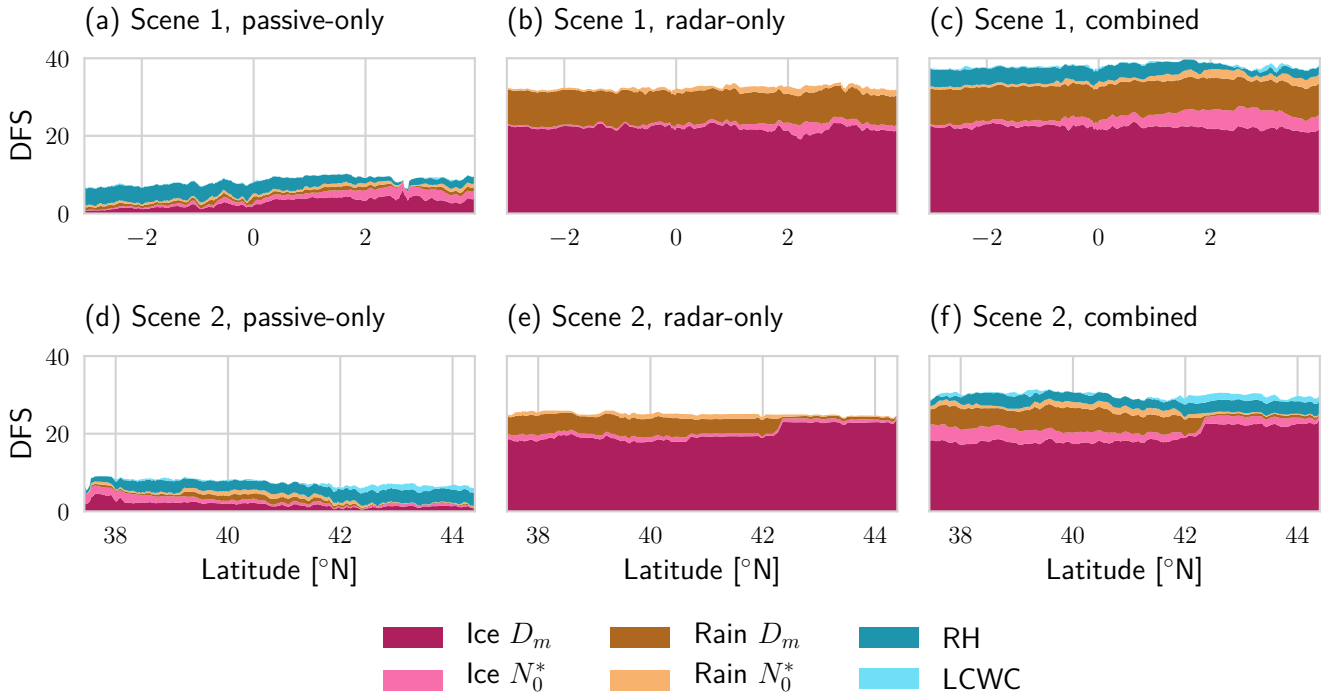
With respect to ice, the passive-only retrieval yields the lowest information content. For the radar-only retrieval the information content is significantly higher, on the order of 20 degrees of freedom, but the major part of it is attributed to the  $D_m$  parameter. For the combined retrieval, the total information content on ice hydrometeors is increased compared to the radar-only retrieval in regions where the passive-only retrieval provides information on frozen hydrometeors. In addition to that, a clear shift of information content from  $D_m$  to  $N_0^*$  can be observed over both scenes.

The information content for rain is much smaller but in relative terms the general behavior is the same as for ice. For RH, no difference is observed for the information content provided by the passive-only and combined retrievals. For LCWC, the information content of the combined observations is increased slightly but remains limited to a few degrees of freedom.

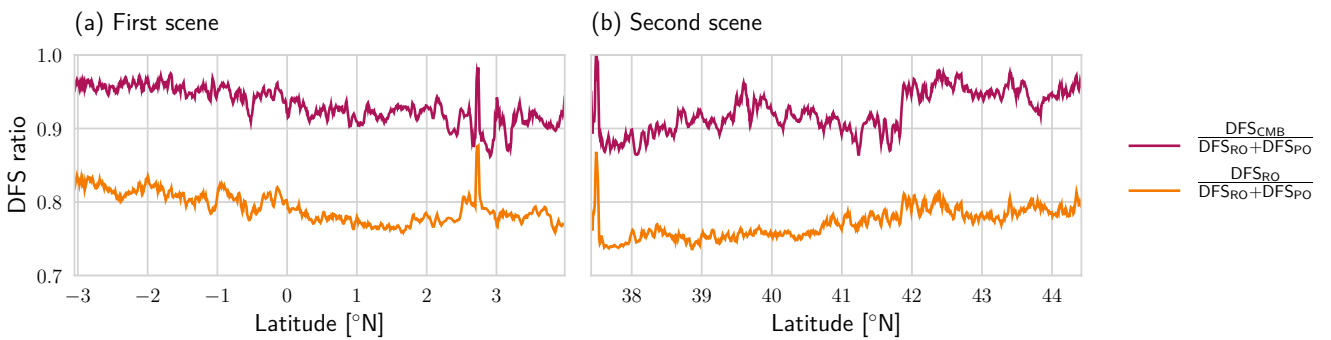
In order to allow a more detailed analysis of the complementarity of the information in the passive and active observations, Fig. 13 displays the ratio of the DFS of the combined retrieval and the sum of the DFS in the radar- and passive-only retrievals. Comparison with the information content provided by the radar-only observations confirms that the active and passive observations consistently provide a fairly high amount of complementary information across both scenes.

### 3.2.4 Impact of assumed ice particle shape

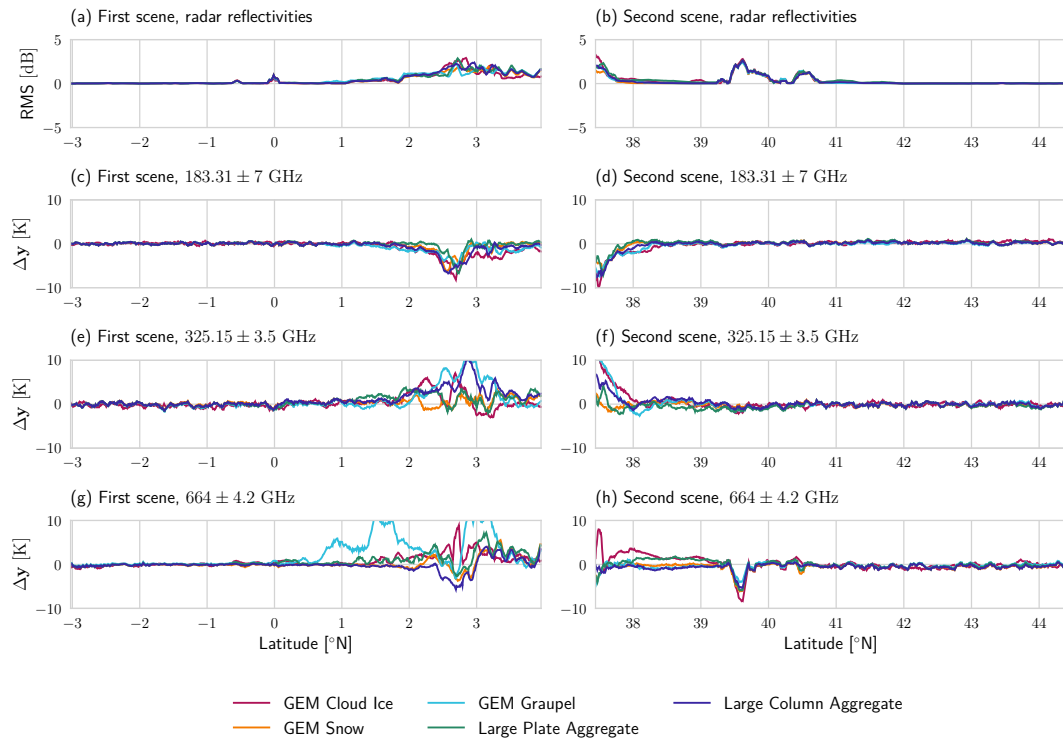
The impact of the assumed ice particle shape on the retrieval results raises the question whether it also affects the quality of the fit to the observations. To investigate this, the residuals for the radar observations and three ICI channels are displayed in Fig. 14. Each test scene contains a region where the retrieval does not fit the observations well and where substantial deviations between the fitted and true observations are observed. It is also in these regions, where the fits obtained with different particle models differ. These are both regions where the cloud is very thick and both the radar and passive observations are likely saturated. Since these are difficult regions for the retrieval it is not clear whether these differences can be related directly to the assumed particle shape. In contrast to this, the retrieval fits the observations well in the remaining parts of the scene. The exception is the GEM Graupel particle, for which quite-significant misfits are observed in the first test scene between  $0^\circ\text{N}$  and  $1^\circ\text{N}$  latitude.



**Figure 12.** Degrees of Freedom content in terms of freedom-DFS using Large Plate Aggregate for signal-for all retrieval configurations and both test scenes obtained with the Large Plate Aggregate model. The colored areas in each plot represent the contribution to the cumulative degrees of freedom from each retrieval quantity. Results for the first and second test scene are displayed in the first and second row, respectively. The first, second and third panel in each row show the results for the passive-only, radar-only and the combined retrieval.



**Figure 13.** DFS ratios of the combined retrieval ( $DFS_{CMB}$ ) and the sum of the DFS of the single-instrument retrievals ( $DFS_{RO} + DFS_{PO}$ ) as well as the radar-only retrieval and the sum of the DFS of the single-instrument retrievals for the two test scenes.



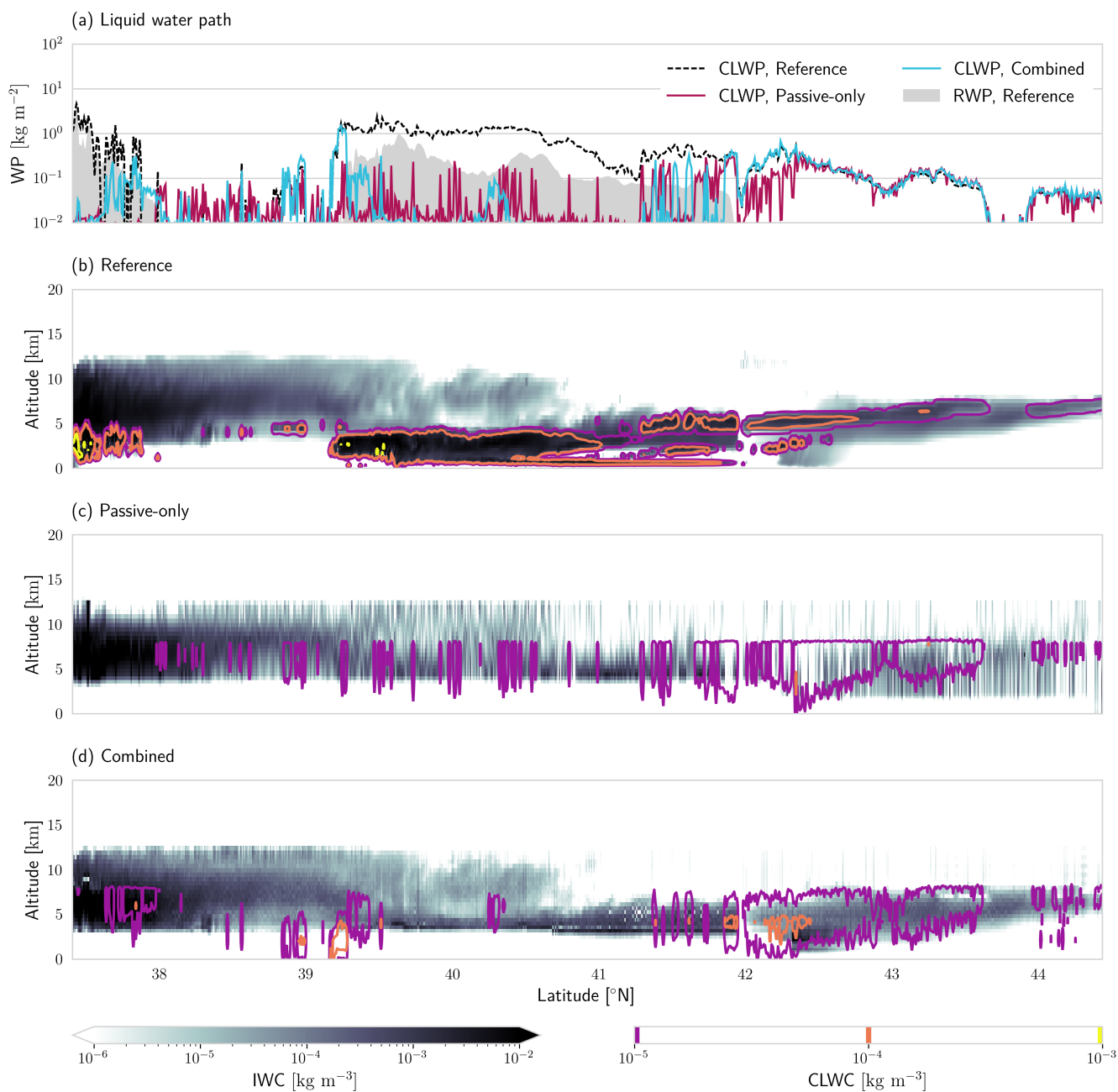
**Figure 14.** Residuals of the fitted observations. First row of panels shows the profile root mean squared error (RMS) between fitted ( $\hat{y}$ ) and true ( $y$ ) radar observations for the two test scenes. Rows 2, 3 and 4 show the residual  $\Delta y = \hat{y} - y$  for a selection of ICI channels.

### 3.2.5 Humidity and cloud water

The developed passive and combined retrieval algorithms also retrieve profiles of RH and LCWC. For RH, both retrievals demonstrate sensitivity but no improvement was observed in the results of the combined retrieval compared to the passive-only retrieval.

445 Results of the LCWC retrieval are shown in Fig. 15. For the retrieved LCWC, the combined retrieval yields slightly improved results compared to the passive-only retrieval. The improvements are observed mostly in the retrieved liquid cloud water path (LCWP) in the northern part of the scene. It should be noted that the cloud in this part is a mixed-phase cloud and that both retrievals successfully retrieve IWC and LCWC. At the center of the scene both retrievals fail to retrieve the LCWC. The reason for this ~~is that in these regions seems to be that~~ rain is present ~~in these regions~~, whose signal ~~likely swamps any signal from~~  
 450 ~~can't be separated by the retrieval from that of~~ the liquid cloud droplets.





**Figure 15.** Reference and retrieved LCWP, rain water path (RWP), CLWC and IWC. Panel (a) shows the reference and retrieved LWP for each profile. Panel (b) displays reference LWC contours drawn on top of the total hydrometeor content. Retrieval results for passive-only and combined retrieval are given in Panel (c) and (d).

## 4 Discussion

The principal aim of this study was to investigate the synergies between radar and passive sub-millimeter observations for the retrieval of frozen hydrometeors. To this end, a simplified numerical experiment has been presented, which demonstrates the existence of complementary information [on the microphysical properties of ice clouds](#) in the radar and passive microwave observations. Furthermore, a combined retrieval algorithm has been developed to demonstrate the feasibility of the synergistic retrieval and further explore ~~their~~ [its](#) potential as well as current limitations.

The novelty of this work ~~for~~ lies, in part, in the application of ICI's sub-millimeter channels, which sets it apart from the combined retrievals developed for the TRMM and GPM missions. Moreover, the development of a fully consistent variational retrieval in which all retrieval quantities are retrieved simultaneously using the observations from all sensors is ~~also novel~~ [a key aspect of this study](#). This allows comparison of the combined retrieval to equivalent radar-only and passive-only configurations and therefore a direct analysis of the synergies between the active and passive observations.

### 4.1 Fundamental synergies

The experiment presented in the first part of this study aimed to illustrate the fundamental synergies of active and passive microwave observations. It compared the cloud signals observed by a radar, a millimeter-wave radiometer and a sub-millimeter-wave radiometer. The results indicate that the combined observations can constrain the size and concentration of particles in the cloud. However, the complementary information content between the active and passive observations depends on both the properties of the observed cloud and the frequency of the observations. For the lower frequencies considered in this study, i.e. the highest frequency channels of the MWI radiometer, the regions where both observations provide complementary information on the particle size distribution of the cloud are limited to very high water content and particle sizes. It should be noted, however, that since the radar simulations neglect multiple scattering, these results may not fully carry over to space-borne observations.

As the passive observing frequency increases, the regions of complementary information content extend down to smaller particle sizes and [lower](#) water content. Especially the highest-frequency channels of the ICI radiometer can therefore be expected to provide complementary information to a W-band radar in a combined observation scenario.

### 4.2 Combined cloud retrieval

In the second part of the study, we have presented results from a combined, variational cloud retrieval applied to synthetic observations from two test scenes from a CRM. The results of the combined retrieval were compared to that of a passive- and a radar-only version of the retrieval algorithm. The simulated observations assumed an airborne viewing geometry and therefore neglected potential errors caused by different or non-overlapping antenna beams as well as inhomogeneity of the atmosphere across the beams. A source of forward model error was included by applying a more complex microphysics scheme in the simulations than the one used in the retrieval. This permits [a rough](#) assessment of the retrieval error caused by the simplified modeling of cloud microphysics in the retrieval.

### 4.2.1 Retrieval performance

Of the three considered retrieval implementations, the passive-only retrieval clearly performs worst in terms of retrieved IWC. It should be noted, however, that the passive-only retrieval presented here has not been fully optimized and should therefore not be taken as representative of the potential performance of the MWI and ICI radiometers for IWC retrievals. To ensure a fair comparison, the retrieval uses almost the same a priori assumptions as the other two retrievals, which in the presented case provide only very limited information on the vertical structure of the cloud. As has been shown also by other studies, the passive observations do provide information on the vertical distribution of ice in the atmospheric column (Wang et al., 2017; Grützun et al., 2018), but the information content is limited to a few degrees of freedom. It is therefore unlikely that the vertical resolution of the passive-only retrieval can be improved drastically without further constraining it a priori, as ~~it~~ is typically done in retrievals that use Monte Carlo integration or neural networks (Pfreundschuh et al., 2018).

With respect to IWP, however, the passive retrieval can perform as well or even better than the radar-only retrieval. Furthermore, the results in Fig. 10 indicate that the passive observations provide some information on the particle number concentrations, which is not the case for the radar observations. This shows that passive observations at multiple frequencies can **actually** constrain the microphysics better than single-frequency ~~radar-only observations alone~~ although at a much radar observations alone, albeit at lower vertical resolution.

As expected, the radar-only retrieval provides much better IWC retrievals than the passive-only version. However, the results of the two-moment retrieval exhibit systematic deviations from the reference values in certain regions of the cloud. The analysis shown in Fig. 8 and A2 reveals that these are caused by systematic errors in the retrieval of specific hydrometeor species from the GEM model. Interestingly, the ~~1M-one-moment~~ version of the radar-only retrieval did not produce the large errors in the second scene but produces systematic errors for the first test scene. This indicates that the a priori assumptions used in the retrieval do not provide a sufficiently good description of how the  $D_m$  and  $N_0^*$  parameters of the PSD co-vary and that the radar-only observations alone do not constrain both of them well enough. This is plausible also from an information content perspective since the radar provides only one piece of independent information at each range gate, which is insufficient to determine the two degrees of freedom ( $N_0^*$  and  $D_m$ ) of the PSD. This hypothesis is confirmed by the radar-retrieved number concentration fields shown in Fig. 10 and Fig. 11. While the distribution of reference values has two modes corresponding to ice and snow, the retrieved values are nearly the same throughout the whole scene indicating that the observations themselves provide almost no information on particle concentrations.

Despite certain visible artifacts in the retrieved IWC field (Fig. 7), the combined retrieval yields the best overall performance for IWC and IWP as shown in Fig. 8 and Fig. 9 given that a suitable particle model is used. The benefit of the combined observations is even more pronounced in the retrieved number concentrations (Fig. 10). Here, the passive- and radar-only retrievals show little to no skill in retrieving the number concentrations. In contrast to this, the combined retrieval was able to reproduce the general structure of the number concentration field in regions where the cloud composition is homogeneous (Fig. 11). This shows that the combined retrieval is able to distinguish the microphysical properties of ice and snow in the test

scenes. Instead of relying on the a priori, the combined retrieval can use information from the observations to constrain the cloud microphysics, which avoids the systematic errors observed in the radar-only retrievals.

The a priori assumptions used in this study were chosen similar to those of the DARDAR-CLOUD ~~product retrieval~~ since they represent well established and validated assumptions for ice cloud retrievals. The role of the a priori is to complement the observations with additional information required to make the retrieval problem tractable. For the hydrometeor retrieval this means that the a priori determines how information from the observations, which alone is insufficient to determine both degrees of freedom of the PSD, is distributed between its  $D_m$  and  $N_0^*$  parameters. For the radar-only retrieval, this works well for cloud systems containing both ice and snow but leads to biased retrievals of both IWC and IWP when this is not the case (Fig. 9). The DARDAR product ~~uses~~ resolves the ambiguity of the radar-only observations by combining the observations with ~~co-located lidar observations to resolve the ambiguity where observations from both sensors are available. As our results show~~ ~~;~~ ~~this can be achieved also by combining a lidar measurements.~~ Our results show that a similar effect can also be achieved by combining the radar with passive microwave radiometers. However, ~~while the~~ these two different types of synergies will generally be effective in different regions of the cloud: While the overlap between lidar and radar is restricted to relatively thin clouds and cloud tops (for a down-looking configuration), microwave radiometers ~~can provide sensitivity even inside thick~~ clouds will provide sensitivity further down in the cloud where particles are larger and the water content higher.

#### 4.2.2 Impact of the assumed particle shape

Our experiments show a stronger sensitivity to the assumed ice particle shape for the passive-only and the combined retrievals than the radar-only retrieval. The passive observations probe the particle at multiple frequencies and their sensitivity to particle shape, especially of the sub-millimeter channels, has been highlighted in several studies (~~Ekelund et al., 2020; Fox et al., 2019~~) ~~-(e.g. Fox et al. (2019); Ekelund et al. (2020)).~~

Only the combined retrieval was able to yield accurate IWC retrievals for both test scenes for suitable choices of the particle model. However, if an unsuitable particle shape is chosen, the induced errors may ~~actually~~ outweigh the benefits of the combined retrieval as is the case for the Large Column Aggregate and the GEM Cloud Ice shapes (Fig. 9). Judging from the particle properties displayed in Fig. 4, a likely explanation for the good performance of the Large Plate Aggregate and the GEM Graupel particle is that their properties are intermediate to those of GEM Cloud Ice and GEM Snow, which are the dominating shapes in the test scenes. For the test scenes considered here, this means that accurate IWC retrievals can be achieved using only a single hydrometeor species with suitable scattering properties which are intermediate to snowflakes and heavily rimed particles. ~~This is in agreement with Ekelund et al. (2020) who found the Large Plate Aggregate to yield good agreement with observations from the GPM Microwave Imager at  $183.31 \pm 7$  GHz.~~

The analysis of the residuals of the retrieval fit (Fig. 14) showed that the residuals for different particle shapes differ most where the ~~cloud is thick~~ clouds are thickest. Differences between ~~different~~ particles are observed, but no relationship to the retrieval accuracy in terms of IWC can be established. The GEM Graupel particle, for example, yields accurate IWC retrievals but gives the worst fit for the first test scene. A likely explanation for this is that the retrieved IWC depends mostly on the ~~efficiency with respect to water content~~ overall strength of the interaction between ~~the particle and the radiation~~ particles and

550 radiation for given water content, whereas the retrieval residual is likely ~~due to the~~ caused by relative efficiencies at different frequencies. Moreover, in the remaining parts of the scenes, there are no differences in the residuals for different particles. This means that the retrieval can fit the observations well regardless of the assumed particle shape and indicates that the observations alone do not strongly constrain the particle shape. This makes it unlikely that particle shape can be retrieved from observations, thus requiring it to be determined a priori.

555 It should be noted, that none of the presented retrievals accounts for the error caused by the simplified forward model and the choice of the particle model. This has not been pursued here because of the difficulty of fitting a suitable error model to these errors, which ~~are likely~~ can be expected to be non-Gaussian and scene-dependent. However, it is likely that accounting for them can improve retrieval performance and weaken the impact of the particle choice on the retrieval results.

### 4.2.3 Humidity and cloud water

560 As an outlook, results from the LCWC retrieval have been provided despite it not being a focus of this study. Fig. 15 shows improvements in retrieved LCWP and LCWC in the results of the combined retrieval compared to the passive-only retrieval. Although ~~also~~ the passive-only retrieval also shows sensitivity to LCWC, the results are less robust than those of the combined retrieval. This shows that combined millimeter and sub-millimeter radiometers, in particular in combination with radar observations, can be used for retrieving both frozen and liquid cloud water content in mixed-phase clouds. This conclusion is supported  
565 by the information content analysis in Fig. 12 ~~;~~ which shows that the passive observations provide some information on LCWC and that this is increased slightly for the combined retrieval. and Fig. 13. In particular, the DFS ratio of the combined retrieval shows a distinct increase around 42°N, where the scene contains non-precipitating mixed-phase clouds. This coincides with a slight increase in information content on LCWC in the combined compared to the passive-only retrieval shown in Fig. 12.

For the water vapor retrieval, no significant improvements in the combined retrieval results were observed and also the analy-  
570 sis of the information content does not show any increase in information content. This indicates that the combined observations do not provide any direct synergies for the retrieval of humidity.

### 4.2.4 Limitations

An important limitation of this study is its scope: The aim here was not to develop a production-ready combined retrieval product but rather a proof-of-concept to explore this observational approach. The retrieval results presented here should therefore  
575 not be interpreted in absolute terms. The primary results are based on the relative performances of the three retrieval methods: Given equivalent a priori assumptions, the combined retrieval demonstrates higher sensitivity to the microphysical properties than the radar-only retrieval and lower errors in terms of IWC than the passive-only retrieval.

Moreover, this study is purely based on simulations ~~and restricted to two selected model test scenes. The validity of from~~ two selected CRM scenes. These two scenes are certainly insufficient to accurately represent the variability of clouds in the  
580 atmosphere. Furthermore, the accuracy of the estimated retrieval performance will depend on the ~~presented results thus depends~~ on how well cloud microphysics are represented in the GEM model. While this may affect interpretation of the results realism of the test scenes. Because of this, this study does not aim to provide an accurate assessment of the performance of the combined

retrieval in absolute terms, ~~the main findings of this work, which are based on a relative comparison of the retrieval results, should be less dependent on the realism of the test scenes~~ but instead a qualitative assessment of the potential of a combined retrieval based on the comparison of its results to the single instrument retrievals.

As has been stated above, simulated observations used in this study ~~assumed~~ assume a viewing geometry that is realistic only for airborne observations. They therefore do not provide a realistic assessment of the potential of a space-borne satellite mission involving ICI, MWI and a W-band radar. For this it would be necessary to take into account a more realistic viewing geometry, beam-filling errors as well as multiple scattering in the radar observations. Quantifying the effect of these error sources on the retrieval synergies is left for future investigation.

## 5 Conclusions

The main conclusion from this work is that the combination of radar and sub-millimeter radiometer observations can, to some extent, constrain both the size and number concentration of frozen hydrometeors (Fig. 5). The increased sensitivity of the combined observations to the microphysical properties of hydrometeors helps to improve the accuracy of IWC retrievals and avoid systematic errors observed in an equivalent radar-only retrieval (Fig. 8, 9). Moreover, the combined retrieval showed clear sensitivity to particle number concentrations and was able to reproduce their vertical structure in regions where the cloud composition is homogeneous (Fig. 10, 11).

The results particularly highlight the importance of sub-millimeter observations for combined retrievals of frozen hydrometeors. While observations at currently available microwave frequencies provide information complementary to that from a radar only for thick clouds with very large particles ( $D_m > 800 \mu\text{m}$ ,  $\text{IWC} > 10^{-4} \text{ kg m}^{-3}$ ), frequencies above 200 GHz provide additional information on cloud microphysics (Fig. 5) at smaller particles sizes and water content ( $D_m > 200 \mu\text{m}$ ,  $\text{IWC} > 10^{-5} \text{ kg m}^{-3}$ ).

Regarding the representation of hydrometeors in the retrieval, our results indicate that complex mixes of hydrometeors can be accurately represented using a single, suitable habit mix. In particular, our results indicate that a suitable habit should have scattering properties that are intermediate between strongly rimed and more snow-flake like particles (Fig. 4, 9).

A direct application of the synergistic retrieval algorithm developed in this study are flight campaigns involving the International Sub-millimetre Airborne Radiometer (ISMAR, Fox et al. (2017)) combined for example with a radar on another aircraft or the Microwave Radar/radiometer for Arctic Clouds (MiRAC, Mech et al. (2019)). The ability of the combined retrieval to constrain two moments of the PSD of frozen hydrometeors should make it a valuable tool for validating the representation of clouds in cloud-resolving or large-eddy simulations which typically employ two-moment schemes. Moreover, since our results indicate retrieval skill also for LCWC in mixed-phase clouds, such observations can be used to study the properties of these clouds, which play an important role for the climate of the arctic. The sensitivity to LCWC of the passive observations is also a promising indication for combined ICI/MWI retrievals.

Ultimately, spaceborne combined radar and sub-millimeter observations can be a way forward towards reducing the large uncertainties in the observational record of ice hydrometeors. The Metop program provides an opportunity for a

synergistic radar mission involving the MWI and ICI radiometers. Alternatively, the combination could be realized also by a dedicated small mission, such as the Earth's Next-generation ICE mission (ENTICE) described in Jiang et al. (2019). The results presented here clearly show the potential of this approach and can provide a first step towards the development of a retrieval algorithm for a space-borne configuration. This, however, will require extending the algorithm to the more complex   
620 space-borne viewing geometry. Moreover, to quantify the potential benefits of such a mission additional studies will be required to analyze the ~~additional~~-error sources which affect spaceborne observations.

*Code availability.* All code used to produce the results in this study is available from a public repository (Simon Pfreundschuh, 2019).

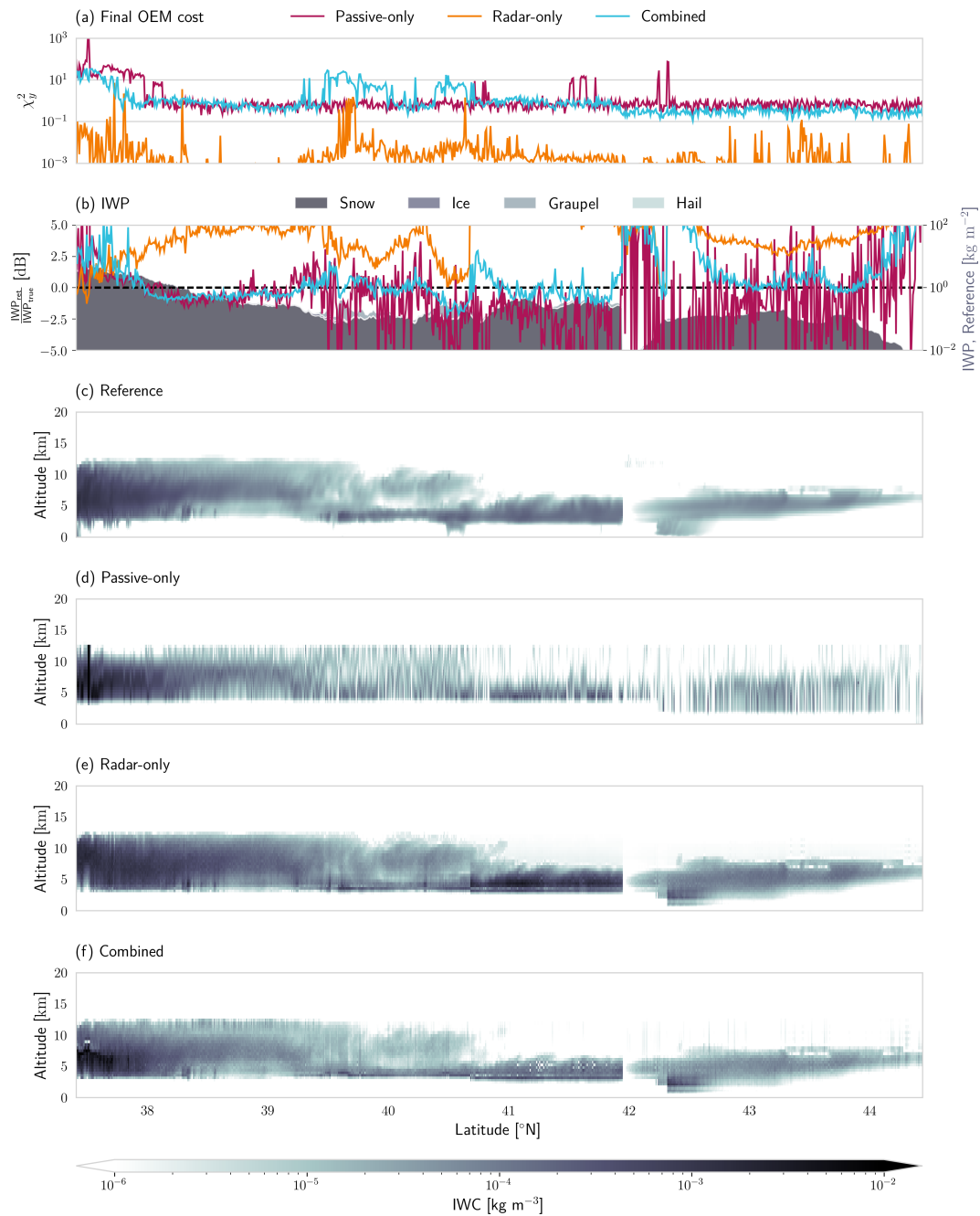
*Data availability.* Data to reproduce the simulations leading to the presented results will be made available on request.

## Appendix A: Results from second test scene

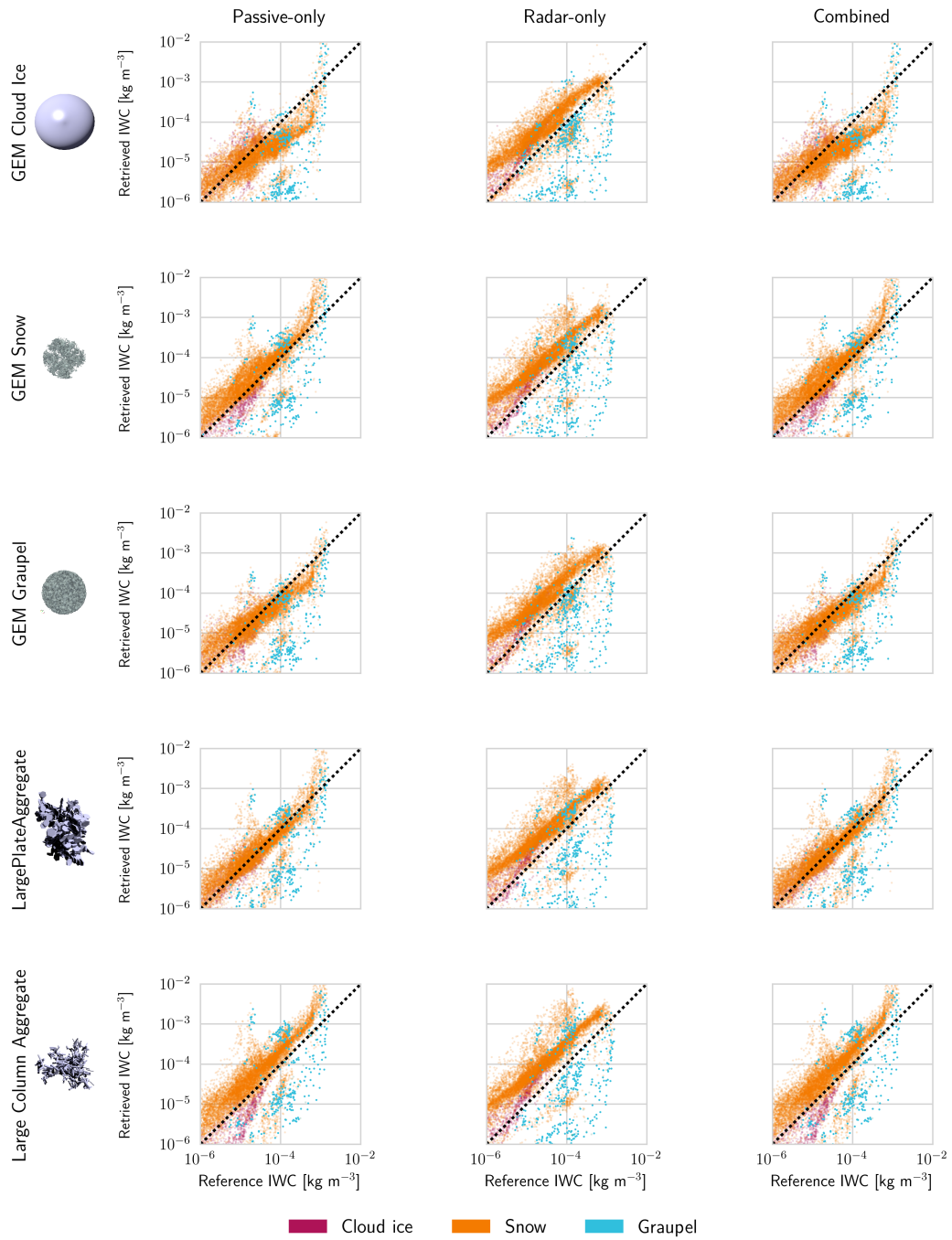
625 The retrieved IWC obtained using the Large Plate Aggregate for the second scene is shown in Fig. A1. Just as the first scene, this test scene contains a region in the south where the final OEM cost, shown in Panel (a), is increased for the passive-only and combined retrievals. This is again a region of very dense cloud consisting of graupel and snow. Qualitatively, the results of the IWC retrieval are very similar to those from the first scene. While the passive-only retrieval provides only very low vertical resolution, both the radar-only and combined retrieval reproduce the vertical structure of the cloud well. The radar-only retrieval  
630 consistently overestimates the IWC in the scene, which is not the case for the combined retrieval.

Scatter plots for the retrieval results from the second scene are shown in Fig. A2. Except for the lack of cloud ice in the scene, the results are similar to what has been observed in the first scene: The radar-only retrieval exhibits the same systematic error for the retrieval of snow as in the first scene. Again, this is corrected by the combined retrieval for most of the tested particle shapes. The exception are the GEM Cloud Ice and the Large Column Aggregate particles for which the retrieval does  
635 not perform as well.





**Figure A1.** Results of the ice hydrometeor retrieval for the second test scene. Panel (a) displays the value of the  $\chi_y^2$  diagnostic normalized by the dimension of the measurement space of the corresponding retrieval. Panel (b) shows retrieved IWP in dB relative to the reference IWP. Reference IWP and the contributions from different hydrometeor classes are displayed by the filled areas in the background. Panel (c) displays the reference mass concentrations from the model scene. Panel (d), (e) and (f) display the retrieval results for the passive-only, radar-only and combined retrieval, respectively.



**Figure A2.** Scatter plots of the reference and retrieved IWC for the second test scene. The rows show the retrieval results for a given assumed ice particle model. The first column of each row displays a rendering of the particle model. The following rows columns display the results for the passive-only, the radar-only and the combined retrieval.

*Author contributions.* Simon Pfreundschuh has implemented the retrieval, performed the data analysis and written the manuscript. Patrick Eriksson and Richard Larsson have added code to the ARTS radiative transfer model that was required to perform the presented calculations. Stefan A. Buehler, Patrick Eriksson, Manfred Brath and Simon Pfreundschuh have collaborated on the study that lead to the results presented here. David Duncan and Robin Ekelund have contributed to the conceptualization of the study through comments and advice.

640 *Competing interests.* No competing interests are present.

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The computations for this study were performed using several freely available programming languages and software packages, most  
650 prominently the Python language (The Python Language Foundation, 2018), the IPython computing environment (Perez and Granger, 2007), the numpy package for numerical computing (van der Walt et al., 2011) and matplotlib for generating figures (Hunter, 2007).

The computations were performed on resources at Chalmers Centre for Computational Science and Engineering (C3SE) provided by the Swedish National Infrastructure for Computing (SNIC).

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