

Response to Referees' Comments

S.-H. Kim, H.-Y. Chun, J.-H. Kim, R. D. Sharman, and M. Strahan

February 8, 2020

Dear editor and reviewers,

We received reviews for our manuscript “Retrieval of eddy dissipation rate from derived equivalent vertical gust included in aircraft meteorological data relay (AMDAR)”. All reviews have been beneficial and made us aware of some major and minor points which had to be reflected. We, the authors, are therefore thankful for their contribution to further improve the manuscript’s quality. We carefully addressed all comments and tried our best to improve the manuscript based on the suggestions and comments. We answer questions in the following paragraphs. Below, we indicate the original comment of the respective reviewer in blue and our answer is denoted in black. In addition, we provide a tracked-changes version of the manuscript.

Sincerely,

Hye-Yeong Chun

[Responses to the Comment by the Anonymous Referee #1]

>> We deeply appreciate the referee#1 for providing constructive comments. The manuscript is revised following the comments below.

This study attempts to map the values of a turbulence diagnostic (derived equivalent vertical gust-DEVG) to a standard measure of turbulence intensity (cube root of the eddy dissipation rate-EDR). The motivation for obtaining such a mapping is that a limited fraction of commercial aircraft report either EDR or DEVG; therefore, establishing a correspondence between the two would allow turbulence data to be collected, studied, and exploited over an expanded global area using a single, consistent metric-the aircraft-type-independent EDR. The derived relationships are based on statistical comparisons of mutually exclusive data sets for DEVG and EDR over specific world regions. Although reasonable relationships result from the analysis, because DEVG and EDR measurements were not made simultaneously on the same flights, care must be taken to assure that apples are being compared to apples. Specific comments on this and other issues are given below.

Major Comments:

1) Section 2.2: QC procedures. Quality control is absolutely critical for the DEVG data. Fits to the PDFs of DEVG (e.g., Figure 9) is at the core of this analysis. The PDF tails are very sensitive to small changes in the bin counts. However, these tails are where the raw DEVG have quite large bin counts in some regions that manifest as secondary modes in the PDF. The post-QC PDF tail is the residual of the difference between fairly large numbers. Thus, it is important to justify the QC procedure.

a. Why are there so many invalid DEVG values? Are there documented case studies that show how these errors occur? And why do they occur primarily in certain regions?

As far as we know, there is no official document on the quality issue of the derived equivalent vertical gust (DEVG) data. Instead, in the Aircraft Meteorological Data Relay (AMDAR) observing system newsletters published by the World Meteorological Organization (WMO), the horizontal distribution of the DEVG has been reported since April 2016

(<https://sites.google.com/a/wmo.int/amdar-news-and-events/newsletters/volume-11-april-2016>). As in Fig. A1, the DEVG indicates relatively large values over some regions of Australia, New Zealand, and Europe, which is a consistent distribution with the current study. It is noted that the WMO newsletter did not mention the quality of the DEVG. The possible reasons of suspicious DEVG values can be a power loss of electrical power contactor and a bug in the DEVG initialization logic, which is related to intermittently added 1-g-bias, where g is the acceleration due to gravity (D. Body, personal communication, November, 2019). Considering that the DEVG data merged point samples from many kinds of flight over the globe, and time series of the DEVG and other recorded variables are not available, it is difficult to clearly identify the reason of suspicious DEVG values. A further investigation of the quality control (QC) procedures of the DEVG remains for future work, after obtaining the time series of recorded variables. A statement is included in the revised manuscript. [Page 6, Line 6-8]

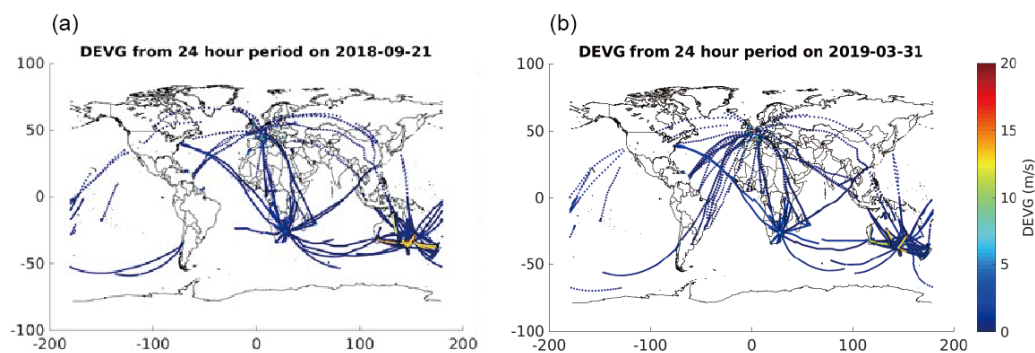


Figure A1. The horizontal distribution of the DEVG values for one day on (a) 21 September 2018 and (b) 31 March 2019, adapted from the WMO AMDAR observing system newsletter (<https://sites.google.com/a/wmo.int/amdar-news-and-events/newsletters/volume-16-october-2018> and <https://sites.google.com/a/wmo.int/amdar-news-and-events/newsletters/volume-17-april-2019>).

b. Related to (a), can you provide physical justifications for the four steps of the QC procedure?

As done in previous studies (e.g., Gill 2014; Meneguz et al. 2016; Kim et al. 2017), the minimum flight time is considered, which is set to approximately one hour within an individual file that has the same flight tail number. As the time series of recorded variables are not available, we adopt an approach that uses a cluster of the DEVG data within a certain spatiotemporal window to increase a confidence of a turbulence event. An early version of the QC procedures in the current study is designed based on those by Gill (2014) and Meneguz et

al. (2016) that used the Global Aircraft Data Set. These QC procedures to the Australian AMDAR data for four years (from 2011 to 2014) are revised through interactive discussions with two scientists affiliated in the Met Office (D. Turp and P. G. Gill, personal communications, February 2015). Again, these QC procedures are revised based on active discussions with scientists and forecasters associated in the Aviation Weather Center/NCEP (personal communications, from June to August 2018). During the QC procedures, we checked horizontal distributions of the raw and QC'd DEVG data when all moderate (MOD) and severe (SEV) turbulence events are reported. At least in the current study, the irrelevant turbulence events are discarded and a probability density function (PDF) of the DEVG follows the lognormal distribution, which is consistent with previous studies (e.g., Nastrom and Gage 1985; Frehlich 1992; Frehlich and Sharman 2004; Sharman et al. 2014; Kim et al. 2017). A statement is included in the revised manuscript. [Page 5, Line 29-33; Page 6, Line 17-19]

c. Page 5, lines 29-30 state that the threshold values used in the QC steps are empirically determined. This empirical process needs to be explained clearly in detail. How can you tell that too few or too many reports were not removed? This is crucial, because errors in this process directly affect the tails of the DEVG PDFs.

As mentioned above, the validity of QC procedures was discussed with the experts of the aircraft-based observations. In the raw DEVG data, only SEV (MOD) turbulence events were reported without MOD (LGT) turbulence event (Fig. A2), which is the most suspicious distribution. We checked all SEV and MOD turbulence events and excluded irrelevant turbulence events by comparing surrounding turbulence events. It is confirmed that the PDF of QC'd DEVG follows a lognormal distribution, as shown in Kim et al. (2017). A further investigation of the QC procedures of the DEVG remains to be accomplished in the future, after obtaining the time series of recorded variables. A statement is included in the revised manuscript. [Page 5, Line 29-33; Page 6, Line 17-19]

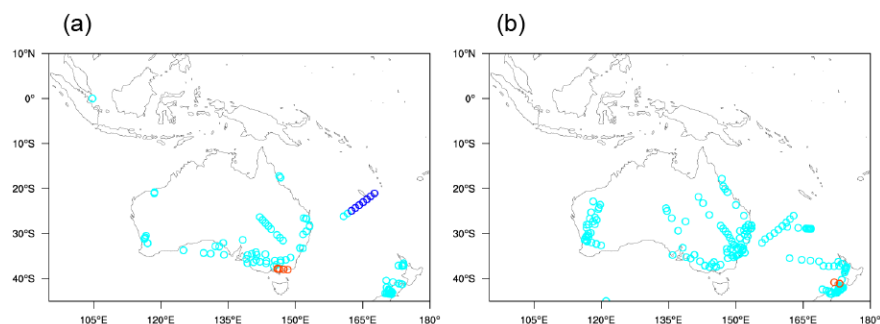


Figure A2. The horizontal distribution of the raw DEVG data for one hour of (a) 1000-1059 UTC 5 October 2015 and (b) 0100-0159 UTC 11 October 2016. The null ($\text{DEVG} < 2 \text{ m s}^{-1}$), MOD ($4.5 \leq \text{DEVG} < 9 \text{ m s}^{-1}$), and SEV ($\text{DEVG} \geq 9 \text{ m s}^{-1}$) turbulence events are indicated as cyan, blue, and red circles, respectively.

2. Is parsing DEVG PDFs by northern or southern hemisphere the most meaningful and useful classification? There are reasons why the PDFs might differ for flights (a) over land vs. over ocean, (b) at different altitudes, (c) during different seasons, (d) during day vs. night, (e) in different latitude bands, etc.

As discussed in comment #5, the reporting frequency is changed when the aircraft passes the equator, which is indicated as an abrupt change in a data count around the equator. Considering the geographical difference in the data count, the PDFs over the Northern Hemisphere (NH) and Southern Hemisphere (SH) were computed and examined in the current study. During the revision process, we examined the PDF of the DEVG over land and ocean, different altitude ranges (15-25 kft, 25-35 kft, and 35-45 kft), seasons (spring, summer, autumn, and winter), day and night, and different latitude bands of a spacing of 20° . The mean and standard deviation of the natural logarithm of the DEVG (Table A1) are not significantly changed for aforementioned conditions, except that those in latitudes equatorward of 30° are clearly smaller than those poleward of 30° . This statement is included in the revised manuscript. [Page 8, Line 12-16]

Table A1. Values of the mean and standard deviation (SD) of the natural logarithms of the DEVG. The unit is m s^{-1} .

(a) Land or Ocean			
	Land	Ocean	
Mean	-1.1610	-1.1290	
SD	0.7181	0.7881	
(b) Altitude bands			
	15-25 kft	25-35 kft	35-45 kft
Mean	-1.8025	-1.3114	-0.8702
SD	1.1149	0.7974	0.6106
(c) Seasons			

	Spring	Summer	Autumn	Winter
Mean	-1.1985	-1.2953	-1.2812	-1.2448
SD	0.7776	0.8278	0.8124	0.8005

(d) Daytime or Nighttime		
	Daytime	Nighttime
Mean	-1.2298	-1.2185
SD	0.7488	0.8277

(e) Latitude bands							
	70°S-50°S	50°S-30°S	30°S-10°S	10°S-10°N	10°N-30°N	30°N-50°N	50°N-70°N
Mean	-1.9345	-1.2325	-0.6136	-0.8136	-0.4624	-1.6851	-1.8362
SD	0.9532	0.5945	0.4269	0.7049	0.5833	1.3877	1.2280

3. As noted in p. 2, line 22, DEVG estimates may be inaccurate during ascent or descent, and, thus, the data at cruise altitudes (> 15 kft) only are used. However, even above 15 kft, aircraft can change altitudes and direction that could affect the measurements. Why not restrict the use of data by only accepting estimates made during straight-and-level flight?

Thank you for pointing out this rather important issue. Unfortunately, the AMDAR data used in the current study do not provide the phase of flight which indicates ‘level flight’, ‘ascending’, and ‘descending’. As in this study, Kim and Chun (2016) used 15 kft as the lower limit of altitude based on the time series of the DEVG and several variables recorded in the in situ flight data recorders. This statement is included in the revised manuscript. [Page 4, Line 19-21]

4. Figure 9 (and explanation in p. 7, lines 26-29). How do you justify throwing out some of the points in the PDFs for the fitting procedure?

At the highest bins, there are not enough data for reliable lognormal fits, while at the lowest bins, instrument noise may be affecting the result and the small DEVG values corresponding to nonturbulent conditions are not of practical interest. This statement is included in the revised manuscript. [Page 8, Line 8-10]

5. In Figures 1 and 8, there is an oddly abrupt change in the data count right around the equator over the central Pacific. There is much more data across a wider swath south of the equator. Is this real? What is the cause of this sharp transition?

The abrupt change in the data count around the equator can be found in the WMO AMDAR observing newsletter (Figs. A1 and A3), which is consistent with the current study (Fig. 1 of the original manuscript). For some reasons, when the aircraft passes the equator, the reporting frequency is changed from relatively lower to higher or higher to lower (Figs. A3 and A4). This difference in the reporting frequency between the NH and SH brings a sharp transition between two hemispheres. The abrupt transition across the equator may be related to systematic settings in aircraft-to-ground reporting during navigation. As the raw DEVG data indicate the abovementioned features, we would like to mention that this can be one of the characteristics of the DEVG data included in the AMDAR data and therefore the DEVG data can provide much more turbulence observations over the SH. This statement is included in the revised manuscript. [Page 4, Line 16-19]

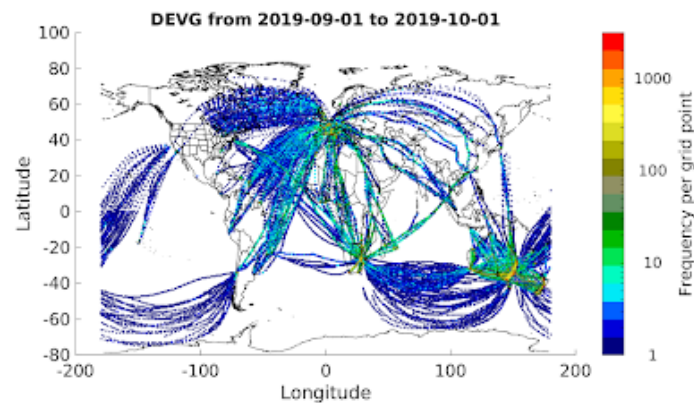


Figure A3. The horizontal distribution of the number of the DEVG data, accumulated within a 50×50 km grid box from 1 September to 1 October 2019. Adapted from the WMO AMDAR observing system newsletter (<https://sites.google.com/a/wmo.int/amdar-news-and-events/newsletters/volume-18-october-2019>).

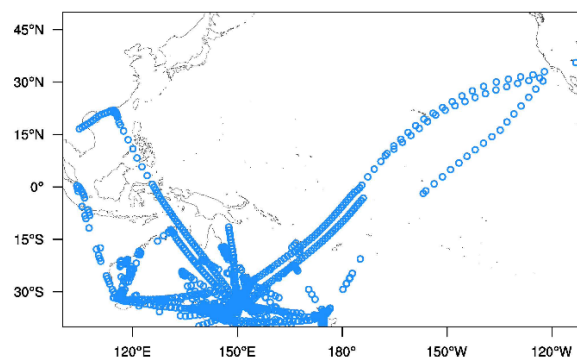


Figure A4. The horizontal location of the DEVG reports of the same flight tail number for one day (5 October 2015).

Minor Comments:

1. DEVG and EDR have different units. Is there a physical basis on which to make a unit conversion? Or is there an explanation of why it is acceptable to ignore the difference in units?

As written in the original manuscript (section 3.1), a simple mapping equation from a certain turbulence diagnostics D to the EDR was proposed by Sharman and Pearson (2017) using the observed in situ EDR data. First, turbulence diagnostics D and the EDR are standardized as:

$$X_1 = \frac{\ln(D^*) - \langle \ln(EDR) \rangle}{SD \ln(EDR)}, \quad (1)$$

$$X_2 = \frac{\ln(D) - \langle \ln(D) \rangle}{SD \ln(D)}, \quad (2)$$

where the angle brackets indicate an ensemble mean, SD is a standard deviation, D^* is the remapped EDR value corresponding to the raw turbulence diagnostics, and EDR is the in situ EDR values. Second, two standardized values, X_1 and X_2 , are set to be equal and Eqs. (1) and (2) can be combined as:

$$\ln(D^*) = \langle \ln(EDR) \rangle + \frac{SD \ln(EDR)}{SD \ln(D)} \{ \ln(D) - \langle \ln(D) \rangle \}. \quad (3)$$

Therefore, Eq. (3) is written as the simple form as:

$$\begin{aligned} \ln(D^*) &= \ln(EDR) = a + b \ln(D), \\ a &= \langle \ln(EDR) \rangle - b \langle \ln(D) \rangle, \text{ and} \\ b &= \frac{SD \ln(EDR)}{SD \ln(D)}. \end{aligned} \quad (4)$$

In the current study, the turbulence diagnostics D is replaced with the DEVG value as:

$$\begin{aligned} \ln(DEVG^*) &= \ln(EDR) = a + b \ln(DEVG), \\ a &= \langle \ln(EDR) \rangle - b \langle \ln(DEVG) \rangle, \text{ and} \\ b &= \frac{SD \ln(EDR)}{SD \ln(DEVG)}. \end{aligned} \quad (5)$$

where $DEVG^*$ is the remapped EDR value corresponding to the DEVG value included in the AMDAR data. In this regard, it is acceptable to ignore a difference in units, although the EDR is a direct turbulence intensity metric, while the DEVG is not a direct turbulence intensity metric but a gust-load transfer factor.

2. Page 6, lines 6-7: It's not very informative that some MOD and SEV turbulence reports coincide with a high Ellrod1 index. Unless a statistical analysis is conducted to show a meaningful correlation, this remark should be omitted.

We agree with the reviewer and the sentence is deleted in the revised manuscript.

References

- Frehlich, R., 1992: Laser scintillation measurements of the temperature spectrum in the atmospheric surface layer. *J. Atmos. Sci.*, **49**, 1494-1509, doi:10.1175/1520-0469(1992)049<1494:LSMOTT>2.0.CO;2.
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and derived climatologies of automated in situ eddy-dissipation-rate reports of atmospheric turbulence, *J. Appl. Meteor. Climatol.*, **53**, 1416-1432, doi:10.1175/JAMC-D-13-0329.1.

[Responses to the Comment by the Anonymous Referee #3]

>> We deeply appreciate the referee#3 for providing constructive comments. The manuscript is revised following the comments below.

General comments:

This paper investigates two methods of converting derived equivalent vertical gust (DEVG) turbulence measurements to the preferred ICAO standard turbulence metric eddy dissipation rate (EDR), using 3 years of archived AMDAR measurements. The two methods explored were proposed in two previous studies. The original DEVG measurements were subjected to a comprehensive quality control process which is described in detail. The accuracy of the resulting converted EDR values were examined by comparing them statistically to in-situ EDR turbulence measurements over two regions: over Europe and over the trans-Pacific Ocean area. The whole process is well described and discussed. The results of this study would enable a wider range of homogenized aircraft observations of turbulence to be available for development and research work. This would aid the development of turbulence forecasts and enable the construction of an upper-level turbulence climatology over a much larger area of the globe. In general, the paper is well written and well organised, and the results are of considerable interest. I therefore recommend that this manuscript should be accepted for publication with (very) minor revisions.

Specific comments:

1) Page 8, Line 8: I didn't follow why only one of the equations in the best-fit function was used, rather than the correct equation for the aircraft type recoding the DEVG. Is it that the aircraft type was missing from some of the observations in the dataset, so you needed to choose one equation?

The aircraft-related information, such as aircraft type and tail number, is limited in the Aircraft Meteorological Data Relay (AMDAR) dataset. Kim et al. (2017) showed that the two turbulence indicators [the cube root of eddy dissipation rate (EDR) and derived equivalent vertical gust (DEVG)] from Boeing aircraft have higher correlation than those from Airbus aircraft, which is related to differences in the number of decimals and sampling frequency of

the recorded variables for each aircraft type [Table 1 of Kim et al. (2017)]. In this regard, we decided to use the best-fit curve from the Boeing aircraft. This statement is included in the original manuscript.

Technical corrections:

1) Page 1, Line 12: ... in the AMDAR **data** archived ...

The sentence is modified as suggested. [Page 1, Line 12]

2) Page 1, Line 15: The first method **remaps** the DEVG ...

The sentence is modified as suggested. [Page 1, Line 15]

3) Page 1, Line 16: ... while the second one **uses** the best-fit curve ...

The sentence is modified as suggested. [Page 1, Line 16]

4) Page 1, Line 16: “developed in the previous study”. Which previous study was this (I don’t think it’s been mentioned yet)? Perhaps this part should be deleted, or written as: ... developed in **a** previous study.”

The sentence is modified as suggested. [Page 1, Line 16]

5) Page 3, Line 1: some aircraft of **a** Hong-Kong based airline.

The sentence is modified as suggested. [Page 3, Line 1]

6) Page 3, Line 10: “Because **the** two aforementioned turbulence metrics ...”. Actually, I’d re-write this sentence as “As these two turbulence metrics ...” which sounds clearer?

The sentence is modified as suggested. [Page 3, Line 10]

7) Page 3, Line 10: different **airlines**

The sentence is modified as suggested. [Page 3, Line 10]

8) Page 3, Line 14: This may be better worded as “This will lead to improvements in the verification of ...”?

The sentence is modified as suggested. [Page 3, Line 13]

9) Page 3, Line 14: “as well as global climatology of aviation turbulence”. This would be better as “as well as aid the construction of a global climatology of aviation turbulence”, or similar ?

The sentence is modified as suggested. [Page 3, Line 14]

10) Page 3, Line 19: either “some aircraft of a Hong-Kong based airline” or “some aircraft of the Hong-Kong based airline”

The sentence is modified as suggested. [Page 3, Line 19]

11) Page 3, Line 20: (39 months from February 2011 to April 2014) of data.

The sentence is modified as suggested. [Page 3, Line 20]

12) Page 3, Line 25: delete the hyphen between “(NOAA)” and “archives”.

The hyphen between “NOAA” and “archives” is deleted in the revised manuscript.

13) Page 4, Lines 9-11: I would switch the first two sentences around, so it is something like: “The data before the QC procedures have been applied are referred to as the raw DEVG in the current study. Figure 1 shows the horizontal distribution of the number of raw DEVG data collected over 36 months (from October 2015 to September 2018) above 15 kft accumulated within a $1^{\circ} \times 1^{\circ}$ horizontal box. The raw DEVG covers a large portion of the SH ...”.

The sentence is modified as suggested. [Page 4, Line 8-10]

14) Page 4, Line 13: “this raw DEVG can complement the SH turbulence information” I didn’t follow this ... the raw DEVG data complements the in-situ data (which mainly covers the NH), as it provides coverage over the SH. I think this line just needs re-wording?

We would like to emphasize that the raw DEVG data will complement the Southern Hemisphere (SH) turbulence information, given that the in situ EDR data covered most the Northern Hemisphere (NH) (Figure 10 of the original manuscript) and did not provide coverage over most SH regions. The sentence is modified as suggested. [Page 4, Line 12-13]

15) Page 5, Line 11: I would replace “That is, because” with “Since”?

The sentence is modified as suggested. [Page 5, Line 15]

16) Page 5, Line 23: I would replace “Applying the aforementioned QC procedures” with “Applying these QC procedures”

The sentence is modified as suggested. [Page 5, Line 28]

17) Page 7, Lines 18-20: I got a bit confused with the first half of this sentence. Do you mean that there’s a choice of several values of C_1 and C_2 for the altitude ranges in this study? And if so, isn’t there a choice of 4 values? Or did I misunderstand something? I would also re-word the part in brackets so it is shorter and simpler – e.g., ... for three altitude ranges (> 0 ft, 20-45 kft, 10 – 20 kft and 20 – 45 kft).

To avoid any confusion, the sentence is modified. [Page 8, Line 1-2]

18) Page 10, Line 19: “homogenized global turbulence **dataset**” or “homogenized global turbulence **archive**”

The sentence is modified as suggested. [Page 11, Line 4]

References section:

1) There were several references listed here which I couldn’t find in the contents of the paper: Gultepe et al. (2019), Tvaryanas (2003), Warner (2013), Williams (2017).

The aforementioned references are deleted in the revised manuscript.

References

- Kim, S.-H., H.-Y. Chun, and P. W. Chan, 2017: Comparison of turbulence indicators obtained from in situ flight data. *J. Appl. Meteor. Climatol.*, **56**, 1609-1623, doi:10.1174/JAMC-D-16-0291.1
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Retrieval of Eddy Dissipation Rate from Derived Equivalent Vertical Gust included in Aircraft Meteorological Data Relay (AMDAR)

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Abstract. Some of the Aircraft Meteorological Data Relay (AMDAR) data include a turbulence metric of the derived
10 equivalent vertical gust (DEVG), in addition to wind and temperature. As the cube root of the eddy dissipation rate (EDR) is
the International Civil Aviation Organization standard turbulence reporting metric, we attempt to retrieve the EDR from the
DEVG for more reliable and consistent observations of aviation turbulence globally. Using the DEVG in the AMDAR data
archived from October 2015 to September 2018 covering a large portion of the Southern Hemisphere and North Pacific and
North Atlantic Oceans, we convert the DEVG to the EDR using two methods, after conducting quality control procedures to
15 remove suspicious turbulence reports in the DEVG. The first method ~~is to remap~~remaps the DEVG to the EDR using a
lognormal mapping scheme, while the second one ~~is using~~uses the best-fit curve between the EDR and DEVG developed in
~~the~~a previous study. The DEVG-derived EDRs obtained from the two methods are evaluated against in situ EDR data reported
by United States-operated carriers. For two specified regions of the trans-Pacific Ocean and Europe, where both the DEVG-
derived EDRs and in situ EDRs were available, the DEVG-derived EDRs obtained by the two methods are generally consistent
20 with in situ EDRs, with slightly better statistics by the first method than the second one. This result is encouraging for extending
the aviation turbulence data globally with the single preferred EDR metric, which will contribute to the improvement of global
aviation turbulence forecasting as well as to the construction of the climatology of upper-level turbulence.

1 Introduction

Turbulence observations are routinely provided verbally by pilots in the form of pilot reports (PIREPs). There may
25 be an uncertainty in the intensity, timing, and location of turbulence encounters in PIREPs (Schwartz, 1996; Sharman et al.,
2006, 2014), as the turbulence intensity in PIREPs is determined by a pilot's subjective ~~measure~~experience of the aircraft
response to turbulence. Although PIREPs provide subjective categorized turbulence intensity scales (null, light, moderate, and
severe), the interpretation is aircraft dependent and null reports of turbulence events are not routine, therefore PIREPs are not
adequate for constructing reliable maps of turbulence levels. To address this deficiency, ~~the~~ automated objective aircraft-based
30 reports of turbulence are essential.

The Aircraft Meteorological Data Relay (AMDAR) system has been developed and operated by the World Meteorological Organization (WMO) as an operational observing system of automated aircraft weather observations. Given that the AMDAR data can provide routinely global atmospheric observations ranging from the surface to the upper air, these AMDAR data have been widely applied for monitoring and predicting weather systems and improving numerical weather prediction (NWP) models (e.g., Moninger et al., 2003). In addition to temperature and wind that are mandatory variables to report, two turbulence metrics are recommended to be included in the AMDAR data as measures of turbulence (WMO, 2003): the cube root of the eddy dissipation rate (EDR) (Sharman et al., 2014) and the derived equivalent vertical gust velocity (DEVG) (e.g., Hoblit, 1988).

The DEVG was introduced by Pratt and Walker (1954) and approximated to simplify the implementation (Sherman, 1985; Truscott, 2000) as:

$$DEVG \text{ (m s}^{-1}\text{)} = \frac{Am|\Delta n|}{V_c}, \quad (1)$$

where parameter A is the aircraft-specified parameter, m is aircraft mass, Δn is the maximum value of the deviation of vertical acceleration from 1 g over a specified time interval, and V_c is the calibrated air speed. For aircraft types, parameter A can be approximated as

$$A = \bar{A} + c_4(\bar{A} - c_5) \left(\frac{m}{\bar{m}} - 1 \right), \quad (2)$$

$$\bar{A} = c_1 + \left(\frac{c_2}{c_3 + H} \right), \quad (3)$$

where H is the altitude in kft, \bar{m} is the reference mass of the aircraft, and c_1 , c_2 , c_3 , c_4 , and c_5 are empirical constants dependent on the aircraft type that were given in Truscott (2000).

Due to the empirical parameters such as c_1 , c_2 , c_3 , c_4 , and c_5 in Eqs. (2) and (3), the DEVG could still include some uncertainties, which are assumed to be negligible after the rigorous quality control (QC) procedures in the current study. It is also noted that the DEVG does not consider the impact of pitch damping due to the autopilot (WMO, 2003; Kim et al., 2017). Since the DEVG can contain misleading values during the ascent and descent phases, previous studies have only considered the cruise-level DEVG values (e.g., Gill, 2014; Kim and Chun, 2016; Meneguz et al., 2016; Kim et al., 2017). The turbulence information defined by the DEVG has been utilized in statistical analyses on aviation turbulence (e.g., Kim and Chun, 2016; Kim et al., 2017) and in evaluations of the performances of NWP-based turbulence forecasts (e.g., Gill, 2014; Gill and Buchanan, 2014; Kim and Chun, 2016). Currently, the DEVG algorithm has been implemented on several international air-carriers such as the Qantas, South African, British Airways, and other European-based airline aircraft.

The EDR is estimated using aircraft vertical acceleration or estimated vertical wind velocity (MacCready, 1964; Cornman et al., 1995; Haverdings and Chan, 2010; Sharman et al., 2014; Cornman, 2016). The vertical winds-based EDR algorithm developed by the National Center for Atmospheric Research (NCAR) (Sharman et al., 2014; Cornman, 2016) is currently implemented on some fleets of the United Airlines, Delta Air Lines, and South-west Airlines, while that developed

by Haverdings and Chan (2010) is tested on some aircraft of a Hong Kong-based airline. Although Haverdings and Chan (2010) estimated the EDR in a similar way to Cornman (2016), they adopted the different angle-of-attack calibration and different time window and this may cause a difference between two EDRs. The EDR is more useful than the DEVG for turbulence metric detection and forecasting applications (Sharman et al., 2014), given that the DEVG is not a direct turbulence intensity metric but a gust-load transfer factor. Indeed, the International Civil Aviation Organization (ICAO) assigned EDR as the preferred and standard metric for turbulence reporting (ICAO, 2001, 2010; Sharman et al., 2014). The EDR has been widely used in evaluations of the performances of global turbulence forecasting systems (e.g., Pearson and Sharman, 2017; Sharman and Pearson, 2017; Kim et al., 2018; Lee and Chun, 2018), as well as in many case studies on turbulence (e.g., Trier et al., 2012; Bramberger et al., 2018; Trier and Sharman, 2018).

~~Because~~As these two ~~aforementioned~~ turbulence metrics have been reported from different ~~airliners~~airlines, the EDR covers most areas in the Northern Hemisphere (NH), while the DEVG has been reported over a large portion of the Southern Hemisphere (SH). To complement the limited availability of global turbulence observations, in the current study, we attempt to convert the DEVG of the AMDAR data to the EDR to obtain more reliable and consistent observations for aviation turbulence. This will lead to ~~improve~~improvements in the verification of global aviation turbulence forecasts as well as ~~the~~ construction of a global climatology of aviation turbulence.

The relationship between the EDR and DEVG has been studied using flight data (e.g., Stickland, 1998; Kim et al., 2017). Stickland (1998) conducted a direct comparison between a vertical acceleration-based EDR and DEVG time series of Qantas Airways Boeing 747 data over a 3-month period (from October to December 1997) and showed that the two turbulence metrics are roughly correlated; however, this study considered a limited data period and only one aircraft type. Kim et al. (2017) compared the EDR from some aircraft of the Hong Kong-based airline (Haverdings and Chan, 2010) and the DEVG from the same aircraft using a relatively long period (39 months from February 2011 to April 2014) of data. Kim et al. (2017) developed the best-fit curves between the EDR and DEVG for Airbus and Boeing aircraft data, separately. Although it was not directly used for the conversion of the DEVG to the EDR, Sharman and Pearson (2017) suggested a methodology to convert various turbulence diagnostics to the EDR by assuming that the turbulence diagnostics follow a lognormal distribution at upper levels. Here we propose to use this technique to convert the DEVG to the EDR.

For homogenized global aviation turbulence observations, in the current study, we convert the DEVG to the EDR using two conversion methods, one based on Sharman and Pearson (2017) and the other based on Kim et al. (2017), using historical DEVG records in the AMDAR National Oceanic and Atmospheric Administration (NOAA) ~~+~~ archives (hereafter, DEVG) dataset for 36 months (October 2015–September 2018). This paper is organized as follows. In section 2, the descriptions of the DEVG data, QC procedures applied on the DEVG data, and the QC'd DEVG statistics are provided. In section 3, the conversion methods from the DEVG to the EDR and the DEVG-derived EDR statistics are examined. In section 4, a summary and discussion are provided.

2 Data and methodology

~~The~~We used the AMDAR data archived at NOAA include both the EDR and DEVG from October 2015 to September 2018. Ideally, DEVG-based data and EDR-based data would be implemented and reported by the same aircraft so that direct comparisons could be made; however, this ~~was~~is not the case ~~for the current AMDAR data~~currently. Furthermore, due to route structure differences, the spatiotemporal coincidence between the AMDAR EDR and DEVG data from different but nearby aircraft could not be constructed. Therefore, only a statistical comparison is examined, rather than ~~the~~one-to-one comparison between ~~the~~ EDR and DEVG.

2.1 DEVG data

~~The data before the QC procedures have been applied are referred to as the raw DEVG in the current study.~~ Figure 1 shows the horizontal distribution of the number of the raw DEVG data ~~samples~~ collected over 36 months (from October 2015 to September 2018) above 15 kft accumulated within a $1^\circ \times 1^\circ$ horizontal grid box. ~~The data before the QC procedures to turbulence information are referred to as the raw DEVG in the current study. Fig. 1 shows that the~~The raw DEVG covers a large portion of the SH, Africa, Europe, and the trans-Pacific and trans-Atlantic Oceans. Given that in situ EDR represents a large portion of the NH (Sharman and Pearson, 2017; Kim et al., 2018), this raw DEVG can complement the ~~SH~~turbulence information. ~~Reporting over the globe (especially over the SH). This reporting~~ time window at ~~the~~crising ~~level~~levels is generally between 7 and 21 minutes, ~~and each with~~ DEVG ~~is reported as~~ the maximum value over each time window (Gill, 2016). The raw DEVG data in some ~~areas~~ of the NH (e.g., the trans-Pacific Ocean and equatorial region) indicate relatively low reporting time window compared with those in the SH. ~~This is apparent in the abrupt change in the data counts either side of the equator, which can also be found in the WMO AMDAR observing newsletters (https://sites.google.com/a/wmo.int/amdar-news-and-events/newsletters/volumn-18-october-2019). The change in reporting frequency between the NH and the SH may be related to systematic settings in aircraft-to-ground reporting during navigation. In the current study, we consider the raw DEVG data only above 15 kft. This lower limit of altitude (15 kft) is chosen based on Kim and Chun (2016) that examined the time series of the DEVG and other recorded variables in the in situ flight data recorders.~~

Figure 2 shows the horizontal locations of turbulence encounters expressed in raw DEVG values. When the DEVG is classified using the thresholds of 2, 4.5, and 9 m s^{-1} for light (LGT), moderate (MOD), and severe (SEV) turbulence severity, respectively (Truscott, 2000; Gill, 2014; Kim and Chun, 2016), the numbers (percentage) of null (NIL), LGT, MOD, and SEV turbulence are 6,821,802 (95.5%), 187,985 (2.63%), 10,273 (0.14%), and 123,320 (1.73%), respectively. ~~It~~However, there seems to ~~have~~be some unrealistic SEV turbulence reports along the entire flight routes over the regions of Australia, New Zealand, and Europe, indicating the need for more careful QC procedures on those reports.

Figure 3 shows the probability density functions (PDFs) of the raw DEVG values at altitudes above 15 kft over the globe, the NH, and the SH for the same period (36 months). The primary peak falls within relatively small DEVG values (less

than 8 m s^{-1}), and the secondary peak falls within relatively large DEVG values (greater than 8 m s^{-1}). This bimodal distribution, which is more prominent in the NH (blue curve) than in the SH (red curve), is highly suspicious considering that Kim et al. (2017) showed that the PDFs of the DEVG have a unimodal distribution following a lognormal distribution.

To examine the regional PDFs of the raw DEVG, we choose the following eight regions: region 1 covers some of Europe, Africa, and Asia (8°S – 57°N , 5°E – 65°E), region 2 covers East Asia (2°N – 45°N , 60°E – 160°E), region 3 covers the trans-Pacific Ocean and North America (28°S – 50°N , 70°W – 178°W), region 4 covers the trans-North Atlantic Ocean (5°N – 65°N , 10°W – 68°W), region 5 covers the trans-Indian Ocean (15°S – 70°S , 30°E – 108°E), region 6 covers Australia and New Zealand (0°S – 45°S , 110°E – 180°E), region 7 covers the trans-South Pacific Ocean (30°S – 75°S , 70°E – 178°E), and region 8 covers the trans-South Atlantic Ocean (42°S – 4°N , 60°W – 28°E).

Figure 4 shows the PDFs of the raw DEVG over these eight regions. As shown in Fig. 3, the PDFs of the DEVG in regions 1 and 6, covering Europe and Australia-New Zealand, respectively, show clear bimodal distributions. In contrast, the PDFs of the DEVG in regions 2–5 and 7–8 show the expected unimodal distributions. The DEVG in regions 4, 7, and 8 does not include strong turbulence events (e.g., $\text{DEVG} > 9 \text{ m s}^{-1}$). ~~Commonly~~, Figs. 2–4 show that the raw DEVG reports may contain erroneous turbulence reports values, which requires QC procedures to remove ~~those erroneous turbulence reports from the raw DEVG~~.

2.2 QC procedures

In the QC procedures, the DEVG, longitude, latitude, altitude, and flight tail number are used. Notably, aircraft-related information, such as aircraft type and tail number, is limited in the AMDAR dataset, and time series of basic variables required for a DEVG calculation are not available. ~~That is, because~~ Since the raw DEVG data with the same tail number sometimes include multiple flights, the flight tail number is only used to separate individual flights.

Figure 5 shows a flow chart of the QC procedures: used, after some trial and error. First, the raw DEVG data are redistributed into an individual file which has the same flight tail number. Second, data are considered to be erroneous according to the following criteria:

- 1) If the number of observations in the individual file is less than eight.
- 2) If, for the individual file, more than two SEV and more than six MOD turbulence events are counted within the spatiotemporal window, which is defined as a circle with 100 km radius, a time window of ± 1 hour, and an altitude window of ± 3 kft.
- 3) If there is only one reported SEV turbulence event, but no MOD turbulence event within a 200 km radius-circle and time window of ± 1 hour.
- 4) If there is only one reported MOD turbulence event, but no LGT turbulence event within a 200 km radius-circle and time window of ± 1 hour.

Applying ~~the aforementioned~~ these QC procedures, only the QC'd DEVG data (hereafter, QCDEVG) are examined in the present study. ~~The current QC procedures are designed~~

We adopt an approach that uses a cluster of the raw DEVG data within a certain spatiotemporal window to increase a confidence in the observed of a turbulence events considering surrounding turbulence events, as the time series of recorded variables are not available. An early version of the QC procedures in the current study is designed, based on those by Gill (2014) and Meneguz et al. (2016) that used the Global Aircraft Data Set. These QC procedures to the AMDAR data are revised based on active discussion with scientists and forecasters associated in the Aviation Weather Center (personal communications, from June to August 2018). The ratio of SEV to MOD turbulence events is larger in the current study ($> 2/6$) than in other observational studies. For example, over South Korea, Kim and Chun (2011) showed 2.94% MOD and 0.08% SEV turbulence events from the PIREPs, while Kim and Chun (2016) showed 0.25% (0.33%) MOD and 0.04% (0.04%) SEV turbulence events from 1-minute aircraft data over the globe (East Asia) and 5.1% MOD and 0.34% SEV turbulence events from the PIREPs over East Asia. Nevertheless, in the current study, the spatial and temporal windows are empirically determined to satisfactorily remove suspicious turbulence reports from the raw DEVG data. Considering that the raw DEVG data merged point samples from many kinds of flight over the globe, and time series of the DEVG and other recorded variables are not available, it is difficult to clearly identify the reason of suspicious DEVG values. A further investigation of the QC procedures of the DEVG remains for future work.

Figure 6 shows the horizontal locations of turbulence encounters according to the QCDEVG above 15 kft for 36 months (from October 2015 to September 2018). The QC procedures indicate that 6,269,077 (97.28%) NIL, 170,199 (2.64%) LGT, 5,380 (0.083%) MOD, and 32 (0.0005%) SEV turbulence events defined by the DEVG values are valid. Most of the SEV turbulence events over Europe, Australia and New Zealand are discarded by the QC procedures. Many discarded turbulence observations over Australia and New Zealand are due to continuous SEV turbulence reports or single SEV turbulence reports without consecutive NIL, LGT, and MOD turbulence events (not shown), while those over Europe are due to a single SEV or MOD turbulence report of the 8 reports within an individual file. Relatively many A relatively large number of SEV turbulence events over the trans-Pacific Ocean and trans-Indian Ocean pass the QC procedures and they these are considered as valid turbulence reports. Some During the QC procedures, we checked horizontal distributions of the raw and QC'd DEVG data when all MOD and SEV turbulence reports coincide with the regions indicating high events are reported. At least in the current study, the irrelevant turbulence potential determined by the Ellrod1 index (Ellrod and Knapp, 1992) which is a conventional clear air turbulence diagnostic (not shown) events are discarded.

2.3 Spatial statistics of the QCDEVG

Figure 7 shows the PDFs of the QCDEVG at altitudes above 15 kft over the globe, the NH, and the SH. As shown in Fig. 6, the secondary peaks in Fig. 3 are no longer apparent in Fig. 7. The SEV turbulence events defined by the DEVG values account for highly reduced percentages of 10^{-4} %. The PDFs of the QCDEVG indicate a unimodal distribution, which is consistent with Fig. 4 of Kim et al. (2017). The PDF for the NH indicates a relatively steep slope for low DEVG values compared with the PDF for the SH. Accordingly, the lognormal fitting, which will be shown in section 3, is conducted for the NH and SH, separately, as characteristics of the QCDEVG are hemisphere dependent.

Figure 8 shows the regional PDFs of the QCDEVG values over the eight regions shown in Fig. 4. The horizontal distribution of the number of the QCDEVG data accumulated within the $1^\circ \times 1^\circ$ horizontal grid box is also indicated in Fig. 8. Most DEVG reports are in the SH and along the narrow flight tracks over the trans-Atlantic Ocean and between Africa and Europe or Asia. The PDFs of the QCDEVG archived in regions 1 and 6 show unimodal distributions. The PDFs of the QCDEVG show quite similar distributions to those calculated using the raw DEVG for the six regions (regions 2–5 and 7–8). The QCDEVG data in regions 5–8 generally are concentrated in the low DEVG value compared with those in regions 1–4. Our focus is to remove suspicious turbulence reports within the limited aircraft-related information and to obtain a reasonable PDF indicating a unimodal distribution. In this regard, the quality of the QCDEVG is considered adequate for the EDR conversion.

3 Conversion of the QCDEVG to the EDR

The QCDEVG is ~~now~~ converted to the EDR using two methods (hereafter, DEVG-derived EDR), as EDR is the preferred turbulence forecast metric. The methods considered in the current study are based on Sharman and Pearson (2017) and Kim et al. (2017). Brief descriptions of the two methods are provided below.

3.1 EDR conversion using the lognormal mapping scheme

Considering that the distribution of observed EDR in the free atmosphere approximately follows a lognormal distribution (Nastrom and Gage, 1985; Frehlich, 1992; Cho et al., 2003; Frehlich and Sharman, 2004; Sharman et al., 2014; Kim et al., 2017), Sharman and Pearson (2017) proposed a statistical mapping equation applying NWP-based turbulence diagnostics to the EDR. Assuming the lognormal property of turbulence forecasting diagnostics, the simplest mapping between a raw turbulence diagnostic D and the EDR is provided by:

$$\ln(D^*) = \ln(\text{EDR}) = a + b \ln(D), \quad (4)$$

where D^* is the remapped EDR value corresponding to the raw turbulence diagnostic D , slope b is the ratio between the standard deviation (SD) of $\ln(\text{EDR})$ and SD of $\ln(D)$ [$b = \text{SD}(\ln(\text{EDR}))/\text{SD}(\ln(D)) = C_2/\text{SD}(\ln(D))$] and the intercept a is the difference between the mean of $\ln(\text{EDR})$ and mean of $\ln(D)$ [$a = \langle \ln(\text{EDR}) \rangle - b \langle \ln(D) \rangle = C_1 - b \langle \ln(D) \rangle$], where the angle brackets indicate the ensemble mean]. Here, C_1 and C_2 are the climatological values of the mean and SD of $\ln(\text{EDR})$, respectively, which are obtained from the lognormal fits to the EDR estimates of in situ equipped aircraft from 2009 to 2014. It is noted that C_1 and C_2 may be different in different regions.

To utilize this statistical mapping equation to obtain the DEVG-derived EDRs, the turbulence diagnostic D is replaced with the DEVG value. Thus, Eq. (4) can be written as:

$$\ln(\text{DEVG}^*) = \ln(\text{EDR}) = a + b \ln(\text{DEVG}), \quad (5)$$

where $DEVG^*$ is the remapped EDR value corresponding to the QCDEVG value. The intercept a and the slope b can be written as:

$$a = \langle \ln(EDR) \rangle - b \langle \ln(DEVG) \rangle = C_1 - b \langle \ln(DEVG) \rangle \text{ and}$$

$$b = SD \ln(EDR) / SD \ln(DEVG) = C_2 / SD \ln(DEVG) \quad (6)$$

The parameters C_1 and C_2 for four different altitude bands (-2.248 and 0.4235 for altitudes of 0–10 kft, -2.578 and 0.557 for altitudes of 10–20 kft, -2.953 and 0.602 for altitudes of 20–45 kft, and -2.572 and 0.5067 for altitudes above 0 ft, respectively) are given in Sharman and Pearson (2017). ~~Although the values~~ The parameters C_1 and C_2 ~~can be used for three different~~ the 20–45 kft altitude ~~ranges (one is the altitudes above 0 ft, another is the altitudes of 20–45 kft, band (-2.953 and the other is the altitudes of 10–20 kft and 20–45 kft), the values for the upper levels of 20–45 kft (0.602, respectively)~~ are utilized in the current study, ~~considering that the values C_1 and C_2 are not significantly altitude dependent.~~ To obtain the mean and SD of $\ln(DEVG)$, the values of the QCDEVG over the NH and SH are calculated ~~for~~ from the lognormal fitting via the optimization function “fminsearch” in the MATLAB package (Lagarias et al., 1998; see also <https://www.mathworks.com/help/matlab/ref/fminsearch.html>). The EDR converted from this method is called for EDR-SP17, hereafter.

Figure 9 shows the lognormal fits (curves) applied to the PDFs (~~filled~~ circles) of the QCDEVG values over the NH and SH (blue and red lines in Fig. 8, respectively). To obtain an optimized lognormal curve, some of the highest and lowest bins (open circles) of the ~~QCDEVG are not used for the lognormal fits.~~ QC DEVG are not used for the lognormal fits. ~~At the highest bins, there are not enough data for reliable lognormal fits, while at the lowest bins, instrument noise may be affecting the result and the small QCDEVG values corresponding to nonturbulent conditions are not of practical interest.~~ The mean values of $\ln(DEVG)$ over the NH and SH are -0.69926 and -1.4397 $m s^{-1}$, respectively, and the SDs of $\ln(DEVG)$ over the NH and SH are 0.6956 and 0.7773 $m s^{-1}$, respectively. The mean and SD of $\ln(DEVG)$ over the SH and NH are used for the EDR conversion (EDR-SP17). ~~When the PDFs of the QCDEVG over different conditions [over land and ocean, different altitude ranges (15–25 kft, 25–35 kft, and 35–kft), seasons (spring, summer, autumn, and winter), times (day and night), and different latitude bands of a spacing of 20°] are computed, the mean and SD of $\ln(DEVG)$ are not significantly changed for~~ ~~aforementioned conditions, except that those in latitudes equatorward of 30° are clearly smaller than those poleward of 30° (not shown).~~

3.2 EDR conversion using the prescribed best-fit function

Kim et al. (2017) investigated two turbulence indicators (the EDR and the DEVG) calculated by the algorithms using the time series of several variables recorded by Hong Kong-based airline flight data recorders for 39 months from February 2011 to April 2014. On a one-to-one basis, relationships between the EDR and DEVG are calculated for three different Boeing

(B) aircraft models (B747-400, B777-200, and B777-300) and three different Airbus (A) aircraft models (A320-200, A321-200, and A330-300), which developed the best-fit quadratic functions for Boeing and Airbus aircraft, separately.

The quadratic equations for the Boeing and Airbus aircraft data are as follows:

$$\text{DEVG}^* = \text{EDR} = 0.0031(\text{DEVG}^2) + 0.0286(\text{DEVG}) + 0.0114, \text{ for Boeing} \quad (7)$$

$$5 \quad \text{DEVG}^* = \text{EDR} = 0.003(\text{DEVG}^2) + 0.0324(\text{DEVG}) + 0.0516, \text{ for Airbus} \quad (8)$$

where DEVG^* is the converted EDR corresponding to the QCDEVG. Although two different DEVG-derived EDRs can be derived using the above two quadratic equations, the DEVG-derived EDR obtained from the quadratic equation for the Boeing aircraft (Eq. 7), which shows a high correlation between the EDR and DEVG, is only considered ~~exclusively~~ in the current study. The EDR converted from this method is called for EDR-KCC17, hereafter.

10 3.3 Spatial statistics of the DEVG-derived EDRs

Table 1 shows the mean and SD of the natural logarithms of EDR-SP17 and EDR-KCC17, $\ln(\text{EDR-SP17})$ and $\ln(\text{EDR-KCC17})$, respectively, for the eight regions indicated by rectangles in Fig. 8. The mean and SD of the resultant DEVG-derived EDRs differ slightly among the eight specified regions. Nevertheless, regarding the mean of the natural logarithm of the EDR, EDR-SP17 (from -2.9986 to -1.8083 $\text{m}^{2/3} \text{s}^{-1}$) is larger than EDR-KCC17 (from -3.9340 to -3.0691 $\text{m}^{2/3} \text{s}^{-1}$) for all
15 eight regions, with differences in magnitude ranging from 0.4788 to 1.2608 $\text{m}^{2/3} \text{s}^{-1}$. For the SD of the natural logarithm of the EDR, EDR-SP17 (from 0.3057 to 1.0538 $\text{m}^{2/3} \text{s}^{-1}$) is larger than EDR-KCC17 (from 0.2196 to 0.6941 $\text{m}^{2/3} \text{s}^{-1}$) for all eight regions, with differences in magnitude ranging from 0.0861 to 0.3597 $\text{m}^{2/3} \text{s}^{-1}$.

Given that EDR-SP17 and EDR-KCC17 have different characteristics, validation of the two different methods is required. Accordingly, the EDRs estimated from in situ equipped aircraft implemented in some United States (US) commercial
20 aircraft (Sharman et al., 2014; Cornman, 2016) are used as the reference data (hereafter, USEDRE). The comparison between the USEDRE and DEVG-derived EDRs proposed in the current study for the same period (from October 2015 to September 2018) is conducted by comparing the mean and SD values of the natural logarithms of three different EDRs (EDR-SP17, EDR-KCC17, and USEDRE) for the specified regions.

Figure 10 shows the horizontal distribution of the USEDRE counts (reference data) at altitudes above 15 kft
25 accumulated within a $1^\circ \times 1^\circ$ horizontal grid box from the same period (36 months) with the DEVG data. Compared with Fig. 8, the USEDRE data mainly cover large portions of the NH, which include the flight routes of the trans-Pacific Ocean, North and South America, the trans-Atlantic Ocean, and Europe. To evaluate the feasibility of deriving the EDRs from the DEVG using the two methods (EDR-SP17 and EDR-KCC17), the mean and SD of three different EDRs are calculated over the two specified regions represented by the rectangles in Fig. 10; one region covers some of Europe and the other covers the trans-
30 Pacific Ocean, which includes flight routes between North America and Australia. Although there are much USEDRE data (Fig. 10) over North America and the trans-Atlantic Ocean, unfortunately, the DEVG data (Fig. 8) over these two regions are insufficient for further analysis.

Figure 11 shows the PDFs of EDR-SP17, EDR-KCC17, and USEDR data over the two rectangles in Fig. 10 from October 2015 to September 2018. Over both Europe and the trans-Pacific Ocean, the distributions of the PDF of EDR-SP17 and USEDR are similar. Especially for the trans-Pacific Ocean region, the PDFs of EDR-SP17 and USEDR at values larger than $\sim 0.22 \text{ m}^{2/3} \text{ s}^{-1}$ are in very good agreement. Over Europe (Fig. 11a), the values of EDR-SP17 are generally larger than those of EDR-KCC17 and USEDR, while over the trans-Pacific Ocean (Fig. 11b), EDR-SP17 and USEDR are similar. The EDR-KCC17 has a larger percentage of low EDR values ($< \sim 0.1 \text{ m}^{2/3} \text{ s}^{-1}$) compared to EDR-SP17 and USEDR in the two regions. For each PDF shown in Fig. 11, the root mean square error (RMSE) of the occurrence frequency of two different EDRs (EDR-SP17 and EDR-KCC17) is calculated with respect to that of the USEDR. Over Europe, the RMSE of EDR-SP17 is 0.0157, and that of EDR-KCC17 is 0.0441. Over the trans-Pacific Ocean, the RMSE of EDR-SP17 is 0.0504, and that of EDR-KCC17 is 0.0903, implying that the occurrence frequency of EDR-SP17 is relatively close to that of the USEDR. The PDFs of EDR-SP17 and USEDR generally follow lognormal distributions, whereas the PDF of EDR-KCC17 departs somewhat from a lognormal distribution especially at low EDR values ($< \sim 0.14 \text{ m}^{2/3} \text{ s}^{-1}$) (not shown). It is noted that the slight difference between the EDR calculations of Cornman (2016) and Haverdings and Chan (2010) might result in the observed difference in the EDR statistics and affect the DEVG-derived EDRs.

Table 2 shows the mean and SD of the natural logarithm of three different EDRs (EDR-SP17, EDR-KCC17, and USEDR) over Europe and the trans-Pacific Ocean. For the region of Europe, the mean values of $\ln(\text{EDR-SP17})$ and $\ln(\text{EDR-KCC17})$ are -2.2394 and $-2.5674 \text{ m}^{2/3} \text{ s}^{-1}$, respectively, and the SDs of $\ln(\text{EDR-SP17})$ and $\ln(\text{EDR-KCC17})$ are 0.4782 and $0.3522 \text{ m}^{2/3} \text{ s}^{-1}$, respectively. For the trans-Pacific Ocean region, the mean values of $\ln(\text{EDR-SP17})$ and $\ln(\text{EDR-KCC17})$ are -2.0299 and $-2.7384 \text{ m}^{2/3} \text{ s}^{-1}$, respectively, and the SDs of $\ln(\text{EDR-SP17})$ and $\ln(\text{EDR-KCC17})$ are 0.4136 and $0.2678 \text{ m}^{2/3} \text{ s}^{-1}$, respectively. The EDR-SP17 and USEDR generally have relatively close mean and SD values, which implies that the EDR-SP17 technique is more accurate at least in the current case. In our current limited study, the statistical properties between EDR-SP17 and USEDR appear slightly different, with higher intensities overall over Europe than the trans-Pacific Ocean. However, because the results are considered only over two regions, further evaluation of the two different methods for deriving EDRs from DEVG is required over different regions and longer period datasets.

4 Summary and discussion

In the current study, we convert the AMDAR provided turbulence indicator, the DEVG, to the EDR to obtain quantitative and consistent turbulence observations globally. We use the DEVG data archived in the NOAA AMDAR (raw DEVG) data for 36 months (October 2015 to September 2018). In the raw DEVG data, there are many suspicious strong-intensity turbulence reports that cause bimodal distributions in the PDFs of the DEVG. To remove erroneous turbulence reports in the raw DEVG data, QC procedures are developed by applying optimally determined thresholds to the raw DEVG dataset. The QC'd DEVG values are converted to the EDR, which is the ICAO standard turbulence intensity metric. The conversion of the DEVG to the EDR is conducted using two methods. Sharman and Pearson (2017) proposed a linear mapping equation

assuming the lognormal property of raw turbulence diagnostics, while Kim et al. (2017) proposed the best-fit curve (quadratic equation) between the EDR and DEVG, based on the one-to-one comparison between the EDR and DEVG calculated using the same flight data. The PDFs of the resultant DEVG-derived EDRs from the two methods, referred to as EDR-SP17 and EDR-KCC17, are compared with those of the USEDR for the two regions covering Europe and the trans-Pacific Ocean. It is found that EDR-SP17 has a relatively similar distribution with the USEDR at least for the current case.

The robust conversion of the DEVG to the EDR would improve the verification of turbulence forecasts globally and the investigation of global characteristics of aviation turbulence, as the USEDR data are still of limited availability globally (Fig. 10). Indeed, the characteristics of aviation turbulence over the NH have been investigated in many previous studies, while those over the SH have not, in part due to a lack of observational data. In this regard, qualified DEVG-derived EDRs can be an important additional source of information globally, especially in most of the SH. Additionally, the DEVG data used in the current study can represent valuable observations for the evaluation of turbulence diagnostics related to convection (Kim et al., 2019), given that the DEVG data contain substantial turbulent information over the tropical region. Together with the existing the USEDR data over the NH, the DEVG-derived EDRs in the SH and tropical regions can be merged into a homogenized global turbulence ~~information~~dataset, which will contribute to improvement of global aviation turbulence forecasting as well as to construction of global climatology of upper-level turbulence.

Data availability. The AMDAR data archived at NOAA are available at <https://madis-data.ncep.noaa.gov/madisPublic1/data/archive>.

Author contributions. SHK, HYC, and JHK designed the study. SHK prepared the original draft of the paper with contributions from HYC, JHK, RDS, and MS. Together, SHK, HYC, JHK, and RDS interpreted the results and reviewed and edited the paper.

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Table 1. Values of the mean and standard deviation (SD) of the natural logarithms of EDR-SP17 and EDR-KCC17 over the eight selected regions indicated in Fig. 8, from October 2015 to September 2018. The unit is $\text{m}^{2/3} \text{s}^{-1}$. Note that EDR-SP17 and EDR-KCC17 are the DEVG-derived EDRs obtained using the methods of Sharman and Pearson (2017) and Kim et al. (2017), respectively.

(a) Mean								
	region 1	region 2	region3	region 4	region 5	region 6	region 7	region 8
EDR-SP17	-2.8144	-2.6072	-2.5612	-2.9192	-2.0771	-2.9986	-2.4930	-1.8083
EDR-KCC17	-3.3845	-3.2647	-3.4031	-3.3980	-3.3083	-3.9340	-3.6562	-3.0691
(b) Standard deviation								
	region 1	region 2	region 3	region 4	region 5	region 6	region 7	region 8
EDR-SP17	0.8755	0.7308	0.6539	1.0538	0.5353	0.6090	0.5150	0.3057
EDR-KCC17	0.6360	0.5240	0.5144	0.6941	0.4148	0.3955	0.4026	0.2196

Table 2. Values of the mean and SD of the natural logarithms of EDR-SP17, EDR-KCC17, and USEDR over (a) Europe and (b) the trans-Pacific Ocean routes indicated in Fig. 10, from October 2015 to September 2018. The unit is $\text{m}^{2/3} \text{s}^{-1}$.

(a) Europe			
	EDR-SP17	EDR-KCC17	USED R
Mean	-2.2394	-2.5674	-2.3258
SD	0.4782	0.3522	0.4118
(b) Trans-Pacific Ocean			
	EDR-SP17	EDR-KCC17	USED R
Mean	-2.0299	-2.7384	-2.3171
SD	0.4136	0.2678	0.4010

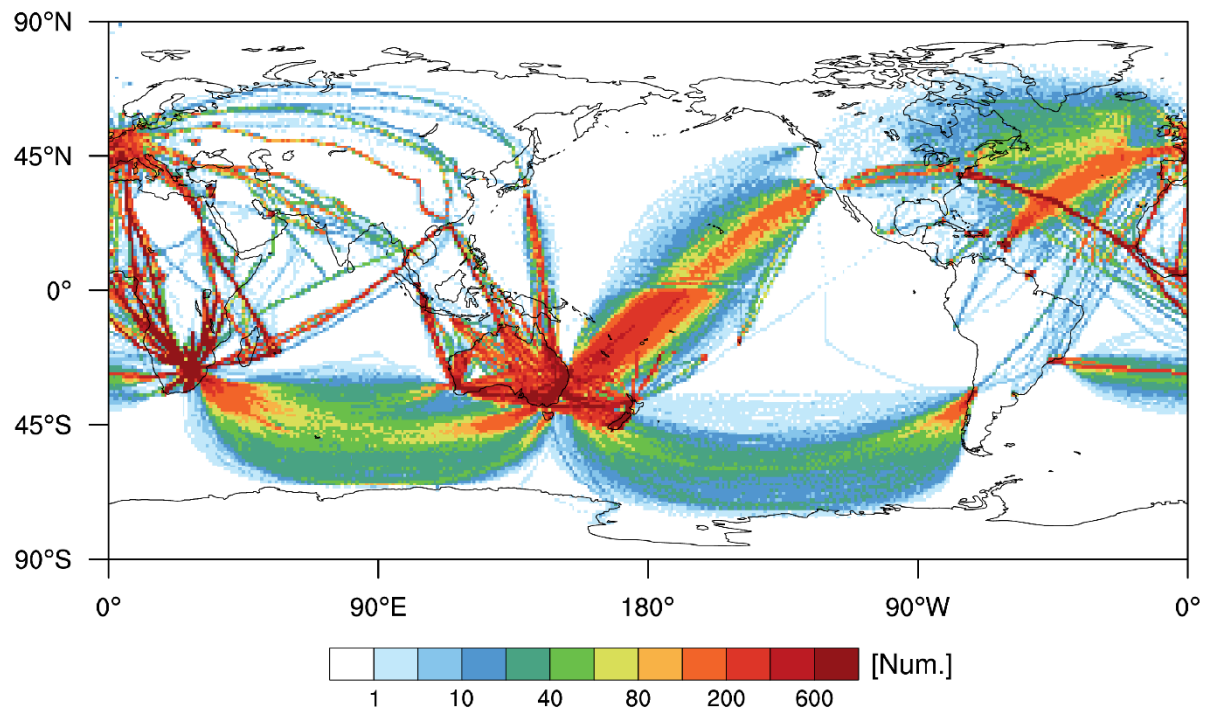


Figure 1. Horizontal distribution of the number of the raw DEVG data at altitudes above 15 kft, accumulated within a $1^\circ \times 1^\circ$ horizontal grid box from October 2015 to September 2018.

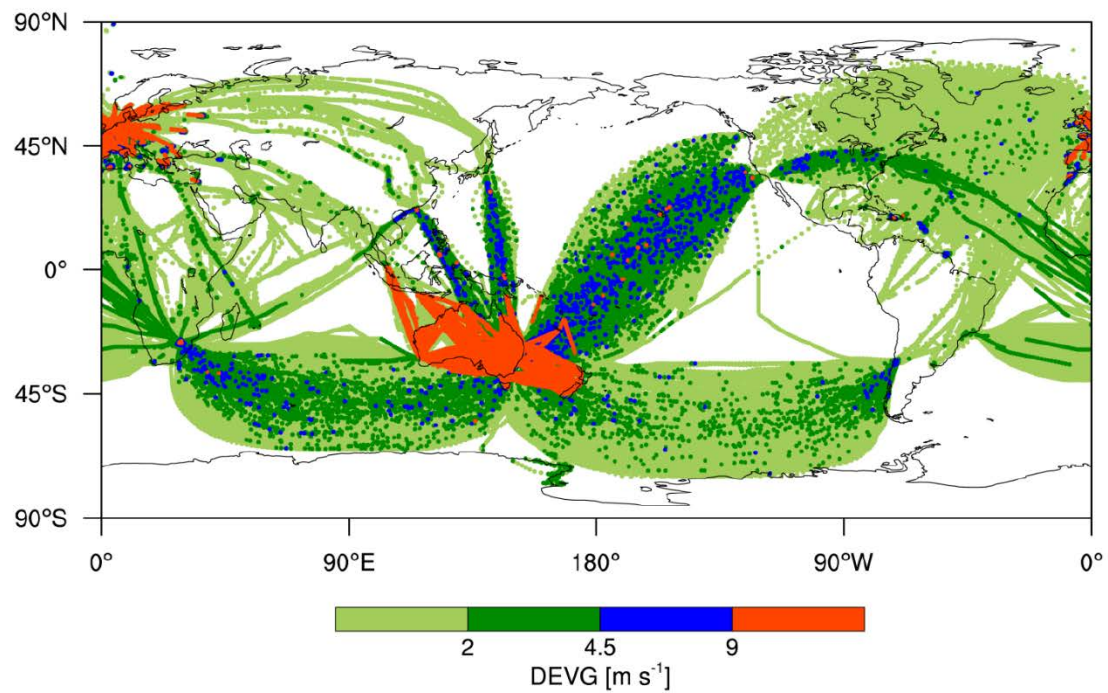


Figure 2. Horizontal locations of turbulence encounters expressed in raw DEVG values at altitudes above 15 kft from October 2015 to September 2018.

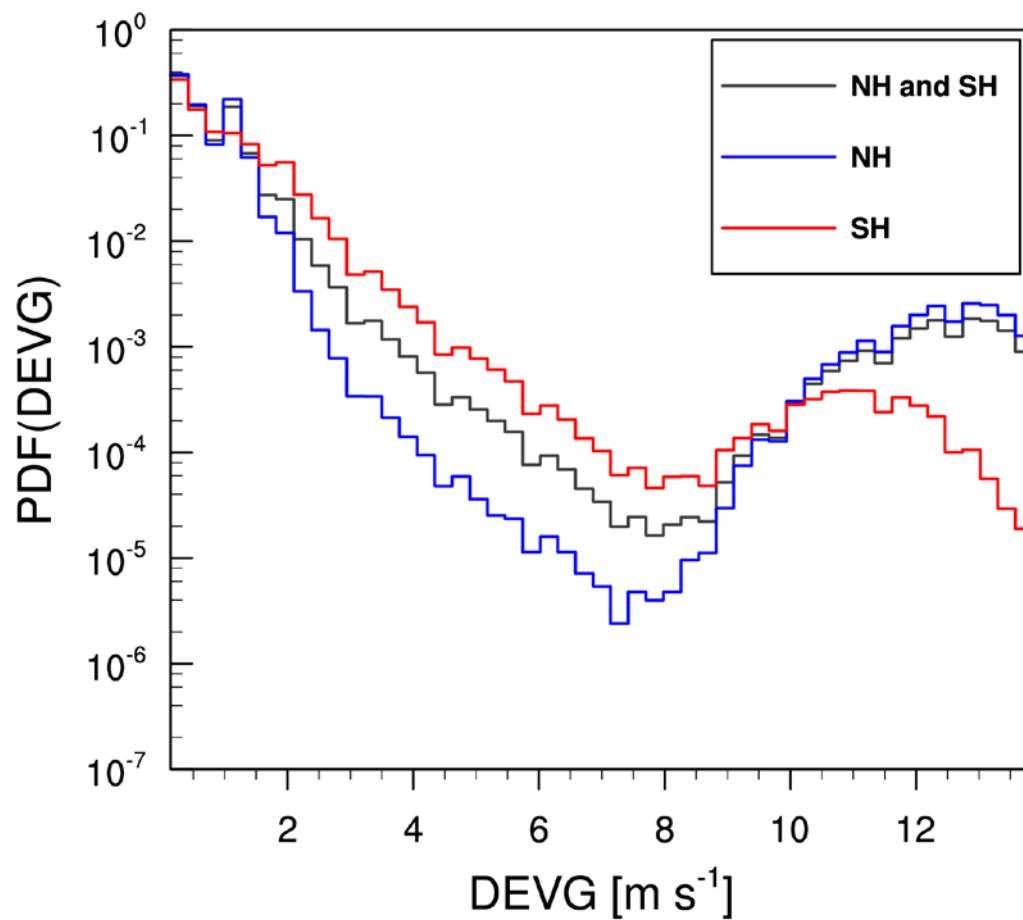


Figure 3. The probability density functions (PDFs) of the raw DEVG over the Northern Hemisphere (NH: blue line), the Southern Hemisphere (SH: red line), and the globe (NH and SH: black line) at altitudes above 15 kft from October 2015 to September 2018.

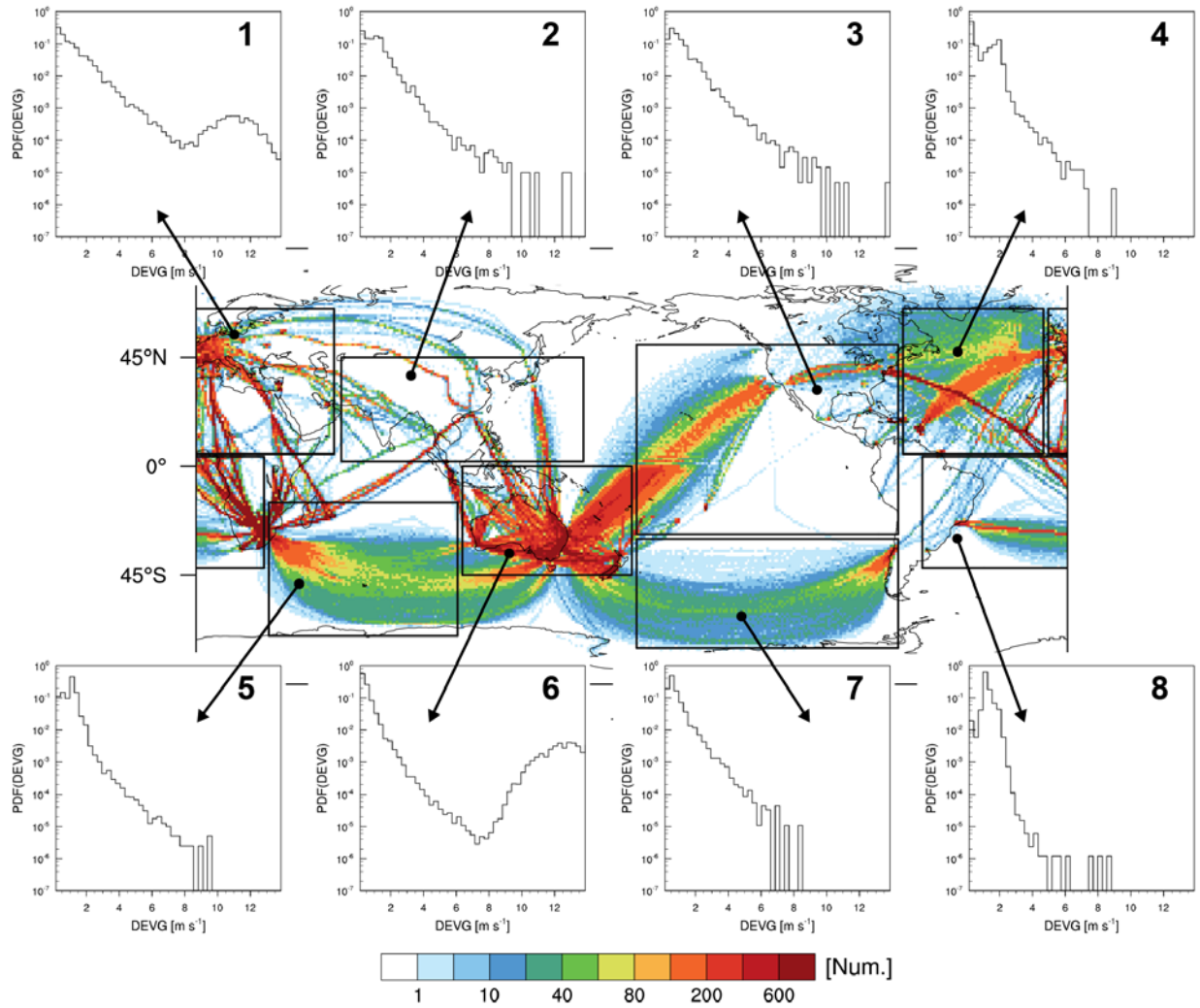


Figure 4. The PDFs of the raw DEVG over eight selected regions, which are indicated as rectangles in the global map, at altitudes above 15 kft from October 2015 to September 2018. The eight regions are located in 8°S–57°N, 5°E–65°E (region 1); 2°N–45°N, 60°E–160°E (region 2); 28°S–50°N, 70°W–178°W (region 3); 5°N–65°N, 10°W–68°W (region 4); 15°S–70°S, 30°E–108°E (region 5); 0°S–45°S, 110°E–180°E (region 6); 30°S–75°S, 70°E–178°E (region 7); and 42°S–4°N, 60°W–28°E (region 8).

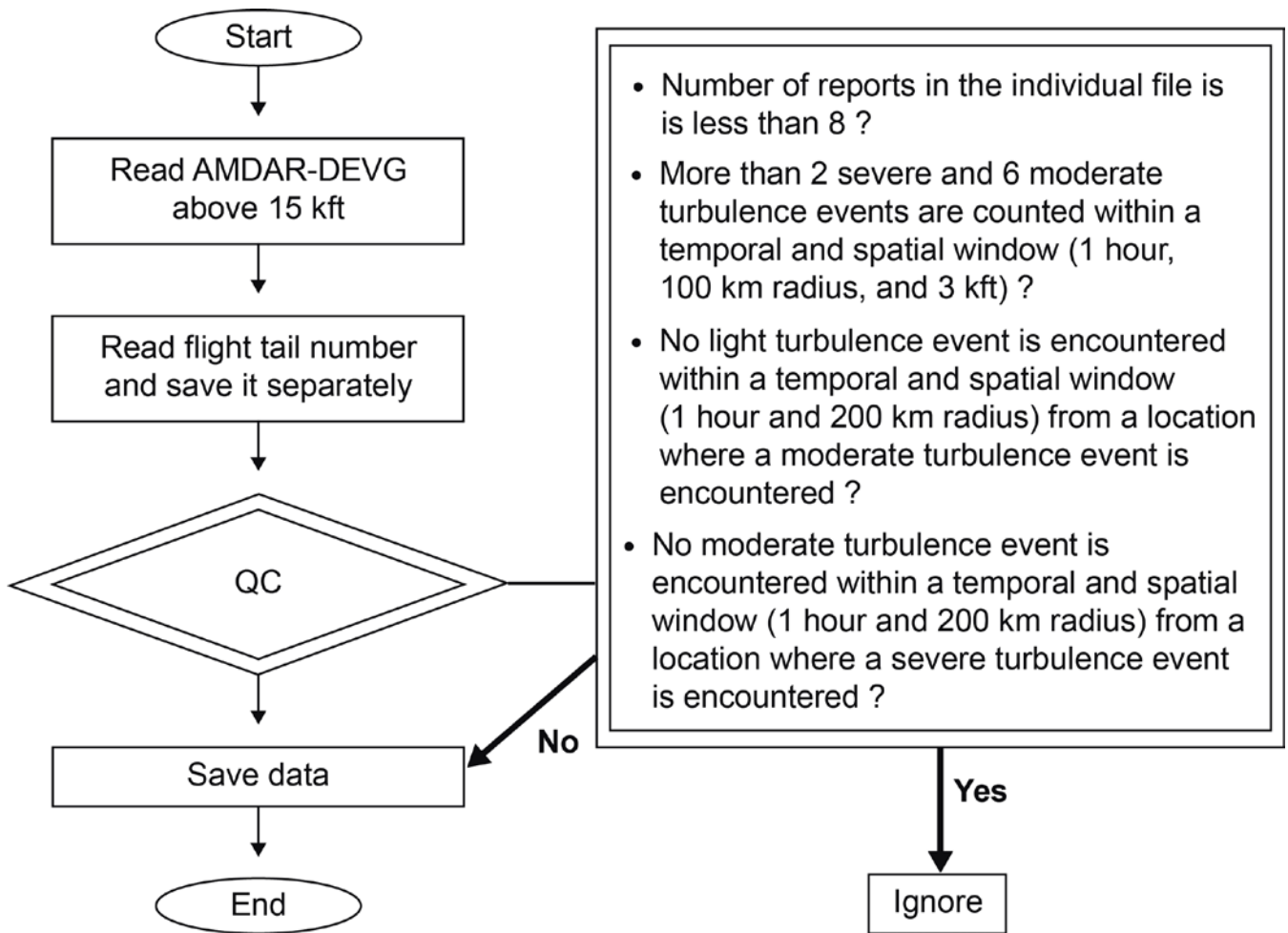


Figure 5. The flow chart of quality control procedures.

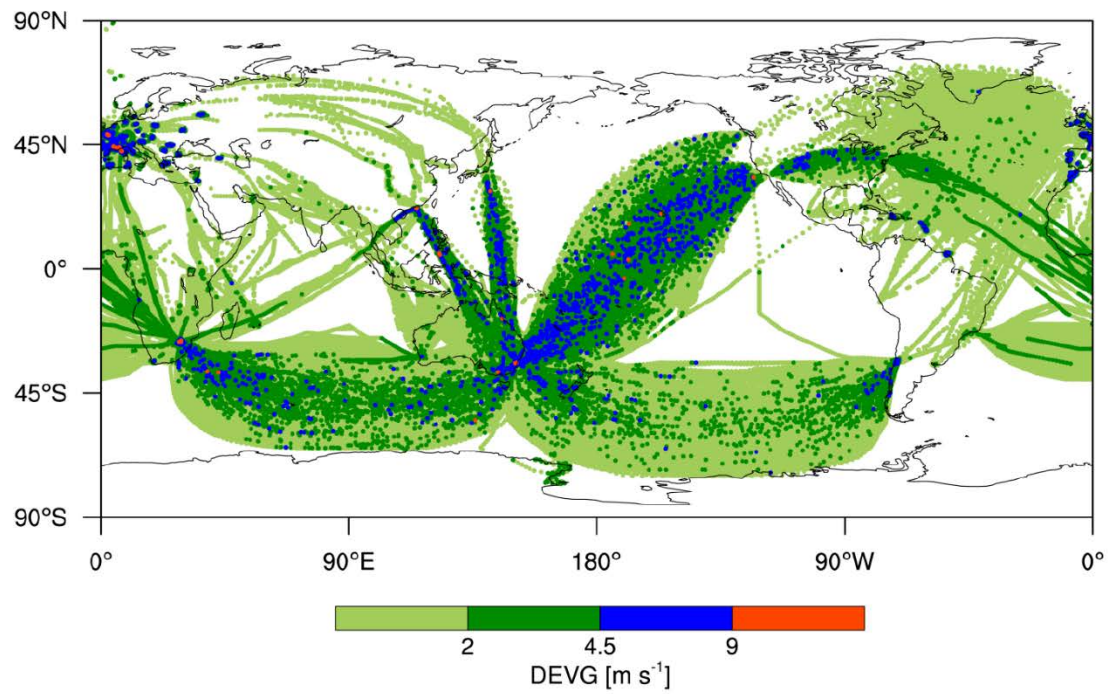


Figure 6. As in Fig. 2, except for the QCDEVG.

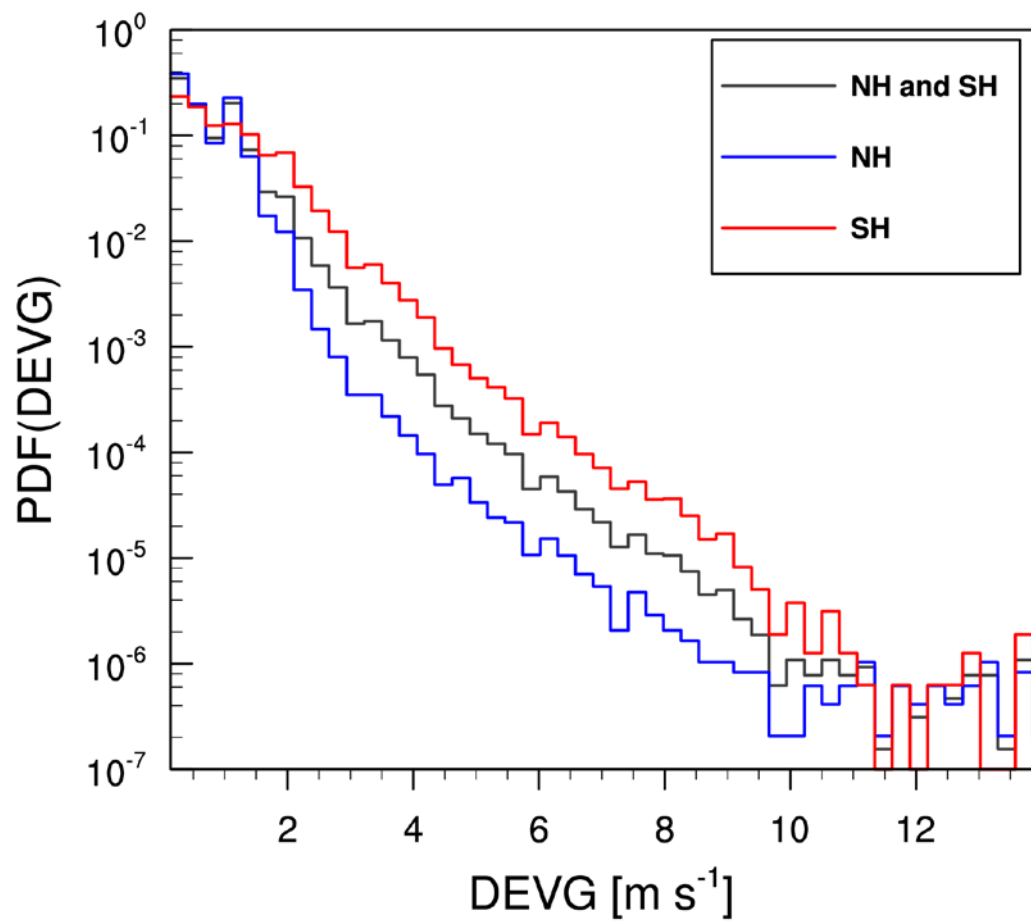


Figure 7. The PDFs of the QCDEVG over the globe (NH and SH: black line), NH (blue line), and SH (red line) at altitudes above 15 kft from October 2015 to September 2018.

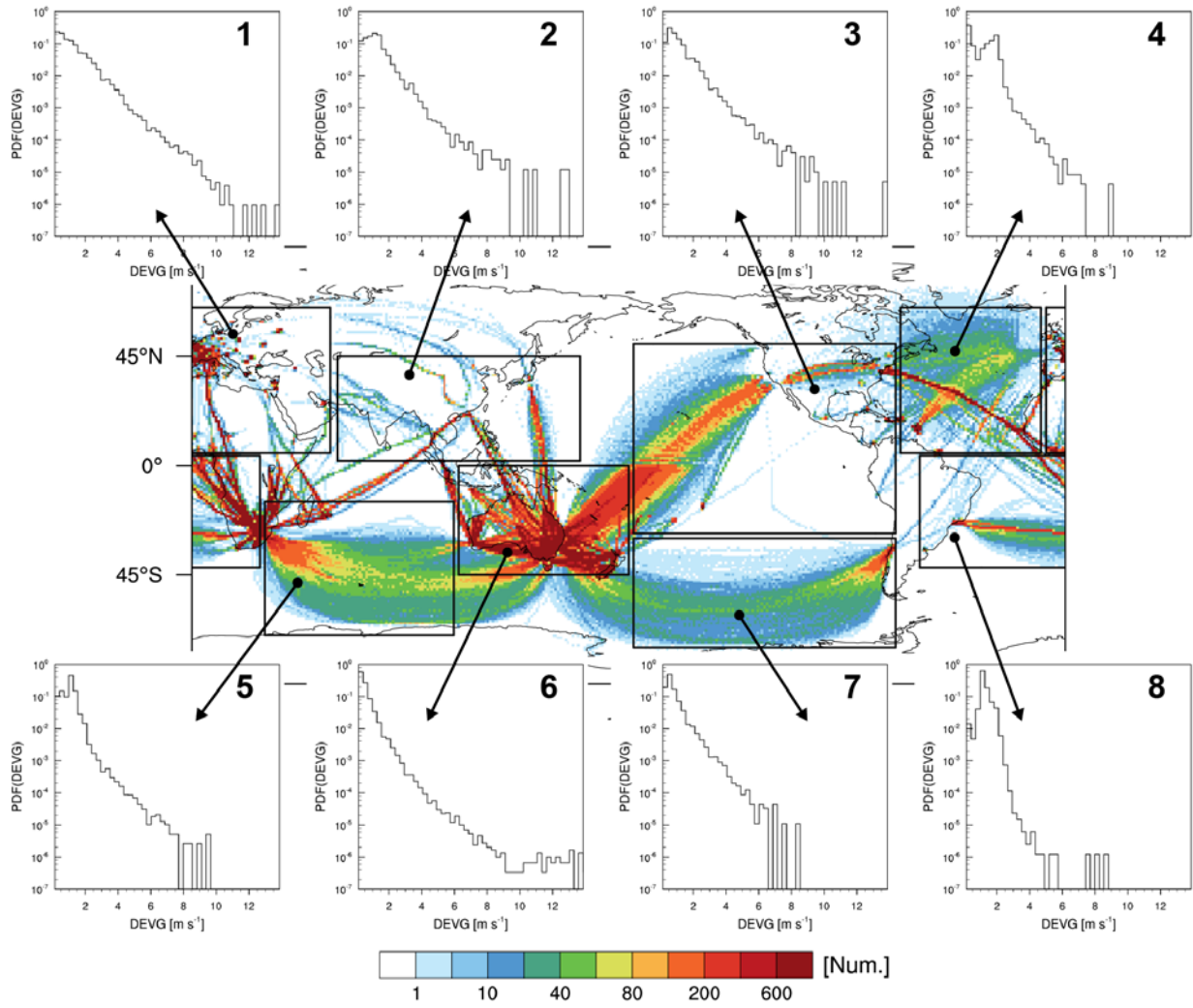


Figure 8. Horizontal distribution of the number of the QCDEVG data at altitudes above 15 kft, accumulated within a $1^\circ \times 1^\circ$ horizontal grid box from October 2015 to September 2018. The PDFs of the QCDEVG over eight selected regions, superimposed on the global map by rectangles.

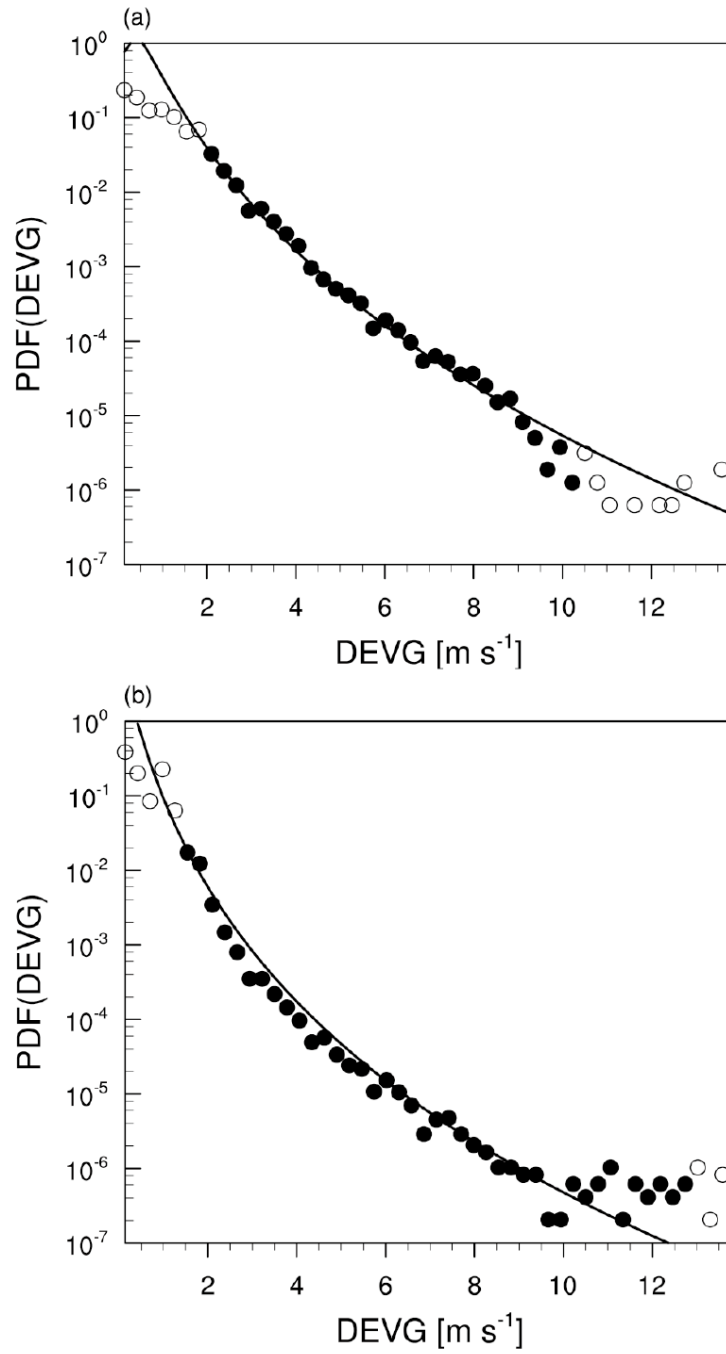


Figure 9. The PDFs (circles) of the QCDEVG and lognormal fit (continuous line) over the QCDEVG over the (a) NH and (b) SH. The filled circles indicate data that were used in the fit, and the open circles indicate data that are excluded from the fit.

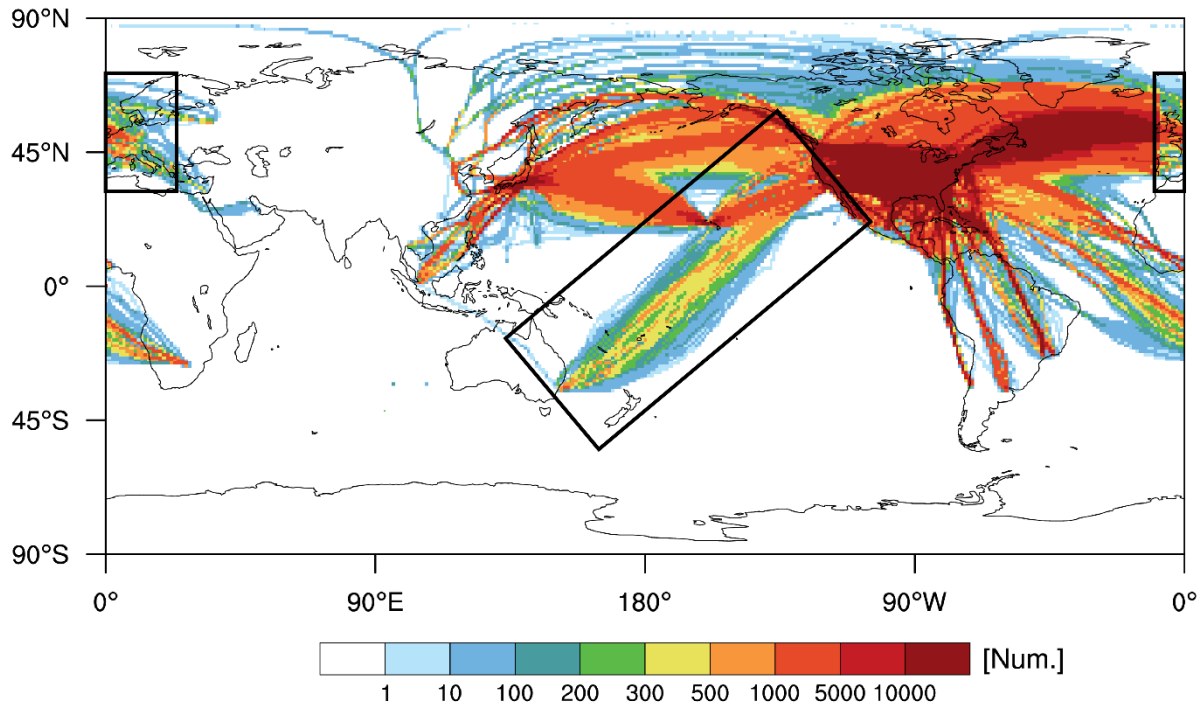


Figure 10. Horizontal distribution of the number of USED data at altitudes above 15 kft, accumulated within a $1^\circ \times 1^\circ$ horizontal grid box from October 2015 to September 2018. The regions of Europe and the trans-Pacific Ocean are indicated by rectangles.

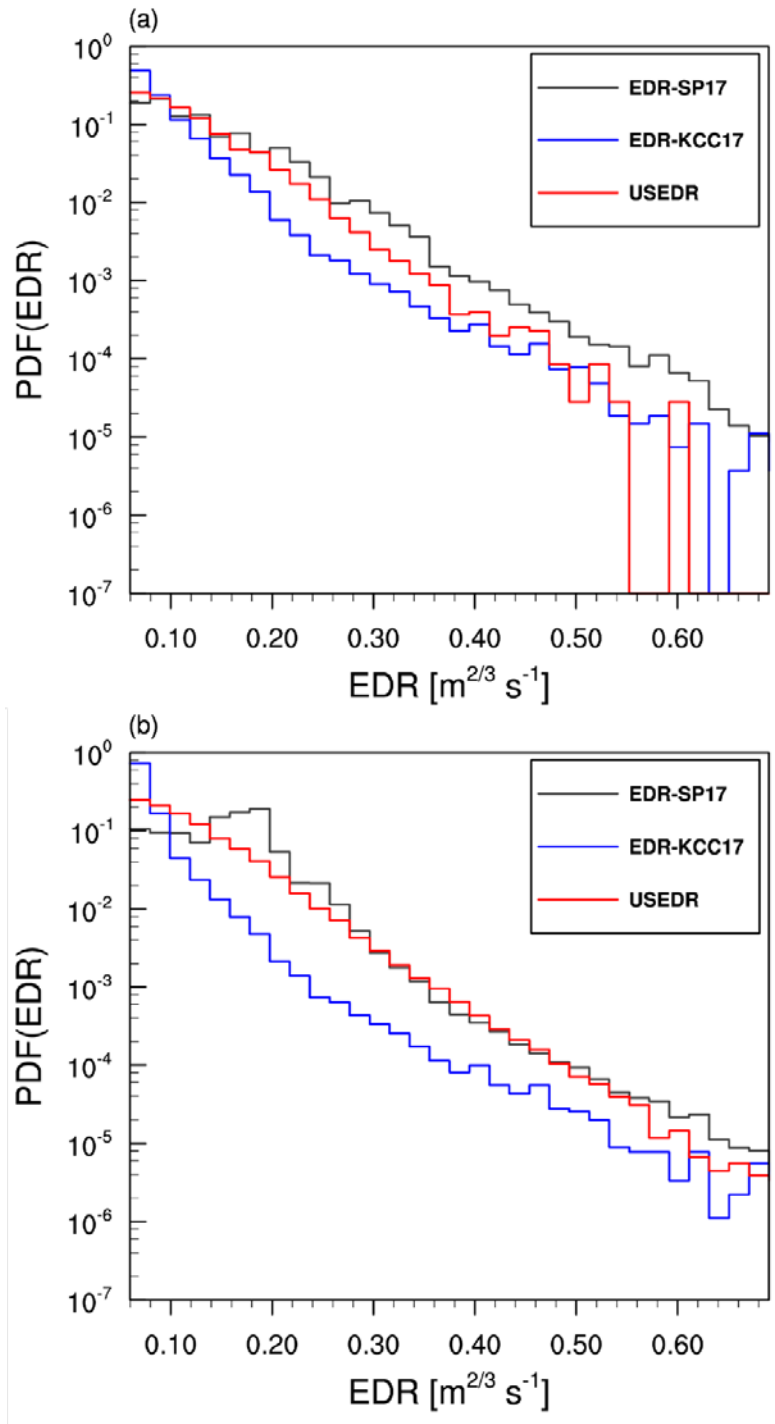


Figure 11. The PDFs of EDR-SP17 (black line), EDR-KCC17 (blue line), and USEDR (red line) at altitudes above 15 kft from October 2015 to September 2018 over (a) Europe and (b) the trans-Pacific Ocean routes indicated in Fig. 10.

Retrieval of Eddy Dissipation Rate from Derived Equivalent Vertical Gust included in Aircraft Meteorological Data Relay (AMDAR)

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Abstract. Some of the Aircraft Meteorological Data Relay (AMDAR) data include a turbulence metric of the derived equivalent vertical gust (DEVG), in addition to wind and temperature. As the cube root of the eddy dissipation rate (EDR) is the International Civil Aviation Organization standard turbulence reporting metric, we attempt to retrieve the EDR from the DEVG for more reliable and consistent observations of aviation turbulence globally. Using the DEVG in the AMDAR data archived from October 2015 to September 2018 covering a large portion of the Southern Hemisphere and North Pacific and North Atlantic Oceans, we convert the DEVG to the EDR using two methods, after conducting quality control procedures to remove suspicious turbulence reports in the DEVG. The first method remaps the DEVG to the EDR using a lognormal mapping scheme, while the second one uses the best-fit curve between the EDR and DEVG developed in a previous study. The DEVG-derived EDRs obtained from the two methods are evaluated against in situ EDR data reported by United States-operated carriers. For two specified regions of the trans-Pacific Ocean and Europe, where both the DEVG-derived EDRs and in situ EDRs were available, the DEVG-derived EDRs obtained by the two methods are generally consistent with in situ EDRs, with slightly better statistics by the first method than the second one. This result is encouraging for extending the aviation turbulence data globally with the single preferred EDR metric, which will contribute to the improvement of global aviation turbulence forecasting as well as to the construction of the climatology of upper-level turbulence.

1 Introduction

Turbulence observations are routinely provided verbally by pilots in the form of pilot reports (PIREPs). There may be an uncertainty in the intensity, timing, and location of turbulence encounters in PIREPs (Schwartz, 1996; Sharman et al., 2006, 2014), as the turbulence intensity in PIREPs is determined by a pilot's subjective experience of the aircraft response to turbulence. Although PIREPs provide subjective categorized turbulence intensity scales (null, light, moderate, and severe), the interpretation is aircraft dependent and null reports of turbulence events are not routine, therefore PIREPs are not adequate for constructing reliable maps of turbulence levels. To address this deficiency, automated objective aircraft-based reports of turbulence are essential.

The Aircraft Meteorological Data Relay (AMDAR) system has been developed and operated by the World Meteorological Organization (WMO) as an operational observing system of automated aircraft weather observations. Given that the AMDAR data can provide routinely global atmospheric observations ranging from the surface to the upper air, these AMDAR data have been widely applied for monitoring and predicting weather systems and improving numerical weather prediction (NWP) models (e.g., Moninger et al., 2003). In addition to temperature and wind that are mandatory variables to report, two turbulence metrics are recommended to be included in the AMDAR data as measures of turbulence (WMO, 2003): the cube root of the eddy dissipation rate (EDR) (Sharman et al., 2014) and the derived equivalent vertical gust velocity (DEVG) (e.g., Hoblit, 1988).

The DEVG was introduced by Pratt and Walker (1954) and approximated to simplify the implementation (Sherman, 1985; Truscott, 2000) as:

$$DEVG \text{ (m s}^{-1}\text{)} = \frac{Am|\Delta n|}{V_c}, \quad (1)$$

where parameter A is the aircraft-specified parameter, m is aircraft mass, Δn is the maximum value of the deviation of vertical acceleration from 1 g over a specified time interval, and V_c is the calibrated air speed. For aircraft types, parameter A can be approximated as

$$A = \bar{A} + c_4(\bar{A} - c_5) \left(\frac{m}{\bar{m}} - 1 \right), \quad (2)$$

$$\bar{A} = c_1 + \left(\frac{c_2}{c_3 + H} \right), \quad (3)$$

where H is the altitude in kft, \bar{m} is the reference mass of the aircraft, and c_1, c_2, c_3, c_4 , and c_5 are empirical constants dependent on the aircraft type that were given in Truscott (2000).

Due to the empirical parameters such as c_1, c_2, c_3, c_4 , and c_5 in Eqs. (2) and (3), the DEVG could still include some uncertainties, which are assumed to be negligible after the rigorous quality control (QC) procedures in the current study. It is also noted that the DEVG does not consider the impact of pitch damping due to the autopilot (WMO, 2003; Kim et al., 2017). Since the DEVG can contain misleading values during the ascent and descent phases, previous studies have only considered the cruise-level DEVG values (e.g., Gill, 2014; Kim and Chun, 2016; Meneguz et al., 2016; Kim et al., 2017). The turbulence information defined by the DEVG has been utilized in statistical analyses on aviation turbulence (e.g., Kim and Chun, 2016; Kim et al., 2017) and in evaluations of the performances of NWP-based turbulence forecasts (e.g., Gill, 2014; Gill and Buchanan, 2014; Kim and Chun, 2016). Currently, the DEVG algorithm has been implemented on several international air-carriers such as the Qantas, South African, British Airways, and other European-based airline aircraft.

The EDR is estimated using aircraft vertical acceleration or estimated vertical wind velocity (MacCready, 1964; Cornman et al., 1995; Haverdings and Chan, 2010; Sharman et al., 2014; Cornman, 2016). The vertical winds-based EDR algorithm developed by the National Center for Atmospheric Research (NCAR) (Sharman et al., 2014; Cornman, 2016) is currently implemented on some fleets of the United Airlines, Delta Air Lines, and South-west Airlines, while that developed

by Haverdings and Chan (2010) is tested on some aircraft of a Hong Kong-based airline. Although Haverdings and Chan (2010) estimated the EDR in a similar way to Cornman (2016), they adopted the different angle-of-attack calibration and different time window and this may cause a difference between two EDRs. The EDR is more useful than the DEVG for turbulence metric detection and forecasting applications (Sharman et al., 2014), given that the DEVG is not a direct turbulence intensity metric but a gust-load transfer factor. Indeed, the International Civil Aviation Organization (ICAO) assigned EDR as the preferred and standard metric for turbulence reporting (ICAO, 2001, 2010; Sharman et al., 2014). The EDR has been widely used in evaluations of the performances of global turbulence forecasting systems (e.g., Pearson and Sharman, 2017; Sharman and Pearson, 2017; Kim et al., 2018; Lee and Chun, 2018), as well as in many case studies on turbulence (e.g., Trier et al., 2012; Bramberger et al., 2018; Trier and Sharman, 2018).

As these two turbulence metrics have been reported from different airlines, the EDR covers most areas in the Northern Hemisphere (NH), while the DEVG has been reported over a large portion of the Southern Hemisphere (SH). To complement the limited availability of global turbulence observations, in the current study, we attempt to convert the DEVG of the AMDAR data to the EDR to obtain more reliable and consistent observations for aviation turbulence. This will lead to improvements in the verification of global aviation turbulence forecasts as well as the construction of a global climatology of aviation turbulence.

The relationship between the EDR and DEVG has been studied using flight data (e.g., Stickland, 1998; Kim et al., 2017). Stickland (1998) conducted a direct comparison between a vertical acceleration-based EDR and DEVG time series of Qantas Airways Boeing 747 data over a 3-month period (from October to December 1997) and showed that the two turbulence metrics are roughly correlated; however, this study considered a limited data period and only one aircraft type. Kim et al. (2017) compared the EDR from some aircraft of the Hong Kong-based airline (Haverdings and Chan, 2010) and the DEVG from the same aircraft using a relatively long period (39 months from February 2011 to April 2014) of data. Kim et al. (2017) developed the best-fit curves between the EDR and DEVG for Airbus and Boeing aircraft data, separately. Although it was not directly used for the conversion of the DEVG to the EDR, Sharman and Pearson (2017) suggested a methodology to convert various turbulence diagnostics to the EDR by assuming that the turbulence diagnostics follow a lognormal distribution at upper levels. Here we propose to use this technique to convert the DEVG to the EDR.

For homogenized global aviation turbulence observations, in the current study, we convert the DEVG to the EDR using two conversion methods, one based on Sharman and Pearson (2017) and the other based on Kim et al. (2017), using historical DEVG records in the AMDAR National Oceanic and Atmospheric Administration (NOAA) archives (hereafter, DEVG) dataset for 36 months (October 2015–September 2018). This paper is organized as follows. In section 2, the descriptions of the DEVG data, QC procedures applied on the DEVG data, and the QC'd DEVG statistics are provided. In section 3, the conversion methods from the DEVG to the EDR and the DEVG-derived EDR statistics are examined. In section 4, a summary and discussion are provided.

2 Data and methodology

We used the AMDAR data archived at NOAA include both the EDR and DEVG from October 2015 to September 2018. Ideally, DEVG-based data and EDR-based data would be implemented and reported by the same aircraft so that direct comparisons could be made; however, this is not the case currently. Furthermore, due to route structure differences, the spatiotemporal coincidence between the AMDAR EDR and DEVG data from different but nearby aircraft could not be constructed. Therefore, only a statistical comparison is examined, rather than one-to-one comparison between EDR and DEVG.

2.1 DEVG data

The data before the QC procedures have been applied are referred to as the raw DEVG in the current study. Figure 1 shows the horizontal distribution of the number of the raw DEVG data samples collected over 36 months (from October 2015 to September 2018) above 15 kft accumulated within a $1^\circ \times 1^\circ$ horizontal grid box. The raw DEVG covers a large portion of the SH, Africa, Europe, and the trans-Pacific and trans-Atlantic Oceans. Given that in situ EDR represents a large portion of the NH (Sharman and Pearson, 2017; Kim et al., 2018), this raw DEVG can complement the turbulence information over the globe (especially over the SH). This reporting time window at cruising levels is generally between 7 and 21 minutes, with DEVG reported as the maximum value over each time window (Gill, 2016). The raw DEVG data in some areas of the NH (e.g., the trans-Pacific Ocean and equatorial region) indicate relatively low reporting time window compared with those in the SH. This is apparent in the abrupt change in the data counts either side of the equator, which can also be found in the WMO AMDAR observing newsletters (<https://sites.google.com/a/wmo.int/amdar-news-and-events/newsletters/volumn-18-october-2019>). The change in reporting frequency between the NH and the SH may be related to systematic settings in aircraft-to-ground reporting during navigation. In the current study, we consider the raw DEVG data only above 15 kft. This lower limit of altitude (15 kft) is chosen based on Kim and Chun (2016) that examined the time series of the DEVG and other recorded variables in the in situ flight data recorders.

Figure 2 shows the horizontal locations of turbulence encounters expressed in raw DEVG values. When the DEVG is classified using the thresholds of 2, 4.5, and 9 m s^{-1} for light (LGT), moderate (MOD), and severe (SEV) turbulence severity, respectively (Truscott, 2000; Gill, 2014; Kim and Chun, 2016), the numbers (percentage) of null (NIL), LGT, MOD, and SEV turbulence are 6,821,802 (95.5%), 187,985 (2.63%), 10,273 (0.14%), and 123,320 (1.73%), respectively. However, there seems to be some unrealistic SEV turbulence reports along the entire flight routes over the regions of Australia, New Zealand, and Europe, indicating the need for more careful QC procedures on those reports.

Figure 3 shows the probability density functions (PDFs) of the raw DEVG values at altitudes above 15 kft over the globe, the NH, and the SH for the same period (36 months). The primary peak falls within relatively small DEVG values (less than 8 m s^{-1}), and the secondary peak falls within relatively large DEVG values (greater than 8 m s^{-1}). This bimodal distribution, which is more prominent in the NH (blue curve) than in the SH (red curve), is highly suspicious considering that Kim et al. (2017) showed that the PDFs of the DEVG have a unimodal distribution following a lognormal distribution.

To examine the regional PDFs of the raw DEVG, we choose the following eight regions: region 1 covers some of Europe, Africa, and Asia (8°S–57°N, 5°E–65°E), region 2 covers East Asia (2°N–45°N, 60°E–160°E), region 3 covers the trans-Pacific Ocean and North America (28°S–50°N, 70°W–178°W), region 4 covers the trans-North Atlantic Ocean (5°N–65°N, 10°W–68°W), region 5 covers the trans-Indian Ocean (15°S–70°S, 30°E–108°E), region 6 covers Australia and New Zealand (0°S–45°S, 110°E–180°E), region 7 covers the trans-South Pacific Ocean (30°S–75°S, 70°E–178°E), and region 8 covers the trans-South Atlantic Ocean (42°S–4°N, 60°W–28°E).

Figure 4 shows the PDFs of the raw DEVG over these eight regions. As shown in Fig. 3, the PDFs of the DEVG in regions 1 and 6, covering Europe and Australia-New Zealand, respectively, show clear bimodal distributions. In contrast, the PDFs of the DEVG in regions 2–5 and 7–8 show the expected unimodal distributions. The DEVG in regions 4, 7, and 8 does not include strong turbulence events (e.g., $DEVG > 9 \text{ m s}^{-1}$). Figs. 2–4 show that the raw DEVG reports may contain erroneous turbulence values, which requires QC procedures to remove.

2.2 QC procedures

In the QC procedures, the DEVG, longitude, latitude, altitude, and flight tail number are used. Notably, aircraft-related information, such as aircraft type and tail number, is limited in the AMDAR dataset, and time series of basic variables required for a DEVG calculation are not available. Since the raw DEVG data with the same tail number sometimes include multiple flights, the flight tail number is only used to separate individual flights.

Figure 5 shows a flow chart of the QC procedures used, after some trial and error. First, the raw DEVG data are redistributed into an individual file which has the same flight tail number. Second, data are considered to be erroneous according to the following criteria:

- 1) If the number of observations in the individual file is less than eight.
- 2) If, for the individual file, more than two SEV and more than six MOD turbulence events are counted within the spatiotemporal window, which is defined as a circle with 100 km radius, a time window of ± 1 hour, and an altitude window of ± 3 kft.
- 3) If there is only one reported SEV turbulence event, but no MOD turbulence event within a 200 km radius-circle and time window of ± 1 hour.
- 4) If there is only one reported MOD turbulence event, but no LGT turbulence event within a 200 km radius-circle and time window of ± 1 hour.

Applying these QC procedures, only the QC'd DEVG data (hereafter, QCDEVG) are examined in the present study.

We adopt an approach that uses a cluster of the raw DEVG data within a certain spatiotemporal window to increase a confidence of a turbulence event, as the time series of recorded variables are not available. An early version of the QC procedures in the current study is designed, based on those by Gill (2014) and Meneguz et al. (2016) that used the Global Aircraft Data Set. These QC procedures to the AMDAR data are revised based on active discussion with scientists and forecasters associated in the Aviation Weather Center (personal communications, from June to August 2018). The ratio of

SEV to MOD turbulence events is larger in the current study ($> 2/6$) than in other observational studies. For example, over South Korea, Kim and Chun (2011) showed 2.94% MOD and 0.08% SEV turbulence events from the PIREPs, while Kim and Chun (2016) showed 0.25% (0.33%) MOD and 0.04% (0.04%) SEV turbulence events from 1-minute aircraft data over the globe (East Asia) and 5.1% MOD and 0.34% SEV turbulence events from the PIREPs over East Asia. Nevertheless, in the current study, the spatial and temporal windows are empirically determined to satisfactorily remove suspicious turbulence reports from the raw DEVG data. Considering that the raw DEVG data merged point samples from many kinds of flight over the globe, and time series of the DEVG and other recorded variables are not available, it is difficult to clearly identify the reason of suspicious DEVG values. A further investigation of the QC procedures of the DEVG remains for future work.

Figure 6 shows the horizontal locations of turbulence encounters according to the QCDEVG above 15 kft for 36 months (from October 2015 to September 2018). The QC procedures indicate that 6,269,077 (97.28%) NIL, 170,199 (2.64%) LGT, 5,380 (0.083%) MOD, and 32 (0.0005%) SEV turbulence events defined by the DEVG values are valid. Most of the SEV turbulence events over Europe, Australia and New Zealand are discarded by the QC procedures. Many discarded turbulence observations over Australia and New Zealand are due to continuous SEV turbulence reports or single SEV turbulence reports without consecutive NIL, LGT, and MOD turbulence events (not shown), while those over Europe are due to a single SEV or MOD turbulence report of the 8 reports within an individual file. A relatively large number of SEV turbulence events over the trans-Pacific Ocean and trans-Indian Ocean pass the QC procedures and these are considered as valid turbulence reports. During the QC procedures, we checked horizontal distributions of the raw and QC'd DEVG data when all MOD and SEV turbulence events are reported. At least in the current study, the irrelevant turbulence events are discarded.

2.3 Spatial statistics of the QCDEVG

Figure 7 shows the PDFs of the QCDEVG at altitudes above 15 kft over the globe, the NH, and the SH. As shown in Fig. 6, the secondary peaks in Fig. 3 are no longer apparent in Fig. 7. The SEV turbulence events defined by the DEVG values account for highly reduced percentages of 10^{-4} %. The PDFs of the QCDEVG indicate a unimodal distribution, which is consistent with Fig. 4 of Kim et al. (2017). The PDF for the NH indicates a relatively steep slope for low DEVG values compared with the PDF for the SH. Accordingly, the lognormal fitting, which will be shown in section 3, is conducted for the NH and SH, separately, as characteristics of the QCDEVG are hemisphere dependent.

Figure 8 shows the regional PDFs of the QCDEVG values over the eight regions shown in Fig. 4. The horizontal distribution of the number of the QCDEVG data accumulated within the $1^\circ \times 1^\circ$ horizontal grid box is also indicated in Fig. 8. Most DEVG reports are in the SH and along the narrow flight tracks over the trans-Atlantic Ocean and between Africa and Europe or Asia. The PDFs of the QCDEVG archived in regions 1 and 6 show unimodal distributions. The PDFs of the QCDEVG show quite similar distributions to those calculated using the raw DEVG for the six regions (regions 2–5 and 7–8). The QCDEVG data in regions 5–8 generally are concentrated in the low DEVG value compared with those in regions 1–4. Our

focus is to remove suspicious turbulence reports within the limited aircraft-related information and to obtain a reasonable PDF indicating a unimodal distribution. In this regard, the quality of the QCDEVG is considered adequate for the EDR conversion.

3 Conversion of the QCDEVG to the EDR

The QCDEVG is converted to the EDR using two methods (hereafter, DEVG-derived EDR), as EDR is the preferred turbulence forecast metric. The methods considered in the current study are based on Sharman and Pearson (2017) and Kim et al. (2017). Brief descriptions of the two methods are provided below.

3.1 EDR conversion using the lognormal mapping scheme

Considering that the distribution of observed EDR in the free atmosphere approximately follows a lognormal distribution (Nastrom and Gage, 1985; Frehlich, 1992; Cho et al., 2003; Frehlich and Sharman, 2004; Sharman et al., 2014; Kim et al., 2017), Sharman and Pearson (2017) proposed a statistical mapping equation applying NWP-based turbulence diagnostics to the EDR. Assuming the lognormal property of turbulence forecasting diagnostics, the simplest mapping between a raw turbulence diagnostic D and the EDR is provided by:

$$\ln(D^*) = \ln(\text{EDR}) = a + b \ln(D), \quad (4)$$

where D^* is the remapped EDR value corresponding to the raw turbulence diagnostic D , slope b is the ratio between the standard deviation (SD) of $\ln(\text{EDR})$ and SD of $\ln(D)$ [$b = \text{SD}\ln(\text{EDR})/\text{SD}\ln(D) = C_2/\text{SD}\ln(D)$] and the intercept a is the difference between the mean of $\ln(\text{EDR})$ and mean of $\ln(D)$ [$a = \langle \ln(\text{EDR}) \rangle - b\langle \ln(D) \rangle = C_1 - b\langle \ln(D) \rangle$], where the angle brackets indicate the ensemble mean]. Here, C_1 and C_2 are the climatological values of the mean and SD of $\ln(\text{EDR})$, respectively, which are obtained from the lognormal fits to the EDR estimates of in situ equipped aircraft from 2009 to 2014. It is noted that C_1 and C_2 may be different in different regions.

To utilize this statistical mapping equation to obtain the DEVG-derived EDRs, the turbulence diagnostic D is replaced with the DEVG value. Thus, Eq. (4) can be written as:

$$\ln(\text{DEVG}^*) = \ln(\text{EDR}) = a + b \ln(\text{DEVG}), \quad (5)$$

where DEVG^* is the remapped EDR value corresponding to the QCDEVG value. The intercept a and the slope b can be written as:

$$a = \langle \ln(\text{EDR}) \rangle - b\langle \ln(\text{DEVG}) \rangle = C_1 - b\langle \ln(\text{DEVG}) \rangle \text{ and}$$

$$b = \text{SD}\ln(\text{EDR})/\text{SD}\ln(\text{DEVG}) = C_2/\text{SD}\ln(\text{DEVG}) \quad (6)$$

The parameters C_1 and C_2 for four different altitude bands (-2.248 and 0.4235 for altitudes of 0–10 kft, -2.578 and 0.557 for altitudes of 10–20 kft, -2.953 and 0.602 for altitudes of 20–45 kft, and -2.572 and 0.5067 for altitudes above 0 ft,

respectively) are given in Sharman and Pearson (2017). The parameters C_1 and C_2 for the 20–45 kft altitude band (-2.953 and 0.602, respectively) are utilized in the current study. To obtain the mean and SD of $\ln(\text{DEVG})$, the values of the QCDEVG over the NH and SH are calculated from the lognormal fitting via the optimization function “fminsearch” in the MATLAB package (Lagarias et al., 1998; see also <https://www.mathworks.com/help/matlab/ref/fminsearch.html>). The EDR converted from this method is called for EDR-SP17, hereafter.

Figure 9 shows the lognormal fits (curves) applied to the PDFs (circles) of the QCDEVG values over the NH and SH (blue and red lines in Fig. 8, respectively). To obtain an optimized lognormal curve, some of the highest and lowest bins (open circles) of the QC DEVG are not used for the lognormal fits. At the highest bins, there are not enough data for reliable lognormal fits, while at the lowest bins, instrument noise may be affecting the result and the small QCDEVG values corresponding to nonturbulent conditions are not of practical interest. The mean values of $\ln(\text{DEVG})$ over the NH and SH are -0.69926 and -1.4397 m s^{-1} , respectively, and the SDs of $\ln(\text{DEVG})$ over the NH and SH are 0.6956 and 0.7773 m s^{-1} , respectively. The mean and SD of $\ln(\text{DEVG})$ over the SH and NH are used for the EDR conversion (EDR-SP17). When the PDFs of the QCDEVG over different conditions [over land and ocean, different altitude ranges (15-25 kft, 25-35 kft, and 35-45 kft), seasons (spring, summer, autumn, and winter), times (day and night), and different latitude bands of a spacing of 20°] are computed, the mean and SD of $\ln(\text{DEVG})$ are not significantly changed for aforementioned conditions, except that those in latitudes equatorward of 30° are clearly smaller than those poleward of 30° (not shown).

3.2 EDR conversion using the prescribed best-fit function

Kim et al. (2017) investigated two turbulence indicators (the EDR and the DEVG) calculated by the algorithms using the time series of several variables recorded by Hong Kong-based airline flight data recorders for 39 months from February 2011 to April 2014. On a one-to-one basis, relationships between the EDR and DEVG are calculated for three different Boeing (B) aircraft models (B747-400, B777-200, and B777-300) and three different Airbus (A) aircraft models (A320-200, A321-200, and A330-300), which developed the best-fit quadratic functions for Boeing and Airbus aircraft, separately.

The quadratic equations for the Boeing and Airbus aircraft data are as follows:

$$\text{DEVG}^* = \text{EDR} = 0.0031(\text{DEVG}^2) + 0.0286(\text{DEVG}) + 0.0114, \text{ for Boeing} \quad (7)$$

$$\text{DEVG}^* = \text{EDR} = 0.003(\text{DEVG}^2) + 0.0324(\text{DEVG}) + 0.0516, \text{ for Airbus} \quad (8)$$

where DEVG^* is the converted EDR corresponding to the QCDEVG. Although two different DEVG-derived EDRs can be derived using the above two quadratic equations, the DEVG-derived EDR obtained from the quadratic equation for the Boeing aircraft (Eq. 7), which shows a high correlation between the EDR and DEVG, is only considered in the current study. The EDR converted from this method is called for EDR-KCC17, hereafter.

3.3 Spatial statistics of the DEVG-derived EDRs

Table 1 shows the mean and SD of the natural logarithms of EDR-SP17 and EDR-KCC17, $\ln(\text{EDR-SP17})$ and $\ln(\text{EDR-KCC17})$, respectively, for the eight regions indicated by rectangles in Fig. 8. The mean and SD of the resultant DEVG-derived EDRs differ slightly among the eight specified regions. Nevertheless, regarding the mean of the natural logarithm of the EDR, EDR-SP17 (from -2.9986 to -1.8083 $\text{m}^{2/3} \text{s}^{-1}$) is larger than EDR-KCC17 (from -3.9340 to -3.0691 $\text{m}^{2/3} \text{s}^{-1}$) for all eight regions, with differences in magnitude ranging from 0.4788 to 1.2608 $\text{m}^{2/3} \text{s}^{-1}$. For the SD of the natural logarithm of the EDR, EDR-SP17 (from 0.3057 to 1.0538 $\text{m}^{2/3} \text{s}^{-1}$) is larger than EDR-KCC17 (from 0.2196 to 0.6941 $\text{m}^{2/3} \text{s}^{-1}$) for all eight regions, with differences in magnitude ranging from 0.0861 to 0.3597 $\text{m}^{2/3} \text{s}^{-1}$.

Given that EDR-SP17 and EDR-KCC17 have different characteristics, validation of the two different methods is required. Accordingly, the EDRs estimated from in situ equipped aircraft implemented in some United States (US) commercial aircraft (Sharman et al., 2014; Cornman, 2016) are used as the reference data (hereafter, USEDR). The comparison between the USEDR and DEVG-derived EDRs proposed in the current study for the same period (from October 2015 to September 2018) is conducted by comparing the mean and SD values of the natural logarithms of three different EDRs (EDR-SP17, EDR-KCC17, and USEDR) for the specified regions.

Figure 10 shows the horizontal distribution of the USEDR counts (reference data) at altitudes above 15 kft accumulated within a $1^\circ \times 1^\circ$ horizontal grid box from the same period (36 months) with the DEVG data. Compared with Fig. 8, the USEDR data mainly cover large portions of the NH, which include the flight routes of the trans-Pacific Ocean, North and South America, the trans-Atlantic Ocean, and Europe. To evaluate the feasibility of deriving the EDRs from the DEVG using the two methods (EDR-SP17 and EDR-KCC17), the mean and SD of three different EDRs are calculated over the two specified regions represented by the rectangles in Fig. 10; one region covers some of Europe and the other covers the trans-Pacific Ocean, which includes flight routes between North America and Australia. Although there are much USEDR data (Fig. 10) over North America and the trans-Atlantic Ocean, unfortunately, the DEVG data (Fig. 8) over these two regions are insufficient for further analysis.

Figure 11 shows the PDFs of EDR-SP17, EDR-KCC17, and USEDR data over the two rectangles in Fig. 10 from October 2015 to September 2018. Over both Europe and the trans-Pacific Ocean, the distributions of the PDF of EDR-SP17 and USEDR are similar. Especially for the trans-Pacific Ocean region, the PDFs of EDR-SP17 and USEDR at values larger than $\sim 0.22 \text{ m}^{2/3} \text{s}^{-1}$ are in very good agreement. Over Europe (Fig. 11a), the values of EDR-SP17 are generally larger than those of EDR-KCC17 and USEDR, while over the trans-Pacific Ocean (Fig. 11b), EDR-SP17 and USEDR are similar. The EDR-KCC17 has a larger percentage of low EDR values ($< \sim 0.1 \text{ m}^{2/3} \text{s}^{-1}$) compared to EDR-SP17 and USEDR in the two regions. For each PDF shown in Fig. 11, the root mean square error (RMSE) of the occurrence frequency of two different EDRs (EDR-SP17 and EDR-KCC17) is calculated with respect to that of the USEDR. Over Europe, the RMSE of EDR-SP17 is 0.0157, and that of EDR-KCC17 is 0.0441. Over the trans-Pacific Ocean, the RMSE of EDR-SP17 is 0.0504, and that of EDR-KCC17 is 0.0903, implying that the occurrence frequency of EDR-SP17 is relatively close to that of the USEDR. The PDFs of EDR-

SP17 and USEDR generally follow lognormal distributions, whereas the PDF of EDR-KCC17 departs somewhat from a lognormal distribution especially at low EDR values ($< \sim 0.14 \text{ m}^{2/3} \text{ s}^{-1}$) (not shown). It is noted that the slight difference between the EDR calculations of Cornman (2016) and Haverdings and Chan (2010) might result in the observed difference in the EDR statistics and affect the DEVG-derived EDRs.

Table 2 shows the mean and SD of the natural logarithm of three different EDRs (EDR-SP17, EDR-KCC17, and USEDR) over Europe and the trans-Pacific Ocean. For the region of Europe, the mean values of $\ln(\text{EDR-SP17})$ and $\ln(\text{EDR-KCC17})$ are -2.2394 and $-2.5674 \text{ m}^{2/3} \text{ s}^{-1}$, respectively, and the SDs of $\ln(\text{EDR-SP17})$ and $\ln(\text{EDR-KCC17})$ are 0.4782 and $0.3522 \text{ m}^{2/3} \text{ s}^{-1}$, respectively. For the trans-Pacific Ocean region, the mean values of $\ln(\text{EDR-SP17})$ and $\ln(\text{EDR-KCC17})$ are -2.0299 and $-2.7384 \text{ m}^{2/3} \text{ s}^{-1}$, respectively, and the SDs of $\ln(\text{EDR-SP17})$ and $\ln(\text{EDR-KCC17})$ are 0.4136 and $0.2678 \text{ m}^{2/3} \text{ s}^{-1}$, respectively. The EDR-SP17 and USEDR generally have relatively close mean and SD values, which implies that the EDR-SP17 technique is more accurate at least in the current case. In our current limited study, the statistical properties between EDR-SP17 and USEDR appear slightly different, with higher intensities overall over Europe than the trans-Pacific Ocean. However, because the results are considered only over two regions, further evaluation of the two different methods for deriving EDRs from DEVG is required over different regions and longer period datasets.

4 Summary and discussion

In the current study, we convert the AMDAR provided turbulence indicator, the DEVG, to the EDR to obtain quantitative and consistent turbulence observations globally. We use the DEVG data archived in the NOAA AMDAR (raw DEVG) data for 36 months (October 2015 to September 2018). In the raw DEVG data, there are many suspicious strong-intensity turbulence reports that cause bimodal distributions in the PDFs of the DEVG. To remove erroneous turbulence reports in the raw DEVG data, QC procedures are developed by applying optimally determined thresholds to the raw DEVG dataset. The QC'd DEVG values are converted to the EDR, which is the ICAO standard turbulence intensity metric. The conversion of the DEVG to the EDR is conducted using two methods. Sharman and Pearson (2017) proposed a linear mapping equation assuming the lognormal property of raw turbulence diagnostics, while Kim et al. (2017) proposed the best-fit curve (quadratic equation) between the EDR and DEVG, based on the one-to-one comparison between the EDR and DEVG calculated using the same flight data. The PDFs of the resultant DEVG-derived EDRs from the two methods, referred to as EDR-SP17 and EDR-KCC17, are compared with those of the USEDR for the two regions covering Europe and the trans-Pacific Ocean. It is found that EDR-SP17 has a relatively similar distribution with the USEDR at least for the current case.

The robust conversion of the DEVG to the EDR would improve the verification of turbulence forecasts globally and the investigation of global characteristics of aviation turbulence, as the USEDR data are still of limited availability globally (Fig. 10). Indeed, the characteristics of aviation turbulence over the NH have been investigated in many previous studies, while those over the SH have not, in part due to a lack of observational data. In this regard, qualified DEVG-derived EDRs can be an important additional source of information globally, especially in most of the SH. Additionally, the DEVG data used in the

current study can represent valuable observations for the evaluation of turbulence diagnostics related to convection (Kim et al., 2019), given that the DEVG data contain substantial turbulent information over the tropical region. Together with the existing the USED data over the NH, the DEVG-derived EDRs in the SH and tropical regions can be merged into a homogenized global turbulence dataset, which will contribute to improvement of global aviation turbulence forecasting as well as to construction of global climatology of upper-level turbulence.

Data availability. The AMDAR data archived at NOAA are available at <https://madis-data.ncep.noaa.gov/madisPublic1/data/archive>.

Author contributions. SHK, HYC, and JHK designed the study. SHK prepared the original draft of the paper with contributions from HYC, JHK, RDS, and MS. Together, SHK, HYC, JHK, and RDS interpreted the results and reviewed and edited the paper.

Competing interests. The authors declare they have no conflict of interest.

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Table 1. Values of the mean and standard deviation (SD) of the natural logarithms of EDR-SP17 and EDR-KCC17 over the eight selected regions indicated in Fig. 8, from October 2015 to September 2018. The unit is $\text{m}^{2/3} \text{s}^{-1}$. Note that EDR-SP17 and EDR-KCC17 are the DEVG-derived EDRs obtained using the methods of Sharman and Pearson (2017) and Kim et al. (2017), respectively.

(a) Mean								
	region 1	region 2	region3	region 4	region 5	region 6	region 7	region 8
EDR-SP17	-2.8144	-2.6072	-2.5612	-2.9192	-2.0771	-2.9986	-2.4930	-1.8083
EDR-KCC17	-3.3845	-3.2647	-3.4031	-3.3980	-3.3083	-3.9340	-3.6562	-3.0691
(b) Standard deviation								
	region 1	region 2	region 3	region 4	region 5	region 6	region 7	region 8
EDR-SP17	0.8755	0.7308	0.6539	1.0538	0.5353	0.6090	0.5150	0.3057
EDR-KCC17	0.6360	0.5240	0.5144	0.6941	0.4148	0.3955	0.4026	0.2196

Table 2. Values of the mean and SD of the natural logarithms of EDR-SP17, EDR-KCC17, and USEDR over (a) Europe and (b) the trans-Pacific Ocean routes indicated in Fig. 10, from October 2015 to September 2018. The unit is $\text{m}^{2/3} \text{s}^{-1}$.

(a) Europe			
	EDR-SP17	EDR-KCC17	USED R
Mean	-2.2394	-2.5674	-2.3258
SD	0.4782	0.3522	0.4118
(b) Trans-Pacific Ocean			
	EDR-SP17	EDR-KCC17	USED R
Mean	-2.0299	-2.7384	-2.3171
SD	0.4136	0.2678	0.4010

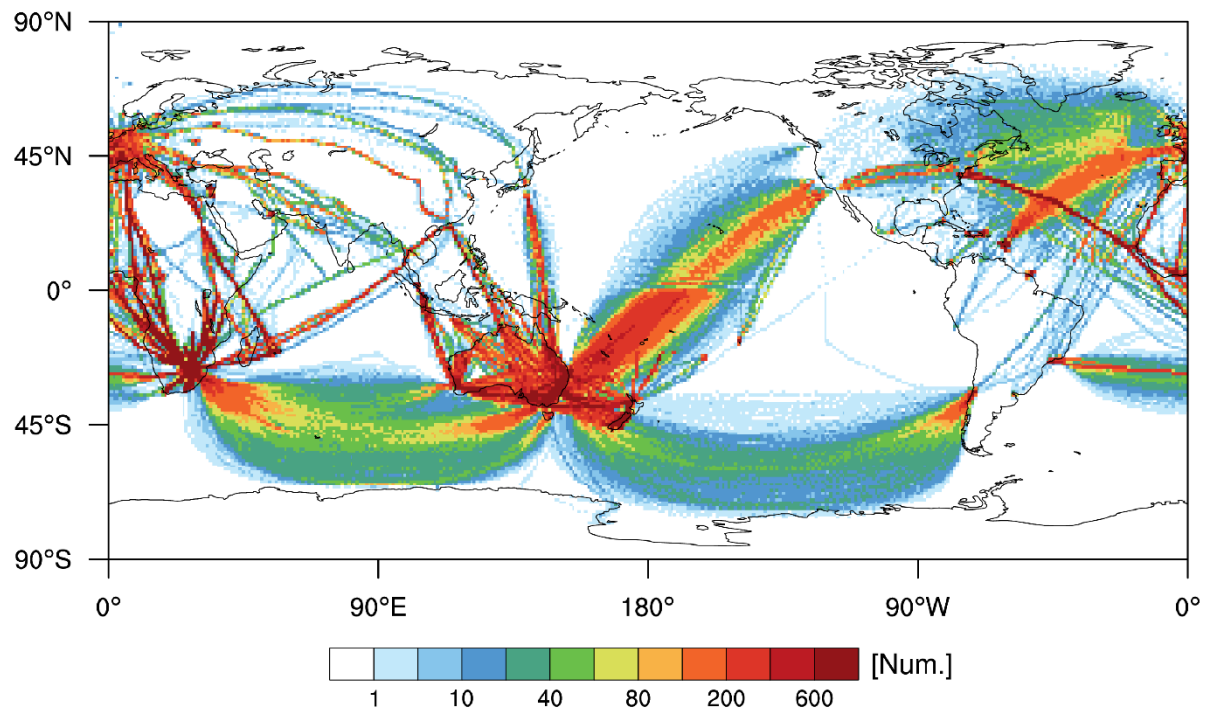


Figure 1. Horizontal distribution of the number of the raw DEVG data at altitudes above 15 kft, accumulated within a $1^\circ \times 1^\circ$ horizontal grid box from October 2015 to September 2018.

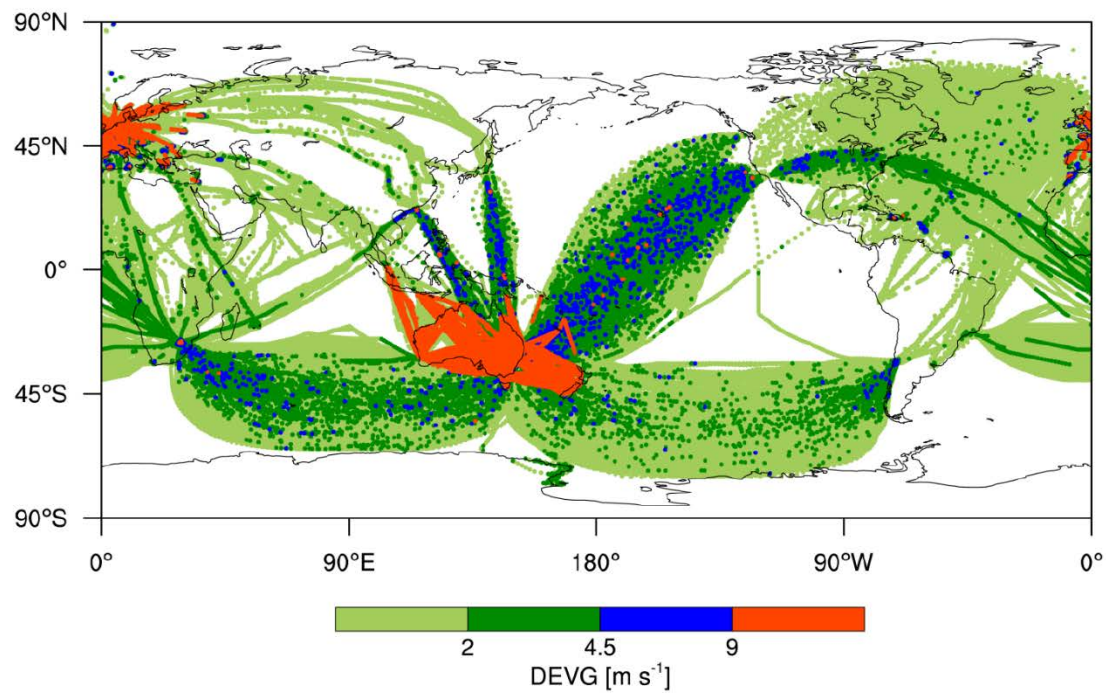


Figure 2. Horizontal locations of turbulence encounters expressed in raw DEVG values at altitudes above 15 kft from October 2015 to September 2018.

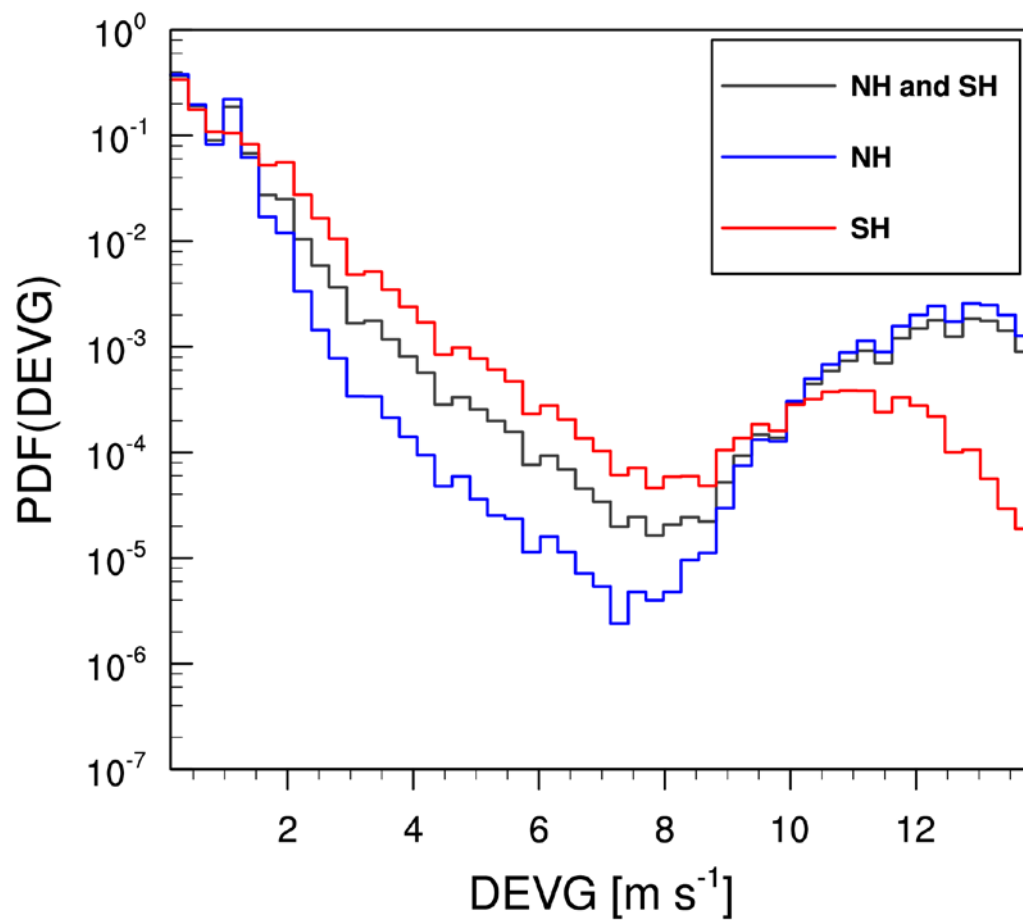


Figure 3. The probability density functions (PDFs) of the raw DEVG over the Northern Hemisphere (NH: blue line), the Southern Hemisphere (SH: red line), and the globe (NH and SH: black line) at altitudes above 15 kft from October 2015 to September 2018.

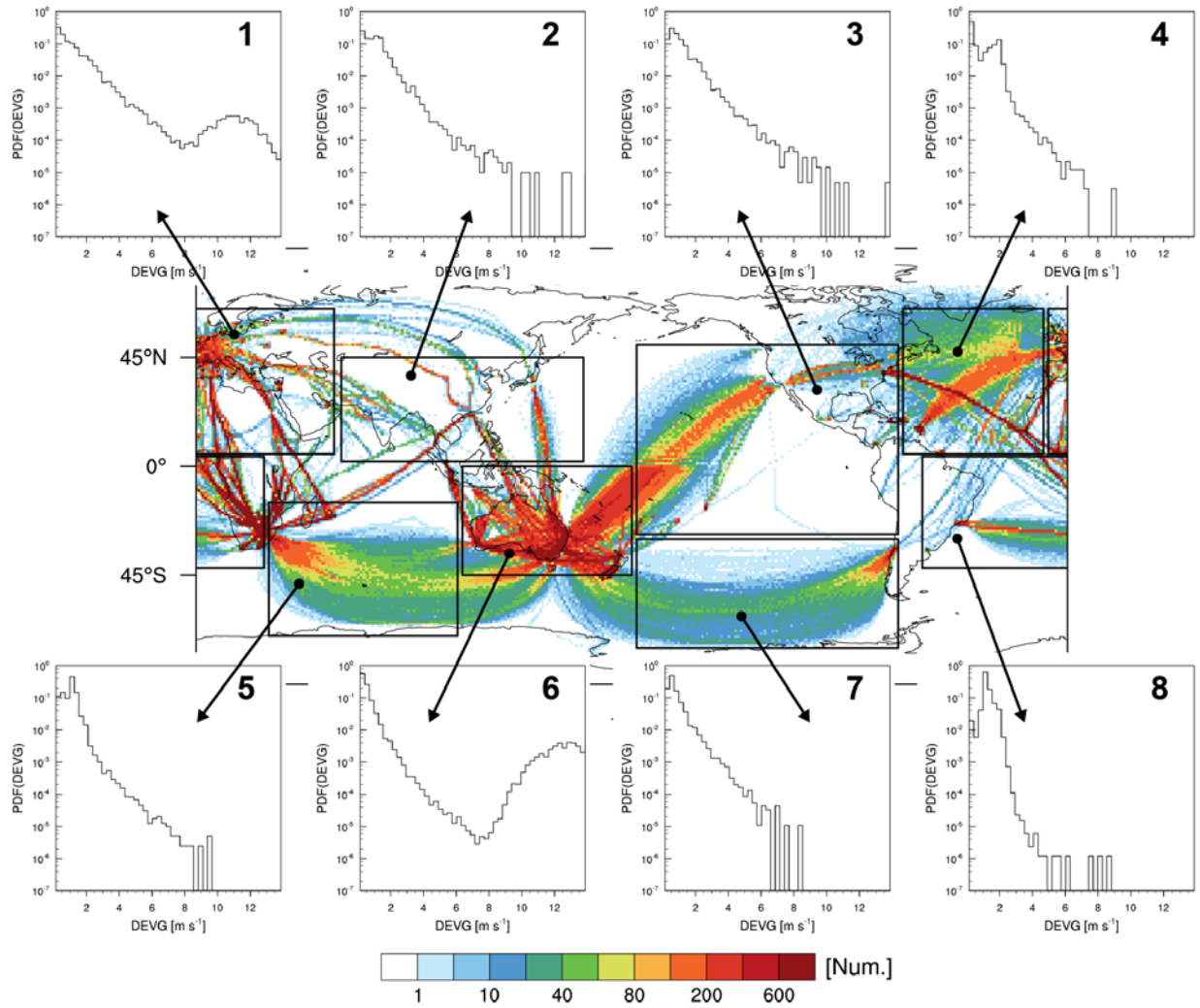


Figure 4. The PDFs of the raw DEVG over eight selected regions, which are indicated as rectangles in the global map, at altitudes above 15 kft from October 2015 to September 2018. The eight regions are located in 8°S–57°N, 5°E–65°E (region 1); 2°N–45°N, 60°E–160°E (region 2); 28°S–50°N, 70°W–178°W (region 3); 5°N–65°N, 10°W–68°W (region 4); 15°S–70°S, 30°E–108°E (region 5); 0°S–45°S, 110°E–180°E (region 6); 30°S–75°S, 70°E–178°E (region 7); and 42°S–4°N, 60°W–28°E (region 8).

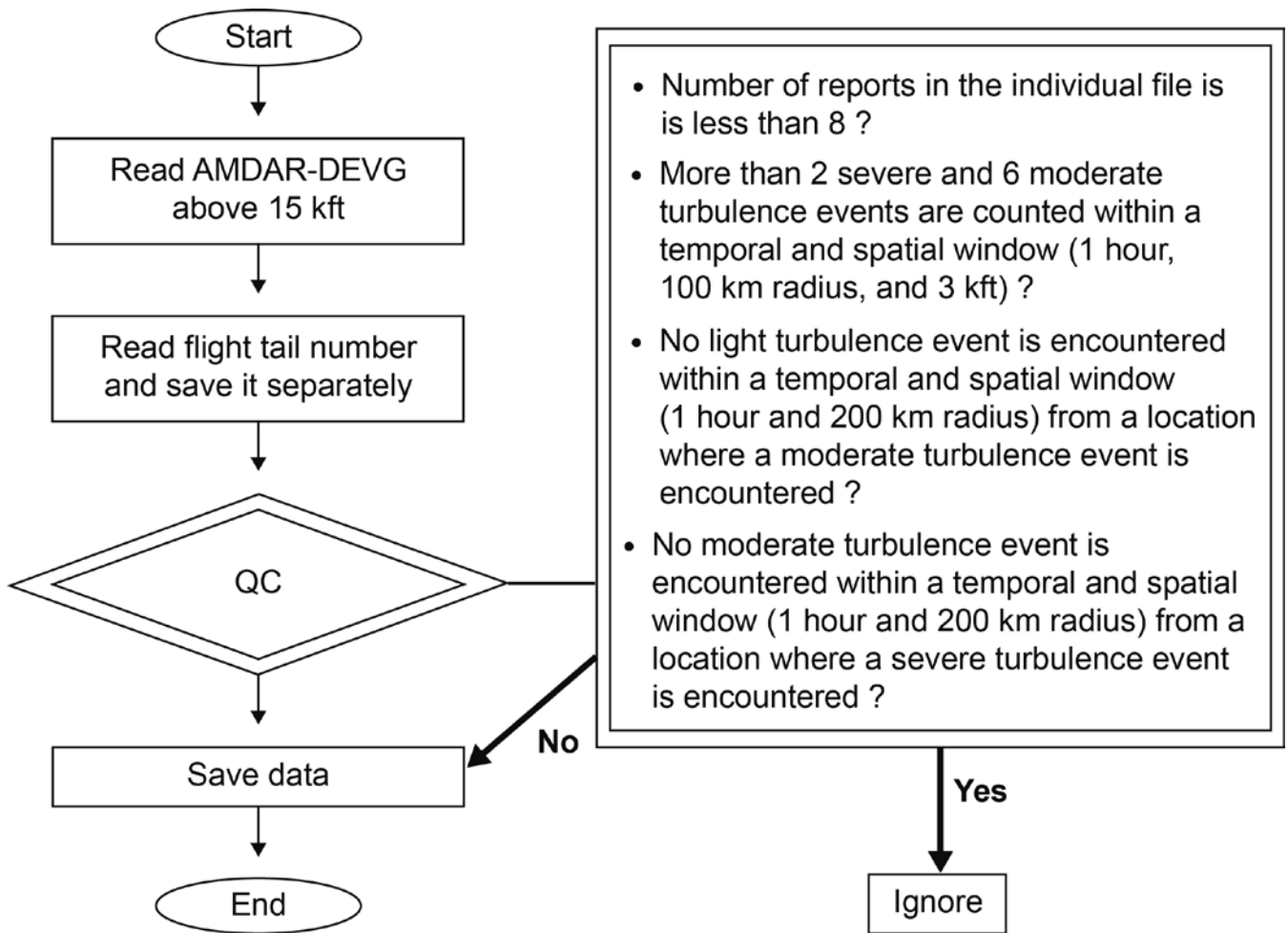


Figure 5. The flow chart of quality control procedures.

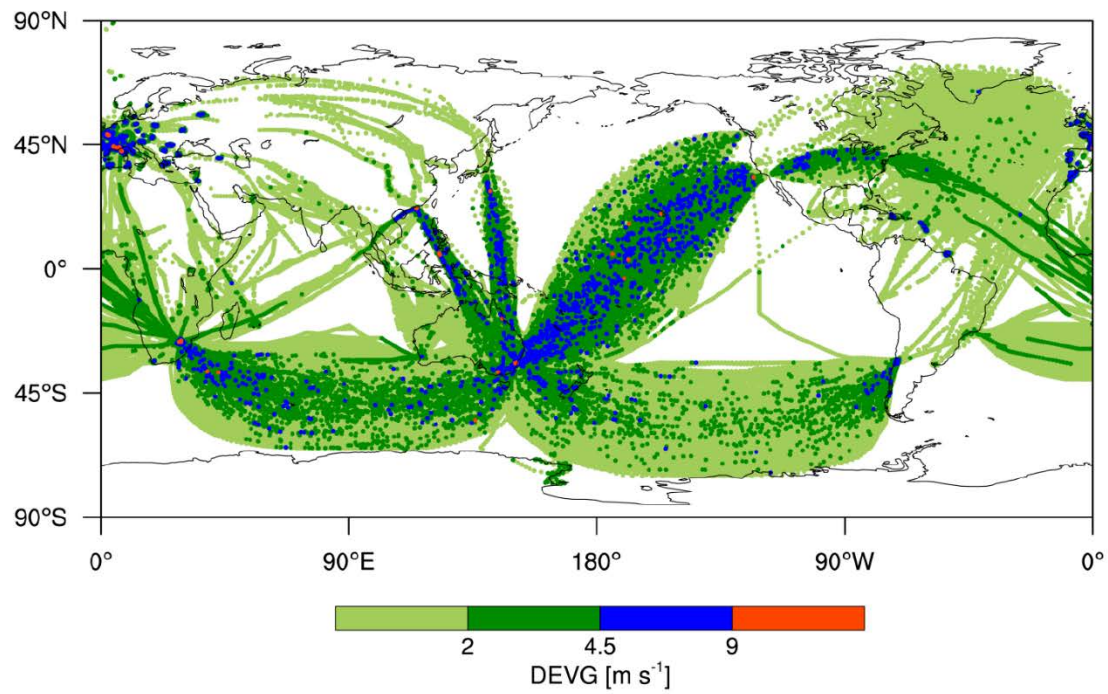


Figure 6. As in Fig. 2, except for the QCDEVG.

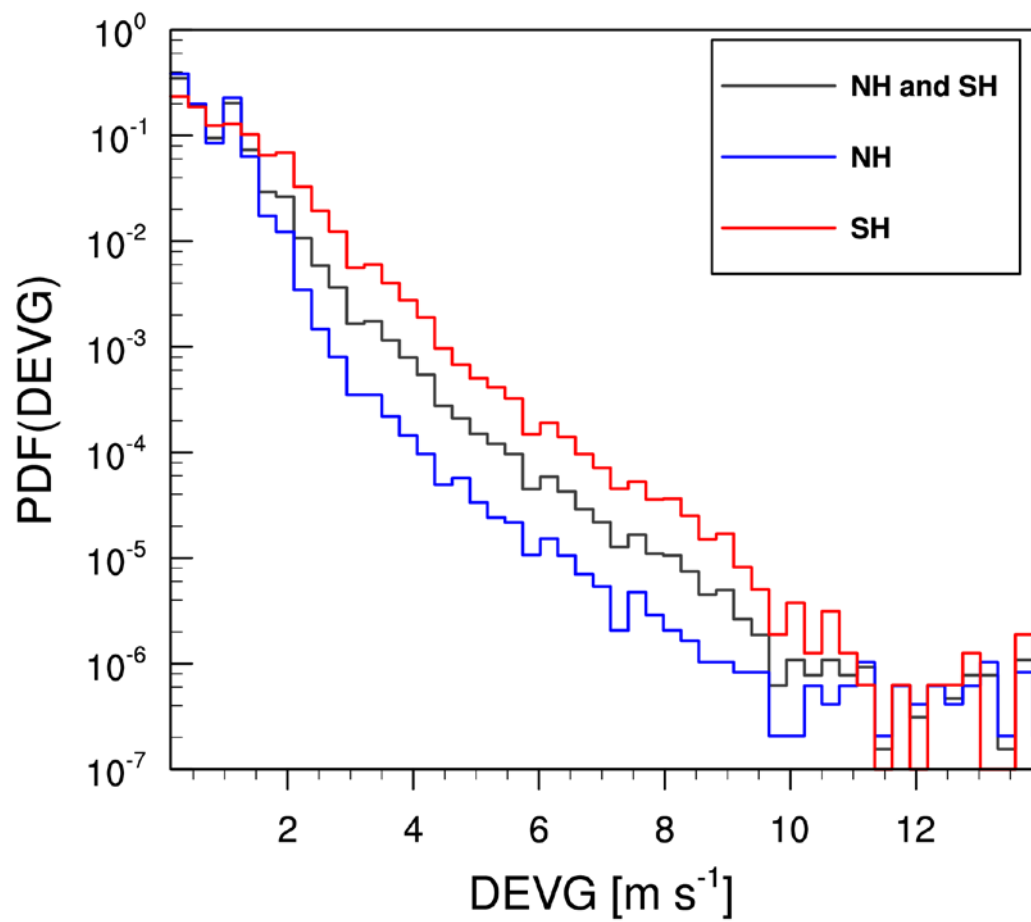


Figure 7. The PDFs of the QCDEVG over the globe (NH and SH: black line), NH (blue line), and SH (red line) at altitudes above 15 kft from October 2015 to September 2018.

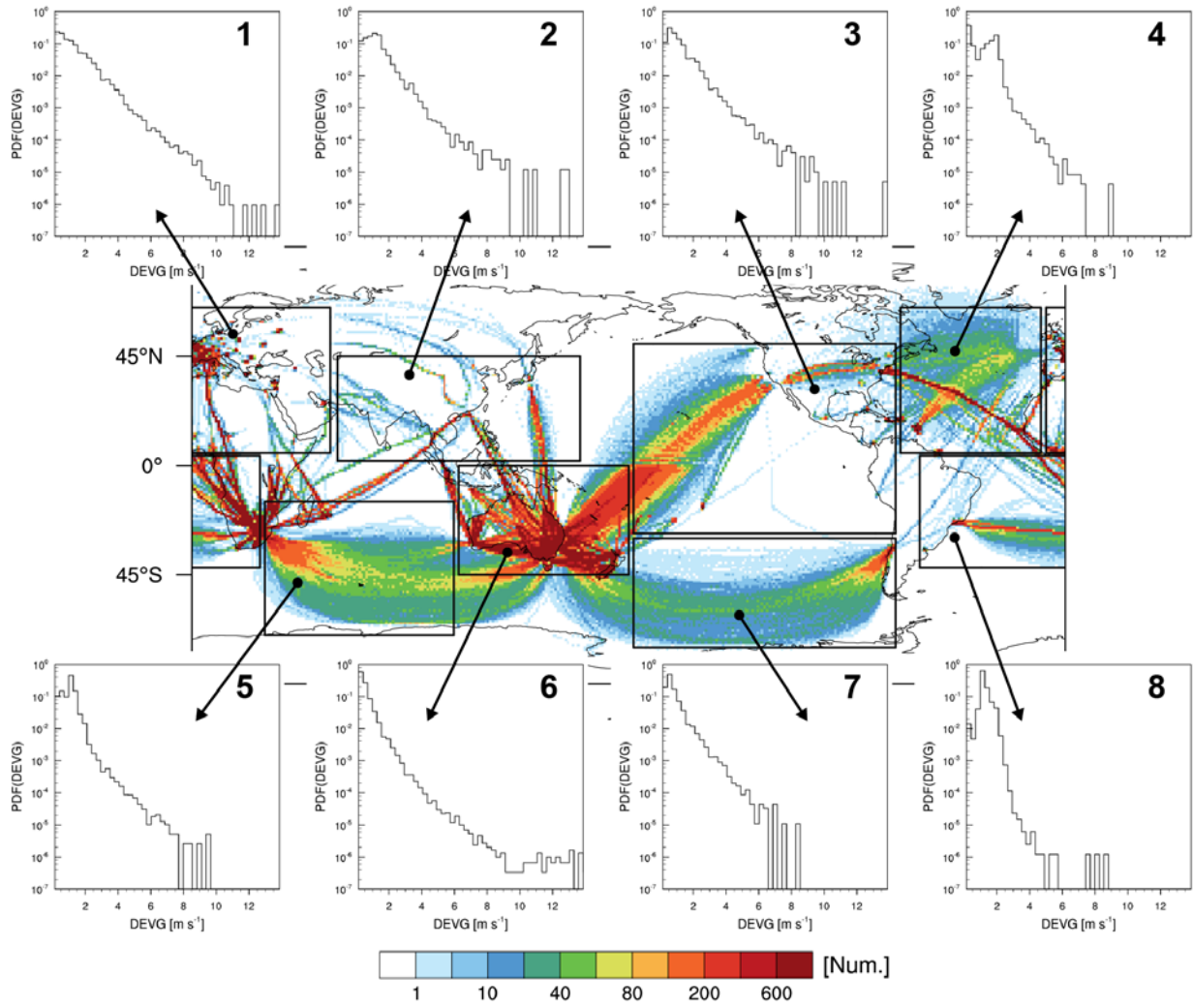


Figure 8. Horizontal distribution of the number of the QCDEVG data at altitudes above 15 kft, accumulated within a $1^\circ \times 1^\circ$ horizontal grid box from October 2015 to September 2018. The PDFs of the QCDEVG over eight selected regions, superimposed on the global map by rectangles.

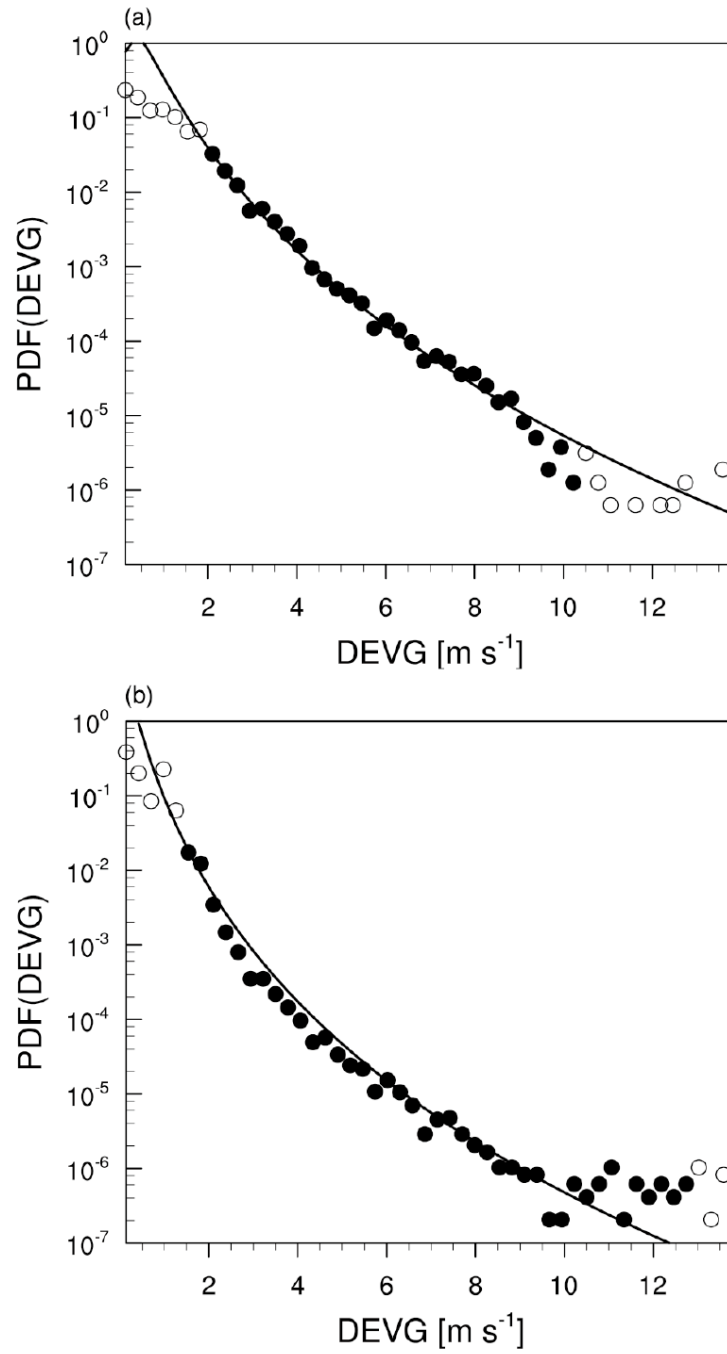


Figure 9. The PDFs (circles) of the QCDEVG and lognormal fit (continuous line) over the QCDEVG over the (a) NH and (b) SH. The filled circles indicate data that were used in the fit, and the open circles indicate data that are excluded from the fit.

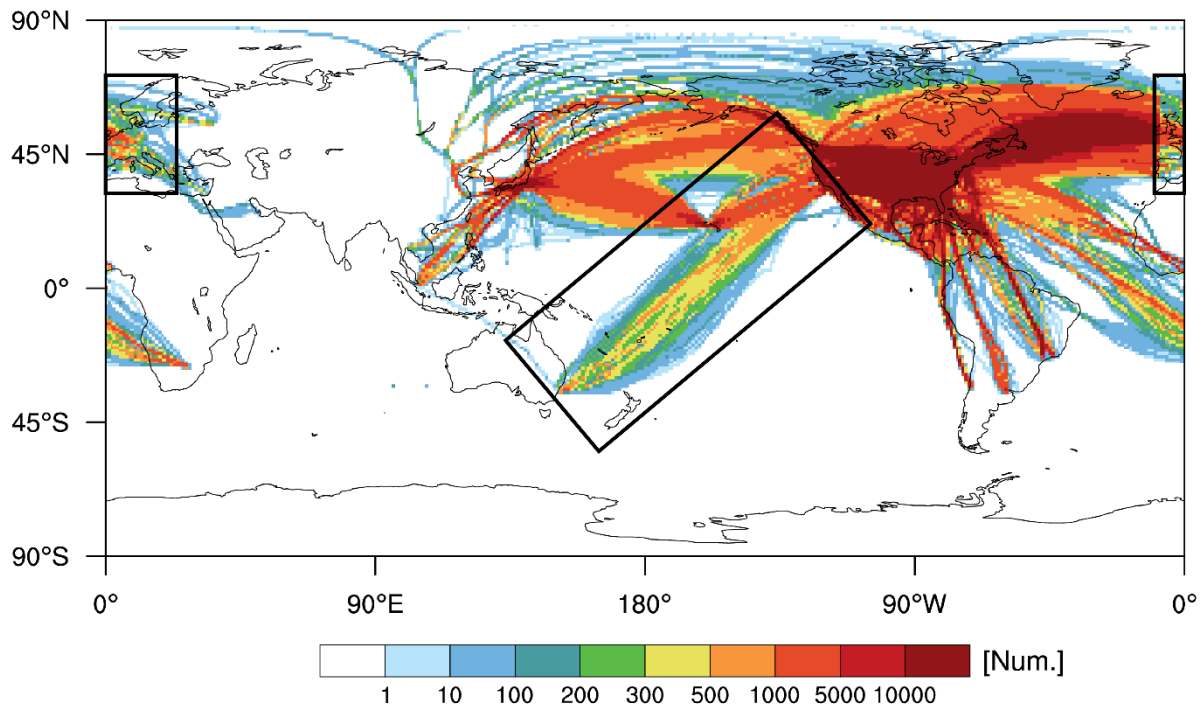


Figure 10. Horizontal distribution of the number of USED data at altitudes above 15 kft, accumulated within a $1^\circ \times 1^\circ$ horizontal grid box from October 2015 to September 2018. The regions of Europe and the trans-Pacific Ocean are indicated by rectangles.

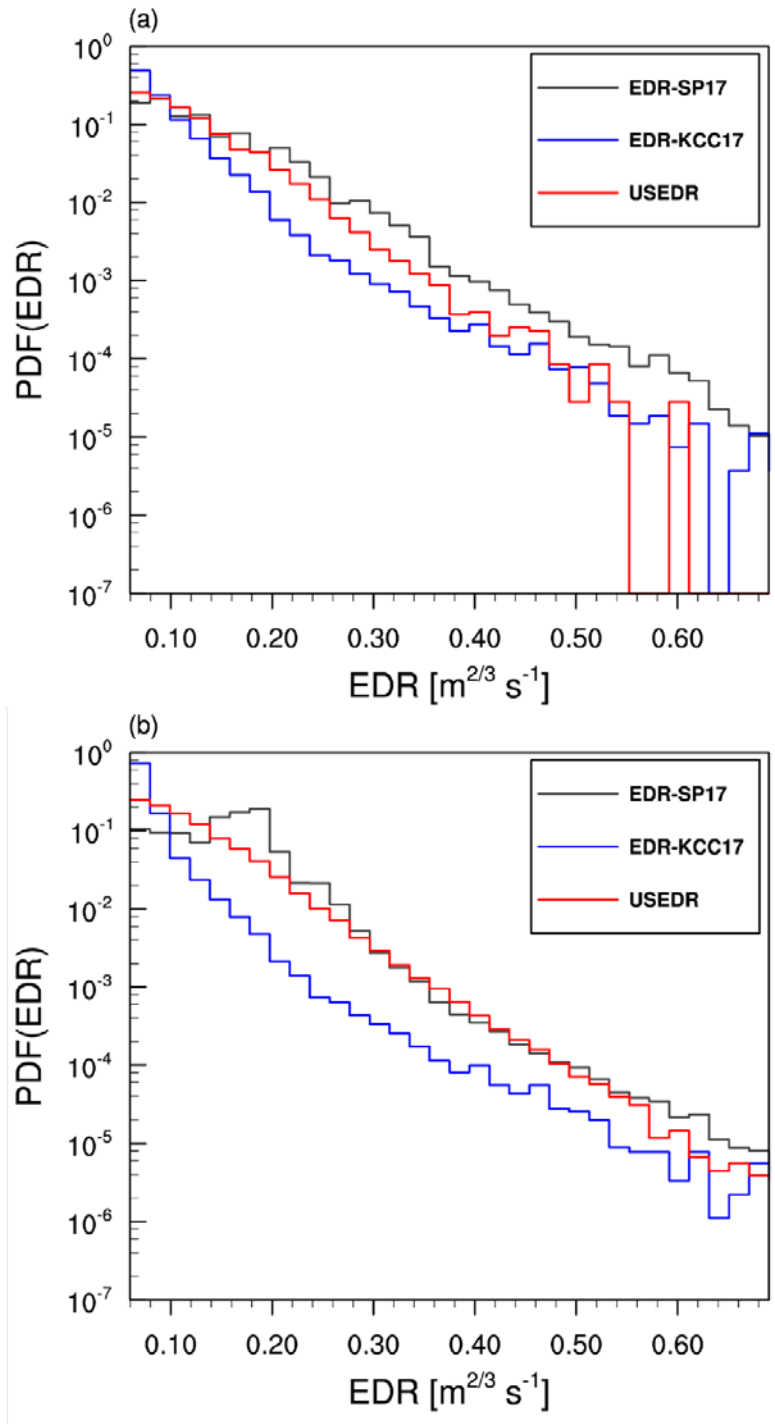


Figure 11. The PDFs of EDR-SP17 (black line), EDR-KCC17 (blue line), and USEDR (red line) at altitudes above 15 kft from October 2015 to September 2018 over (a) Europe and (b) the trans-Pacific Ocean routes indicated in Fig. 10.