Response to the Referee 1 comments

This is a very important study demonstrating a potential of a polarimetric radar for accurate estimation of ice water content in clouds by using a unique experimental setup combining X-band polarimetric radar measurements and in situ microphysical observations on the same airborne platform. It is shown in a number of flights that the polarimetric method grossly outperforms existing IWC-Z relations and that the combination of KDP and ZDR yields better accuracy of the IWC estimate than a use of sole KDP. I am particularly pleased to find out that empirically derived relations IWC(KDP) and IWC(KDP,ZDR) are very close to the theoretical relations derived by Ryzhkov et al. (1998, 2018). I found that the multipliers a1 and a2 in the empirical formulas (12) and (13) (shown in Table 1) are within 6% of the theoretical ones which is remarkable. I think that this should probably be mentioned in the paper. There are several technical deficiencies in the manuscript which have to be addressed before the paper can be recommended for publication.

We would like to thank the referee for these very helpful and constructive comments. We have highlighted the significance of our experimental result as you suggested. We have also addressed the various deficiencies that are pointed out by the referee throughout the paper. Please find our detailed responses to your comments as follows.

(1) I was confused by the definitions of IWCmeas and IWCmod. It took me awhile to realize that $IWC_{mod} = (1-Z_{DR}-1)IWC_{meas}$. This is very weird and, I am sure, will confuse other readers as well. I would recommend simply using $(1-Z_{DR}-1)IWC$ instead of IWCmod in the text and labels in Figs. 5 and 12.

We agree with the referee’s comment. In the revised manuscript, IWCmod is replaced by $(1-Z_{DR}^{-1})IWC$ to avoid any confusion.

(2) I may hypothesize that increasing negative bias in the radar IWC retrieval shown in Fig. 14 could be related to the minimal ZDR threshold of 0.6 dB. I would recommend to decrease the ZDR threshold in the IWC(KDP,ZDR) relation below 0.6 dB and see what happens. Adding large aggregates may disproportionally increase KDP and IWC. At the same time, ZDR decreases and may fall below 0.6 dB. Using values of ZDR lower than 0.6 dB will provide some “boost” for the IWC(KDP,ZDR) estimate.

We thank the referee for this very good suggestion. We have tested and found out that reducing the $Z_{DR}$ threshold indeed improve the estimation bias. However, smaller $Z_{DR}$ threshold increase rms as $(1-Z_{DR}^{-1})$ comes close to zero. Thus, we selected the threshold at which rms of Kdp-only method and $(K_{dp},Z_{DR})$ method are equal. We have revised the text and added figures to include this change.

(3) Number concentration $n$ in Eq (2) is not defined in the text.

The definition and unit of variable $n$ in Eq. (2) is added.
In Eq (5), $K_p^2$ is not equal to 0.177. It has to be the one for water.

We thank the referee for pointing out this error. The dielectric factor of water at 0°C is used for the computation of equivalent reflectivity, $K_p^2 = 0.93$.

Page 4. Cross sections $\sigma_{hh, vv}$ are not used in Eqs (1) – (6).

We agree. The radar cross sections are now removed.

Page 5. The approximation (1-ZDR$^{-1}$)IWC $\approx$ KDP is not correct and is not consistent with the value $a_2 = 0.135$ shown in Table 1.

We thank the referee for pointing this out. We actually meant “proportional” instead of “approximately equal”.

The reference to Korolev et al. (2018) cannot be found in the reference list.

The reference to Korolev et al. (2018) has been added.

Page 8. Both $\Phi_{DP}$ and $\Psi_{DP}$ may exhibit discontinuities due to phase wrapping.

We agree. Correction has been made.

Page 9. Two equations IWC(Z) are very different and both differ much from the popular Hogan et al. IWC(Z) equation. Please clarify and comment.

The two equations were derived by fitting a simple power-law curve to the joint frequency distribution of IWC and reflectivity (similar to Eq. (1) in Protat et al. (2016) but for measured X-band reflectivity in the HIWC flights). There might be a small bias in the radar reflectivity calibration so the coefficients in those equations could present a small error. However, the IWC(Z) is included just to demonstrate the traditional approach that uses $Z$ can lead to large uncertainties in the HIWC regions.

English usage has to be improved, e.g., data are plural, not single, etc.

We thank the referee for this comment. We have tried to correct language errors and improved the manuscript.

References:


Thanks for this reference. It has been added to the revision.
Response to the Referee 2 comments

This manuscript presents an assessment of ice water content (IWC) retrieval algorithms based on KDP only and combined KDP-ZDR observations using measured IWC from aircraft in-situ probes. Results show that both the KDP-only and combined KDP-ZDR method works much better than the reflectivity-based retrieval algorithms. Although KDP-only and KDP-ZDR combined IWC retrieval algorithms are not new concept, an algorithm derived from quasi-collocated in-situ measurement and radar observations is a good addition to the existing literature. Some sections of the manuscript lack details and are somewhat difficult to follow, especially section 2. Modifications to the manuscript are needed before it can be recommended for publication. Major concerns and questions that needed to be addressed are outlined below.

We would like to thank the reviewer for many constructive comments which helped improve the manuscript greatly. We have made many changes in the revised manuscript, and have added more references to improve the presentation of the manuscript. Please find our responses to your comments as follows.

General Comments:

1. Combining KDP and ZDR in IWC retrieval is not new concept. For example, Eq. (13) in the current manuscript is very similar to Eq. (29) in Ryzhkov et al. (1998). In my opinion, the authors should discuss more on the relationships and differences between the current study and the other more theoretical studies.

We agree that combining KDP and ZDR in IWC retrieval is not a new concept. As a result, we didn’t really provide an in depth review. In literature, there are many different equations representing the relationships between IWC, Z, $K_{dp}$, $Z_{dr}$ and parameters of the particle size distribution. We tested most of them and only focused on the methods (Kdp-only and $(K_{dp}, Z_{DR})$ combination) that work best for our data sets in the HIWC environment. We believe we have included enough review of the concept and we have also added a recent reference (Ryzhkov et al. (2018)) in the revised version of the manuscript.

2. Section 2 lacks detailed derivation and/or reference to existing literatures and is very difficult to follow. This section needs to be heavily rewritten. The author should provide detailed derivations or clearly refer to existing literatures for the equations. When doing so, the authors should make sure that the conventions of the equations are consistent.

In the revised manuscript, we have added references for each equation in section 2. Part of section 2.2 (P5) was re-written. Again, because the concept is not new, we did not include all the derivations that can be found in the literatures. Instead, we summarized the main findings which are important to our study.
We thank the referee for the comment on the inconsistence of the convention of the equations. We have corrected the errors.

3. The parameters \((a, b)\) used in the Kdp only and Kdp-ZDR combined algorithm are obtained from linear fittings of data from 7 cases. By looking at Figure 12, it seems different values of \((a, b)\) could be obtained if data from only one, or some of, the 7 cases are used in the fitting. What is the variability of the parameters \((a, b)\)? How large the retrieval uncertainty will be due to the uncertainty in \((a, b)\)?

In the revised manuscript, we have included the fitting coefficients for both methods in Table 2. The standard deviations for \((a_1, b_1)\) for the \(K_{dp}\)-only method and for \((a_2, b_2)\) for the \((K_{dp}, Z_{DR})\) method are \((0.12, 0.33)\) and \((0.032, 0.033)\), respectively. The uncertainty of the retrieval depends on the uncertainty in \((a, b)\) and the values of \(K_{dp}\) and \(Z_{DR}\). Typical values of \(K_{dp}\) and \(Z_{DR}\) for HIWC regions (MMD between 0.25 mm to 0.8 mm) are about 1 deg/km and 1.12 (or 0.5 dB) (from Fig. 6 in the revision). At those typical values, standard deviation of IWC estimates using \((K_{dp}, Z_{DR})\) is 0.6 g/m\(^3\).

Specific comments:

P2, L14: What is the conclusion of Ryzhkov et al. (1998)?

The conclusion of Ryzhkov et al. (1998) is briefly summarized in Section 2. In the revision, the text has been modified and a new reference (Ryzhkov et al. (2018)) has been added.

P3, L11 and L14: Which convention is used for the back-scattering matrices and forward scattering amplitudes?

It is in forward scatter alignment (FSA) convention. We thanks the referee for pointing this out. Additional text has been added to the revision to make it clear.

P3, L10 and L13: The radar observables, Zdr and Kdp, are usually integrated over a particle size distribution. Although Eq. (1) and Eq. (2) are OK if all the particles are of the same size and aspect ratio, this situation rarely happens. I think these equations can be removed since Eq. (5) and Eq. (6) are more general. Instead, the authors can discuss scattering properties in single particle level here.

We thanks the referee for this comment. The Eq. (1) and (2) are for \(n\) particles of same size \(D\) and axis ratio \(r\). The purpose of including Eq. (1) and (2) is to show that large number ice particles (which is relevant to HIWC regions) can contribute to a significant \(K_{dp}\). We’d like to keep those equations instead of including a discussion on the particle’s scattering properties because this paper mainly focuses on an empirically derived estimator for IWC based on radar polarimetric parameters \((K_{dp}, Z_{DR})\).
P3, L15-17: This sentence is confusing. I guess the authors mean that Zdr does not change with increasing number of small particles while Kdp increases with increasing number of particles. The authors may want to rephrase this sentence.

We agree with the referee. The sentence has been rephrased.

P3, L20: Is the permittivity of particle based on solid ice?

It is the relative permittivity of ice particles in the radar volume, which is unknown. An approximate relationship between relative permittivity and density of snow/ice particle can be found in Matrosov et al. (1996).

P5, Eq. (9-11): By using symbol for “approximately equal”, do the authors really mean “proportional”?

We thank the referee for pointing this out. The error has been corrected.

P5, Eq. (11): Derivation for this equation is needed. Also, Eq. (9) and Eq. (10) use integration over a PSD, why Eq. (11) only use one mass?

(please see the response after the next question)

P5, L7-9: Again, detailed derivation is needed. How to derive a closed form of IWC as a function of Kdp and ZDR? What does “particle mass variation is small within the radar volume” mean?

In the revised manuscript, we have removed Eqs (9)-11 and revised the text in L7-9. We’ve also added a recent reference by Ryzhkov et al. (2018). Detailed theoretical derivation and discussion of the IWC approximations based on (Kdp, ZDR) can be found in Ryzhkov et al. (1998, 2018); therefore, we decided not to include them in the paper.

P5, L19-20: What are the physical meanings of the constants b1 and b2?

We thank the reviewer for this question. Mathematically, the intercepts (b1 and b2) are mean values of IWC at Kdp = 0°. Physically, we do not know their meaning. When the ice particle orientation uniformly distributed in a plane perpendicular to the radar beam, Kdp = 0° but IWC can be larger than zero.

P10, L7: What does “initial observations” mean? Should the “include” be replaced with “indicate”?

We have modified the text to remove the confusion. It now reads “From Fig. 4, it follows: ...”

P10, L8: “latter” is confusing. Better to clearly state which observations are weighted and biased towards Zdr.

The sentence has been modified as suggested.

P10, L20: No blue line in Fig. 5(c).
We thank the referee for pointing this error. It is now corrected.

P10, L7-12: Are the polarimetric variables Kdp, Zdr, Zh, and rho_hv shown in Figure (4) measured at a specific distance from the airplane or averaged over a range? How about those shown in Figure (5) and (6)?

Those radar parameters were measured at a distance of 1000 m from the aircraft. The data were not averaged over the range but were decimated in time (along the flight path) to match with the temporal resolution of the in-situ data. Additional information on this has been included in the revised manuscript.

P13, L6: What are the coefficients (a, b) used for Kdp-only and (Kdp, ZDR) algorithms? Are same values used for the other case?

In study case May 26, the coefficients (a, b) for Kdp-only and (Kdp, ZDR) algorithms are (0.94, 0.7) and (0.12, 0.07), accordingly. The coefficients are different and are optimized for each case. We have added estimated coefficients for all selected flights in Table 2 and discussed on the variability of those coefficients in section 6.

P20, L12: I think the word “significantly” is too subjective and optimistic. For example, when Kdp=1, in panel (a), IWC varies by 50% of the maximum value (range 1∼2 with maximum 2), and in panel (b), modified IWC also varies by 50% (range 0.15∼0.3 with maximum 0.3). I would suggest remove the word “significantly”. We completely agree with the referee. The word “significantly” has been removed.

Technical corrections:

P1, L9: Is the differential reflectivity here in linear scale or log scale?

It is in log scale.


We apologize for the error. It has been corrected.

P3, L8: The book of Bringi and Chandrasekar (2001) has over 600 pages. Detailed page numbers or equation numbers are needed. The same for P3 L22 and other places.

We have added equation numbers in the book of Bringi and Chandrasekar (2001) to the revised manuscript.

P4, L26: IWC is not sensitive to shape and orientation sounds strange. IWC is independent of them. The authors may want to rephrase this sentence.

We thank the referee for this comment. This sentence has been revised. It now reads “For a given radar volume, if the orientation of the ice crystal changes, $K_{dp}$ value changes (Eq. (7)) while the IWC of the radar volume is not.”
P11, Figure 3 caption: “Bottom panel is shows” remove “is”.
This typo has been corrected.

P13, Figure 5 caption: using two values (0.1 and 0.05 degree) and “respectively” for three panels is confusing.
The values are for the last two panels (panel b and c). The caption has been modified to avoid the confusion.

P13, L5: “blue” should be “black” for measured IWC.
The error has been corrected.

P14, L5: “estimations” should be “estimation”.
We thank the referee for pointing this error. It has been corrected.

P14, L5: The panels of Figure 6 are not labeled by ‘a’ or ‘b’. Same for Figure 11.
We apologize for the missing labels. In the revised manuscript, all the figures have been checked and missing labels have been added.

P15, Figure 6: Should vertical axis labeled as “Error” instead of “Bias”?
In this study, measured IWC is considered as ground truth, hence, the difference between estimated IWC from radar data and measured IWC is labeled as bias. However, we have corrected the second sentence in the caption of Fig. 6 in the revision: “Bottom panel shows estimation (errors) biases for the three estimators.”

P18, L8: No ellipses in Fig. 11a.
We thank the reviewer for pointing this out. Ellipses have been added to Fig. 11a (it is now Fig. 12 in the revision).
Response to the Referee 3 comments

RC#3:

General Comment

The manuscript compared three radar measurement based IWC retrieval methods (Z only based, Kdp only based, and Kdp and Zdr based) using X-band polarimetric observation and in-situ observation and demonstrated that the Kdp and Zdr based method can provide better IWC estimates. The retrieved IWC agreed very well with the observed IWC from the in-situ measurement. The methods are based on observations, and I would expect to extend the techniques to other places in future; however, the manuscript did not mention effectiveness of the methods for other cloud types at different locations. The subject and results of the manuscript are suitable for the scope of the journal. However, this manuscript lacked detailed descriptions about how to estimate coefficients. In particular, estimated coefficient values were not presented. Some figure captions lacked explanations. I recommend major revision in terms of comments below.

We thank the referee for his/her review and encouraging comments. Regarding the suitability of our method to other non-HIWC environments, we focused our analysis to HIWC environment so didn’t speculate on if our result is applicable to other conditions. We are planning to extend our analysis of large dataset we accumulated in a recent projects and will report our findings once we complete the work.

As outlined in our responses the two other reviewers, we have made significant changes in the manuscript and added new figures and tables. We hope these changes make the paper easier to follow. Please find our responses to your specific comments as follows.

Specific comments

1. The manuscript lacked detailed descriptions about how to estimate coefficients (a1, b1, a2, and b2) and their values. Information below is at least needed:

1) The estimated coefficient values

2) Were the coefficient values estimated for each case or constant for all cases?

We thank the referee for pointing this out. In the revision, we have added texts to describe how to estimate the fitting parameters (in the caption of Fig. 5). Values of those parameters were estimated for each study cases are given in Table 2 of the revision. They were also computed for combined data of seven selected flights. The variability of those fitting parameters is briefly discussed in section 6.
3) How did you sample radar data? In-situ data was valid near the aircraft, while the radar could not collect data below a range of 1000 m from the aircraft. What are locations of the radar data used for the coefficient estimations? How did you match the radar data and the in-situ data? The sampling method may control the accuracy of the linear regression technique.

As provided in section 3.1, radar profiles were extracted at a horizontal distance of 1000 m from the aircraft. The data rate of the processed in-situ microphysics data is much lower than the radar data. Hence, the radar data were decimated to match with temporal resolution of the in-situ data (e.g. 1 s). At the Convair-580 average ground speed of 100 m s^{-1}, this results in a 100 m resolution along the flight line. The radar range resolution is 75 m and the data were not average over range.

4) How many cases (how many hours) were used for coefficient estimates?

It was 4.91 hours of data collection time (17699 data point at 1 s sampling period) for the seven selected cases.

5) Is there a dependency of the estimated coefficients on cases?

We do not see a dependency of the estimated coefficients over the study cases.

6) It is very worth to add a flow chart of the IWC retrieval technique.

We thank the reviewer for this good suggestion. However, we haven’t added additional flowchart as we felt the processes of our analysis has been detailed in the revised manuscript. Also, it may be more adequate to have the flowchart of the IWC retrieval technique when we complete a work where additional steps are added to the technique to improve its performance further.

2. Details about the radar data are needed. What are the beamwidth, radar range gate spacing, and time resolution? Did the radar point at a fixed direction during the flights or scan some directions (in that case, what are the elevation and azimuth)? Did the radar sampling volume match the in-situ measurement sampling volume?

We thank the referee for this comment. We have added a table (Table 1 in the revised manuscript), which lists some important radar parameters. All the antennas of the X-band radar system are fixed. As mentioned in section 3, the radar data used in this study were sampled at 1000 m horizontal distance from the aircraft, whereas the in-situ data were measured right at the aircraft location. For in-situ probes, the sampling volume is much smaller compared to the radar sampling volume.
3. A more description about IWC from PSD is also needed. What D-M parameterization was used? How was it tuned using IKP2 measurements? Again, a flow chart of the IWC calculation should be useful. Did the image probes scan particles at a horizontal plane (parallel to the horizontal plane) or vertical plane (perpendicular to the horizontal plane)? Can the scan direction cause some errors in the IWC calculation?

IWC was calculated from composite 2DS+PIP PSDs based on $M = aD^b$ size-to-mass parameterization. We agree that a flowchart of IWC calculation should be useful but it is beyond the scope of this work and should be found in the IWC reference paper (Korolev et al. 2018). The coefficient $a$ and $b$ were tuned using a non-linear regression to find the best correlation between IWC measured by IKP2 and calculated from PSD. The coefficients $a$ and $b$ are determined by dominant particle habits, and therefore they may vary depending on type of clouds, temperature range and altitude were the particles were sampled. For the particle images sampled from the Convair580 during the HIWC campaign the best agreement between two ways of IWC measurements were obtained for $a=7.0044e^{-12}$ and $b=2.3$. The laser beams of both PIP and 2DS probes used for particle image sampling were oriented vertically (the horizontal 2DS channel was not used). Such arrangement provides measurements of the maximum projection of particle images. The direction of scanning may affect assessment of IWC from 2D particle imagery. However, tuning of the $a$ and $b$ coefficients, which was employed in this study, compensates the effect of the direction of particle image sampling.

4. Is the technique presented in the manuscript valid for cases where graupel existed? Graupel particles generally have aspect ratio ~1, which are not sensitive to Kdp or Zdr. Deep convective cases could include supercooled liquid droplets and heavily- rimed particles. Were there effects of supercooled liquid droplets and heavily-rimed particles in the cases used in the analysis? Was the case dependency of the proposed technique? More case descriptions would be needed to help understanding the case dependency.

As briefly mentioned in the manuscript, the fraction of flight segments with supercooled drops was <5%. Our data are also consistent with a multi-year and multi-aircraft observations of the HAIC-HIWC flight data that are detailed in FAA report (Strapp et. al, 2018). We didn’t try to filter out those data points with supercooled drops in our analysis. Having said that we agree with the reviewer that the convective clouds we flew are likely consisted of heavily rime particles and graupel at the convective cores of the storms we flew.

Our main goal is to investigate if adding polarimetric capability to operational pilot X-band radars allows to detect and avoid HIWC environment. In this regard, commuter aircraft typically avoid the convective cores based of high reflectivity values and other data. So our work and conclusion don’t extend to convective core areas.
5. P. 14, lines 2-3: This sentence does not make sense to me. Please give more description about why Kdp can improve large aggregates effect, although it is sensitive small crystals. Just before the sentence, it was stated that (???) is more sensitive to the oriented small ice crystals.” Why Kdp can improve large aggregates effect? How did you know the orientation of ice particles?

We agree with the referee on this comment. We’ve added information about $K_{dp}$ and $Z_{dr}$ as a function of MMD (Fig. 6) in the revised manuscript. The text also has been modified in the revised manuscript: “The large errors in the $IWC - Z$ estimator are due to the presence of mixtures of large aggregates and small ice crystal regions as indicated in the PIP images (not shown) in clouds. Large aggregates have a dominant contribution into the radar reflectivity, which explains the positive biases of the $IWC - Z$ estimates. On the other hand, the magnitude of $K_{dp}$ in aggregates with MMD > 2 mm is usually smaller than 0.4 °/km and in small ice particles (MMD in the range 0.3 – 1 mm) is between 0.6 °/km to 1 °/km (Fig. 6a). It follows that estimators utilizing $K_{dp}$ information may not have strong biases toward large aggregates in radar volumes like the $IWC - Z$ estimator.”

6. P. 18 lines 10-11 “On the other hand,. . .”: This sentence does not make sense to me. Why the modified IWC was less sensitive to the particles’ shape and orientation, even though the Zdr constraint well worked for the IWC estimate?

We thank the reviewer for this comment. The sentence has been modified in the revised manuscript to have a better explanation: “On the other hand, the product $(1 - \frac{1}{Z_{DR}^2})IWC$ already includes the particles’ shape and orientation effects, thus, estimates based on it yield should better results.”

7. Evaluations for mode error sources should be discussed; how could Kdp estimation resolution, Zdr bias, and in-situ instrument limitation (difference between IWCmeas and IWCpsd) affect the IWC retrievals?

We agree with the referee that the error analysis of the retrieval algorithms is important. In addition to the factors mentioned by the referee, errors in IWC retrievals also depends on the uncertainty of the fitting coefficients. A complete error analysis of the IWC retrieval is beyond the scope of this work. In the revised manuscript, we have added some text to discuss the retrieval uncertainty at typical values of $K_{dp}$ and $Z_{DR}$ in the HIWC regions (section 6, P21-22). In summary, standard deviation of IWC estimates at HIWC regions is about 0.6 $g/m^3$.

8. Fig. 12: I do not know the meaning of Fig. 12. Why can you see “the modified version of IWC is better replicated by a simple linear regression model” from this figure? “Modified IWC” is the just measured IWC scaled by Zdr. Why is this better replicated by a simple linear regression
model then measured IWC? In both Fig. 12a and Fig. 12b, it seems that there is \( \sim 50\% \) variability in IWC at \( \text{Kdp} = 1 \). There is no significant difference between Fig. 12a and Fig. 12b. If you wanted to say that Eq. 13 can provide better correlations between IWC and polarimetric variables (Kdp and Zdr), this has been already shown by \( R^2 \) values in Fig. 5.

The \( Z_{\text{dr}} \) constraint is used to avoid large errors when \( Z_{\text{DR}} \approx 1 \). In general, Zdr values are not constant at different radar volumes; hence, \( (1 - Z_{\text{DR}}^{-1}) \text{IWC} \) is not a simply scaled version of IWC. We agree that the \( R^2 \) goodness of fit parameters in Fig. 5 already show that a linear regression fits \( (1 - Z_{\text{DR}}^{-1}) \text{IWC} \) better than IWC for the case of May 25. Figure 12 (now Fig. 14 in the revision) shows that the method also works well for other cases. In the revised manuscript, the sentence has been removed to avoid the confusion. We have also added estimated fitting coefficients for all the selected cases in Fig. 14 in Table 2 and discussed the variability in the coefficients in section 6.

9. “Modified IWC” is a confused phrase. In the manuscript, “modified IWC” represents the left hand side of Eq. 13. \((1-\text{ZDR}^{-1}) \text{IWC}\). This is IWC scaled by \([1-\text{ZDR}^{-1}]\), not actual IWC. Use an appropriate phrase through the text.

We completely agree with the reviewer. As it is also mentioned by another reviewer, “modified IWC” will confuse the readers. For a clear presentation, we have placed it with \((1 - Z_{\text{DR}}^{-1}) \text{IWC} \) throughout the revised manuscript.

Minor comments

1. Did you do attenuation corrections for reflectivity and Zdr? Attenuation corrections may not be needed for pure ice precipitation, but it would be good to mention about this.

No, in this work, no attenuation correction was applied to reflectivity and \( Z_{\text{dr}} \) as it pointed out by the referee that in ice precipitation and at close range, attenuation at X-band is negligible. Some text has been added to section 3.1 as suggested.

2. Did you do calibrate Zdr values for systematic offset?

Yes, we did.

3. What was the window size for calculating Kdp? What is the special resolution of Kdp?

The window size for calculating Kdp in our algorithm is 31 and the original Kdp range gate spacing (before decimation) is 30 m.
4. P. 10, lines 1-2 “The radar estimates. . .”: This sentence is unclear. Please add detailed descriptions.

We thank the referee for this question. It should read “The IWC estimates from radar data ...”. The sentence has been changed in the revision.

5. P. 10, line 8 (2): This feature is unclear in Fig. 4. Scatter plots of MMD, RHOhv and Zdr should be helpful.

The data shown in Fig. 4 are measured time series data so we do not have scatter plots of the parameters. Between 11:16:6 and 11:21:46 UTC, RHOhv decreased and Zdr increased at MMD peaks.

6. P. 10, line 9 and p. 14, line 2: How did you know the orientation of small crystals? Kdp should also be sensitive to larger crystals with aspect ratio /= 1. How did you know the particle aspect ratios?

We agree that, in general, the orientation of ice particles is unknown and saying $K_{dp}$ is only sensitive to small ice particle is not correct. The sentence in P10, L9 has been rewritten to remove this confusion. We have added a new figure (Fig. 6a in the revision) to show the typical values of the magnitude of $K_{dp}$ as a function of MMD for all the data used in this work. In general, $K_{dp}$ of large aggregates is smaller than that of small ice particles. The text in P14 has been revised to reflect this addition.

7. P. 10, lines 10-11: In Fig. 5, it seems to me that the break point where Zdr started increasing and RHOhv deceased was at Kdp ~1.5 deg/km.

We agree with the referee. Corrected as suggested.

8. P. 10, line 20: I cannot see any blue line Fig. 5.

The line colors in Fig. 5 were changed from blue to black but not the text. We apologize for this confusion. The text has been corrected.

9. P. 10, lines 20-21: I cannot see measured IWC or modified IWC in Fig. 5.

In the revision, the measured IWC and $(1 - Z_{DR}^{-1})IWC$ (was “modified IWC”) are in black.

10. Fig. 3b and Fig. 7b: Why is there a break line at 6-7 km range in reflectivity fields?

The break lines in those figures are locations of ground clutters which were filtered out. More information about the ground clutter contamination and filtering was given in section 3.1.
the revised manuscript, we have added some text to the figure captions to explain for those lines.

11. Please give height information for Figs. 3, 7, 9, 10.

Aircraft height information has been added for the figures as suggested.

12. Please give information about height, range, and temperature for Figs. 4, 5, 6, 8, 11, 13.

We have added a sentence in section 3.1 to indicate that in this work, the radar profiles were extracted at 1000 m from the aircraft for all the study case. The information of aircraft altitude and static air temperature for Fig. 4, 5, and 6 (May 26 case) is given in section 5.1 and for Fig. 8, and 11 (May 23 case) is given in section 5.2. The intervals of aircraft altitude and static air temperature for Fig. 13 (all study cases) are given in the Fig. 13 caption.

13. Unit of Kdp should be degrees / km through the manuscript?

We thank the referee for this question. It was a mistake. Correction has been made.

14. Fig. 5: What do red lines represent?

They are the linear fitting curves to IWC and \((1 - Z_{DR}^{-1}) IWC\) data. Last paragraph in P10 has been modified to include this information.

15. Fig. 5: I confused ‘scatter plots’ with red and black dots. I guess that ‘scatter plots’ here meant color shades representing frequency distributions. I recommend using ‘frequency distribution’ instead of ‘scatter plot.’

We agree with the referee and thank for the comment. The caption has been changed as suggested.

16. Fig 5: missed (a), (b), and (c)

In the revised manuscript, all the figures have been checked and missing labels have been added.

17. P. 18 line 8: I cannot find ellipses in Fig. 11.

We apologize for missing ellipses in Fig. 11. They are now included in the revised figure.

18. Caption of Fig. 3: Delete “is”

The redundant word “is” has been removed from the Fig. 3’s caption.
In addition to some correction to typos/mistakes pointed out by the RCs, below are a list of major changes made in the manuscript:

1. Section 2.2 was significantly re-written.
2. Most figures are updated. Some with labels changed, some with new analysis results.
3. Two new figures were added (Fig. 7 and Fig. 13 in the revised manuscript).
4. Additional text to describe the selection of optimal Zdr threshold used in the algorithm (section 6).
5. Added 1 table (Table 1 in the revised manuscript).
6. Updated Table 2 with values of fitting coefficients and new results using new Zdr threshold.
7. Discussion to the estimation error was added to section 6.
Determination of Ice Water Content (IWC) in tropical convective clouds from X-band dual-polarization airborne radar

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Abstract. This paper presents a methodology for ice water content (IWC) retrieval from a dual-polarization side-looking X-band airborne radar. Measured IWC from aircraft in-situ probes is weighted by a function of the radar differential reflectivity (Z_{dr}) to reduce the effects of ice crystal shape and orientation on the variation of IWC - specific differential phase (K_{dp}) joint distribution. A theoretical study indicates that the proposed method, which does not require a knowledge of the particle size distribution (PSD) and number density of ice crystals, is suitable for high ice water content (HIWC) regions in tropical convective clouds. Using datasets collected during the High Altitude Ice Crystal – High Ice Water Content (HAIC-HIWC) international field campaign in Cayenne, French Guiana (2015), it is shown that the proposed method improves the estimation bias by 35 % and increases the correlation by 4 % on average, compared to the method using specific differential phase (K_{dp}) alone.

1 Introduction

Ice water content (IWC) and its spatial distribution inside clouds are known for the significant effects they exert on the Earth’s energy budget and hydrological cycle (e.g. Stocker et al., 2013). Aside from its significant effect on the atmospheric processes, high ice water content (IWC > 1 g m⁻³), which is resultant from high concentration of small ice crystals in tropical mesoscale convective systems has been linked to aircraft incidents and accidents (Lawson et al., 1998, Mason et al., 2006; Grzych and Mason, 2010; Strapp et al., 2018). Since early 1990’s, over 150 engine roll-back and power-loss events have been attributed to the ingestion of ice particles produced in convective clouds (Grzych and Mason, 2010). Many studies have been undertaken to understand the details of the meteorological processes responsible for producing areas of HIWC. Equally important, methods using multi-platform observations from ground, airborne and space supplemented by weather models are being developed for improving detection and avoidance of high IWC regions that would be potentially hazardous for aviation (Strapp et al., 2018).

Conventional methods of deducing IWC from radar measurements assume a statistical relationship between the radar reflectivity factor (Z) and IWC. Such relationships are usually obtained based on IWC and Z calculated from in-situ measurements of particle size distributions (PSDs) and a size-to-mass parameterization (m(D)) (e.g. Heymsfield et al., 1977, Hogan et al., 2006). In recent studies (Protat et al., 2016), IWC was measured directly by bulk microphysical probes and Z
was measured from either an airborne or ground based radar. However, all of these studies show large uncertainties in the IWC-Z relationship despite the introduction of additional constraints such as air temperature (T) or the inclusion of refined \( m(D) \) in the IWC calculations (Fontaine et al., 2014, Protat et al., 2016).

Lu et al. (2015) conducted an extensive simulation on both millimeter- and centimeter- wavelength radar and concluded that the IWC-Z relationship is very sensitive to ice crystal PSDs (from one to two orders of magnitude in variability) and as such, is not recommended for IWC retrievals. Another approach employs polarimetric observations. The non-spherical geometry of ice crystals provides information on the types and habits of ice crystals (Matrosov et al., 1996, Wolde and Vali, 2001). It has been shown that the radar specific differential phase \( (K_{dp}) \) is less dependent on PSD, hence, is potentially useful for IWC retrieval (Vivekanandan et al., 1994; and Lu et al., 2015). Aydin and Tang (1997) suggested the possibility of combining \( K_{dp} \) and differential reflectivity ratio \( (Z_{dr}) \) for IWC estimation for clouds composed of pristine ice crystals. However, even for the polarimetric approach, knowledge about ice crystal mass density \( (\rho) \) and axis ratio is still needed to obtain accurate estimates of IWC. Simulation results (Lu et al., 2015) show that if only the general type of ice crystals is known, errors in IWC retrieval based on \( K_{dp} \) are within 30 % of their true values. Unfortunately, the aforementioned parameters \( (\rho \) and particle axis ratio) are, in general, unknown and additional assumptions are often invoked. Ryzhkov et al. (1998), for instance, took into consideration ice crystal shapes, size-density parameterization of scatterers to reduce the uncertainty in IWC estimates. Modelling work (Ryzhkov et al., 1998) shows that for average-sized pristine and moderately aggregated ice crystals, the ratio between the reflectivity difference \( Z_{DP} = Z_H - Z_V \) and \( K_{dp} \) is practically insensitive to the shape and density of the ice particles and is a good estimator of their mass.

In this paper we present a new method for assessment of IWC based on the \( K_{dp} \) and \( Z_{dr} \) measurements from a side-looking X-band airborne radar in tropical mesoscale convective systems (MCS). The IWC will be weighted with a function of \( Z_{dr} \) to minimize the dependency of the IWC-\( K_{dp} \) relationship on the particle shape and orientation, hence improve the IWC estimation errors without knowledge of the PSD or density of the ice particles. The proposed method is examined using datasets collected during the High Altitude Ice Crystal – High Ice Water Content (HAIC-HIWC) international field campaign in Cayenne, French Guiana in May, 2015. The campaign was carried out to enhance the knowledge of microphysical properties of high altitude ice crystal and mechanisms of their formation in deep tropical convective systems in order to address aviation safety issues related to engine icing (Strapp et al., 2018).

2 Background

2.1 Polarimetric parameters characterizing ice crystals

In conventional single-polarization Doppler radar, measured radar reflectivity, and radial velocity are used to assess cloud and precipitation spatial variability, precipitation rate and characteristic hydrometeor types. In dual-polarization radar systems, measurements are made at more than one polarization state (Bringi and Chandrasekar, 2001). Such systems can be configured
in several ways depending on the measurement goals and the choice of orthogonal polarization states. In this study, the results and discussions will be limited to the consideration of linear horizontal and vertical (H/V) polarization basis. The intrinsic backscattering properties of the hydrometeors to the two polarization states enable the characterization of microphysical properties such as size, shape and spatial orientation of the cloud/precipitation particles in the radar resolution volume. Hence, using polarization, it is generally possible to achieve more accurate classification of hydrometeor types and estimate hydrometeor amounts such as rain fall rate. Polarimetric backscattering properties of hydrometeors depend on many factors such as radar wavelength, radar elevation angle, particle size, shape, orientation, etc. In this section, we summarize how the differential reflectivity \( Z_{dr} \, \text{dB} \) and the specific differential phase \( K_{dp}, \text{o} \, \text{km}^{-1} \) are measured by a polarimetric Doppler radar in the Rayleigh scattering regime and at low radar elevation angles.

In general, the differential reflectivity of an ensemble of \( n \) particles of size \( D \) and axis ratio \( r \) is given by (1) (Eq. (7.4) in Bringi and Chandrasekar, 2001),

\[
Z_{dr} = 10 \log_{10} \left[ \frac{|S_{hh}(r,D)|^2}{|S_{vv}(r,D)|^2} \right] \tag{1}
\]

where, \( S_{hh} \) and \( S_{vv} \) are the diagonal elements of the back scattering matrices in the forward scatter alignment (FSA) convention.

The specific differential phase is defined as (Eq. (7.6) in Bringi and Chandrasekar, 2001),

\[
K_{dp} = \frac{2\pi n}{k} \text{Re} \left[ f_{hh}(r,D) - f_{vv}(r,D) \right] \tag{2}
\]

Where \( n \) is the number concentration in \( l^{-1} \), \( k \) is wavenumber in \( m^{-1} \), \( \text{Re}[] \) stands for the real part of a complex number and \( f_{hh}, f_{vv} \) are the forward scattering amplitudes in \( m \) at horizontal and vertical polarization, respectively. Equation (2) shows that \( Z_{dr} \) does not change with increasing number of ice particles while \( K_{dp} \) is proportional to \( n \). Consequently, for a large number of small particles with the axis ratio close unity \( (r \approx 1) \), \( Z_{dr} \rightarrow 0 \, \text{dB} \) and the second term in Eq. (2) becomes small but \( K_{dp} \) still can be large.

In a simple form of the calculations of \( Z_{dr} \) and \( K_{dp} \) of ice crystals, it is customary to approximate columns as homogeneous prolate spheroids and plates as homogeneous oblate spheroids. In the case of side incidence, the elevation angle is assumed to be close to zero and there is no (or very small) canting in the vertical plane. In the absence of wind shear and turbulence, and assuming a perfectly aligned spheroid model, \( Z_{dr} \) and \( K_{dp} \) can be expressed as functions of ice particle size, axis ratio and the relative permittivity of the particle \( (\varepsilon) \). For example, for oblate spheroid ice particles with a particle size distribution, \( N(D) \) (Eq. (7.5) – (7.8) in Bringi and Chandrasekar, 2001),

\[
|S_{hh}(r,D)| \approx \frac{k^2}{4\pi} \frac{V(D)|\varepsilon - 1|}{[1 + \frac{k^2}{2} (1 - \lambda_o)|\varepsilon - 1|]} \tag{3}
\]

\[
|S_{vv}(r,D)| \approx \frac{k^2}{4\pi} \frac{V(D)|\varepsilon - 1|}{[1 + \lambda_o|\varepsilon - 1|]} \tag{4}
\]

\[
Z_{hh, vv} = \frac{\lambda^4}{\pi^5 K_p^2} \int 4\pi |S_{hh, vv}|^2 N(D) dD \tag{5}
\]
\[ K_{dp} = \frac{k}{2} \int \left[ \frac{|\varepsilon - 1|}{1 + \frac{1}{2}(1 - \lambda_o) |\varepsilon - 1|} - \frac{|\varepsilon - 1|}{1 + \lambda_o |\varepsilon - 1|} \right] V(D) N(D) dD \]  

where, \( K_p \) is dielectric factor of water at 0°C (\( K_p^2 = 0.93 \)) and \( V(D) \) is the particle volume, \( \lambda_o \) is the depolarizing factor, which is only a function of the axis ratio \( r = b/a \) (for oblate particles, \( a \) is the semi-major axis length and \( b \) is the semi-minor axis length \( (a > b) \)). The depolarizing factor is defined as:

\[
\lambda_o = \lambda(\text{oblate}) = \frac{1}{f^2} \left( 1 - \frac{1}{f} \tan^{-1} f \right); \quad f^2 = \frac{1}{r^2} - 1
\]

A similar equation for \( K_{dp} \) can also be derived for prolate spheroid ice particles with symmetry axis parallel to the horizontal plane (Hogan et al., 2006).

On other hand, the IWC can be defined in terms of the size distribution,

\[
\text{IWC} = \int \rho(D) V(D) N(D) dD
\]

where, \( \rho(D) \) is the mass density of ice crystals with size \( D \).

### 2.2 Polarimetric methods for IWC retrieval

An inspection of Eqs. (3) and (4) suggests that for small ice crystal particles, the radar cross section \( \sigma_{\text{hh,vv}} = 4\pi |S_{\text{hh,vv}}|^2 \) is roughly proportional to the square of the ice particle mass \( (\rho_i^2(D) V(D)^2) \), a conclusion also confirmed by results from simulated data (Lu et al., 2015). In addition, according to Lu et al. (2015), for particles with sizes comparable or larger than the radar wavelength, there is no clear relationship between the radar cross section and ice particle mass due to the Mie resonance effects. In either case, \( \sigma_{\text{hh,vv}} \) is not directly proportional to the particle mass. Hence, the \( Z - \text{IWC} \) relationship depends strongly on the particle size distribution and the radar frequency. Consequently, using \( Z \) only to estimate IWC without knowledge of the PSD can lead to errors as large as one order of magnitude. On the other hand, Eq. (6) indicates that if the terms in square brackets \( (\alpha) \), are proportional to the ice density \( (\rho(D)) \), then the \( K_{dp} - \text{IWC} \) relationship is independent of PSD. The proportionality constant depends on several factors such as the ice crystal type, orientation and the measurement elevation angle. It is shown that the variability of this proportionality constant significantly increases at large elevation angles (Lu et al., 2015). Furthermore, when the exact ice crystal type is known, averaged relative error in the estimated IWC using \( K_{dp} \) can be as small as 10 %, regardless of whether PSD is known or not. If the ice crystal types are unknown but can be generally categorized, the errors can be higher, but mostly less than 30 %. These numbers were averaged from elevations in the interval \([0° – 70°]\). If IWC is estimated using \( K_{dp} \) at small elevation angles (less than 10°) such as from a side looking antenna, we would expect better results.

For a given radar volume, if the orientation of the ice crystal changes, \( K_{dp} \) value changes (Eq. (7)) while the IWC of the radar volume is not. Consequently, in the case of spatial variability of ice crystal shapes and orientations, the IWC estimation based solely on \( K_{dp} \) may be biased. To mitigate this problem, the measured IWC need to be modified to include the information of the ice particles’ orientation. One way to do this is to weight the measured IWC by a function of ice crystal shapes and
orientations before applying a linear regression model to the $K_{dp} - IWC$ relationship. In a simple approach, the weighting function can be in a form of $Z_{DR}^a (Z_{DR}^a$ is the linear version of $Z_{dr}$ and $a$ is a constant coefficient) as suggested in Aydin and Tang (1997) (derived from their approximation $IWC \approx K_{dp}^a Z_{DR}^b$ where $a$ and $b$ are constant coefficients). Proceeding more rigorously, Ryzhkov et al. (1998 and 2018) demonstrated that both $K_{dp}$ and difference reflectivity $Z_{DP} (Z_{DP} = Z_H - Z_V)$ are dependent on the particles’ aspect ratios and orientation, whereas their ratio is very robust with respect to those factors. Indeed, simulation and modelling work considering 12 different crystal habits, Ryzhkov et al. (2018) showed that the ratio $Z_{DP} / K_{dp}$ in combination with reflectivity can be used to estimate IWC. In detail, for exponential size distribution and with assumption of $\rho(D) = aD^{-\beta}$, $\beta \approx 1$, $(1 - Z_{DR}^{-1})IWC$ is proportional to $K_{dp}$. Also, according to Ryzhkov et al. (2018), this approximation is almost insensitive to the ice habit, aspect ratio, and orientation of the ice particles, but is affected by the degree of riming. Hence, it works better for clouds with low degree of riming. This condition might not be true for all the types of ice clouds, but might be suitable for HIWC regions, which are often composed of high concentration of small ice particles (Leroy et al., 2016).

At $Z_{DR} \approx 1$ (or $Z_{dr} \approx 0$ dB), the weighting function $(1 - Z_{DR}^{-1})$ is close to zero; and hence, it can introduce large errors in the estimates. Therefore, there should be a certain threshold for $Z_{dr}$ to determine how the weighting function would be calculated. In detail, if $Z_{dr}$ is less than a threshold, the weighting function $(1 - Z_{DR}^{-1})$ is replaced by $(1 - Z_{DR-threshold}^{-1})$. In this paper, we use $Z_{DR-threshold} = 1.12$ (see section 6 for more detailed derivation of this threshold value). This threshold is very close to a 1.15 threshold proposed by Ryzhkov et al. (1998) for “cold” storms for temperature below $-5^\circ C$.

In summary, there are two polarimetric methods for IWC retrieval, which will be investigated and compared in this paper. They are expressed as,

\[ IWC = a_1 K_{dp} + b_1 \quad (9) \]
\[ (1 - Z_{DR}^{-1})IWC = a_2 K_{dp} + b_2 \quad (10) \]

where, model parameters $(a_i, b_i)$ will be estimated from measured data.

### 3 Airborne measurements

During the Cayenne HAIC-HIWC project, the NRC Convair-580 conducted fourteen research flights in both continental and oceanic mesoscale convective systems with high IWC. For this campaign, the Convair aircraft was instrumented by the NRC and Environment and Climate Change Canada with an array of in-situ cloud microphysics probes, atmospheric sensors and the NRC Airborne W- and X-band (NAWX) Doppler dual-polarization radars (Wolde and Pazmany, 2005). The unique quasi-collocated in-situ and radar data collected during the HAIC-HIWC mission provided a means for developing techniques for detection and estimation of high IWC that could be adopted in operational airborne weather radars.
3.1 Airborne radar data

In this study, dual-polarization radar data from the NRC airborne X-band radar (NAX) (Fig. 1) side looking antenna are used. Some important radar parameters are given in Table 1. More detailed information on the radar system can be found in Wolde and Pazmany (2005). In the Cayenne project, the radar complex I and Q samples are processed to powers and complex pulse pair products according to the radar parameter specifications table and the products are recorded in binary format. Due to the size of the aircraft radar radome, the NAX dual-polarization parabolic side antenna is relatively small (26”), hence, exhibits some limitations in terms of sidelobe performance. The antenna OMT/feedhorn combination is relatively large compared to the parabolic dish. The large feed structure creates some significant sidelobes at ±90° planes. As a result, when the sidelobes intercept targets with strong returns below the aircraft, such as the earth surface or a storm melting layer, significant returns from the sidelobes will contaminate signals coming via the antenna’s main lobe. In most situations, the effect is more prominent at a range equal to or greater than the distance where the antenna sidelobes hit the ground. At regions where signals are contaminated by ground clutter via the sidelobes, the data are intermittent and exhibits large biases. Unfortunately, with the pulse pair data from the Cayenne campaign, methods to separate clutter from the precipitation signals are limited. To overcome this issue, a method is developed to detect regions with strong clutter contamination based on signal correlations between the nadir and zenith returns. If the correlation coefficient exceeds a pre-defined threshold, the corresponding side data in those regions are discarded. If the width of the discarded data region is relatively small (less than 300 m in radar range) it will be filled through interpolation. In addition, due to the limitation of the radar hardware, the measurements of dual-polarization parameters are not useable below a range of 1000 m from the aircraft, but reflectivity can be measured accurately from 450 m. Hence, in this work, radar profiles were extracted at a horizontal distance of 1000 m from the aircraft. This is not an ideal condition, when the in-situ data and the radar data are not spatially coincident. However, in most scenarios the advantage of having fine radar sampling volumes with high order of accuracy in time synchronization between in-situ probes overcomes the location offset. At large distances from cloud boundaries and convective cores, the microphysics properties of glaciated clouds can be considered spatially quasi-uniform at scales of the order of few hundred meters. This is specifically relevant to the measurements in MCSs during the HAIC-HIWC project. Moreover, there was no attenuation correction applied to reflectivity and \( Z_{dr} \) because in ice precipitation regions and at close range, attenuation at X-band is negligible.

For the Cayenne project, the in-situ microphysical data are processed at 1 Hz which is lower than that of the radar data. Hence, the radar data were decimated to match with temporal resolution of the in-situ data. At the Convair-580 average ground speed of 100 m\( \text{s}^{-1} \), this results in a 100 m radar sampling volume.
Table 1: X-band radar parameters for the Cayenne campaign.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>RF output frequency</td>
<td>9.41 GHz ± 30 MHz</td>
</tr>
<tr>
<td>Side antenna beamwidth</td>
<td>3.5°</td>
</tr>
<tr>
<td>Pulse width/range resolution</td>
<td>500 ns / 75 m</td>
</tr>
<tr>
<td>Dwell time</td>
<td>0.136 s</td>
</tr>
<tr>
<td>Sampling resolution</td>
<td>75 m</td>
</tr>
</tbody>
</table>

3.2 In-situ data

For the project, the NRC Convair-580 was equipped with state-of-the-art in-situ sensors for measurements of aircraft and atmospheric state parameters and cloud microphysics. There were multiple sensors to measure bulk liquid water content (LWC) and total water content (TWC), hydrometeor size distribution ranging from small cloud drops to large precipitation particles. Detailed list of the Convair in-situ sensors used during the Cayenne HIWC-HIWC project are provided in Wolde et al. (2016). Here we will briefly describe the in-situ microphysical sensors used in correlating the airborne radar measurements with regions of HIWC. TWC was measured by an Isokinetic probe (IKP2) that was specifically designed to measure very high TWC (Davison et al., 2016). Alternatively, IWC was estimated from the measured PSDs with the D-M parameterization was tuned using IKP2 measurements. In the Cayenne Convair datasets, IWCs calculated from PSDs and measured by IKP2 agreed
quite well and the difference between them in the HIWC regions on average did not exceed 15 %. Because the IKP2 data were not available in all flights, estimated IWC from PSDs ($IWC_{PSD}$) has been used in this work. Additionally, mean mass diameter (MMD) was also used to characterize the microphysical properties of the high IWC regions and interpret X-band radar measurements. MMD was calculated from composite particle size distributions measured by SPEC 2D-S and DMT PIP 2D imaging probes.

As shown in Korolev et al. (2018) in the MCSs studied during the Cayenne HAIC-HIWC project, the fraction of mixed phase clouds at -15 °C<T<-5 °C did not exceed 4.6 %, and that in most mixed phase cloud regions LWC<IWC. Hence, we didn’t filter out the very small fraction of liquid observed in our analysis, i.e., we assumed TWC = IWC. This finding significantly simplifies the processing and interpretation of cloud microphysical measurements.

4 $K_{dp}$ estimation algorithm for X-band airborne weather radar

The radar specific differential phase ($K_{dp}$) is defined as the slope of the range profile of the differential propagation phase shift $\Phi_{dp}$ between horizontal and vertical polarization states (Bringi and Chandrasekar, 2001). The measured differential phase shift between the two signals at the H and V polarizations, $\Psi_{dp}$, contains both $\Phi_{dp}$ and differential backscatter phase shift $\delta_{dp}$. If $\delta_{dp}$ is relatively constant or negligible, the profile of $\Psi_{dp}$ can be used to estimate $K_{dp}$. The estimated phase $\Psi_{dp}$ usually exhibits discontinuities due to phase wrapping, statistical fluctuations in estimation and the gate-to-gate variation of $\delta_{dp}$. Because the statistical fluctuations in the estimates of $\Psi_{dp}$ will be magnified during the differentiation, resulting in a large variance of the $K_{dp}$ estimates, the following considerations need to be addressed in the $K_{dp}$ estimation algorithm.

- Phase unfolding: phase wrapping occurs when the total $\Phi_{dp}$ accumulation exceeds the unambiguous ranges. This depends on the system differential phase $\Phi_{dp}(0)$ and the cumulative phase due to the medium. The NAX radar operates in the simultaneous transmission mode (VHS) and the unambiguous range is 360 °. The system differential phase $\Phi_{dp}(0)$ of NAX is about 64 °. For the Cayenne dataset, no observations have been made when the phase was folded.

- $\delta_{dp}$ “bump”: it seems that $\delta_{dp}$ was negligible in the HIWC environment in the Cayenne campaign. We did not observe the presence of significant changes in $\delta_{dp}$ over a short range.

- Range filtering: in this work, the range scale was set at 500m, thus, the fluctuations at scales smaller than 500 m will be suppressed.

Once the phase data are quality controlled, filtered and decimated to match the temporal resolution of the in-situ data, a heuristic algorithm similar to one reported in Rotemberg (1999) is applied to the data to extract $\Psi_{dp}$ smooth trend and then $K_{dp}$ is computed from it. This approach does not require an assumption of $\Phi_{dp}$ being a monotonically increasing function as it is in some other existing $K_{dp}$ retrieval algorithms (Wang and Chandrasekar, 2009); therefore, it would also work well with
negative $K_{dp}$ which possibly exhibits in ice clouds. Our preliminary analysis shows that the algorithm can provide estimates with standard deviation no greater than $1\,\text{km}^{-1}$. The NRC $K_{dp}$ estimation algorithm is summarized in the flowchart below.

![Flowchart](image)

Figure 2: The NRC $K_{dp}$ estimation algorithm for X-band radar diagram.

5 Results

In this section, preliminary results illustrating the performance of the proposed polarimetric algorithms are presented. Besides the polarimetric method, we also include results from the conventional $IWC - Z$ relations for comparison. Because the histogram of static temperature (not shown) indicated a bimodal distribution with two centres at around -5 °C and -10 °C, two $IWC - Z$ relations at $T = -5\,\text{°C}$ ($IWC = 0.257Z^{0.391}$) and at $T = -10\,\text{°C}$ ($IWC = 0.253Z^{0.596}$) were obtained by fitting power-law curves to scatter plots of all the data points at those two temperature levels (Wolde et al., 2016).

5.1 Case study I: May 26 flight

In this case, a 20-minute segment of the flight on May 26, 2015 is selected. Figure 3a shows IR satellite imagery obtained during the flight where the aircraft’s flight track is shown in different colors, which represent the aircraft’s location at different time segments. The reflectivity field from the NAX side antenna is shown in Fig. 3b. The selected period begins at a point...
when the aircraft started to sample at the proximity of the convective core of the storm with the lowest cloud top brightness temperature (white segment in the IR image). The brightness temperature was increasing toward the end of the segment (magenta segment). The aircraft flew between 6.9 km to 7.2 km altitude and the static air temperature ($T_s$) varied from -12.8°C to -8.2°C. In addition to the radar data, $IWC_{PSD}$ and MMD time series from particle probes are shown in Fig. 4. The IWC estimates from radar data have been decimated to match with the temporal resolution of the in-situ data.

The aircraft sampled two regions: a convective region before 11:23 UTC and a stratiform region after 11:25 UTC (Fig. 3b), with IWC in both regions was mostly higher than $1.5 \, gm^{-3}$ (Fig. 4a). It is worth noticing that the reflectivity measurements along the flight path was fairly constant at ~20 $dBZ$ and the MMD values were relatively small at HIWC regions ($IWC > 1.5 \, gm^{-3}$) (Fig 4a). From Fig. 4, it follows: (1) $K_{dp}$, in general, is highly correlated with IWC; (2) $K_{dp}$ increases at the regions dominated by small ice crystals (between 11:08 to 11:16 UTC and 11:24 to 11:27 UTC); (3) regions with larger MMD exhibits deceasing $\rho_{hv}$ and increasing $Z_{dr}$. In Fig. 5, $Z_{dr}$, $\rho_{hv}$ and IWC are expressed as functions of $K_{dp}$. In this case, there is a break point at $K_{dp} \approx 1.5^o/\text{km}$ (and $Z_{DR} \approx 1.12$) where $Z_{dr}$ started increasing and $\rho_{hv}$ deceased with respect to $K_{dp}$. At $K_{dp} < 1^o/\text{km}$, $Z_{dr}$ was mainly flat and IWC linearly increased with respect to $K_{dp}$ (Fig. 5b). This suggests the pristine ice crystals’ axis ratio might be fairly constant but the particle number density increased resulting in an enhancement in both $K_{dp}$ and IWC (shown by a linear IWC-$K_{dp}$ relationship). From $K_{dp} > 1^o/\text{km}$, $Z_{dr}$ increment with respect to $K_{dp}$ was greater, but the IWC increase does not follow the same degree as in the previous segment. If a linear IWC-$K_{dp}$ relationship derived from the first segment ($K_{dp} < 1^o/\text{km}$) is applied to the second portion, IWC will be overestimated. It is not easy to identify the exact reasons of this observations. Many factors could contribute to this circumstance such as changes in ice crystals’ size, shape, orientation (e.g. particle with higher axis ratio that are aligned in the horizontal plane) or particle’s density. In this work we used $K_{dp}$ and $Z_{dr}$ to mitigate this dependency and improve estimation of IWC. In Fig. 5b, and 5c, measured $IWC$ and $(1 - Z_{DR}^{-1})IWC$ are shown in solid black lines and their linear fitting curves (red lines) are superimposed. The $R^2$ goodness of fit parameter indicates that a linear regression fits $(1 - Z_{DR}^{-1})IWC$ better in comparison to IWC.
Figure 3: Top panel shows IR GOES-13 image with the overlaid segments of the Convair580 flight track on May 26, 2015. Different time segments of the flight track are shown by different colors. Bottom panel shows X-band side reflectivity from a period of [11:07 - 11:30] UTC corresponding to white, yellow and purple segments in the top panel. A break line at around 7.1 km is the location of contaminating ground clutter via the side antenna’s sidelobe (section 3.1) which was filtered out.
Figure 4: Time series of (a) IWC$_{PSD}$, MMD, (b) $K_{dp}$, $Z_{dr}$, (c) $\rho_{hv}$ and $Z_{H}$ for May 26 Convair-580 flight.
Figure 5: $Z_{dr}$ and $\rho_{hv}$ (a), $IWC_{PSD}$ (b) and $(1 - Z_{DR}^{-1})IWC$ (c) as functions of $K_{dp}$. In panel (b) and (c), mean values and frequency distributions are computed from data points in each $K_{dp}$ bin of 0.1° and 0.05° respectively. Regression parameters $(a_1, b_1)$ for
the $K_{dp}$-only method and $(a_2,b_2)$ for the $(K_{dp},Z_{DR})$ method are estimated from the mean values using a simple linear fitting algorithm.

To gauge the performance of the polarimetric methods, results from the conventional $IWC - Z$ estimator are also included in Fig. 6a. This figure shows the measured IWC along the Convair’s flight path is depicted in black, IWC-Z result is shown in green and IWC estimates using polarimetric methods are shown in blue and red for $K_{dp}$-only and $(K_{dp},Z_{DR})$ algorithms, respectively. One can observe that the two polarimetric methods agree well with measured IWC while the IWC estimates from just using radar reflectivity exhibit biases as large as one order of magnitude. The large errors in the $IWC - Z$ estimator are due to the presence of mixtures of large aggregates and small ice crystal regions as indicated in the PIP images (not shown) in clouds. Large aggregates have a dominant contribution into the radar reflectivity, which explains the positive biases of the $IWC - Z$ estimates. On the other hand, $K_{dp}$ is not biased toward large aggregates. The magnitude of $K_{dp}$ in aggregates with MMD > 2 mm is usually smaller than 0.4 °/km and in small ice particles (MMD in the range 0.3 – 1 mm) $K_{dp}$ is between 0.6 °/km to 1 °/km (Fig. 7a). It follows that estimators utilizing $K_{dp}$ information would overcome the large aggregates effects in radar volumes. It is worth noting that the two algorithms capture well the IWC variation at the end of the segment. If the in-situ measurements are considered as the ground truth, the estimation biases are computed and shown in Fig. 6b. On average, biases are -0.082 $gm^{-3}$ and 0.018 $gm^{-3}$, and the root mean squared differences (hereinafter referred to as the rms differences) are 0.49 $gm^{-3}$ and 0.48 $gm^{-3}$ for the $K_{dp}$ alone and $(K_{dp},Z_{DR})$ methods, respectively. The correlation coefficients between $IWC_{PSD}$ and estimated IWCs are 0.66 and 0.70 for the two methods. In this case study, the inclusion of $Z_{dr}$ improves the accuracy of the IWC estimates.
Figure 6: Top panel shows measured IWC from the Nevzorov (black line), estimated IWC using reflectivity (dash green line), $K_{dp}$ alone (blue line) and $(K_{dp}, Z_{DR})$ combination (red line) for the May 26 case. Bottom panel shows estimation biases for the three estimators. Average biases for IWC($K_{dp}$) and IWC($K_{dp}$, $Z_{DR}$) are -0.002 g m$^{-3}$ and 0.006 g m$^{-3}$ and rms differences are 0.48 g m$^{-3}$ and 0.45 g m$^{-3}$ for the two algorithms, correspondingly.
Figure 7: $K_{dp}$ (a) and $Z_{dr}$ (b) as functions of median mass diameter (MMD). Over 17000 data points from seven selected flights (section 6) during the Cayenne campaign are used.

5.2 Case study II: May 23 flight

For this case, a segment consisting of a region of high IWC of very high concentration of small ice particles and a region of mixture of moderately large aggregates and pristine ice crystals was analysed. This affords an excellent example to gauge the performance of the algorithms. In Fig. 8a, the selected segment is displayed in purple. The radar reflectivity field from the side antenna is shown in Fig. 8b. In this segment, the aircraft’s altitude was between 6.74 km and 6.78 km and $T_s$ ranged from -11° C to -8° C.
Figure 8: Similar to Fig. 3 but for the May 23 case.

In addition to the radar data, $IWC_{PSD}$ and MMD time series particle probe are shown in Fig. 9. The aircraft sampled two small cores where $IWC$ was higher than $1 \text{ gm}^{-3}$ (~18:30 UTC, and ~18:34 UTC). In these high IWC cores, the MMD was in the 400 µm range. In contrast, for the flight segment between 18:36-18:44 UTC, when the temperature was higher, the aircraft sampled a mixture of large aggregates with sizes exceeding 6 mm, and small ice particles (Fig. 10), where the IWC was less than $0.5 \text{ gm}^{-3}$. 
Figure 9: IWC_{PSD} and MMD time series for the May 23 case.

![Figure 9](image)

Figure 10: Sample of 2D imagery from the DMT PIP probe at two time stamps as in Fig. 9. The width of the PIP image strips is 6.4 mm. The aircraft’s altitude was 6.75 km at A and 6.74 km at B.

![Figure 10](image)

The IWC estimates from the methods are plotted in Fig. 12a. In the region dominated by small particles (before 18:33:29 UTC), results from the three estimators agree quite well with IWC_{PSD}. There are small biases in the outcomes of the two polarimetric algorithms at the two HIWC peaks. These biases can be attributed to the errors of fitting linear regression models to the data and/or the difference in the sampling locations of the radar and the in-situ data (section 3.1). In the region after 18:38:01 UTC, the IWC − Z results show very large errors due to the presence of mixtures of aggregates and ice crystals.
(shown in the PIP imagery in Fig. 10 and in high resolution 2DS particle imagery (Fig. 11) in the clouds. The large aggregates dominate the measurements of radar reflectivity, which explains the positive biases of the $IWC - Z$ estimates. The errors for this case are as large as 300% in most estimates. In contrast, both the polarimetric methods provide much better results compared to the conventional IWC-Z method. They capture well the variation of IWC at smaller scales (around 18:33:58 UTC) and larger scales (after 18:36:14 UTC). This again confirms that these algorithms are robust to the variation of ice crystal type, shape and distribution. The rms differences and correlation coefficients for $K_{dp}$-only and $(K_{dp}, Z_{DR})$ methods are (0.84 $gm^{-3}$, 0.41) and (0.79 $gm^{-3}$, 0.55), respectively. The combination of $K_{dp}$ and $Z_{DR}$ provides better results which can be seen at the edges of the second IWC peak (indicated by ellipses) in Fig. 12a. At those regions, MMD (Fig. 9) and $Z_{dr}$ (not shown) values are large. This may be an indication of ice crystals with high axis ratio aligned in the horizontal plane. When this happens, the algorithm based on $K_{dp}$ alone will over-estimate IWC. On the other hand, the product $(1 - Z_{DR}^{-1})IWC$ already includes the particles’ shape and orientation effects, thus, estimates based on it should yield better results. When large particles dominated the volume (after 18:36:14 UTC) $Z_{dr}$ become small (Fig. 7b) then the $(K_{dp}, Z_{DR})$ estimator provides no advantage over the $K_{dp}$-only estimator.

![Images of ice particles sampled by the SPEC 2DS probe on the flight on 23 May 2015. The width of the vertical strip is 1.28 mm.](image)

Figure 11: Images of ice particles sampled by the SPEC 2DS probe on the flight on 23 May 2015. The width of the vertical strip is 1.28 mm.
Figure 12: Similar to Fig. 6 but for the May 23 case.

6 Experimental evaluation

In the previous section, two case studies were analysed in detail. In both cases, results from the polarimetric methods show a much better agreement with in-situ measurements compared to the IWC estimates from the radar reflectivity factor, especially
when larger particles dominate the radar volume. In addition, applying a function of $Z_{DR}$ to IWC before fitting a linear regression model to the data improves the estimation accuracy and correlation. In this section, more data from different flights collected during the mission were analysed and summarized. Out of total 14 campaign flights, there were seven flights with good data quality (radar and in-situ) and with applicable number of high IWC data points and data from those flights were used for this analysis.

$Z_{DR}$ threshold (section 2.2) is determined from all selected data (17699 points in total). In order to find an optimal $Z_{DR}$ threshold from the available data, average bias and rms of IWC estimates are expressed as a function of $Z_{DR}$ threshold (Fig. 13). $Z_{DR}$ threshold was changed within [1.01, 1.2] with 0.1 increment and bias and rms were computed for each value of $Z_{DR}$ threshold. In Fig. 13, average bias and rms of IWC estimates from the $K_{dp}$-only algorithm which are independent of $Z_{DR}$ threshold are also displayed (blue lines). It follows that the average biases for the two methods are very small (within ±0.08 g/m$^3$ ) and the ($K_{dp}, Z_{DR}$) method provides unbiased estimates at $Z_{DR}$ threshold of 1.06. However, rms of the ($K_{dp}, Z_{DR}$) method is quite large at small $Z_{DR}$ threshold and reduces with increasing $Z_{DR}$ threshold. It gets saturated at 0.498 which is slightly below rms of the $K_{dp}$-only algorithm. Considering all the factors, we selected an optimal $Z_{DR}$ threshold of 1.12 where rms of the two methods are equal but the average bias is smaller with the ($K_{dp}, Z_{DR}$) method.

In Fig. 14, IWC and $(1 − Z_{DR}) IWC$ are expressed as functions of $K_{dp}$ for the selected flights. For most cases, the linear relationships are well approximated up to $K_{dp} = 2^\circ/km$. At larger $K_{dp}$, IWC saturates at 2.5 g/m$^{-3}$ and the IWC-$K_{dp}$ relationship departs from the linear trend. Due to the limited amount of data of large measured $K_{dp}$ and IWC, identifying the major reasons for this saturation is not attempted. In these scenarios, applying a more sophisticated method (such as a parametric model) will likely reduce errors at high $K_{dp}$ but this is beyond the scope of this paper. Here, a simple linear regression model (based on the approximation in Eq. (13)) is used and errors are computed from all data points.

It is also worth noting from Fig. 14 that the scattering of the modified IWC-$K_{dp}$ curves is narrower compared to that of the original IWC-$K_{dp}$ curves. The scattering in IWC-$K_{dp}$ relationship can be attributed to the properties of ice crystals and the medium’s state. In other words, when the dependency of IWC-$K_{dp}$ relationship on ice crystal shape and orientation was removed (or partially removed), the scattering of IWC-$K_{dp}$ should be tighter. This is a very important outcome which helps to reduce estimation errors when a single estimator is used for all the cases. Results for IWC estimates are shown in Table 2 for the two polarimetric methods only. In each row, statistical error analysis is shown for each flight with the optimal fitting model derived from data of that flight. The last row displays results computed from all selected data of 17699 points. In all cases, improvement in IWC estimation when $Z_{dr}$ information is utilized in the algorithm is clear. For all data, the bias changes from -0.07 g/m$^{-3}$ to -0.045 g/m$^{-3}$ and correlation coefficient increases from 0.69 to 0.72. The standard deviations of the fitting coefficients ($a_1, b_1$) for the $K_{dp}$-only method and for ($a_2, b_2$) for the ($K_{dp}, Z_{DR}$) method are (0.12, 0.33) and (0.032, 0.033), respectively. The uncertainty of the retrieval depends on the uncertainty in the fitting parameters as well as the values of $K_{dp}$ and $Z_{DR}$ and their measurement accuracy. Typical values of $K_{dp}$ and $Z_{DR}$ for HIWC regions (MMD between 0.3 mm to 1 mm)
are about 1 deg/km and 1.12 (Fig. 7). At those typical values, standard deviation of IWC estimates using \((K_{dp}, Z_{DR})\) algorithm is 0.6 g/m\(^3\).

Figure 15 shows time series of \(IWC_{PSD}\) from the seven flights and estimated IWC from the two algorithms. As mentioned before, for each algorithm, a single set of fitting parameters is used for the combined data. Evidently, the method utilizing \(Z_{dr}\) yields better results in term of estimation bias and correlation (Fig. 13b and Table 2). In Fig. 16, estimation bias and std are expressed as a function of IWC. Note, that inclusion of \(Z_{dr}\) improves estimation bias at all IWC points. On average, an improvement of 35% in average bias was achieved. As observed in Fig. 14, larger biases happen at IWC greater than 2 gm\(^{-3}\). It is attributed to strong departures from the linear model in the joint IWC-\(K_{dp}\) distribution. The inclusion of \(Z_{dr}\) has been proved to be able to mitigate these large errors but not completely fix the problems. To improve the radar-derived IWC estimates further, more additional data processing (such as hydrometeorology classification) and/or more sophisticated regression models are needed.

Figure 13: Average bias and rms as a function of \(Z_{DR}\) threshold for all data from the seven selected flights.
Figure 14: $IWC_{PSD}$ (a) and $(1 − Z_{DR}^{-1})IWC$ (b) as functions of $K_{dp}$ for the seven selected flights.

Table 2: Polarimetric methods performance for selected flights during the Cayenne 2015 campaign.

<table>
<thead>
<tr>
<th>Flight</th>
<th>$K_{dp}$ only</th>
<th>$K_{dp}$ and $Z_{dr}$</th>
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<tbody>
<tr>
<td></td>
<td>$(a_1, b_1)$</td>
<td>$(a_2, b_2)$</td>
</tr>
<tr>
<td></td>
<td>bias ($gm^{-3}$)</td>
<td>bias ($gm^{-3}$)</td>
</tr>
<tr>
<td>May 15am</td>
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</tr>
<tr>
<td>May 16am</td>
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<td>-0.117</td>
</tr>
<tr>
<td>May 16pm</td>
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<td>-0.051</td>
</tr>
<tr>
<td>May 20am</td>
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<td>0.012</td>
</tr>
<tr>
<td>May 23pm</td>
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</tr>
<tr>
<td>May 26am</td>
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</tr>
<tr>
<td>May 26pm</td>
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<td>-0.046</td>
</tr>
<tr>
<td>All*</td>
<td>-0.070</td>
<td>0.53</td>
</tr>
</tbody>
</table>

* for all data points, optimal fitting parameters (0.90, 0.31) was used for $K_{dp}$-only algorithm and (0.13, 0.02) was used for $(K_{dp}, Z_{dr})$ algorithm.
Figure 15: (a) Combined IWC time series data from the selected flights: measured IWC (black line), estimated IWC using $K_{dp}$ alone (blue line) and estimated IWC using $K_{dp}$ and $Z_{DR}$ (red line). (b) Estimation errors for the two estimators. For all study cases, the aircraft flew between [5.6, 7.5] km and most of the data points were within a temperature range of ($-10^\circ C \pm 2.5^\circ C$).
Figure 16: Bias and rms difference as a function of IWC derived from the seven selected flights. Mean values and std are computed from data points in each IWC bin of 0.2 g m\(^{-3}\).

7 Conclusion

Accurate detection and estimation of HIWC in tropical mesoscale convective systems are critical for reducing hazards caused by the ingestion of ice particles into the engines of commercial aircraft. The objective of this paper is to find a method to improve IWC retrieval from a side-looking X-band dual-polarization airborne radar. It is shown that the use of the specific differential phase (\(K_{dp}\)) and differential reflectivity ratio (\(Z_{dr}\)) significantly reduces errors in IWC retrieval over the conventional IWC-Z method. In general, IWC-\(K_{dp}\) relationship can be approximated by a linear model and IWC retrieval using \(K_{dp}\) captures the IWC variation very well, regardless of the information of PSD. One major drawback of the \(K_{dp}\) algorithm is that it provides large estimation biases when the ice particle’s aspect ratio and/or orientation is changing. To mitigate this effect, \(Z_{dr}\) is used to reduce the dependency of IWC on the variation of ice particles’ shapes and orientation. We proposed a method, in which, IWCs are weighted by a function of \(Z_{dr}\) before applying a linear model to the IWC-\(K_{dp}\) joint distribution. This approach uses an assumption of constant particle mass within the radar volume. This is suitable for HIWC regions which are often composed of very high density of small ice particles. \(Z_{dr}\) at regions of mixtures of small pristine ice crystals and larger particles such as aggregates is generally low (\(\sim 0.2\) dB) and will not be used in the weighting function. Results from selected Convair-580 flights from the Cayenne campaign show that the proposed method is able to improve estimation biases by 35 % and correlation by 4 %, on average. In our analysis, a single set of fitting parameters is applied for all the data points. The results can be improved further by including advanced data processing techniques such as ice crystal type classification and/or using a more sophisticated regression model for the modified IWC-\(K_{dp}\) joint distribution.
Most of HIWC data points used in this are measured at a narrow window of the temperature range ($\pm 10 ^\circ C \pm 2.5 ^\circ C$). More data is needed to study the temperature variability of the proposed method.

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References


