

Assimilation of lidar planetary boundary layer height observations

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Response to reviews

Reviewer 1

Major comments:

1. *L216-L225 and the assimilation impact from 00-08 UTC: I am confused why there appears to be exactly zero assimilation impact during the overnight hours. In Fig. 2, the forecast and analysis lines are exactly on top of each other for the first four verification times. However, looking at Figure 1, the innovation (observation minus background) can still be large during the overnight hours, especially for MYNN. For example, Fig. 1 shows MYNN underpredicting the PBLH by 300 m at 0400 UTC. Given that the error covariances at this time are also non-zero, as shown in Figure 7, I would expect at least some impact. Additionally, Fig. 2 shows the MYJ and MYNN RMS values of (T, Q, U, V) being exactly equal. This seems odd given that Fig. 1 shows them predicting very difference values of PBLH. Thus, I wonder if there is some error in the assimilation scheme or analysis techniques that could be leading to this appearance of zero-impact.*

The analysis increments are never zero, but are much smaller from 0-8 UTC. But we also found an inconsistency in the definitions geopotential height and PBLH (the former defined above ground level and the latter above sea level), and have redone the assimilation. You can now see somewhat larger changes in some of the profiles during this time. Also, the smaller increments are also due to the variation in the lidar observation error estimates, which vary substantially during the day.

2. *Figure 2: Given the large data gap between 08-22 UTC and the use of only six soundings for verification, I disagree with the use of a time-series to show the assimilation impacts. This choice leads to the appearance of the impact linearly increasing between 08-22 UTC, when it likely shows a very different shape in reality. Additionally, statements line L207 (water vapor mixing ratio has little impact until 22 UTC) are not correct given that there is likely an impact beginning at 12 UTC when the innovation becomes much larger. It is just that you do not have any radiosondes confirm that. I suggest removing this figure, or at least removing the lines that connect the verification times. I also suggest removing any text referring to temporal changes in the impacts C2*

We have removed the lines between the radiosonde measurement times. It became difficult to see both of the PBL model forecasts without them, so we split Figure 2 into two figures (2 and 3). The text has been changed to reflect this.

3. *Figures 3-6: These figures can be difficult to interpret given the lack of any innovation information. I found myself having to flip back and forth between these plots and Figure 1 to try and understand why the impacts were small at certain times. Please include the forecast PBLH on these figures, or at least annotate the innovation (Lidar PBLH minus forecast PBLH).*

We have included the forecast PBLH in the profile plots.

4. *Overly general writing: Sometimes I felt that the author's made general statements when those statements only were instead meant to refer to a specific PBL scheme. For example, it is stated in the abstract that assimilating PBLH observation improves water vapor relative to independent radiosondes. However, this does not appear to be the case for MYJ (figure 2). Additional examples of this are at L217, L228, L241, and L279. Please check and modify such statements throughout the manuscript.*

The text has been changed to reflect the changes to assimilation (described in item 1 above), and to make the comments more specific. Though the L228 comment was concerning a plot that we didn't include. And L279 is a more speculative statement on how changing the state variables would be carried forward in time, though we have modified this to make it more qualified.

Minor comments:

L16 (and throughout): the use of "sonde" instead of "rawinsonde" or "radiosonde" feels a little informal. Please correct.

This has been changed.

L46: I suggest stating “non-local flux schemes” since that helps separate those types of schemes from the local TKE schemes.

done.

L50: The sentence beginning “These varying and distinct” is confusing. I suggest rewording.

It has been rewritten as: “The variety of definitions PBLH make it difficult to effectively evaluate existing models or develop new ones.”

L58: I am not sure what the point of this reference to GPSRO is. This seems oddly specific and overly verbose. It could probably be removed.

Removed.

L73: Jumping from the discussion of ceilometers to lidars feels a little abrupt. Please improve the flow between these two paragraphs (i.e., stating something like “we use Doppler lidars as a proxy to determine the impact of assimilating PBLH from a network of ceilometers”).

We have added further wording to make this transition less abrupt.

L74: Please provide a little more information on the brand and type of Doppler lidar used. There were multiple instruments employed during PECAN so it wouldn't hurt to be more specific.

This information has been added.

L81-L82 and L94-100: I suggest moving some of this content into the methodology sections. It doesn't really fit in an introduction.

We don't agree with making this move. These details are not about the assimilation algorithm, which is described in the methodology section. I don't think details about the observations belongs in methodology because the retrievals are not a part of the methodology developed in this work. Further, you are asking for more details about the lidar observations in this section already (L74 and L82). So it seems best to leave this the way it is.

L82: I would like to see more details on how PBLH is estimated from the Doppler lidar data instead of just giving the reference. This could provide needed context for understanding how different the estimates of PBLH are between the lidars, radiosondes, and the PBL parameterization schemes.

Additional description of the PBLH retrieval algorithm has been added.

Introduction: One thing I was curious about when reading this manuscript is the motivation for assimilating PBLH instead of directly assimilating the wind profiles collected by the lidars. Lidar wind profiles have been assimilated in the past with positive results shown (Kawabata et al. 2014, Degelia et al. 2020), so why go through the extra steps of deriving PBLH from those data? I suggest adding a sentence or two in the introduction to discuss this.

We have added “But we are interested assimilating the PBLH observations directly because the ceilometer network described above will focus on these retrievals, and satellite missions which measure PBLH are also planned.”.

L116 and EnOI discussion: It seems that the EnOI computes the covariance structure with a spatial component (covariance over a given area). How representative is that of the EnKF method which can estimate covariance at a single point? Does that cause any issues with extrapolating these impacts to a hypothetical EnKF system (i.e., L269)?

We are only using the EnOI to compute covariance in the vertical direction, since we are concerned with the profile correction. With the EnKF one would also compute the horizontal structure as well. In addition, the variance estimate will depend on the distance spacing of the profiles, with a larger distance resulting in a larger variance. We chose a relatively small set of 20x20 grid locations to minimize this effect. In the EnKF, one would also include inflation and horizontal localization. These would need to be worked out when an EnKF is constructed for this data type. We have added a couple of sentences on this.

L127: Is the same method used to compute PBLH for both the stable and convective boundary layer? I know MYNN is supposed to be more accurate at night compared to MYJ.

The PBLH estimate approaches are the same at all times. The values changed in this version as we found an inconsistency in the definition of PBLH, so now the MYNN scheme is more accurate during the night. We think the manuscript is reasonably clear on this.

L132: Please also list the grid-spacing for these simulations.

The grid spacing is 3km, and was already in the first version of the manuscript.

L111: Is there a reference for the NU-WRF forecasts run during PECAN?

The only reference at this point is Santanello, et al. 2019, which is an AGU meeting abstract.

L137-139: Is this true? I would expect that the covariance/correlation would be smaller when computed over a larger region?

Over a large region the meteorological conditions become more varied, so the variance becomes larger.

L148: Please include more information on the observation error variance! This term is equally as important in the analysis as the background error covariance. How is it determined? How do you convert the lidar wind errors into PBLH errors? Do you include any representation factors?

The PBLH observations are determined from the combined velocity variance dropoff, wind speed gradient and backscatter dropoff. The uncertainty is smallest where these values decay rapidly over a short distance. When the dropoff is more gradual (as in the morning), the estimated uncertainty is much larger. This is described in the text.

L151-155: It might be good to reference an EnKF paper for these approximations since it is the same technique applied here (i.e., Houtekamer and Zhang 2016).

Reference added.

L162: Please state the chosen value of α .

$\alpha = 8$ has been added to the paper.

L172-L179: Much of this paragraph detailing the model configuration is repeated from the methods paragraph beginning at L124. Please reduce.

We reduced the details in the results section slightly.

L181: Is there a reference for the parcel method?

We added Holzworth, 1964.

L196: Why 800 hPa? Why not compute the RMS from the surface to the top of the PBL since you know its height? Please provide some justification for this number.

We chose 800mb because this is roughly the maximum height of the PBL on this day. If we chose to compute the RMS up to levels that vary with the PBLH, then it would be difficult to make direct comparisons between the RMS at different times in the day. We have added a sentence on this in the paper.

Figure 1: Should there be an additional sounding observation during the late evening? I only see five green triangles, but you reference six radiosonde launches. Additionally, there are six verification points shown in the time series plots.

The sixth radiosonde PBLH has been added to the figure.

L207: I recommend using absolute differences instead of percent changes.

We have changed this to absolute differences.

L213: I disagree with saying the assimilation reduces by the RMS "significantly". Is statistical significance computed here? Also, this sentence appears to be referring to the impact to U-wind in Fig. 2c, of which the impacts look extremely small to me.

We have changed the discussion here, and removed the term "significantly".

Figs. 2-6: Please add (a,b,c,d) headings to each figure to match the figure caption.

We changed the caption to read upper left, upper right, etc instead of using letters to identify the figure location.

Figure 2: I recommend changing (hour) in the x-axis to (UTC) to be consistent with the text. Also please be consistent between saying "U wind" and "zonal velocity" in the figure captions.

These have all been changed to "U wind".

L221-223, L276: I disagree with the statement of the model profiles "accurately" following the radiosonde profiles in Figs. 3-4. For example, the u-wind shows errors of 4 m/s, and the mixing ratio errors can be as large as 1-2 g/kg which is not exactly "accurate".

This has been changed so that the profiles are described as "more accurate" during the early morning than they are in the late afternoon.

Figs. 3-6: I recommend reducing the vertical extent of these profiles you are primarily focusing on impacts within the PBL. Maybe 800 hPa since that is what you use for the RMS calculations?). Also, I notice that some of the axis labels and formats are different between these figures, so please be consistent.

We have kept the upper limit at about 600 mb because we felt it was important to show how the profile reveals the location of the top of the PBL (either the model or observation estimates), so it was helpful to include a region above the PBL. This also enables us to show how much correction is made above the PBLH. But we have made the fonts on the axis labels consistent.

L235-L38: I am not sure that the discussion of vertical localization fits with the rest of this paragraph. We removed these two sentences. This had already been discussed in the methodology section.

L244: I do not understand this statement that suggests PBLH is more representative of water vapor flux. Please elaborate.

We removed the last two sentences from this discussion.

L279-282. There is a mix-up of tenses here. The first sentence uses present tense (the water vapor mixing ratio is over corrected), while the second sentence uses past tense (the assimilation corrected: : :). Please fix. I also noticed other instances of this so I recommend doing a pass to fix issues throughout the manuscript.

These sentences have been corrected.

Typos and wording changes

1. *L5-6: Please spell out the affiliations.*

Done.

2. *L35-39: this sentence is overly long. Please split up or condense.*

Done.

3. *L42: Add a comma after “Alternatively”.*

Done.

4. *L55: Please use UTC instead of “Z” time to be consistent with the rest of the paper.*

Done.

5. *L62: Change the reference to Hicks et al. 2016 to use parenthesis instead of brackets.*

Done.

6. *L114: The sentence beginning “Instead we use: : :” seems broken. Please fix.*

Done.

7. *L198: ntop is not used in this equation. Please remove.*

Changed to $i = 8$.

8. *L233: Fix the spelling for “independent”.*

Done.

9. *L238: Please define “WV”.*

Done.

10. *L267: Please change “assimilation” to “assimilating”.*

Done.

11. *L288: Sentence beginning “The covariances” is broken. Please fix.*

Done.

Reviewer 2

1. *The definition of PBLH. As described on lines 77-82, for PBLH data calculation, the Doppler shift of the backscattered signal is used to calculate wind speed as a function of range, which can then be used to produce a multitude of wind and turbulence variables useful for PBL characterization (e.g. vertical velocity variance and signal-to-noise ratio variance). The PBLH algorithm applied for this study combines several such aerosol and wind variables for PBLH measurement and was described at length in Bonin et al. (2018). The PBLH in the model is estimated using the total kinetic energy (TKE) method. The two definitions are different but seem close enough. Is there a way to show to what extent the two PBLH definitions are comparable?*

This Doppler lidar was not making measurements capable of direct TKE retrieval, only TKE proxies (such as vertical velocity variance), so an explicit apples-to-apples comparison is not possible here. To make further inference would be speculative, so instead we only present and discuss this best possible PBLH measurement from the Doppler lidar to assess model performance.

Once a much larger number of PBLH lidar observations are obtained, along with radiosonde observations, it would be worthwhile to generate some statistics on this, on both bias and random differences. We have 6 sonde observations to compare with our forecasts, and with these we can show here is how the lidar observations can impact the thermodynamic profiles within the PBL using assimilation of the lidar observations. With a better understanding of differences between the two PBLH schemes, and a much larger data set to compare with, it's likely that further improvements can be made.

2. *The vertical localization factor. How is the parameter alpha in equation (6) chosen? According to the equation, this parameter works the same way for layers both above and below the PBL height, for example, if $k_{PBLH} = 4$, then C_{loc} at layer 3 is the same as C_{loc} at layer 5. However, that seems not the case in Fig. 5.*

We have redone the assimilation to fix a couple of inconsistencies in the code, including this. The profile plots now show the vertical localization above and below the top of the PBL, though the final form of any localization that would be needed will be more clear once this is implemented with an enKF.

3. *Equation (7). Where is number “8” coming from? The top of boundary layer is not a constant during the 22 hours, which can be seen clearly in Figures 3-6.*

The maximum extent of the PBL in the late afternoon is at layer 8, and we felt it was more consistent to compare the same levels at each time, rather than comparing a much smaller number of layers during the night and early morning. This is explained further in the text.

4. *In the abstract, it states that water vapor is improved by assimilating lidar PBLH. However, Fig. 5 shows that it is degraded.*

We have corrected this statement. A more accurate statement is that the assimilation changes the water vapor profile in the right direction, but the increment is too large, so that the RMS difference with the radiosondes increases. This would require additional tuning in an EnKF.

Reviewer 3

1. *Line 212 – “: :the assimilation reduces the RMS differences with sonde profiles significantly by 22 UTC for both models.” From Fig. 2, the RMS difference of potential temperature, WVMR and V component of velocity have reasonable impact but there is little or no impact on U wind. Please correct the statement if it was a mistake, or, if not, please elaborate how the impact is significant. Also please adjust the Y axis limits of V wind to the same as that of U wind.*

We have made some changes here due to changes in the solution in this revision. Please see the response to the last item from reviewer 2. We have made the y-axis limits the same for the U and V plots.

2. *In Figs. 3 and 4 both analysis and forecasts profiles of potential temperature, WVMR and velocities, U and V, coincide each other at 4 UTC. However, in Fig. 1, the PBLH at 4 UTC is not the same for MYNN forecast although MYJ forecast PBLH has the same value as the radiosonde. The PBLH difference of MYNN forecast to radiosonde is around 300 m from Fig. 1 which creates a doubt regarding Fig. 4 (MYNN scheme) at least if not Fig. 3. May be the innovation was not large enough to create an impact in the assimilation system. Also another reason for doubt is due to the significant magnitude of covariance of PBLH with the variables for 4 and 8 UTC. Hence, I would suggest the author to create the same Figs. 3 and 4 with an additional background profile (may be use a dashed line of the same colour) for each of the variables to remove the doubt.*

We have made some corrections to the code, which has changed both the innovations and the corrections to the profiles. We have also put the lidar observation levels (in pressure) on the profile plots to make more clear the magnitude of the innovations. There are now some what larger corrections to the profiles in the early morning, and none of them is zero.

Minor Comments:

1. *I would suggest the author to include a brief description of Doppler lidar just after the ceilometers. A brief description on the pros and cons of Doppler lidar (with references to the system used) and how it is superior to ceilometers could be added.*

We have added further details on the Doppler lidar.

2. *Line 134 - Please add some more details regarding the assimilation design in the methodology section. The sentence “: :experiments are all less than 24 hours from the most recent global analysis” is not clear enough for readers. Line 98 - “The assimilation is done on 22 hourly WRF forecast fields: :” may be omitted or modified after the above addition in the methodology section.*

We have added further explanation as to where the forecasts start (0 UTC) from the NOAA global forecast system (GFS) with a final initialization at 0 UTC.

3. *Line 178 – Radiosonde launches were 6 times in total. The reader understands MYJ has 5 radiosonde comparisons since it stopped at 22 UTC whereas MYNN has 6 radiosondes. Please clarify this point.*

The missing radiosonde has been added to the PBLH plot.

Typos and corrections:

1. Line 59 – “Wulfmeyer et al. 2015” not found in the reference section.

Added.

2. Line 67 - Please check “Brooks, 2003”. I could not find the reference in the reference section.

Added.

3. Line 144 – The sentence “Instead we use: : error statistics” should be corrected.

We have changed this sentence, but we think you had meant line 115.

4. Line 119 – “We use profiles from: :” feels like repetition from line 115.

We think you meant line 144 here. And we have shortened and simplified the sentence to avoid repetition.

5. Line 129 – Please describe “W”.

W is the vertical velocity, but we are not showing it here because there are not observations to validate it. So we have removed it.

6. Line 220 – Please change “plue” to “blue”.

Done.

7. Line 244 – “Demoz et al 2006; Crook, 1996” could not be found in the reference section.

These citations have been added to the reference list.

8. Line 272 – “an” is used twice, please correct.

Done.

9. The following references were found in the reference section without citation in the manuscript. Please cite these wherever necessary.

“Banks, R. F., J. Tiana-Alsina, F. Rocadenbosch, and J. M. Baldasano (2015) Performance evaluation of the boundary-layer height from lidar and the Weather Research and Forecasting Model at an urban coastal site in the north-east Iberian Peninsula. *Bound.-Layer Meteor.*, 157, 265–292, <https://doi.org/10.1007/s10546-015-0056-2>.”

“Cohen, A.E., S.M. Cavallo, M.C. Coniglio and H.E. Brook (2015), A Review of Planetary Boundary Layer Parameterization Schemes and Their Sensitivity in Simulating Southeastern U.S. Cold Season Severe Weather Environments, *Wea. Forecast.*, 30, 591-612.”

“Tucker, S.C., S.J. Senff, A.M. Weickmann, W.A. Brewer, R.M. Banta, S.P. Sandberg, D.C. Law and R.M. Hardesty (2009), Doppler Lidar Estimation of Mixing Height Using Turbulence, Shear, and Aerosol Profiles, *J. Atmos. Ocean Tech.*, 26, 673-688.”

These References have been removed.

1 **Assimilation of lidar planetary boundary layer height**
2 **observations.**

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Abstract

Lidar backscatter and wind retrievals of the planetary boundary layer height (PBLH) are assimilated into 22 hourly forecasts from the NASA Unified - Weather and Research Forecast (NU-WRF) model during the Plains Elevated Convection at Night (PECAN) campaign on July 11, 2015 in Greensburg, Kansas, using error statistics collected from the model profiles to compute the necessary covariance matrices. Two separate forecast runs using different PBL physics schemes were employed, and comparisons with ~~5 independent sonde~~ 6 independent radiosonde profiles were made for each run. Both of the forecast runs accurately predicted the PBLH and the state variable profiles within the planetary boundary layer during the early morning, and the assimilation had ~~little~~ a small impact during this time. In the late afternoon, the forecast runs showed decreased accuracy as the convective boundary layer developed. However, assimilation of the doppler lidar PBLH observations were found to improve the temperature ~~, water vapor and~~ and V velocity profiles relative to independent ~~sonde profiles~~ radiosonde profiles. Water vapor was over corrected, leading to an increased differences with independent data. Errors in the U velocity were made slightly larger. The computed forecast error covariances between the PBLH and state variables were found to rise in the late afternoon, leading to the larger improvements in the afternoon. This work represents the first effort to assimilate PBLH into forecast states using ensemble methods.

1 Introduction

The planetary boundary layer (PBL) plays an important role in both weather and climate. This layer is where the Earth's surface interacts with the atmosphere, exchanging heat, moisture and pollutants. The PBL height (PBLH) is central to these interactions and is controlled by the energy flux from the surface. Under certain conditions during daytime it defines the convective boundary layer (CBL) and during nighttime it is the stable (non-convective) boundary layer (SBL). Trace gases and aerosols emitted from the surface are rapidly transported within this layer by turbulent atmospheric motion, and transfer of energy and mass into the free troposphere occurs across an interfacial layer at the top of the PBL. The PBLH is fundamental to weather, climate, atmospheric turbulence and pollution through its role in land-atmosphere interactions and mediation of Earth's water and energy cycles (Santanello et al. 2018) ~~and its impact on~~. It affects convection in the troposphere, which is generally initiated within the boundary layer and

then penetrates the top (Hong and Pan, 1998; Browning, et al. 2007). Thus, accurate knowledge of the PBLH is essential for both weather, pollution and climate forecasting.

The PBLH is defined by thermodynamic properties such as a temperature inversion or hydrolapse which can be measured by radiosonde. Alternatively, the drop off in aerosol concentration that occurs across the top of the PBL is used, since aerosols are well mixed throughout the PBL (Hicks, et al., 2019). Atmospheric models rely on parameterization schemes to define the structure of the PBL and compute PBLH. These are generally either local mixing schemes that use local turbulent kinetic energy (TKE, Janjic, 1994) or non-local flux schemes (Hong and Pan, 1996). Generally, these PBL parameterizations have systematically higher PBLH relative to observed values (Hegarty et al., 2018), and also have difficulties modeling the growth of the convective layer during the morning. ~~These varying and distinct~~ The variety of definitions of PBLH ~~across models and observations remain a challenge in terms of utilizing both for process understanding or model evaluation/development~~ make it difficult to effectively evaluate existing models or develop new ones.

Observations of PBLH are traditionally made by radiosonde measurements, which have high vertical resolution but are expensive to launch frequently and are thus limited to special experiments and/or ill-timed launches (*e.g.* 00/~~12Z~~-12 UTC National Weather Service launches) with respect to ~~the~~ convective and stable PBL development. Likewise, spaceborne measurements of the lower troposphere from passive and active instruments ~~(with the exception of Global Positioning System Radio Occultation (GPSRO), Ao, et al. 2008)~~ are severely limited in vertical, spatial, and/or temporal resolution (Wulfmeyer et al. 2015). Ground based measurement of PBLH has been proposed for an extensive network of ceilometers by adding to the functionality of instruments that were designed for measuring cloud heights (Hicks et al., 2016). The ceilometer measures the time required for a laser pulse to return to a receiver, from which the height of the scattering is determined. The intensity of the backscatter is correlated with the density of aerosols at a given height and the PBLH is inferred from the location of the maximum negative gradient of the backscatter intensity. Several algorithms employ wavelet transforms to identify the location of the negative gradient (*e.g.* Brooks, 2003; Knepp, *et al.*, 2017); ~~which relies on finding the wavelet dilation that is large enough to be distinct from noise and small-scale gradients in the backscatter profile.~~ This existing network of ceilometers could be used to create a relatively dense network of frequent PBLH observations,

75 as was recommended by the 2009 study from the National Research Council (NRC, 2009)
 76 and the Thermodynamic Profiling Technologies Workshop (NCAR, 2012).

77 ~~The lidar observations used in this study were taken~~ Since the ceilometer PBLH
 78 observations were not yet available for the campaign we are using, we employ doppler
 79 lidar observations made at the PECAN site in Greensburg, Kansas, to demonstrate the
 80 methodology. The data is from a ~~commercial~~ Leosphere WINDCUBE-200S Doppler li-
 81 dar owned and operated by the University of Maryland, Baltimore County (Delgado et
 82 al., 2016). This lidar operates at an infrared wavelength, and hence receives its strongest
 83 backscattered signal within the aerosol-laden PBL and is often below the measurement
 84 noise floor above the PBL. The Doppler shift of the backscattered signal is used to cal-
 85 culate wind speed as a function of range, which can then be used to produce a multi-
 86 tude of wind and turbulence variables useful for PBL characterization (e.g. vertical ve-
 87 locity variance and signal-to-noise ratio variance). While Doppler lidars and ceilometers
 88 are similar in aerosol detection, a Doppler lidar’s additional wind measurement capability
 89 makes it more broadly applicable and at times more accurate than a ceilometer for PBLH
 90 measurement. The PBLH algorithm applied for this study combines several such aerosol
 91 and wind variables for PBLH measurement ~~and was~~. Each PBLH retrieval involves measurement
 92 of turbulence intensity, horizontal wind profiles and backscatter intensity. The heights
 93 of steep gradients in these quantities are determined using empirical thresholds and wavelet
 94 transform techniques, and the three estimates are combined using fuzzy logic. This is
 95 described at length in Bonin et al. (2018). Additional lidar parameters and the appli-
 96 cation of the algorithm to PECAN data were presented in Carroll et al. (2019). ~~Each~~
 97 ~~PBLH measurement was~~ The PBLH measurements were made from a repeating 25-minute
 98 lidar scan cycle. This Doppler lidar and PBLH algorithm combination are generally well-suited
 99 for accurate and precise measurement of the PBLH during the daytime boundary layer,
 100 nocturnal boundary layer, and morning transition period (Bonin et al. 2018, Carroll et
 101 al. 2019). The evening transition is the most challenging for this setup due to due to difficulties
 102 in defining a clear mixing layer during the decay of a turbulent daytime PBL (Lothon
 103 et al. 2014).

104 The question remaining is how to assimilate these observations into a numerical
 105 weather prediction (NWP) model. ~~PBLH~~ A number of studies have explored assimilating
 106 thermodynamic profile measurements from lidar (Hu et al. 2019, Coniglio et al. 2019,
 107 Degelia et al. 2019) and have shown that this increases the accuracy of model PBLH estimates.

108 But we are interested assimilating the PBLH observations directly because the ceilometer
109 network described above will focus on these retrievals, and satellite missions which measure
110 PBLH are also planned. PBLH is a diagnostic variable in NWP parameterized physics
111 models. This means any correction to PBLH will be lost during the model forecast un-
112 less the PBLH height observation is used to correct state variables such as temperature
113 and moisture. This could be done either by creating an adjoint of the PBL parameter-
114 ization scheme, or through the use of an ensemble Kalman filter which would determine
115 the error covariances between PBLH and state variables in the model. The structure of
116 the covariance, and how the state variables are changed by assimilating PBLH, will de-
117 pend on which PBL scheme is used. We will show how such a system could work by con-
118 ducting a posteriori lidar PBLH observation impact experiments using forecast fields from
119 a NASA Unified - Weather and Research Forecast (NU-WRF, Lidard-Peters, 2015) model
120 runs for one day during the Plains Elevated Convection at Night (PECAN) campaign
121 on July 11, 2015. The assimilation is done on 22 hourly WRF forecast fields through-
122 out the day without cycling the analysis fields back into the model ~~with~~, using two dif-
123 ferent PBL parameterizations. In this paper, we demonstrate a new and promising method
124 that uses the ~~relative~~ lidar-based aerosol backscatter and wind derived PBLH to correct
125 model forecasted state variables. The purpose here is to show how ensemble computed
126 error covariance can transfer observational information from PBLH to the state variable
127 profiles.

128 **2 Methodology**

129 The assimilation methodology is based on the ensemble Kalman filter (EnKF)(Evensen,
130 2009), where the analysis state is the estimate with the minimum estimated errors, rel-
131 ative to the given error statistics. It differs from the EnKF in that the analysis is not
132 used as an initial state for the next model forecast. Rather, two existing one day NU-
133 WRF forecasts, with different PBL physics schemes, are used when lidar measurements
134 are available at a single location. These forecasts were produced as a part of the PECAN
135 campaign in 2015, and we reuse them here to demonstrate the assimilation algorithm
136 that we have developed. These were not ensemble forecasts so we cannot build a stan-
137 dard ensemble Kalman filter from them. Instead we use Ensemble Optimal Interpolat-
138 ion (EnOI), ~~we use in which~~ profiles from neighboring model gridpoints ~~to obtain and~~
139 are used to obtain an estimate of error statistics (Oke, *et al.*, 2010; Keppenne, *et al.*, 2014).

140 This approach will allow for the construction of the vertical component of covariance,
 141 which is needed in order to understand how PBLH can be used to correct atmospheric
 142 profiles through the use of profile and PBLH statistics. We use profiles from nearby model
 143 grid points and have tested the system with varying numbers of grid points in the en-
 144 semble. An ensemble Kalman filter would likely give different covariance information,
 145 but the basic relationship between the state variable profiles and the PBLH are deter-
 146 mined by the model in the same manner here.

147 The two NU-WRF simulations use the Mellor–Yamada–Janjic (MYJ)[Mellor and
 148 Yamada, 1974, 1982; Janjic, 2002] and Mellor–Yamada–Nakanishi–Niino level 2.5 (MYNN)
 149 [Nakanishi and Niino, 2009] which are local 1.5 and 2.5 order turbulence closure schemes
 150 respectively. The PBLH in each of these models is estimated using the total kinetic en-
 151 ergy (TKE) method. The NU-WRF forecast state variables are temperature (T), mois-
 152 ture (Q) and velocity (U,V), and we define the forecast vector $\mathbf{x}^f = [T^f \ Q^f \ U^f \ V^f \ (PBLH)^f \ W^f]$ $\mathbf{x}^f = [T^f \ Q^f \ U^f \ V^f \ W^f]$
 153 where we have combined PBLH with the state variables to enable the covariance calcu-
 154 lation between them. The forecast runs are initiated from ~~a global~~ the NOAA global forecast
 155 system (GFS) reanalysis interpolated to the local domain of 30-48N and 84-110 W, with
 156 220×220 lat/lon and 54 vertical levels. ~~Therefore the state at the initial time, at 0 UTC.~~
 157 At this time, the initial state has assimilated all of the conventional and satellite observa-
 158 tions globally. ~~This means that our experiments are all less than 24 hours from the most~~
 159 ~~recent global analysis~~ The two WRF forecast experiments start at 0 UTC, and are run
 160 for 22 and 23 hours for the MYJ and MYNN experiments, respectively. We use an en-
 161 semble of the 20×20 nearest gridpoints, so that all of the ensemble members are within
 162 about 30 km of the lidar observations (since the grid spacing is about 3 km). Generally,
 163 larger ensembles using gridpoints farther away will result in larger forecast error covari-
 164 ance because the geographic variability. So this ensemble size was chosen as a balance
 165 between ensemble size and geographic localization. The forecast standard deviation for
 166 PBLH on the chosen ensemble was around 27 m at 22 UTC.

167 The forecast error covariance, \mathbf{P}^f is defined as

$$\mathbf{P}^f = \langle (\mathbf{x}^f - \mathbf{x}^t)(\mathbf{x}^f - \mathbf{x}^t)^T \rangle \quad (1)$$

168 where the summation is over the grid points $i = 1, N_{lon}$, $j = 1, N_{lat}$ and \mathbf{x}^t is the (un-
 169 known) true state, on the discrete model grid. We only assimilate the observation $y^o =$
 170 $PBLH = H(\mathbf{x}^f)$ where H is the non-linear observation operator. The analysis equa-

171 tion is

$$\mathbf{x}^a = \mathbf{x}^f + \mathbf{K}(y^o - H(\mathbf{x}^f)) \quad (2)$$

172 where the gain matrix, \mathbf{K} is defined by:

$$\mathbf{K} = \mathbf{P}^f \mathbf{H}^T (\mathbf{H} \mathbf{P}^f \mathbf{H}^T + (\sigma^o)^2)^{-1}, \quad (3)$$

173 σ^o is the observation error standard deviation supplied with the lidar retrievals, and [is](#)
 174 [determined from the combined uncertainty of the vertical velocity variance, velocity gradient](#)
 175 [and backscatter gradient. Generally, when these quantities change rapidly at the top of](#)
 176 [the PBL, then the estimated error is small. The error estimates are larger when \(during](#)
 177 [the evening\), the gradients are much more gradual.](#) \mathbf{H} is the linearized observation op-
 178 erator for PBLH. Because the PBLH is related to the state variables via the two PBL
 179 physics schemes, determining \mathbf{H} would require linearizing the PBL physics at every anal-
 180 ysis time. ~~Instead of this approach, Rather, here~~ we use the ~~ensemble of profiles from~~
 181 ~~the forecast field locations \mathbf{x}^f and the boundary layer heights $PBLH^f$ to obtain the ensemble~~
 182 ~~estimates~~ [EnOI described above to get:](#)

$$\mathbf{P}^f \mathbf{H}^T \approx \langle (\mathbf{x}^f - \mu_{\mathbf{x}}^f) (H(\mathbf{x}^f - \mu_{\mathbf{x}}^f))^T \rangle \quad (4)$$

183 and

$$\mathbf{H} \mathbf{P}^f \mathbf{H}^T \approx \langle H(\mathbf{x}^f - \mu_{\mathbf{x}}^f) (H(\mathbf{x}^f - \mu_{\mathbf{x}}^f))^T \rangle \quad (5)$$

184 where $\mu_{\mathbf{x}}^f$ is the mean forecast state of the ensemble of profiles. [See Houtekamer and](#)
 185 [Zhang \(2016\) for a review of ensemble Kalman filter techniques.](#)

186 We expect the correlation between the air mass within the PBL and the free tro-
 187 posphere to drop away rapidly, because of limited interactions between them. We found
 188 that this can cause errors in the analysis profiles if error covariance and PBLH is allowed
 189 to continue into the troposphere. To reduce these errors we have added an exponential
 190 decay starting at the model level closest to the PBLH (k_{PBLH}) to define a vertical lo-
 191 calization factor:

$$C_{loc} = exp \left[-\alpha \left(\frac{k - k_{PBLH}}{k_{PBLH}} \right)^2 \right] \quad (6)$$

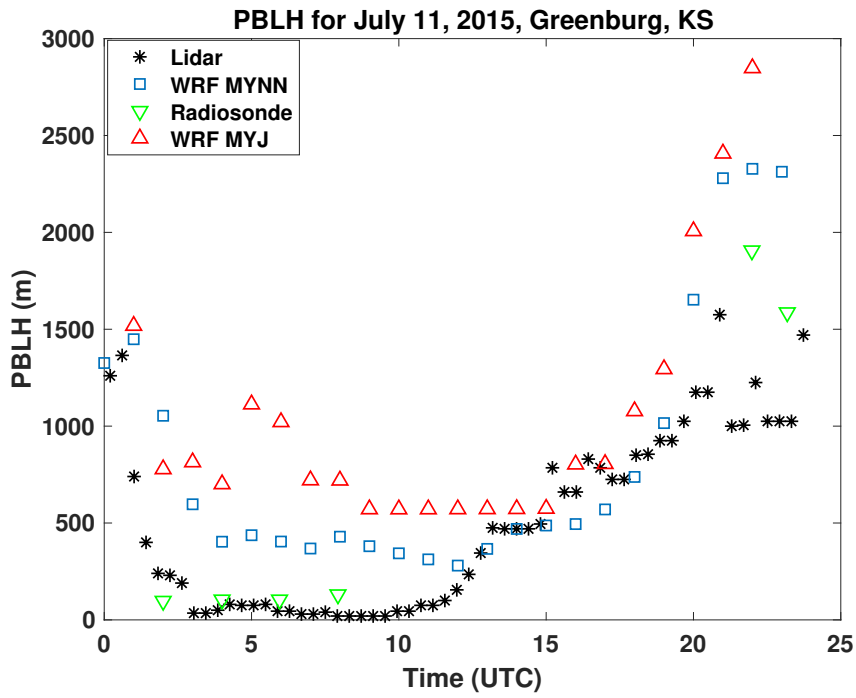
192 where k is the model level and ~~α~~ [8](#) is an experimentally determined factor. This en-
 193 sures that the covariance between the PBLH and the state variables becomes small within
 194 a couple of model levels into the free troposphere.

This system is solved at each hour using the nearest lidar profile ~~observations~~observation in time, and the resulting analysis fields are compared to ~~sonde radiosonde~~profiles when the latter are also available. There are 22 ~~or 23~~analyses (for each forecast run), and ~~5~~6 times where comparison with ~~sonde radiosonde~~profiles are made. We focus on the impact of the assimilation on the state variables T, Q, U and V rather than the PBLH because only the state variables would be retained by a forecast.

3 Results

The NU-WRF simulations, taken from existing forecast runs used for the PECAN campaign (Santanello *et al.*, 2019) are initialized using a National Center for Environmental Prediction (NCEP) Global Forecast System (GFS) reanalysis~~interpolated to the domain 30-48N and 84-110 W, with 54 vertical levels~~. The two forecast runs were conducted using MYJ PBL physics (2-22 UTC) and MYNN (2-23 UTC) on July 11, 2015. Lidar PBLH observations were made every 25 minutes on that day in Greensburg, KS (37.6 N, 99.3 W), while balloon soundings were launched from that location 6 times as part of the Plains Elevated Convection At Night (PECAN; Gerts *et al.* 2017). Figure ?? shows the PBLH during that day~~and~~, derived from the two NU-WRF forecasts, lidar observations and soundings. We have determined the sounding PBLH using the parcel method ~~,~~(Holzworth, 1964), which defines the top as the height where the potential temperature first exceeds the ground temperature. The lidar PBLH (black *, derived using the method reported in Bonin, 2018) closely matches the ~~sonde radiosonde~~estimates (green triangles) in the late evening to early morning (2-7 UTC), while it is somewhat lower in the afternoon. The two NU-WRF forecasts differ from the observations depending on the time of day. In the early morning and early afternoon the MYJ forecasts (red triangles) ~~are slightly both are~~higher than the observations, then ~~fall behind the rise seen in rise less than~~the lidar observations (in the late morning and early afternoon (12-17 UTC, there are no sonde radiosonde measurements to compare to here) before rising much higher than the observations in the late afternoon .The MYNN forecasts (blue squares)are lower than the observations from early morning until early afternoon before rising higher (but not as high as MYJ)(18-24 UTC).

Since we are primarily interested in the impact of the assimilation on state variables within the boundary layer, in ~~Figure ??~~Figures ?? and ?? we plot the RMS dif-



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Figure 1. PBLH vs UTC time for July 11, 2015 for lidar backscatter (black *), WRF model - MYJ (red triangles), ~~sonde observations using parcel method (green triangles) and~~ WRF model - MYNN (blue squares), ~~and radiosonde observations using parcel method (green triangles).~~

226 difference between the model and the independent (unassimilated) ~~sonde radiosonde~~ pro-
 227 files from the surface to roughly the top of the boundary layer (~~in the late afternoon. This~~
 228 ~~corresponds to the~~ first 8 ~~levels~~ layers, or about 800 mb). ~~So for the~~. We use a fixed number
 229 of layers so as to make the comparisons of the RMS differences consistent during the day,
 230 rather than computing the RMS over a different number of layers as the PBL grows during
 231 the day. For the temperature forecast, the RMS difference would ~~be is~~

$$RMS(t_a) = \left[\frac{1}{8} \sum_{i=1}^8 (T_i^f - T_i^{sonde})^2 \right]^{1/2} \quad (7)$$

232 where t_a is the analysis time and ~~ntop~~ $i = 8$ is the model level at the top of the PBL ~~.~~
 233 ~~Figure ?? shows in the late afternoon. Figures ?? and ?? show~~ the RMS differences with
 234 the ~~sonde radiosonde~~ profiles throughout the day for the forecasts (blue ~~x~~) and analy-
 235 ses (red ~~squares~~) for potential temperature (~~a~~upper left), water vapor mixing ratio (~~b~~WV
 236 (upper right) and the U (~~e~~lower left) and V (~~d~~lower right) components of velocity. ~~The~~
 237 ~~MYNN profiles are shown by solid lines while the MYJ profiles are dashed lines.~~

238 During the night (2-9 UTC), the assimilation has ~~very little a~~ relatively smaller im-
 239 pact on the potential temperature RMS differences (upper left) in the early morning (6
 240 and 8 UTC), and the two forecasts have similar accuracy. By late afternoon (22 and 23
 241 UTC, note that the MYJ forecast stops at 22 UTC) the ~~sonde radiosonde~~ comparisons
 242 show that the assimilation reduces RMS differences in the potential temperatures by ~~nearly~~
 243 ~~50% for MYNN and around 80% for MYJ around 1.5K for MYJ and 2K for MYNN.~~
 244 The water vapor mixing ratio (~~b~~upper right) also has little impact from the assimilation
 245 ~~until 22 UTC, and then the~~ between 2 and 8 UTC, but at 22 UTC (the next radiosonde
 246 profile) the RMS difference for ~~the MYJ analysis more than doubles whereas it decreases~~
 247 ~~by roughly half for MYNN. The forecasts for the 2 schemes show about the same differences~~
 248 ~~with the sonde moisture profiles throughout the day~~ both MYJ and MYNN analysis increase
 249 by at least $1.5 \times 10^{-3} \text{ kg/kg}$ in the late afternoon. The U-velocity profiles (~~e~~) begin to
 250 show lower right) show small differences between the MYJ and MYNN by through 8 UTC
 251 (3 a.m. local time) and the assimilation ~~reduces~~ increases the RMS differences with ~~sonde~~
 252 profiles significantly by radiosonde profiles by nearly $1\text{m}/2$ starting at 22 UTC for both
 253 models. The V-velocity profiles (d) begin to differ between MYJ and MYNN for the fore-
 254 casts at 8 UTC ($0.5\text{m}/2$ decrease), and assimilation ~~reduces~~ also decreases the RMS dif-
 255 ferences with ~~sondes radiosondes~~ in late afternoon by ~~10-20%~~ $1.5 - 2\text{m}/s$.

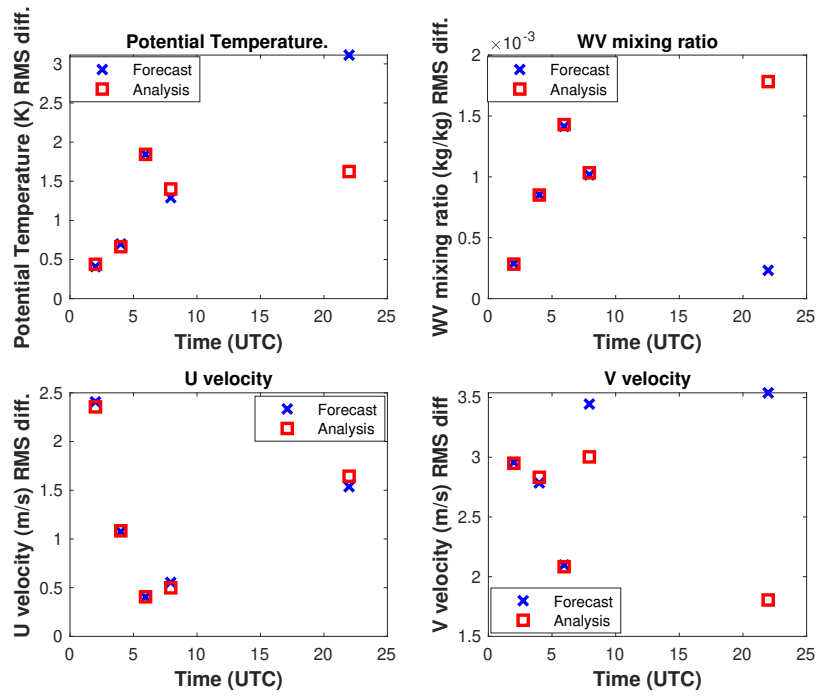


Figure 2. RMS difference ~~from surface to top of PBL for lowest 8 layers~~, vs. time of forecast (blue x) and analysis (red square) with ~~sonde radiosonde~~ profiles for ~~(a)~~ potential temperature ~~(upper left)~~, water vapor ~~(upper right)~~ zonal, U velocity and ~~(lower left)~~ meridional and V velocity ~~(lower right)~~. The solid lines are for the MYNN PBL model and the dashed lines are for the MYJ PBL model. Times shown are UTC.

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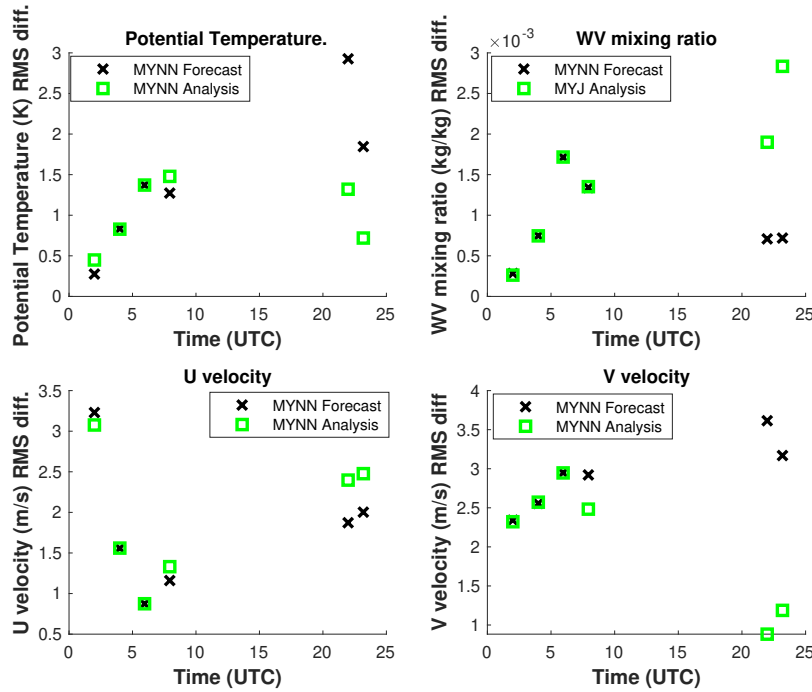


Figure 3. Same as Figure ??, but for MYNN PBL model, with forecast (black x) and analysis (blue square).

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We would like to understand why there is ~~no data a smaller~~ impact during night time and early morning, whereas there ~~is overall improvement in~~ ~~are decreases in the~~ ~~RMS differences in temperature and V velocity and increases in moisture and U velocity in~~ the late afternoon. To this end, we plot the forecast, analysis and ~~sonde radiosonde~~ profiles (T, Q, U and V) at 4 UTC (11 p.m. local time) and 22 UTC (5 p.m. local time) in Figures ??-??. At 4 UTC, (Figures ??,??) these clearly indicate that there ~~is no correction~~ ~~are small corrections~~ made by the assimilation, as the red and ~~blue profiles coincide~~ ~~blue profiles closely overlap~~. But it also shows that the profiles (particularly temperature and moisture) ~~more~~ accurately follow the ~~sonde profiles~~ ~~radiosonde profiles (except for the U velocity above the PBL)~~, meaning that there is ~~little less~~ room for improvement to the forecast state. ~~This is consistent with the PBLH forecasts in~~ ~~In contrast,~~ Figure (??) ~~;~~ ~~which shows that little difference between the forecast shows that the forecast PBLH (particular MYJ) and lidar observation is very small~~ ~~is quite a bit higher than the lidar observation~~

271 at 4 UTC. In the late afternoon (Figures ??, ??) ~~show indicate~~ that there are large dif-
 272 ferences ~~forecast~~ between the forecast and ~~sonde radiosonde~~ profiles for all of the state
 273 variables, and the forecast PBLH values differ substantially from the lidar measurements
 274 as well. The correction to to the ~~profiles is generally in the correct direction, indicating~~
 275 ~~that the forecast error covariance from the ensemble can relate the PBLH to the state~~
 276 ~~variables. forecast profiles generally pushes the analyses towards the independent radiosonde~~
 277 ~~profiles, particularly for temperature and V velocity.~~

278 So the forecasts that ~~accurately that~~ predicted both PBLH and state ~~variable profiles~~
 279 ~~variables with relatively greater accuracy~~ in the early morning were not corrected, while
 280 the less accurate afternoon forecast was drawn towards the independent ~~sonde radiosonde~~
 281 measurements. The assimilation also made changes to the vertical velocity (W) in the
 282 afternoon, but there is no ~~independent independent~~ data to compare with so we have not
 283 included it.

284 ~~Initial experiments without vertical covariance localization (not shown) found that~~
 285 ~~the analysis profiles were changed substantially well into the troposphere, which increased~~
 286 ~~the RMS differences with the sonde profiles there. With the addition of the vertical correlation~~
 287 ~~the analysis profiles relax back to the forecast in the troposphere.~~ The WV profile is shown
 288 to be increased by the assimilation (since WV and PBLH are negatively correlated and
 289 higher PBLH corresponds to lower WV levels in the PBL models), but the analysis over-
 290 shoots the ~~sonde radiosonde~~ WV profile, hence causing the increase in the water vapor
 291 RMS difference in ~~Figure ??(b) Figures ?? and ??~~. Compared to temperature, WV is highly
 292 variable in time and space and it has been shown in the past that slanted balloon tra-
 293 jectories under estimate the WV present (Demoz et al 2006; Crook, 1996). The ~~PBLH~~
 294 ~~may be a macroscale observation that is forcing a correction to the WV flux and hence~~
 295 ~~pointing out an issue in measurements. Future studies should look at the profile measurements~~
 296 ~~of WV from lidars. The two components of velocity (c, d) are both drawn towards the~~
 297 ~~sonde profiles, but by more modest amounts~~ U velocity difference with the radiosonde is
 298 larger for the analysis, but this correction is more difficult because the differences (at least
 299 for MYJ) are both positive and negative and the PBLH observation only contains a single
 300 piece of information. The V velocity is, on the other hand, greatly improved by the assimilation.
 301 These analysis profiles in show that, for this one analysis time, the assimilation is push-
 302 ing the state variables in the proper direction for temperature, V velocity and moisture,
 303 though the moisture correction overshoots the readiosonde profile. The reason for these

304 corrections to the state variable profiles is that the error covariance between PBLH and
 305 each state variable, $\mathbf{P}^f \mathbf{H}^T$, can be computed from the ensemble of profiles that was col-
 306 lected from the model grid. The forecast PBLH for each profile was computed using the
 307 full PBL physics, and therefore contains the essential correlation information between
 308 these variables.

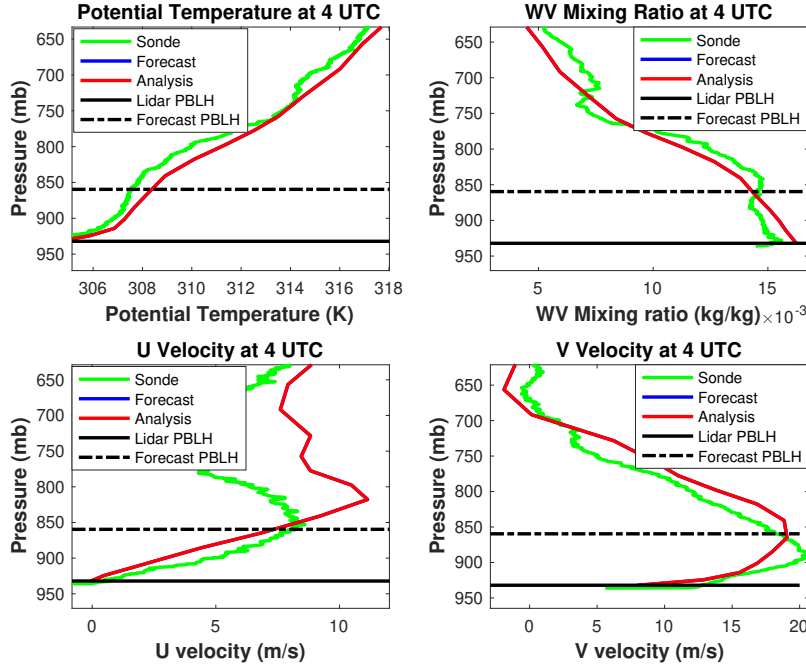


Figure 4. Profiles from sonde-radiosonde (green), forecast (blue) and analysis (red) for poten-
 tial temperature (upper left), water vapor mixing ratio (upper right), u-velocity (lower left) and
 v-velocity (lower right) at 4 UTC, July 11, 2015 in Greensburg, KS. The model uses the MYJ
 physics parameterization.

309 The increasing differences between ~~the~~-PBLH and profile forecasts from early morn-
 310 ing to late afternoon only partly explain the much larger impact of the assimilation at
 311 22 UTC. We can also analyze this by plotting the error covariance between PBLH and
 312 each of the state variables, seen in Figure ?? at different times during the day. The co-
 313 variance with temperature (~~a~~) is always positive, and grows by a factor of 4 by late af-
 314 ternoon near the surface. The covariance with WV is mostly negative and grows by roughly
 315 a factor of 5, while the covariance with the two components of velocity oscillate between

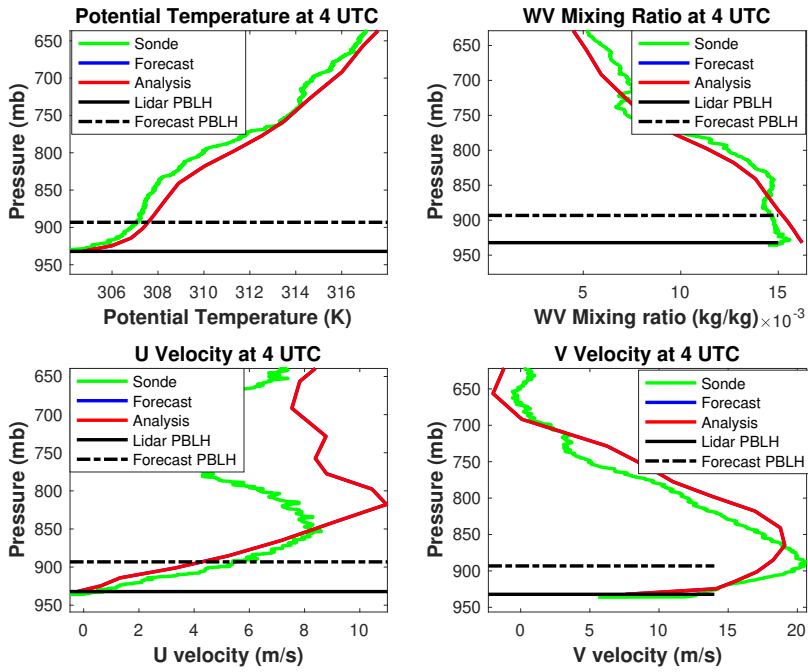


Figure 5. Same as figure ?? except using MYNN model.

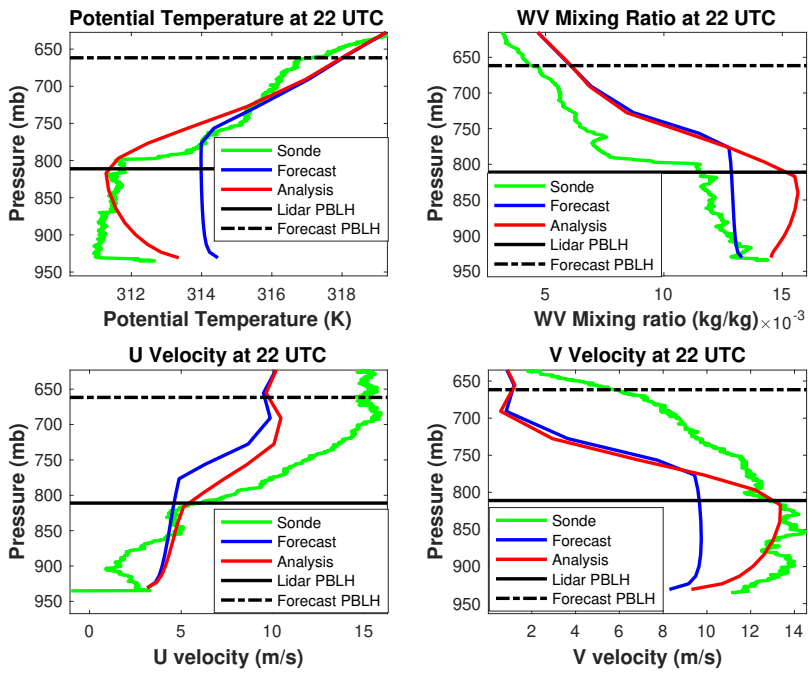


Figure 6. Same as figure ?? except using except at time 22 UTC.

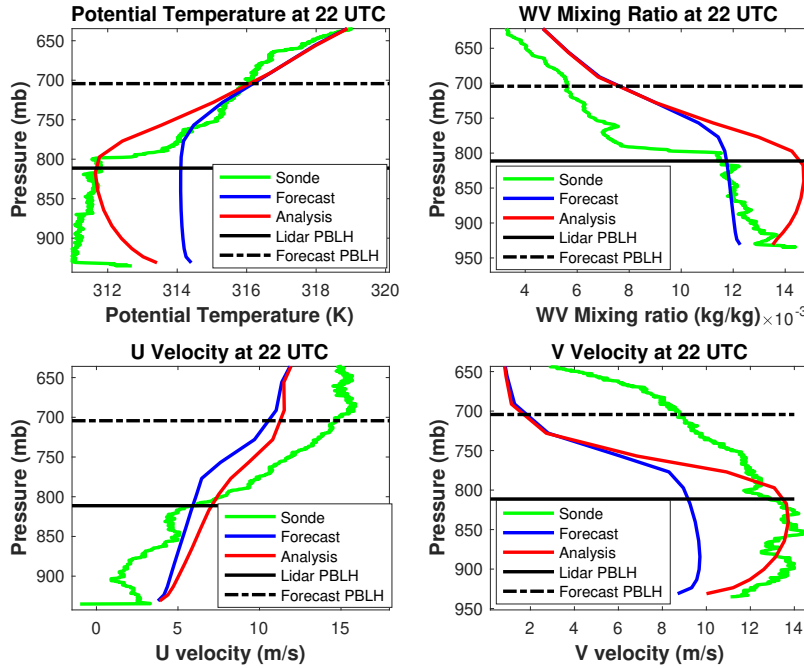
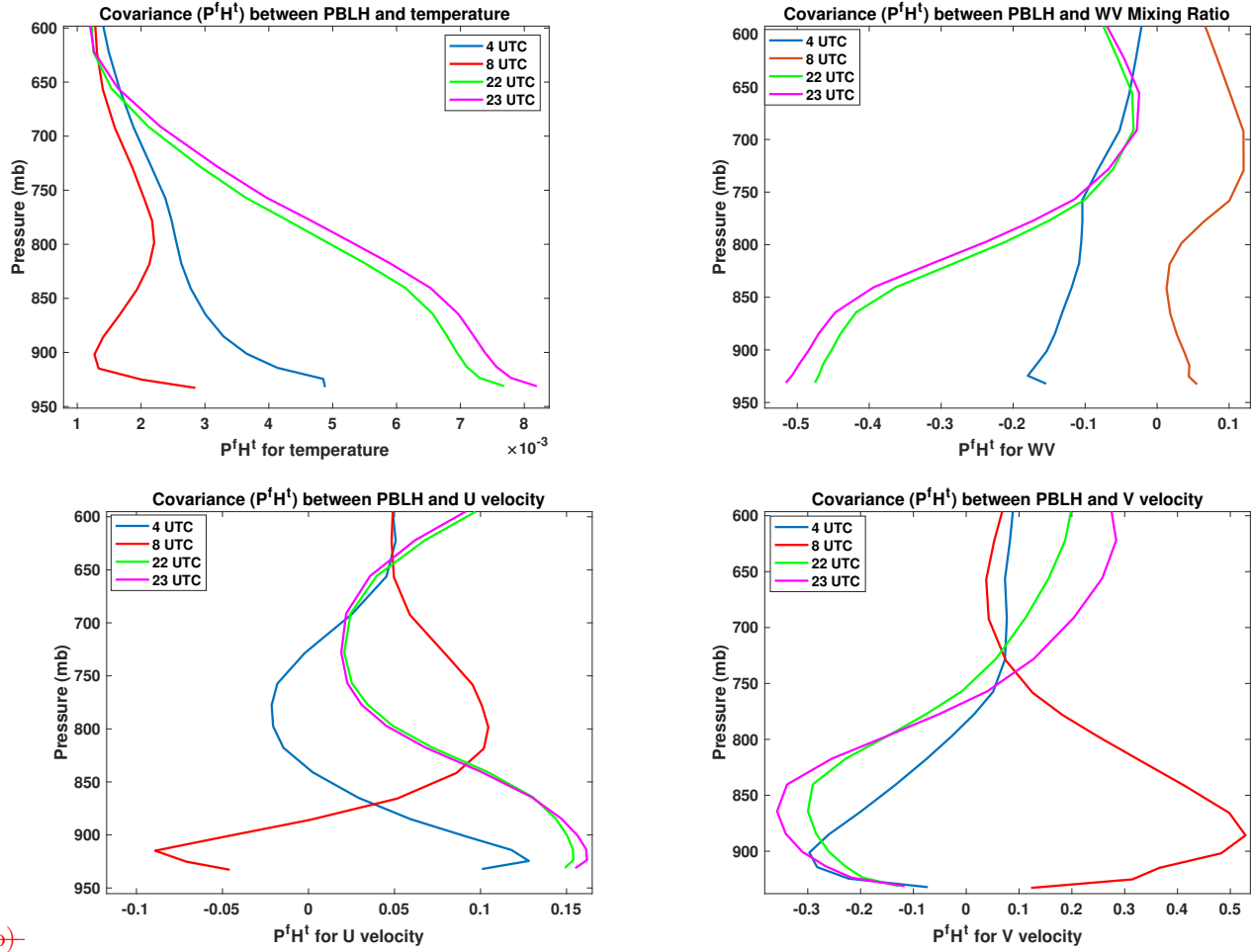


Figure 7. Same as figure ?? except using MYNN model.

316 positive and negative and shows less consistent growth. Thus, the ~~most significant~~ largest
 317 impact of assimilation ~~to on~~ temperature and moisture ~~occur~~ occurs in late afternoon
 318 while more limited velocity corrections are largely constrained by the correlations de-
 319 termined by the ensemble of model forecast states.

320 4 Conclusions

321 These offline data assimilation experiments indicate that ~~assimilation~~ assimilating
 322 ground based lidar backscatter and wind measurements of PBLH into a regional NWP
 323 model will likely lead to ~~significant improvements~~ corrections to profiles within the PBL,
 324 particularly when this approach is applied to an EnKF assimilation system with cycling.
 325 Using two NU-WRF forecasts over a period of one day with different PBL physics mod-
 326 els, we show how the state variables, T, WV, U and V can be corrected using an ~~an~~-
 327 assimilation system with ensemble based error covariances. During the night and early morn-
 328 ing the assimilation has ~~little or no~~ relatively little impact on the state variables, but by
 329 late afternoon the temperature field is drawn closer to independent ~~sonde~~ radiosonde mea-
 330 surements. We have shown that the lack of data impact early in the day is the due to
 331 the ~~high~~ relatively higher accuracy of the model and lack of correlation between the fore-



~~(a) (b)~~

~~(b) (c)~~

Figure 8. Covariance $P^f H^T$ between PBLH and temperature (~~upper left~~), water vapor (~~upper right~~), ~~U-velocity-U velocity~~ (~~lower left~~) and ~~V-velocity-V velocity~~ (~~lower right~~), at times 4, 8, 22 and 23 UTC, for PBL physics model MYHH.

332 cast PBLH and temperature profiles at that time. Later in the day, when the model is
 333 less accurate in predicting the growth of the boundary layer, the data begins to draw the
 334 ~~analysis towards the independent sonde~~ analyses mostly toward the independent radiosonde
 335 profiles. The assimilation over corrected the water vapor mixing ratio ~~is over corrected~~
 336 in the direction of ~~sonde radiosonde~~ data, and this could likely be tuned in an assimi-
 337 lation system. ~~The assimilation corrected the two velocity components by smaller amounts;~~
 338 ~~but still~~ And it corrected the the V velocity component by a smaller amount, and re-
 339 duced differences with the ~~sonde profiles~~ radiosonde profiles for the V velocity. These
 340 corrections are the result of ensemble computed error covariances between the PBLH and
 341 the state variable profiles within the PBL. The results here indicate that this approach
 342 ~~could~~ has some potential to be used in a forecast system in a way that that the PBLH
 343 observational information could be carried forward in time so as to ~~improve~~ impact the
 344 forecast accuracy within the PBL. An additional value of assimilating PBLH is its close
 345 connection with the PBL scheme used in the model. The covariances between PBLH and
 346 the different state variables are defined through the PBL physics scheme. This has an
 347 impact on the corrections made to the profiles within the PBL, which can be used as an-
 348 other way to evaluate the physics parameterizations. For example, the MYJ and MYNN
 349 result in analysis profiles that differ, ~~though~~ particularly in WV in the late afternoon.
 350 And the differences in reponse to assimilation are an indication of how the two different
 351 PBL schemes affect the covariance between PBLH and the state variables. However, a
 352 full evaluation would require that the assimilation be implemented into a cycling data
 353 assimilation system.

354 This work is intended only to demonstrate a necessary first step in terms of how
 355 ensemble statistics can help to constrain profiles within the PBL by assimilating PBLH
 356 observations. A more complete demonstration of this approach will require the construc-
 357 tion of an EnKF, and run over many days with a variety of weather patterns, including
 358 significantly warmer(cooler) and wetter(drier) days. This is needed to show how the as-
 359 similated PBLH observations will impact future forecasts within the PBL. In addition,
 360 an EnKf will involve spatial covariances in both horizontal and vertical directions, and
 361 will allow for both inflation and horizontal localization. This will enable further tuning
 362 of the system to optimize the analysis state relative to the independent radiosonde observations.
 363 The PBLH assimilation withn the EnKF framework could be done in any of numerous

364 existing enKF assimilation systems that connect with WRF, including NU-WRf (Lidard-
365 Peters *et al.*, 2015) and WRF-DART (Anderson *et al.*, 2009).

366 5 Acknowledgments

367 B. Demoz was funded by National Science Foundation award (AGS-1503563) to
368 the University of Maryland, Baltimore County and through NOAA Cooperative Science
369 Center in Atmospheric Sciences and Meteorology, funded by the Educational Partner-
370 ship Program at NOAA in collaboration with Howard University.

371 6 Data Sets

372 PECAN (https://data.eol.ucar.edu/master_list/?project=PECAN\verb) data are
373 archived by NCAR/EOL, which is funded by NSF. The forecast and analysis fields pro-
374 duced for this work are stored at <https://alg.umbc.edu/pecan/>.

375 7 Competing Interests

376 The authors declare that they have no conflict of interest.

377 8 Author Contributions

378 Andrew Tangborn built the assimilation system, with input from Jeffrey Anderson on
379 the algorithm. Belay Demoz and Brian Carroll provided the lidar observations. Joseph
380 Santanello provided background information on PBL physics. All of the authors contributed
381 to writing and revising the paper.

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