



Quantitative imaging of volcanic SO₂ plumes with Fabry Péro^t Interferometer Correlation Spectroscopy

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Abstract. We present first measurements with a novel imaging technique for atmospheric trace gases in the UV spectral range. Imaging Fabry Péro^t Interferometer Correlation Spectroscopy (IFPICS), employs a Fabry Péro^t Interferometer (FPI) as wavelength selective element. Matching the FPIs distinct, periodic transmission features to the characteristic differential absorption structures of the investigated trace gas allows to measure differential atmospheric column density (CD) distributions of numerous trace gases, e.g. sulphur dioxide (SO₂), bromine monoxide (BrO), or nitrogen dioxide (NO₂), with high spatial and temporal resolution. The high specificity in the spectral detection of IFPICS minimises cross interferences to other trace gases and aerosol extinction allowing precise determination of gas fluxes. Furthermore, the instrument response can be modelled using absorption cross sections and a solar atlas spectrum from the literature, thereby avoiding additional calibration procedures, e.g. using gas cells. In a field campaign, we recorded the temporal CD evolution of SO₂ in the volcanic plume of Mt. Etna with an integration time of 1 s and 400 × 400 pixels spatial resolution. The first IFPICS prototype can reach a detection limit of 2.1×10^{17} molec cm⁻² s^{-1/2}, which is comparable to traditional and much less selective volcanic SO₂ imaging techniques.

1 Introduction

Ground based imaging of atmospheric trace gas distributions has a great potential to give new insights into mixing processes and chemical conversion of atmospheric trace gases by allowing their observation at high spatio-temporal resolution. Whereas present space borne trace gas imaging provides daily global coverage with a spatial resolution of a few km (e.g. Veeffkind et al., 2012), ground based observation can potentially reach a spatial resolution in the order of metres and a temporal resolution in the single digit Hz range. Such techniques in particular allow the investigation of trace gas distributions with strong gradients and short time scale chemical conversions.

There are several approaches for imaging trace gas distributions using scattered sunlight in the UV-Vis wavelength range (see e.g. Platt and Stutz, 2008; Platt et al., 2015): An image can be scanned pixel by pixel with a telescope and recorded spectra are evaluated to determine the trace gas column density (whiskbroom approach). Alternatively, with a more complex optics and a two dimensional detector, one detector dimension of the spectrograph can be used for spatially resolving an image column. Column by column (or pushbroom) scanning then resolves an image. A third approach applies a small number of (typically



25 two) wavelength channels by using wavelength selective optical elements for the entire image frame, thereby usually strongly
reducing the spectral resolution (e.g. Mori and Burton, 2006; Dekemper et al., 2016). The high spectral resolution of the first
two approaches allows the accurate and simultaneous identification of several trace gases, however, the light throughput and
the scanning process severely limit the temporal resolution. The third approach can be quite fast, the trace gas selectivity, how-
ever, strongly depends on the correlation of trace gas absorption with the wavelength selective elements and usually is rather
30 marginal.

Fabry Péro Interferometers (FPIs) exhibit a periodic spectral transmission pattern, which can be matched to periodic spectral
features (typically due to rotational or vibrational structures of electronic transitions) of the trace gas absorption, thereby yield-
ing very high correlation for some trace gases. Imaging Fabry Péro Interferometer Correlation Spectroscopy (IFPICS) thus
essentially combines the advantage of fast image acquisition with selective spectral identification of the target trace gas. IFPICS
35 was proposed by Kuhn et al. (2014) and discussed in Platt et al. (2015) for volcanic SO₂. Kuhn et al. (2019) demonstrated the
feasibility with a one-pixel prototype for volcanic SO₂ and evaluated its applicability to other trace gases.

Here we present first imaging measurements (at a resolution of 400×400 pixels, 1 s exposure time) performed with IFPICS and
confirm its high selectivity and sensitivity. A prototype instrument for SO₂ was tested at Mt. Etna volcano, Italy, showing a
noise equivalent signal between $2.1 \times 10^{17} - 5.5 \times 10^{17}$ molec cm⁻² s^{-1/2}. Furthermore, we show that the instrument response
40 can be modelled and thereby intrinsically calibrated, using a solar atlas spectrum and literature trace gas absorption cross sec-
tions.

Existing interference filter based SO₂ cameras used for e.g. the quantification of volcanic trace gas emission fluxes into the
atmosphere (Mori and Burton, 2006; Bluth et al., 2007; Kern et al., 2015), exhibit strong cross interferences to aerosol scat-
tering extinction and other trace gases (Lübcke et al., 2013; Kuhn et al., 2014). Furthermore, these techniques require in field
45 calibration. Besides the thereby induced systematic errors that propagate into the emission flux quantification, the detection
limit is mostly determined by these cross interferences. Thus, the applicability of the technique is limited to strong emitters
with respective plume and weather conditions. The much higher selectivity of IFPICS largely extends the range of applicable
conditions (e.g. to ship emissions and weaker emitting volcanoes) and significantly reduces the systematic errors. Furthermore,
the extension of the technique to other trace gases e.g. bromine monoxide (BrO), formaldehyde (HCHO) or nitrogen dioxide
50 (NO₂) can give new important insights into short scale chemical conversion processes in the atmosphere.

2 Imaging Fabry Péro Interferometer Correlation Spectroscopy (IFPICS)

Similarly to the SO₂ camera principle (e.g. Mori and Burton, 2006; Bluth et al., 2007), IFPICS uses an apparent absorbance
(AA) $\tilde{\tau} = \tau_A - \tau_B$, i.e. the difference between two measured optical densities τ_A and τ_B , to quantify the column density (CD)
 $S = \int_0^L c(l) dl$, i.e. the integrated concentration c of the measured gas along a light path L for each pixel of the image. The AA
55 is calculated from two (or more) spectral settings that yield a maximum correlation difference to the gas absorption spectrum.
Ideally the periodicity of the FPI fringes are matched to periodic spectral absorption features as shown in Fig. 1 for SO₂. For
IFPICS we use two spectral settings A and B. Setting A exhibits on-band absorption, where the FPI transmission maxima

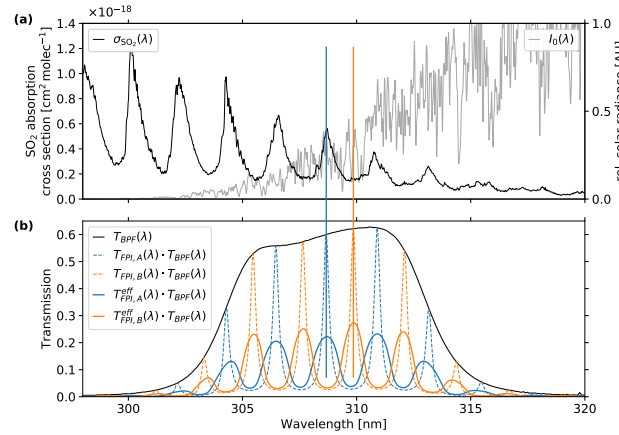


Figure 1. Spectral variation of: **(a)** The SO₂ absorption cross section σ_{SO_2} (black drawn, left axis, according to Bogumil et al. (2003)) and the scattered skylight radiance $I_0(\lambda)$ (gray drawn, right axis in relative units), given by Eq. 2. **(b)** The FPI transmissions in settings A and B yielding the maximum AA detectable (best correlation/anti-correlation to σ_{SO_2}) in the spectral range specified by the used band pass filter (BPF). Shown are: The BPF transmission $T_{\text{BPF}}(\lambda)$ (black) and the FPI transmission spectrum for a single beam approach according to Eq. 6 in on-band $T_{\text{FPI,A}}(\lambda)$ (dashed blue, correlation with σ_{SO_2}) and off-band $T_{\text{FPI,B}}(\lambda)$ setting (dashed orange, anti-correlation with σ_{SO_2}). The effective FPI transmission spectrum including an incident angle distribution according to Eq. 7 in on-band $T_{\text{FPI,A}}^{\text{eff}}(\lambda)$ (drawn blue) and off-band $T_{\text{FPI,B}}^{\text{eff}}(\lambda)$ setting (drawn orange).

coincide with the SO₂ absorption maxima and hence correlating with the differential absorption structures of SO₂. Setting B, uses an off-band position where the FPI transmission maxima anti-correlate with the differential SO₂ absorption structures (see Fig. 1). The spectral separation between setting A and B is thereby reduced by a factor of ≈ 30 (in the case of SO₂) to only ≈ 0.5 nm in contrast to $\approx 10 - 15$ nm for traditional SO₂ cameras (see Lübcke et al., 2013; Kern et al., 2015), which minimises broad band interferences due to e.g. scattering and extinction by aerosols or other absorbing gases. This application of an FPI is similar to approaches reported by Wilson et al. (2007) and Vargas-Rodríguez and Rutt (2009), for the detection of carbon monoxide, carbon dioxide and methane in the infrared spectral range.

By measuring the optical density $\tau_A = \ln(I_A/I_{0,A})$ and $\tau_B = \ln(I_B/I_{0,B})$ in both spectral settings A and B respectively, the relation between the AA $\tilde{\tau}(S)$ with the CD S is given by

$$\tilde{\tau}(S) = \tau_A - \tau_B = -\log \frac{I_A}{I_{0,A}} + \log \frac{I_B}{I_{0,B}} = k(S) = \Delta\tilde{\sigma}(S) \cdot S, \quad (1)$$

where I_A , I_B denote the radiances with and $I_{0,A}$, $I_{0,B}$ the radiance without the presence of the target trace gas in the absorption light path. The absorber free reference radiances $I_{0,A}$ and $I_{0,B}$ can be determined from e.g. a reference region within the image. The differential weighted effective trace gas absorption cross section $\Delta\tilde{\sigma}(S)$ becomes independent of S for small AAs ($\tilde{\tau} \ll 1$). At higher AAs saturation effects occur due to the non-linearity of Lambert-Beer's law, however knowledge of the absorption cross sections, the background radiation spectrum, and the instrument transmission allows to calculate $\tilde{\tau}$ for



arbitrary CDs S using a numerical model.

75 2.1 Instrument model

The AA $\tilde{\tau}$ is modelled for given target trace gas CDs S by simulating the incoming radiances I_A , I_B and $I_{0,A}$, $I_{0,B}$. As incident radiation a high-resolution, top of atmosphere (TOA) solar atlas spectrum $I_{0,TOA}(\lambda)$ is used according to Chance and Kurucz (2010). The TOA spectrum is scaled by the wavelength λ^{-4} approximating a Rayleigh scattering atmosphere. Since our measurement wavelength range, of 304-313 nm for SO_2 , overlaps with absorption of ozone (O_3), the TOA spectrum is

80 corrected for the stratospheric O_3 absorption by multiplying all intensities with the Lambert-Beer's term $e^{-\sigma_{\text{O}_3}(\lambda) \cdot S_{\text{O}_3}}$. Where S_{O_3} denotes the total atmospheric ozone slant column density, e.g. according to TEMIS Database, (Veefkind et al., 2006), and σ_{O_3} the O_3 absorption cross section according to Serdyuchenko et al. (2014). This yields the scattered skylight radiance $I_0(\lambda)$

$$I_0(\lambda) = I_{0,TOA}(\lambda) \cdot e^{-\sigma_{\text{O}_3}(\lambda) \cdot S_{\text{O}_3}} \cdot f(\lambda^{-4}). \quad (2)$$

Based on $I_0(\lambda)$ the radiances measured by the instrument for the two respective spectral settings are calculated with the

85 absorption of trace gases and the spectral instrument transfer function $T_{instr}(\lambda)$. The investigated target trace gas j (in this work SO_2) and potentially interfering trace gas species k (in this work O_3) are added according to Lambert-Beer's law. In the following we use the index i , denoting the FPI settings A and B, respectively. The quantity $I_{0,i}$ thereby denotes the reference radiance excluding the target trace gas j from the light path.

$$I_i = \int d\lambda I_0(\lambda) \cdot \exp\left(-\sigma_j(\lambda) S_j - \sum_k \sigma_k(\lambda) S_k\right) \cdot T_{instr,i}(\lambda) \quad (3)$$

90
$$I_{0,i} = \int d\lambda I_0(\lambda) \cdot \exp\left(-\sum_k \sigma_k(\lambda) S_k\right) \cdot T_{instr,i}(\lambda) \quad (4)$$

The spectral instrument transfer functions $T_{instr,i}(\lambda)$ for the two spectral settings

$$T_{instr,i}(\lambda) = T_{FPI,i}^{eff}(\lambda) \cdot T_{BPF}(\lambda) \cdot Q(\lambda) \cdot \eta(\lambda) \quad (5)$$

consists of the measured band pass filter (BPF) transmission spectrum $T_{BPF}(\lambda)$, the spectral (i.e. wavelength dependent) quantum efficiency $Q(\lambda)$ of the detector, and a spectral loss factor $\eta(\lambda)$ of the employed optical components (e.g. by reflections).

95 Considering only a single, parallel beam of light traversing the instrument the FPI transmission spectrum $T_{FPI,i}(\lambda)$ is defined by the Airy function (Perot and Fabry, 1899)

$$T_{FPI,i}(\lambda; \alpha_i, d, n, R) = \left[1 + \frac{4 \cdot R}{(1 - R)^2} \cdot \sin^2\left(\frac{2\pi \cdot d \cdot n \cdot \cos \alpha_i}{\lambda}\right)\right]^{-1} \quad (6)$$

with the light beam incidence angle α_i for the two spectral settings onto the FPI, the FPI mirror separation d , the refractive index n of the medium inside the FPI, and the FPI reflectivity R (see Tab. 1, Fig. 1 and Fig. 2, (c)).

100 However, in reality a spectral setting will always contain a range of incidence angles onto the FPI. In this work we assume cone



shaped light beams, with half cone opening angles ω_c , where the entire cone can be tilted by α_i relative to the normal of the FPI mirrors (see Fig. 2, (c)). From this assumption follows that the incidence angles α_i are distributed over a cone with the incidence angle distribution $\gamma(\alpha_i, \omega_c, \vartheta, \varphi)$, where ϑ and φ are the polar and azimuth angles, respectively. Hence, the single beam FPI transmission spectrum $T_{FPI,i}(\lambda)$ of Equation 6 is extended by a weighted average over $T_{FPI,i}(\lambda; \gamma(\alpha_i, \omega_c, \vartheta, \varphi), d, n, R)$,
 105 giving the effective FPI transmission spectrum $T_{FPI,i}^{eff}(\lambda)$

$$T_{FPI,i}^{eff}(\lambda; \gamma(\alpha_i, \omega_c), d, n, R) = \frac{1}{N(\gamma(\alpha_i, \omega_c))} \int_0^{\varphi_{max}} \int_{\vartheta_{min}}^{\vartheta_{max}} T_{FPI,i}(\lambda; \gamma(\alpha_i, \omega_c, \vartheta, \varphi), d, n, R) \sin \vartheta d\vartheta d\varphi. \quad (7)$$

Thereby, $N(\gamma(\alpha_i, \omega_c))$ denotes the weighting function, ϑ the polar angle and φ the azimuth angle of the spherical integration within boundaries defined by the tilted cone shaped light beams. E.g.: for a non-tilted FPI ($\alpha_i = 0$) the integration boundaries are $\vartheta \in [0, \omega_c]$ and $\varphi \in [0, 2\pi]$, for a tilted FPI however, the transformation of $\gamma(\alpha_i, \omega_c, \vartheta, \varphi)$ is more complex and requires
 110 several case analyses.

The incidence angle distribution $\gamma(\alpha_i, \omega_c)$ will affect the shape of the FPI transmission spectrum by decreasing the effective finesse F of the FPI leading to a blurring of the FPI fringes (see Fig. 1).

2.2 The IFPICS prototype

The IFPICS prototype is a newly developed instrument, designed to function under harsh environmental conditions in re-
 115 mote locations like e.g. in the proximity to volcanoes. Hence, the prototype is designed to be small with dimensions of 200 mm \times 350 mm \times 130 mm, lightweight with 4.8 kg (see Fig. 2, (a)) and has a power consumption < 10 W, thus can be battery-operated for several hours. A 2D UV-sensitive CMOS sensor (SCM2020-UV provided by *EHD imaging*) is used to acquire images. However, we found that the software of the SCM2020-UV image sensor does not allow sufficiently precise triggering. Therefore ≈ 0.6 seconds are lost in each image acquisition, which severely limits the operation of the IFPICS cam-
 120 era. Replacement of the sensor by a scientific-grade UV detector array will solve this problem in future studies.

The internal camera optics is highly modular and easily adjustable. The IFPICS prototype employs an image side telecentric optical setup as proposed in Kuhn et al. (2014, 2019). A photograph and a schematic drawing are shown in Fig. 2. An aperture and a lens (lens 1) parallelise incoming light from the imaging field of view (FOV) before it traverses the FPI and the BPF. A second lens (lens 2) focusses the light onto the 2D UV-sensitive sensor. Thereby, in good approximation, all the pixels of
 125 the image experience the same spectral instrument transfer function $T_{instr,i}(\lambda)$ for the two wavelength settings. The static air-spaced FPI (d , n and R fixed, provided by *SLS Optics Ltd.*) can be tilted within the parallelised light path in order to tune its spectral transmission T_{FPI}^{eff} between setting A and B via variation of the incidence angle α (see Section 2.1). The half cone opening angle ω_c is determined by the entrance aperture a and the focal length f of lens 1 and can be calculated by $\omega_c = \arctan(a/2f)$. The physical properties of the optical components and the instrument are listed in Tab. 1 and were mostly
 130 chosen according to the dimensioning assumed in the calculations of Kuhn et al. (2019).

The FPI design with fixed d , n and R (see Fig. 2, (c)) in particular is chosen to inherently generate a transmission spectrum matching the differential absorption structures of SO_2 . This includes the basic idea that the untilted FPI ($\alpha_i = 0^\circ$) al-

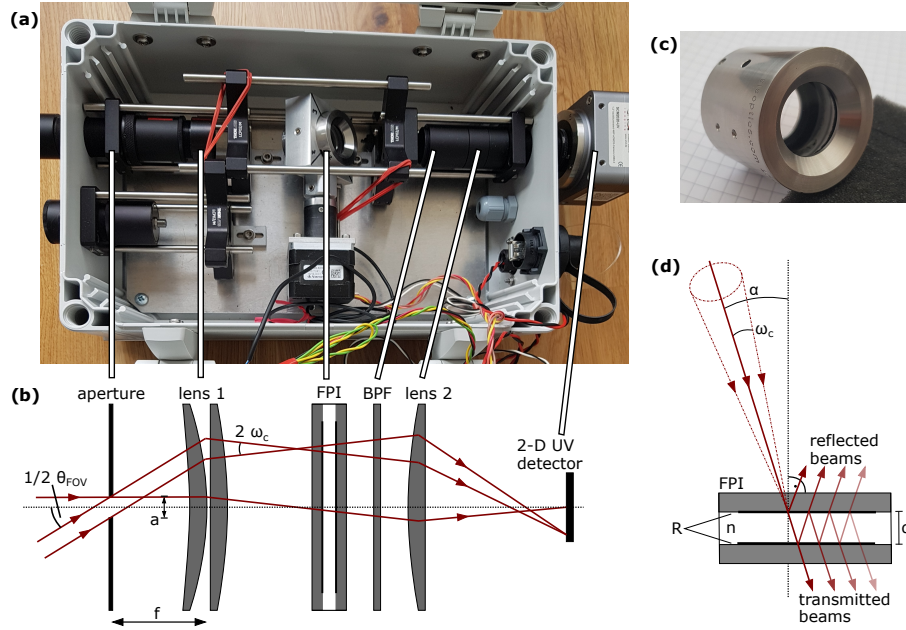


Figure 2. (a): Photograph of the IFPICS instrument. The physical dimensions are $200\text{ mm} \times 350\text{ mm} \times 130\text{ mm}$ ($w \times l \times h$) and 4.8 kg . (b): Sketch of the image side telecentric optical setup of the IFPICS prototype. Incident radiation is parallelized by an entrance aperture and lens 1 before traversing the FPI and the band pass filter (BPF). The maximum half cone opening angle ω_c is dependent on the aperture diameter a and the focal length f of lens 1. The camera field of view is $\theta_{FOV} = 18^\circ$. A second lens maps the image onto a 2-D UV sensitive CMOS detector. (c): Photograph of the static air-spaced etalon (FPI) provided by *SLS Optics Ltd.*. (d): Sketch of the FPI. An incoming single beam (drawn red) with incidence angle α is reflected multiple times between the FPI mirrors with reflectance R and separation d . Visualisation of an incoming cone shaped beam (red dash-dotted) with half cone opening angle ω_c and incidence angle α of the cone axis.

ready matches the on-band position A. In our case however, the manufacturing accuracy of d lies within one free spectral range ($\approx 2\text{ nm}$ for SO_2) yielding that $\alpha_B = 0^\circ$, corresponds to a off-band (B) position ($T_{FPI,B}^{eff}$) and the on-band (A) position ($T_{FPI,A}^{eff}$) is reached by a small tilt of $\alpha_A = 4.5^\circ$. The basic advantages of using small incident angles α_i are, that they keep the spread of the incidence angle distribution $\gamma(\alpha_i, \omega_c)$ (see Section 2.1) low and thereby retain the FPIs effective finesse F high (since the reflectivity R of the FPI-mirror coating is somewhat dependent on the angle of incidence so is the finesse F). This leads to a much weaker blurring of the FPI fringes in the FPI transmission spectrum $T_{FPI,i}^{eff}$ resulting in a higher sensitivity of the instrument (see Fig. 1). With the prototype setup, however, we encountered disturbing reflections for low FPI incidence angles. For that reason we used the subsequent correlating order of the FPI transmission with $\alpha_A = 8.17^\circ$ for an on-band and $\alpha_B = 6.45^\circ$ for an off-band setting (see Tab. 1), thereby making a compromise between sensitivity and accurate evaluable images.



Table 1. Parameters of the optical components installed in the IFPICS prototype and used in the calibration model. The uncertainties of the model input parameters are shown.

| parameter | value | uncertainties | description |
|-----------------------------|--------|---------------|-------------------------|
| d [μm] | 21.666 | ± 0.002 | FPI plate separation |
| R | 0.65 | | FPI reflectivity |
| F | 7.15 | | FPI finesse |
| n | 1.0003 | | refractive index (air) |
| α_A [$^\circ$] | 8.17 | ± 0.02 | FPI tilt, on-band |
| α_B [$^\circ$] | 6.45 | ± 0.02 | FPI tilt, off-band |
| $T_{BPF,max}$ | 0.63 | | BPF peak transmission |
| λ_{BPF} [nm] | 308.5 | | BPF central wavelength |
| δ_{BPF} [nm] | 9.0 | | BPF FWHM |
| f [mm] | 47 | ± 2 | lens 1 focal length* |
| a [mm] | 1.55 | ± 0.05 | aperture diameter |
| ω_c [$^\circ$] | 0.945 | | half cone opening angle |
| θ_{FOV} [$^\circ$] | 18 | | imaging FOV |

*: two lenses: $f = \frac{f_1 \cdot f_2}{f_1 + f_2}$ with $f_1 = f_2 \approx 94 \text{ mm}$ @ $\lambda = 310 \text{ nm}$

3 Proof of concept study

3.1 Measurements at Mt. Etna, Italy

145 First measurements with the prototype describe above were performed at the Osservatorio Vulcanologico Pizzi Deneri (lat 37.766, long 15.017, 2800 m a.s.l.) at Mt. Etna, on July 21 and 22, 2019. The physical properties of the IFPICS prototype and the FPI tilt angles α_i for tuning $T_{FPI,i}^{eff}(\lambda)$ between on-band $i = A$ and off-band setting $i = B$ were selected according to Tab. 1. The exposure time was set to 1 s for all acquired images.

150 3.2 Validation of the instrument model

To quantify the accuracy of our model two SO_2 gas cells were measured with the IFPICS prototype and by Differential Optical Absorption Spectroscopy (DOAS, see Platt and Stutz, 2008), on July 21, 2019, 11:10 - 11:20 CET. The sky was used as light source with a constant viewing angle (10° elevation, 270°N azimuth) in a plume free part of the sky. To enhance the image quality a flat-field correction is used, compensating pixel to pixel variations in sensitivity. The flat-field correction requires the acquisition of dark and flat-field images. The dark images are determined by the arithmetic mean over five images with no light entering the IFPICS instrument and the flat-field images are obtained by the arithmetic mean over five images acquired in a plume free sky region. The flat field images thereby directly including the reference measurement $I_{0,i}$, making a later correction for the atmospheric background unnecessary. In the same viewing direction I_i is measured for each gas cell and FPI setting i in order to calculate the AA according to Eq. 1. Figure 3 shows the gas cell measurements (red) including uncertainties (error-



160 bars, $1-\sigma$). The uncertainties directly arise from the errors of the DOAS measurement and due to variations in optomechanical settings of the IFPICS prototype.

The instrument model (Eq. 2 - 7) was used to calculate the IFPICSs AA $\tilde{\tau}_{\text{SO}_2}(S_{\text{SO}_2})$ from a given SO_2 CD S_{SO_2} . The model parameters are mostly fixed by the IFPICS prototype optics as given in Tab. 1. The remaining parameter, the atmospheric O_3 slant column density S_{O_3} (see Eq. 2) is calculated in a geometric approximation $S_{\text{O}_3} = \text{VCD}_{\text{O}_3} / \cos(\text{SZA})$ using the solar
165 zentih angle (SZA) and vertical O_3 column density (VCD_{O_3}) which both are location, date and time dependent. They were: $\text{SZA} = (53 \pm 3)^\circ$ (according to the solar geometry calculator by NOAA) and $\text{VCD}_{\text{O}_3} = (335 \pm 5)$ DU (according to TEMIS database; Veeffkind et al., 2006). The VCD_{O_3} can be treated to be approximately constant over the period of a day.

The output of the instrument model (drawn, black) for an SZA of 53° is shown in Fig. 3. The model uncertainty (shaded grey) is determined by a root mean square over the errors in the output by individually varying the input parameters within their
170 stated uncertainties. The thus calculated calibration function using the instrument model matches the SO_2 gas cells validation measurement within the range of confidence. The model nicely describes the flattening of the AA-CD relation for high CDs (up to $\approx 2.5 \times 10^{18}$ molec cm^{-2}), which originates from the CD dependence of $\Delta\tilde{\sigma}(S)$ (see Eq. 1).

To show the impacts of the SZA on the instrument model the model output is also calculated for three other SZAs while keeping the other parameters constant. The model output is shown in Fig. 3 for an SZA of 80° (dash-dotted grey) for early
175 morning/late afternoon conditions, SZA of 70° (dashed grey) for morning/afternoon conditions and SZA of 25° (dotted grey) for noon conditions. High SZAs lead to an increase of stratospheric O_3 absorption which alters the spectral shape of the scattered skylight radiance $I_0(\lambda)$ (see Eq. 2) which is used in the forward model. I. e. for high O_3 absorption, lower wavelength radiance, where the differential SO_2 absorption features are stronger, will contribute less to the integrated radiances $I_i, I_{0,i}$ (Eq. 3, 4). The thereby induced SZA dependence of the sensitivity can easily be accounted for in the model. Note, that this influence
180 of strong O_3 absorption only occurs at our chosen wavelength range for the SO_2 measurement. When applying IFPICS to other trace gases, e.g. BrO or NO_2 at higher wavelength, this effect will be negligible.

3.3 Results of the field measurements

Volcanic plume measurements were performed on July 22, 2019, 08:50 - 09:10 CET. The instrument was pointing towards the plume of Mt. Etna's South East crater with a constant viewing direction (azimuth 204°N , elevation 5° , see Fig. 4). The wind
185 direction was $\approx 5^\circ\text{N}$ with a velocity of $\approx 6 \text{ m s}^{-1}$ (wind data from UWYO). Hence, the plume was partly covered by the crater flank. The frame rate during the measurement was 0.2 Hz for a pair (I_A and I_B) of images.

The flat-field correction was performed as described in section 3.2, using the arithmetic mean over five dark images and flat-field images, obtained in a plume free sky region. An exemplary set of volcanic plume SO_2 images, obtained with the IFPICS instrument in on-band setting I_A and off-band setting I_B , are shown in Fig. 5. Further images of I_A and I_B are shown in
190 Appendix A. The circular shape of the retrieved image arises from the FPI's circular clear aperture limiting the imaging FOV. The IFPICS SO_2 AA $\tilde{\tau}_{\text{SO}_2}$ is calculated pixel-wise according to Eq. 1 from I_A and I_B . For the conversion into SO_2 CD S_{SO_2} the forward instrument model (Eq. 2 - 7) is inverted by least square fitting of a 4th order polynomial to the calculated CD relation $S_{\text{SO}_2}(\tilde{\tau}_{\text{SO}_2})$. The model input parameters of the instrument are shown in Tab. 1. The SZA during the time of the

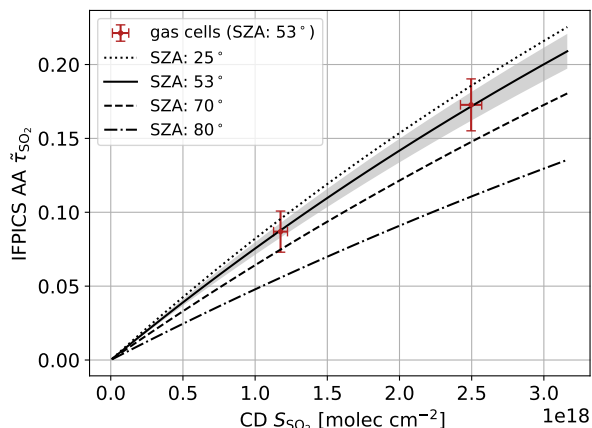


Figure 3. The validation measurement with two SO_2 gas cells (red, with $1\text{-}\sigma$ error) with the IFPICS prototype and by DOAS on 21 July 2019, 11:10 - 11:20 CET with a solar zenith angle (SZ) of 53° .

The instrument forward model (Eq. 2-7) is used to calculate the IFPICS AA $\tilde{\tau}_{\text{SO}_2}$ for a given CD S_{SO_2} range. The model input parameters are shown in Tab. 1 and (335 ± 5) DU is used as VCD_{O_3} . The calculated model output (black) is shown for four different SZAs (25° (dotted), 53° (drawn), 70° (dashed) and 80° (dash-dotted)). The model output and the validation measurement are in good agreement if a model SZA of 53° is used, which is equivalent to the SZA during the measurement time. The model uncertainty is shown in shaded grey.

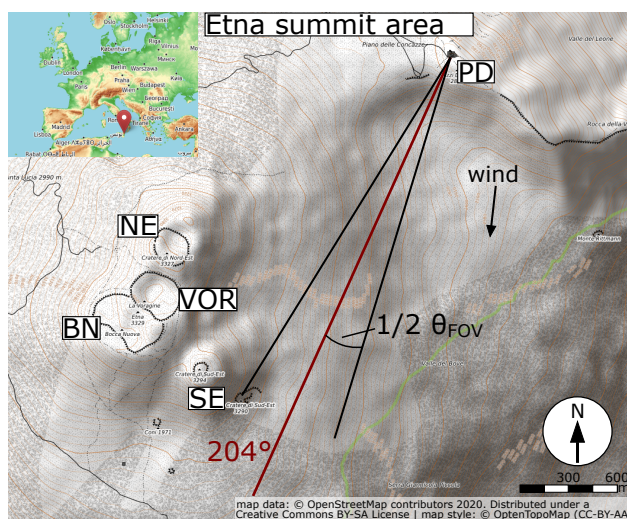


Figure 4. Topographic map of the Mt. Etna summit area, North East crater (NE), Voragine (VOR), Bocca Nuova (BN), South East crater (SE) and measurement location at the Osservatorio Vulcanologico Pizzi Deneri (PD) are indicated. The viewing direction on 22 July 2019 is 204° (red drawn) with an FOV of $\theta_{\text{FOV}} = 18^\circ$ (black drawn) and an elevation of 5° . The FOV is partly covering the plume emanating from SE crater. The average wind direction is $\approx 5^\circ$ with a speed of ≈ 6 m/s (wind data from UWYO).

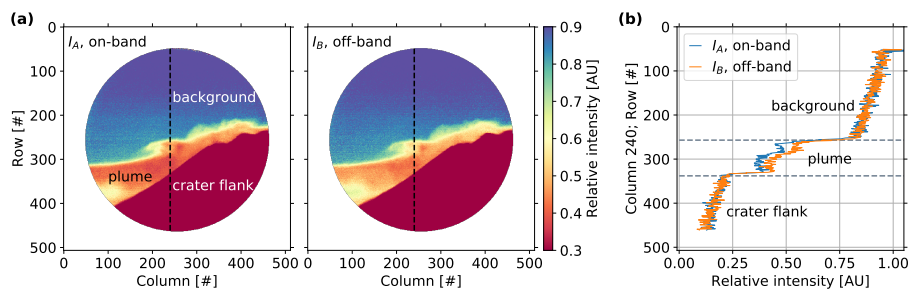


Figure 5. (a): Flat-field corrected intensity images (400×400 pixel) acquired with the IFPICS prototype in on-band I_A and off-band setting I_B . The I_A image shows the expected higher SO_2 absorption in comparison with I_B ($I_A < I_B$ in plume region). The plume is visible in both images due to the broad band SO_2 absorption and other extinction in the measurement spectral range. The circular image shape arise from the FPIs circular clear aperture. **(b):** Intensity column 240 (dashed black lines in (a)) for I_A (blue) and I_B (orange). The enhanced absorption (reduced intensity) is clearly visible in the plume section with $I_A < I_B$, whereas in the background sky and crater flank sections the intensities are equal $I_A = I_B$.

195 measurement is $(78 \pm 3)^\circ$ (NOAA) with a VCD_{O_3} of 335 ± 5 DU (according to TEMIS database; Veeckind et al., 2006). The retrieved calibration function $S_{\text{SO}_2}(\tilde{\tau}_{\text{SO}_2})$ is

$$S_{\text{SO}_2}(\tilde{\tau}_{\text{SO}_2}) = \sum_0^4 x_i \cdot \tilde{\tau}_{\text{SO}_2}^i \quad (8)$$

with $x_0 = 1.0 \times 10^{13}$, $x_1 = 1.1 \times 10^{19}$, $x_2 = 9.3 \times 10^{18}$, $x_3 = 7.9 \times 10^{18}$, and $x_4 = 1.6 \times 10^{19}$ in units of molec cm^{-2} respectively. This approximation yields an average relative deviation of 0.006% for S_{SO_2} from the modelled value, with a maximum relative deviation of 0.07% for small SO_2 CDs. An evaluated image of the volcanic plume SO_2 CD distribution corresponding to the intensities shown in Fig. 5 is shown in Fig. 6. Further evaluated CD distribution images of the same time series are presented in Appendix A. A time series of the plume evolution is visualised in a flip-book from the supplementary material. The volcanic plume of Mt. Etna's South East crater is clearly visibly and reaches SO_2 CDs higher than $3 \times 10^{18} \text{ molec cm}^{-2}$. The atmospheric background is $S_{\text{SO}_2, bg} = 4.3 \times 10^{16} \text{ molec cm}^{-2}$ and was determined by the arithmetic mean over a plume free area within the evaluated image (white square, 100×100 pixel, in Fig. 6, (a)). The $S_{\text{SO}_2, bg}$ was subtracted from the displayed image in the final step of the evaluation. The similar plume free area (white square, 100×100 pixel, in Fig. 6, (a)) is further used to give an estimation for the SO_2 detection limit of the IFPICS prototype by calculating the $1-\sigma$ pixel-pixel standard deviation. The obtained detection limit is $5.5 \times 10^{17} \text{ molec cm}^{-2} \text{ s}^{-1/2}$ given by the noise equivalent signal. The measurements were performed in the morning with an SZA of 78° and therefore reduced sensitivity and under relatively low light conditions. For decreasing SZA the sensitivity will increase according to Fig. 3 and the increasing sky radiance will reduce the photon shot noise. I.e. the gas cell measurements (taken at SZA of 53° , with approximately twice the sky radiance compared to SZA of 78°) show a detection limit of $2.1 \times 10^{17} \text{ molec cm}^{-2} \text{ s}^{-1/2}$. For ideal measurement conditions (lowest SZA, highest sky radiance) the detection limit will be further improved.

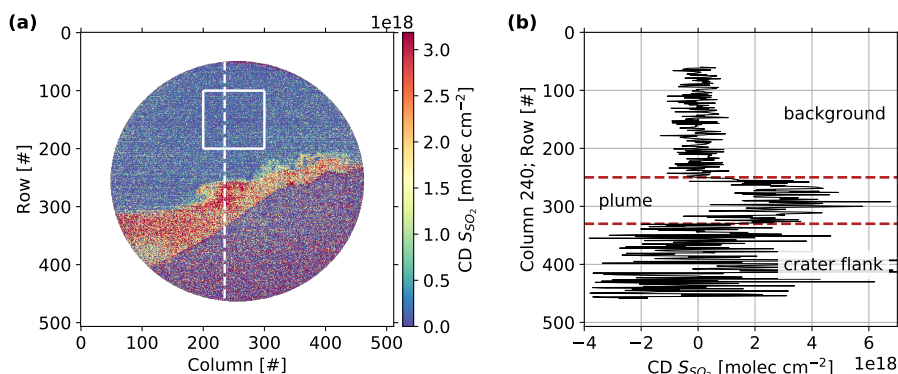


Figure 6. (a): Volcanic plume SO_2 CD distribution calculated from images acquired with the IFPICS prototype and using the instrument forward model conversion function $S_{\text{SO}_2}(\tilde{\tau}_{\text{SO}_2})$ (see Eq. 8). The plume free area indicated by a white square (100×100 pixel) is used to correct for atmospheric background and to obtain an estimation for the detection limit. (b): Individual SO_2 CD column 240 (indicated by dashed white line in (a)) showing that background, plume and crater flank region are clearly distinguishable. High scattering in the crater flank region is induced by low radiance.

4 Conclusion

By imaging and quantifying the SO_2 distribution in the volcanic plume of Mt. Etna we successfully demonstrate the feasibility of the IFPICS technique proposed by Kuhn et al. (2014). We were able to unequivocally resolve the dynamical evolution of SO_2 in a volcanic plume with a high spatial and temporal resolution (400×400 pixel, 1 s integration time). The retrieved detection limit for the SO_2 measurement is $5.5 \times 10^{17} \text{ molec cm}^{-2} \text{ s}^{-1/2}$. The detection limit however varies with the SZA and can reach values below $2 \times 10^{17} \text{ molec cm}^{-2} \text{ s}^{-1/2}$ under ideal conditions, comparable to traditional SO_2 imaging techniques (see Kern et al., 2015).

The specific spectral detection scheme of IFPICS allows to use a numerical instrument model to directly convert the measured AA $\tilde{\tau}$ into CD S distributions. This inherent calibration method makes in-field calibrations methods, e.g. by gas cells, unnecessary. The accuracy of the instrument model could be demonstrated using SO_2 cells with a known CD, determined by simultaneous DOAS measurements.

Our IFPICS instrument is still an early stage prototype. The employed optics are highly modular allowing easy adjustments even outside a laboratory. The physical dimensions of < 10 litres, and < 5 kg and the low power consumption of < 10 W combined with the fact that no maintenance and in-field calibration is needed, make it already a close to ideal field instrument. Furthermore, the temporal resolution of the instrument can further be increased by replacing the employed sensor as it does not allow for time-optimised control of image acquisition.

Compared to traditional SO_2 cameras the minimised cross interferences to broad band plume extinction increases selectivity and thus should allow to apply the IFPICS technique to much weaker SO_2 sources. Furthermore, the small interference to broadband effects extends the range of meteorological conditions acceptable for field measurement. Also, the imaging tech-



nique lends itself to the determination of gas fluxes. For instance the wind velocity and also the angle between the observation direction and plume propagation direction can be determined from the images series (see e.g. Klein et al., 2017).

235 The demonstrated IFPICS technique is not limited to the detection of SO_2 . In general the technique is applicable to numerous further trace gases which show a distinct pattern (ideally periodic) in their absorption spectrum (see Kuhn et al., 2019). In the case of volcanic emissions detectable trace species are e.g. bromine monoxide BrO or chlorine dioxide OClO . Beyond volcanic applications IFPICS could be used to investigate e.g. air pollution by measuring nitrogen dioxide NO_2 or formaldehyde HCHO .

Appendix A

240 Further evaluated images of the time series acquired on July 22, 2019, 08:50 - 09:10 CET at Mt. Etna, Italy are shown in Fig. A1. The evaluation procedure is analogous to the routine explained in Section 3.3. The time difference between a set (1 - 4) of images accounts for ≈ 120 s and allows to trace back plume dynamics.

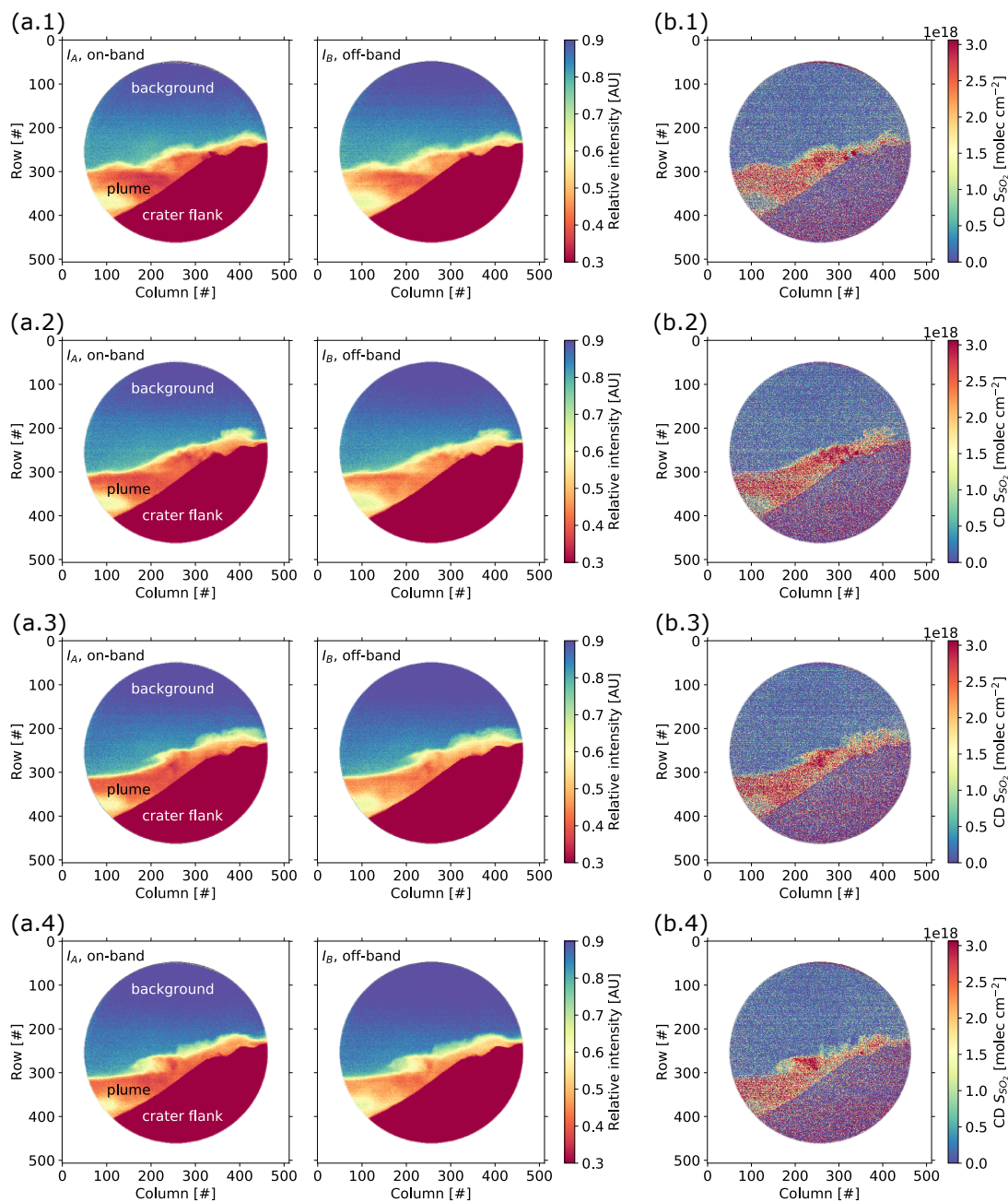


Figure A1. Exemplary set of evaluated images (400×400 pixel) acquired with the IFPICS prototype on 22. July 2019, 08:50 - 09:10 CET at Mt. Etna, Italy. The time difference between each set of images (1-4) accounts for ≈ 120 s, allowing to trace back plume dynamics. (a): Flat-field corrected intensity images I_A and I_B . (b): Volcanic plume SO_2 CD S_{SO_2} distribution calculated with the conversion function shown in Eq. 8.



Data availability. The data can be obtained from the authors upon request.

Author contributions. JK, NB and UP developed the question of research. JK, NB and CF conducted the field campaign. JK and CF developed the instrument model. CF designed, constructed and characterised the instrument, evaluated the data and wrote the manuscript with all authors contributing by revising it within several iterations.

Competing interests. The authors declare that they have no conflict of interest.

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