Supplementary text S1:

Truncation correction sensitivity analysis

- 5 We performed a sensitivity test to determine how the choice of truncation model input parameters affects the calculated, timeresolved truncation correction factors. The results of this analysis are presented in Fig. S12. The following ranges of model input parameters were investigated. The real and imaginary parts of the aerosol refractive index were varied from 1.50 to 1.59 and 0.00 to 0.01, respectively, based on the summary of measurements presented by Espinosa et al. (2019). The extra path length beyond the integrating sphere *l* was varied from 0 to 4.7 cm, based on the results and approach presented and discussed
- 10 in Sect. 5. Finally, we tested the sensitivity of γ to a third dimension of information, the accuracy of the measured coarse mode size distribution measurements. Here only two limiting cases were considered with the size distributions integrated up to 10 μ m (i.e., PM10) and 2.5 μ m (PM2.5). The first case represents the size distributions measured as they were, and the second case crudely represents the possibility that the CAPS630b sampled coarse particles less efficiently than the APS due, for example, to sampling line losses.

15

Supplementary figures:



Figure S1: Theoretically-calculated relative uncertainty in 1-minute averaged (left panel) and 1-second averaged (right panel) CAPS PMssa b_{abs} measurements as a function of the relative uncertainty in the combined scattering correction factor (defined in Eq. 6 using the ratio of the truncation correction factor γ and the instrument cross-calibration factor β). Curves are shown for four different SSA values (grey shading) and two different aerosol loadings (b_{ext} of 10 and 100 Mm⁻¹). The curves were generated using the error model presented in Sect. 2.3 and Appendix A2 with inputs that were chosen to represent instrument characteristics during

25 the Cabauw field campaign, as detailed in the main text.



Figure S2: Experimental arrangement for measuring CAPS PMssa scattering cross-calibration ($\beta_{Rayleigh}$) and scattered light truncation (γ) factors. Solutions of non-absorbing particles (PSL spheres, ammonium sulfate, DEHS) were used in the nebulizer. When PSL spheres with diameters less than ~200 nm were used, a simplified arrangement involving no size classifier was investigated as a way of measuring cross-calibration factors in the field.



Figure S3: Example number 1 of laboratory measurements used to determine the scattering cross calibration factor $\beta_{Rayleigh}$. The calibration aerosol was 240 nm PSL particles and a storage volume was employed to cover a broad range of aerosol loadings.



Figure S4: Example number 2 of measurements used to determine the scattering cross calibration factor $\beta_{Rayteigh}$. The calibration aerosol was 240 nm PSL particles. These particles were passed directly to the CAPS PMssa without passing through a storage volume, which means the calibration covers a narrower range of aerosol loadings than the calibration shown in Fig. S3.



45

Figure S5: Comparison of cross calibration factors determined back to back with and without an AAC size classifier.



Figure S6: Example measurements from a field campaign in Melpitz, Germany showing the effect that contamination of the CAPS PMssa optical cavity has on measured extinction and scattering coefficients.



Figure S7: Measured and modeled truncation values as a function of volume equivalent particle diameter for ammonium sulfate. Discrepancies between these measurements and the DEHS measurements in the manuscript are interpreted as being due to the asphericity of the ammonium sulfate particles.



Figure S8: Baseline characteristics for the PMssa unit CAPS630b during the Cabauw field campaign.



65 Figure S9: Scattering and extinction coefficients measured by the CAPS630b during the Cabauw field campaign processed with both step-function and linear interpolation between measured baseline periods.

150 & 200 nm AS, measured at 1-sec time resolution on 2016-09-09 with instrument unit CAPS_{630b}



Figure S10: Cross calibration performed for the instrument unit CAPS630b on 2016-09-09 at the beginning of the Cabauw field campaign.



Figure S11: Cross calibration performed for the instrument unit CAPS630b on 2016-10-10 at the beginning of the Cabauw field campaign.



Figure S12: The distributions of hourly time-resolved truncation correction factors (γ) for the Cabauw campaign calculated with the new model introduced in Sect. 2.2.3 and presented in Appendix A1. A range of different model input parameters were chosen to investigate the sensitivity of γ to these parameters. In particular, we varied the refractive index (two values shown on the y-axis), the extra path length *l* considered in the calculation (three values shown as separate figure panels), and the accuracy of the coarse mode size distribution measurements between diameters of 2.5 and 10 µm, which was crudely represented by changing the upper limit of integration across the size distribution from 10 µm (i.e., PM10) to 2.5 µm (i.e., PM2.5). The vertical green and purple lines in each panel indicate the values of γ that result from using constant, campaign-averaged SMPS and SMPS+APS size distributions in the calculations, respectively, rather than the corresponding time-resolved size distribution measurements.

85





the right panel for reference.



Figure S14: As above for Fig. S12 but for Cabauw data separated into fine-mode dominated and coarse-mode containing samples.



105 Figure S15: Comparison of CAPS PMssa absorption coefficients at 630 nm (b_{abs}^{630nm}) and MAAP absorption coefficients at 637 nm (b_{abs}^{637nm}) for five different truncation correction scenarios. The three columns represent different subsets of the dataset, as indicated in the column titles. The five rows represent the different truncation correction scenarios, as indicated in the row labels. All data

points are colored by the SSA values calculated from the same CAPS PMssa data shown in each panel. The mean ratios of CAPS PMssa to MAAP b_{abs} are plotted as solid orange lines in each panel. The uncertainty bands represent the 95th percentiles of theoretical uncertainties calculated with the error model and inputs described in Sect. 2.3, with relative uncertainties in γ of 4, 9, and 6% for the fine-mode dominated, coarse-mode containing, and full dataset, respectively.

Center of the optical cavity (z = 0 cm)



115 Figure S16: Curves representing the probability that light is reflected from the glass sampling tube of the CAPS PMssa for a single reflection event (Eq. A7), the number of reflection events that is needed for light to exit the integrating sphere in the instrument (Eq. A8), and the resulting total fraction of light that is reflected out of the sphere (Eq. A9), all as a function of scattering angle θ and for the case of a particle at the center of the optical cavity of the instrument (z = 0 cm)