The author's text in italics, the referee comments in plain text.

General comments:

Shen et al. present a new algorithm for the size-resolved correction of the hygroscopicity, κ considering shrinking effect caused by to multi-charge number contribution. I recommend this manuscript to be published in AMT after the following issues to be addressed and modified.

Major comments:

1. The term "shrinking effect" seems to be unfortunate, since it used for actual irregular particles restructuring in the humid conditions caused by surface or capillary forces of absorbed/adsorbed water. To avoid confusion I recommend using another term, say "compression effect" or "displacement effect".

2. The shrinking function S(i, v) is not properly described in the text. Please show which expression/algorithm was used to calculate it.

3. The multi-charge algorithm for hygroscopicity correction has not been properly tested. As a first step, I would suggest to apply it for single-component particles (100; 200, and 300 nm) with well-defined thermodynamic and hygroscopic properties, ammonium sulfate as an example. Please show the particle's growth factors change taking into account (x,v), $\Omega(x,v,i)$ and S(i, v) and then κ initial and κ corrected as a function RH.

4. Due to typos and errors, the text is difficult to read.

Minor comments:

Page 1, line 30: Swietlicki et al. should be Swietlicki et al., 2008;

Page 2, Line 33: (*Cubison, Coe, & Gysel, 2005; Gysel, McFiggans, & Coe, 2009; Stolzenburg & McMurry, 2008; Voutilainen, Stratmann, & Kaipio, 2000*). Correct citation according to AMT instruction,

Line 41: "*Duplissy et al. (2008) obtained* ..." Note, Gysel et al., 2009 obtained the kernel function, Duplissy et al. (2008) just used it for multi-charge correction.

Line 42 "GFs" The abbreviation is not defined.

Page 3, Line 70, please define the scale parameter *x* once.

Line 74, term n(x) is not defined.

Lne 77, Fig, 1b. *The corresponding ratio of particles carrying different charges is calculated from the PNSD using the abovementioned DMA electrical mobility and charging theory.* Please specify in detail how data in Fig.1b were obtained? Show in the explicit form the (x,v) and $\Omega(x,v, i)$, at least in Supplement.

Line 80 For example, when we set 100 nm in the first DMA, more than 40% of the selected particles are multiply charged. Please double check a 40 % value. How it was obtained? Page 3, line 88. An illustration figure (Fig.2) was shown to explain the cause of this shrinking effect Correct the sentence.

Page 4, Line 117 ... where x is the scale parameter. It was defined in page 3, line 70.

Line 122 So the question can be simplified as the following. Change to equation. Page 5, Line 132 One hypothetical κ distribution along with the corresponding multi-charge corrected κ distributions are shown in Fig.4. Here is discrepancy between "hypothetical κ distribution" in the text and "measured κ distribution" in the Fig.4 captions. Is it measured or hypothetical κ distribution? Page 6, Line 156, Eq.(12) C(i,x) represents the correction factor caused by the shrinking effect In Eq.(6) the correction factor was defined as S(i, v). Is it the same or new one?

Line 160, ... *the question can be simplified into*... Change to **equation**. Line 167 ... *distributions are also shown in Fig.4.* Change to **Fig.5**. References Page 9, line 283

Wiedensohler, A., Lütkemeier, E., Feldpausch, M., & Helsper, C. (1986). Investigation of the bipolar charge distribution at various gas conditions. Journal of Aerosol ence, 17(3), 413-416. Should be:

Wiedensohler, A., Lütkemeier, E., Feldpausch, M., and Helsper, C.: Investigation of the bipolar charge distribution at various gas conditions, J. Aerosol Sci., 17, 413-416, https://doi.org/10.1016/0021-8502(86)90118-7, 1986.

Please follow the AMT instruction for paper submission, especially references and citation section.